FACULDADE DE ENGENHARIA DA UNIVERSIDADE DO PORTO

Exploring Visual Programming Concepts for Probabilistic Programming Languages

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WORKING VERSION



Mestrado Integrado em Engenharia Informática e Computação

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Abstract

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Resumo

O Resumo fornece ao leitor um sumário do conteúdo da dissertação. Deverá ser breve mas conter detalhe suficiente e, uma vez que é a porta de entrada para a dissertação, deverá dar ao leitor uma boa impressão inicial.

Este texto inicial da dissertação é escrito no fim e resume numa página, sem referências externas, o tema e o contexto do trabalho, a motivação e os objectivos, as metodologias e técnicas empregues, os principais resultados alcançados e as conclusões.

Este documento ilustra o formato a usar em dissertações na Faculdade de Engenharia da Universidade do Porto. São dados exemplos de margens, cabeçalhos, títulos, paginação, estilos de índices, etc. São ainda dados exemplos de formatação de citações, figuras e tabelas, equações, referências cruzadas, lista de referências e índices. É usado texto descartável, *Loren Ipsum*, para preencher a dissertação por forma a ilustrar os formatos.

Seguem-se umas notas breves mas muito importantes sobre a versão provisória e a versão final do documento. A versão provisória, depois de verificada pelo orientador e de corrigida em contexto pelo autor, deve ser publicada na página pessoal de cada estudante/dissertação, juntamente com os dois resumos, em português e em inglês; deve manter a marca da água, assim como a numeração de linhas conforme aqui se demonstra.

A versão definitiva, a produzir somente após a defesa, em versão impressa (dois exemplares com capas próprias FEUP) e em versão eletrónica (6 CDs com "rodela" própria FEUP), deve ser limpa da marca de água e da numeração de linhas e deve conter a identificação, na primeira página, dos elementos do júri respetivo. Deve ainda, se for o caso, ser corrigida de acordo com as instruções recebidas dos elementos júri.

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The Name of the Author



"You should be glad that bridge fell down. I was planning to build thirteen more to that same design" Isambard Kingdom Brunel



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Abbreviations

ADT Abstract Data Type

PP Probabilistic Programming

PPL Probabilistic Programming Language

PPAML Probabilistic Programming for Advancing Machine Learning

ML Machine Learning VP Visual Programming

VPL Visual Programming Language

DARPA Defense Advanced Research Projects Agency

PR Probabilistic Reasoning

Chapter 1

Introduction

This first chapter aims to provide the reader with an overview of this dissertation. It starts by introducing the context this work is inserted in, identifying the problem which we aim to solve, how we plan on solving it, and the expected outcome. Lastly, it gives a bird's eye view of this report's structure.

1.1 Context

There is, among several domains with interesting and relevant problems to solve (computer vision [KT15], cryptography, biology, fraud detection, recommender systems [Alp10], ...), the recurring necessity to be able to make decisions in the face of uncertainty using machine learning (ML) methods.

Successful ML applications include Google's personalized advertising and context-driven information retrieval, Facebook's studies of how information spreads across a network or UC Berkeley's AMPLab contributions towards Amazon Web Service and SAP's products [BAF+15].

Typically, there are two approaches for this class of problems): either use an existing machine learning model (such as KNN, neural networks or similar) [Sch08] and try to fit your data into the model, or build a probabilistic model for your particular problem so you can leverage domain knowledge [Gri13].

In the second approach one common way to tackle it is to use bayesian reasoning, where you model unknown causes with random variables, feed the model the data you have gathered and then perform inference to reverse the story and query for the desired variables [Dow12]. The tricky issue is this last step, since it is non-trivial to write an inference method [DL].

