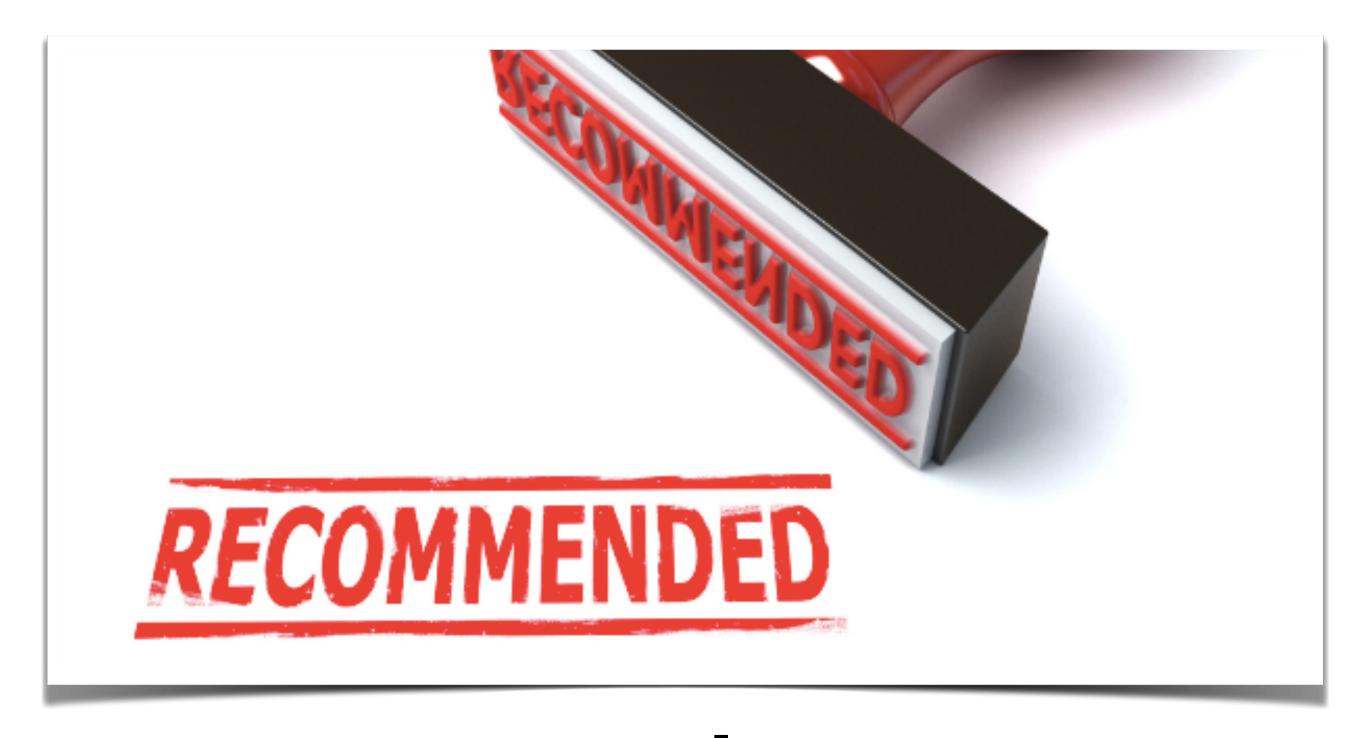




Master on Foundations of Data Science



Recommender Systems

Collaborative Recommender Systems: Factorization Models meets Factorization Machines

Matrix Factorization Hybrid Models

Matrix Factorization with side features

Side (or content) features can be useful for 1) cold-start problem and 2) extra information about items/users

Side features can be attributes (e.g. demographics) or implicit feedback.

Bias term for occupation

$$\hat{r}_{ui} = b + b_i + b_u + p_u q_i^T + q_i t_o + b_o$$

Side term for occupation



Matrix Factorization with temporal features

Matrix factorization models have been static. However, in reality, **item**popularity and user preferences change constantly.

We should account for the temporal effects reflecting the dynamic nature of user-item interactions

We can add a temporal term that affects user preferences and, therefore, the interaction between users and item

User factor a a function of time $\hat{r}_{ui} = b + b_i + b_u + p_u q_i^T + p_u t_o + p_u(t)$



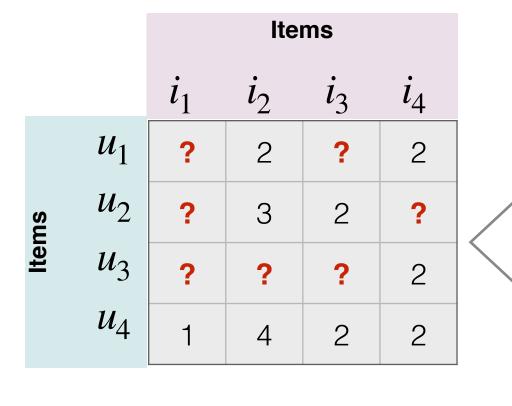
Factorization machines

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... factorization machines using such feature vectors as input data are related to specialized state-of-the-art factorization ... between factorization machines and support vector machines as ...

