Learning to Generate Textual Data

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Abstract

To learn text understanding models with millions of parameters, one needs a massive amount of data. We argue that generating data can compensate for this need for large datasets. While defining generic data generators is tricky, we propose to allow these generators to be "weakly" specified, letting the undetermined coefficients be learned from data. We derive an efficient algorithm called GENERE that jointly estimates the parameters of the model and the undetermined sampling coefficients. We illustrate its benefits by learning to solve math exam questions using a highly parametrized sequence-to-sequence neural network.

1 Introduction

Many tasks require a large amount of background knowledge to be solved efficiently, but acquiring a huge amount of data is costly, both in terms of time and money. In several situations, a human trainer can specify domain knowledge by providing a generator of virtual data, such as a negative data sampler for implicit feedback in recommendation systems, physical 3D rendering engines as a simulator of data in a computer vision system, simulators of physical processes to solve science exam question, and math problem generators for the automatic solving of math problems. Domain-specific data simulators can generate an arbitrary amount of data, that can be treated exactly the same way as standard observations, but since they are virtual, they can also be seen as regularizers dedicated to the task we want to solve (Scholkopf and Smola, 2001). While simple, the idea of data simulation is powerful and can lead to significantly better estimations of a predictive model because it prevents overfitting. At the same time it is subject to a strong model bias, because such data generators often generate data that is different from the observed data.

Creating virtual samples is strongly linked to transfer learning when the task to transfer is correlated to the objective (Pan and Yang, 2010). The computer vision literature adopted this idea very early through the notion of *virtual samples*, which have a natural interpretation: by creating artificial perturbations of an image, its semantics is likely to be unchanged, i.e. training samples can be rotated, blurred, or slightly cropped without changing the category of the objects contained in the image (Niyogi et al., 1998).

However, for natural language applications, this idea of creating invariant transformations is difficult to apply directly, as simple meaning-preserving transformations, such as the replacement of words by their synonyms or active-passive verb transformations, are quite limited. More advanced meaning-preserving transformations would require an already good model that understands natural language. Another option more targeted to textual applications is to build top-down generators, such as probabilistic grammars, with a much wider coverage of linguistic phenomena. This way of being able to leverage many years of research in computational linguistics to create good data generators would be a natural and useful reuse of scientific knowledge, and better

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than blindly believing in the current trend of "data takes all".

While the idea of generating data is straightforward, one could argue that it may be difficult to come up with good generators. What we mean by a good generator is the ability to help predicting test data when the model is trained on the generated data. In this paper, we will show several types of generators, some contributing more than others in their ability to generalize to unseen data. In fact, finding good generators is more difficult than one might initially expect: should we generate data by modifying existing training samples, or "go wild" and derive a full probabilistic context-free grammar that could possibly generate unnatural examples and add noise to the estimator? While we do not arrive at a specific framework to build programs that generate virtual data, we assume in this work that a domain expert can easily write a program in her own programming language, leaving some generation parameters unspecified. In our approach these unspecified parameters are automatically learned from the data, by selecting the ones most compatible with the model. More precisely, we assume that the correct parameters are the ones for which the data generator gives on average the smallest penalty to the likelihood. Learning generative models discriminatively (Petrov and Klein, 2007) would be an alternative to our approach that could be more practical as it decouples the definition of the prediction model from the structural biases that we want to impose trough generative regularization.

In the next section, we introduce GENERE, a generic algorithm that extends any gradient-based learning approach with a data generator that can be tuned while learning the model on the training data using stochastic optimization. In Section 2.2, we show how GENERE can be adapted to handle a (possibly non-differentiable) black-box sampler without requiring modifications to it. We also illustrate how this framework can be implemented in practice for a specific use case: the automatic solving of math exam problems. Further discussion is given in the concluding section.

2 Regularization Based on a Generative Model

As with any machine learning approach, we assume that given the realisation of a variable $x \in \mathcal{X}$ representing the input, we want to predict the distribution of a variable $y \in \mathcal{Y}$ representing the output. The goal is to find this predictive distribution by learning it from examples $\mathcal{D} := \{(x_i, y_i)\}_{i=1}^n$.

