# Parameter estimation of binary black hole systems using numerical relativity surrogates and a rapid inference framework

Feroz Hussain Shaik

Dept. of Physics, UMass Dartmouth

APS New England Fall 2018 Meeting April 24, 2019

/home/frz/WORK/be

Ongoing MS Thesis Project supervised by

Scott Field (UMass Dartmouth)

Joint work with

- Jacob Lange (RIT) (RIFT+ILE)
- Richard O'Shaughnessy (RIT) (RIFT+ILE)
- Vijay Varma (Caltech) (NR Surrogate Model)

### Introduction

### **GW** Parameter Estimation

- Figuring out what are the properties of the binary sources using the data
- Usually minimum 15 parameters required

### Introduction

### **GW** Parameter Estimation

- Figuring out what are the properties of the binary sources using the data
- Usually minimum 15 parameters required

#### Parameters include

- Masses and spins of black holes
- Luminosity distance to binary  $D_L$
- Inclination angle  $\iota$
- RA and dec (position in sky)
- ..and so on

### Introduction

Why do we need parameter estimation?

- Accurate parameter estimation required for science (eg. population studies, tests of GR)
- Fast algorithms can help follow-up observations

# Bayes' Theorem

Updating and maximizing our knowledge from the data and our prior belief

$$p_{post}(\lambda, \theta) = \frac{\mathcal{L}(\lambda, \theta)p(\theta)p(\lambda)}{\int d\lambda d\theta \mathcal{L}(\lambda, \theta)p(\lambda)p(\theta)}$$

- Posterior  $p_{post}$  probability of parameter value to be correct given the data. This is what we are looking for
- $\bullet$  Likelihood  ${\cal L}$  probability of data assuming model is true i.e. how well does the model parameter fit the data
- ullet Prior  $p( heta)p(\lambda)$  what we think the model parameter PDF looks like
- Evidence normalization constant, important for model selection

# Bayes' Theorem

Updating and maximizing our knowledge from the data and our prior belief

$$p_{post}(\lambda, \theta) = \frac{\mathcal{L}(\lambda, \theta)p(\theta)p(\lambda)}{\int d\lambda d\theta \mathcal{L}(\lambda, \theta)p(\lambda)p(\theta)}$$

- $\bullet$   $\lambda$  Intrinsic parameters, describes dynamics of binary
- ullet Extrinsic parameters, describes space and time orientation

### Models

### Templates for aligned spin

- SEOBNRv4 Effective-one-body model
- IMRPhenomD
- Numerical Relativity (NR) simulations solving Einstein's equations on a computer. Very expensive to compute, but gives most accurate results

### Models

### Templates for aligned spin

- SEOBNRv4 Effective-one-body model
- IMRPhenomD
- Numerical Relativity (NR) simulations solving Einstein's equations on a computer. Very expensive to compute, but gives most accurate results
- Surrogate models

## Surrogate Models

- Fast and accurate evaluation using reduced order modeling (ROM)
- No assumptions of underlying model
- Will converge to the model by improving representation
- Need to specify model and range of parameters
- Non-intrusive
- gwsurrogate Publicly available package

# NR Surrogate Models

### NRHybSur3dq8

- Aligned spin hybrid model made by stitching together PN for early inspiral, NR simulation for the rest
- ullet Contains higher modes upto Imax  $\leq 5$
- Training region:  $1 \le q \le 8$ ,  $0.8 \le \chi_{1z/2z} \le 0.8$ .

# NRHybSur3dq8

ModelErrors.png

# NRHybSur3dq8

SurrogateTrainingSet.png

### LALInference (LIGO)

- Using variants of optimized MCMC and nested sampling
- Well-tested and reliable
- Doesn't scale well to massive (>1000) core counts
- Model must be made available in LALSimulation (need low level C to interface)

### LALInference (LIGO)

- Using variants of optimized MCMC and nested sampling
- Well-tested and reliable
- Doesn't scale well to massive (>1000) core counts
- Model must be made available in LALSimulation (need low level C to interface)
- ILE (with RIFT extensions) (Pankow et al.(2015) and Lange et al.(2018))
  - Fast highly parallelized algorithm
  - Easily extended with other models (using Python)

### LALInference (LIGO)

- Using variants of optimized MCMC and nested sampling
- Well-tested and reliable
- Doesn't scale well to massive (>1000) core counts
- Model must be made available in LALSimulation (need low level C to interface)
- ILE (with RIFT extensions) (Pankow et al.(2015) and Lange et al.(2018))
  - Fast highly parallelized algorithm
  - Easily extended with other models (using Python)
- gwin (in development, Capano et al.)
  - Next gen python package for parameter estimation

### ILE+RIFT

- Specify and separate intrinsic and extrinsic parameters
- Lay out grid on intrinsic parameters
- Independent, Parallelized, Log-Likelihood calculation over each grid point using Monte Carlo Integration and marginalization of extrinsic parameters
- Gaussian Process Regression to interpolate over grid points with high likelihood
- Setup for next iteration over new interpolated grid

### **MGHPCC**

Massachusetts Green High Performance Computing Center

- Developed as a joint venture of Boston University, Harvard, MIT,
  Northeastern, and the University of Massachusetts system
- Can be accessed by UMass students under participating faculty



Figure: The MGHPCC facility at Holyoke, Massachusetts

### Progress so far

- Interfacing the new model with the codebase
- Performing test runs on a local cluster at RIT
- Setting up the codebase at MGHPCC to begin PE runs

# **Preliminary Results**

- Preliminary is the key word here
- Signal injected and PE study done using same model
- Sparse grid, only 5 points per dimension
- SNR 20
- $m_1 = 56$
- $m_2 = 14$
- $\chi_{1z} = -0.5$
- $\chi_{2z} = 0.5$

mspin.png

mcetachiE.png

### Conclusion

### Remarks

- First PE study with this new model
- NR surrogates provide fast and accurate waveform models
- ILE+RIFT performs rapid parameter estimation using parallelized computation in order of hours

### Future Outlook

- Investigate effects of higher harmonic modes
- Understand bias in PE studies using statistical techniques
- Compare with other models