INSTITUTO TECNOLÓGICO DE AERONÁUTICA



Gabriel Barbosa Martinz

USE OF GENERATIVE NEURAL NETWORKS FOR INSTANCE SPACE CODIFICATION AND GENERATION OF DATA WITH SPECIFIC PROPERTIES

Final Paper 2023

Course of Computer Engineering

Gabriel Barbosa Martinz

USE OF GENERATIVE NEURAL NETWORKS FOR INSTANCE SPACE CODIFICATION AND GENERATION OF DATA WITH SPECIFIC PROPERTIES

Advisor

Prof^a. Dr^a. Ana Carolina Lorena (ITA)

COMPUTER ENGINEERING

São José dos Campos Instituto Tecnológico de Aeronáutica

Cataloging-in Publication Data

Documentation and Information Division

Barbosa Martinz, Gabriel

Use of generative neural networks for instance space codification and generation of data with specific properties / Gabriel Barbosa Martinz.

São José dos Campos, 2023.

Final paper (Undergraduation study) - Course of Computer Engineering- Instituto Tecnológico de Aeronáutica, 2023. Advisor: Profa. Dra. Ana Carolina Lorena.

1. Neural networks. 2. Instance space. 3. GAN. I. Instituto Tecnológico de Aeronáutica. II. Title.

BIBLIOGRAPHIC REFERENCE

BARBOSA MARTINZ, Gabriel. Use of generative neural networks for instance space codification and generation of data with specific properties. 2023. 33f. Final paper (Undergraduation study) – Instituto Tecnológico de Aeronáutica, São José dos Campos.

CESSION OF RIGHTS

AUTHOR'S NAME: Gabriel Barbosa Martinz

PUBLICATION TITLE: Use of generative neural networks for instance space codification

and generation of data with specific properties.

PUBLICATION KIND/YEAR: Final paper (Undergraduation study) / 2023

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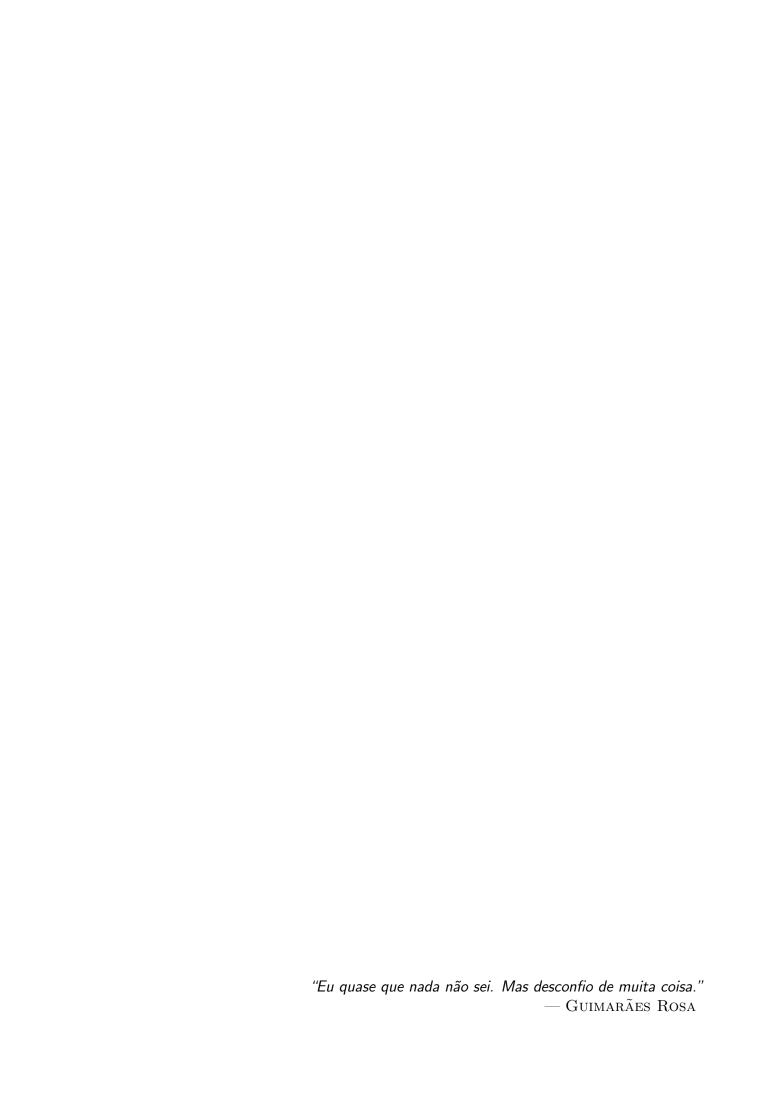
USE OF GENERATIVE NEURAL NETWORKS FOR INSTANCE SPACE CODIFICATION AND GENERATION OF DATA WITH SPECIFIC PROPERTIES