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Our Data





u4

One-hot-encoding



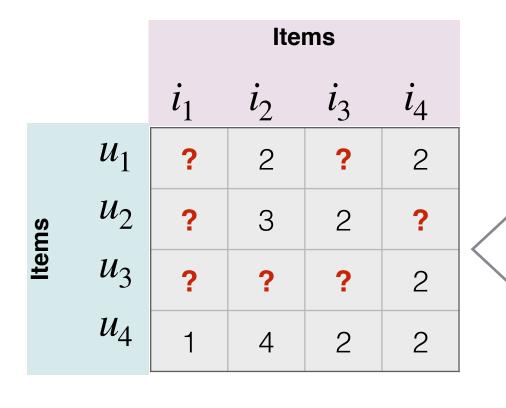
1	1	0	0	0	0	1	0	0	2
2	1	0	0	0	0	0	0	1	2
3	0	1	0	0	0	1	0	0	3
4	0	1	0	0	0	0	1	0	2
5	0	0	1	0	0	0	0	1	2
6	0	0	0	1	1	0	0	0	1
7	0	0	0	1	0	1	0	0	4
8	0	0	0	1	0	0	1	0	2
9	0	0	0	1	0	0	0	1	2





Linear Models

$$\hat{y} = w_0 + \sum_{j=1}^{N} w_j x_j$$



	1	u1	i2	2
	2	u1	i4	2
	3	u2	i2	3
	4	u2	i3	2
>	5	u3	i4	2
	6	u4	i1	1
	7	u4	i2	4
	8	u4	i3	2
	9	u4	i4	2

One-hot-encoding



1	1	0	0	0	0	1	0	0	2
2	1	0	0	0	0	0	0	1	2
3	0	1	0	0	0	1	0	0	3
4	0	1	0	0	0	0	1	0	2
5	0	0	1	0	0	0	0	1	2
6	0	0	0	1	1	0	0	0	1
7	0	0	0	1	0	1	0	0	4
8	0	0	0	1	0	0	1	0	2
9	0	0	0	1	0	0	0	1	2



Polynomial Models

$$\hat{y} = w_0 + \sum_{j=1}^{N} w_j x_j + \sum_{j=1}^{N} \sum_{k=j+1}^{N} x_j x_k v_{jk}$$

Model parameters w_0 , $\mathbf{w} \in \mathbb{R}^n$, $\mathbf{V} \in \mathbb{R}^{n \times n}$



$$\hat{y} = w_0 + \sum_{j=1}^{N} w_j x_j + \sum_{j=1}^{N} \sum_{k=j+1}^{N} x_j x_k < \mathbf{v}_j, \mathbf{v}_k >$$

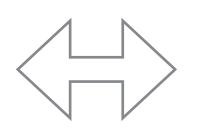
Model parameters w_0 , $\mathbf{w} \in \mathbb{R}^n$, $\mathbf{V} \in \mathbb{R}^{n \times k}$

$$\hat{y} = w_0 + \sum_{j=1}^{N} w_j x_j + \sum_{j=1}^{N} \sum_{k=j+1}^{N} x_j x_k \sum_{f=1}^{l} v_{fj} v_{fk}$$



Matrix Factorization vs. Factorization Machines

		Items						
		i_1	i_2	i_3	i_4			
	u_1	?	2	?	2			
Items	u_2	?	3	2	?			
	u_3	?	?	?	2			
	u_4	1	4	2	2			



1	1	0	0	0	0	1	0	0	2
2	1	0	0	0	0	0	0	1	2
3	0	1	0	0	0	1	0	0	3
4	0	1	0	0	0	0	1	0	2
5	0	0	1	0	0	0	0	1	2
6	0	0	0	1	1	0	0	0	1
7	0	0	0	1	0	1	0	0	4
8	0	0	0	1	0	0	1	0	2
9	0	0	0	1	0	0	0	1	2

$$\mathbf{x} = (0, \dots, 0, 1, 0, \dots, 0, 0, \dots, 0, 1, 0, \dots, 0)$$

If this is your data



(Biased) Matrix Factorization == Factorization Machines

$$\hat{y}(\mathbf{x}) = \hat{y}(u, i) = w_0 + w_u + w_i + \sum_{i=1}^k v_{u,j} v_{i,j}$$





FM and SVM

- FM combines the advantages of SVM and factorization models
- Good estimates interaction model with huge sparsity where SVM fail.
- Comparable to polynomial kernel in SVM, but works for very sparse data and much faster



• Example:

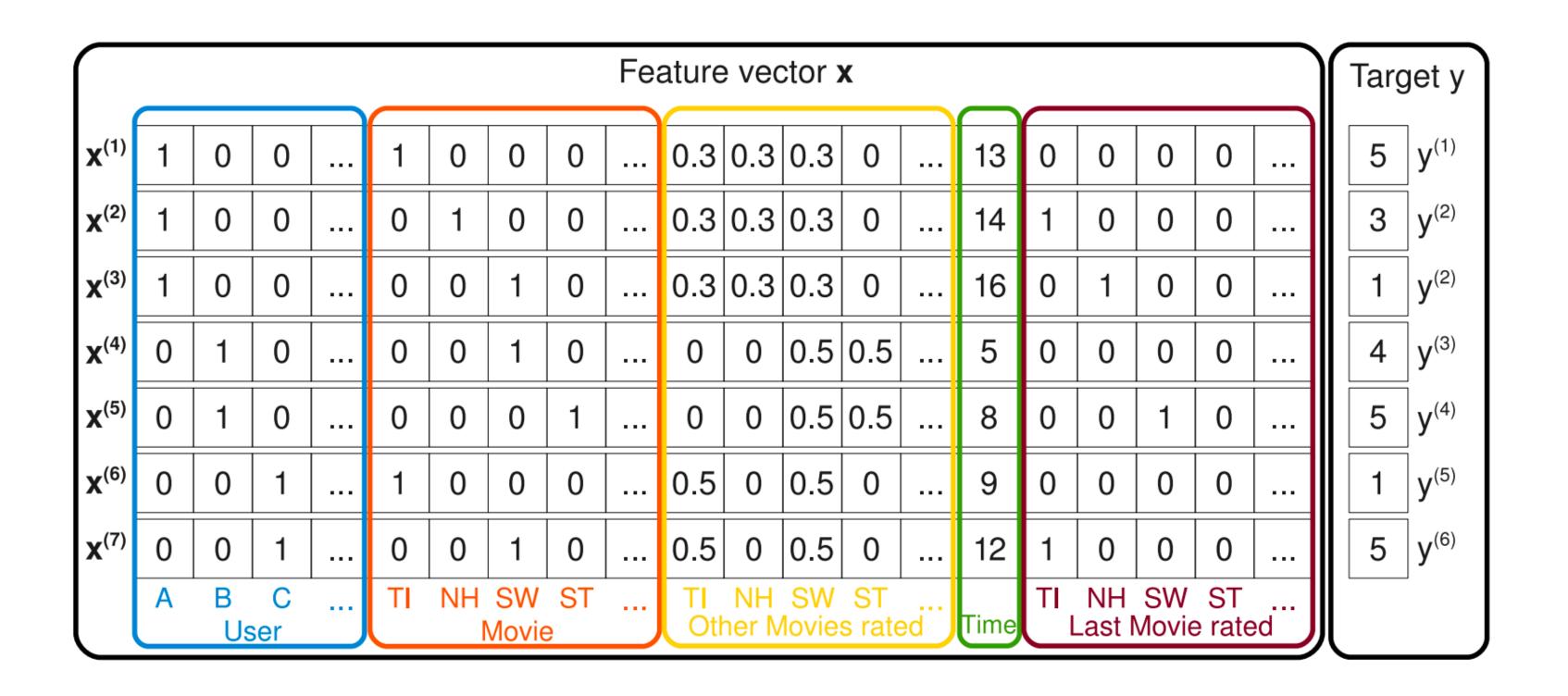
```
U = \{ \text{Alice (A), Bob (B), Charlie (C), ...} \}
I = \{ \text{Titanic (TI), Notting Hill (NH), Star Wars (SW), } 
\text{Star Trek (ST), ...} \}
```

The observed data:

```
S = \{(A, TI, 2010-1, 5), (A, NH, 2010-2, 3), (A, SW, 2010-4, 1), \\ (B, SW, 2009-5, 4), (B, ST, 2009-8, 5), \\ (C, TI, 2009-9, 1), (C, SW, 2009-12, 5)\}
```







Factorization machines

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... factorization machines using such feature vectors as input data are related to specialized state-of-the-art factorization ... between factorization machines and support vector machines as ...