Building on the current success in the application of deep learning to NLP, we assume that there exists a good model family $\{f_\theta, \theta \in \Theta\}$ to predict y given x, where θ is an element of the parameter space Θ. For example, the stacked LSTM encoder-decoder is a general purpose model that has helped to improve results on relatively complex tasks, such as machine translation (Sutskever et al., 2014), syntactic parsing (Vinyals et al., 2014), semantic parsing (Dong and Lapata, 2016) and textual entailment (Rocktäschel et al., 2016).

For many applications, the amount of training data is too small or too costly to acquire. We hence look for alternative ways to regularize the model so that we can achieve good performance using few data points. One way is to use surrogate tasks in a transfer learning framework, but finding these surrogate tasks is sometimes difficult. Another way is to use domain knowledge that can partially explain the data.

Let $p_\theta(y|x)$ be the target prediction model. Given the training dataset $\mathcal{D}$, the penalized maximum likelihood estimator is obtained by $\min_{\theta\in\Theta} \mathcal{L}(\theta)$ where:

$$\mathcal{L}(\theta) := \ell(\theta) + \lambda\Omega(\theta) \ . \tag{1}$$

where $\ell(\theta) := -\sum_{i=1}^n \log p_\theta(y_i|x_i) = P$ is the negative log-likelihood. Here, $\Omega(\theta)$ is a regularizer that prevents over-fitting, $\lambda \in \mathbb{R}$ the regularization parameter that can be set by cross-validation, and $\hat{P}$ is the empirical distribution. Instead of using a standard regularizer, such as the squared norm or the Lasso penalty which are domain-agnostic, we propose in this paper to use a generative model to regularize the estimator.

Domain knowledge A natural way to inject background information is to define a generative model that simulates the way the data is generated. In text understanding applications, such generative mod-

els are common and include probabilistic context-free grammars (PCFG) and natural language generation frameworks (e.g. SimpleNLG (Gatt and Reiter, 2009)). Let $P_\gamma(x, y)$ be such a generative model parametrized by a continuous parameter vector $\gamma \in \Gamma$, such as the concatenation of all the parameters of the production rules in a PCFG. One important difference between the discriminative and the generative probability distributions is that the inference problem of y given x might be intractable[1] for the generative model, even if the joint model can be computed efficiently.

In this work, we use the following regularizer:

$$\Omega(\theta) \quad := \quad \min_{\gamma \in \Gamma} \mathbb{E}_{P_\gamma(x,y)} \left[\log \left(\frac{P_\gamma(y|x)}{p_\theta(y|x)} \right) \right] \quad (2)$$

This regularizer makes intuitive sense as it corresponds to the smallest possible Kullback-Leibler divergence between the generative and discriminative models. We can see that if the generator p_γ is close to the distribution that generates the test data, the method can potentially yield good performance. However, in practice, γ is unknown and difficult to set. In this work, we focus on several techniques that can be used to estimate the generative parameter vector γ on the training data, making the regularizer data-dependent.

Minimizing the objective from Equation (1) is equivalent to minimize the following function over $\Theta \times \Gamma$:

$$\mathcal{L}(\theta, \gamma) \quad := \quad \ell(\theta) + \lambda \mathbb{E}_{P_\gamma(x,y)} \left[\log \left(\frac{p_\gamma(y|x)}{p_\theta(y|x)} \right) \right] \quad .$$

This estimator is called GENERE for *Generative Regularization* and can be viewed as a Generative-Discriminative Tradeoff estimator (GDT (Bouchard and Triggs, 2004)) that smoothly interpolates between a purely un-regularized discriminative model when $\lambda = 0$ and a generative model when λ tends to infinity. Note that when there is no regularization, the sampling parameters γ do not need to be estimated as the objective function does not depend on them.

[1]Even if tractable, the inference can be very costly: for example, PCFG decoding can be done using dynamic programming and has a cubic complexity in the length of the decoded sentence, which is still too high for some applications with long sentences.

