A Hopfield Network for Digits Recognition

Artificial Intelligence Course Project

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Abstract

This report describes the artificial intelligence course project. This project consists in the implementation of a Hopfield Network using python. The weight matrix will be computed by using different algorithms, in such a way to analyse performances and thus identify the best solution.

1 Introduction

1.1 Neural Networks

They are used for recognition and classification problem, they are capable to learn and so to generalize, that is produce outputs in correspondence of inputs never met before. The training of the net take place presenting a training set (set of example) as input. The answer given by the net for each example will be compared to the desired answer, the difference (or error) between the two will be evaluated and finally the weights will be adjusted by looking at this difference, the process is repeated for the entire training set, until the produced error is minimized, so under a preset threshold.

1.1.1 Classification Problems

Classification problems consists in the classification of an object by looking at its features.

1.2 Hopfield Network [3]

Hopfield networks are neural networks that can be seen as non linear dynamic systems. They are also called recurring networks or feedback networks. We consider neural networks as non linear dynamic systems, where we consider the time variable. In order to do this, we must take into account loops, so we will use recurrent networks. recurrent networks with non linear units are difficult to analyse: they can converge to a stable state, oscillate or follow chaotic trajectories whose behaviour

is not predictable. However, the american physicist J.J. Hopfield discovered that with symmetric connections there will exist a stable global energy function. The Hopfield networks have the following properties:

- **sigle layer recurrent networks** in which each neuron is connected to all the others, with the exception of itself (so no cycles are admitted)
- **symmetric:** the synaptic weight matrix is symmetric, so $W = W^T$. This means that the weights is the same in both direction between two neurons.
- not linear: in the continuous formulation, each neuron has a non linear invertible activation function

As for the neuron update, we can use three possible approaches:

- **asynchronous update:** where neurons are updated one by one
- **synchronous update:** all neurons are updated at the same moment
- continuous update: all neurons are updated in a continuous way

There exists two formulation of the Hopfield model: the discrete one and the continuous one, that differ for the way in which the time flows. For this project we will use the discrete model. In this model the time flows in discrite way and neurons updates in asynchronous way. as for the neuron input, the McCulloch and Pitts model is used, with the adding of an external influence (or bias?) factor:

$$H_i = \underbrace{\sum_{j \neq i} w_{ij} V_j}_{\text{M\&P model}} + \underbrace{I_i}_{\text{external input}}$$

The activation function is the following:

$$V_{i} = \begin{cases} +1 & \text{se } H_{i} > 0 \\ -1 & \text{se } H_{i} < 0 \end{cases}$$
 (1)

The update of the neurons is a random process and the selection of the unit to be updated can be done in two ways:

- 1. at each time instant the unit to be updated is chosen randomly (this mode is useful in simulations)
- 2. each unit is updated independently with constant probability at each time instant

Unlike feedforward networks, a Hopfield network is a dynamic system. It starts from an initial state

$$\vec{V}(0) = (V_1(0), \dots, V_n(0))^T$$

and evolves through a trajectory until it reach a fixed point in which V(t+1)=V(t) (convergence). The Hopfield theorem supplies a sufficient condition for the convergence of the system. It uses an energy function E that govern the systems :

$$E = -\frac{1}{2} \sum_{i=1}^{n} \sum_{\substack{j=1\\ i \neq i}}^{n} w_{ij} V_i V_j - \sum_{i=1}^{n} I_i V_i$$
 (2)

Theorem 1.1 (Hopfield theorem: discrete case). If the weights matrix in a Hopfield network is symmetric, diag(W) = 0, the Energy Function will be a Lyapunov function for the system, so:

$$\Delta E = E(t+1) - E(t) \le 0$$

with the equivalence when the system reach a stationary point.

1.3 Learning Algorithms

Learning rule have some characteristics:

- locality: a rule can be local, this means that the update of a given weight depends only on informations available to neurons on either side of the connection. Locality provides natural parallelism that is one of the component that makes an Hopfield network a truly parallel machine.
- incremental: an incremental rule modifies the old network configuration to memorize a new pattern without needing to refer to any of the previous learnt patterns. This behaviour allows an Hopfield net to be adaptive, thus more suitable for real time situations and changing environments
- **immediate:** an immediate update of the network allows faster learning
- capacity: it measure how many patterns can be stored in the network of a given size (number of neurons). Moreover higher capacity allows faster processing times, because the update time is at least proportional to the number of neurons.

