

Figure 1: Dynamic Bayesian network

1 Exercises

Exercise 1.1 *Markov Assumption.* If a dynamic system X satisfies the Markov assumption for all time $t \geq 0$, which of the following statements must be true? You may select 1 or more options, or none of them.

- a) $X^{(t+1)} \perp\!\!\!\perp X^{(t)}$
- b) $X^{(t+1)} \perp\!\!\!\perp X^{(t)} | X^{(t-1)}$
- c) $X^{(t+1)} \perp\!\!\!\perp X^{(0:(t-1))} | X^{(t)}$

Exercise 1.2 *Independencies in DBNs.* In the DBN of Figure 1, which of the following independence assumptions are true? You may select 1 or more options, or none of them.

- a) $O^{(t)} \perp\!\!\!\perp X^{(t+1)} | X^{(t)}$
- b) $O^{(t)} \perp\!\!\!\perp X^{(t-1)} | X^{(t)}$
- c) $O^{(t)} \perp\!\!\!\perp O^{(t-1)}$
- d) $O^{(t)} \perp\!\!\!\perp O^{(t-1)} | X^{(t)}$

Exercise 1.3 *Applications of DBNs.* For which of the following applications might one use a DBN (i.e. the Markov assumption is satisfied)? You may select 1 or more options, or none of them.

- a) Modeling data taken at different locations along a road, where the data at each location is influenced by the data at many other locations.
- b) Predicting the probability that today will be a snow day (school will be closed because of the snow), when this probability depends only on whether yesterday was a snow day.
- c) Predicting the probability that today will be a snow day (school will be closed because of the snow), when this probability depends only on whether yesterday, the day before yesterday, and 2 Mondays ago were snow days.
- d) Modeling time-series data, where the events at each time-point are influenced by only the events at the one time-point directly before it

Exercise 1.4 *Plate Semantics.* Let A and B be random variables inside a common plate indexed by i . Which of the following statements must be true? You may select 1 or more options, or none of them.

- a) For each i , $A(i)$ and $B(i)$ have different CPDs.
- b) For each i , $A(i)$ and $B(i)$ have edges connecting them to the same variables outside of the plate.
- c) For each i , $A(i)$ and $B(i)$ have the same CPDs.
- d) There is an instance of A and an instance of B for every i .

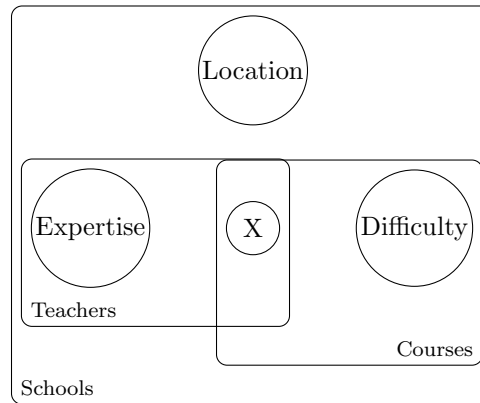


Figure 2: Plate model without edges for schools

Exercise 1.5 *Plate Interpretation.* Consider the plate model of Figure 2 (with edges removed). Which of the following might a given instance of X possibly represent in the grounded model? You may select 1 or more options, or none of them.

- a) Whether a specific teacher T taught a specific course C at school S
- b) Whether someone with expertise E taught something of difficulty D at a place in location L
- c) Whether a specific teacher T is a tough grader
- d) None of these options can represent X in the grounded model
- e) Whether a teacher with expertise E taught a course of difficulty D

Exercise 1.6 *Grounded Plates.* Consider the plate model of Figure 2 and assume that there are s schools, t teachers and c courses in each school. How many instances of the Difficulty variable are there?

- a) c
- b) $s \cdot c$
- c) Not enough information to answer
- d) $s \cdot t$

Exercise 1.7 *Plate models.* Consider the plate model of Figure 3. Assume we are given K Markets, L Products, M Consumers and N Locations. Which is the total number of instances of the variable P in the grounded BN?

