Project 2 MI3

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In MI2, we cleaned our data and stored the average minimum and maximum temperatures as time series objects in R. We also performed basic EDA to view how temperatures have changed over time, looking at specific months and looking at the overall trend. As we plotted our time series data, it was obvious there was a seasonal component we would have to keep in mind as we moved on to building a model.

```
# from MI2!!
mintemp <- read.csv("C:\\Users\\gbhar\\OneDrive - University of Virginia\\ds 4002\\mean_min_monthly_tem</pre>
maxtemp <- read.csv("C:\\Users\\gbhar\\OneDrive - University of Virginia\\ds 4002\\mean_max_monthly_tem
mintemp_dat <- mintemp[mintemp$Year != c(2024,2025), ]
maxtemp_dat <- maxtemp[maxtemp$Year != c(2024,2025), ]</pre>
# order of months
month_levels <- c("Jan", "Feb", "Mar", "Apr", "May", "Jun",
                   "Jul", "Aug", "Sep", "Oct", "Nov", "Dec")
# min temp reordered and stored as time series
mintemp_dat$Month <- factor(mintemp_dat$Month, levels = month_levels)</pre>
mintemp_sorted <- mintemp_dat[order(mintemp_dat$Year, mintemp_dat$Month), ]</pre>
mintemp_timeseries <- ts(mintemp_sorted$Mean_Min_Temp,frequency=12,start=c(2000,1))
# max temp reordered and stored as time series
maxtemp_dat$Month <- factor(maxtemp_dat$Month, levels = month_levels)</pre>
maxtemp_sorted <- maxtemp_dat[order(maxtemp_dat$Year, maxtemp_dat$Month), ]</pre>
maxtemp_timeseries <- ts(maxtemp_sorted$Value,frequency=12,start=c(2000,1))</pre>
```

We used https://a-little-book-of-r-for-time-series.readthedocs.io/en/latest/src/timeseries.html as a reference to guide us in our analysis.

Minimum Average Temperatures

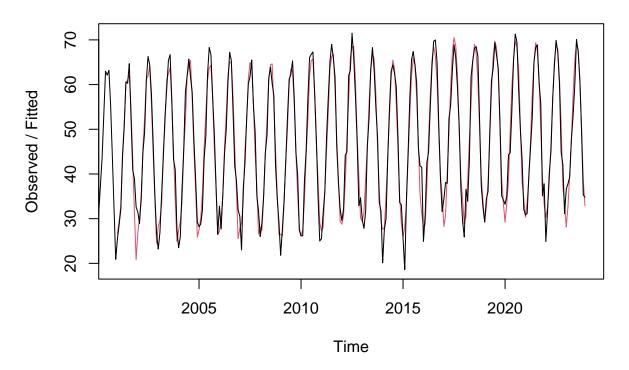
We first built a model using exponential smoothing. Due to the obvious seasonality, we opted to use Holt-Winters exponential smoothing.

```
# fit predictive model
mintempmodel <- HoltWinters(mintemp_timeseries)
mintempmodel # estimated values of alpha, beta, gamma</pre>
```

```
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = mintemp_timeseries)
##
## Smoothing parameters:
  alpha: 0.1172071
## beta: 0.01432105
##
    gamma: 0.1856539
##
## Coefficients:
##
                [,1]
## a
       47.940093133
## b
        0.002574581
## s1 -18.105619060
## s2 -15.060639672
## s3
       -9.520059313
       -1.797080738
## s4
## s5
        7.640912560
       15.723107829
## s6
## s7
       21.270803516
## s8
       19.466157860
## s9
       12.894557061
## s10
       1.806070982
## s11 -10.017447454
## s12 -14.509994740
```

plot(mintempmodel) # plot model on top of existing data

Holt-Winters filtering



```
library(forecast)

## Warning: package 'forecast' was built under R version 4.4.3

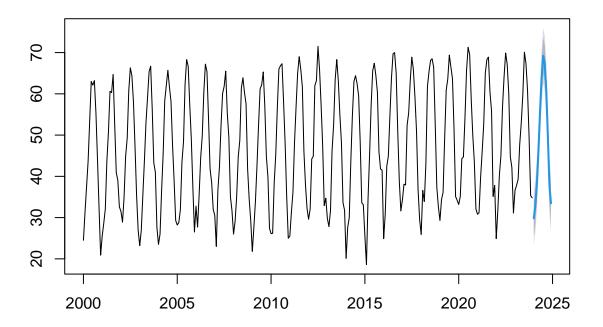
## Registered S3 method overwritten by 'quantmod':

## method from

## as.zoo.data.frame zoo

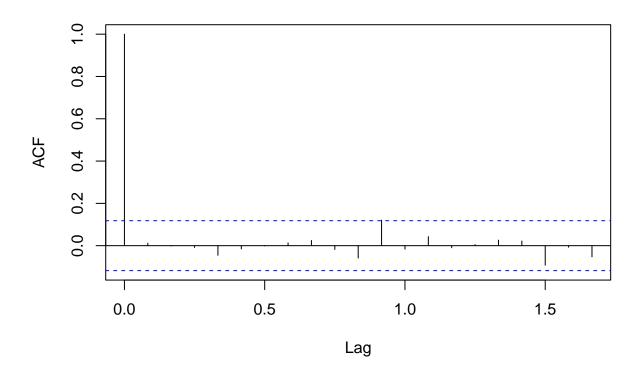
# forecasting
mintempforecast <- forecast(mintempmodel, h=12) # 12 more months (2024)
plot(mintempforecast) # plot our forecast values</pre>
```

Forecasts from HoltWinters



checking if there are any non-zero autocorrelations
acf(na.omit(mintempforecast\$residuals), lag.max=20) # correlogram

Series na.omit(mintempforecast\$residuals)



```
Box.test(na.omit(mintempforecast$residuals), lag=20, type = "Ljung-Box") # Ljung-Box test
##
## Box-Ljung test
##
## data: na.omit(mintempforecast$residuals)
```

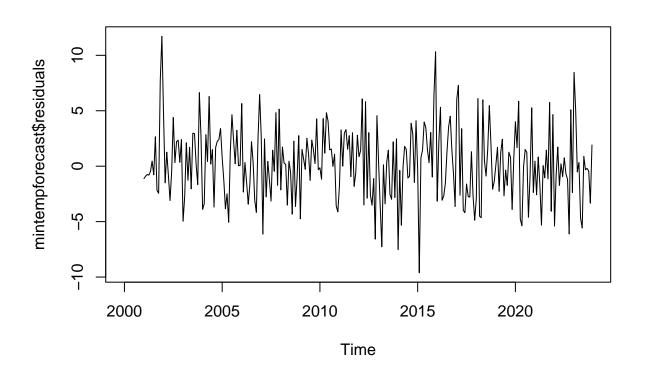
Fitting our model and forecasting for 2024 shows that the model does pick up on seasonality and follow existing trends. To check our accuracy, we can see in the correlogram that autocorrelations for forecast errors do not exceed significance bounds for almost all lags. The p-value for our Ljung-Box test is 0.95, further proving there is little evidence of non-zero autocorrelations at lags 1-20.