The solution to this has been building generic inference engines for graphical models, so that modeling and inference can be treated as separate concerns and people can focus on the modeling [JW96]. However, not all models can be represented as graphical models, and that's why we now

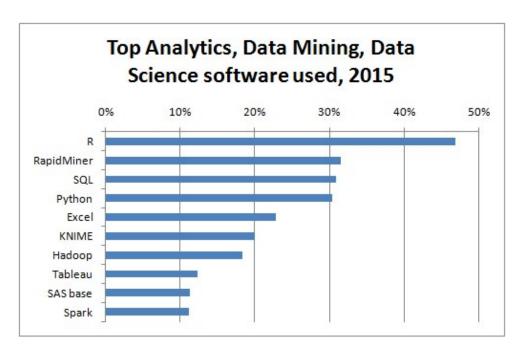


Figure 1.1: Top 10 Analytics Tools [Pia15]

have Probabilistic Programming Languages (PPLs). Probabilistic Programs let you write your model as a program and have off-the-shelf inference [Pre03].

1.2 Problem

In spite of these examples of applications in the industry, ML has been identified by Gartner, in its Hype Cycle annual review, to be in the "Peak of Inflated Expectations" stage, still far from the "Plateau of Producitvity" [Sta15].

It has also been said that ML's applications are rarely seen outside the academia, with Wagstaff claiming that there is a "frequent lack of connection between machine learning research and the larger world of scientific inquiry and humanity" [Wag12].

Arguably the scenario is even worse for PPLs, having even lesser adoption among tech companies. One factor which may be contributing to this lack of usage, despite PP's power and flexibility, is the difficulty for data scientists to adapt to textual interface these languages provide, which lack the graphical intuiton provided by other tools they are accustomed to. In a poll made to about 2800 data scientists (see Figure 1.1), half of the top 10 tools are graphically-interactable.

1.3 Motivation and Goals

The Defense Advanced Research Projects Agency (DARPA), one of the funders behind PPLs' research, has recognized some of the problems identified by Wagstaff and started a program called

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Probabilistic Programming for Advancing Machine Learning (PPAML) to address the shortcomings of current ML methods [Jag13]. It identifies five strategic goals:

- Shorten machine learning model code to make models faster to write and easier to understand
- Reduce development time and cost to encourage experimentation
- Facilitate the construction of more sophisticated models that incorporate rich domain knowledge and separate queries from underlying code
- Reduce the level of expertise necessary to build machine learning applications
- Support the construction of integrated models across a wide variety of domains and tool types

The purpose of this work is to try addressing the first four. In order to do so we aim to overcome the difficulties in learning a new language, either for unexperienced developers or seasoned ones, such as learning yet another syntax or getting accostumed to the language's idioms. It is known that typical languages are difficult to learn and use [LO87] and that there are advantages in providing a language with a visual interface [AA92]. Also, studies have shown that programmers and data scientists alike resort to mental imagery when solving problems [Das02][PB99], so by providing such an interface we can approximate how people think and how they use the language to solve the problem at hand.

So, the goal of this dissertation will be to develop a Visual Programming Language (VPL) with probabilities programming capabilities. The targeted audience are programmers and data scientists with background knowledge in statistics who aren't still comfortable with full blown PPLs, but wish to educate themselves in the topic so they can eventually leverage the power of this novel machine learning approach.

The way to do so would be developing a graphical node-based editor, similar to RapidMiner or Blender Composite Nodes, but that runs in the browser. The given editor would have the capability to compile its graph to the textual representation in the target PPL so that the user can run what it has designed, either as a standalone script or even by integrating it with his existing projects.

The hypothesis under consideration is this graphical representation is more intuitive and easy to learn that a full-blown PPL. We intend to validate such hypothesis by ensuring that classical problems solved in the literature by PPLs are also supported by our graphical representation, and then measure how quickly a group of people trained in statistics would produce a viable model in both alternatives.

1.4 Outline

Para além da introdução, esta dissertação contém mais x capítulos. No capítulo 2, é descrito o estado da arte e são apresentados trabalhos relacionados. No capítulo 3, ipsum dolor sit amet,

Introduction

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Chapter 2

Background State of the Art

This chapter has two purposes: describing the foundations on which this work is built on, namely Machine Learning (ML), Probabilistic Reasoning (PR), Prograbilistic Programming (PP) and Visual Programming(VP) while enumerating different tools which are based on one of these concepts.