- a) $K \cdot (L + M)$
- b) $L \cdot M$
- c) $K \cdot L \cdot M$
- d) $K \cdot (N + (L \cdot M))$
- e) $K + L + M$

Exercise 1.8 *Plate interpretation.* Consider the plate model of Figure 3. What might P represent?

- a) Whether a specific product PR was consumed by consumer C in market M

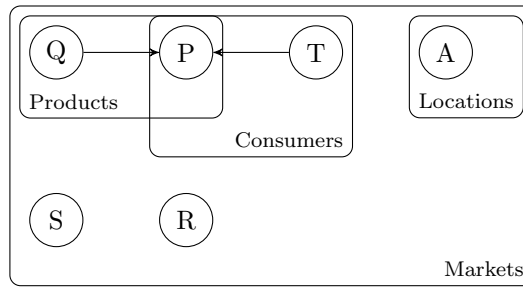


Figure 3: Plate model *market*

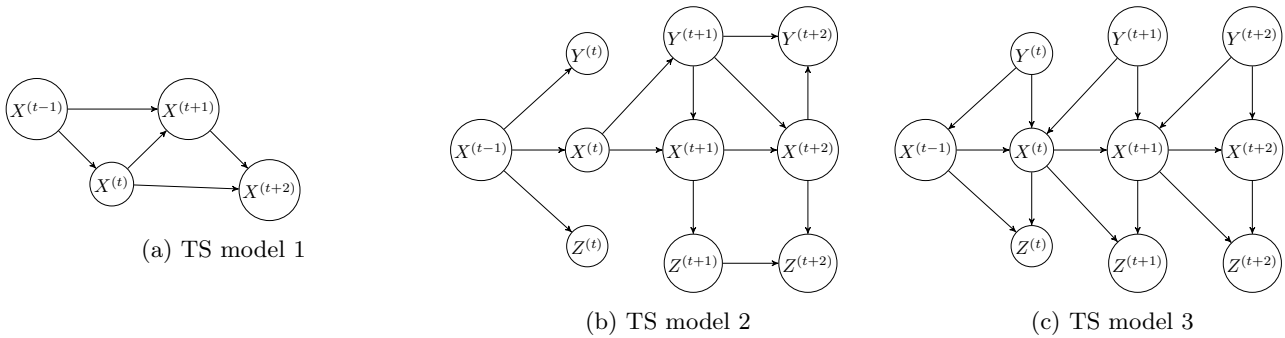


Figure 4: Different TS models

- b) Whether a specific product PR was consumed by consumer C in market M that is supervised by supervisor S (assuming that there is exactly 1 unique supervisor per market) and has target audience R (assuming that there is exactly a unique target audience per market)
- c) Whether a specific product PR was consumed by consumer C in all markets
- d) Whether a specific product of brand Q was consumed by a consumer with age T in a market of type M

Exercise 1.9 *Graphs for time series modeling. Which of the graphs in Figure 4 satisfies the Markov assumption? You may select 1 or more options, or none of them.*

- a) 4a
- b) 4b
- c) 4c

Exercise 1.10 *Grounded plates. Which graph in Figure 5 is a valid grounded model for the plate 5d? You may select 1 or more options, or none of them.*

- a) 5a
- b) 5b
- c) 5c

Exercise 1.11 *Unrolling DBNs. In Figure 6 there are several 2-TBNs that could be unrolled into DBNs. Consider these unrolled DBNs (note that there are no edges within the first time-point). In which of them will $(X(t) \perp\!\!\!\perp Z(t) | Y(t))$ hold for all t , assuming $Obs(t)$ is observed for all t and $X(t)$ and $Z(t)$ are never observed? You may select 1 or more options, or none of them.*

Hint: Unroll these 2-TBNs into DBNs that are at least 3 time steps long (i.e., involving variables from $t-1, t, t+1$)