X-squared = 10.616, df = 20, p-value = 0.9556

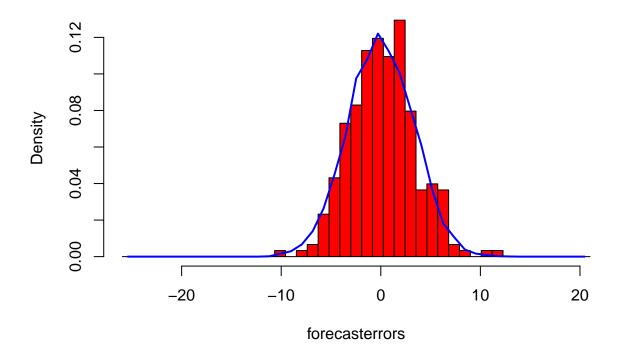
We can also check if forecast errors have constant variance over time and are normally distributed with mean zero.

```
# from the guided tutorial we followed
plotForecastErrors <- function(forecasterrors)
{
    forecasterrors <- na.omit(forecasterrors)
        # make a histogram of the forecast errors:
        mybinsize <- IQR(forecasterrors)/4
        mysd <- sd(forecasterrors, na.rm=T)
        mymin <- min(forecasterrors, na.rm=T) - mysd*5
        mymax <- max(forecasterrors, na.rm=T) + mysd*3</pre>
```

```
# generate normally distributed data with mean O and standard deviation mysd
     mynorm <- rnorm(10000, mean=0, sd=mysd)</pre>
     mymin2 <- min(mynorm)</pre>
     mymax2 <- max(mynorm)</pre>
     if (mymin2 < mymin) { mymin <- mymin2 }</pre>
     if (mymax2 > mymax) { mymax <- mymax2 }</pre>
     # make a red histogram of the forecast errors, with the normally distributed data overlaid:
     mybins <- seq(mymin, mymax, mybinsize)</pre>
     hist(forecasterrors, col="red", freq=FALSE, breaks=mybins)
     # freq=FALSE ensures the area under the histogram = 1
     # generate normally distributed data with mean O and standard deviation mysd
     myhist <- hist(mynorm, plot=FALSE, breaks=mybins)</pre>
     # plot the normal curve as a blue line on top of the histogram of forecast errors:
     points(myhist$mids, myhist$density, type="1", col="blue", lwd=2)
  }
plot.ts(mintempforecast$residuals)
```



plotForecastErrors(mintempforecast\$residuals) # normally distributed with mean 0



From the time plot, we can see that the forecast errors have constant variance over time. From the histogram, we can also assume that forecast errors are normally distributed with mean zero.

ARIMA MODEL

While Holt-Winters exponential smoothing provides an adequate predictive model, we can make a better model by taking correlations in the data into account. We wanted to try making an ARIMA (Autoregressive Integrated Moving Average) model as well.

Based on the tutorial and some trial-and-error in our model building, we realized our data needed to be differenced prior to determing what ARIMA parameters would best fit our model.

