

Binary Tree - optimized for searching

Node
↓
* data
* Left
* right

property:-

Right child $<$ root

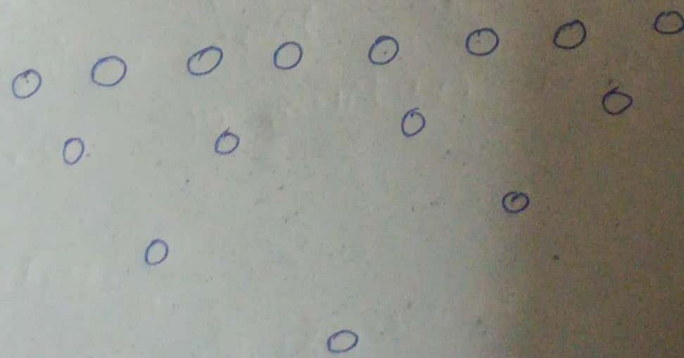
Left child $>$ root

At each step, it'll cut down the search time

E.g.

Tennis Tournament

2 \rightarrow 4 \rightarrow 8 \rightarrow 16 \rightarrow 32



semi final

final

F(256) \rightarrow 8

F(128) \rightarrow 7

F(64) \rightarrow 6

F(32) \rightarrow 5

$\log(256)$
 $\log(2^8)$

$8 \log 2$

8

Logarithmic complexity

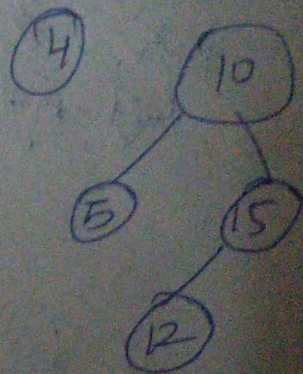
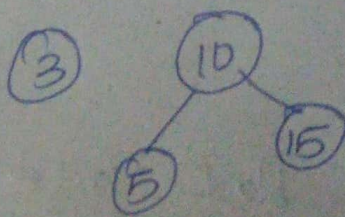
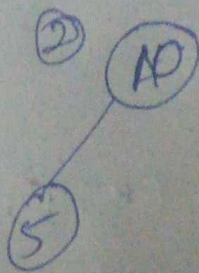
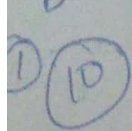
At every step, state space is cut down by half.

e.g. $3 \xrightarrow{3^2} 9 \xrightarrow{3^3} 27 \xrightarrow{3^4} 81 \xrightarrow{3^5} 243$

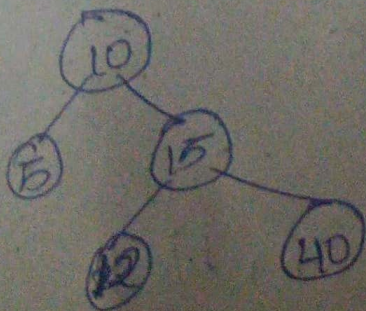
order of time complexity:-

$O(1) \rightarrow O(\log n) \rightarrow O(n) \rightarrow O(n \log n)$

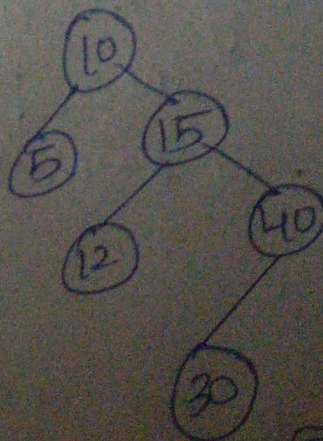
Binary Tree Insertion



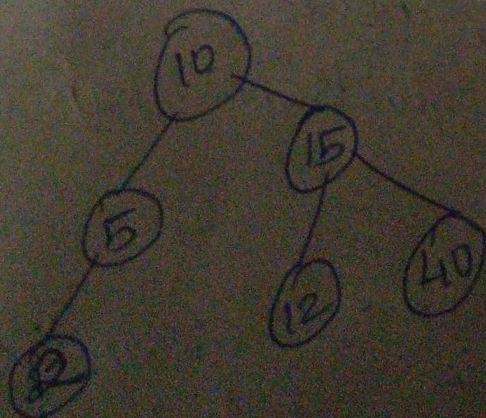
⑤



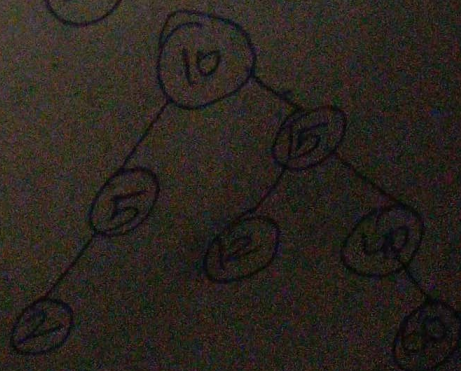
⑥



⑦



⑧



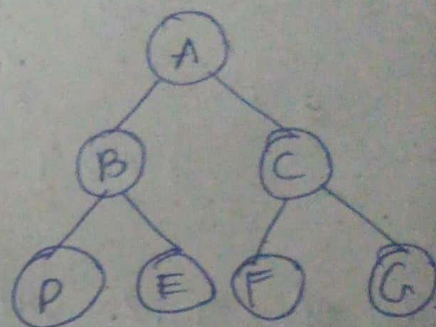
Binary Tree Traversal

- 1) Inorder
- 2) pre order
- 3) post order

Inorder

Left \rightarrow Root \rightarrow Right

E.g. DBEAF CG



pre order

Root \rightarrow Left \rightarrow Right e.g.:

ABDE CFG

post order :-

Left \rightarrow Right \rightarrow Root e.g. ~~DEB~~ DEBFGCA

Red black Tree

- \Rightarrow self balancing binary search tree (BST)
- \Rightarrow utilize color property on each node to maintain balance.

properties :-

- \Rightarrow Every node is colored Red (or) black
- \Rightarrow root = black, leaf = black
- \Rightarrow If red node has childrens then childrens = black
- \Rightarrow any simple path from this node to

descendant leaf has the same black-length

Tree node

- 1) color
- 2) left
- 3) right
- 4) parent
- 5) key

Rotation:-

Used to maintain properties of red-black tree when violated by,
* insertion
* deletion

- 1) Left rotate
- 2) Right rotate
- 3) Left Right rotate
- 4) Right Left rotate