A web search for linear systems related to my field of study in electrical engineering resulted in the following links.

https://sites.math.washington.edu/~king/coursedir/m308a01/Projects/m308a01-pdf/taing.pdf

http://faculty.uaeu.ac.ae/w_ahmed/differential/Lectures/Applications%20of%20Systems%20of%20Line ar%20Equations.pdf

There are two types of problems discussed in these web pages that would apply to electrical engineering. The first is node voltage analysis of resistor circuits. Complex resistive circuits form a linear system of n equations and n unknowns. The following is an example to illustrate using a linear solver to analyze the node voltages in a complex resistor circuit. The circuit has a 12VDC power source and a common reference at the negative side of the power source. This means we know the value for the two nodes the power source is connected to, 12VDC on the positive side and 0VDC on the negative side. The nodes labeled X1 through X7 are unknown and we can form a linear system to compute the unknown voltages at each of the nodes. The system will be seven equations and seven unknowns and can be derived using Kirchhoff's Current Law which states that all currents entering and leaving a node must sum to zero. As a note, the node voltages X1 through X7 are values with respect to the common reference at the negative side of the power source. See figure 1 through 3 for the resistor circuit and derived equations for the linear system to solve. Figure 4 defines equalities between variable names in the circuit for comparison with the results from my linear solving routine and the results from simulating the circuit in LTspice (a computer application for circuit analysis). The derived node voltage equations are put in matrix form and augmented with the known values forming the linear problem Hx=b where x is a vector of unknowns to solve for. The results from my programed linear solver are shown in figure 5, the results of my linear solver can also be viewed in homework problem 10. For comparison, the LTspice simulator results are shown in figure 6.

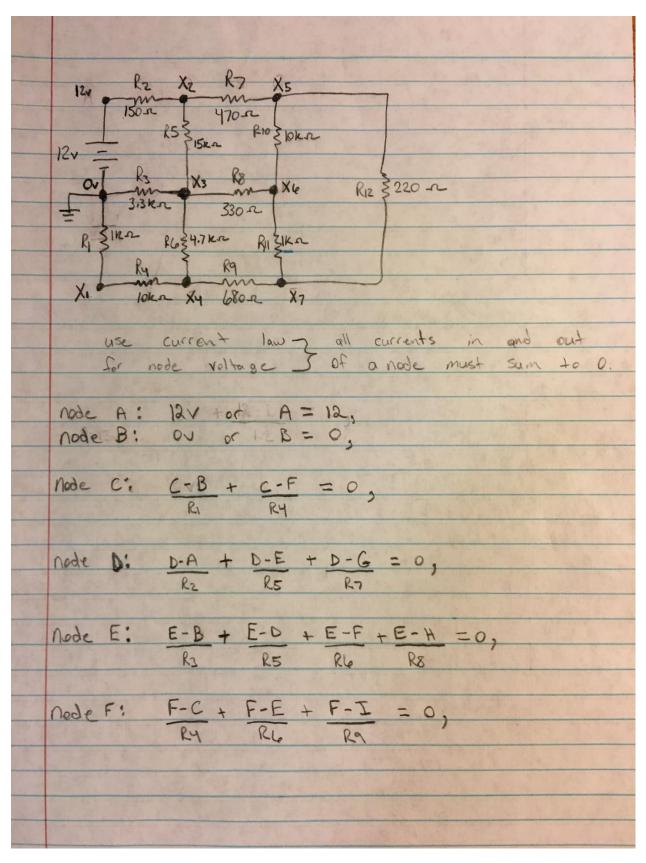


Figure 1: Resistor circuit and node voltage equations.

node G:
$$G-D + G-H + G-I = 0$$
,

 $R7$
 $R10$
 $R12$

node H: $H-G+H-I+B=0$,

 $R10$
 $R11$
 $R2$

node T: $I-F+I-H+I-G=0$.

