

A New Method for Inter-Cell Interference Estimation in Uplink SC-FDMA Networks

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Abstract—This paper addresses a power control and Inter-Cell Interference (ICI) estimation problem in uplink Single Carrier Frequency Division Multiple Access (SC-FDMA) networks. We consider a power control based on Signal to Interference plus Noise Ratio (SINR) target to be achieved, which requires knowledge of the interference level. We propose a simple method to estimate ICI in uplink SC-FDMA networks, less greedy than the classical Monte Carlo method which has higher computation complexity. Numerical results validate the new method in multiple environments even after adding fast fading and shadowing effect. Moreover, it shows robustness against variation of above mentioned parameters.

Keywords: Uplink PC, Inter-Cell Interference (ICI) estimation, SC-FDMA.

I. INTRODUCTION

The 3GPP Long Term Evolution (LTE) represents a major advance in cellular technology. LTE offers significant improvements over previous technologies by introducing a new physical layer and reforming the core network. The main reasons for these changes in the Radio Access Network (RAN) system design are the need to improve the average user throughput (in order to reach peak data rates of 100 Mbits/s in downlink and 50 Mbits/s in the uplink) and the coverage area [1]. To achieve these targets, Orthogonal Frequency Division Multiple Access (OFDMA) was adopted for the LTE downlink and Single Carrier Frequency Division Multiple Access (SC-FDMA) for the LTE uplink. These methods were selected in order to provide higher spectral efficiency, lower delay, high immunity to inter-symbol interference, good bandwidth scalability, and more multi-user flexibility than the currently deployed networks [2].

The radio air interface must be able to provide both high peak bit rates and acceptable cell-edge bit rates, even to cell edge users who are the most interfered by Inter-Cell Interference (ICI), i.e by users using the same radio resource in neighboring cells [3]. This problem is specially noticeable on the uplink, where ICI generated by mobile users must be evaluated.

The existing techniques to mitigate the level of inter-cell interference rely on two possible radio resource allocation techniques: (i) subcarrier allocation, which consists in determining a proper frequency planning (ii) power control: the transmission power must be as low as possible to achieve the target throughput while generating the least possible interference. Power control in SC-FDMA has been studied in the literature. An open-loop fractional power control has been

considered in [4] and inter-cell power control in [5]. In [6] the authors propose to decrease or increase the transmit power by 1 dB if needed. A radio resource management using the cooperation of base stations is detailed in [7]. The power allocation presented in our study is based on the Signal to Interference plus Noise Ratio target $\text{SINR}_{\text{target}}$ required by users in their environment (path loss, noise, ICI...). To perform this power control, we need to know the inter-cell interference generated at the base station level. The ICI determination can be done by estimating the transmission channel, as it is done in [8], where pilots are distributed in the transmitted signal. This idea is shared by the authors of [9] in Rayleigh fading channels. The authors of [10] and [11] propose an analytical method based on collision probability distribution to analyze the ICI.

In this paper, we present a new method to estimate the interference caused by neighboring cells in the uplink case. We consider that the interference received by the base station of the central cell in the total allocated bandwidth is equal to the received power from a virtual point situated at the barycenter of each interfering sector, radiating with a median power. The way to compute this median power is exhibited. This method is simple to be implemented on simulators and is less greedy than classical Monte Carlo simulations which require higher computation complexity.

The remainder of the paper is organized as follows. Section II introduces the system model and notations. Section III presents the new method for estimating inter-cell interference. Performance results are represented in Section IV. Conclusions are given in the last section.

II. SYSTEM MODEL

We consider an LTE network composed of 19 cells: one central cell and two rings of interfering cells (i.e 18 cells). We focus on the uplink transmission, where a SC-FDMA technique is used. To simplify the problem, we assume that each user is assigned one Resource Block (RB), which is described by N_{sc}^{RB} adjacent subcarriers and N_{sym}^{UL} SC-FDMA symbols where $N_{sc}^{RB} = 12$ and $N_{sym}^{UL} = 6$ (with a normal cyclic prefix). The adjacency property allows us to average the Signal to Interference plus Noise Ratio (SINR) over the whole used band, since the fast fading on adjacent subcarriers is correlated, instead of computing it by subcarrier as in OFDMA. Therefore, a $\text{SINR}_{\text{target}}$ can be defined for each RB.