1.3.1 Hebb's rule

In contrast with computer's byte-addressable memory, that adopt a precise memory address to locate information, the human brain utilize content-addressable memory, that uses the content of data to locate information. The Hebb rule has been introduced to describe such behaviour and states that the weight between two neurons increases if the two neurons activate simultaneously. In detail, the Hebb postulate says that:

Let us assume that the persistence or repetition of a reverberatory activity (or "trace") tends to induce lasting cellular changes that add to its stability. [...] When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased. [1]

The memory is represented like a set of P patterns x^{μ} , where $\mu = 1, \dots, \P$: when a new pattern x is presented, the net typically answers producing the pattern in memory that most resembles to x. Accordingly to the Hebb postulate, proportional weights are used in the activation between a pre and a post synaptic neurons:

$$w_{ij} = \frac{1}{N} \sum_{\mu=1}^{P} x_i^{\mu} x_j^{\mu}$$

where N is the number of binary units with output s_1, \ldots, s_N . The recall mechanism is the following:

$$s_i = \operatorname{sgn}\left(\sum_j w_{ij} s_j\right)$$

Anyway, there are some problems in the use of Hopfield network as content-addressed memories:

- the maximum number of pattern is 0.15N
- sometimes the net produces spurious states, that is states that do not belong to the memorized patterns
- the recalled pattern is not necessarily the most similar to the input one
- patterns are not recalled with the same emphasis

1.3.2 Pseudo-Inverse Rule

Pseudo inverse rule try to map a memory to itself before thresholding. In this way the problem can be treated as a real value regression problem, the solution of which is given by the pseudo-inverse. We can consider the Hebb rule as a special case of pseudo-inverse rule for orthogonal training vectors. However, in this rule we have no local computation and no incremental updates, because it involves the calculation of an inverse.

$$w_{ij} = \frac{1}{N} \sum_{\substack{u=1\\v=1}}^{m} x_i^u (Q^{-1})^{uv} x_j^v$$

where m is the total number of patterns and q is:

$$q_{uv} = \frac{1}{N} \sum_{i=1}^{N} x_i^u x_j^v$$

This rule, also called projection learning rule [2], allows to improve the retrieval capability of the net with respect to Hebb rule, bringing the maximum number of pattern to 0.5N.

1.3.3 Storkey Rule [4]

Even if the pseudo-inverse rule performs better than the Hebbian one, it is never incremental and local only if not immediate. Storkey propose an algorithm to increase the capacity of the Hebbian rule without losing locality and incrementality.

$$w_{ij}^0 = 0 \ \forall i,j$$
 and

$$w_{ij}^{\mathbf{v}} = w_{ij}^{\mathbf{v}-1} + \frac{1}{N} x_i^{\mathbf{v}} x_j^{\mathbf{v}} - \frac{1}{N} x_i^{\mathbf{v}} h_{ji}^{\mathbf{v}} - \frac{1}{N} h_{ij}^{\mathbf{v}} x_j^{\mathbf{v}}$$

where h_{ij} is a form of local field at neuron i:

$$h_{ij}^{\mu} = \sum_{\substack{k=1\\k \neq i \ i}}^{n} w_{ij}^{\mu-1} x_{k}^{\mu}$$

2 Implementation

The Hopfield network is implemented with the Hopfield-Net class. Thus, a network will be an instance of this class. When an HopfieldNet object is created, the net is immediately initialized with the given input and the given training algorithm. The class is provided with a test function that performs the test of the whole net with the given test set. This function uses a neuron activation function, called $single_unit_updater$, that operates on a single unit. The behaviour of the net is governed by the energy function, called by the test function at each iteration. Units to be updated are chosen randomly; when every units has been updated, the energy is computed and compared to the one obtained at time t-1. When the difference between the two is zero, the update phase is stopped and result is returned to the user.