Once forcing a manual difference, we can use the auto.arima function to figure out the parameters of our ARIMA model.

```
##
## ARIMA(0,1,0)(0,1,0)[12] : 1753.354
## ARIMA(0,1,0)(0,1,1)[12] : Inf
```

```
ARIMA(0,1,0)(0,1,2)[12]
                                                  : 1589.917
##
                                                  : 1665.576
    ARIMA(0,1,0)(1,1,0)[12]
    ARIMA(0,1,0)(1,1,1)[12]
                                                  : 1590.103
##
    ARIMA(0,1,0)(1,1,2)[12]
                                                  : Inf
    ARIMA(0,1,0)(2,1,0)[12]
                                                  : 1643.012
##
    ARIMA(0,1,0)(2,1,1)[12]
                                                  : 1591.984
                                                  : Inf
    ARIMA(0,1,0)(2,1,2)[12]
##
    ARIMA(0,1,1)(0,1,0)[12]
                                                  : Inf
##
    ARIMA(0,1,1)(0,1,1)[12]
                                                  : Inf
##
                                                  : Inf
    ARIMA(0,1,1)(0,1,2)[12]
    ARIMA(0,1,1)(1,1,0)[12]
                                                  : 1513.352
##
                                                  : Inf
    ARIMA(0,1,1)(1,1,1)[12]
    ARIMA(0,1,1)(1,1,2)[12]
                                                  : Inf
##
    ARIMA(0,1,1)(2,1,0)[12]
                                                  : 1490.029
    ARIMA(0,1,1)(2,1,1)[12]
                                                  : Inf
##
    ARIMA(0,1,1)(2,1,2)[12]
                                                  : Inf
##
    ARIMA(0,1,2)(0,1,0)[12]
                                                  : Inf
##
    ARIMA(0,1,2)(0,1,1)[12]
                                                  : Inf
                                                  : Inf
##
    ARIMA(0,1,2)(0,1,2)[12]
    ARIMA(0,1,2)(1,1,0)[12]
                                                  : 1515.409
##
    ARIMA(0,1,2)(1,1,1)[12]
                                                  : Inf
    ARIMA(0,1,2)(1,1,2)[12]
                                                  : Inf
##
    ARIMA(0,1,2)(2,1,0)[12]
                                                  : 1491.978
    ARIMA(0,1,2)(2,1,1)[12]
                                                  : Inf
##
##
    ARIMA(0,1,3)(0,1,0)[12]
                                                  : Inf
    ARIMA(0,1,3)(0,1,1)[12]
                                                  : Inf
##
                                                  : Inf
    ARIMA(0,1,3)(0,1,2)[12]
                                                  : 1517.363
    ARIMA(0,1,3)(1,1,0)[12]
##
                                                  : Inf
    ARIMA(0,1,3)(1,1,1)[12]
    ARIMA(0,1,3)(2,1,0)[12]
                                                  : 1494.027
##
    ARIMA(0,1,4)(0,1,0)[12]
                                                  : Inf
##
    ARIMA(0,1,4)(0,1,1)[12]
                                                  : Inf
##
    ARIMA(0,1,4)(1,1,0)[12]
                                                  : 1519.449
##
    ARIMA(0,1,5)(0,1,0)[12]
                                                  : Inf
    ARIMA(1,1,0)(0,1,0)[12]
                                                  : 1661.144
##
    ARIMA(1,1,0)(0,1,1)[12]
                                                  : Inf
    ARIMA(1,1,0)(0,1,2)[12]
                                                  : Inf
##
    ARIMA(1,1,0)(1,1,0)[12]
                                                  : 1587.862
##
    ARIMA(1,1,0)(1,1,1)[12]
                                                  : Inf
##
                                                  : Inf
    ARIMA(1,1,0)(1,1,2)[12]
                                                  : 1567.045
    ARIMA(1,1,0)(2,1,0)[12]
##
    ARIMA(1,1,0)(2,1,1)[12]
                                                  : Inf
    ARIMA(1,1,0)(2,1,2)[12]
                                                  : Inf
##
                                                  : Inf
    ARIMA(1,1,1)(0,1,0)[12]
    ARIMA(1,1,1)(0,1,1)[12]
                                                  : Inf
##
                                                  : Inf
    ARIMA(1,1,1)(0,1,2)[12]
##
    ARIMA(1,1,1)(1,1,0)[12]
                                                  : Inf
##
    ARIMA(1,1,1)(1,1,1)[12]
                                                  : Inf
    ARIMA(1,1,1)(1,1,2)[12]
                                                  : Inf
##
    ARIMA(1,1,1)(2,1,0)[12]
                                                   Inf
##
    ARIMA(1,1,1)(2,1,1)[12]
                                                  : Inf
    ARIMA(1,1,2)(0,1,0)[12]
                                                  : Inf
    ARIMA(1,1,2)(0,1,1)[12]
                                                  : Inf
    ARIMA(1,1,2)(0,1,2)[12]
                                                  : Inf
```

```
ARIMA(1,1,2)(1,1,0)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(1,1,2)(1,1,1)[12]
                                                 : 1494.057
    ARIMA(1,1,2)(2,1,0)[12]
   ARIMA(1,1,3)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(1,1,3)(0,1,1)[12]
                                                 : Inf
##
    ARIMA(1,1,3)(1,1,0)[12]
                                                 : Inf
   ARIMA(1,1,4)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(2,1,0)(0,1,0)[12]
                                                 : 1630.335
##
    ARIMA(2,1,0)(0,1,1)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(2,1,0)(0,1,2)[12]
    ARIMA(2,1,0)(1,1,0)[12]
                                                 : 1562.511
    ARIMA(2,1,0)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(2,1,0)(1,1,2)[12]
                                                 : Inf
    ARIMA(2,1,0)(2,1,0)[12]
##
                                                 : 1532.239
    ARIMA(2,1,0)(2,1,1)[12]
                                                 : Inf
    ARIMA(2,1,1)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(2,1,1)(0,1,1)[12]
                                                 : Inf
    ARIMA(2,1,1)(0,1,2)[12]
                                                 : Inf
   ARIMA(2,1,1)(1,1,0)[12]
                                                 : Inf
    ARIMA(2,1,1)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(2,1,1)(2,1,0)[12]
                                                 : 1494.019
    ARIMA(2,1,2)(0,1,0)[12]
                                                 : Inf
    ARIMA(2,1,2)(0,1,1)[12]
##
                                                 : Inf
   ARIMA(2,1,2)(1,1,0)[12]
                                                 : 1519.455
##
                                                 : Inf
##
    ARIMA(2,1,3)(0,1,0)[12]
    ARIMA(3,1,0)(0,1,0)[12]
                                                 : 1620.793
##
                                                 : Inf
    ARIMA(3,1,0)(0,1,1)[12]
##
    ARIMA(3,1,0)(0,1,2)[12]
                                                 : Inf
                                                 : 1550.529
    ARIMA(3,1,0)(1,1,0)[12]
    ARIMA(3,1,0)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(3,1,0)(2,1,0)[12]
                                                 : 1523.49
##
    ARIMA(3,1,1)(0,1,0)[12]
                                                 : Inf
    ARIMA(3,1,1)(0,1,1)[12]
                                                 : Inf
   ARIMA(3,1,1)(1,1,0)[12]
                                                 : 1519.443
    ARIMA(3,1,2)(0,1,0)[12]
                                                 : Inf
                                                 : 1614.582
##
    ARIMA(4,1,0)(0,1,0)[12]
    ARIMA(4,1,0)(0,1,1)[12]
                                                 : Inf
##
    ARIMA(4,1,0)(1,1,0)[12]
                                                 : 1545.551
##
    ARIMA(4,1,1)(0,1,0)[12]
                                                 : Inf
##
                                                 : 1604.366
    ARIMA(5,1,0)(0,1,0)[12]
##
##
##
    Best model: ARIMA(0,1,1)(2,1,0)[12]
mintemp_arima
## Series: mintemp_timeseries
## ARIMA(0,1,1)(2,1,0)[12]
##
## Coefficients:
##
                               sar2
             ma1
                      sar1
```

-0.8623

0.0341

s.e.

-0.6417

0.0598

-0.3145

0.0603

```
## ## sigma^2 = 12.62: log likelihood = -740.94 ## AIC=1489.88 AICc=1490.03 BIC=1504.35
```

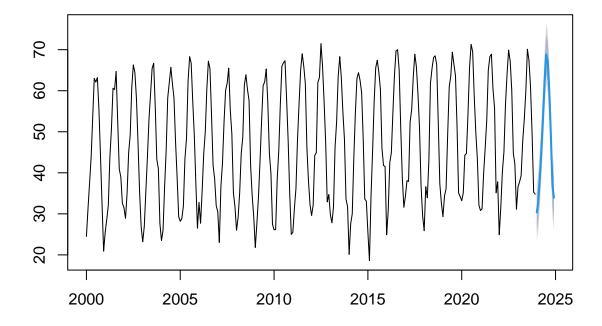
Based on the auto.arima() function, we can determine that an ARIMA(0,1,1)x(2,1,0)[12] best fits our data. We can use this model to forecast for 2024. We want to check that this model meets all assumptions.

```
mintempforecast2 <- forecast(mintemp_arima, h=12) # forecast using ARIMA model
mintempforecast2</pre>
```

