

Leptophilic Dark Matter

Gerrit Bickendorf

April 23, 2019

- Introduce need for leptophilic mediators
- Introduce a vector and scalar model
- Constrains from muon decay spectrum
- Constrains from lepton universality in π^+ decays
- Constrains from π^+ decay spectrum

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- Only interaction: Through mediator
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- No tree level coupling to quarks and SM-gauge bosons
- Only direct coupling to leptons
→ "Leptophilic"

Leptophilic Mediator

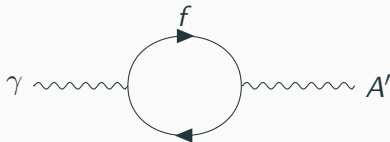
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$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{\text{SM}} - \frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} + \frac{m_{A'}^2}{2} A'_\mu A'^\mu + \frac{\epsilon}{2} F'_{\mu\nu} F^{\mu\nu} \\ & - \sum_{l=e,\mu,\tau} e'_l (\bar{l} \gamma^\mu A'_\mu l + \bar{\nu}_l \gamma^\mu A'_\mu \nu_l) \\ & + \bar{\chi} (i \not{\partial} - m_\chi) \chi - g_D \bar{\chi} \gamma^\mu A'_\mu \chi\end{aligned}$$

Vector Model

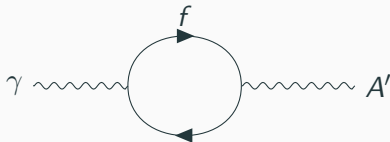


$$\epsilon = \sum_l \frac{ee'_l}{12\pi^2} \ln \left(\frac{m_\tau^2}{\mu^2} \right)$$

After diagonalisation:

$$\mathcal{L} \supset e\epsilon A'_\mu J_{em}^\mu$$

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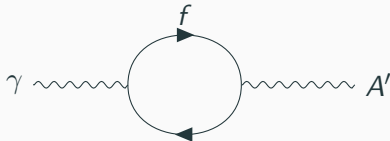


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Scalar Model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{m_\phi^2}{2} \phi - \sum_{l=e,\mu,\tau} e'_l \bar{l} l \phi \\ + \bar{\chi} (i \not{\partial} - m_\chi) \chi - g_D \bar{\chi} \chi \phi$$

- From effective dim. 5 operator

$$\frac{c_l}{\Lambda} \phi \bar{L}_l \Phi e_{lR} + h.c.$$

- After SSB

$$e'_l = \frac{c_l v}{\Lambda \sqrt{2}}.$$

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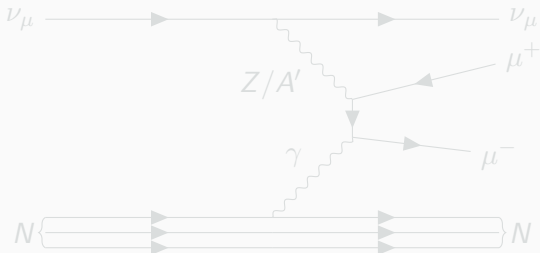
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Experimental constraints

Neutrino Trident Production

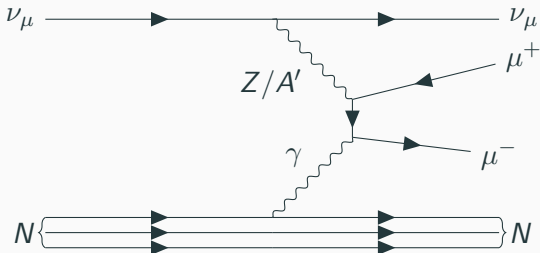


Contribution to [1]

$$\frac{\sigma_{CCFR}}{\sigma_{SM}} = 0.82 \pm 0.28$$

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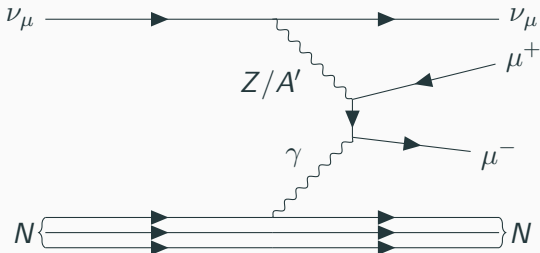


