# Mitigating Overfitting

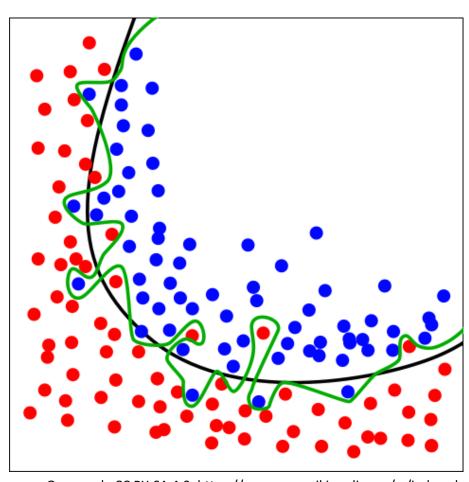
Matthew Engelhard

#### Recall the NDP

- Complex models are capable of dramatically overfitting the data
- We can think of this as "memorizing" the data
- It is therefore <u>critical</u> to evaluate on a held-out test set (supposing what you care about is out-of-sample performance)



#### Which boundary performs better on unseen data?



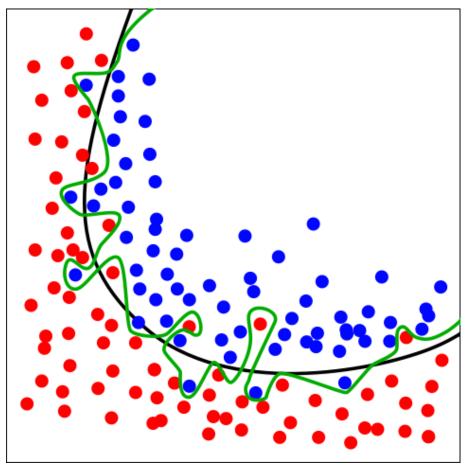
#### Green boundary:

- Correct predictions for *all* training data
- Very likely to be overfitting

#### Black boundary:

Balance between fit and model complexity

#### Quantifying Overfitting



Which boundary performs better when applied to new data? And by how much?

- We can quantify overfitting as the difference in performance (usually the cross-entropy loss) between the training and validation sets
- Greater overfitting usually (but not always) means worse out-of-sample performance
- So, we almost always take steps to mitigate it

## Let's teach our robot to identify beaches.



We show it a bunch of images and ask:

What do you see?

It starts listing features from most to least obvious.



## Let's teach our robot to identify beaches.



#### I think beaches have:

- water
- land
- sky
- sand
- palm trees
- clouds
- ripples
- foam
- white sand
- clear water
- deep blue sky
- exactly 0 or 1 seashells
- Instagram color palette

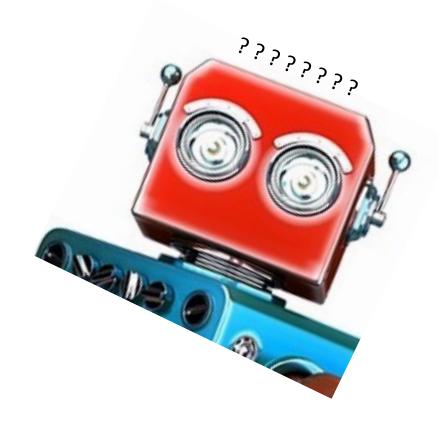
## It just doesn't know when to stop.



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We need to give it a strategy to decide how far to go.