This pu	blication	was ac	cepted	like I	Final	Work	of Und	ergradı	ation	Study
•			Gabri	el Bai	rbosa	Marti	nz			
					thor					
				Au	tillor					
			Ana Ca	arolina	a Lor	ena (I'	ΓΑ)			
				Ad	visor					

Prof. Dr. Marcos Máximo Course Coordinator of Computer Engineering

Acknowledgments

To my parents, Michelle and Raimundo, for always supporting me in my academic journey. To my advisor, Prof. Ana Carolina Lorena for the guidance provided over this research. To my beloved Vitória, for the love and emotional support she gives to me. To my roommates over these years for being great friends. To the friends I've made when at ITA and before it for helping me and making my undergraduate journey more fun. To all the amazing professors I had over my undergraduate studies for shaping my interests in engineering.



Abstract

One topic of study in Machine Learning is the study of algorithmic performance and which methodologies may be used to assess this performance. A methodology known as Instance Space Analysis has been used to relate predictive performance in classification algorithms to instance hardness (how hard an instance is for an algorithm to classify). The original methodology has been defined with the instance being an entire dataset, but further work has been made to make the instance as fine-grained as an individual observation. In this work we will build upon this methodology and we propose the creation of a generative neural network model to generate new observations for a classification algorithm with predefined hardness properties.

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1 Introduction

1.1 Motivation

Often in a problem being tackled with Machine Learning (ML) techniques one of the most important part of the solving process is the algorithm selection. Each algorithm has a specific bias which makes it more suitable for some classes of problems than others (ADAM et al., 2019).

It is desirable, then, that we may have a way of measuring the relationship of the performance of a given algorithm in a problem with the problem's characteristics, since knowing which data is easy or difficult for a given model to classify is useful in the way that we may make changes to the original model.

Muñoz et al. (2018) has introduced a methodology called Instance Space Analysis (ISA), a novel way of performance evaluation and algorithm selection in classification problems by mapping the statistical properties of an instance (an entire dataset) into how difficult the instance is for the classification algorithm to perform. Further, in Paiva et al. (2022), the methodology has been modified to have a more fine-grained analysis, with the instance being reduced to an individual observation in a classification dataset.

Given this, we can map each observation into a hardness level. But one feature of the ISA not investigated in the instance-level proposal of Paiva *et al.* (2022) is how to generate new problem instances with desired characteristics in order to expand the dataset with instances that may defy the classification techniques. This project aims to fill this gap.

One type of model that may give us this feature from this data is a neural network that encodes the data into the instance space and decodes from it. Using this approach, we can then generate data in a region of the instance space and use the decoding part of the network to infer a reconstruction of the original data and find difficulty metrics from it, as well as be able to challenge the classification techniques at different levels. We can use this to verify how the original model behaves with data with a given instance space profile or to challenge the model, such as generating adversarial examples (YUAN et al., 2019).

1.2 Objective

This work's objective lies in providing a framework for data generation based on the instance space generated for the data and monitor the original model's behaviour using the generated data.

1.3 Scope

The scope of this work will be limited to exploring an encoder-decoder implementation for the generation of data. The modelling will be made entirely using Python, with the PyTorch (PASZKE et al., 2019) framework. PyHard (PAIVA et al., 2022) will be used for reproducing the ISA methodology.

1.4 Outline of this work

The document is organized as follows:

- Chapter 2 introduces some Machine Learning terminology and describes the encoder and decoder neural network models;
- Chapter 3 describes the ISA framework;
- Chapter 4 presents the methodology to be followed in the computational experiments;
- Chapter 5 concludes the work presenting future activities and a work schedule.

2 Machine Learning

This chapter will introduce Machine Learning (ML) concepts and techniques being explored in this work, namely the classification problem, feature learning, neural networks and encoder and decoder neural networks.

2.1 Classification

In Statistics and Machine Learning, a problem is defined as a classification problem when it consists in identifying to which categories a member of a population belongs to. An example might be identifying which race of domestic cat is shown in a picture containing a cat (KOLLA, 2020). An algorithm that implements classification is known as a classifier. The classifier works by analysing each observation into dependent variables and either mapping those to the categories or by comparing each observation to previous observations by means of a similarity function or loss function (FACELI et al., 2021).

Terminology between Statistics and Machine Learning tend to differ. In this work, we will be using the terminology found in Machine Learning, namely:

- dependent variables are called features;
- categories are called classes;

In this work, we will not focus on a specific classification algorithm since ISA is not dependent on the algorithm used, only on the problem of classification.

2.2 Feature learning

Feature learning, or representation learning(??), is a set of techniques that allow a model to discover representations needed for feature detection or classification from raw data. This is a method by which we replace feature engineering and have the model both learn the features and use them to perform the task.