2.1 Learning Algorithms

2.1.1 Hebbian rule

The Hebbian rule has been implemented in three different ways. The first one is the original algorithm, with three nested loops: the outer one to iterate over training patterns, while the internal one iterate over the elements of the matrix. This solution, while perfectly follows the algorithm, does not performs wells, so it has been decided to exploits the strengths of the python language to improve performances. Following this idea, solution two uses the dot product function provided by python in order to compute the product between points of a pattern and the sum of the corresponding results for each point between different patterns, thus avoiding the outer loop. This advantage is better exploited in solution three (the one adopted in the definitive version), where also the two loops that iterates over elements are removed. This solution perform directly the dot products between the transposed input patterns matrix and the normal one. Anyway, even if solution three is the best one, it has been discovered that solution one and two are the best choice for very small images.

2.1.2 Pseudo-inverse rule

The pseudo-inverse rule has not been improved with predefined python functions, because of the complexity of the formula. Thus, the pseudo inverse training algorithm is implemented with four nested loops: the external ones iterate over training patterns while the internal ones iterate over single units for the weight computation. Moreover, this algorithm exploits a separate function for the computation of the Q matrix. The original algorithm that iterated the units for the sum computation has been substituted with a dot product operator thanks to numpy library. Finally, in the pseudo inverse implementation the Q matrix is already returned as an inverse, in order to save computational time.

2.1.3 Storkey's rule

The core Storkey formula has been implemented using loops. Improvement where not possible, because dot product could not be exploited. As for the pseudo-inverse alg. also this one uses an external function, the $h_storkey$ function, that computes h. Also this function has not been optimized, even if this was possible, because the result with the dot product where too bad with respect to the normal one.

Notice that both pseudo inverse and Storkey avoid the computation of half of the matrix, by taking advantage of the fact that the matrix is symmetric.

2.2 Data set

The training data set As for testing,

2.2.1 Corruption function

3 Results

Hebbian rule results are improved by adding a filter in the image sampling before the network training

4 Conclusions

References

- [1] D. O. Hebb. *The Organization of Behavior*. Wiley, New York, 1949.
- [2] I. G. L. Personnaz and G. Dreyfus. Collective computational properties of neural networks: New learning mechanisms. *Phys. Rev. A*, 1986.
- [3] M. Pelillo. Artificial intelligence course, 2014.
- [4] A. Storkey. Increasing the capacity of a hopfield network without sacrificing functionality. In *ICANN97: Lecture Notes in Computer Science 1327*, pages 451–456. Springer-Verlag, 1997.

A Appendix: Code

A.1 HopfieldNet.py

```
__author__ = 'gbarbon'
1
2
3
   import numpy as np
   import random as rd
5
   import trainers as tr
6
7
8
   class HopfieldNet:
9
10
        def __init__(self , train_input , trainer_type , image_dimensions):
11
            #number of training patterns and number of units
12
13
            n_patterns = train_input.shape[0]
14
            self.n_units = train_input.shape[1]
15
16
            # crating threshold array (each unit has its own threshold)
17
            self.threshold = np.zeros(self.n_units)
18
19
            # setting image dimension
20
            self.image_dimensions = image_dimensions
21
            # net training
22
23
            if trainer_type == "hebbian":
24
                self.weights = tr.hebb_train(train_input, n_patterns, self.n_units)
25
            elif trainer_type == "pseudoinv":
26
                self.weights = tr.pseudo_inverse_train(train_input, n_patterns, self.n_units)
2.7
            #else:
28
29
        def single_unit_updater(self, unit_idx, pattern):
30
31
            #temp = sum(weights[unit_idx,:]*pattern[:]) - threshold[unit_idx]
            # we implement a powerful version that uses dotproduct with numpy
32
33
            temp = np.dot(self.weights[unit_idx, :], pattern[:]) - self.threshold[unit_idx]
34
            if temp >= 0:
35
                \# pattern[unit_idx] = 1
36
                return 1
37
            else:
38
                \# pattern[unit_idx] = 0
39
                return -1
40
41
        def energy(self, pattern):
42
            e = 0
            length = len(pattern)
43
44
            for i in range (length):
                for j in range(length):
45
46
                    if i == j:
                         continue
47
48
                    else:
49
                         e += self.weights[i][j] * pattern[i] * pattern[j]
50
51
            sub_term = np.dot(self.threshold, pattern)
52
            e = -1 / 2 * e - sub\_term
53
            return e
54
55
        # function overloading in threshold
```

```
def test (self, pattern, threshold=0):
56
57
58
            #setting threshold if threshold != 0
59
            if threshold != 0:
                self.threshold = threshold
60
61
            pattern = pattern.flatten() # flattening pattern
62
            energy = self.energy(pattern) # energy init
63
64
65
           k = 0
            while k < 10:
66
                randomrange = range(len(pattern))
67
                rd.shuffle(randomrange)
68
                for i in randomrange:
69
70
                    pattern[i] = self.single_unit_updater(i, pattern)
71
                    #nota: l'energia deve essere calcolata ad ogni cambiamento di una singola unita' o d
                temp_e = self.energy(pattern)
72
73
                if temp_e == energy:
74
                    #break while loop
                    pattern.shape = (self.image_dimensions[0], self.image_dimensions[1])
75
76
                    return pattern
77
                else:
78
                    energy = temp_e
79
                k += 1
80
81
            pattern.shape = (self.image_dimensions[0], self.image_dimensions[1])
82
            return pattern
```