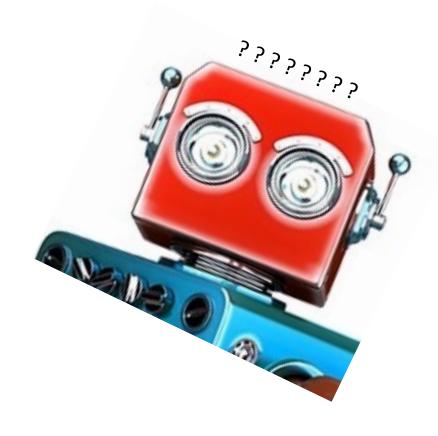


#### I think beaches have:



Instagram color palette

### Strategy 1: Use as few features as you can.



#### I think beaches have:



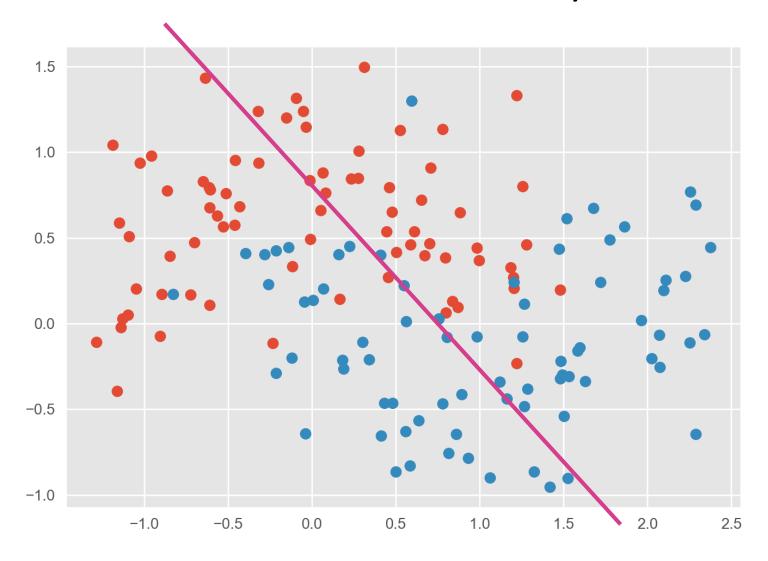
Penalize: loss, but also total parameter magnitude

## Strategy 2: Keep checking other data



Initial decision boundary

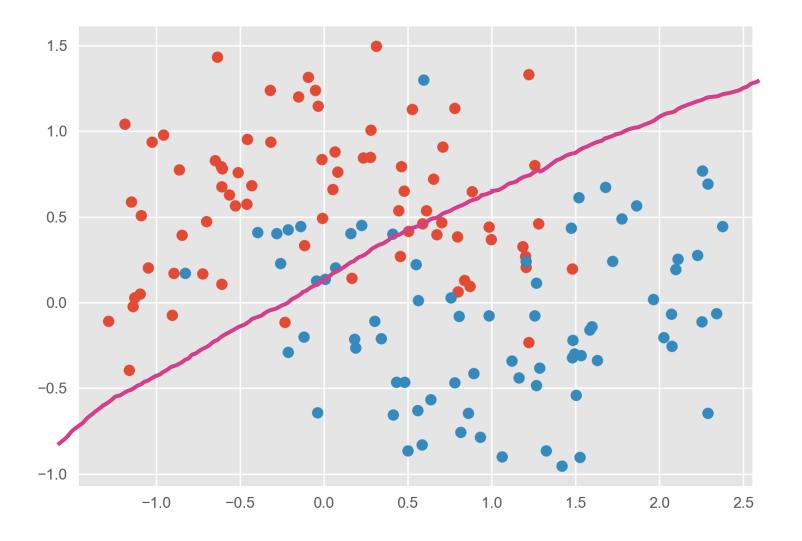
(epoch 0)



Updated decision boundary

(epoch 1)

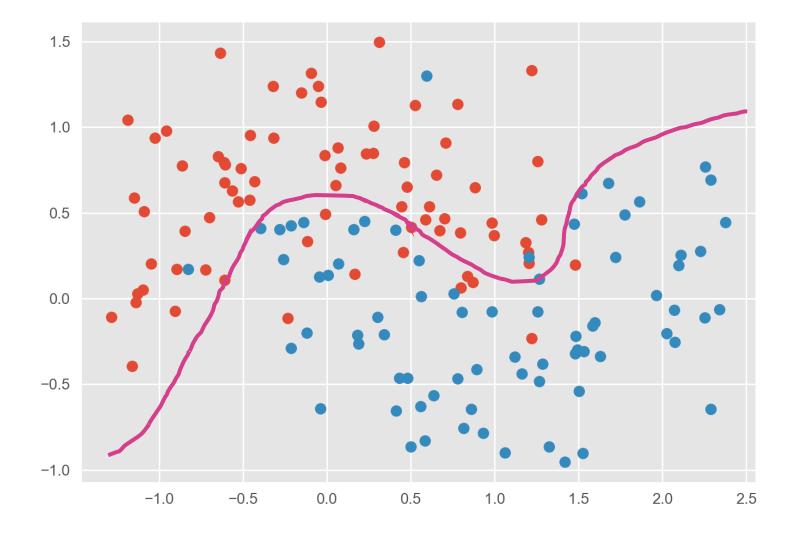
<u>Sure.</u>



Updated decision boundary

(epoch 4)

Wow!

