

# Recommender Systems with Deep Learning



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# WHAT is an EMBEDDING?

- **Embeddings** are a way to represent entities using learned vectors.



# How do we use embeddings for RS?

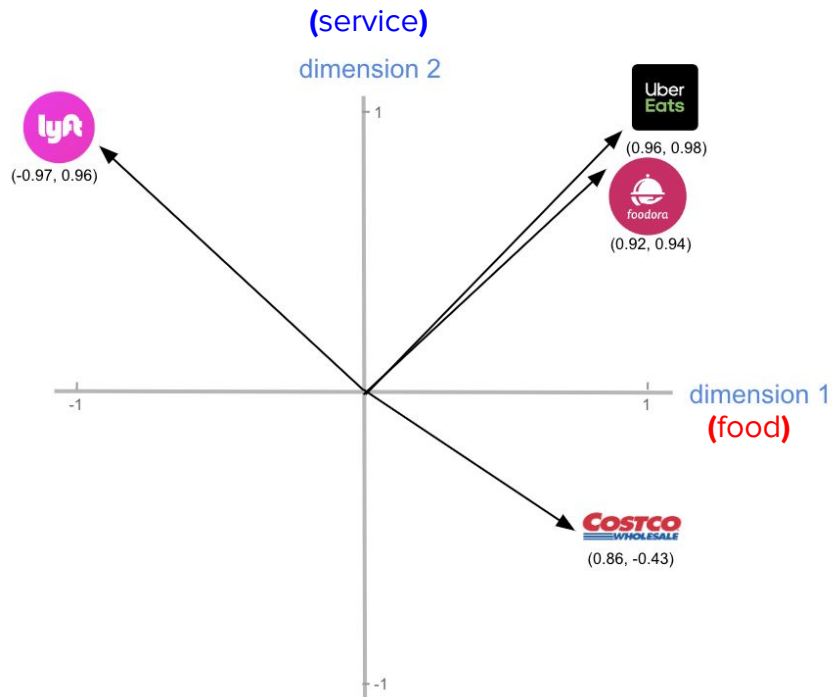


Figure from [this](#) blog.