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FM and SVD++

• **Explicit** (e.g. numerical rantings) + **Implicit** information (e.g. likes, purchases, skipped, bookmarked,...)

$$\hat{r}_{ui} = b_{ui} + q_i^T \left(p_u + |\mathrm{N}(u)|^{-rac{1}{2}} \sum_{j \in \mathrm{N}(u)} y_j
ight)$$

• N(u) is the set of items for which the user u has implicit information



FM and SVD++

• **Explicit** (e.g. numerical rantings) + **Implicit** information (e.g. likes, purchases, skipped, bookmarked,...) $\hat{r}_{ui} = b_{ui} + q_i^T \left(p_u + |N(u)|^{-\frac{1}{2}} \sum_{j \in N(u)} y_j \right)$

$$(u, i, \{l_1, \ldots, l_m\}) \to \mathbf{x} = (\underbrace{0, \ldots, 1, 0, \ldots}_{|U|}, \underbrace{0, \ldots, 1, 0, \ldots}_{|I|}, \underbrace{0, \ldots, 1/m, 0, \ldots, 1/m, 0, \ldots}_{|L|}),$$

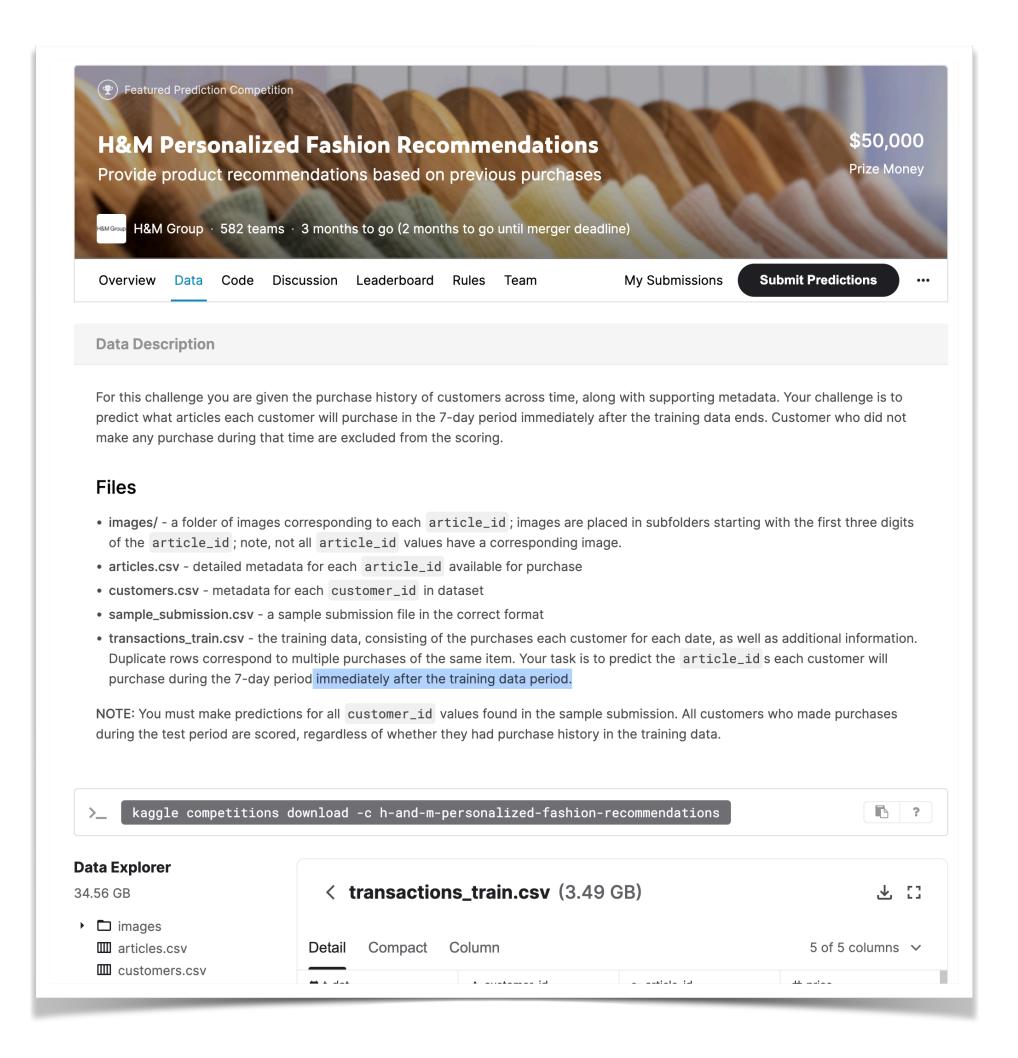
$$\hat{y}(\mathbf{x}) = \hat{y}(u, i, \{l_1, \dots, l_m\}) = w_0 + w_u + w_i + \langle \mathbf{v}_u, \mathbf{v}_i \rangle + \frac{1}{m} \sum_{j=1}^m \langle \mathbf{v}_i, \mathbf{v}_{l_j} \rangle$$





- Offers combination of regression and factorization models
- Low rank approximation ranking enables estimation of unobserved interactions
- Effective for sparse and extremely sparse data sets
- Flexible through feature engineering





Exercice:

Implement a Factorization Machine and apply to HM Challenge Notebook and Submission are mandatory

Groups of up to 3 people are allowed

How to submit:

Upload the code at Campus Virtual + share the notebook via Kaggle

Deadline: March 20th