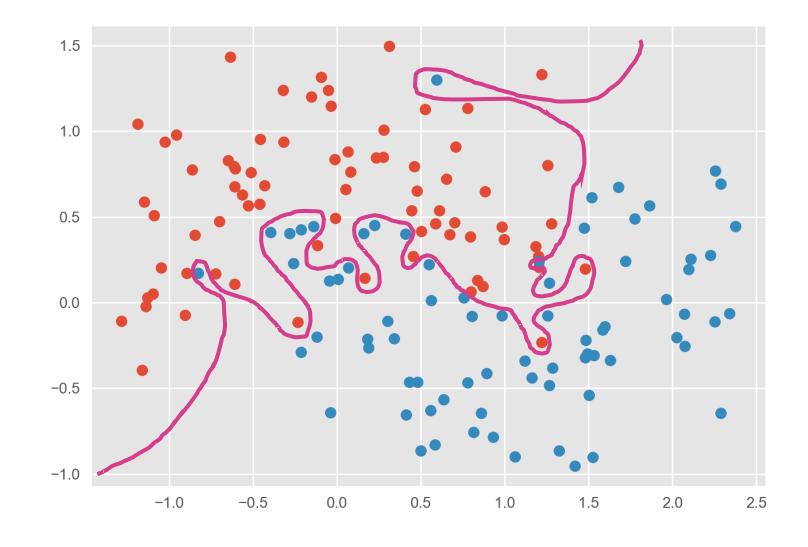


Updated decision boundary

(epoch 23)

Uh... let's dial it back.

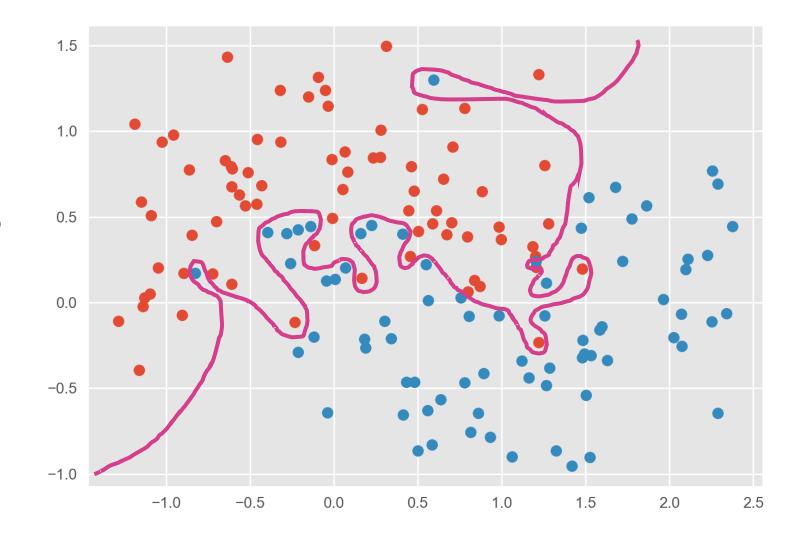
Just like our robot, it doesn't know when to stop.



#### We need a strategy to decide when to stop.

Strategy 1: Penalize complexity (regularization)

We could quantify how curvy the line is and add that value to the loss.