2.1 The GENERE Algorithm

The objective $\mathcal{L}(\theta, \gamma)$ can also be written as an expectation under a mixture distribution $\tilde{P}_\gamma := \frac{1}{1+\lambda}\hat{P} + \frac{\lambda}{1+\lambda}P_\gamma$. The two components of this mixture are the empirical data distribution $\hat{P}$ and the generation distribution P_γ. The final objective is penalized by the entropy of the the generation $\mathcal{H}(\gamma) := \mathbb{E}_{P_\gamma}[\log p_\gamma(y|x)]$:

$$\mathcal{L}(\theta, \gamma) = -(1+\lambda)\mathbb{E}_{\tilde{P}_\gamma}[\log p_\theta(y|x)] - \lambda \mathcal{H}(\gamma) \ . \quad (3)$$

This can be minimized using stochastic gradient descent by sampling real data or generated data according to the proportions $\frac{1}{1+\lambda}$ and $\frac{\lambda}{1+\lambda}$, respectively. The pseudocode is provided in Algorithm 1. It can be viewed as a variant of the REINFORCE algorithm which is commonly used in Reinforcement Learning (Williams, 1988) using the policy gradient. It is straightforward to verify that at each iteration, GENERE computes a noisy estimate of the exact gradient of the objective function $\mathcal{L}(\theta, \gamma)$ with respect to both parameter vectors θ and γ.

An important quantities introduced in Algorithm 1 is the baseline quantity μ, that approximates the average log-likelihood of a point sampled according to $\tilde{P}_\gamma$. Since it is unknown in general, an average estimate is obtained using a geometric averaging scheme with a coefficient α, that is typically set to 0.98.

Algorithm 1 The GENERE Algorithm

Require: $\hat{P}$: real data sampler
Require: P_γ: parametric data generator
Require: λ: generative regularization strength
Require: η: learning rate
Require: α: baseline smoothing coefficient

1: Initialize parameters θ, sampling coefficients γ and baseline μ
2: **for** $t = 1, 2, \cdots$ **do**
3: $\quad x, y \sim \frac{1}{1+\lambda}\hat{P} + \frac{\lambda}{1+\lambda}P_\gamma$
4: $\quad g_\theta \leftarrow \nabla_\theta \log p_\theta(y|x)$
5: $\quad g_\gamma \leftarrow (\log p_\theta(y|x) - \mu) \nabla \log p_\gamma(x, y)$
6: $\quad (\theta, \gamma) \leftarrow (\theta, \gamma) - \eta(g_\theta, g_\gamma)$
7: $\quad \mu \leftarrow \alpha\mu + (1-\alpha) \log p_\theta(y|x)$
8: **end for**

Generative modeling is natural because we can consider latent variables that add interpretable

meaning to the different components of the model. For example, in NLP we can define the latent variable as being the relations that are mentioned in the sentence.

We could consider two main types of approaches to choose a good latent variable:

- Discrete data structure: we can use efficient algorithms, such as dynamic programming to perform sampling and which can propagate the gradient
- Continuous distribution: having a continuous latent variable enables easy handling of correlations across different parts of the model.

It is often laborious to design data generators which can return the probability of the samples it generates, as well as the gradient of this probability with respect to the input parameters γ. In the next section, we show how to alleviate this constraint by allowing any data-generating code to be used with nearly no modification.

2.2 GENERE with a Black Box Sampler

Let us assume the data generator is a black box that takes a K-dimensional seed vector as input and outputs an input-output sample x, y. To enable GENERE to be applied without having to modify the code of data generators, we used the following data generation process:

1. Sample a Gaussian seed vector $\Delta \sim \mathcal{N}(0, I)$
2. Use the data generator G_z with seed value $z := \Delta+\gamma$ to generate an input-output sample (x, y).

This two-step generation procedure enables the gradient information to be computed using the density of a Gaussian distribution. The use of a standardized centered variable for the seed is justified by the fact that the parametrization of G_z takes into account possible shifts and rescaling. Formally, this is equivalent to Algorithm 1 with the following generative model:

$$p_\gamma(x, y) = \mathbb{E}_{\Delta\sim\mathcal{N}(0,I)}\left[g_{\gamma+\Delta}(x, y)\right] \quad (4)$$

where g_z is the density of the black-box data generator G_z for the seed value $z \in \mathbb{R}^K$. Ideally, the second data generator that takes z as an input and generates the input/output pair (x, y) should be close to a deterministic function in order to allocate more uncertainty in the trainable part of the model which corresponds to the Gaussian distribution.[2]

Learning The pseudo-code for the Black Box GENERE variant is shown in Algorithm 2. It is basically the same as Algorithm 1, but where the sampling phase is decomposed into the two steps: A random Gaussian variable sampling followed by the black box sampling of generators.