 $R11$
 $R12$

node C: $-1/R_1B+1/R_2C=1/R_1C=0$
 $-1/R_1B+1/R_2C=1$

Figure 2: Node voltage equations.

node F:
$$\begin{pmatrix} 1 + 1 + 1 \\ RY & RQ \end{pmatrix}$$
 F - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ C - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ C - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ F - 0.0001 C - 0.000212765957 E - 0.001470588235 I = 0

Node G: $\begin{pmatrix} 1 + 1 \\ RY \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ D - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ H - $\begin{pmatrix} 1 \\ RY \end{pmatrix}$ I = 0

10.00677311412 G - 0.002127659574 D - 0.0001 H - 0.004545454545 I = 0

Node H: $\begin{pmatrix} 1 + 1 + 1 \\ RIO \end{pmatrix}$ H - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ G - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ I - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ E = 0

10.00413030303 H - 0.0001 G - 0.001 I - 0.00303030303 S = = 0

Node I: $\begin{pmatrix} 1 + 1 + 1 \\ RIO \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ F - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ H - $\begin{pmatrix} 1 \\ RIO \end{pmatrix}$ G = 0.00303030303 S = 0.001 I - 0.00303030303 S = 0.003030303 S = 0.003

Figure 3: Node voltage equations.

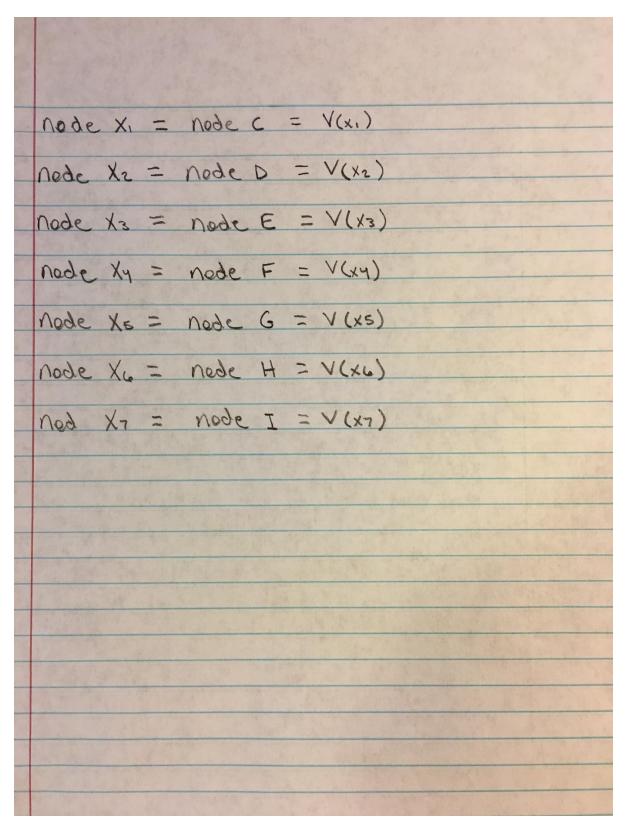


Figure 4: Equalities between variable names.

```
Augmented matrix H =
1.100e-03
0.000e+00
                 0.000e+00
                                                                                                                             |0.000e+00
|8.000e-02
                                   0.000e+00
                                                     -1.000e-04
                                                                       0.000e+00
                                                                                         0.000e+00
                                                                                                          0.000e+00
                 8.861e-03
                                   -6.667e-05
                                                     0.000e+00
                                                                       2.128e-03
                                                                                         0.000e+00
                                                                                                          0.000e+00
 .000e+00
                 -6.667e-05
                                   3.613e-03
                                                     -2.128e-04
                                                                       0.000e+00
                                                                                         -3.030e-03
                                                                                                          0.000e+00
                                                                                                                             0.000e+00
1.000e-04
                 0.000e+00
                                   -2.128e-04
                                                     1.783e-03
                                                                       0.000e+00
                                                                                         0.000e+00
                                                                                                          -1.471e-03
                                                                                                                             0.000e+00
                                                                      6.773e-03
-1.000e-04
 .000e+00
                 -2.128e-03
                                   0.000e+00
                                                     0.000e+00
                                                                                         -1.000e-04
                                                                                                           -4.545e-03
                                                                                                                             0.000e+00
 .000e+00
                 0.000e+00
                                   -3.030e-03
                                                     0.000e+00
                                                                                         4.130e-03
                                                                                                           -1.000e-03
                                                                                                                             0.000e+00
 .000e+00
                 0.000e+00
                                   0.000e+00
                                                     -1.471e-03
                                                                       -4.545e-03
                                                                                         -1.000e-03
                                                                                                          7.016e-03
                                                                                                                             0.000e+00
Solution Hx=b, using Cholesky decomposition on matrix H
x1 = 8.080e-01
  = 1.154e+01
   = 7.539e+00
     8.888e+00
     1.021e+01
     8.111e+00
     9.632e+00
```