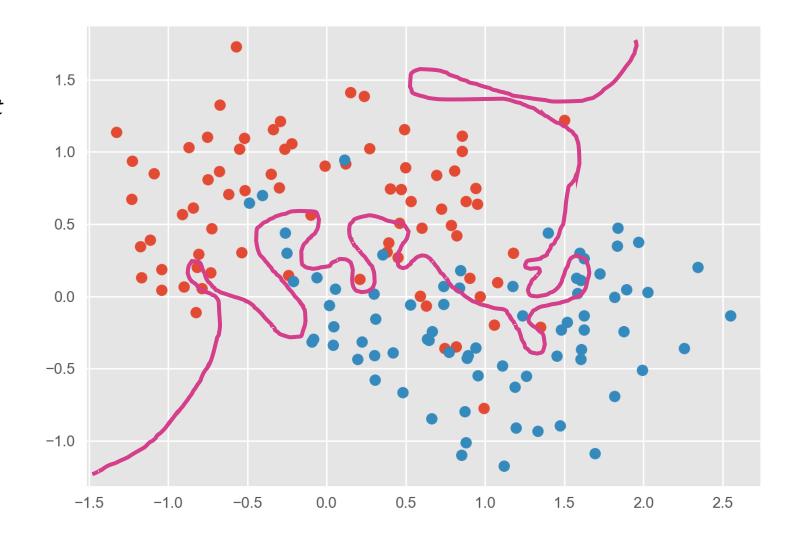
#### We need a strategy to decide when to stop.

Strategy 2:

Keep checking the validation set

(early stopping)

When our boundary no longer works well on new data, we know we've gone too far.



#### Strategy 1: Explicit Regularization

- We add a term to the loss (L) that quantifies complexity
- By minimizing the loss, we're now striking a balance between two competing objectives:
  - 1. Improve goodness of fit (i.e. reduce cross-entropy loss *H*)
  - 2. Limit complexity (i.e. reduce regularization term R)
- The hyperparameter  $\lambda$  controls how much we care about (1) vs (2)

$$L = H + \lambda R$$

### Examples of Explicit Regularization

- L2 (i.e. *ridge*) regularization:  $R = \sum_{i} \beta_{i}^{2}$
- In other words, we penalize the sum of squares of parameters
- Common in linear models and in neural networks

$$L = H + \lambda R$$

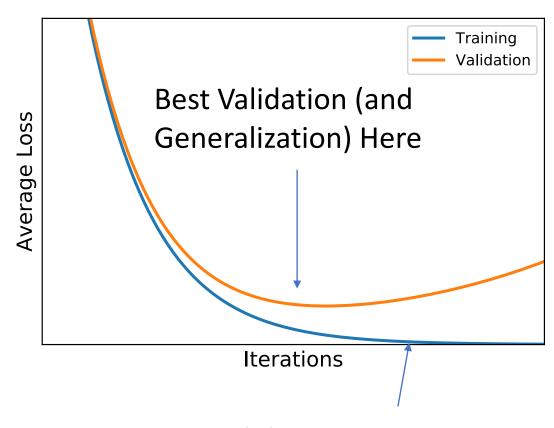
#### Examples of Explicit Regularization

- L1 (i.e. *LASSO*) regularization:  $R = \sum_{i} |\beta_{i}|$
- In other words, we penalize the sum of absolute values of parameters
- Common in linear models; less so in neural networks
- Tends to shrink many parameters to 0
  - This may be viewed as a form of feature selection
  - This also improves interpretability

$$L = H + \lambda R$$

### Strategy 2: Early Stopping

- During optimization, we can check the validation loss as we go.
- Instead of optimizing to convergence, we can optimize until the *validation* loss stops improving
  - Saves computational cost
  - Performs better on validation (and test) sets
- Widely used technique



Training Loss Keeps Improving

#### Strategy 3: Dropout

- Exclusive to neural networks
- During training, we set some hidden features to zero at random (different features for each training step)
- This has a dual effect:
  - Parameter shrinkage (similar to L2)
  - Encourages redundancy / redundant features; in other words, the network must model the relationship between x and y in multiple ways

### Mitigating Overfitting in Practice

- Machine learning almost always uses some form of regularization and/or early stopping
- Very common to use multiple forms at once
  - Dropout + early stopping in neural networks
  - Combination of L1 and L2 regularization in linear models (i.e. elastic net)
- The validation set is the key: used to choose between strategies
- You will see this when working on data science projects.

