



3F — Framework for FEMM

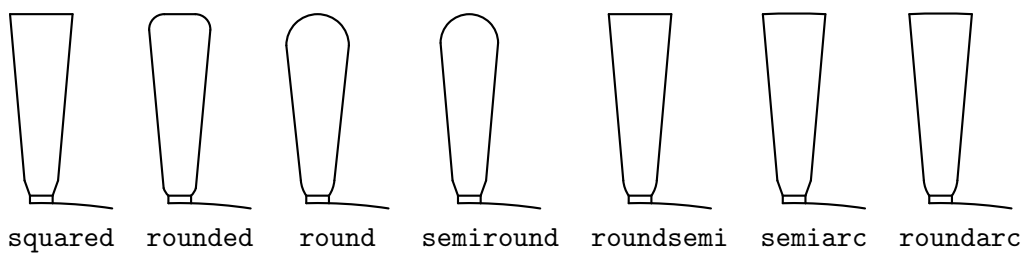
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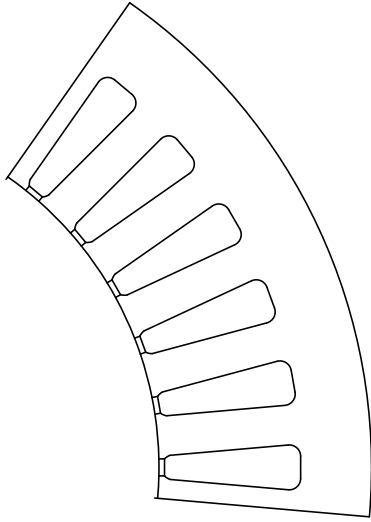
# Chapter 1