2.0.1 Machine learning

Machine learning is a field which can be seen as a subfield of artifical intelligence that incorporates mathematics and statistics and is concerned with conceiving algorithms that learn autonomously, that is, without human interventation [Bri16][Sch08]. It has the potential to impact a wide spectrum of different areas such as biology, medicine, finance, astronomy [Ama13], computer vision, sales forecast, robotics [Alp10], product recommendations, fraud detection or internet ads bidding [Gri13].

Learning from data is commercially and scientifically important. ML consists of methods that automatically extract interesting knowledge in databases of sometimes chaotic and redundant information. ML is a data-based knowledge-discovering process that has the potential not only to analyze events in retrospect but also to predict future events or important alterations [Geo16].

2.0.2 Probabilistic Reasoning

Probabilistic reasoning is the formation of probability judgments and of subjective beliefs about the likelihoods of outcomes and the frequencies of events [?], it is a way to combine our knowledge of a situation with the laws of probability. There are subjective belifs because, in non-trivial decision-making there are unobserved factors that are critical to the decision in conjunction with several sources of uncertainty [GSD], such as:

• Uncertain inputs, due to missing or noisy data

Uncertain knowledge, where multiple causes lead to multiple effects, or there is an incomplete knowledge of conditions, effects and causality of the domain or simply because the effects are inherently stochastic.

So, probabilistic reasoning only gives probabilistic results.

It is one way to overcome cognitive bias and be able to make rational decisions [SG01]. A trial has been made [CSB82] where physicians were asked to estimate the probability that a woman with a positive mammogram actually has breast cancer, given a base rate of 1% for breast cancer, a hit rate of about 80%, and a false-alarm rate of about 10%. It reported that 95 of 100 physicians estimated the probability that she actually has breast cancer to be between 70% and 80%, whereas Bayes's rule gives a value of about 7.5%. Such systematic deviations from Bayesian reasoning have been called "cognitive illusions,". We will describe both Bayes's rules and Bayesian reasoning in the next section.

2.0.2.1 Bayesian Reasoning

One way to approach PR is by using bayesian reasoning, which is inspired in the Bayes Theorem. An equivalent rule to the theorem, in its simplest form (applied to a single event) is:

$$P(A \mid B) = \frac{P(A \land B)}{P(B)}$$

Where P(A|B) defines the probability of event A given that B occurred. The theorem defines how hidden causes (A) relate to observed events (B), given a causality model (P(A, B) or P(B|A)*P(A)) and our knowledge of the probability of the occurrence of events (P(B)). As an example, P(penalty | goal) defines the probability that a penalty kick was scored, knowing that there was a goal.

There are at least two interpretations to the theorem and regarding how one may think about its results [Fie06]:

- Frequentist interpretation: probabilities are defined by the relative frequency of events, given a natural sampling. Meaning, the probability of obtaining 'Heads' when rolling a dice is equal to the number of 'Heads' obtained after rolling the dice a sufficient number of times relative to the total number of times the dice has been rolled.
- Epistemological interpreation: probabilities represent a measure of belief. It can either be a
 result logical combination of probabilities through the usage of axioms (it's closely related
 to Aristotlean logic) or it can also reflect a personal belief (which is called a subjective
 view).

One example of the application of this theorem is [GSD]: you know your home's alarm is ringing, but you don't know whether that was caused by a burglar or something else (maybe a bird triggered it, or there was a malfunction in the alarm system). How confident are you that you're

Table 2.1: Alarm system confusion matrix

	alarm	¬alarm
burglary	0.09	0.01
$\neg burglary$	0.1	0.8

being robbed? Consider that the alarm company, based on quality trials, defined in the confusion matrix for P(alarm, burglary) (Table 2.1).

You can interpret each table's cell as P(A, B). For instances, the top left cell is the probability that the alarm rings and there is a burglar, while the bottom left cell is the probability that the alarm rang but there was no burglar (a false positive).

If we substitute the values of the Bayes rule described above, we get:

$$P(burglar \mid alarm) = \frac{P(burglar, alarm)}{P(alarm)}$$

Which results in 0.09 / 0.19 = 0.47.

