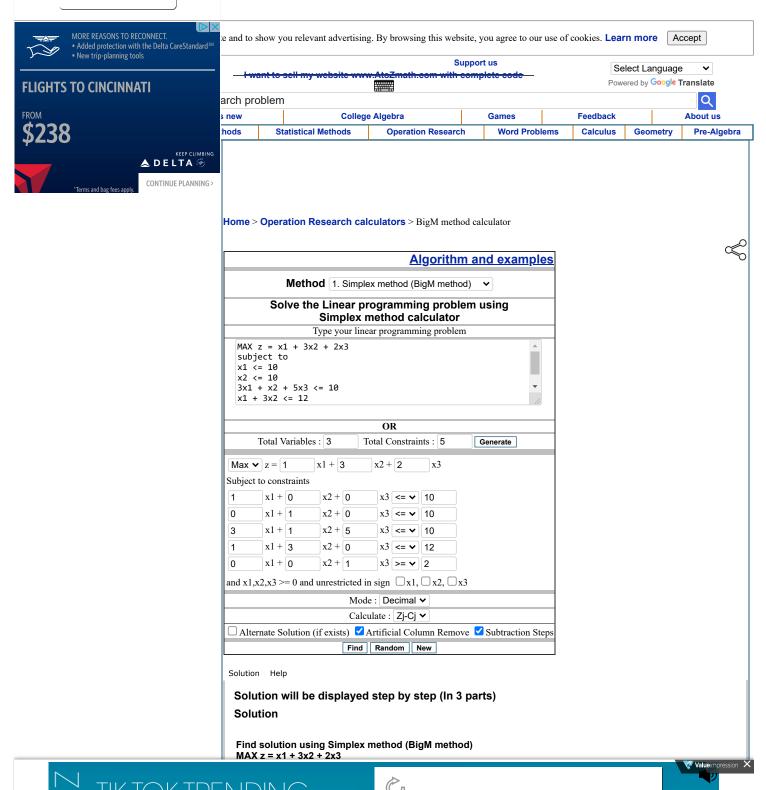


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$$3x_1 + x_2 + 5x_3 \le 10$$

 $x_1 + 3x_2 \le 12$
 $x_3 \ge 2$
and $x_1, x_2, x_3 \ge 0$;

The problem is converted to canonical form by adding slack, surplus and artificial variables as appropiate

- 1. As the constraint-1 is of type ' \leq ' we should add slack variable S_1
- 2. As the constraint-2 is of type ' \leq ' we should add slack variable S_2
- 3. As the constraint-3 is of type ' \leq ' we should add slack variable S_3
- 4. As the constraint-4 is of type ' \leq ' we should add slack variable S_4
- 5. As the constraint-5 is of type ' \geq ' we should subtract surplus variable S_5 and add artificial variable A_1

After introducing slack, surplus, artificial variables

subject to
$$x_1 + S_1 = 10$$

$$x_2 + S_2 = 10$$

$$3x_1 + x_2 + 5x_3 + S_3 = 10$$

$$x_1 + 3x_2 + S_4 = 12$$

$$x_3 - S_5 + A_1 = 2$$
 and
$$x_1, x_2, x_3, S_1, S_2, S_3, S_4, S_5, A_1 \ge 0$$

and $x_1, x_2, x_3, S_1, S_2, S_3, S_4, S_5, A_1 \ge 0$

Iteration-1		C_{j}	1	3	2	0	0	0	0	0	-M	
В	C_B	X_{B}	<i>x</i> ₁	x ₂	<i>x</i> ₃	<i>S</i> ₁	S ₂	S ₃	S ₄	S ₅	A_1	MinRatio $\frac{X_B}{X_3}$
S_1	0	10	1	0	0	1	0	0	0	0	0	
S_2	0	10	0	1	0	0	1	0	0	0	0	
S_3	0	10	3	1	5	0	0	1	0	0	0	$\frac{10}{5} = 2$
S_4	0	12	1	3	0	0	0	0	1	0	0	
A_1	-M	2	0	0	(1)	0	0	0	0	- 1	1	$\frac{2}{1} = 2 \longrightarrow$
z = -2M		Z_{j}	0	0	-M	0	0	0	0	М	-M	
		Z_j - C_j	-1	-3	-M - 2 ↑	0	0	0	0	М	0	

Negative minimum Z_i - C_i is -M - 2 and its column index is 3. So, the entering variable is x_3 .

Minimum ratio is 2 and its row index is 5. So, the leaving basis variable is A_1 .

∴ The pivot element is 1.

Entering = x_3 , Departing = A_1 , Key Element = 1

 $+ R_5(\text{new}) = R_5(\text{old})$









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Iteration-2		C_j	1	3	2	0	0	0	0	0	
В	<i>C</i> _B	X_B	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> ₃	<i>S</i> ₁	S ₂	S ₃	S_4	S ₅	MinRatio $\frac{X_B}{x_2}$
S_1	0	10	1	0	0	1	0	0	0	0	
S_2	0	10	0	1	0	0	1	0	0	0	$\frac{10}{1} = 10$
S_3	0	0	3	(1)	0	0	0	1	0	5	$\frac{0}{1} = 0 \longrightarrow$
S_4	0	12	1	3	0	0	0	0	1	0	$\frac{12}{3} = 4$
x_3	2	2	0	0	1	0	0	0	0	-1	
z = 4		Z_j	0	0	2	0	0	0	0	-2	
		Z_j - C_j	-1	-3 ↑	0	0	0	0	0	-2	

Negative minimum Z_i - C_j is -3 and its column index is 2. So, the entering variable is x_2 .

Minimum ratio is 0 and its row index is 3. So, the leaving basis variable is S_3 .

∴ The pivot element is 1.

Entering $= x_2$, Departing $= S_3$, Key Element = 1

- $+ R_3(\text{new}) = R_3(\text{old})$
- $+ R_1(\text{new}) = R_1(\text{old})$
- $+ R_2(\text{new}) = R_2(\text{old}) R_3(\text{new})$
- $+ R_4(\text{new}) = R_4(\text{old}) 3R_3(\text{new})$
- $+ R_5(\text{new}) = R_5(\text{old})$

	C_{j}	1	3	2	0	0	0	0	0	
C_B	X_B	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> ₃	<i>S</i> ₁	S ₂	S ₃	S ₄	S ₅	MinRatio
0	10	1	0	0	1	0	0	0	0	
0	10	-3	0	0	0	1	- 1	0	-5	
3	0	3	1	0	0	0	1	0	5	
0	12	-8	0	0	0	0	-3	1	-15	
2	2	0	0	1	0	0	0	0	-1	
	0 0 3 0	C _B X _B 0 10 0 10 3 0 0 12	$ \begin{array}{c ccccc} & C_j & 1 \\ \hline & C_B & X_B & x_1 \\ \hline & 0 & 10 & 1 \\ \hline & 0 & 10 & -3 \\ \hline & 3 & 0 & 3 \\ \hline & 0 & 12 & -8 \\ \hline $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	C_B X_B x_1 x_2 x_3 S_1 S_2 S_3 S_4 0 10 1 0 0 1 0 0 0 0 10 -3 0 0 0 1 -1 0 3 0 3 1 0 0 0 1 0 0 12 -8 0 0 0 0 -3 1	C_B X_B x_1 x_2 x_3 S_1 S_2 S_3 S_4 S_5 0 10 1 0 0 1 0 0 0 0 10 -3 0 0 0 1 -1 0 -5 3 0 3 1 0 0 0 1 0 5 0 12 -8 0 0 0 -3 1 -15







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