For the sake of fairness, its value will be the same for all users. To mitigate interference, an appropriate frequency planning is required. Using a tri-sectored antenna located at the center of the hexagonal cell, we use three frequency bandwidths B , one for each sector of each cell (as illustrated on Figure 1). The

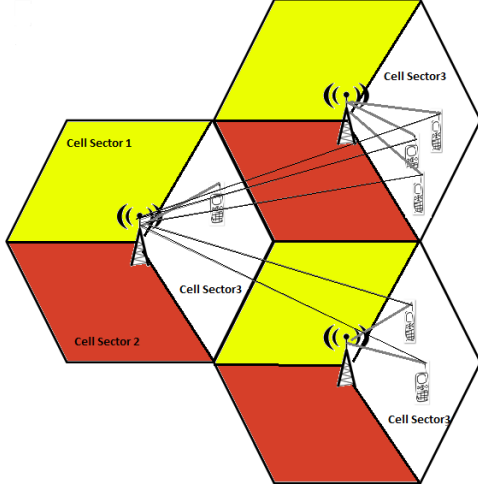


Fig. 1. Frequency planning with tri-sectored antennas - Example of interference in the uplink

total interference I_c suffered by the central Base Station (BS) is the sum of the interference suffered by this BS from each neighboring cells, i.e:

$$I_c = \sum_{k=2}^{19} I_{kc}, \quad (1)$$

where I_{kc} is the interference caused by the neighboring sector k to the central cell c . The computation of I_{kc} will be detailed in section III.

The model uses power control to determine the transmission power of each user, so as to reach $\text{SINR}_{\text{target}}$. In addition, we set a throughput threshold that users can not overstep, even if their radio conditions could enable them to achieve more. Thus, every mobile station (MS) j of the central cell is going to transmit on the resource block l , at the power $P_{em_j}^l$ obtained after power control as follows:

$$P_{em_j}^l = \min \left[\frac{\text{SINR}_{\text{target}} * (N + I_c)}{G_t * G_r(\theta_{jc}) * G_c(r_{jc})}, P_{max} \right] \quad (2)$$

where,

- N represents the noise in the used frequency band. In practice, the noise is predominantly thermal.
- $G_t = 0$ dBi is the mobile's transmission antenna gain.
- G_r is the BS antenna gain (used for reception) which depends on θ_{jc} : the angle between the mobile j situated in the central cell and the main lobe of the central cell's BS radiation antenna pattern [12]:

$$G_r(\theta_{jc}) = -\min \left[12 * \left(\frac{\theta_{jc}}{\theta_{3dB}} \right)^2, A_m \right] \quad (3)$$

where $\theta_{jc} \in [-60^\circ, 60^\circ]$, θ_{3dB} is the 3 dB beamwidth which is 70° for tri-sectored cell and $A_m = 20$ dB is the maximum attenuation [13].

- G_c is the path loss depending of r_{jc} , the distance between the mobile j and the base station of the central cell c .

$$G_c(r_{jc}) = 10^{-\frac{a}{10}} * r_{jc}^{-\frac{b}{10}} \quad (4)$$

By using the Okumura Hata model [14], we obtain the coefficients $a = 136.7$ and $b = 34.4$.

- P_{max} is the maximum mobile transmission power, set to 125 mW, i.e. 21 dBm [15].

III. NEW METHOD OF ICI ESTIMATION

Our objective is to develop an easier method than Monte Carlo simulations to estimate the LTE uplink inter-cell interference.

As illustrated on Figure 2, we consider that the contribution of each sector is equivalent to the power received at the central base station from a point situated at the barycenter of the interfering sector and radiating at P_m , where P_m is the median power of $P_{em_j}^l$, $j = 1, \dots, M_S$, M_S representing the number of active users in the sector.

It follows that,

$$I_{kc} = P_m * G_t * G_r(\theta_{kc}) * G_c(r_{kc}), \quad (5)$$

where,

- θ_{kc} is the angle between the barycenter of the interfering sector and the main lobe of the central cell's BS antenna pattern ($\theta_{kc} \in [-180^\circ, 180^\circ]$).
- r_{kc} is the distance between the barycenter of the interfering sector and the central cell's BS.