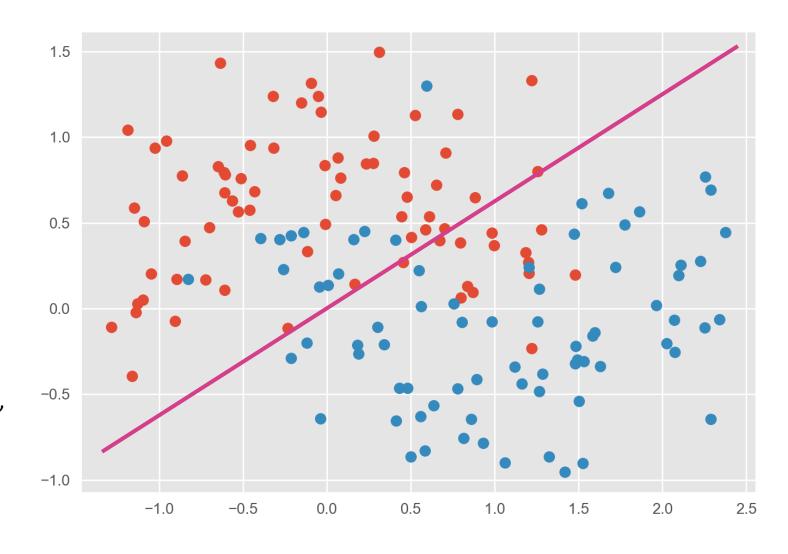
#### Linear models can also overfit!!! (How?)

#### Linear decision boundary

In this scenario -> (# points >> # predictors) it is not possible.

However, as # points approaches # predictors, we will see overfitting.

And for # points  $\leq$  # predictors (assuming linear independence), we can memorize the dataset.



# Scenarios

How to mitigate overfitting?

### Scenario 1: Interpretable CDP

 You are building a clinical decision support system using variables from structured EHR fields

 You have a thousand predictors and a few thousand data points (i.e. patients) in your training set

 You want it to be easy for providers to understand how the model works, and what features are important

#### Scenario 2: Pure prediction

 You are building a neural network-based model that identifies nicotine withdrawal from digital health data

 Your input data is a high-dimensional time series of physiologic measurements from multiple sensors

 There is no need to interpret or explain the model: you care only about out-of-sample performance

# Overfitting in linear models

(time permitting)

### Suppose we have the following data

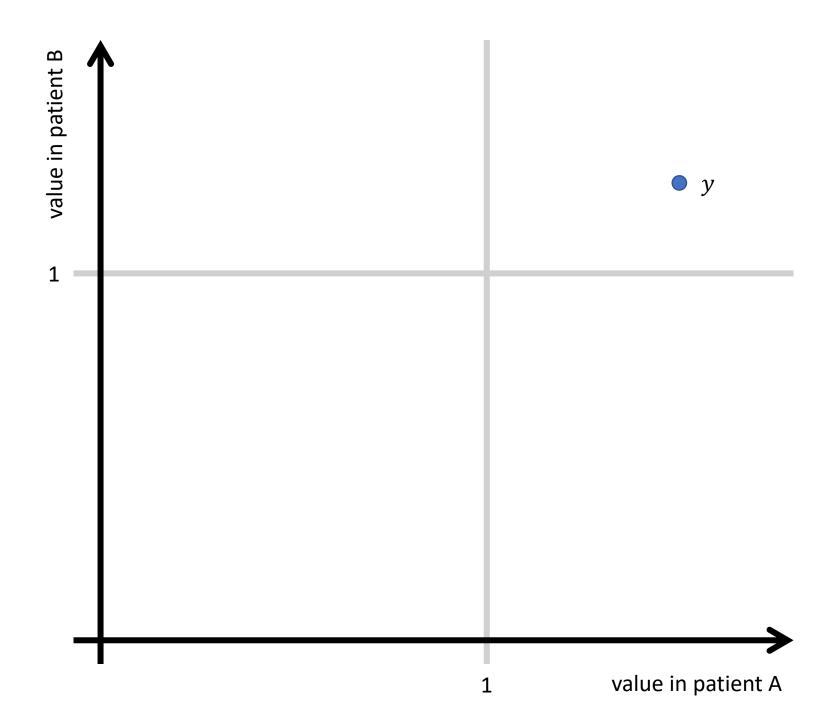
Patient	Predictor 1 (numeric)	Predictor 2 (numeric)	Outcome (numeric)
Α	.5	.75	1.5
В	1	.75	1.25