# EMBEDDINGS can be **learned** and **reused** across models:

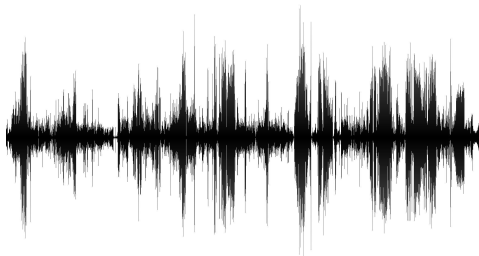


-1	0.4	0.2	...	-0.45	0.87	0.23	-0.67
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1	-0.2	...	0.5	0.9
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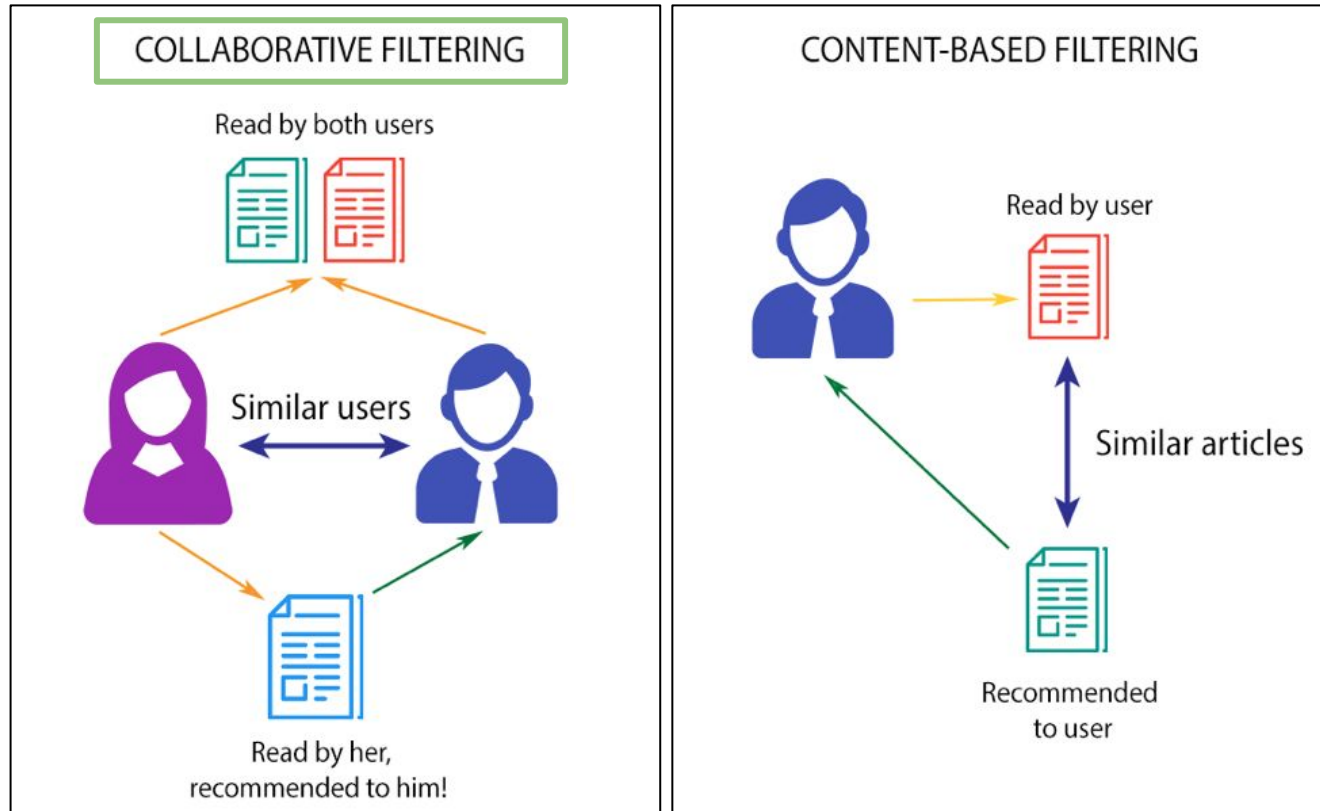


Corporate Social Responsibility (CSR) can generate a positive reputation for a company leading to possibly more sales and growth. According to Jones et al (2019), a corporation that invests in the environmental and ethical approaches of CSR will demonstrate to the public and the media that they are a responsible company. Watson (2018) provides evidence that this improves consumer sales as customers tend to support ethical green business practice thus improving profitability and encouraging growth. For example, a yoghurt company called Yeo Valley has been investing in making its products organic, creating fully recyclable packaging and reducing its CO2 output. As a result, profits have doubled within the last two years providing the company with a range of opportunities to expand (Peterson, 2019). Overall, the evidence seems to suggest that investing in CSR can improve brand image and productivity.



0.8	0.2	-0.87	...	-0.52	0.7	-0.32	-0.79
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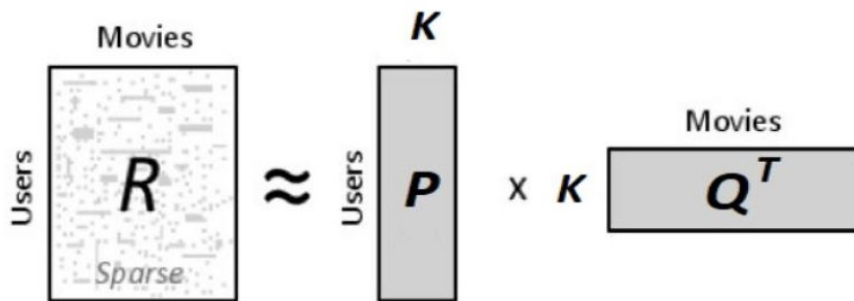
# TECHNIQUES FOR RECOMMENDATION:



# SOTA models



# 1. Matrix Factorization



$$r_{ij} = p_i^T q_j$$

$\mathbf{p} \rightarrow$  latent features for users (user embeddings)  
 $\mathbf{q} \rightarrow$  latent features for items (item embeddings)

## 2. Factorization Machines (FM)

( Paper [here](#) )

$$\hat{y}(\mathbf{x}) := w_0 + \sum_{i=1}^n w_i x_i + \sum_{i=1}^n \sum_{j=i+1}^n \langle \mathbf{v}_i, \mathbf{v}_j \rangle x_i x_j$$

All nodes

LINEAR  
REGRESSION

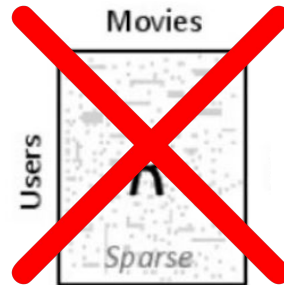
EMBEDDING  
LAYER

USER-ITEM  
FEATURES

All nodes

	User_0	...	User_N <sub>u</sub>	Item_0	...	Item_N <sub>i</sub>
User_0 ... User_N <sub>u</sub>	0			Interactions user-item		
Item_0 ... Item_N <sub>i</sub>	Interactions user-item			0		

Adjacency matrix





JUST FOR AN EASIER  
IMPLEMENTATION ...

FM part

$$\sum_{i=1}^n \sum_{j=i+1}^n \langle \mathbf{v}_i, \mathbf{v}_j \rangle x_i x_j$$

$$= \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \langle \mathbf{v}_i, \mathbf{v}_j \rangle x_i x_j - \frac{1}{2} \sum_{i=1}^n \langle \mathbf{v}_i, \mathbf{v}_i \rangle x_i x_i$$

$$= \frac{1}{2} \left( \sum_{i=1}^n \sum_{j=1}^n \sum_{f=1}^k v_{i,f} v_{j,f} x_i x_j - \sum_{i=1}^n \sum_{f=1}^k v_{i,f} v_{i,f} x_i x_i \right)$$

$$= \frac{1}{2} \sum_{f=1}^k \left( \left( \sum_{i=1}^n v_{i,f} x_i \right) \left( \sum_{j=1}^n v_{j,f} x_j \right) - \sum_{i=1}^n v_{i,f}^2 x_i^2 \right)$$

$$= \frac{1}{2} \sum_{f=1}^k \left( \left( \sum_{i=1}^n v_{i,f} x_i \right)^2 - \sum_{i=1}^n v_{i,f}^2 x_i^2 \right)$$

# Why is FM a generalization of MF ?

**MF**

$$r_{ij} = p_i^T q_j$$

→

**FM**

$$r_{ij} = \langle \mathbf{v}_i, \mathbf{v}_j \rangle x_i x_j$$

- **Forced to learn features of users and items while factorizing.**
- **Allow side-info in  $\mathbf{x}_i$  vector**
  - **Allow more dimensions**

	User_0    ...    User_N <sub>u</sub>	Item_0    ...    Item_N <sub>i</sub>	Context_0    ...    Context_N <sub>c</sub>
User_0 ... User_N <sub>u</sub>	0	Interactions user-item	Interactions user-context
Item_0 ... Item_N <sub>i</sub>	Interactions user-item	0	Interactions item-context
Context_0 ... Context_N <sub>c</sub>	Interactions user-context	Interactions item-context	0