Feature learning can be either supervised, unsupervised or self-supervised:

- in supervised learning, features are learned using labeled input data;
- in unsupervised learning, features are learned using the relationship between the individual observations in the input data. Examples include principal component analysis and various forms of clustering;
- in self-supervised learning, features are learned using unsupervised methods and then input-label pairs are constructed, enabling supervised learning. Examples include autoencoders and word embeddings.

2.3 Neural networks

Neural networks, formally called artificial neural networks (ANNs), are computational models inspired by networks of biological neurons (PURI et al., 2016). They are made up of multiple nodes called artificial neurons that map an input to an output based on mathematical operations. This model is used extensively in ML applications because of its perceived intelligent behaviour that comes from the interactions between neurons.

2.3.1 Artificial neuron

The artificial neuron is the most basic block of an ANN. It maps inputs to an output in the given fashion:

$$y = f(\mathbf{w} \cdot \mathbf{x} + b), \tag{2.1}$$

where the symbols are defined as:

$$\mathbf{x} = [x_1, x_2, \dots, x_n]$$
 Input vector;
 $\mathbf{w} = [w_1, w_2, \dots, w_n]$ Weight vector;
 f Activation function;
 y Neuron output;
 y Bias,

Figure 2.1 shows the artificial neuron model. This model of neuron is useful because it incorporates both the linear combination of input values and bias and the non-linearity of the activation function, which means it may function as a part of an universal function approximator (HORNIK *et al.*, 1989).

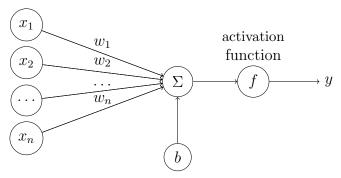


FIGURE 2.1 – Model of an artificial neuron.

2.3.2 The network

As said before, an ANN is a network of artificial neurons. Such network may be built by having the neurons configured in layers, having each neuron in a layer connected only to neurons in either preceding or following layers or with other arrangement of connections. Figure 2.2 shows a simple model of a fully-connected (a neuron in a layer connects to every neuron in the next layer) neural network, having 3 inputs, 4 middle nodes (called a hidden layer) and 3 output nodes.

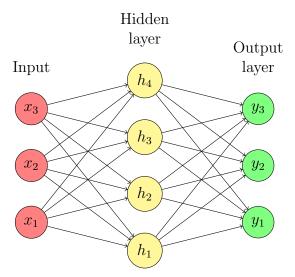


FIGURE 2.2 – A model of a simple fully-connected neural network with 3 inputs, 3 outputs and a hidden layer with 4 nodes.

2.3.3 Learning

Learning is the process by which an ANN adapts itself to a given task using data. It involves adjusting the weights of the network to improve some predefined metric (e.g. accuracy) and minimizing observed errors. In practice, learning is done by defining a loss function which is evaluated during learning and as long as its output (called loss, for short) decreases, the learning continues.

Most learning models are applications of optimization theory, like the gradient descent algorithm. In this algorithm the purpose is to find a local minima by moving against the gradient of the function. It is the basis for the Adam optimizer (KINGMA; BA, 2017), used extensively in ANNs.

2.3.3.1 Learning rate

The learning rate is a parameter in an optimization algorithm, defining the size of each step towards the local minima of a loss function. Higher learning rates shorten the learning time, but at a cost of possibly never converging and higher errors, while setting it at a value too low might have it converging in an undesirable local minimum.

2.3.3.2 Backpropagation

Backpropagation is a method to adjust the weights of the network and minimize the mean squared error. It computes the gradient of the loss function with respects to the weights and propagates backwards from the output layer to the initial layers in order to avoid redundant calculations.

2.4 Encoder, decoder and autoencoder neural networks

Neural networks can be used in feature learning tasks, as shown in section 2.2. We can construct neural networks to learn efficient codings of the input data.

An **autoencoder** is one such networks, composed of two parts: an encoder (or *encoding* function f) that transforms input data into a representation in a latent space and a decoder (or decoding function g) that recreates the data from this representation. The learning problem is then defined as minimizing a loss function $L(\mathbf{x}, g)$

It is not useful to have the autoencoder copy each input perfectly to

3 Instance Space Analysis

In this chapter we will be introducing the novel methodology for algorithm selection and performance evaluation called Instance Space Analysis (ISA), introduced in Muñoz et al. (2018). We will be showing the original definition of an instance space and the adaptation of the methodology brought up by Paiva et al. (2022) relating instance hardness.