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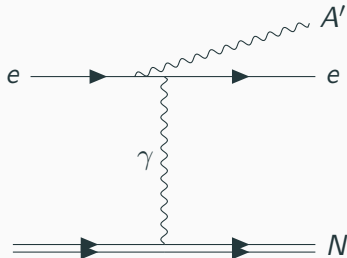
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NA64 [2]:

- Missing energy search for invisible dark photo decay

$$e^- N \rightarrow e^- N A' (A' \rightarrow \bar{\chi} \chi)$$

- Only $m_{A'} > 1\text{MeV}$



BABAR:

- e^+e^- collider process:

$$e^+e^- \rightarrow \gamma A' (A' \rightarrow \bar{\chi}\chi)$$

- Detect mono photon events with CM energy E_γ^* and search for peak in $M_X^2 = s - 2E_\gamma^*\sqrt{s}$
- $0 < m_{A'} < 8\text{GeV}$

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Atomic physics [3] :

- Additional scalars add potential:

$$V^{ij}(r) = -\frac{e'_i e'_j}{4\pi} \frac{e^{-m_\phi}}{r}$$

→ Energy shift

- Positronium (e^+e^-) 1S-2S transition
→ bound on e'_e
- Muonium ($e^-\mu^+$) 1S-2S transition and Lamb shift
→ bound on $e'_e \times e'_\mu$

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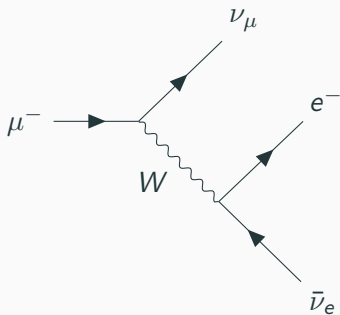
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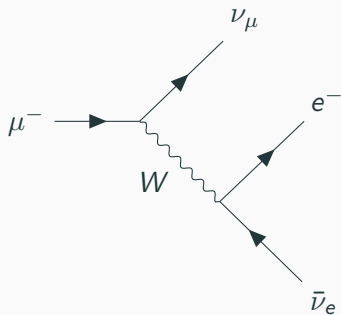
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Standard Model Muon Decay



$$\mathcal{M} = \frac{g^2}{8m_W^2} \bar{u}(P_{\nu_\mu}, s_{\nu_\mu}) \gamma_\mu (1 - \gamma^5) u(P, s) \bar{u}(P_e, s_e) \gamma^\mu (1 - \gamma^5) v(P_{\nu_e}, s_{\nu_e})$$

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Muon decay spectrum

$$\frac{d^2\Gamma}{dx d\cos\theta} = \frac{m_\mu}{4\pi^3} W_{e\mu}^4 G_f^2 \sqrt{x^2 - x_0^2} (F_{IS}(x) - P_\mu \cos\theta F_{AS}(x))$$

$$F_{IS} = x(1-x) + \frac{2}{9}\rho(4x^2 - 3x - x_0^2) + \eta x_0(1-x)$$

$$F_{AS} = \frac{1}{3}\xi\sqrt{x^2 - x_0^2} \left[1 - x + \frac{2}{3}\delta(4x - 4 + \sqrt{1 - x_0^2}) \right]$$

SM Michel Parameters values:

$$\rho = 3/4$$

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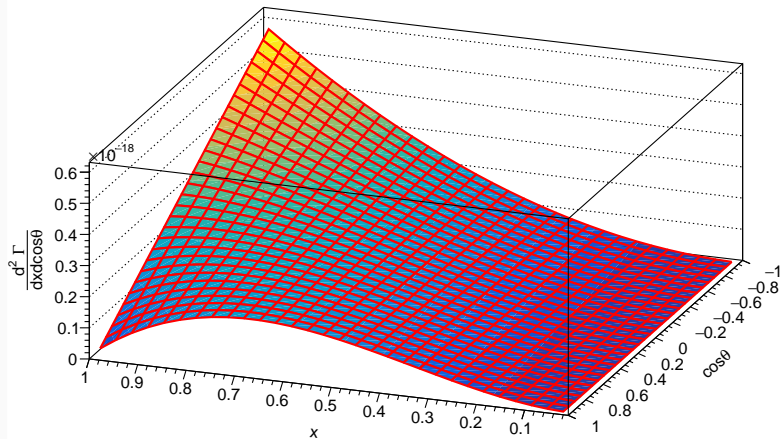
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- Sensitive to interactions besides V-A
- Experimental results [4]:

$$\rho = 0.74979 \pm 0.00026$$

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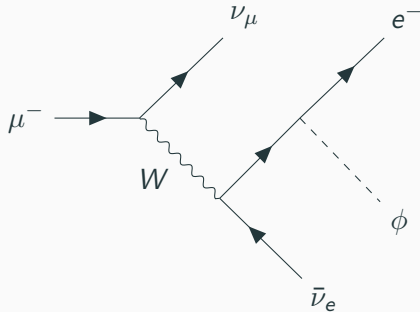
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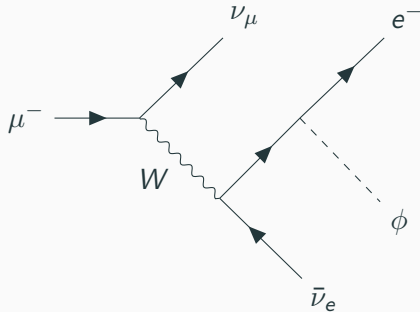
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2. Numerically integrate phase space except E_e and $\cos \theta$
Standard MC (e.g. MadGraph) slow for $N \sim 10^9$
→ Quadrature on GPU
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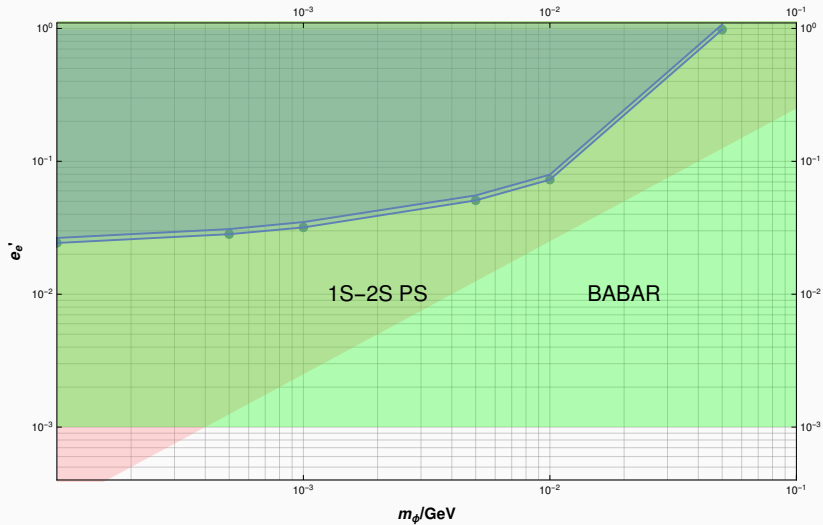
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Scalar to Electron



- Muon specific scalar mediator badly motivated
→ no existing bounds
- Better motivated: Mass-hierarchical couplings