Algorithm 2 Black Box GENERE

Require: $\hat{P}$: real data sampler
Require: $G(\gamma)$: black box data generator
Require: λ: generative regularization strength
Require: η_γ, η_θ: learning rates
Initialize parameters θ, sampling coefficients γ and baseline μ
for $t = 1, 2, \cdots$ **do**
  if $\frac{1}{1+\lambda} > \mathcal{U}([0, 1])$ **then**
    $x, y \sim \hat{P}$
  else
    $\Delta \sim \mathcal{N}(\mathbf{0}, I)$
    $x, y \sim G_{\gamma+\Delta}$
    $\gamma \leftarrow \gamma - \eta_\gamma(\log p_\theta(y|x) - \mu)\Delta$
  end if
  $\theta \leftarrow \theta - \eta_\theta \nabla_\theta \log p_\theta(y|x)$
  $\mu \leftarrow \alpha\mu + (1 - \alpha) \log p_\theta(y|x)$
end for

3 Application to Encoder-Decoder

In this section, we show that the GENERE algorithm is well suited to tune data generators for problems that are compatible with the encoder-decoder architecture commonly used in NLP.

3.1 Mixture-based Generators

In the experiments below, we consider mixture-based generators with known components but unknown mixture proportions. Formally, we parametrize the proportions using a softmax link $\sigma(t) := \exp(t_k)/\sum_{k'=1}^{K}\exp(t_{k'})$. In other words,

[2] What we mean by deterministic is that the black-box sampler has the form $\delta\{f(\Delta+\gamma) = (x, y)\}$, where δ is the indicator function.

the data generator distribution is:

$$p_\gamma(x, y) = \sum_{k=1}^{K} \sigma_k(\gamma + \Delta) p_k(x, y),$$

where $p_k(x, y)$ are data distributions, called *base generators*, that are provided by domain experts, and Δ is a K-dimensional centered Gaussian with an identity covariance matrix. This class of generator makes sense in practice, as we typically build multiple base generators $p_k(x, y)$, $k = 1, \cdots, K$, without knowing ahead of time which one is the most relevant. Then, the training data is used by the GENERE algorithm to automatically learn the optimal parameter γ that controls the contribution $\{\pi_k\}_{k=1}^K$ of each of the of the base generators, equal to $\pi_k := \mathbb{E}_{\Delta \sim \mathcal{N}(\mathbf{0}, I)} [\sigma_k(\gamma + \Delta)]$.

3.2 Synthetic Experiment

In this section, we illustrate how GENERE can learn to identify the correct generator, when the data generating family is a mixture of multiple data generators and only one of these distributions – say p_1 – has been used to generate the data. The other distributions $(p_2, \cdots, p_K)$ are generating input-output data samples (x, y) with different distributions.

We verified that the algorithm correctly identifies the correct data distribution, and hence leads to better generalization performances than what the model learns without the generator.

In this illustrative experiment, a simple text-to-equation translation problem is created, where inputs are sentences describing an equation such as "compute one plus three minus two", and outputs are symbolic equations, such as "X = 1 + 3 - 2". Numbers were varying between -20 and 20, and equations could have 2 or 3 numbers with 2 or 3 operations.

As our model, we used a 20-dimensional sequence-to-sequence model with LSTM recurrent units. The model was initialized using 200 iterations of standard gradient descent on the log-probability of the output. GENERE was run for 500 iterations, varying the fraction of real and generated samples from 0% to 100%. A ℓ_2 regularization of magnitude 0.1 was applied to the model. The baseline smoothing coefficient was set to 0.98 and the shrinkage parameter was set to 0.99. All the experiments were repeated 10 times and a constant learning rate of 0.1 was used.

Results are shown on Figure 1, where the average loss computed on the test data is plotted against the fraction of real data used during learning.