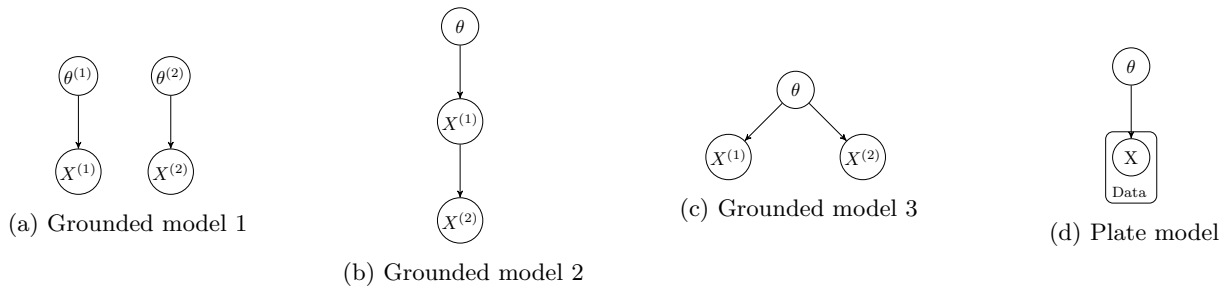


Figure 5: Different grounded models

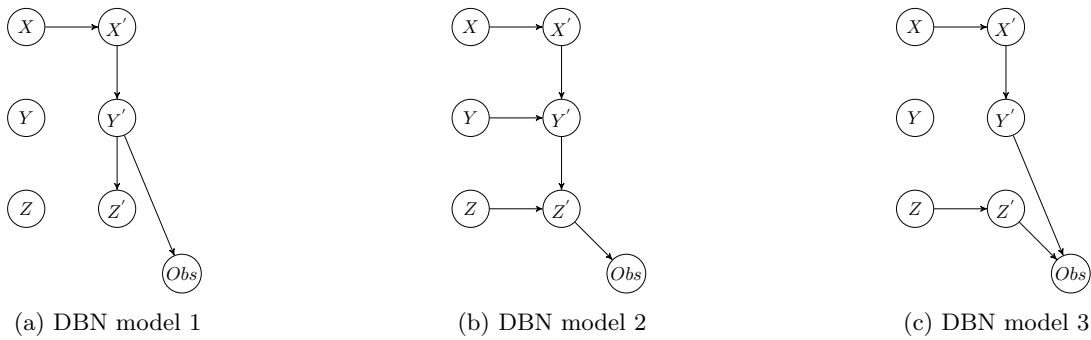


Figure 6: Different DBN models

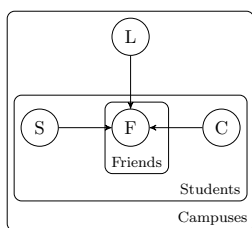
- a) 6a
- b) 6b
- c) 6c

Exercise 1.12 *Plate interpretation. Consider the following scenario:*

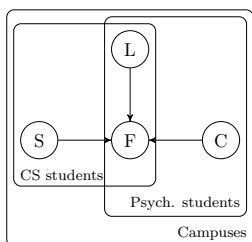
On each campus there are Computer Science and Psychology students. We have a binary variable for whether the campus is large, a binary variable for whether the CS student is shy, a binary variable for whether the Psychology student likes computers, and a binary variable for whether the Computer Science student and the Psychology student are friends.

Which of the following plate models can represent this scenario?

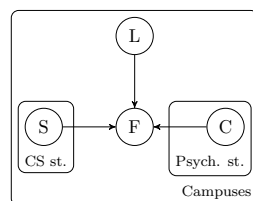
- a) Figure 7a
- b) Figure 7b
- c) Figure 7c
- d) Figure 7d



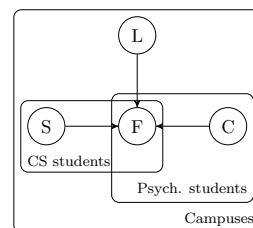
(a) Plate model 1



(b) Plate model 2



(c) Plate model 3



(d) Plate model 4

Figure 7: Different plate models

Answers

Ex. 1.1: c

Ex. 1.2: a, b, d

Ex. 1.3: b, d

Ex. 1.4: d

Ex. 1.5: a

Ex. 1.6: b

Ex. 1.7: c

Ex. 1.8: a

Ex. 1.9: b

Ex. 1.10: c

Ex. 1.11: a

Ex. 1.12: d