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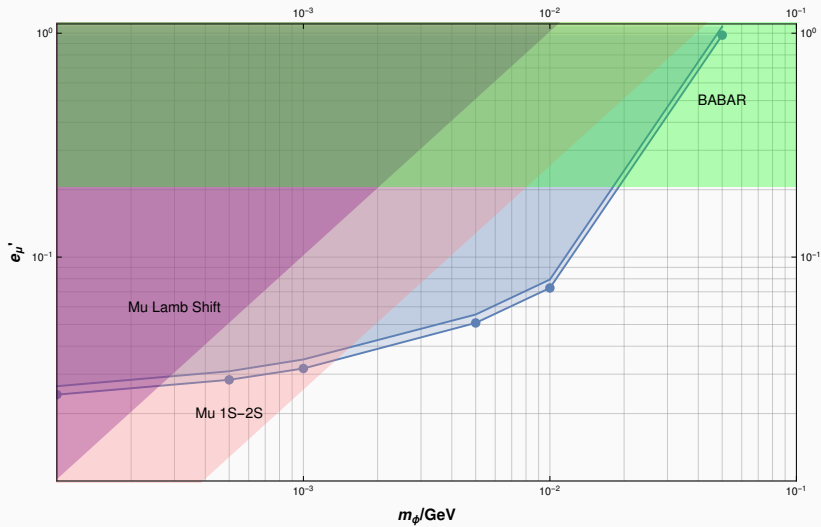
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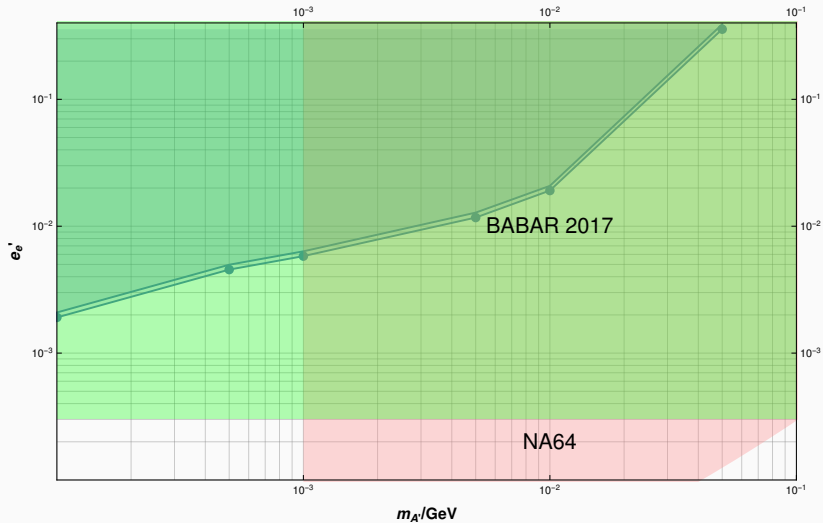
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Scalar to Muon



Vector to Electron



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→ scarce literature
- Use least constrained model:
Gauged $L_{\mu-\tau}$
- Additionally constrained by 1 loop kinetic mixing