Rede bayesianana

Think Bayes: diachronic

2.0.2.2 Probabilistic Programming

Auto PR+BR

"If we view the semantics of the underlying deterministic language as a map from programs to executions of the program, the semantics of a PPL built on it will be a map from programs to distributions over executions. When the program halts with probability one, this induces a proper distribution over return values. Indeed, any computable distribution can be represented as the distribution induced by a Church program in this way" [FR12]

Probabilistic programming is a way to create systems that help us make decisions in the face of uncertainty. Lots of everyday decisions involve judgment in determining relevant factors that we do not directly observe [SP93]. Historically, one way to help make decisions under uncertainty has been to use a probabilistic reasoning system [Las12]. Probabilistic reasoning combines our knowledge of a situation with the laws of probability to determine those unobserved factors that are critical to the decision. Typically, the way the several observations are combined is through the usage of bayesian statistics, due to its anachronistic interpretation where existing knowledge (priors) are combined with observations in order to gather evidence towards competing hypothesis.

When compared to other machine learning methods (such as random forests, neural networks or linear regression), which take homogeneous data as input (requiring the user to separate their domain into different models), probabilistic programming is used to leverage the data's original structure. Plus, it provides full probability distributions over both the predictions and parameters

Background State of the Art

of the model, whereas ML methods can only give the user a certain degree of confidence on the predictions.

Until recently, probabilistic reasoning systems have been limited in scope, and have been hard to apply to many real world situations. Models are communicated using a mix of natural language, pseudo code, and mathematical formulae and solved using special purpose, one-off inference methods. Rather than precise specifications suitable for automatic inference, graphical models typically serve as coarse, high-level descriptions, eliding critical aspects such as fine-grained independence, abstraction and recursion.

Probabilistic programming is a new approach that makes probabilistic reasoning systems easier to build and more widely applicable. A probabilistic programming language (PPL) is a programming language designed to describe probabilistic models, in a such a way we can say that the program itself is the model, and then perform inference in those models. PPLs have seen recent interest from the artificial intelligence, programming languages, cognitive science, and natural languages communities. By empowering users with a common dialect in the form of a programming language, rather than requiring each one of them to the non-trivial and error-prone task of writing their own models and hand-tailored inference algorithms for the problem at hand, it encourages exploration, since different models require less time to setup and evaluate, and enables sharing knowledge in the form of best practices, patterns and tools such as optimized compilers or interpreters, debuggers, IDE's, optimizers and profilers.

PPLs are closely related to graphical models and Bayesian networks, but are more expressive and flexible. One can easily realize this by looking at the re-usable components PPLs offer, being one of them the inference engine, which can be plugged in into different models. For instances, it is easy to replace the exact-solution traditional Bayesian networks inference, which requires time exponential in the number of variables to run, with approximation algorithms such as the Markov Chain Monte Carlo (MCMC) or Variational Message Passing (VMP), which make it possible to compute large hierarchical models by resorting to sampling and approximation. PPLs often extend from a basic language (i.e., they are embedded in a host language like R, Java or Scala), although some PPLs such as WinBUGS and Stan offer a self-contained language, with no obvious origin in another language.

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2.0.3 Visual Programming

- 2.0.3.1 Visual Dataflow Programming
- 2.0.4 State of the Art
- 2.0.4.1 Stan
- **2.0.4.2 WinBUGS**
- 2.0.4.3 Church
- 2.0.4.4 Infer.NET
- 2.0.4.5 PyMC
- 2.0.4.6 VIBES
- 2.0.4.7 NoFlo
- 2.0.4.8 RapidMiner
- 2.0.4.9 Weka Knowledge FLow
- 2.0.4.10 GoJS
- 2.0.4.11 Blockly

2.1 Conclusions

Background State of the Art

Chapter 3

Visualização de Sinópticos SVG

Este capítulo deve começar por fazer uma apresentação detalhada do problema a resolver¹ podendo mesmo, caso se justifique, constituir-se um capítulo com essa finalidade.

Deve depois dedicar-se à apresentação da solução sem detalhes de implementação. Dependendo do trabalho, pode ser uma descrição mais teórica, mais "arquitetural", etc.