A.2 trainers.pv

```
1
   __author__ = 'gbarbon'
2
3
   import numpy as np
4
5
6
   # train intput is in the form of a vector
   def hebb_train(train_input, n_patterns, n_units):
8
        # weights matrix init to zeros
9
        weights = np.zeros((n_units, n_units))
10
11
        # 1
12
        for 1 in range(n_patterns):
13
            for i in range(n_units):
14
                for j in range(n_units):
15
                    if i == j:
                         continue
16
17
                \# weights[i,j] = (1/n\_units)* sum(...)
18
                     else:
                         weights[i, j] += train_input[l, i] * train_input[l, j]
19
20
                    # print("Temp weight at this point is", weights[i,j])
                    # uguale???: weights[i,j] = sum(train_input[:,i]*train_input[:,j])
21
22
23
        return weights
24
25
   # uses the storkey rule
   def storkey_train(train_input, n_patterns, n_units):
27
        weights = np.zeros((n_units, n_units))
28
29
        #..#
30
31
        return weights
32
33
   def q_pseudo_inv(train_input, n_patterns, n_units):
34
        q = np.zeros((n_patterns, n_patterns))
35
36
        for v in range(n_patterns):
37
            for u in range(n_patterns):
38
                # for i in range(n_units):
39
                      q[u][v] += train_input[v][i]*train_input[u][i]
40
                q[u][v] = np.dot(train_input[v], train_input[u])
41
42.
        q *= 1 / float(n_units)
43
        q = np.linalg.inv(q) # inverse of the matrix
44
45
        return q
46
   # uses the pseudo inverse training rule
47
48
   def pseudo_inverse_train(train_input, n_patterns, n_units):
49
        weights = np.zeros((n_units, n_units))
50
51
        q = q_pseudo_inv(train_input, n_patterns, n_units)
52
53
        for v in range(n_patterns):
            for u in range(n_patterns):
54
55
                for i in range(n_units):
                    for j in range(n_units):
56
                         if i == i:
57
```