3.1 Instance spaces

ISA is, at its core, an extension of the Algorithm Selection Problem (ASP) (RICE, 1976). Figure 3.1 shows the ISA framework with the ASP highlighted in blue. The objective in the ASP is to automate the process of selecting algorithms based on past similar solved problems. The following sets compose the core of the ASP:

- Problem Space \mathcal{P} : contains all instances of the problem being analysed;
- Instance Sub-space \mathcal{I} : contains a subset of instances from \mathcal{P} for which the characteristics and solutions are available;
- Feature Space \mathcal{F} : a set of descriptive characteristics of the instances in \mathcal{I} . These are also known as meta-features;
- Algorithm Space A: contains algorithms that may be used to solve the instances in \mathcal{I} ;
- Performance Space \mathcal{Y} : contains the performance evaluations of the algorithms in \mathcal{A} over the instances in \mathcal{I} .

The combination of tuples $(x, f(x), \alpha, y(\alpha, x))$, where $x \in \mathcal{I}$, $f(x) \in \mathcal{F}$, $\alpha \in \mathcal{A}$ and $y(\alpha, x) \in \mathcal{Y}$, composes a meta-dataset \mathcal{M} . A meta-learner S can then be trained to select the best algorithm for an instance x based on its meta-features, that is, an algorithm α^* with maximum predictive performance for x as given by y:

$$\alpha^* = S(f(x)) = \arg\max_{\alpha} ||y(\alpha, x)||. \tag{3.1}$$

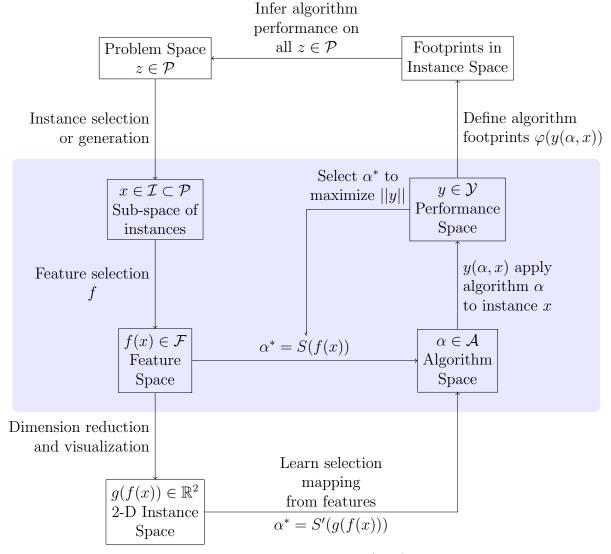


FIGURE 3.1 – ISA framework. Extracted from Muñoz et al. (2018). The ASP is highlighted in blue.

The ISA framework goes further to give insights into why some instances are harder to solve than others, using both the information of meta-features and algorithmic performance in a 2-D embedding, called Instance Space (IS), that can be visually inspected. An optimization problem is solved to find the mapping from meta-features to the IS g(f(x)), such that the distribution of algorithmic performance metrics and meta-features values display as close a linear trend as possible in the IS embedding. This embedding can then be inspected for regions of good and bad algorithmic performance and a new learner can be created to select new algorithms, as in:

$$\alpha^* = S'(g(f(x))) \tag{3.2}$$

In the IS, it is also possible to define algorithm footprints $\varphi(y(\alpha, x))$, which are areas where an algorithm α is expected to perform well. A set of objective measures can be derived from these footprints and aid in the inference of algorithmic performance for other

instances that were not in \mathcal{I} , such as:

- the area of the footprint A, which can be normalized across multiple algorithms for comparison;
- the density of the footprint ρ , which can be calculated as the ratio between the number of instances enclosed by the footprint and its area;
- the purity of the footprint p, which is the percentage of instances in the footprint that have good performance.

Summarizing, the application of ISA requires (MUÑOZ et al., 2018):

- 1. building the meta-dataset \mathcal{M} ;
- 2. reducing the set of meta-features in \mathcal{M} , keeping only those able to discriminate algorithmic performance;
- 3. creating the 2-D IS from \mathcal{M} ;
- 4. building the algorithms' footprints in the IS.

3.1.1 Instance Space construction

The problem of finding the optimal mapping between the instance metadata domain to a 2-D IS has been modelled using the Prediction Based Linear Dimensionality Reduction (PBLDR) method (SMITH-MILES; MUñOZ, 2023). Given a meta-dataset \mathcal{M} with m meta-features, n instances and a algorithms, let $F \in \mathbb{R}^{m \times n}$ be the matrix containing the meta-features values for all instances and $Y \in \mathbb{R}^{n \text{ timesa}}$ be the matrix containing the performance measure of the algorithms on the same instances. The optimal projection is achieved by minimizing the MSE:

$$MSE = ||\mathbf{F} - \hat{\mathbf{F}}||_F^2 + ||\mathbf{Y} - \hat{\mathbf{Y}}||_F^2, \tag{3.3}$$

such that:

$$\mathbf{Z} = \mathbf{A}_r \mathbf{F},\tag{3.4}$$

$$\hat{\mathbf{F}} = \mathbf{B}_r \mathbf{Z},\tag{3.5}$$

$$\hat{\mathbf{Y}}^T = \mathbf{C}_r \mathbf{Z}.\tag{3.6}$$

Where $\mathbf{A}_r \in \mathbb{R}^{2 \times m}$, $\mathbf{B}_r \in \mathbb{R}^{m \times 2}$ and $\mathbf{C}_r \in \mathbb{R}^{a \times 2}$. $\mathbf{Z} \in \mathbb{R}^{2 \times n}$ is the matrix of instance coordinates in the IS and A_r is the projection matrix. Smith-Miles e Muñoz (2023) solves this problem numerically using the Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm.