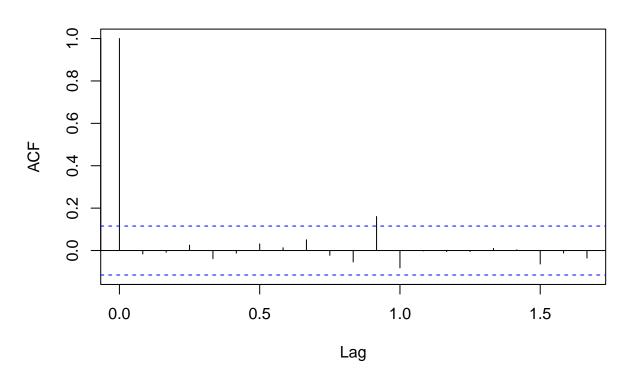
```
##
            Point Forecast
                              Lo 80
                                       Hi 80
                                                 Lo 95
                                                          Hi 95
                  30.34521 25.79311 34.89731 23.38337 37.30705
## Jan 2024
## Feb 2024
                  33.12620 28.53111 37.72128 26.09862 40.15377
## Mar 2024
                  39.14963 34.51196 43.78729 32.05693 46.24232
## Apr 2024
                  45.71244 41.03259 50.39230 38.55522 52.86967
## May 2024
                  53.54706 48.82538 58.26873 46.32588 60.76824
## Jun 2024
                  62.24026 57.47713 67.00338 54.95569 69.52483
## Jul 2024
                  68.86638 64.06216 73.67060 61.51897 76.21380
                  67.20413 62.35917 72.04909 59.79440 74.61386
## Aug 2024
## Sep 2024
                  59.87884 54.99348 64.76421 52.40732 67.35036
## Oct 2024
                  49.37681 44.45137 54.30225 41.84400 56.90962
## Nov 2024
                  36.86023 31.89505 41.82542 29.26664 44.45383
## Dec 2024
                  33.93048 28.92586 38.93510 26.27657 41.58438
```

plot(mintempforecast2) # add forecast values into time series plot

Forecasts from ARIMA(0,1,1)(2,1,0)[12]



Series mintempforecast2\$residuals

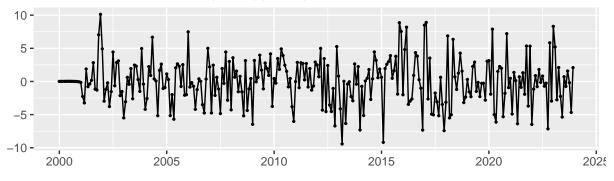


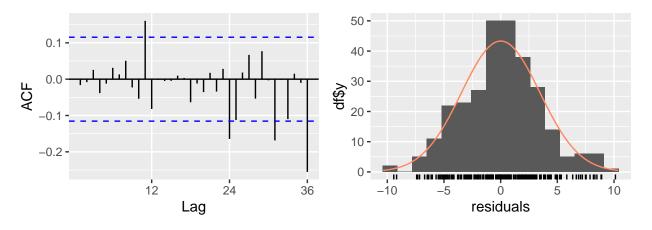
Box.test(mintempforecast2\$residuals, lag=20, type="Ljung-Box") # Ljung-Box test

```
##
## Box-Ljung test
##
## data: mintempforecast2$residuals
## X-squared = 14.434, df = 20, p-value = 0.8078

checkresiduals(mintemp_arima) # chceck that residuals are insignificant
```

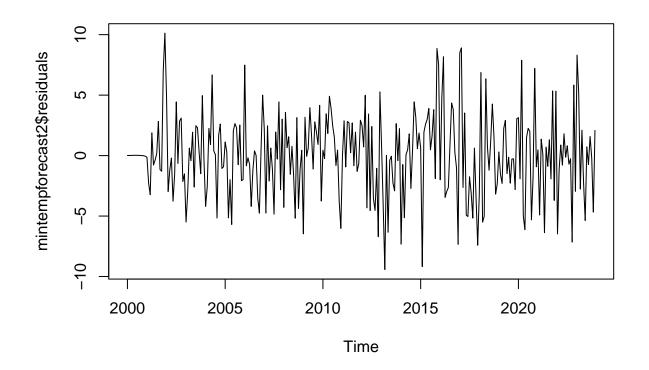




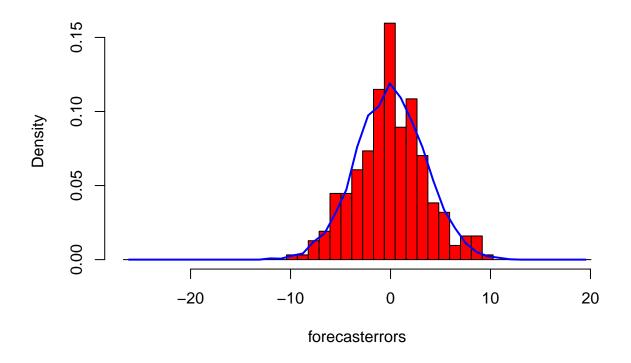


```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(0,1,1)(2,1,0)[12]
## Q* = 23.707, df = 21, p-value = 0.3075
##
## Model df: 3. Total lags used: 24
```

plot.ts(mintempforecast2\$residuals)



plotForecastErrors(mintempforecast2\$residuals) # normally distributed with mean 0



Based on our model and forecast values, we see that the correlogram shows that barely any of the sample autocorrelations for lags 1-20 exceed significance bounds, the p-value of the Ljung-Box test is 0.81, and the p-value of our residuals is 0.31. We can conclude there is little evidence for non-zero autocorrelations in the forecast errors.

From the time plot, we can see that the forecast errors have constant variance over time. From the histogram, we can also assume that forecast errors are normally distributed with mean zero.