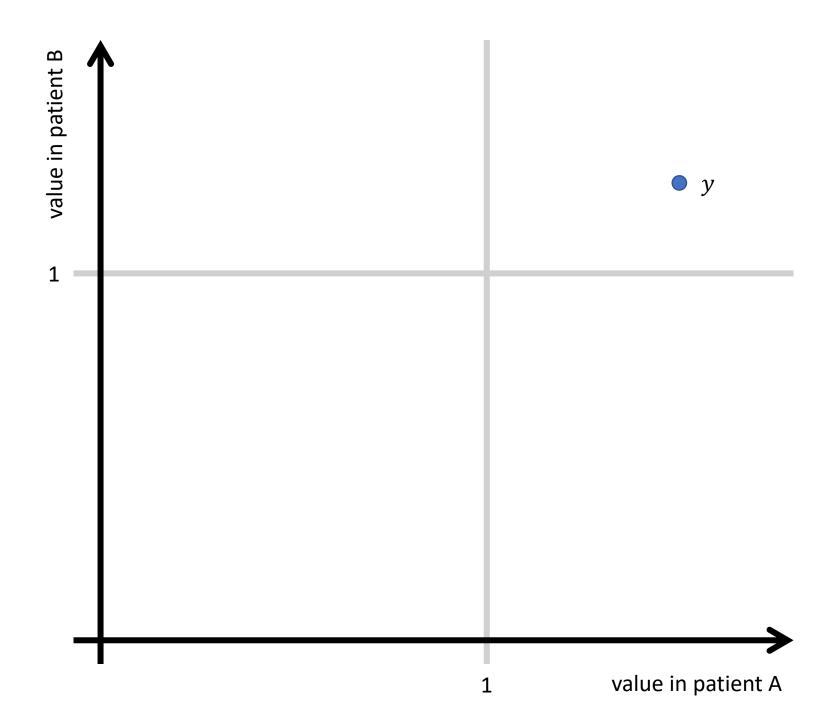
> Goal: find the linear equation that best predicts the outcome

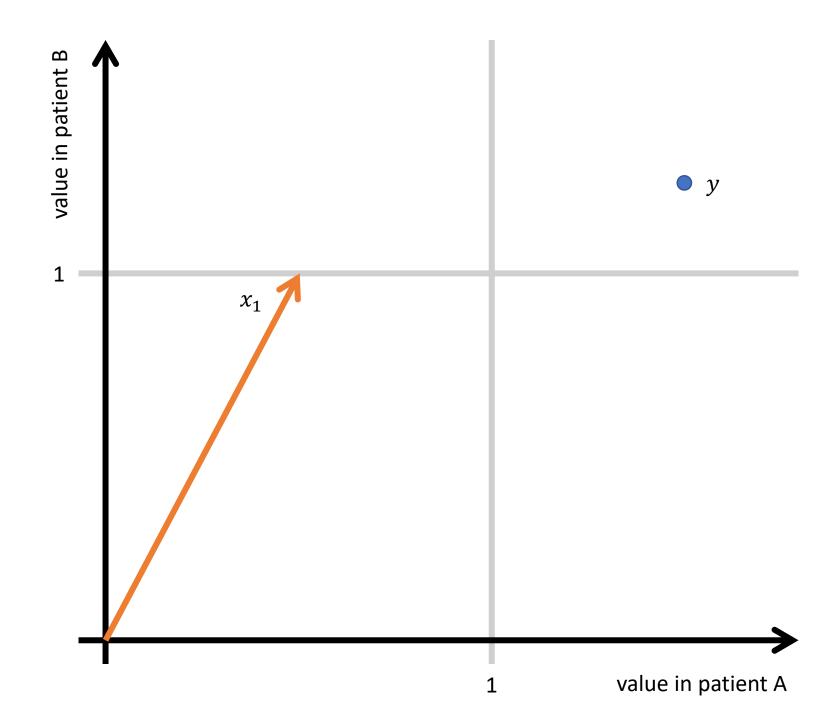
Patient	$x_1$	$\boldsymbol{x}_2$	y
Α	.5	.75	1.5
В	1	.75	1.25