3.1 Secção Exemplo

Neste capítulo apresentam-se exemplos de formatação de figuras e tabelas, equações e referências cruzadas.

Apresenta-se de seguida um exemplo de equação, completamente fora do contexto:

$$CIF_1: F_0^j(a) = \frac{1}{2\pi \iota} \oint_{\gamma} \frac{F_0^j(z)}{z - a} dz$$
 (3.1)

$$CIF_2: F_1^j(a) = \frac{1}{2\pi i} \oint_{\gamma} \frac{F_0^j(x)}{x - a} dx$$
 (3.2)

Na Equação 3.2 lorem ipsum dolor sit amet, consectetuer adipiscing elit. Suspendisse tincidunt viverra elit. Donec tempus vulputate mauris. Donec arcu. Vestibulum condimentum porta justo. Curabitur ornare tincidunt lacus. Curabitur ac massa vel ante tincidunt placerat. Cras vehicula semper elit. Curabitur gravida, est a elementum suscipit, est eros ullamcorper quam, sed cursus velit velit tempor neque. Duis tempor condimentum ante.

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¹Na introdução a apresentação do problema foi breve.



Figure 3.1: Arquitectura da Solução Proposta

est. Sed lectus lorem, congue vel, dignissim laoreet, blandit a, nisi. Aenean nunc ligula, tincidunt eu, hendrerit vel, suscipit non, erat. Aliquam gravida. Integer non pede. In laoreet augue id leo. Mauris placerat.

A arquitetura do visualizador assenta sobre os seguintes conceitos base [?]:

- **Componentes** Suspendisse auctor mattis augue *push*;
- **Praesent** Sit amet sem maecenas eleifend facilisis leo;
- **Pellentesque** Habitant morbi tristique senectus et netus.

3.1.1 Exemplo de Figura

É apresentado na Figura 3.1 um exemplo de figura flutuante.

Loren ipsum dolor sit amet, consectetuer adipiscing elit. Praesent sit amet sem. Maecenas eleifend facilisis leo. Vestibulum et mi. Aliquam posuere, ante non tristique consectetuer, dui elit scelerisque augue, eu vehicula nibh nisi ac est. Suspendisse elementum sodales felis. Nullam laoreet fermentum urna.

Duis eget diam. In est justo, tristique in, lacinia vel, feugiat eget, quam. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Fusce feugiat, elit ac placerat fermentum, augue nisl ultricies eros, id fringilla enim sapien eu felis. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Sed dolor mi, porttitor quis, condimentum sed luctus.

3.1.2 Exemplo de Tabela

É apresentado na Tabela 3.1 um exemplo de tabela flutuante e na Tabela 3.2 um exemplo de tabela flutuante, um pouco mais complicada.

Integer quis pede. Fusce nibh. Fusce nec erat vel mi condimentum convallis. Sed at tortor non mauris pretium aliquet. In in lacus in dolor molestie dapibus. Suspendisse potenti. Pellentesque

Table 3.1: Uma Tabela Simples

Acrónimo	Significado				
ADT	Abstract Data Type				
ANDF	Architecture-Neutral Distri-				
	bution Format				
API	Application Programming				
	Interface				

sagittis porta erat. Mauris sodales sapien id augue. Nam eu dolor. Donec sit amet turpis non orci rhoncus commodo. Etiam condimentum commodo libero.

Mauris pede. Curabitur faucibus dictum nibh. Proin tincidunt diam vitae mauris. Sed hendrerit dolor vel ipsum. Nullam dapibus. Vivamus tellus diam, egestas sit amet, vulputate non, vulputate id, eros. Nunc sit amet nibh eget nibh imperdiet ornare. Cras vehicula mattis ipsum. Sed diam arcu, semper at, gravida vitae, fermentum et, nulla. Aenean massa orci, tristique nec, rutrum id, fringilla eget, erat. Curabitur nulla ipsum, aliquam sed, rutrum vitae, semper quis, ante. Fusce at nunc in dolor condimentum tempor. Duis sit amet massa.