Now, let's compare our forecast values from the ARIMA model to our actual values for 2024.

```
# extract 2024 from our data
mintemp_2024 <- mintemp[mintemp$Year==2024, ]
mintemp_2024</pre>
```

```
##
       Month_Year Year Month Mean_Min_Temp
## 25
         Jan 2024 2024
                                         30.9
                           Jan
## 51
         Feb 2024 2024
                           Feb
                                         34.5
  77
         Mar 2024 2024
                                         42.8
##
                           Mar
  103
         Apr 2024 2024
                                         51.4
##
                           Apr
   129
         May 2024 2024
                           May
                                         58.9
  155
         Jun 2024 2024
                                         65.4
##
                           Jun
## 181
         Jul 2024 2024
                           Jul
                                         68.1
## 207
         Aug 2024 2024
                                         65.0
                           Aug
  233
         Sep 2024 2024
                           Sep
                                         58.5
  259
         Oct 2024 2024
                                         46.2
                           Oct
  285
         Nov 2024 2024
                           Nov
                                         40.8
         Dec 2024 2024
## 311
                                         30.1
                           Dec
```

mintempforecast2

```
##
            Point Forecast
                              Lo 80
                                       Hi 80
                                                 Lo 95
                                                          Hi 95
                  30.34521 25.79311 34.89731 23.38337 37.30705
## Jan 2024
## Feb 2024
                  33.12620 28.53111 37.72128 26.09862 40.15377
## Mar 2024
                  39.14963 34.51196 43.78729 32.05693 46.24232
## Apr 2024
                  45.71244 41.03259 50.39230 38.55522 52.86967
## May 2024
                  53.54706 48.82538 58.26873 46.32588 60.76824
## Jun 2024
                  62.24026 57.47713 67.00338 54.95569 69.52483
## Jul 2024
                  68.86638 64.06216 73.67060 61.51897 76.21380
## Aug 2024
                  67.20413 62.35917 72.04909 59.79440 74.61386
## Sep 2024
                  59.87884 54.99348 64.76421 52.40732 67.35036
## Oct 2024
                  49.37681 44.45137 54.30225 41.84400 56.90962
## Nov 2024
                  36.86023 31.89505 41.82542 29.26664 44.45383
## Dec 2024
                  33.93048 28.92586 38.93510 26.27657 41.58438
```

By comparing our forecast values of 2024 to our actual values of 2024, we can see that all the actual data falls in the 95% prediction interval for the forecast. Thus, we meet our goal of being at least 80% accurate with our model.

Maximum Average Temperatures

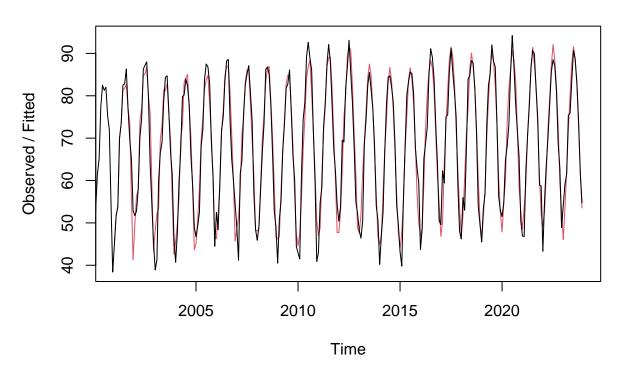
We again built a model using exponential smoothing. Due to the obvious seaonality, we opted to use Holt-Winters exponential smoothing.

```
# fit predictive model
maxtempmodel <- HoltWinters(maxtemp_timeseries)</pre>
maxtempmodel # estimated values of alpha, beta, gamma
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = maxtemp_timeseries)
##
## Smoothing parameters:
    alpha: 0.1484763
##
##
   beta: 0.001741349
##
    gamma: 0.2358454
##
## Coefficients:
##
                [,1]
## a
        72.78009694
         0.05615067
## b
## s1
       -23.05466568
       -17.37428096
## s2
       -10.47583962
## s3
## s4
        -0.20418467
         6.01131442
## s5
## s6
        13.99878463
        19.16614683
## s7
## s8
        16.54661897
```

```
## s9 10.52109934
## s10 0.88235963
## s11 -10.66149562
## s12 -18.84281187
```

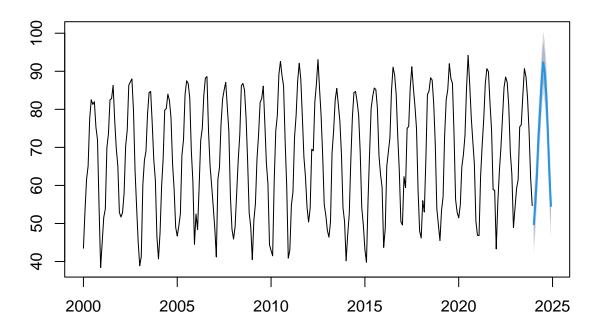
plot(maxtempmodel) # plot model on top of existing data

Holt-Winters filtering



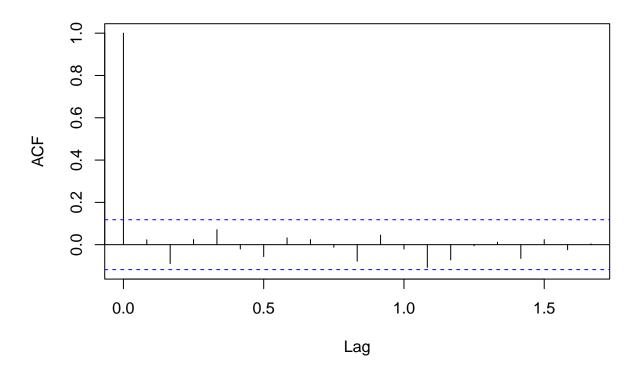
```
# forecasting
maxtempforecast <- forecast(maxtempmodel, h=12) # 12 more months (2024)
plot(maxtempforecast) # plot our forecast values</pre>
```

Forecasts from HoltWinters



checking if there are any non-zero autocorrelations
acf(na.omit(maxtempforecast\$residuals), lag.max=20) # correlogram

Series na.omit(maxtempforecast\$residuals)



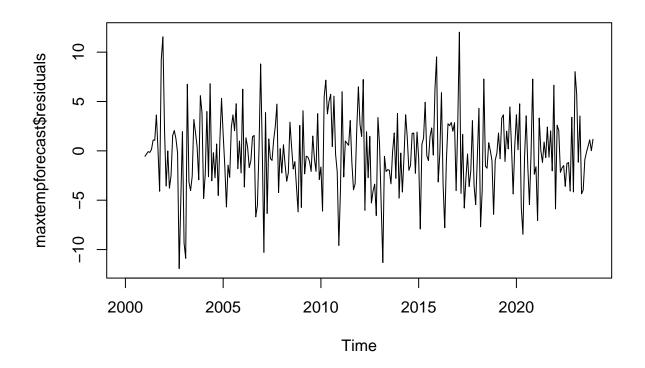
```
Box.test(na.omit(maxtempforecast$residuals), lag=20, type = "Ljung-Box") # Ljung-Box test
```

```
##
## Box-Ljung test
##
## data: na.omit(maxtempforecast$residuals)
## X-squared = 14.52, df = 20, p-value = 0.8032
```