We can see that the best generalization performance is obtained when there is a balanced mix of real and artificial data, but the proportion depends on the amount of training data: on the left hand side, the best performance is obtained with generated data only, meaning that the number of training samples is so small that GENERE only used the training data to select the best base generator (the component p_1), and the best performance is attained using only generated data. The plot on the right hand side is interesting because it contains more training data, and the best performance is not obtained using only the generator, but with 40% of the real data, illustrating the fact that it is beneficial to jointly use real and simulated data during training.

3.3 Math word problems

To illustrate the benefit of using generative regularization, we considered a class of real world problems for which obtaining data is costly: learning to answer math exam problems. Prior work on this problem focuses on standard math problems given to students aged between 8 and 10, such as the following:[3]

> For Halloween Sarah received 66 pieces of candy from neighbors and 15 pieces from her older sister. If she only ate 9 pieces a day, how long would the candy last her?

The answer is given by the following equation:

$$\mathrm{X} = (66 + 15)/9 \ .$$

Note that similarly to real world school exams, giving the final answer of (9 in this case) is not considered to be enough for the response to be correct.

The only publicly available word problem datasets we are aware of contain between 400 and 600 problems (see Table 2), which is not enough to properly train sufficiently rich models that capture the link between the words and the quantities involved in the problem.

[3] From the Common Core dataset (Roy and Roth, 2015)

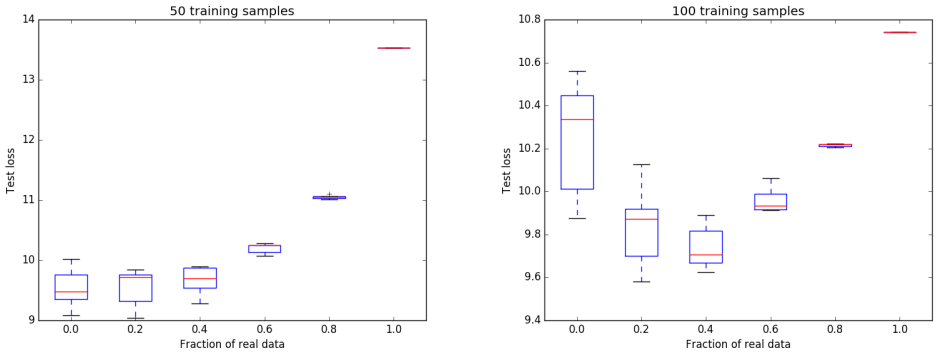

Figure 1: Test loss vs. fraction of real data used in GENERE on the text-to-equation experiment.

Sequence-to-sequence learning is the task of predicting an output sequence of symbols based on a sequence of input symbols. It is tempting to cast the problem of answering math exams as a sequence-to-sequence problem: given the sequence of words from the problem description, we can predict the sequence of symbols for the equation as output. The most successful models for sequence prediction are Recurrent Neural Nets (RNN) with non-linear transitions between states.

Treated as a translation problem, math word problem solving should be simpler than developing a machine translation model between two human languages, as the output vocabulary (the math symbols) is significantly smaller than any human vocabulary. However, machine translation can be learned on millions of pairs of already translated sentences, and such massive training datasets dwarf all previously introduced math exam datasets. Today, standard repositories are restricted to a few hundreds of problems with their solutions (Hosseini et al., 2014; Roy et al., 2015; Roy and Roth, 2015).

We used standard benchmark data from the literature. The first one, AI2, was introduced by Hosseini et al. (2014) and covers addition and subtraction of one or two variables or two additions scraped from two web pages. The second (IL), introduced by Roy et al. (2015), contains single operator questions but covers addition, subtraction, multiplication, and division, and was also obtained from two, although different from AI2, web pages. The last data set (CC) was introduced by Roy and Roth (2015) to cover combinations of different operators and was obtained from a fifth web page.

AI2	IL	CC
$X + Y$	$X + Y$	$X + Y - Z$
$X + Y + Z$	$X - Y$	$X * (Y + Z)$
$X - Y$	$X * Y$	$X * (Y - Z)$
	X/Y	$(X + Y)/Z$
		$(X - Y)/Z$

Table 1: Patterns of the equations seen in the datasets for one permutation of the placeholders.

	AI2	IL	CC
Train	198	214	300
Dev	66	108	100
Test	131	240	200
Total	395	562	600

Table 2: Math word problems dataset sizes.