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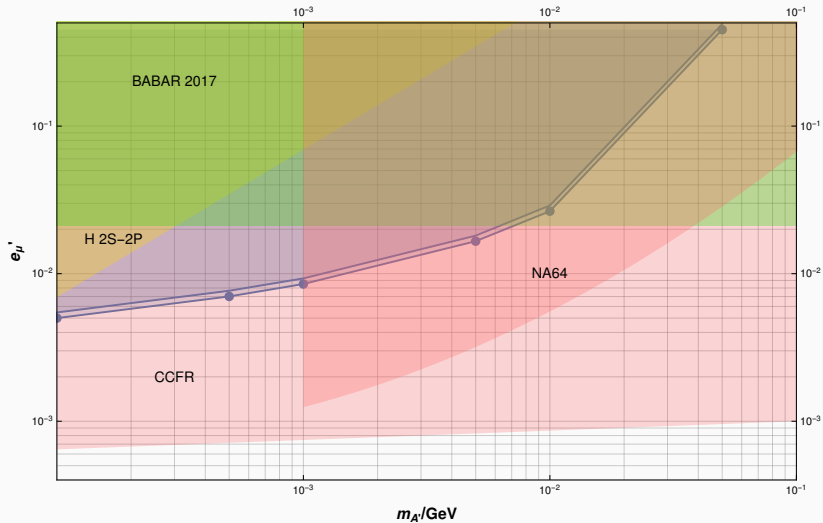
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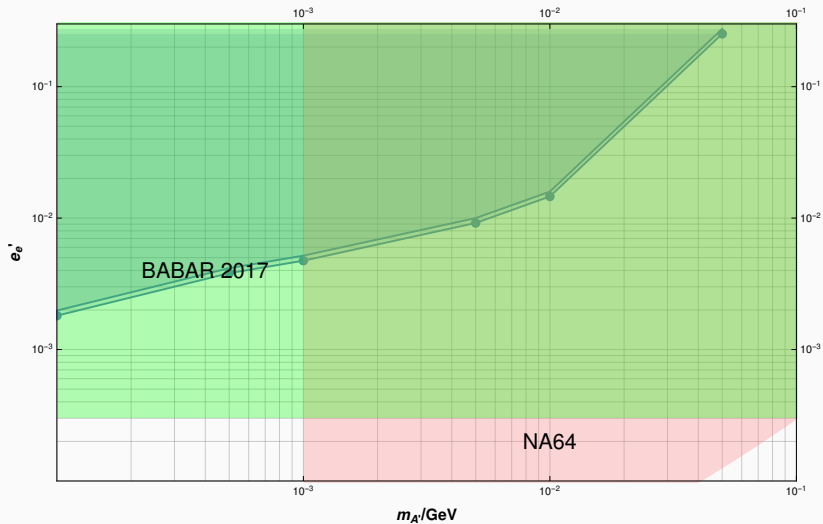
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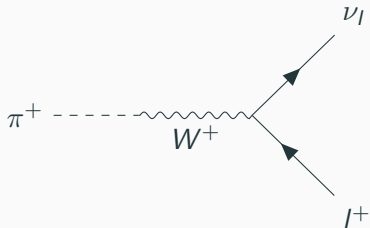
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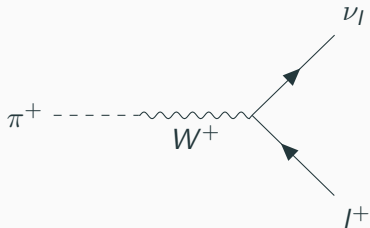
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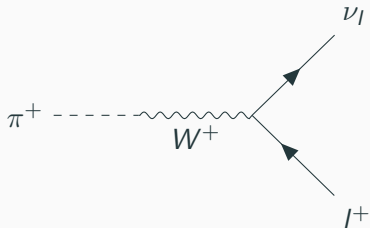
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Helicity Suppression

- $\pi^+ \rightarrow e^+ \nu_e$ suppressed

$$\frac{\Gamma_e}{\Gamma_\mu} \sim \frac{m_e^2}{m_\mu^2}$$

- Full standard model prediction [5]:

$$R_{e/\mu}^\pi \equiv \frac{\Gamma(e^+ \nu_e(\gamma))}{\Gamma(\mu^+ \nu_\mu(\gamma))} = (1.2352 \pm 0.0001) \cdot 10^{-4}$$

- Sensitive to coupling between scalar and electron

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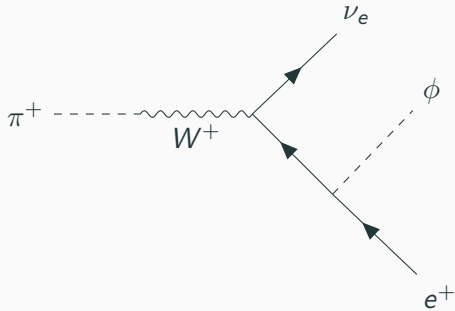
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Method II

- Calculate width

$$\Gamma(e^+\nu_e\phi) = \frac{e_e'^2 G_f^2 F_0^2 V_{ud}^2 m_\pi^3}{384\pi^3} \times$$
$$\left(1 - \left(\frac{m_\phi}{m_\pi} \right)^6 + \left(\frac{m_\phi}{m_\pi} \right)^2 \left(9 + 6 \ln \left(\frac{m_\phi^2}{m_\pi^2} \right) \right) \right.$$
$$\left. - \left(\frac{m_\phi}{m_\pi} \right)^4 \left(9 - 6 \ln \left(\frac{m_\phi^2}{m_\pi^2} \right) \right) \right)$$

- Find e_e' that still agrees with experiment [6]

$$R_{e/\mu}^\pi = (1.2344 \pm 0.0023(\text{stat.}) \pm 0.0019(\text{syst.})) \cdot 10^{-4}$$