Figure 5: Results of my linear solver.

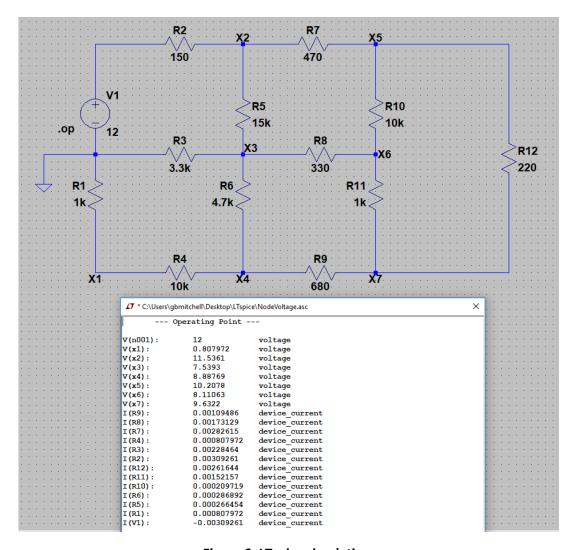


Figure 6: LTspice simulation.

The second example of linear solvers in electrical engineering is loop (mesh) current analysis of resistor circuits. Complex resistive circuits form a linear system of n equations and n unknowns. The following is an example to illustrate using a linear solver to analyze the loop currents in a complex resistor circuit. The circuit has a 12VDC power source and a common reference at the negative side of the power source. Each mesh in the circuit, shown in figure 1, will have an associated loop current. The loop currents labeled X1 through X5 are unknown and we can form a linear system to compute the unknown currents. The system will be five equations and five unknowns and can be derived using Kirchhoff's voltage Law which states that all voltages in a mesh loop must sum to zero. See figure 7 and 8 for the resistor circuit and derived equations for the linear system to solve. At the bottom of figure 8 are variable name equalities defined for comparison with the results from my linear solving routine and the results from simulating the circuit in LTspice. The derived loop current equations are put in matrix form and augmented with the known values forming the linear problem Px=b where x is a vector of unknowns to solve for. The results from my programed linear solver are shown in figure 9, the results of my linear solver can also be viewed in homework problem 10. For comparison, the LTspice simulator results are shown in figure 10.