## Geometry

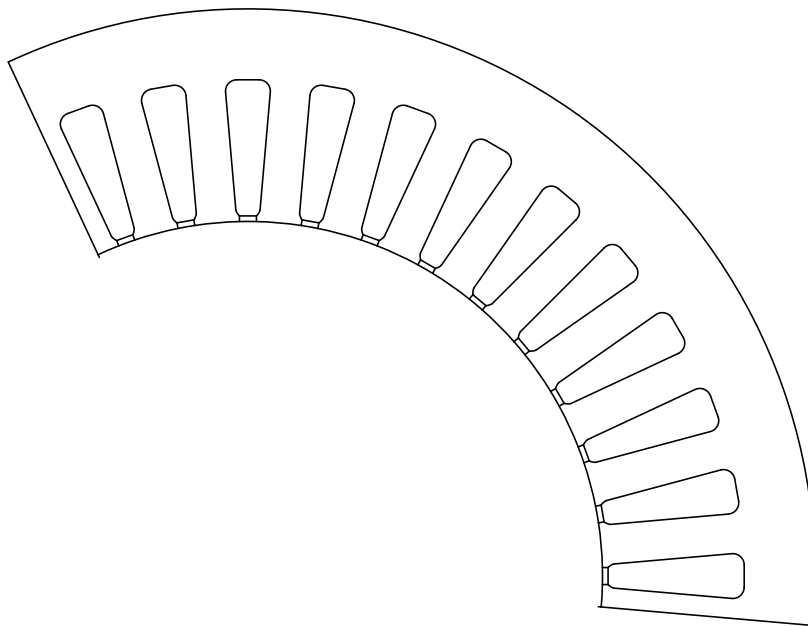
### 1.1 Slots



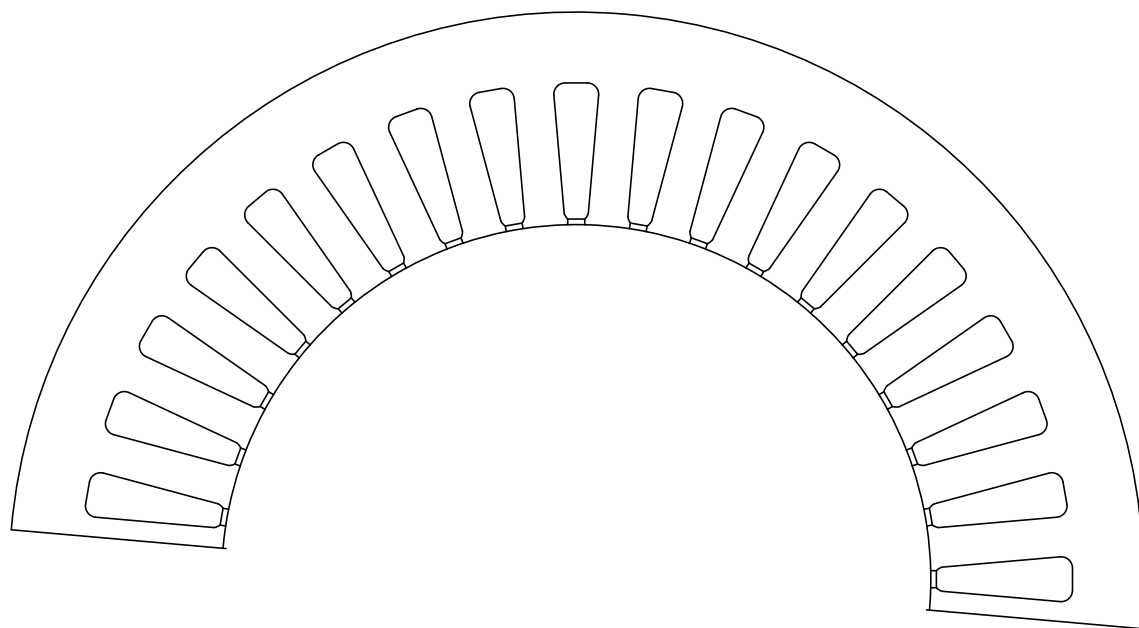
## 1.2 Stators



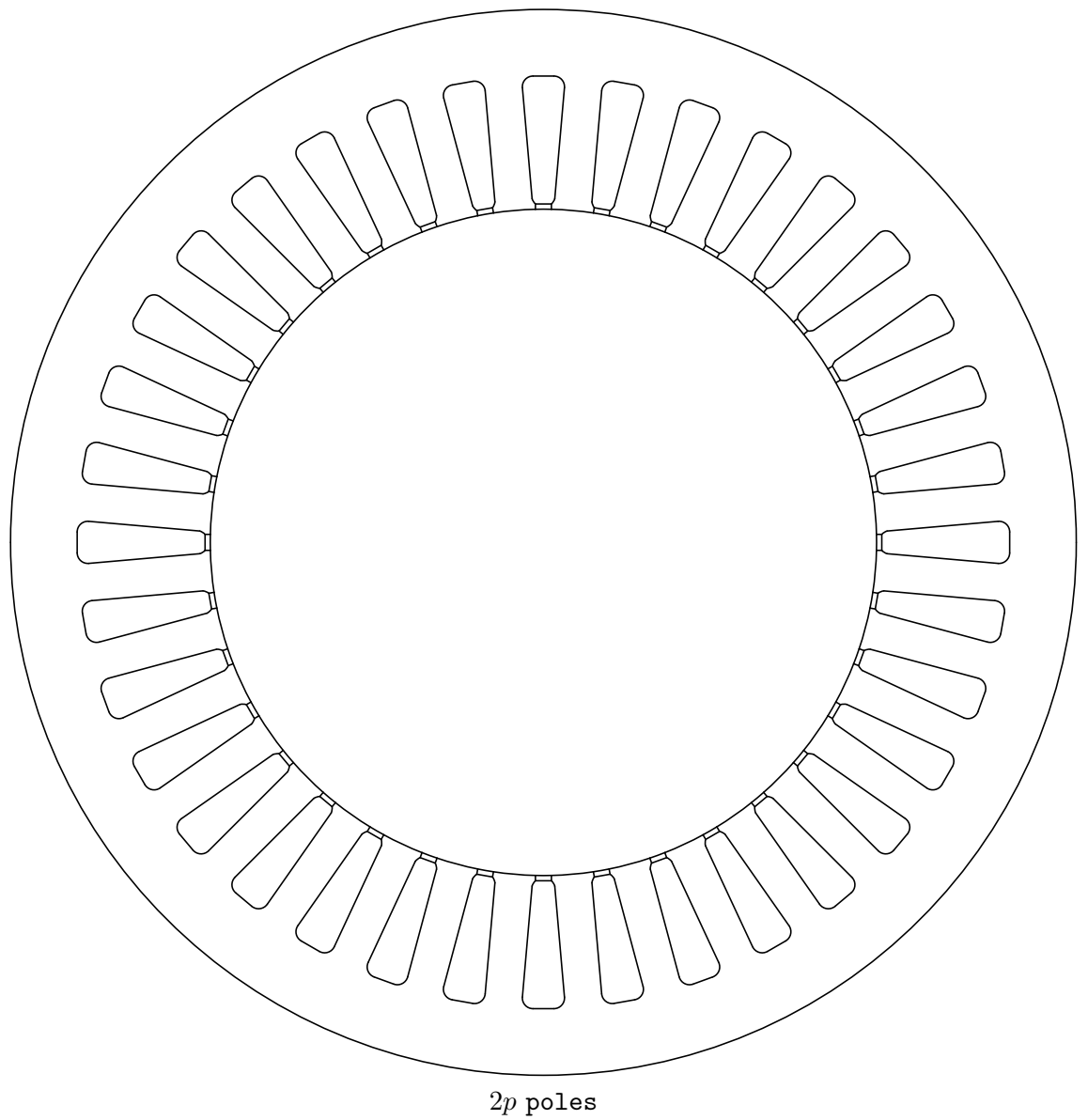
1 pole



2 poles



$p$  poles



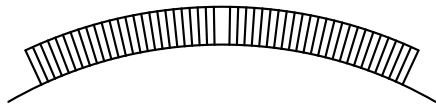
### 1.3 SPM Magnets



parallel + rect

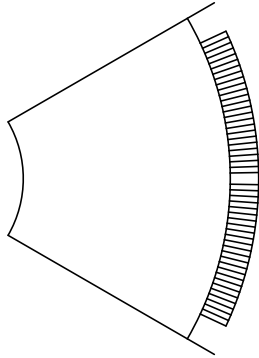


parallel + trapz

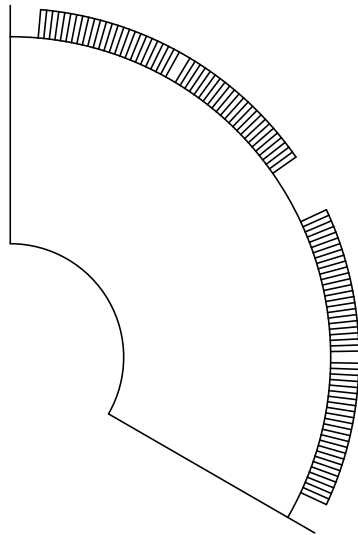


radial (+ trapz)