Method II

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$$\Gamma(e^+\nu_e\phi) = \frac{e_e'^2 G_f^2 F_0^2 V_{ud}^2 m_\pi^3}{384\pi^3} \times \\ \left(1 - \left(\frac{m_\phi}{m_\pi} \right)^6 + \left(\frac{m_\phi}{m_\pi} \right)^2 \left(9 + 6 \ln \left(\frac{m_\phi^2}{m_\pi^2} \right) \right) \right. \\ \left. - \left(\frac{m_\phi}{m_\pi} \right)^4 \left(9 - 6 \ln \left(\frac{m_\phi^2}{m_\pi^2} \right) \right) \right)$$

- Find e_e' that still agrees with experiment [6]

$$R_{e/\mu}^\pi = (1.2344 \pm 0.0023(\text{stat.}) \pm 0.0019(\text{syst.})) \cdot 10^{-4}$$

Method II

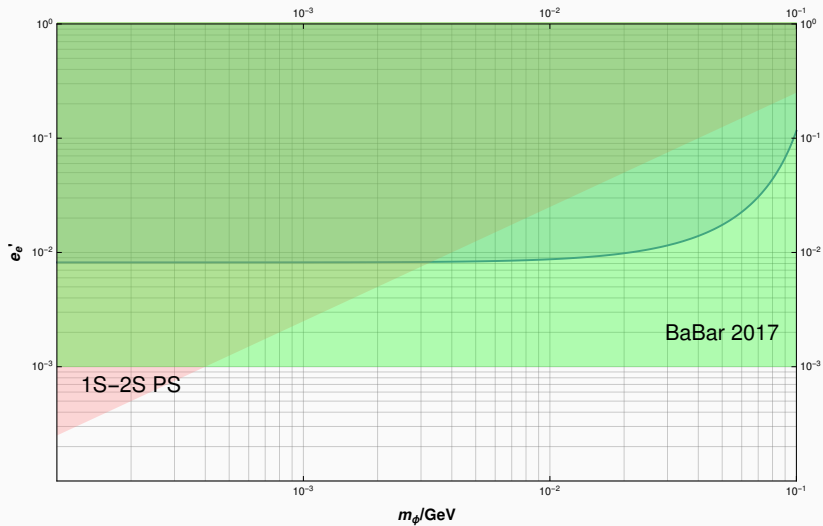
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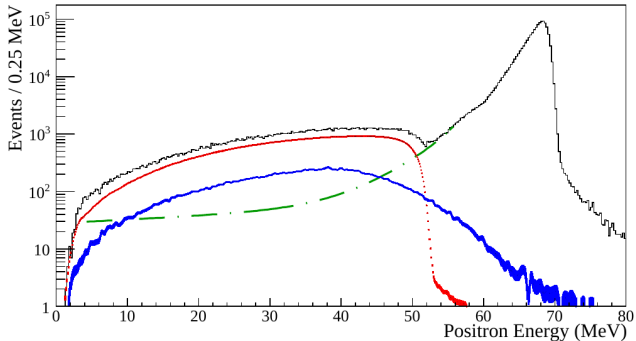
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Result



PIENU: Search for heavy neutrino [7]

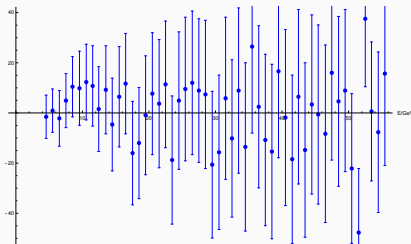


Decay in flight (blue)

$\pi^+ \rightarrow e^+ \nu_e$ (green)

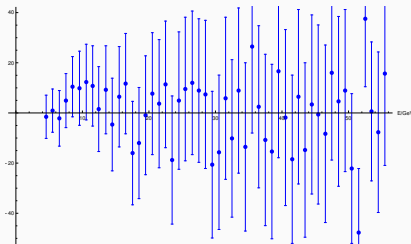
$\pi^+ \rightarrow \mu^+ + \nu_\mu \rightarrow e^+ \nu_e + \nu_\mu$ (red)