3.1.2 Footprint analysis

As said before, a footprint is a region in the IS where an algorithm is expected to perform well based on inference from empirical performance analysis (MUÑOZ et al., 2018). Smith-Miles e Muñoz (2023) goes into more detail of its construction, qualitatively we can infer from the set of footprint measures defined before that a good algorithm will have large quantities of each of those measures, i.e. a large area shows that an algorithm performs well in a large portion of the IS, a large density shows that the footprint contains a large amount of instances and a large purity shows that the algorithm performs well in most instances.

3.2 ISA for a single dataset

In Muñoz et al. (2018), ISA is defined with an instance being an entire classification dataset. Paiva et al. (2022) has adapted the framework and reduced the problem space \mathcal{P} into a single dataset, with each instance being an observation inside the dataset. This has come with the removal of some steps of the original ISA, namely the algorithmic recommendation module and the creation of new instances from the IS.

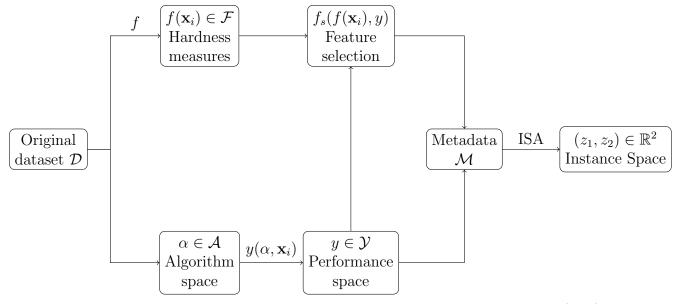


FIGURE 3.2 – ISA framework for a single dataset. Extracted from Paiva et al. (2022).

Given a classification dataset \mathcal{D} with n_D instances \mathbf{x}_i , m_D input features and each instance labelled in a class y_i , we have:

- **Problem space** \mathcal{P} : reduced to the dataset \mathcal{D} ;
- Instance sub-space \mathcal{I} : contains all individual instances \mathbf{x}_i ;
- Feature space \mathcal{F} : contains a set of meta-features known as hardness measures.

The modified framework is shown in Figure 3.2. For each instance, a set of hardness measures are stored in \mathcal{F} , and each algorithm $\alpha \in \mathcal{A}$ is evaluated over the instance \mathbf{x}_i and has its performance $y(\alpha, \mathbf{x}_i)$ measured and stored in \mathcal{Y} . The measure used is a cross-validated log-loss error obtained in the prediction of the instance label. A feature selection is made with these measures and the hardness measures, resulting in a reduced feature set $f_s(f(\mathbf{x}_i), y)$.

Combining the reduced feature set to the predictive performance of the algorithms allows us to construct the meta-dataset \mathcal{M} , from which the IS is extracted. The steps are explained in (PAIVA *et al.*, 2022), we will summarize some important topics.

3.2.1 Hardness measures

(PAIVA et al., 2022) revisits the definition of *Instance Hardness* (IH), a property that indicates the probability of an instance being misclassified given a classification hypothesis (SMITH et al., 2014):

$$IH_h(\mathbf{x}_i, y_i) = 1 - p(y_i|\mathbf{x}_i, h), \tag{3.7}$$

where $h: X \to Y$ is a classification hypothesis mapping an input space of features X to an output space of labels Y. In practice, h is a learning algorithm induced from the dataset \mathcal{D} and hyperparameters β , that is $h = l(\mathcal{D}, \beta)$. We can then compute the IH of the whole algorithm space \mathcal{A} :

$$IH_{\mathcal{A}}(\mathbf{x}_i, y_i) = 1 - \frac{1}{|\mathcal{A}|} \sum_{l \in \mathcal{A}} p(y_i | \mathbf{x}_i, l(\mathcal{D}, \beta)). \tag{3.8}$$

The idea is that instances frequently misclassified over the algorithm space can be considered hard, and instances being correctly classified are considered easy. Paiva *et al.* (2022) also shows a set of *hardness metrics* being extracted for each instance. Table 3.1 lists the measures used, the formal definition for each one is shown in Appendix A.