Curabitur convallis nulla quis risus. Nulla mollis porttitor purus. Fusce ultricies odio at ligula pellentesque suscipit. Nulla velit libero, blandit a, aliquet quis, hendrerit id, arcu. Phasellus porttitor purus. Suspendisse velit tortor, fringilla sit amet, commodo a, ultrices et, mi. Donec eu metus in erat ornare adipiscing. Praesent varius mi ac nunc. Vestibulum leo lacus, elementum in, vestibulum sit amet, hendrerit at, justo. Sed sit amet neque. Donec libero risus, commodo sit amet, dignissim ut, tincidunt a, eros. Ut non lacus quis tortor mattis ullamcorper. Vivamus consequat augue vel erat. Sed tincidunt. Sed leo eros, ornare a, pulvinar non, mattis quis, nibh. Aliquam faucibus mi ac nisi.

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Duis eget diam. In est justo, tristique in, lacinia vel, feugiat eget, quam. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Fusce feugiat, elit ac

Table 3.2: Uma Tabela Mais Complicada

Iteração k de $f(x_n)$										
k	x_1^k	x_2^k	x_3^k	comentários						
0	-0.3	0.6	0.7	_						
1	0.47102965	0.04883157	-0.53345964	$\delta < arepsilon$						
2	0.49988691	0.00228830	-0.52246185	$\delta < arepsilon$						
3	0.49999976	0.00005380	-0.523656	N						
4	0.5	0.00000307	-0.52359743							
:	:	·	:							
7	0.5	0.0	-0.52359878	$\delta < 10^{-8}$						

placerat fermentum, augue nisl ultricies eros, id fringilla enim sapien eu felis. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Sed dolor mi, porttitor quis, condimentum sed luctus.

3.2 Secção Exemplo

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Duis eget diam. In est justo, tristique in, lacinia vel, feugiat eget, quam. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Fusce feugiat, elit ac placerat fermentum, augue nisl ultricies eros, id fringilla enim sapien eu felis. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Sed dolor mi, porttitor quis, condimentum sed luctus.

3.3 Resumo e Conclusões

Resumir e apresentar as conclusões que se podem tirar no fim deste capítulo.

Chapter 4

Implementação

Este capítulo pode ser dedicado à apresentação de detalhes de nível mais baixo relacionados com o enquadramento e implementação das soluções preconizadas no capítulo anterior. Note-se no entanto que detalhes desnecessários à compreensão do trabalho devem ser remetidos para anexos.

Dependendo do volume, a avaliação do trabalho pode ser incluída neste capítulo ou pode constituir um capítulo separado.

4.1 Secção Exemplo

Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Integer hendrerit commodo ante. Pellentesque nibh libero, aliquam at, faucibus id, commodo a, velit. Duis eleifend sem eget leo. Morbi in est. Suspendisse magna sem, varius nec, hendrerit non, tincidunt quis, quam. Aenean congue. Vivamus vel est sit amet sem iaculis posuere. Cras mollis, enim vel gravida aliquam, libero nunc ullamcorper dui, ullamcorper sodales lectus nulla sed urna. Morbi aliquet porta risus. Proin vestibulum ligula a purus. Maecenas a nulla. Maecenas mattis est vitae neque auctor tempus. Etiam nulla dui, mattis vitae, porttitor sed, aliquet ut, enim. Cras nisl magna, aliquet et, laoreet at, gravida ac, neque. Sed id est. Nulla dapibus dolor quis ipsum rhoncus cursus.

4.2 Mais uma Secção

Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Quisque purus sapien, interdum ut, vestibulum a, accumsan ullamcorper, erat. Mauris a magna ut leo porta imperdiet. Donec dui odio, porta in, pretium non, semper quis, orci. Quisque erat diam, pharetra vel, laoreet ac, hendrerit vel, enim. Donec tristique luctus risus. Fusce dolor est, eleifend id, elementum sit amet, varius vitae, neque. Morbi at augue. Ut sem ligula, auctor vitae, facilisis id, pharetra non, lectus. Nulla lacus augue, aliquam eget, sollicitudin sed, hendrerit eu, leo. Suspendisse ac tortor. Mauris at odio. Etiam vehicula. Nam lacinia purus at nibh. Aliquam fringilla lorem ac justo. Ut nec enim.