## 1.4 SPM Rotors

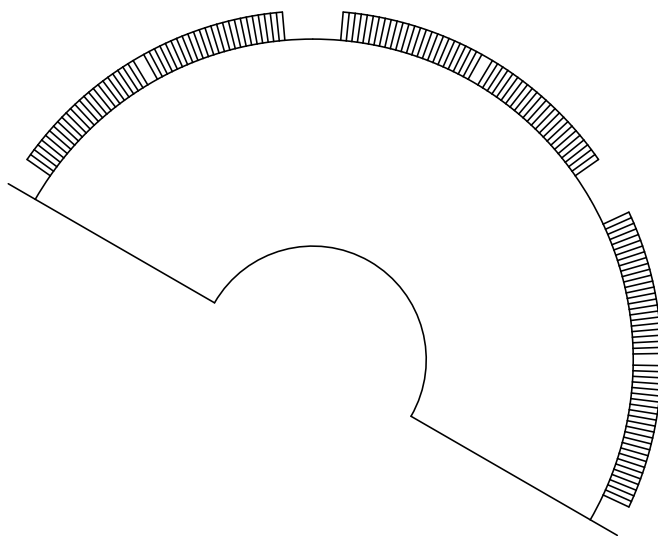


1 pole

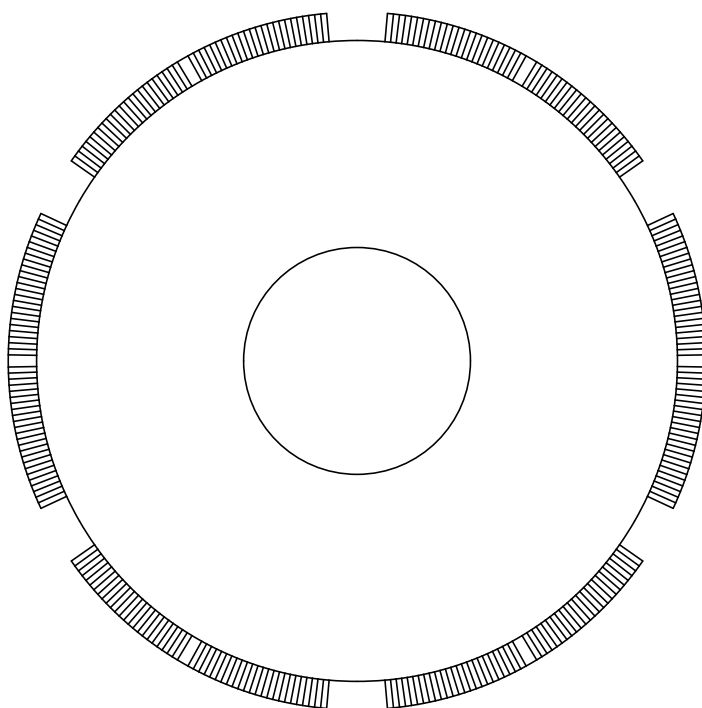


2 poles





$p$  poles



$2p$  poles

## Chapter 2

# Winding

We will characterise a winding through

| Name                     | Math symbol         | Code symbol   |
|--------------------------|---------------------|---------------|
| N. of phases             | $m$                 | <b>m</b>      |
| N. of coils              | $N_{\text{coils}}$  | <b>coils</b>  |
| N. of turns per coil     | $N_{\text{turns}}$  | <b>turns</b>  |
| N. of layers             | $N_{\text{layers}}$ | <b>layers</b> |
| N. of parallel paths     | $n_{\text{pp}}$     | <b>ppath</b>  |
| N. of conductors in slot | $n_c$               | <b>nc</b>     |

Typically, given a lamination stack with  $Q$  slots

$$N_{\text{coils}} = \frac{Q}{2} N_{\text{layers}}$$

so if the number of layers is one, the number of coils is half the number of slots, given the fact that a coil side occupies a full slot.

$$n_c = N_{\text{layers}} N_{\text{turns}}$$

This equation means that in each slot there are  $n_c$  conductors of any phase due to the turns in each coil side in each layer. We bring this number to the equivalent series-connected machine, through the number of parallel paths:

$$n_{\text{cs}} = \frac{n_c}{n_{\text{pp}}}$$

This number,  $n_{\text{cs}}$ , is related to the complete set of slots, while the previous  $n_c$  was related only to a part of them, due to the parallel connection of the winding. Thanks to this fact, we can compute the whole number of conductors for each phase, through

$$N_c = \frac{Q n_{\text{cs}}}{m}$$

Therefore the full number of turns for each phase, which will appear in the flux linkage, is  $N_c/2$ . This number is valid for both the real machine and the equivalent series-connected one.

Another equivalence that we will use is the wye-equivalence. For both the wye and the delta connection of the windings, we will refer to the wye equivalent winding. Each winding sustains either the line(-to-line) voltage in the wye (delta) connection. Therefore

$$U_w = \frac{U_N}{\sqrt{3}} \quad [\text{V}] \quad \text{delta connection}$$

$$U_w = U_N \quad [\text{V}] \quad \text{wye connection}$$

In this way we can obtain the winding current directly from the power

$$I_w = \frac{P}{3U_w \cos \varphi} \quad [\text{A}]$$

and use it as the design current for the winding itself. In fact, if each turn is made by some wires with a full section  $S_c$ , we will refer to the equivalent turn section

$$S_{c,\text{eq}} = n_{\text{pp}} S_c \quad [\text{mm}^2]$$

which sees the complete winding current, giving the current density

$$J = \frac{I_w}{S_{c,\text{eq}}} \quad [\text{A/mm}^2]$$

It is important to highlight that this current density is the conductor's one, while the slot current density is given by

$$J_{\text{slot}} = k_{\text{fill}} J \quad [\text{A/mm}^2]$$

where the fill factor,  $k_{\text{fill}}$ , represents the ratio between the actual conductor area in the slot and the slot section. Depending on the starting point, one can find the rms current in the slot through

$$I_{\text{slot}} = J_{\text{slot}} S_{\text{slot}} = n_{\text{cs}} I_w \quad [\text{A}]$$

## 2.1 Space vectors

## 2.2 Sinusoidal dq control

## 2.3 Trapezoidal control