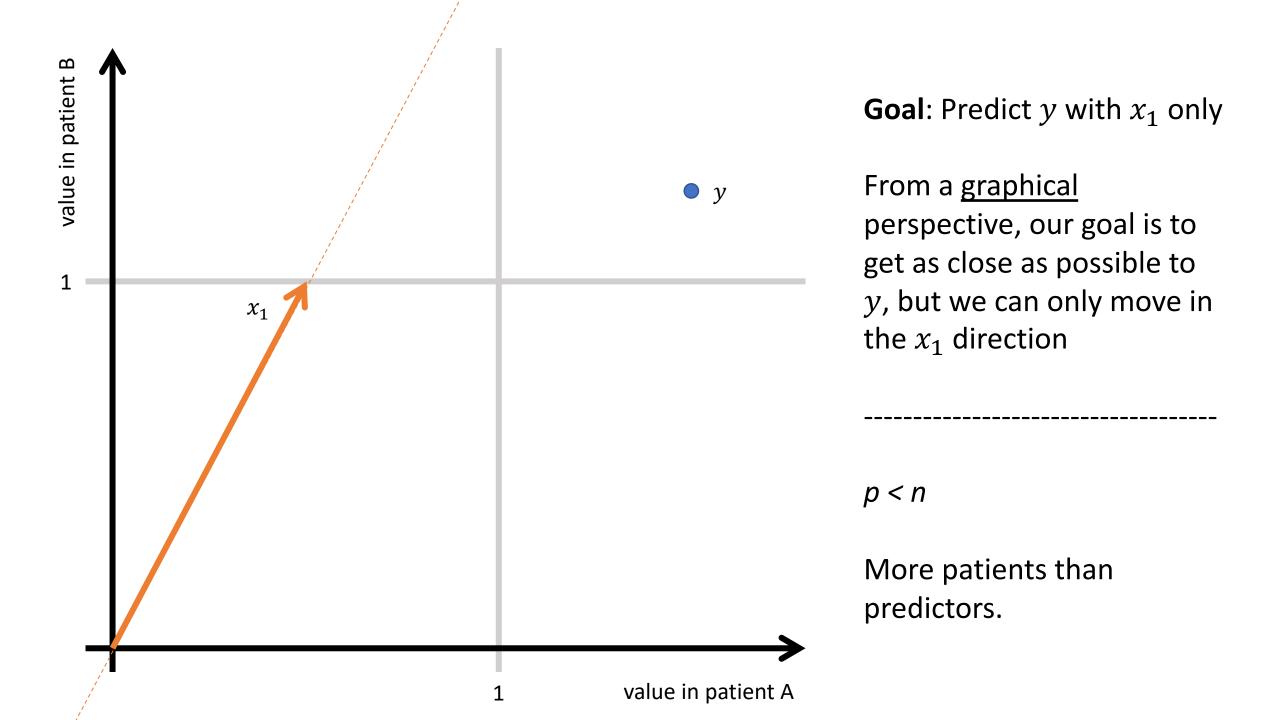
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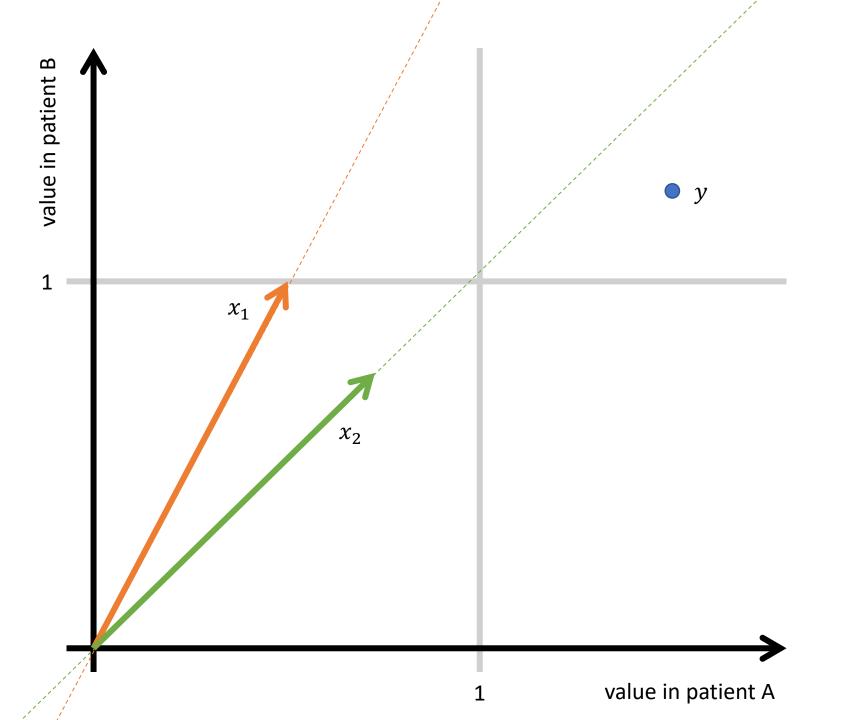
$$b_1 \boldsymbol{x}_1 + b_2 \boldsymbol{x}_2 = \boldsymbol{y}$$