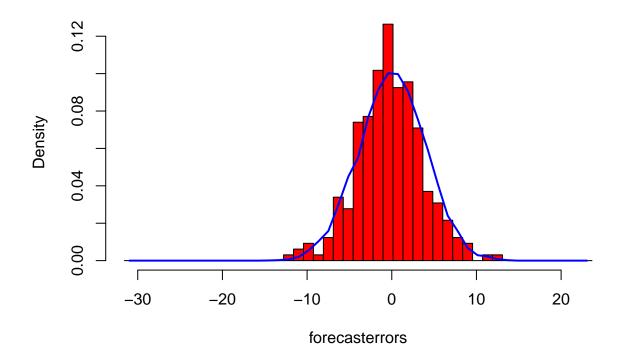
Fitting our model and forecasting for 2024 shows that the model again does pick up on seasonality and follow existing trends. To check our accuracy, we can see in the correlogram that autocorrelations for forecast errors do not exceed significance bounds for all lags. The p-value for our Ljung-Box test is 0.80, further proving there is little evidence of non-zero autocorrelations at lags 1-20.

We can also check if forecast errors have constant variance over time and are normally distributed with mean zero.

```
plot.ts(maxtempforecast$residuals)
```



plotForecastErrors(maxtempforecast\$residuals) # normally distributed with mean 0



From the time plot, we can see that the forecast errors have constant variance over time. From the histogram, we can also assume that forecast errors are normally distributed with mean zero. Despite the curve being a bit wonky, it generally follows the normal distribution curve.

ARIMA MODEL

While Holt-Winters exponential smoothing provides an adequate predictive model, we again wanted to make a better model by taking correlations in the data into account. We wanted to try making an ARIMA (Autoregressive Integrated Moving Average) model for maximum average temperatures as well.

Based on the tutorial and some trial-and-error in our model building, we again noticed our data needed to be differenced prior to determing what ARIMA parameters would best fit our model.

Once forcing a manual difference, we can use the auto.arima function to figure out the parameters of our ARIMA model.

```
## ## ARIMA(0,1,0)(0,1,0)[12] : 1811.063
```

```
ARIMA(0,1,0)(0,1,1)[12]
                                                 : Inf
##
                                                 : Inf
    ARIMA(0,1,0)(0,1,2)[12]
    ARIMA(0,1,0)(1,1,0)[12]
                                                 : 1761.423
##
    ARIMA(0,1,0)(1,1,1)[12]
                                                 : Inf
    ARIMA(0,1,0)(1,1,2)[12]
                                                 : Inf
##
    ARIMA(0,1,0)(2,1,0)[12]
                                                 : 1724.567
    ARIMA(0,1,0)(2,1,1)[12]
                                                 : 1657.14
##
    ARIMA(0,1,0)(2,1,2)[12]
                                                 : 1652.784
##
    ARIMA(0,1,1)(0,1,0)[12]
                                                 : 1683.043
##
    ARIMA(0,1,1)(0,1,1)[12]
                                                 : Inf
    ARIMA(0,1,1)(0,1,2)[12]
                                                 : Inf
##
                                                 : 1624.995
    ARIMA(0,1,1)(1,1,0)[12]
    ARIMA(0,1,1)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(0,1,1)(1,1,2)[12]
                                                 : Inf
    ARIMA(0,1,1)(2,1,0)[12]
                                                 : 1592.023
##
    ARIMA(0,1,1)(2,1,1)[12]
                                                 : Inf
##
    ARIMA(0,1,1)(2,1,2)[12]
                                                 : 1525.06
##
    ARIMA(0,1,2)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(0,1,2)(0,1,1)[12]
                                                 : Inf
    ARIMA(0,1,2)(0,1,2)[12]
                                                 : Inf
##
    ARIMA(0,1,2)(1,1,0)[12]
                                                 : 1626.913
    ARIMA(0,1,2)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(0,1,2)(1,1,2)[12]
                                                 : Inf
    ARIMA(0,1,2)(2,1,0)[12]
                                                 : 1594.074
##
##
                                                 : Inf
    ARIMA(0,1,2)(2,1,1)[12]
    ARIMA(0,1,3)(0,1,0)[12]
                                                 : Inf
##
                                                 : Inf
    ARIMA(0,1,3)(0,1,1)[12]
    ARIMA(0,1,3)(0,1,2)[12]
                                                 : Inf
##
                                                 : 1627.682
    ARIMA(0,1,3)(1,1,0)[12]
    ARIMA(0,1,3)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(0,1,3)(2,1,0)[12]
                                                 : 1594.704
##
    ARIMA(0,1,4)(0,1,0)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(0,1,4)(0,1,1)[12]
##
    ARIMA(0,1,4)(1,1,0)[12]
                                                 : 1629.772
    ARIMA(0,1,5)(0,1,0)[12]
                                                 : Inf
##
                                                 : 1748.582
    ARIMA(1,1,0)(0,1,0)[12]
    ARIMA(1,1,0)(0,1,1)[12]
                                                 : Inf
##
    ARIMA(1,1,0)(0,1,2)[12]
                                                 : Inf
##
    ARIMA(1,1,0)(1,1,0)[12]
                                                 : 1701.23
##
                                                 : Inf
    ARIMA(1,1,0)(1,1,1)[12]
                                                 : Inf
    ARIMA(1,1,0)(1,1,2)[12]
##
    ARIMA(1,1,0)(2,1,0)[12]
                                                 : 1662.546
    ARIMA(1,1,0)(2,1,1)[12]
                                                 : Inf
##
    ARIMA(1,1,0)(2,1,2)[12]
                                                 : 1593.679
    ARIMA(1,1,1)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(1,1,1)(0,1,1)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(1,1,1)(0,1,2)[12]
##
    ARIMA(1,1,1)(1,1,0)[12]
                                                 : 1626.938
    ARIMA(1,1,1)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(1,1,1)(1,1,2)[12]
                                                   Inf
##
    ARIMA(1,1,1)(2,1,0)[12]
                                                 : Inf
    ARIMA(1,1,1)(2,1,1)[12]
                                                 : Inf
    ARIMA(1,1,2)(0,1,0)[12]
                                                 : Inf
    ARIMA(1,1,2)(0,1,1)[12]
                                                 : Inf
```

```
ARIMA(1,1,2)(0,1,2)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(1,1,2)(1,1,0)[12]
   ARIMA(1,1,2)(1,1,1)[12]
                                                 : Inf
## ARIMA(1,1,2)(2,1,0)[12]
                                                 : Inf
    ARIMA(1,1,3)(0,1,0)[12]
                                                 : Inf
##
  ARIMA(1,1,3)(0,1,1)[12]
                                                : Inf
  ARIMA(1,1,3)(1,1,0)[12]
                                                : Inf
## ARIMA(1,1,4)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(2,1,0)(0,1,0)[12]
                                                : 1716.751
##
    ARIMA(2,1,0)(0,1,1)[12]
                                                : Inf
   ARIMA(2,1,0)(0,1,2)[12]
                                                 : Inf
                                                 : 1664.955
    ARIMA(2,1,0)(1,1,0)[12]
                                                 : Inf
    ARIMA(2,1,0)(1,1,1)[12]
    ARIMA(2,1,0)(1,1,2)[12]
                                                 : Inf
    ARIMA(2,1,0)(2,1,0)[12]
                                                 : 1621.051
    ARIMA(2,1,0)(2,1,1)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(2,1,1)(0,1,0)[12]
   ARIMA(2,1,1)(0,1,1)[12]
                                                 : Inf
  ARIMA(2,1,1)(0,1,2)[12]
                                                 : Inf
    ARIMA(2,1,1)(1,1,0)[12]
                                                 : 1627.423
##
    ARIMA(2,1,1)(1,1,1)[12]
                                                 : Inf
  ARIMA(2,1,1)(2,1,0)[12]
                                                 : 1594.292
                                                 : Inf
  ARIMA(2,1,2)(0,1,0)[12]
                                                 : Inf
##
    ARIMA(2,1,2)(0,1,1)[12]
## ARIMA(2,1,2)(1,1,0)[12]
                                                : 1629.51
   ARIMA(2,1,3)(0,1,0)[12]
                                                : Inf
                                                 : 1699.997
    ARIMA(3,1,0)(0,1,0)[12]
    ARIMA(3,1,0)(0,1,1)[12]
                                                 : Inf
                                                 : Inf
   ARIMA(3,1,0)(0,1,2)[12]
  ARIMA(3,1,0)(1,1,0)[12]
                                                 : 1643.218
    ARIMA(3,1,0)(1,1,1)[12]
                                                 : Inf
##
    ARIMA(3,1,0)(2,1,0)[12]
                                                 : 1605.336
    ARIMA(3,1,1)(0,1,0)[12]
                                                 : Inf
                                                 : Inf
  ARIMA(3,1,1)(0,1,1)[12]
    ARIMA(3,1,1)(1,1,0)[12]
                                                 : 1629.5
   ARIMA(3,1,2)(0,1,0)[12]
                                                : Inf
   ARIMA(4,1,0)(0,1,0)[12]
                                                : 1697.362
                                                : Inf
   ARIMA(4,1,0)(0,1,1)[12]
    ARIMA(4,1,0)(1,1,0)[12]
                                                : 1640.132
##
##
    ARIMA(4,1,1)(0,1,0)[12]
                                                : Inf
                                                : 1697.758
    ARIMA(5,1,0)(0,1,0)[12]
##
##
##
    Best model: ARIMA(0,1,1)(2,1,2)[12]
maxtemp_arima
## Series: maxtemp_timeseries
## ARIMA(0,1,1)(2,1,2)[12]
##
## Coefficients:
##
             ma1
                   sar1
                             sar2
                                      sma1
                                              sma2
##
         -0.8468   0.375   -0.1598   -1.3755   0.4570
```

```
## s.e. 0.0430 0.215 0.0744 0.2065 0.2054
##
## sigma^2 = 13.28: log likelihood = -756.37
## AIC=1524.75 AICc=1525.06 BIC=1546.45
```