# FM PROBLEM!

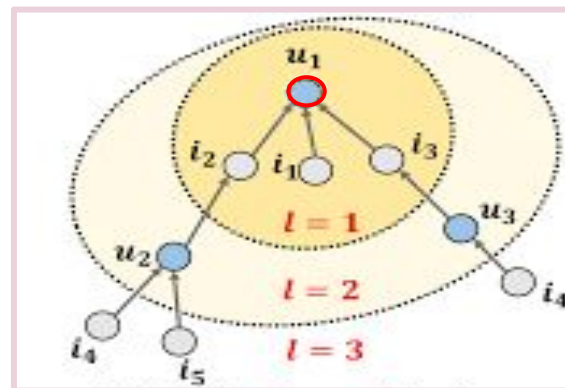
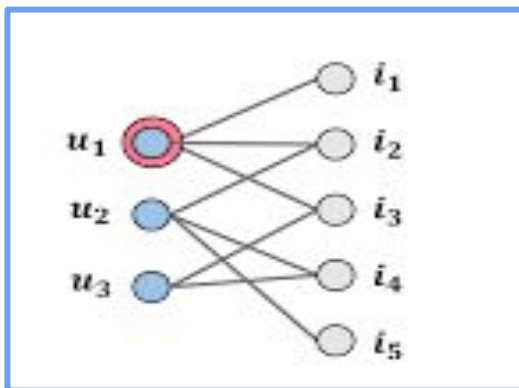
NFM

DFM

WD

FM captures interactions of only second order! ( $\ell = 1$ )

We might want to capture high order interactions ....



```
graph TD; FM([Factorization Machine (FM) model]); NCF([NCF model]); NFM([NFM model]); DFM([DFM model]); WD([WD model]); FM --- NCF; FM --- NFM; FM --- DFM; FM --- WD;
```

**Factorization Machine (FM)  
model**

**NCF  
model**

**NFM  
model**

**DFM  
model**

**WD  
model**

# FM model

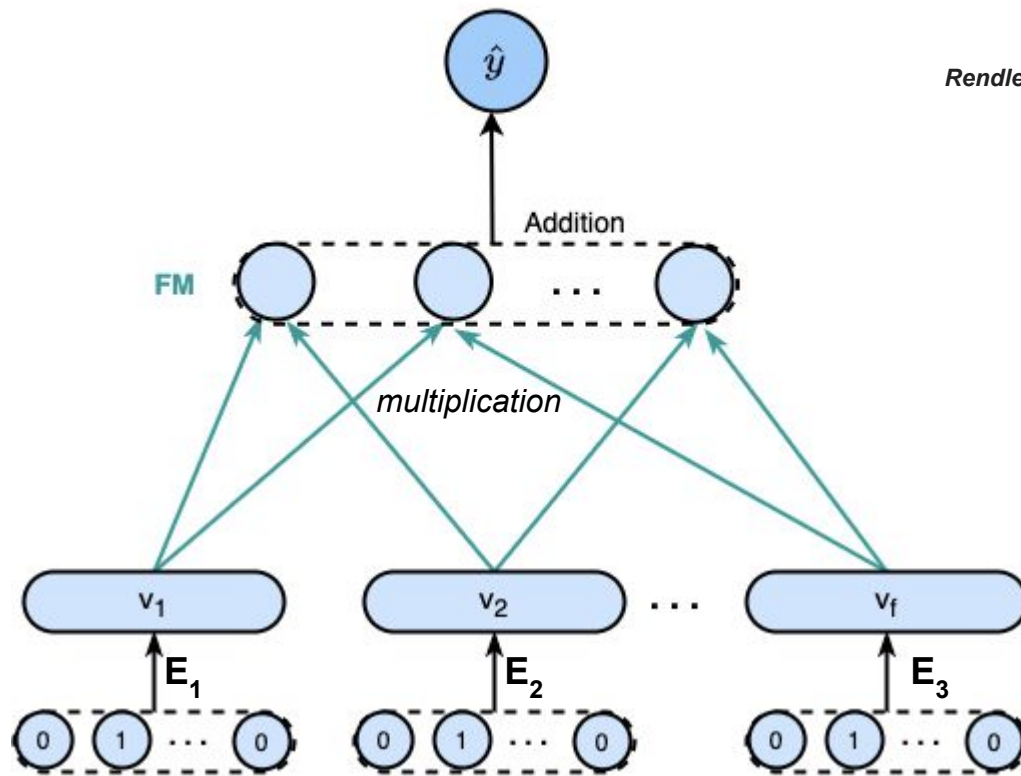
Rendle, Steffen. "Factorization machines." 2010

