

# CSC411 Machine Learning

## Project 4: Reinforcement Learning

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4 April 2018

## 1 Introduction

### 1.1 Results & Report Reproducibility

All results and plots can be generated using the code in `tictactoe.py`. All code is python 3, run with Anaconda 3.6.3. Running the code will save all generated images in the `resources` folder, where they are used by  $\text{\LaTeX}$ . Note that some of the sections require the code for other sections (in the same file) to be run first. To reproduce the report, simply run it through  $\text{\LaTeX}$ . This will pull the most recently generated figures from the `resources` folder.

### 1.2 Tic Tac Toe Environment

The `Environment` class provides the functionality required to play a game of tic tac toe, including against an opponent who plays a random legal move. The game is represented by the `grid` attribute, which is a `numpy` array representing the 9 positions. Each position can have a 0, 1 or 2, representing an empty position, or one filled by player 1 (*X*) or 2 (*O*) respectively. The `turn` attribute can have a value of 1 or 2, and represents which player has the next move. The `done` attribute is a boolean that indicates whether a game has been completed (either with a win, or when the board is full).

The `step()` and `render()` methods allow a tic tac toe game to be played and displayed with text output. Using these methods, a game was played, resulting in the following output:

```
...  
.x.  
...  
=====  
o..  
.x.  
...  
=====  
o.x  
.x.  
...  
=====  
o.x  
ox.
```

```

...
=====
O.X
OX.
X..
=====

```

## 2 Policy

The `Policy` class implements a neural network that learns to play tic tac toe. The provided starter code was modified to be a one-hidden layer neural network; the final code is shown in the code block below.

```

class Policy(nn.Module):
    """
    The Tic-Tac-Toe Policy
    """
    def __init__(self, input_size=27, hidden_size=64, output_size=9):
        super().__init__()
        self.Linear1 = nn.Linear(input_size, hidden_size)
        self.Linear2 = nn.Linear(hidden_size, output_size)

    def forward(self, x):
        h = F.relu(self.Linear1(x))
        out = F.softmax(self.Linear2(h))
        return out

```

In choosing an action, the state is represented as a 27-dimensional vector, using a one-hot encoding type scheme. The first nine elements are 1 if the corresponding location (moving horizontally, and then from top to bottom), and 0 otherwise. Similarly, the next 9 elements are 1 if an *X* (representing player 1) is in the corresponding location; while the last nine elements provide the same functionality for *O* (player 2).

The policy outputs a nine-dimensional vector, which is a probability distribution that is sampled to choose the move for the policy. Thus the policy is stochastic - the `select_action()` function samples this distribution to choose a move.

## 3 Policy Gradient

The `compute_returns()` function computes the returns based on the reward at the end of a game. The following code block shows how the returns are calculated.

```

def compute_returns(rewards, gamma=1.0):
    """
    Compute returns for each time step, given the rewards
    """
    k = len(rewards)
    rewards = np.array(rewards)
    gammas = np.array([gamma**(i) for i in range(k)])
    G = [sum(rewards[i:]*gammas[:k-i]) for i in range(k)]
    return G

```

The weights are updated on the conclusion of a game, though this means that the policy does not improve during a game (this is a minor cost considering how short the games are). For updates to the policy to have any meaning in the middle of the game, there would need to be rewards for intermediate

states. This would require having a metric that evaluates a tic tac toe position. While this could be done in tic tac toe, it would be quite difficult in more complicated games, where it is not obvious how a position should be rewarded. Having rewards only at the end still improves the policy choices earlier in the game (if an early position leads to a win, that position will be weighted more positively when propagating backwards). Thus updating the weights at the end of an episode provides a simple way to provide feedback and improve the policy.

## 4 Rewards

When originally setting the rewards (in the `get_reward()` function), they were set as shown in table 1. The logic behind these rewards was to follow an intuitive feeling for how much the above results are

status	reward
VALID_MOVE	1
INVALID_MOVE	-10
WIN	15
TIE	3
LOSE	-1

Table 1: Original rewards (the `DONE` status was not give a reward).

actually desired. This is somewhat arbitrary, but does represent a reasonable starting point. Thus a valid move should get a small positive reward, while an invalid one should be heavily penalized. A win is highly rewarded, a tie gets some reward for preventing a loss, while a loss is penalized (it would have been reasonable to start with a more negative penalty here too). The `DONE` status was not given a reward; that scenario is taken care of by the `TIE` status.

However, while debugging during training, the rewards were set to much simpler values, and - since after the issues were resolved the win rate was quite high - the changed rewards were kept. These rewards were simply +1 for a win, and -1 for an invalid move. A side-effect of this scheme is that the average return is equivalent to the win rate.