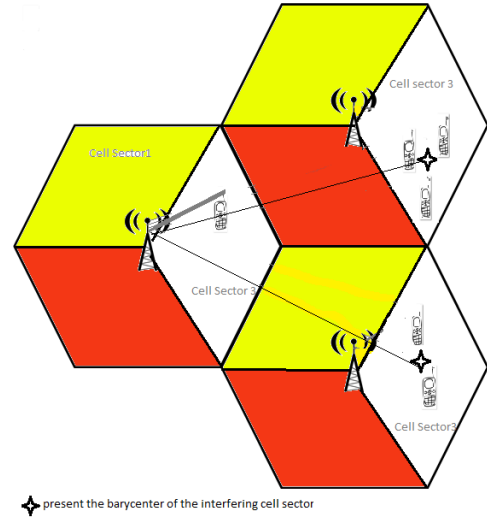


Fig. 2. ICI estimation using a virtual point situated at the barycenter of interfering sectors

To be more fair, we allocate to users the same number of RB per time slot and we suppose that they try to reach the same $\text{SINR}_{\text{target}}$. In order to mitigate interference, we reduce the transmission power by applying power control as expressed

in relation (2). Assuming that all cells behave the same way, we update the interference I_c and recompute $P_{em_j}^l$ until we converge, after S iterations, to a stable transmission power. Considering at the first iteration a noise limited network (i.e. $I_c = 0$), users will converge quickly to a stable transmission power. The following algorithm explains these steps in details. The Cumulative Distribution Function (CDF) of the

Algorithm 1 Estimating ICI model simulation

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Init :  $I_c = 0$ 
Randomly place  $M_S$  active users
Compute their barycenter.
for  $It = 1$  to  $S$  do
  for  $j = 1$  to  $M_S$  do
     $P_{em_j}^l(It) = \min \left[ \frac{\text{SINR}_{target} * (N + I_c)}{G_t * G_r(\theta_{jc}) * G_c(r_{jc})}, P_{max} \right]$ 
  end for
   $P_m = \text{median}[P_{em_j}^l]$ 
   $I_c = \sum_{k=2}^{19} P_m * G_t * G_r(\theta_{kc}) * G_c(r_{kc})$ : ICI generated by the 18 interfering cells
end for
for  $j = 1$  to  $M_S$  do
   $P_{S_j} = P_{em_j}(S)$ : stable transmission power of user  $j$ 
end for
 $V_S(i) = [P_{S_1} P_{S_2} \dots P_{S_{M_S}}]$ : stored MS stable transmission powers

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stable transmission powers P_{S_j} will allow us to evaluate the performance of the proposed method. In our case it concerns the distribution of MS stable transmission powers obtained (i) from our proposed model: d_M , and (ii) from Monte Carlo simulations: d_{MC} . For more noticeability, the comparison is done using two tests: i) the log ratio test, and ii) the Kullback-Leibler divergence test.

- **The log ratio test** is a simple statistical ratio test, which compares two distributions using the logarithm of the ratio. In our case, the log ratio test R is given by:

$$R = \log \frac{\text{Prob}(d_M \leq x)}{\text{Prob}(d_{MC} \leq x)} \quad (6)$$

if R is less than 1, or near to 0 (ideally) the distributions are similar.

- **The Kullback-Leibler divergence test**, mostly used in information theory, is a non-symmetrical measure of the difference between two probability distributions. It can be used to measure the consistency between d_M and d_{MC} . The result, denoted KL , can be expressed as a function of the log ratio test as follows:

$$KL = \text{Prob}(d_M \leq x) * R \quad (7)$$

The Kullback-Leibler test, as it is weighted by the CDF, is more representative of the distributions similarities, especially when the distributions are not uniform.

cellular layout	Hexagonal grid, 19 tri-sector cells.
inter-site distance	1732 m
carrier frequency	2.6 GHz
system bandwidth	$B = 5$ MHz per sector
number of data subcarriers	300
Total number of RB per sector	25
number of RB per user	1
number of active users M_S	25
TTI	1 ms
radio channel gain	Okumura Hata for urban areas: $G_c(r_{jc}) = 10^{-a/10} * r_{jc}^{-b/10}$. $a = 136.7$ and $b = 34.4$.
Antenna configuration	Single-Input-Single-Output
BS antenna pattern	$G_r(\theta_{jc}) = -\min[12 * (\frac{\theta_{jc}}{\theta_{3dB}})^2, A_m]$. $\theta_{3dB} = 70^\circ$, $A_m = 20$ dB
User antenna gain	$G_t = 0$ dBi
User power class	$P_{max} = 21$ dBm (125 mW)
minumum distance between user and BS	30 m
Thermal noise	-174 dBm/ Hz

TABLE I
SIMULATION PARAMETERS

IV. PERFORMANCES OF THE MODEL

In this section, the proposed method for ICI estimation is evaluated. We perform link-level simulations on the LTE SC-FDMA uplink radio interface.

A. Simulation parameters

The parameters for uplink SC-FDMA system are mainly taken from [12]. Table I summarizes the most relevant parameters considered for our simulations.