Feature vector $\mathbf{x}$																			Target $y$		
$\mathbf{x}^{(1)}$	1	0	0	...	1	0	0	0	...	0.3	0.3	0.3	0	...	13	0	0	0	0	...	5 $y^{(1)}$
$\mathbf{x}^{(2)}$	1	0	0	...	0	1	0	0	...	0.3	0.3	0.3	0	...	14	1	0	0	0	...	3 $y^{(2)}$
$\mathbf{x}^{(3)}$	1	0	0	...	0	0	1	0	...	0.3	0.3	0.3	0	...	16	0	1	0	0	...	1 $y^{(2)}$
$\mathbf{x}^{(4)}$	0	1	0	...	0	0	1	0	...	0	0	0.5	0.5	...	5	0	0	0	0	...	4 $y^{(3)}$
$\mathbf{x}^{(5)}$	0	1	0	...	0	0	0	1	...	0	0	0.5	0.5	...	8	0	0	1	0	...	5 $y^{(4)}$
$\mathbf{x}^{(6)}$	0	0	1	...	1	0	0	0	...	0.5	0	0.5	0	...	9	0	0	0	0	...	1 $y^{(5)}$
$\mathbf{x}^{(7)}$	0	0	1	...	0	0	1	0	...	0.5	0	0.5	0	...	12	1	0	0	0	...	5 $y^{(6)}$
	A	B	C	...	TI	NH	SW	ST	...	TI	NH	SW	ST	...	Time	TI	NH	SW	ST	...	
	User				Movie					Other Movies rated						Last Movie rated					

# FM model

$$\hat{y}(\mathbf{x}) := w_0 + \sum_{i=1}^n w_i x_i + \sum_{i=1}^n \sum_{j=i+1}^n \langle \mathbf{v}_i, \mathbf{v}_j \rangle x_i x_j$$