Measure	Acronym	Min.	Max.
k-Disagreeing Neighbours	kDN	0	1
Disjunct Class Percentage	DCP	0	1
Tree Depth (pruned)	TD_P	0	1
Tree Depth (unpruned)	TD_U	0	1
Class Likelihood	CL	0	1
Class Likelihood Difference	CLD	0	1
Fraction of features in overlapping areas	F1	0	1
Fraction of nearby instances different class	N1	0	1
Ratio of intra-extra class distances	N2	0	≈ 1
Local set cardinality	LSC	0	1
Local set radius	LSR	0	1
Usefulness	U	≈ 0	1
Harmfulness	Н	0	≈ 1

TABLE 3.1 – Hardness measures used in Paiva et al. (2022).

3.2.2 Performance assessment

To assess the performance from each algorithm in the dataset \mathcal{D} , it is first split into r folds according to the cross-validation strategy such that each instance from the dataset belongs to only one fold. r-1 folds are used for training the algorithm while the last fold is used for testing. Therefore we can compute a performance estimate for each instance and algorithm combination. The measure used for performance assessment was the log-loss, or cross-entropy, defined in equation 3.9:

$$logloss(\mathbf{x}_i) = -\sum_{c=1}^{C} y_{i,c} \log(p_{i,c}), \qquad (3.9)$$

where C is the number of classes the problem has, $y_{i,c}$ is a binary indicator of whether the class c is an actual label of \mathbf{x}_i or not and $p_{i,c}$ is the probability that the classifier attributes \mathbf{x}_i to class c.

3.2.3 Feature selection

For feature selection, Paiva et al. (2022) employs a method called Minimum Redundancy Maximum Relevance (MRMR), a criterion that gradually reduces the effect of feature redundancy as more features are selected. There is a trade-off between minimizing the number of redundant features and keeping relevant features, this method rejects redundant features at first but tolerates redundancy as more informative features are added. The mathematical model for MRMR is in equation 3.10:

$$J(\mathbf{f}_k) = MI(\mathbf{f}_k; \mathbf{y}_j) - \frac{1}{|\mathcal{S}_j|} \sum_{\mathbf{f}_i \in \mathcal{S}_j} MI(\mathbf{f}_k; \mathbf{f}_i), \tag{3.10}$$

where $J(\mathbf{f}_k)$ is a score for the k-th feature vector \mathbf{f}_k , $MI(\mathbf{f}_k; \mathbf{y}_j)$ is the mutual information between the feature vector and the response variable for the j-th algorithm and S_j is the set of selected features for the j-th algorithm. S_j is initially empty and the first feature chosen is the one with maximum mutual information between the feature vector and the response variable \mathbf{y}_j . Features are selected based on their score in subsequent rounds until there are a desired number of features chosen $n_f = |S_j|$.

3.2.4 IS representation and footprints

Given the now constructed meta-dataset \mathcal{M} after feature selection and performance assessments, the 2-D IS can be constructed. Paiva *et al.* (2022) added a rotation to the IS so that bad instances are placed towards the upper left of the IS, while good instances are placed towards the bottom right.

All of this section is implemented in the Python library PyHard (PAIVA et al., 2022). This work will use this implementation for reproducing this methodology.

4 Methodology

In this chapter, we will describe the problem's modelling and the main tools being used.

4.1 Instance Space generation

For the IS generation, we will use the PyHard (PAIVA et al., 2022) library. The library has some examples of the application. In this work we will generate the IS and create a new dataset using the original data and the resulting 2-D embedding.

4.2 Encoder and Decoder creation

The implementation of the encoding and decoding models is straightforward. Using the PyTorch (PASZKE et al., 2019) framework we can define classes that function as neural network models. It has methods for backpropagation and has multiple optimizers implemented. We will be using the Adam optimizer (KINGMA; BA, 2017) and the minimum squared error as the loss criterion.

4.3 Data generation and re-evaluation of the generated data

For data generation, we will define a region of the IS where we will sample points. Those points will then be passed into the trained decoder to go from the instance space into the data space. We will then re-evaluate the generated data using the adapted ISA. We will use the original 2-D embedding with the generated points and check if it correlates with the 2-D embedding computed from the generated data.

4.4 Implementation of this methodology

The code that implements this methodology is explained in Appendix B

5 Conclusion

5.1 Planned experiments

With the presented methodology, we list the following parts that are central to the problem's solution:

- A. definition of the dataset(s) to use;
- B. GAN architecture implementation;
- C. usage of ISA over the selected dataset(s) and adjustment of GAN training or network architecture;
- D. analysis of the generated instances.

5.2 Preliminary conclusions

In this work so far we have presented the theoretical foundations of GANs and the Instance Space Analysis methodology. The methodology presented shows promising applications of the combination of those technologies and new analyses that may be useful.

Challenges are expected in the implementation of the generator and discriminator networks because of the dataset selection (e.g. image-based datasets vs tabular datasets).