Implementação

```
map(String key, String value):
    // key: document name
    // value: document contents
    for each word w in value:
    EmitIntermediate(w, "1");

reduce(String key, Iterator values):
    // key: a word
    // values: a list of counts
    int result = 0;
    for each v in values:
    result += ParseInt(v);

Emit(AsString(result))
```

Listing 4.1: Example map and reduce functions for word counting

Quisque ullamcorper. Aliquam vel magna. Sed pulvinar dictum ligula. Sed ultrices dolor ut turpis. Vivamus sagittis orci malesuada arcu venenatis auctor. Proin vehicula pharetra urna. Aliquam egestas nunc quis nisl. Donec ullamcorper. Nulla purus. Ut suscipit lacus vitae dui. Mauris semper. Ut eget sem. Integer orci. Nam vitae dui eget nisi placerat convallis.

Sed id lorem. Proin gravida bibendum lacus. Sed molestie, urna quis euismod laoreet, diam dolor dictum diam, vitae consectetuer leo ipsum id ante. Integer eu lectus non mauris pharetra viverra. In feugiat libero ut massa. Morbi cursus, lorem sollicitudin blandit semper, felis magna pellentesque lacus, ut rhoncus leo neque at tellus. Sed mattis, diam eget eleifend tincidunt, ligula eros tincidunt diam, vitae auctor turpis est vel nunc. In eu magna. Donec dolor metus, egestas sit amet, ultrices in, faucibus sed, lectus. Etiam est enim, vehicula pharetra, porta non, viverra vel, nunc. Ut non sem. Etiam nec neque.

4.3 Resumo ou Conclusões

Proin vehicula pharetra urna. Aliquam egestas nunc quis nisl. Donec ullamcorper. Nulla purus. Ut suscipit lacus vitae dui. Mauris semper. Ut eget sem. Integer orci. Nam vitae dui eget nisi placerat convallis.

Chapter 5

Conclusões e Trabalho Futuro

Deve ser apresentado um resumo do trabalho realizado e apreciada a satisfação dos objetivos do trabalho, uma lista de contribuições principais do trabalho e as direções para trabalho futuro.

A escrita deste capítulo deve ser orientada para a total compreensão do trabalho, tendo em atenção que, depois de ler o Resumo e a Introdução, a maioria dos leitores passará à leitura deste capítulo de conclusões e recomendações para trabalho futuro.

5.1 Satisfação dos Objetivos

Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Etiam non felis sed odio rutrum ultrices. Donec tempor dolor. Vivamus justo neque, tempus id, ullamcorper in, pharetra non, tellus. Praesent eu orci eu dolor congue gravida. Sed eu est. Donec pulvinar, lectus et eleifend volutpat, diam sapien sollicitudin arcu, a sagittis libero neque et dolor. Nam ligula. Cras tincidunt lectus quis nunc. Cras tincidunt congue turpis. Nulla pede velit, sagittis a, faucibus vitae, porttitor nec, ante. Nulla ut arcu. Cras eu augue at ipsum feugiat hendrerit. Proin sed justo eu sapien eleifend elementum. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Vivamus quam lacus, pharetra vel, aliquam vel, volutpat sed, nisl.

Nullam erat est, vehicula id, tempor non, scelerisque at, tellus. Pellentesque tincidunt, ante vehicula bibendum adipiscing, lorem augue tempor felis, in dictum massa justo sed metus. Suspendisse placerat, mi eget molestie sodales, tortor ante interdum dui, ac sagittis est pede et lacus. Duis sapien. Nam ornare turpis et magna. Etiam adipiscing adipiscing ipsum. Fusce sodales nisl a arcu. Cras massa leo, vehicula facilisis, commodo a, molestie faucibus, metus. Suspendisse potenti. Duis sagittis. Donec porta. Sed urna. Maecenas eros. Vivamus erat ligula, pharetra sit amet, bibendum et, fermentum sed, dolor. Nullam eleifend condimentum nibh. Integer leo nibh, consequat eget, mollis et, sagittis ac, felis. Duis viverra pede in pede. Phasellus molestie placerat leo. Praesent at tellus a augue congue molestie. Proin sed justo eu sapien eleifend elementum. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas.

