## The EPFL Logic Synthesis Libraries

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#### libraries<sup>1</sup>

alice: command shell library

mockturtle: logic network library

lorina: parsing library

kitty: truth table library

• bill: reasoning library

percy: exact synthesis library

easy: exclusive-or sum-of-product (ESOP) library

¹Mathias Soeken et al. "The EPFL Logic Synthesis Libraries.". In: arXiv: Logic in Computer Science (2022).

DOI: null. URL: https://arxiv.org/abs/1805.05121.

## quantum libraries

- angel: quantum state preparation library
- tweedledum: quantum compilation library
- caterpillar: quantum circuit synthesis library

#### initial state<sup>2</sup>

target:

$$|\varphi_j\rangle = \frac{1}{\sqrt{|on(f)|}} \sum_{x \in on(f)} |x\rangle$$
 (1)

the general idea of state preparation algorithm relies on the identity:

$$QSP_{f}|0\rangle^{\otimes n} = \left(QSP_{f_{\bar{x}_{i}}} \oplus QSP_{f_{x_{i}}}\right) \left(G\left(p_{f}\left(\bar{x}_{i}\right)\right) \otimes I_{2^{n}-1}\right)|0\rangle$$
(2)

•  $G(p_f(\bar{x}_i))$  is a unitary transformation gate that satisfies:

$$G(p_f(\bar{x}_i))|0\rangle = \sqrt{p_f(\bar{x}_i)}|0\rangle + \sqrt{1 - p_f(\bar{x}_i)}|1\rangle$$
(3)

$$G\left(p_f\left(\bar{x}_i\right)\right) = R_y\left(2\cos^{-1}\left(\sqrt{p_f\left(\bar{x}_i\right)}\right)\right) \tag{4}$$

<sup>&</sup>lt;sup>2</sup>Fereshte Mozafari et al. "Automatic Uniform Quantum State Preparation Using Decision Diagrams". In: 2020 IEEE 50th International Symposium on Multiple-Valued Logic (ISMVL) (2020). DOI: 10.1109/ismv149045.2020.00-10.

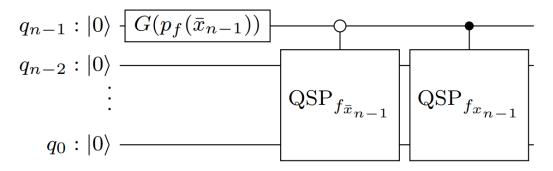


Figure: the general idea of QSP in the quantum circuit model for i = n - 1.

## initial state example

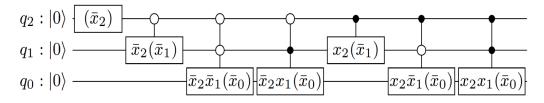


Figure: the abstract quantum gates of  $QSP_{< x_0x_1x_2>}$ 

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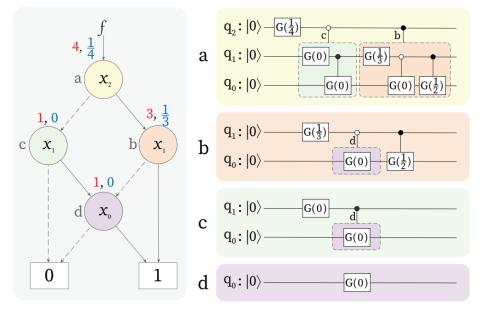


Figure: BDD for boolean function  $f = x_0x_1 \lor x_1x_2 \lor x_2x_0$  and the procedure of extracting gates for each node from bottom to top

## compiling oracle by XAG<sup>3</sup>

• representing an n-variable boolean function using a logic network over the gate basis $\{\neg, \oplus, \wedge\}$ :

$$x_i = x_{j(i)} \oplus x_{k(i)}$$
 or  $x_i = x_{j(i)}^{p(i)} \wedge x_{k(i)}^{q(i)}$  (5)

where  $n < i \le n + r$ 

• the linear transitive fan-in of a node  $x_i$  using the recursive function:

$$\mathsf{ltfi}(x_i) = \begin{cases} \{x_i\} & \text{if } i < n \text{ or } \circ_i = \land, \\ \mathsf{ltfi}\left(x_{j(i)}\right) \triangle \mathsf{ltfi}\left(x_{k(i)}\right) & \text{otherwise} \end{cases}$$
 (6)

<sup>&</sup>lt;sup>3</sup>Giulia Meuli et al. "The Role of Multiplicative Complexity in Compiling Low T-count Oracle Circuits". In: (2019). DOI: 10.1109/iccad45719.2019.8942093.