5.3 Work plan

With the landmarks detailed in section 5.1, we define the work plan in Table 5.1 for their implementation.

Month	Landmark				
WIGHT	A	В	С	D	
July					
August					
September					
October					
November					

TABLE 5.1 – Work plan for the development of this work.

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Appendix A - Instance Hardness

In this appendix, we will show the calculation of each hardness measures shown in table 3.1 extracted from (PAIVA et al., 2022).

k-Disagreeing Neighbours $kDN(\mathbf{x}_i)$: gives the percentage of the k nearest neighbours of \mathbf{x}_i which do not share its label. It is described in equation A.1

$$kDN(\mathbf{x}_i) = \frac{\#\{\mathbf{x}_j | \mathbf{x}_j \in kNN(\mathbf{x}_i) \land y_j \neq y_i\}}{k}$$
(A.1)

Disjunct Class Percentage $DCP(\mathbf{x}_i)$: builds a decision tree using the original dataset \mathcal{D} and considers the percentage of instances in the disjunct of \mathbf{x}_i which share the same label as \mathbf{x}_j . The disjunct of an example is the leaf node where it is classified by the decision tree. Equation A.2 shows the calculation of the measure.

$$DCP(\mathbf{x}_i) = 1 - \frac{\#\{\mathbf{x}_j | \mathbf{x}_j \in Disjunct(\mathbf{x}_i) \land y_j = y_i\}}{\#\{\mathbf{x}_j | \mathbf{x}_j \in Disjunct(\mathbf{x}_i)\}},$$
(A.2)

where $Disjunct(\mathbf{x}_i)$ represents the set of instances contained in the disjunct where \mathbf{x}_i is placed.

Tree Depth $TD(\mathbf{x}_i)$: returns the depth of the leaf node that classifies \mathbf{x}_i in a decision tree DT, normalized by the maximum depth of the tree built from \mathcal{D} :

$$TD(\mathbf{x}_i) = \frac{depth_{DT}(\mathbf{x}_i)}{\max(depth_{DT}(\mathbf{x}_i \in \mathcal{D}))}.$$
(A.3)

There are two versions of this measure, using pruned and unpruned decision trees.

Class Likelihood $CL(\mathbf{x}_i)$: measures the likelihood of \mathbf{x}_i belonging to its class:

$$CL(\mathbf{x}_i) = 1 - P(\mathbf{x}_i|y_i)P(y_i), \tag{A.4}$$

where $P(\mathbf{x}_i|y_i)$ is the likelihood of \mathbf{x}_i belonging to class y_i , measured in \mathcal{D} , and $P(y_i)$ is the prior of class y_i .

Class Likelihood Difference $CLD(\mathbf{x}_i)$: takes the difference between the likelihood of \mathbf{x}_i in relation to its class and the maximum likelihood it has to any other class:

$$CLD(\mathbf{x}_i) = \frac{1 - (P(\mathbf{x}_i|y_i) - \max_{y_j \neq y_i} [P(\mathbf{x}_i|y_j)P(y_j)])}{2}$$
(A.5)

Fraction of features in overlapping areas $F1(\mathbf{x}_i)$: the percentage of features of the instance \mathbf{x}_i whose values lie in an overlapping region of the classes:

$$F1(\mathbf{x}_i) = \frac{\sum_{j=1}^{m_D} I(x_{ij} > \operatorname{maxmin}(\mathbf{f}_j) \land x_{ij} < \operatorname{minmax}(\mathbf{x}\mathbf{f}_j))}{m_D},$$
(A.6)

where I is the indicator function, which return 1 if its argument is true and 0 otherwise, \mathbf{f}_j is the j-th feature vector and:

$$\min\max(\mathbf{f}_i) = \min(\max(\mathbf{f}_i^{c_1}), \max(\mathbf{f}_i^{c_2})), \tag{A.7}$$

$$\max\min(\mathbf{f}_i) = \max(\min(\mathbf{f}_i^{c_1}), \min(\mathbf{f}_i^{c_2})). \tag{A.8}$$

The values $\max(\mathbf{f}_j^{y_i})$ and $\min(\mathbf{f}_j^{y_i})$ are the maximum and minimum values of \mathbf{f}_j in a class $y_i \in c1, c2$.