The final `get_reward()` function is shown in the following code block.

```
def get_reward(status):
    """Returns a numeric given an environment status."""
    return {
        Environment.STATUS_VALID_MOVE : 0,
        Environment.STATUS_INVALID_MOVE: -1,
        Environment.STATUS_WIN         : 1,
        Environment.STATUS_TIE         : 0,
        Environment.STATUS_LOSE        : 0
    }[status]
```

## 5 Training

### 5.1 Learning Curve

Figure 1 shows a learning curve, showing the average returns of the 1000 previous episodes. Note that the policy is modified throughout these episodes. The policy has one hidden layer with 64 hidden

neurons (this is the default value that will be experimented with in the next subsection), a RELU activation, as well as a softmax layer on the output (to convert the output to a probability distribution). A gamma of 0.99 was used to discount the rewards. Using a gamma of 1 lowered the average returns and win rate by over 10% (plots showing these results can be found in the **resources** folder).

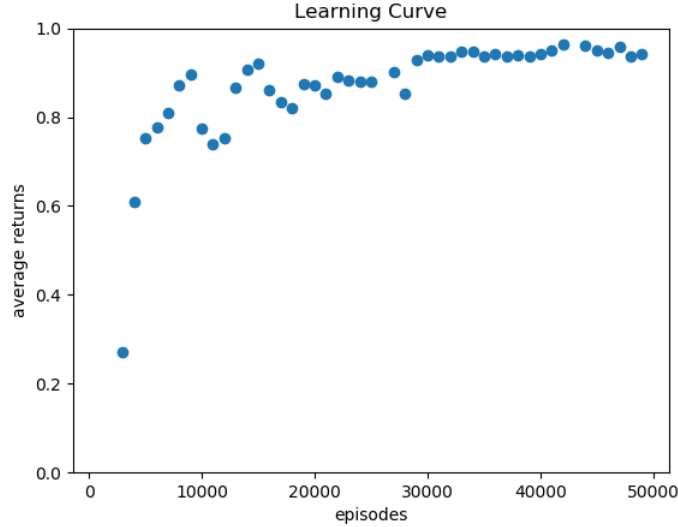


Figure 1: Learning curve showing the average return as a function of the number of episodes that have been played. Only points in the interval  $[0, 1]$  are shown (this gave the best scale), though there are points with lower average returns (a plot with all points is saved as **part5a\_allPoints** in the **resources** folder).

## 5.2 Hidden Units

The value of 64 hidden neurons gave excellent results as shown in figure 1, but changes to this value were explored to show how results changed as this number was varied. Table 2 shows several metrics

number of hidden units	win rate %	avg returns	invalid moves %
2	61.3	-1.4	33
9	91.4	0.88	0.5
27	93.6	0.94	0.1
64	93.9	0.94	0
100	93.9	0.94	0

Table 2: Win rate after 50000 episodes varying with the number of hidden units in the policy. The win rate shown was found by playing the policy against a random opponent for 1000 games.

for evaluation the policy after 50000 episodes. 2 hidden neurons clearly do not have enough capacity to form a good policy, while 9 preforms pretty well (much higher than the 60% baseline win rate for a random player with the first move), and 27 is already almost indistinguishable from 100.

### 5.3 Invalid Moves

Figure 2 shows the fraction of all moves played by the learned policy that were invalid. As above, each point is the average over the previous 1000 episodes. Looking at the graph, invalid moves have pretty much completely stopped before the 10000th episode (less than 1 %), though there are still statistical fluctuations to much higher rates of invalid moves.

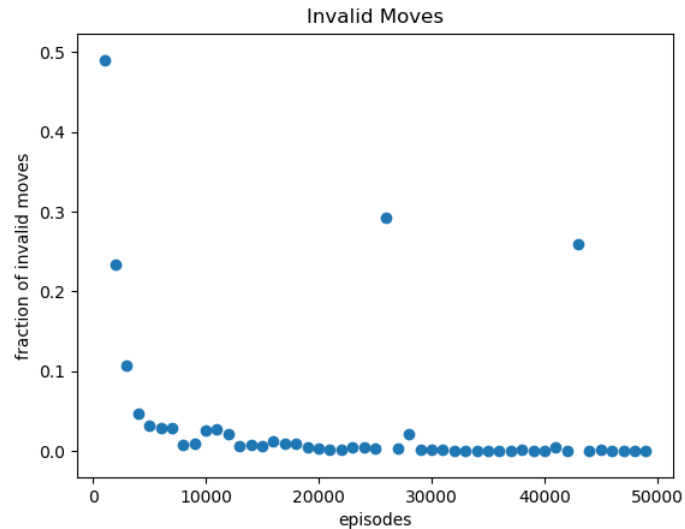


Figure 2: Fraction of invalid moves varying with the number of episodes that have been played as part of training.

### 5.4 Win-Lose-Tie Ratios

Playing 100 games against a randomized opponent...

## 6 Win Rate over Episodes

Figure 3 shows

## 7 First Moves

## 8 Limitations



Figure 3: Win-Lose-Tie Ratios