A.3 imageManager.py

```
__author__ = 'gbarbon'
2
3 from PIL import Image
   from PIL import ImageFilter
   # from PIL import ImageEnhance
   import os
   import numpy as np
8
10
   # NOTE: in images dimension are: first:= columns, second:= rows
11
12
   def image_cropper(image, new_dimensions):
13
        width, height = image.size # Get dimensions
14
15
        left = (width - new_dimensions[1]) / 2
        top = (height - new_dimensions[0]) / 2
16
17
        right = (width + new_dimensions[1]) / 2
        bottom = (height + new_dimensions[0]) / 2
18
19
20
        return image.crop((left, top, right, bottom))
21
22
23
   def image_resizer(image, new_dimensions):
24
        return image.resize(new_dimensions)
25
26
27
   def to_greyscale(image):
28
        return image.convert("L")
29
30
31
   def to_blackwhite(input_image):
        return input_image.convert("1")
32
33
34
35
   # convert image to a matrix of 0 and 1 and to black and white
36
   def tomatrix_bew(image):
37
        imarray = np.array(image.getdata(), np.uint8).reshape(image.size[1], image.size[0])
38
        row = imarray.shape[0]
39
        cols = imarray.shape[1]
40
        newarray = np.zeros((row, cols))
41
42
        for i in range (row):
            for j in range(cols):
43
44
                if imarray[i][j] <= 127:
45
                    newarray[i][j] = 1
46
                else:
47
                    newarray[i][j] = 0
48
        return newarray
49
50
51
   # convert image to a matrix of 0 and 1
52
   def tomatrix (image):
53
        matrix = np.array(image.getdata(), np.uint8).reshape(image.size[1], image.size[0])
54
        rows = matrix.shape[0]
        cols = matrix.shape[1]
55
56
        newarray = np.zeros((rows, cols))
57
```

```
58
         for i in range (rows):
59
             for j in range(cols):
                 if matrix[i][j] == 0:
60
61
                     newarray[i][j] = 1
62
63
         return newarray
64
65
66
    def collectimages(finaldim, img_dir):
67
         i = 0
         entries = 0
68
69
         # number of files checking
70
         for img_file in os.listdir(img_dir):
71
             if img_file.endswith(".tiff"):
 72
 73
                 entries += 1
74
75
         dataset = np.zeros((entries, finaldim[0] * finaldim[1]))
76
         for img_file in os.listdir(img_dir):
77
78
             if img_file.endswith(".tiff"):
79
                 newdir = img_dir + "/" + img_file
80
                 im = Image.open(newdir)
81
82
                 orig_dim = im.size
83
                 # Image conversion to black and white
84
85
                 imp = to_greyscale(im)
86
                 imp = to_blackwhite(imp)
87
88
                 # Image filtering
89
                 imp = imp.filter(ImageFilter.MedianFilter(size=5))
90
                 #imp = imp.filter(ImageFilter.ModeFilter(size=5))
91
92
                 if orig_dim[0] > 100 and orig_dim[1] > 100:
93
                     # crop if dimensions higher than 100
                     imp = image\_cropper(imp, [100, 100])
94
95
                     imp = image_resizer(imp, finaldim)
96
                 else:
97
                     imp = image_resizer(imp, [40, 70])
98
                     imp = image_resizer(imp, finaldim)
99
                 #imp.show() # shows image in external program
100
101
                 imarray = tomatrix(imp)
102
                 dataset[i] = imarray.flatten()
103
                 i += 1
104
105
         return dataset
```

A.4 utils.py

```
__author__ = 'gbarbon'
3 from matplotlib import pyplot as plt
   import random as rnd
   import copy as cp
5
8 # convert images from 0/1 to -1/1
9
   def image_converter(input_image):
10
        image = cp.copy(input_image)
11
        image *= 2
        image -= 1
12
        return image
13
14
15
16
   # corrupts images
   def corrupter(input_image, corrupt_param):
17
18
        dim_row = input_image.shape[0]
19
        dim_col = input_image.shape[1]
        corrupted_image = cp.copy(input_image).flatten()
20
21
22
        for i in range(corrupt_param):
23
            corr_idx = rnd.randint(0, (dim_row*dim_col-1))
24
            corrupted_image[corr_idx] *= -1
25
        corrupted_image.shape = (dim_row, dim_col)
26
27
        return corrupted_image
28
29
30 # Plot the results
31
   def plotter(test_set, result_set):
32
        ntest = len(test\_set)
33
        k = 1
34
        for i in range(ntest):
            plt.subplot(ntest, 2, k)
35
36
            plt.imshow(test_set[i], interpolation="nearest")
37
38
            plt.subplot(ntest, 2, k)
39
            plt.imshow(result_set[i], interpolation="nearest")
            k += 1
40
        plt.show()
41
```