Rendle, Steffen. "Factorization machines." 2010

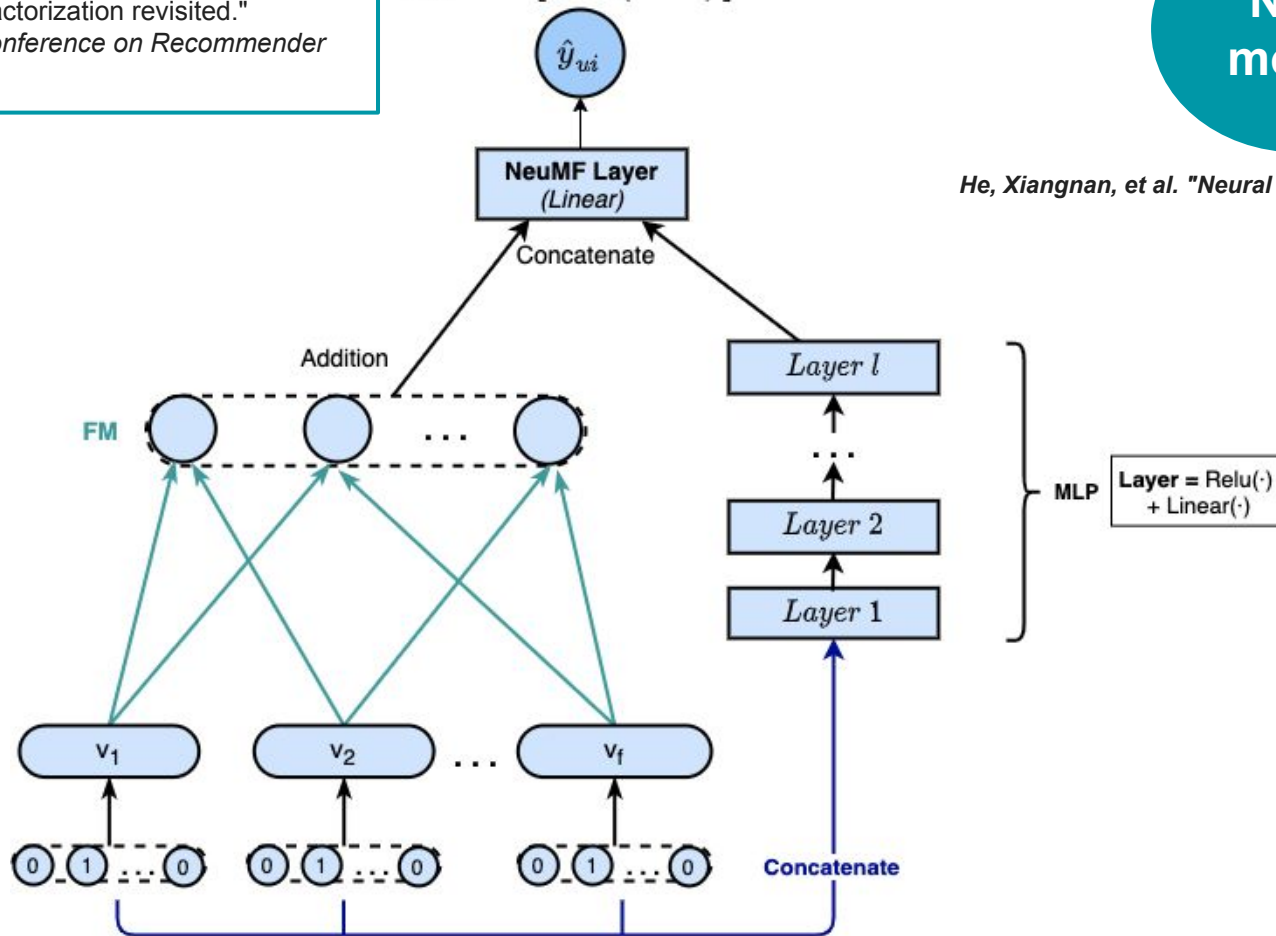


Rendle, Steffen, et al. "Neural collaborative filtering vs. matrix factorization revisited." *Fourteenth ACM Conference on Recommender Systems*. 2020.