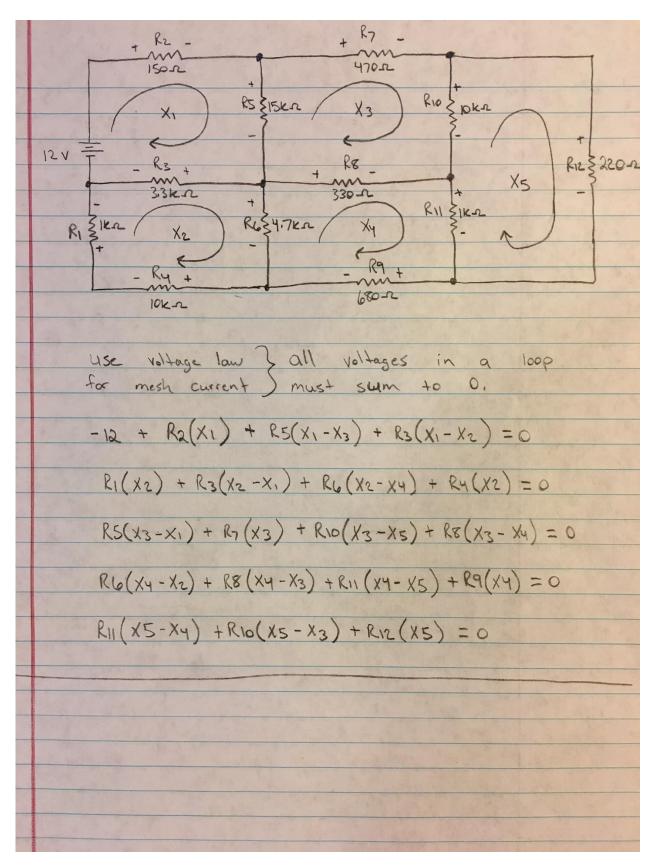


Figure 7: Resistor circuit and loop current equations.

```
(R_2 + R_5 + R_3)X_1 - (R_3)X_2 - (R_5)X_3 = 12
 (RI+R3+ R4+R6)X2-(R3)X,-(R6)X4 = 0
(R5+R7+R8+R10)X3-(R5)X1-(R10)X5-(R8)X4 =0
(R6+ R8+ R11+ R9) X4-(R6) X2-(R8) X3-(R11) X5 = 0
(R11+R10+R12) X5-(R11) X4-(R10) X3 = 0
18450 X1 - 3300 X2 - 15000 X3 = 12
-3300 X1 + 19000 X2 - 4700 X4 = 0
- 15000 x, + 25800 X3 - 330 X4 - 10000 X5 =0
- 4700 X2 - 330 X3 + 6710 X4 - 1000 X5 = 0
- 10000 X3 - 1000 X4 + 11220 X5 =0
 X_1 = I(R_2)
 X_2 = I(R_1) = I(R_4)
 X3 = I(R_7)
 X4 = I(R9)
X5 = I (R12)
```

Figure 8: Loop current equations and variable equalities.

```
Augmented matrix P =
1.845e+04
                 -3.300e+03
                                 -1.500e+04
                                                  0.000e+00
                                                                   0.000e+00
                                                                                    1.200e+01
-3.300e+03
                                 0.000e+00
                                                  -4.700e+03
                                                                   0.000e+00
                                                                                     0.000e+00
                1.900e+04
-1.500e+04
                                 2.580e+04
                                                                   -1.000e+04
                                                                                     0.000e+00
                0.000e+00
                                                  -3.300e+02
0.000e+00
                -4.700e+03
                                 -3.300e+02
                                                  6.710e+03
                                                                   -1.000e+03
                                                                                     0.000e+00
0.000e+00
                0.000e+00
                                 -1.000e+04
                                                  -1.000e+03
                                                                   1.122e+04
                                                                                    0.000e+00
Solution Px=b, using Cholesky decomposition on matrix P
x1 = 3.093e-03
x2 = 8.080e-04
x3 = 2.826e-03
x4 = 1.095e - 03
  = 2.616e-03
```

Figure 9: Results of my linear solver.

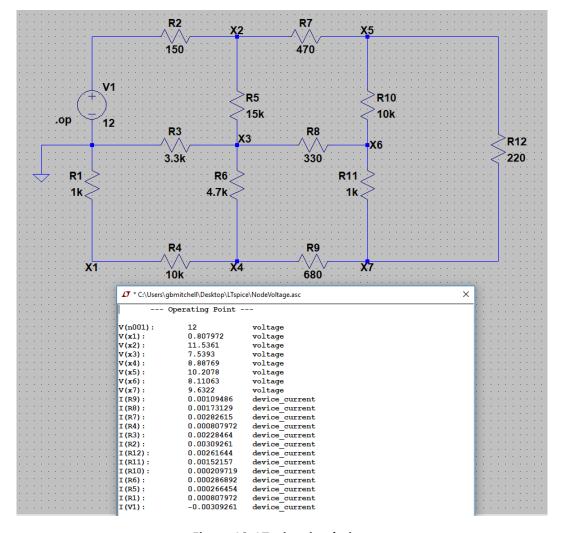


Figure 10: LTspice simulation.