- Subtract background



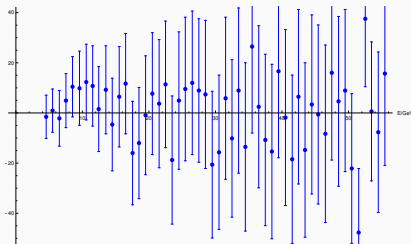
- Additional peaks \rightarrow heavy neutrinos
- Similar to additional couplings

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Method III

1. Generate MC spectrum
2. Compare to PIENU data
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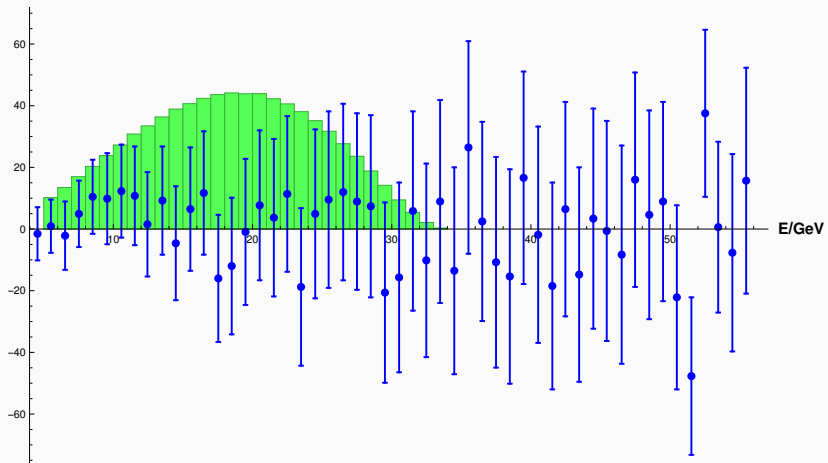
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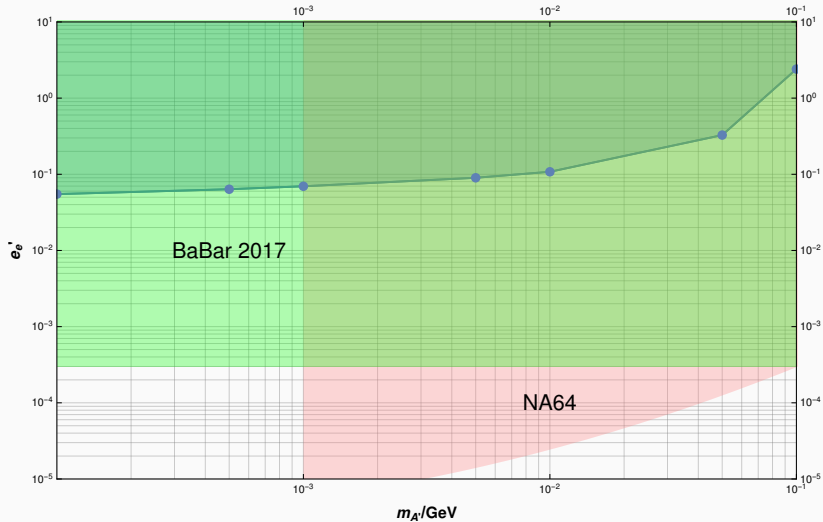
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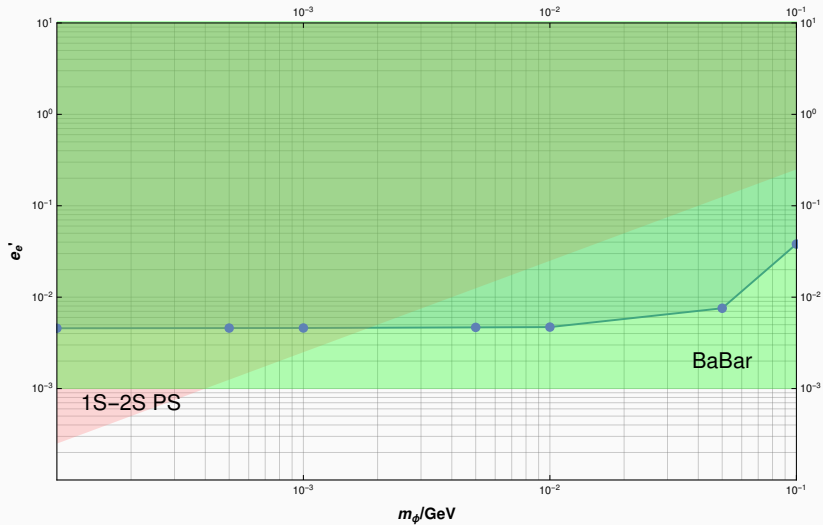
Example 90% C.L bound