**Goal**: Predict y with  $x_1$ ,  $x_2$ 

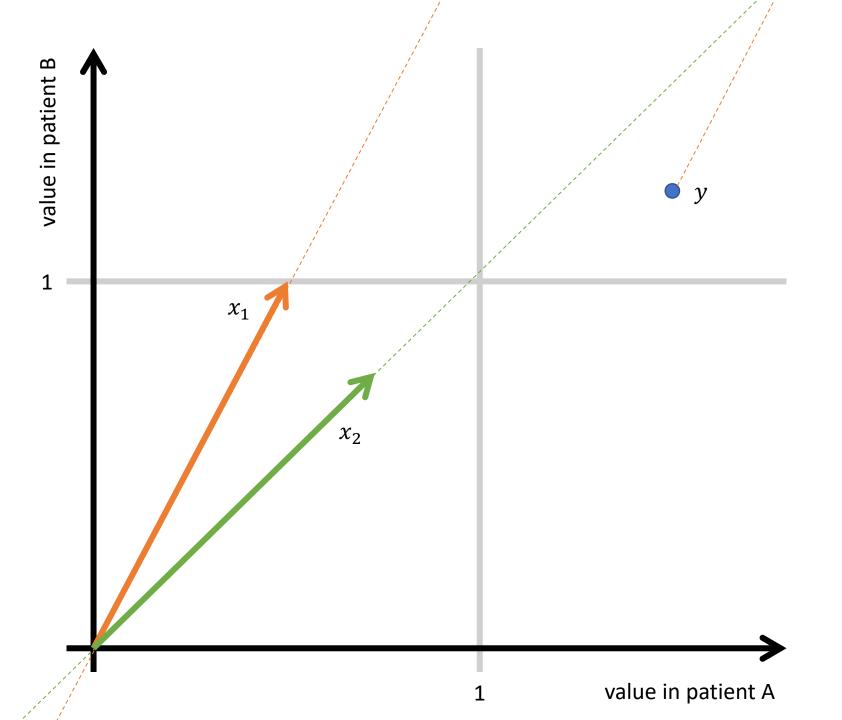
From a graphical perspective, our goal is to get as close as possible to y. We can now move in both the  $x_1$  direction and the  $x_2$  direction.

-----

p = n

Can always\* predict perfectly on training set

<sup>\*</sup>assuming linearly independent predictors



**Goal**: Predict y with  $x_1$ ,  $x_2$ 

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\_\_\_\_\_

p = n

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### Takeaways

 When # points ≤ # predictors, we can get perfect predictions (i.e. memorize the dataset)

However, this typically requires very large model coefficients

 Regularization therefore prevents this behavior, and therefore tends to give us better generalization (i.e. out of sample) performance

# Cross-Validation

(time permitting)

## Traditional "split" for development + eval



#### Cross validation: rotate the test set

Fold 1 Fold 2 Fold 3 Fold 4 Fold 5

Round 1: Train on 1-4, test on 5

Round 2: Train on all but 4, test on 4

Round 3: Train on all but 3, test on 3

Round 4: Train on all but 2, test on 2

Round 5: Train on 2-5, test on 1

Why would we do this?

- More data for the evaluation
- Better estimate of out-of-sample performance

#### What happened to the validation set?

- Use "flat" cross-validation (below) versus "nested" cross-validation
- Both give unbiased estimates and flat is easier



Round 1: Train on 1-3, validate on 4, test on 5

Round 2: Train on 2-4, validate on 5, test on 1

Round 3: Train on 3-5, validate on 1, test on 2

Round 4: Train on 4, 5, and 1; validate on 2, test on 3

Round 5: Train on 5, 1, and 2; validate on 3, test on 4