A.5 tests.py

```
__author__ = 'gbarbon'
2
3
   import numpy as np
   import HopfieldNet
   import utils as utl
   import imageManager as iM
8
9
   def test1():
        # Create the training patterns
10
11
        a_{pattern} = np.array([[0, 0, 0, 1, 0, 0],
12
                                [0, 0, 1, 0, 1, 0, 0],
13
                                [0, 1, 0, 0, 0, 1, 0],
14
                                [0, 1, 1, 1, 1, 1, 0],
                                [0, 1, 0, 0, 0, 1, 0],
15
                                [0, 1, 0, 0, 0, 1, 0],
16
17
                                [0, 1, 0, 0, 0, 1, 0]]
18
19
        b_pattern = np.array([[0, 1, 1, 1, 1, 0, 0],
20
                                [0\,,\ 1\,,\ 0\,,\ 0\,,\ 0\,,\ 1\,,\ 0]\,,
21
                                [0, 1, 0, 0, 0, 1, 0],
22
                                [0\,,\ 1\,,\ 1\,,\ 1\,,\ 1\,,\ 0\,,\ 0]\,,
23
                                [0, 1, 0, 0, 0, 1, 0],
24
                                [0, 1, 0, 0, 0, 1, 0],
25
                                [0, 1, 1, 1, 1, 0, 0]
26
27
        c_{pattern} = np.array([[0, 1, 1, 1, 1, 1, 0],
                                [0, 1, 0, 0, 0, 0, 0],
28
29
                                [0, 1, 0, 0, 0, 0, 0],
30
                                [0, 1, 0, 0, 0, 0, 0],
                                [0, 1, 0, 0, 0, 0, 0],
31
                                [0, 1, 0, 0, 0, 0, 0],
32
33
                                [0, 1, 1, 1, 1, 1, 0]]
34
35
        a_pattern = utl.image_converter(a_pattern)
36
        b_pattern = utl.image_converter(b_pattern)
37
        c_pattern = utl.image_converter(c_pattern)
38
39
        train_input = np.array([a_pattern.flatten(), b_pattern.flatten(), c_pattern.flatten()])
40
41
        #hebbian training
42.
        net = HopfieldNet.HopfieldNet(train_input, "hebbian", [7, 7])
43
44
        # creating test set
45
        a_test = utl.corrupter(a_pattern, 5)
46
        b_test = utl.corrupter(b_pattern, 5)
47
        c_test = utl.corrupter(c_pattern, 5)
48
49
        # training and testing the net
50
        a_result = net.test(a_test)
51
        b_result = net.test(b_test)
52
        c_result = net.test(c_test)
53
54
        #Show the results
55
        test_set = np.array([a_test, b_test, c_test])
56
        result_set = np.array([a_result, b_result, c_result])
57
        utl.plotter(test_set, result_set)
```

```
58
59
60
    def test2():
61
         images_dir = "/Users/jian/Dropbox/AI_dropbox/progetto_2014/dummy_data_set/courier_digits_data_se
        dim = [14, 9] # in the form rows * cols
62
        testel = 8 # elements for training
63
64
        corruption_val = 30
65
66
        image_dim = [dim[1], dim[0]] # changing shape for images
67
68
        # Loading images data set
        temp_train = iM.collectimages(image_dim, images_dir)
69
70
71
        train_input = np.zeros((testel, dim[0] * dim[1]))
 72
        for i in range (testel):
73
             train_input[i] = temp_train[i]
74
75
        # image conversion to 1 and -1 for Hopfield net
76
        for i in range(train_input.shape[0]):
            temp = utl.image_converter(train_input[i].reshape(dim))
77
78
             train_input[i] = temp.flatten()
79
80
        # training the net
81
        net = HopfieldNet.HopfieldNet(train_input, "hebbian", dim)
82
83
        # testing the net
        test\_set = np.zeros((testel, dim[0], dim[1]))
84
85
        result\_set = np.zeros((testel, dim[0], dim[1]))
86
        for i in range (testel):
87
             test_set[i] = utl.corrupter(train_input[i].reshape(dim), corruption_val)
88
             result_set[i] = net.test(test_set[i])
89
90
        # Plotting results
91
        utl.plotter(test_set, result_set)
92
93
    def test3():
        images_dir = "/Users/jian/Dropbox/AI_dropbox/progetto_2014/dummy_data_set/digital7_digit_data_se
94
95
        dim = [25, 16] # in the form rows * cols
96
        testel = 10 # elements for training
97
        corruption_val = 10
98
99
        image_dim = [dim[1], dim[0]] # changing shape for images
100
101
        # Loading images data set
102
        temp_train = iM.collectimages(image_dim, images_dir)
103
104
        train_input = np.zeros((testel, dim[0] * dim[1]))
105
        for i in range(testel):
106
             train_input[i] = temp_train[i]
107
108
        # image conversion to l and -l for Hopfield net
        for i in range(train_input.shape[0]):
109
            temp = utl.image_converter(train_input[i].reshape(dim))
110
111
             train_input[i] = temp.flatten()
112
113
        # training the net
114
        net = HopfieldNet.HopfieldNet(train_input, "pseudoinv", dim)
115
116
        # testing the net
```