Setting B to 5 MHz, we obtain 300 subcarriers for data according to LTE standard [16]. Consequently, 25 RB are available for uplink transmission every Time Transmission Interval (TTI) in each sector. The carrier frequency f_c is equal to 2.6 GHz. In the proposed method of ICI estimation, we have selected the median value for the virtual user transmission power instead of the mean value in order to achieve more accurate results. Indeed, the mean is a central tendency in statistics, which is reliable only in the presence of a symmetrical distribution, whereas the median is still reliable in presence of an asymmetrical distribution, since it is considered as a weighted arithmetic average [17]–[19]. In our case, the distribution of the MS transmission powers follows an asymmetrical distribution. Figure 3 represents the histogram of the users stable transmission powers after Monte Carlo simulations convergence. The asymmetry is caused by extreme values that correspond to some extreme users positions. The method's performances are assessed by comparing the obtained stable transmission powers with those issued from Monte Carlo simulations, where the interference of each active user is computed with M_T random draws of interferers in each

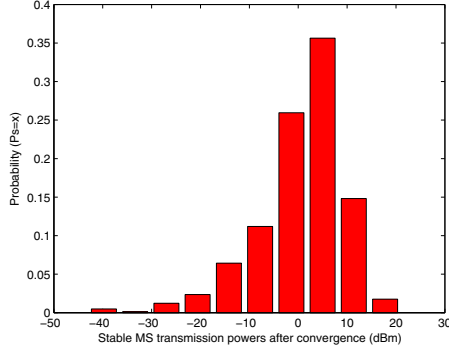


Fig. 3. Histogram of MS transmission powers after convergence

interfering sector.

To validate our model, we use the two tests defined before, and study the method in different and more realistic environments:

- PL: Path Loss (inverse of the channel gain using only the Okumura Hata model)
- PL+Fad : Path Loss with Rayleigh fading of $\sigma_{fading} = 1$
- PL+Fad+Shad : Path Loss with Rayleigh fading of $\sigma_{fading} = 1$, and shadowing of standard deviation $\sigma_{shadowing} = 4$ dB

Many draws of Algorithm I and Monte Carlo simulations have been considered to obtain more representative results. The number of draws is denoted M and set to 4.10^5 . Thanks to adequate initialization of I_c , the stable transmission powers are obtained after S less than 5 iterations.

B. Robustness of the model

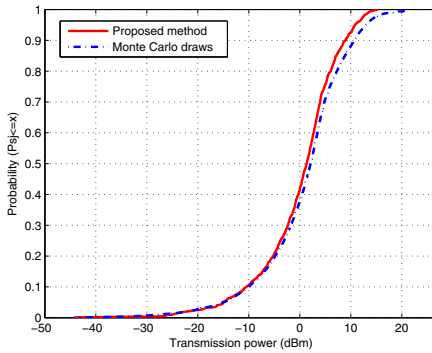


Fig. 4. CDF of MS transmission powers

Figure 4 represents the two CDF obtained, after convergence of MS transmission powers, by our proposed method and by Monte Carlo simulations. For both methods Okumura Hata propagation model without fading and shadowing was firstly used.

1) *Complexity gain*: The two curves are obtained with $M \times M_S$ and $M \times M_T \times M_S$ points respectively. Actually, for each Monte Carlo simulation, M_T iterations are run additionally to drop interferer users in each interfering sector. This last

Power (dBm)	R		
	$\sigma_{fading} = 1, \sigma_{shadowing} = 4$ dB		
	PL	PL + Fad	PL+Fad+Shad
≤ -30	0.14	0.11	0.122
$[-30;-25]$	0.048	0.063	0.11
$[-25;-20]$	0.04	0.009	0.099
$[-20;-15]$	0.024	0.026	0.09
$[-15;-10]$	0.022	0.033	0.078
$[-1;-5]$	0.02	0.024	0.068
$[-5;0]$	0.03	0.042	0.06
$[0;5]$	0.043	0.042	0.049
$[5;10]$	0.026	0.031	0.037
$[10;15]$	0.014	0.018	0.028
$[15;21]$	0.003	0.0042	0.015

TABLE II
R OBTAINED BY LOG RATIO TEST

Power (dBm)	KL		
	$\sigma_{fading} = 1, \sigma_{shadowing} = 4$ dB		
	PL	PL + Fad	PL+Fad+shad
≤ -30	0.0016	0.0002	0.024
$[-30 ; -25]$	0.0028	0.0002	0.04
$[-25 ; -20]$	0.0012	0.00063	0.057
$[-20 ; -15]$	0.0027	0.0009	0.064
$[-15 ; -10]$	0.0019	0.037	0.063
$[-10 ; -5]$	0.0037	0.049	0.057
$[-5 ; 0]$	0.0086	0.014	0.052
$[0 ; 5]$	0.012	0.022	0.044
$[5 ; 10]$	0.024	0.025	0.035
$[10 ; 15]$	0.011	0.022	0.027
$[15 ; 21]$	0.005	0.006	0.014

TABLE III
KL OBTAINED BY KULLBACK-LEIBLER TEST

parameter M_T represents the computation complexity gain of our proposed method as it does not need to drop interfering users to evaluate intercell interference.