$$\hat{y}_{wic} = h^T \left[ x, \phi^L \left( z^{(L-1)} \right) \right]$$

# NCF model

He, Xiangnan, et al. "Neural collaborative filtering." , 2017



# EVALUATION ON RANKING



# Explicit vs Implicit feedback

 **How much did the user like the film?** **(explicit)**

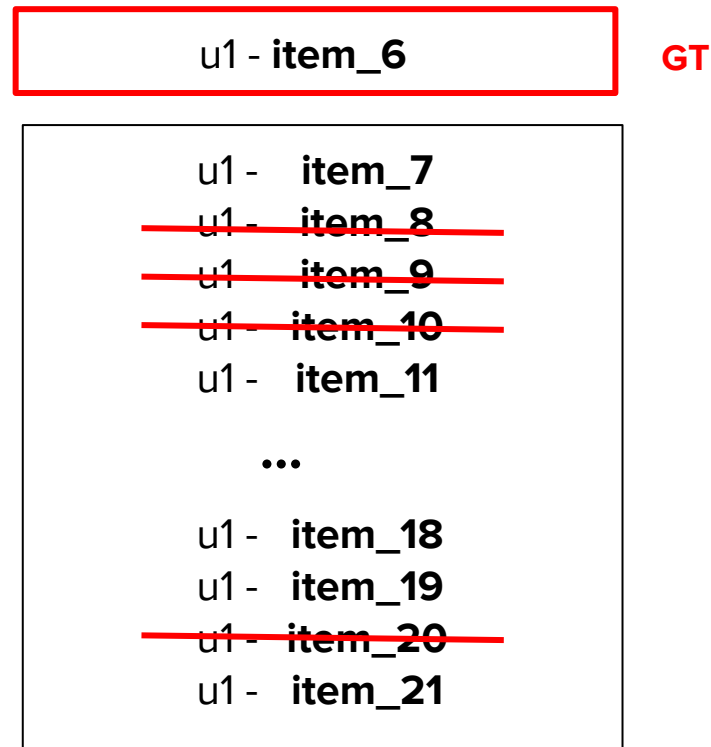
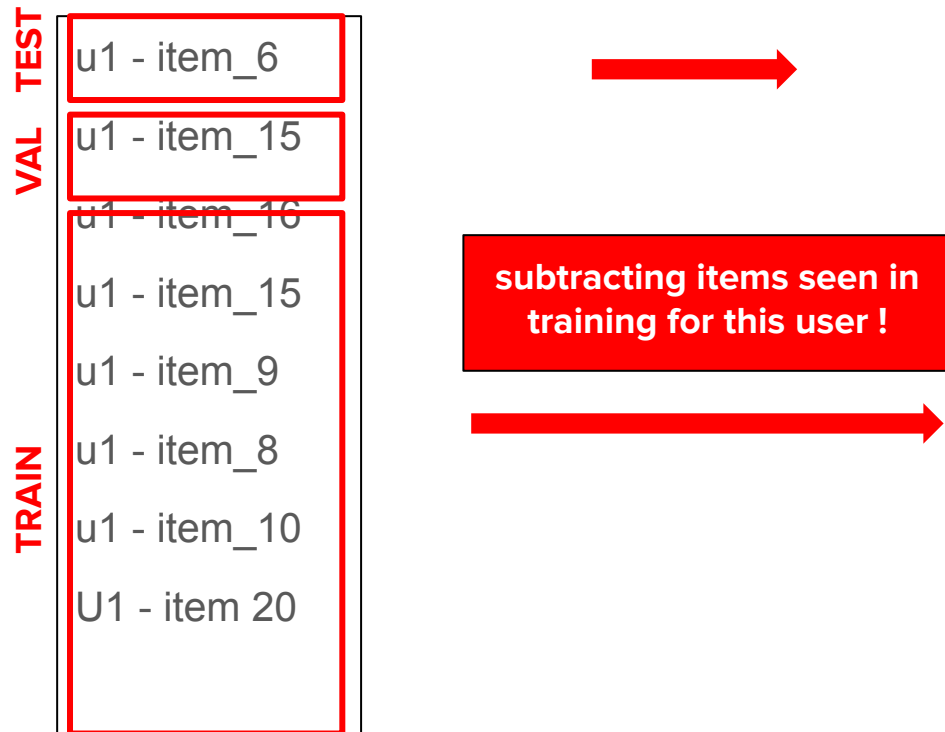
 **Was the user interested in the film?** **(implicit)**

- We won't care about ratings (1-5).
- All provided data will be treated as positive  
→ We will need to perform negative sampling.

# Leave-one-out procedure: (positive samples)

dataset

users: 1 - 5  
items: 6 - 21



# Leave-one-out procedure: (positive samples)

dataset

users: 1 - 5  
items: 6 - 21

**COMPUTE PREDICTIONS  
AND SORT THEM**



Compute HR and NDCG to  
see whether out GT  
prediction is in the TOP@K

**TEST dataset**

u1 - item\_6 (GT)

u1 - Item\_7  
u1 - Item\_11  
u1 - Item\_12  
u1 - Item\_13

...

u1 - Item\_17  
u1 - Item\_18  
u1 - Item\_19  
u1 - Item\_21

# METRICS:



- **Hit Ratio (HR@K)**

Measures whether the test item is in the top@K positions of the recommendation list ( 1 = yes | 0 = no ).

- **Normalized Discounted Cumulative Gain (NDCG@K)**

Measures the ranking quality which gives information about where in the ranking is our test item.