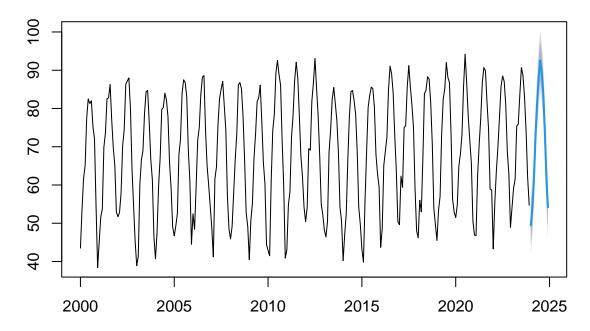
Based on the auto.arima() function, we can determine that an ARIMA(0,1,1)x(2,1,2)[12] best fits our data. We can use this model to forecast for 2024. We want to check that this model meets all assumptions.

```
maxtempforecast2 <- forecast(maxtemp_arima, h=12) # forecast using ARIMA model
maxtempforecast2</pre>
```

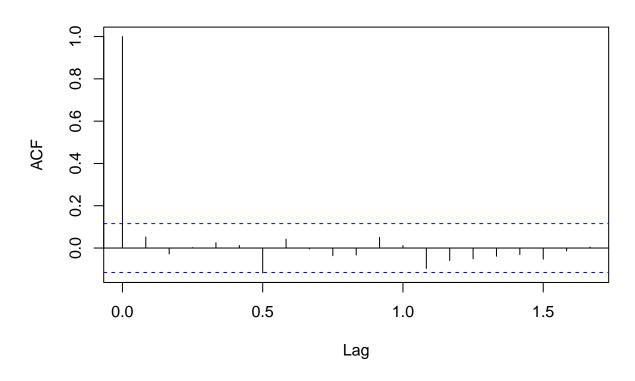
```
##
            Point Forecast
                               Lo 80
                                        Hi 80
                                                 Lo 95
                                                            Hi 95
                                                         56.54211
## Jan 2024
                  49.40025 44.73044 54.07006 42.25839
## Feb 2024
                  53.90951 49.18524 58.63379 46.68436
                                                         61.13467
## Mar 2024
                  61.29836 56.52025 66.07648 53.99086
                                                         68.60586
                  72.74837 67.91701 77.57973 65.35944
                                                         80.13730
## Apr 2024
## May 2024
                  80.60167 75.71765 85.48569 73.13220
                                                         88.07114
  Jun 2024
                  87.89314 82.95702 92.82926 80.34399
                                                         95.44229
  Jul 2024
                  92.58003 87.59235 97.56771 84.95203
                                                        100.20803
## Aug 2024
                  89.47833 84.43962 94.51704 81.77229
                                                         97.18438
## Sep 2024
                  83.84218 78.75296 88.93141 76.05888
                                                         91.62549
## Oct 2024
                  74.10981 68.97056 79.24906 66.25001
                                                         81.96961
## Nov 2024
                  61.50452 56.31573 66.69331 53.56895
                                                         69.44008
## Dec 2024
                  54.19398 48.95612 59.43184 46.18337
                                                         62.20459
```

plot(maxtempforecast2) # add forecast values into time series plot

Forecasts from ARIMA(0,1,1)(2,1,2)[12]