Fraction of nearby instances of different classes $N1(\mathbf{x}_i)$: in this measure, first a minimum spanning tree (MST) is built from \mathcal{D} . In this tree, each instance of the dataset correspond to one vertex and nearby instances are connected according to their distances in the input space in order to obtain a tree of minimal cost concerning the sum of the edges' weights. N1 gives the percentage of instances of different classes that \mathbf{x}_i is connected to.

$$N1(\mathbf{x}_i) = \frac{\#\{\mathbf{x}_j | (\mathbf{x}_i, \mathbf{x}_j) \in MST(\mathcal{D}) \land y_j \neq y_i\}}{\#\{\mathbf{x}_i | (\mathbf{x}_i, \mathbf{x}_j) \in MST(\mathcal{D})\}}$$
(A.9)

Ratio of intra-extra class distances $N2(\mathbf{x}_i)$: first the ratio of the distance of \mathbf{x}_i to the nearest example from its class to the distance it has to the nearest instance from a different class is computed:

$$IntraInter(\mathbf{x}_i) = \frac{d(\mathbf{x}_i, NN(\mathbf{x}_i) \in y_i)}{d(\mathbf{x}_i, NN(\mathbf{x}_i) \in y_i \neq y_i)},$$
(A.10)

where $NN(\mathbf{x}_i)$ represents a nearest neighbour of \mathbf{x}_i . Then, $N2(\mathbf{x}_i)$ is computed as:

$$N2(\mathbf{x}_i) = 1 - \frac{1}{IntraInter(\mathbf{x}_i) + 1}$$
(A.11)

Local Set Cardinality $LSC(\mathbf{x}_i)$: the Local Set (LS) of an instance \mathbf{x}_i is the set of points from \mathcal{D} whose distances to \mathbf{x}_i are smaller than the distance between \mathbf{x}_i and \mathbf{x}_i 's nearest neighbour from another class:

$$LS(\mathbf{x}_i) = \{\mathbf{x}_j | d(\mathbf{x}_i, \mathbf{x}_j) < d(\mathbf{x}_i, NN(\mathbf{x}_i) \in y_j \neq y_i)\}$$
(A.12)

$$LSC(\mathbf{x}_i) = 1 - \frac{|LS(\mathbf{x}_i)|}{\#\{\mathbf{x}_j|y_j = y_i\}}$$
(A.13)

Local Set Radius $LSR(\mathbf{x}_i)$: the normalized radius of the LS of \mathbf{x}_i :

$$LSR(\mathbf{x}_i) = 1 - \min\left(1, \frac{d(\mathbf{x}_i, NN(\mathbf{x}_i) \in y_j \neq y_i)}{\max(d(\mathbf{x}_i, \mathbf{x}_j)|y_j = y_i)}\right)$$
(A.14)

Usefulness $U(\mathbf{x}_i)$: corresponds to the fraction of instances having \mathbf{x}_i in their local sets:

$$U(\mathbf{x}_i) = 1 - \frac{\#\{\mathbf{x}_j | d(\mathbf{x}_i, \mathbf{x}_j) < d(\mathbf{x}_j, NN(\mathbf{x}_j) \in y_k \neq y_j)\}}{|\mathcal{D}| - 1}$$
(A.15)

Harmfulness $H(\mathbf{x}_i)$: number of instances having \mathbf{x}_i as their nearest neighbour of another class:

$$H(\mathbf{x}_i) = \frac{\#\{\mathbf{x}_j | NN(\mathbf{x}_j) \in y_k \neq y_j = \mathbf{x}_i\}}{|\mathcal{D}| - 1}$$
(A.16)

All measures are computed using the entire dataset.

Appendix B - Code for this paper

FOLHA DE REGISTRO DO DOCUMENTO							
1. CLASSIFICAÇÃO/TIPO TC	DATA30 de junho de 2023	3. DOCUMENTO Nº DCTA/ITA/DM-018/2015	4. Nº DE PÁGINAS 33				
	works for instance space cod	ification and generation of da	ta with specific properties				
6. AUTOR(ES): Gabriel Barbosa Martinz							
7. INSTITUIÇÃO(ÕES)/ÓRGÃ Instituto Tecnológico de Ae	O(S) INTERNO(S)/DIVISÃO(Õ ronáutica – ITA	ES):					
8. PALAVRAS-CHAVE SUGER Machine Learning, Neural r	IDAS PELO AUTOR: networks, Instance Space Ana	alysis, Generative models					
9. PALAVRAS-CHAVE RESUL Aprendizagem (inteligência Dados; Computação.	•	assificações; Algoritmos; Com	plexidade computacional;				
10. APRESENTAÇÃO: Trabalho de Graduação, IT	` '	` '					
Trabalho de Graduação, ITA, São José dos Campos, 2023. 33 páginas. 11. RESUMO: One topic of study in Machine Learning is the study of algorithmic performance and which methodologies may be used to assess this performance. A methodology known as Instance Space Analysis has been used to relate predictive performance in classification algorithms to instance hardness (how hard an instance is for an algorithm to classify). The original methodology has been defined with the instance being an entire dataset, but further work has been made to make the instance as fine-grained as an individual observation. In this work we will build upon this methodology and we propose the creation of a generative neural network model to generate new observations for a classification algorithm with predefined hardness properties.							
12. GRAU DE SIGILO: (X) OSTENS:	IVO () RESER	RVADO () SEC	CRETO				