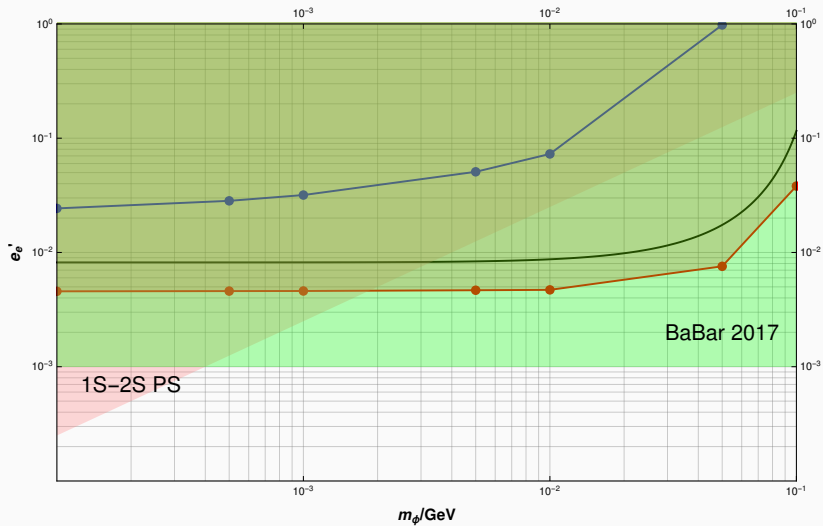
Vector to Electron



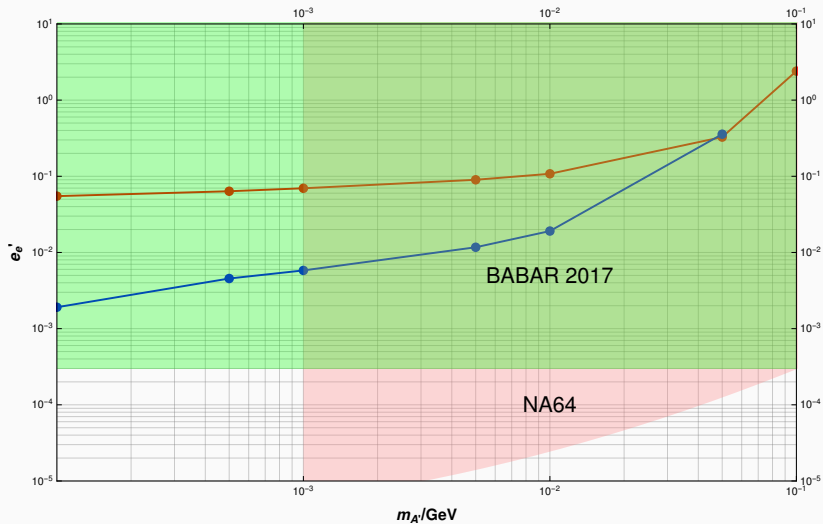
Scalar to Electron



Combined Scalar to Electron



Combined Vector to Electron



Muon decay

- Only scalar-muon coupling bound competitive for $m_\phi = 1 - 10\text{MeV}$
- Others more competitive if Michel parameters \sim two orders of magnitude more precise

Pion decay:

- No new bounds
- New bounds on scalar if $R_{e/\mu}^\pi$ improves by two orders
- New bounds on scalar if heavy neutrino search improves by one order!

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