Series maxtempforecast2\$residuals

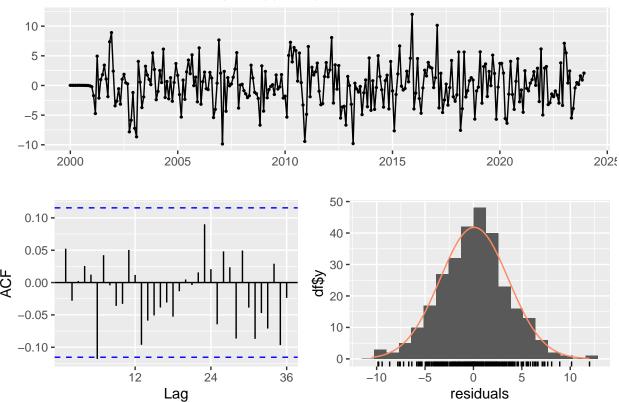


Box.test(maxtempforecast2\$residuals, lag=20, type="Ljung-Box") # Ljung-Box test

```
##
## Box-Ljung test
##
## data: maxtempforecast2$residuals
## X-squared = 13.791, df = 20, p-value = 0.8409

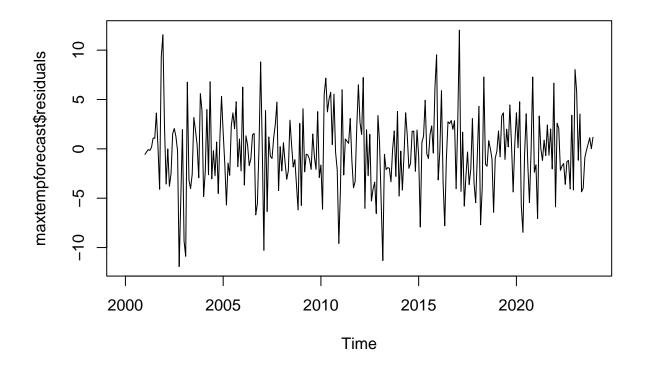
checkresiduals(maxtemp_arima) # check that residuals are insignificant
```

Residuals from ARIMA(0,1,1)(2,1,2)[12]

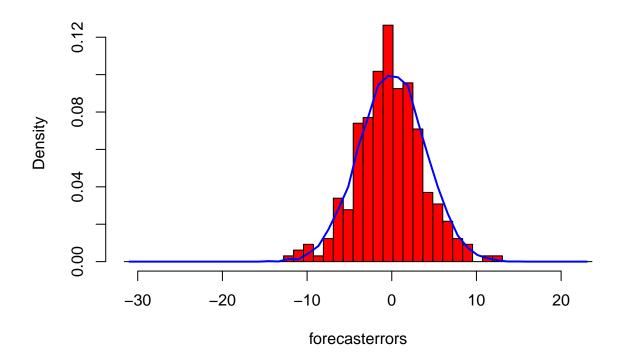


```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(0,1,1)(2,1,2)[12]
## Q* = 16.568, df = 19, p-value = 0.6191
##
## Model df: 5. Total lags used: 24
```

plot.ts(maxtempforecast\$residuals)



plotForecastErrors(maxtempforecast\$residuals) # normally distributed with mean 0



Based on our model and forecast values, we see that the correlogram shows that barely any of the sample autocorrelations for lags 1-20 exceed significance bounds, the p-value of the Ljung-Box test is 0.84, and the p-value of our residuals is 0.62. We can conclude there is little evidence for non-zero autocorrelations in the forecast errors.

From the time plot, we can see that the forecast errors have constant variance over time. From the histogram, we can also assume that forecast errors are normally distributed with mean zero.

Now, let's compare our forecast values from the ARIMA model to our actual values for 2024.

```
# extract 2024 from our data
maxtemp_2024 <- maxtemp[maxtemp$Year==2024, ]
maxtemp_2024</pre>
```

```
##
       Month_Year Year Month Value
## 25
         Jan_2024 2024
                                48.5
                           Jan
## 51
         Feb_2024 2024
                          Feb
                                56.2
         Mar_2024 2024
                                64.7
## 77
                          Mar
## 103
         Apr_2024 2024
                                72.4
                          Apr
##
  129
         May_2024 2024
                                79.4
## 155
         Jun_2024 2024
                                89.2
                           Jun
## 181
         Jul 2024 2024
                           Jul
                                89.3
## 207
         Aug_2024 2024
                          Aug
                                86.2
## 233
         Sep_2024 2024
                          Sep
                                76.2
  259
         Oct_2024 2024
##
                          Oct
                                71.9
## 285
         Nov_2024 2024
                          Nov
                                61.8
         Dec_2024 2024
                                46.6
## 311
                          Dec
```

maxtempforecast2

```
##
            Point Forecast
                              Lo 80
                                        Hi 80
                                                 Lo 95
                                                           Hi 95
## Jan 2024
                  49.40025 44.73044 54.07006 42.25839
                                                        56.54211
## Feb 2024
                  53.90951 49.18524 58.63379 46.68436
                                                        61.13467
                                                        68.60586
## Mar 2024
                  61.29836 56.52025 66.07648 53.99086
## Apr 2024
                  72.74837 67.91701 77.57973 65.35944
                                                        80.13730
                                                        88.07114
## May 2024
                  80.60167 75.71765 85.48569 73.13220
## Jun 2024
                  87.89314 82.95702 92.82926 80.34399
                                                        95.44229
## Jul 2024
                  92.58003 87.59235 97.56771 84.95203 100.20803
## Aug 2024
                  89.47833 84.43962 94.51704 81.77229
                                                        97.18438
## Sep 2024
                  83.84218 78.75296 88.93141 76.05888
                                                        91.62549
## Oct 2024
                  74.10981 68.97056 79.24906 66.25001
                                                        81.96961
## Nov 2024
                  61.50452 56.31573 66.69331 53.56895
                                                        69.44008
## Dec 2024
                  54.19398 48.95612 59.43184 46.18337
                                                        62.20459
```

By comparing our forecast values of 2024 to our actual values of 2024, we again can see that all the actual data falls in the 95% prediction interval for the forecast. Thus, we meet our goal of being at least 80% accurate with our model.

Using ARIMA models with differencing and a seasonality component allowed us to build accurate models which generated prediction intervals that managed to capture our actual data points.