5.2 Trabalho Futuro

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Aliquam felis justo, facilisis sit amet, bibendum ut, tempus ac, dolor. Sed malesuada. Nunc non massa. In erat. Nulla facilisi. Phasellus blandit, est in accumsan cursus, libero augue elementum leo, vitae auctor mauris nisl ac tortor. Cras porttitor ornare elit. Fusce at lorem. Sed lectus tortor, vestibulum id, varius a, condimentum nec, lectus. Maecenas in nisi et magna pretium aliquam. Pellentesque justo elit, feugiat nec, tincidunt a, dignissim vel, ipsum. Sed nunc. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Aliquam tempus rhoncus leo. Donec neque quam, cursus sit amet, ultricies varius, semper non, pede. Donec porttitor. Sed aliquet feugiat elit.

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Appendix A

Loren Ipsum

Depois das conclusões e antes das referências bibliográficas, apresenta-se neste anexo numerado o texto usado para preencher a dissertação.

A.1 O que é o Loren Ipsum?

Lorem Ipsum is simply dummy text of the printing and typesetting industry. Lorem Ipsum has been the industry's standard dummy text ever since the 1500s, when an unknown printer took a galley of type and scrambled it to make a type specimen book. It has survived not only five centuries, but also the leap into electronic typesetting, remaining essentially unchanged. It was popularised in the 1960s with the release of Letraset sheets containing Lorem Ipsum passages, and more recently with desktop publishing software like Aldus PageMaker including versions of Lorem Ipsum [?].

A.2 De onde Vem o Loren?

Contrary to popular belief, Lorem Ipsum is not simply random text. It has roots in a piece of classical Latin literature from 45 BC, making it over 2000 years old. Richard McClintock, a Latin professor at Hampden-Sydney College in Virginia, looked up one of the more obscure Latin words, consectetur, from a Lorem Ipsum passage, and going through the cites of the word in classical literature, discovered the undoubtable source. Lorem Ipsum comes from sections 1.10.32 and 1.10.33 of "de Finibus Bonorum et Malorum" (The Extremes of Good and Evil) by Cicero, written in 45 BC. This book is a treatise on the theory of ethics, very popular during the Renaissance. The first line of Lorem Ipsum, "Lorem ipsum dolor sit amet...", comes from a line in section 1.10.32.

The standard chunk of Lorem Ipsum used since the 1500s is reproduced below for those interested. Sections 1.10.32 and 1.10.33 from "de Finibus Bonorum et Malorum" by Cicero are also reproduced in their exact original form, accompanied by English versions from the 1914 translation by H. Rackham.

A.3 Porque se usa o Loren?

It is a long established fact that a reader will be distracted by the readable content of a page when looking at its layout. The point of using Lorem Ipsum is that it has a more-or-less normal distribution of letters, as opposed to using "Content here, content here", making it look like readable English. Many desktop publishing packages and web page editors now use Lorem Ipsum as their default model text, and a search for "lorem ipsum" will uncover many web sites still in their infancy. Various versions have evolved over the years, sometimes by accident, sometimes on purpose (injected humour and the like).

A.4 Onde se Podem Encontrar Exemplos?

There are many variations of passages of Lorem Ipsum available, but the majority have suffered alteration in some form, by injected humour, or randomised words which don't look even slightly believable. If you are going to use a passage of Lorem Ipsum, you need to be sure there isn't anything embarrassing hidden in the middle of text. All the Lorem Ipsum generators on the Internet tend to repeat predefined chunks as necessary, making this the first true generator on the Internet. It uses a dictionary of over 200 Latin words, combined with a handful of model sentence structures, to generate Lorem Ipsum which looks reasonable. The generated Lorem Ipsum is therefore always free from repetition, injected humour, or non-characteristic words etc.