An overview of the equation patterns in the data is shown in Table 1. It should be noted that there are sometimes numbers mentioned in the problem description that are not used in the equation.

As there are no available train/dev/test splits in the literature we introduced such splits for all three data sets. For AI2 and CC, we simply split the data randomly and for IL we opted to maintain the clusters described in Roy and Roth (2015). We then used the implementation of Roy and Roth (2015) provided by the authors, which is the current state-of-the-art for all three data sets, to obtain results to compare our model against. The resulting data sizes are shown on Table 2. We verified that there are no duplicate problems, and our splits and a fork of the baseline implementation are available online.[4]

[4] https://github.com/ninjin/roy_and_roth_2015

John sprints to William's apartment. The distance is 32 yards from John's apartment to William's apartment. It takes John 2 hours to at the end get there. How fast did John go?	32 / 2
Sandra has 7 erasers. She grasps 7 more. The following day she grasps 18 whistles at the local supermarket. How many erasers does Sandra have in all?	7 + 7
A pet store had 81 puppies In one day they sold 41 of them and put the rest into cages with 8 in each cage. How many cages did they use?	(81 - 41) / 8
S1 V1 Q1 O1 C1 S1(pronoun) V2 Q2 of O1(pronoun) and V2 the rest into O3(plural) with Q3 in each O3. How many O3(plural) V3?	(Q1 - Q2) / Q3

Table 3: Examples of generated sentences (first 3 rows). The last row is the template used to generate the 3rd example where brackets indicate modifiers, symbols starting with 'S' or 'O' indicate a noun phrase for a subject or object, symbols with 'V' indicate a verb phrase, and symbols with 'Q' indicate a quantity. They are identified with a number to match multiple instances of the same token.

3.4 Development of the Generator

Generators were organized as a set of 8 base generators p_k, summarized in Table 4. Each base generator has several functions associated with it. The functions were written by a human, over 3 days of full-time development. The first group of base generators is only based on the type of symbol the equation has, the second group is the pair (#1, #2) to represent equations with one or two symbols. Finally, the last two generators are more experimental as they correspond to simple modifications applied to the available training data. The Noise 'N' generator picks one or two random words from a training sample to create a new (but very similar) problem. Finally, the 'P' generator is based on computing the statistics of the words for the same question pattern (as one can see in Table 1), and generates data using simple biased word samples, where words are distributed according to their average positions in the training data (positions are computed relatively to the quantities appearing in the text, i.e. "before the first number", "between the 1st and the 2nd number", etc.).

3.5 Implementation Details

We use a standard stacked RNN encoder-decoder (Sutskever et al., 2014), where we varied the recurrent unit between LSTM and GRU (Cho et al., 2014), stack depth from 1 to 3, the size of the hidden states from 4 to 512, and the vocabulary threshold size. As input to the encoder, we downloaded pre-trained 300-dimensional embeddings trained on Google News data using the word2vec software (Mikolov et al., 2013). The development data was used to tune these parameters

	The problem...
+	contains at least one addition
-	contains at least one subtraction
*	contains at least one multiplication
/	contains at least one division
1	has a single mathematical operation
2	has a couple of mathematical operations
N	is a training sample with words removed
P	is based on word position frequencies

Table 4: The base generators to create math exam problems.

before performing the evaluation on the test set. We obtained the best performances with a single stack, GRU units, and a hidden state size of 256.

The optimization algorithm was based on stochastic gradient descent using Adam as an adaptive step size scheme (Kingma and Ba, 2014), with mini-batches of size 32. A total of 256 epochs over the data was used in all the experiments.

To evaluate the benefit of learning the data generator, we used a hybrid method as a baseline where a fraction of the data is real and another fraction is generated using the default parameters of the generators (i.e. a uniform distribution over all the base

	AI2	IL	CC	Avg.
RR2015	82.4	75.4	55.5	71.1
100% Data	72.5	53.7	95.0	73.7
100% Gen	60.3	51.2	92.0	67.8
85%Gen + 15%Data	74.0	55.4	97.5	75.6
GENERE	77.9	56.7	98.5	77.7

Table 5: Test accuracies of the math-exam methods on the available datasets averaged over 10 random runs.

generators). The optimal value for this fraction obtained on the development set was 15% real data, 85% generated data. For GENERE, we used a fixed size learning rate of 0.1, the smoothing coefficient was selected to be 0.5, and the shrinkage coefficient to be 0.99.