Setting $SINR_{target} = 3$ dB, less than 2 % of users are in outage, whereas user transmission powers values vary between -48 dBm and 21 dBm, which respect to the standard transmission power interval given in [15]. The corresponding throughput per user is 360 kbps.

2) *Introduction of fast fading and shadowing*: Table II summarizes the most representative results identified by significant probabilities, i.e. MS transmission powers ≥ -30 dBm, obtained by using the log ratio test in different environments. The gap between the two CDF for lower MS transmission powers is larger than the observed one for high transmission powers, which becomes close to zero. Moreover, the complex environment increases this gap. However, the largest value observed is 0.14. Therefore, as it is very lower than 1, the two CDF can be considered as similar and our model is valid. The Kullback-Leibler divergence test, as it takes into account the MS transmission power CDF, softens the differences between the results issued from both methods (see Table III) in the lowest transmission powers area. It enhances that in most case, when MS transmission powers are higher than -15 dBm, the two MS stable transmission powers CDF's are similar.

3) *Variation of the fast fading and shadowing environment parameters*: Using the Kullback-Leibler divergence test, we

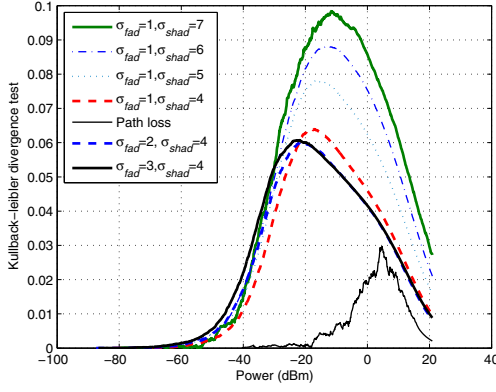


Fig. 5. Kullback-Leibler test curves

take different values for shadowing and fast fading parameters. The variation of these parameters, if it keeps the distributions similarity, will confirm the model's validity. Figure 5 summarizes the simulations results curves. As they come from the product of a decreasing function (R) and an increasing function ($\text{Prob}(d_M \leq x)$), all curves have the same behavior: first they increase, reach a maximum value (that remains so small that it respects the log ratio validity test) and then decrease.

The maximum Kullback-Leibler test in the path loss case was less than 0.03. When the fast fading and the shadowing effects are considered, we observe some fluctuations. The maximum Kullback-Leibler divergence test in presence of fast fading of $\sigma_{fading} = 1$ and shadowing of $\sigma_{shadowing} = 4$ dB is less than 0.07. Moreover, varying fast fading standard deviation σ_{fading} from 1 to 3 does not influence much. The curves remain nearly identical. On the other hand, varying the shadowing parameter changes the simulation results. Setting σ_{fading} at 1 and varying $\sigma_{shadowing}$ from 4 to 7 dB makes the maximum Kullback-Leibler distance increase from 0.06 to 0.1. Nevertheless, the model's robustness is confirmed as the Kullback-Leibler divergence test results remains very small and respects the log ratio validity tests. This confirms the validity of the proposed model in different environments and its robustness against the environment parameters variations.

V. CONCLUSION

Power control applied on the uplink to the mobile terminals transmission power, based on a SINR threshold, reduces efficiently the inter cell interference. This reduction comes at the expense of a higher complexity in the derivation of ICI. The method we proposed to estimate the inter cell interference is less heavy and greedy in computation than the classical Monte Carlo method. Actually, It does not draw the location of users at random in the interfering sectors as Monte Carlo method requires. We have shown that a single virtual point, situated at the barycenter of each the concerned interfering sector, allows us to precisely evaluate the ICI. This virtual interferer, transmits at the median power of the

sector's active users assuming that all neighboring cells behave the same way than the central cell. This equivalent median power creates, in any environment, an intercell interference at the central base station identical to that derived with random interfering users obtained from Monte Carlo simulations. This method reduces computation of the ICI, and complexity of planning and evaluation simulators. Future work will consist in developing a closed form formula for ICI estimation, in order to validate analytically the model proposed in this paper.

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