We also compared our approach to the publicly available math exam solver RR2015 (Roy and Roth, 2015). This method is based on a combination of template-based features and categorizers. The accuracy performance was measured by counting the number of times the equation generated the correct results, so that 10 + 7 and 7 + 10 would both be considered to be correct. Results are shown on Table 5.

We can see that there is a large difference in performance between RR2015 and the RNN-based encoder-decoder approach. While their method seems to be very good on some datasets, it fails on CC, which is the dataset in which one needs two equations involving parentheses. On average, the trend is the following: using data only does not succeed in giving good results, and we can see that with generated data we are performing better already. This could be explained by the fact that the generators' vocabulary has a good overlap with the vocabulary of the real data. However, mixing real and generated data improves performance significantly. When GENERE is used, the sampling is tuned to the problem at hand and give better generalization performance.

To understand if GENERE learned a meaningful data generator, we inspected the coefficients $\gamma_1, \cdots, \gamma_8$ that are used to select the 8 data generators described earlier. This is shown is Figure 2.

The results are quite surprising at first sight: the AI2 dataset only involves additions and subtractions, but GENERE selects the generator generating divisions as the most important. Investigating, we noted that problems generated by the division generator were reusing some lexical items that were present in AI2, making the vocabulary very close to the problems in AI2, even if it does not cover division. We can also note that the differences in proportions are quite small among the 4 symbols $+, -, *$ and $/$ across all the datasets. We can also clearly see that the noisy generator 'N' and 'P' are not very relevant in general. We explain this by the fact that the noise induced by these generators is too artificial to generate relevant data for training. Their likelihood on the model trained on real data remains small.

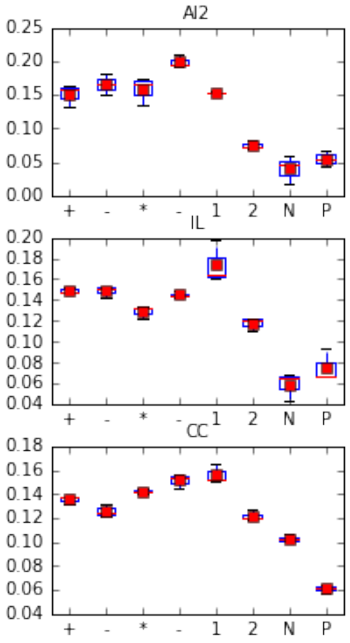

Figure 2: Base generators proportions learned by GENERE.

4 Conclusion

In this work, we argued that many problems can be solved by high-capacity discriminative probabilistic models, such as deep neural nets, at the expense of a large amount of required training data. Unlike the current trend which is to reduce the size of the model, or to define features well targeted for the task, we showed that we can completely decouple the choice of the model and the design of a data generator. We proposed to allow data generators to be "weakly" specified, leaving the undetermined coefficients to be learned from data. We derived an efficient algorithm called GENERE, that jointly estimates the parameters of the model and the undetermined sampling coefficients, removing the need for costly cross-validation. While this procedure could be viewed as a generic way of building informative priors, it does not rely on a complex integration procedure such as Bayesian optimization, but corresponds to a simple modification of the standard stochastic optimization algorithms, where the sampling alternates between the use of real and generated data. While the general framework assumes

that the sampling distribution is differentiable with respect to its learnable parameters, we proposed a Gaussian integration trick that does not require the data generator to be differentiable, enabling practitioners to use *any* data sampling code, as long as the generated data resembles the real data.

We also showed in the experiments, that a simple way to parametrize a data generator is to use a mixture of base generators, that might have been derived independently. The GENERE algorithm learns automatically the relative weights of these base generators, while optimizing the original model. While the experiments only focused on sequence-to-sequence decoding, our preliminary experiments with other high-capacity deep neural nets seem promising.

Another future work direction is to derive efficient mechanisms to guide the humans that are creating the data generation programs. Indeed, there is a lack of generic methodology to understand where to start and which training data to use as inspiration to create generators that generalize well to unseen data.

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