## XAG example

- for  $f(x) = x_1x_2 \lor x_2x_3 \lor x_3x_1$
- can be realized by the logic network:

$$x_4 = x_1 \oplus x_2,$$
  $x_5 = x_2 \oplus x_3$  (7)

$$x_6 = x_4 \wedge x_5, \qquad x_7 = x_2 \oplus x_6$$
 (8)

• the linear transitive fan-in of a node:

$$\mathsf{ltfi}\,(x_4) = \{x_1, x_2\}\,, \qquad \qquad \mathsf{ltfi}\,(x_5) = \{x_2, x_3\} \tag{9}$$

$$\mathsf{ltfi}\,(x_6) = \{x_6\}\,, \qquad \qquad \mathsf{ltfi}\,(x_7) = \{x_2, x_6\} \tag{10}$$

#### function compute is

```
for i = n + 1, \dots, n + r where \circ_i = \wedge do
     set p \leftarrow p(i), q \leftarrow q(i), j \leftarrow j(i), k \leftarrow k(i);
     set L_1 \leftarrow ltfi(x_i), L_2 \leftarrow ltfi(x_k);
     if L_1 \subseteq L_2 then
         swap L_1 \leftrightarrow L_2 and p \leftrightarrow q;
     end
     let t_1 be some element in L_1 \setminus L_2;
     let t_2 be some element in L_2;
     CNOT(x, t_1) for all x \in L_1 \setminus \{t_1\};
     CNOT(x, t_2) for all x \in L_2 \setminus \{t_2\};
     if p then NOT(t_1);
     if q then NOT(t_2);
     TOFFOLI(t_1, t_2, x_i):
     if p then NOT(t_2);
     if q then NOT(t_1);
     CNOT(x, t_2) for all x \in L_2 \setminus \{t_2\};
     CNOT(x, t_1) for all x \in L_1 \setminus \{t_1\};
end
```

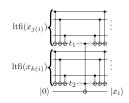


Figure: quantum circuit construction for function compute

#### $\textbf{Algorithm 1} \ \mathsf{Heuristic} \ \mathsf{compilation} \ \mathsf{algorithm}$

```
Input: Logic network with gates x_{n+1}, \ldots, x_{n+r}

Output: Quantum circuit for Uf

compute

CNOT(x_{n+r-1}, y)

if p then

NOT(y)

end if

compute^{\dagger}
```

end

## pebbling<sup>4</sup>

- target: solving iteratively the reversible pebbling game on the given network
- method: the problem is encoded as a SAT problem and addressed by state-of-the-art solvers
- result: get the trade-off between qubits and operations

<sup>&</sup>lt;sup>4</sup>Giulia Meuli et al. "Reversible Pebbling Game for Quantum Memory Management". In: arXiv: Quantum Physics (2019). DOI: 10.23919/date.2019.8715092.

## pebbling example

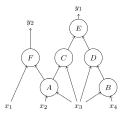


Figure: example of a directed acyclic graph

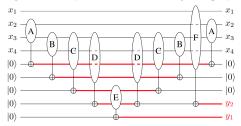


Figure: space-optimized by reordering

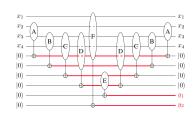


Figure: Bennet strategy

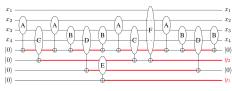


Figure: space-optimized by increasing the number of gates

#### tweedledum<sup>5</sup>

- narrowing the gap between high-level algorithms and physical devices
- an intuitive and flexible intermediate representation that supports different abstraction levels across the same circuit structure

Gcc (ISCAS) logic synthesis libraries October 24, 2022

<sup>&</sup>lt;sup>5</sup>Bruno Schmitt and Giovanni De Micheli. "Tweedledum: A Compiler Companion for Quantum Computing". In: 2022 Design, Automation Test in Europe Conference Exhibition (DATE) (2022). DOI: 10.23919/date54114.2022.9774510

## compilation flow

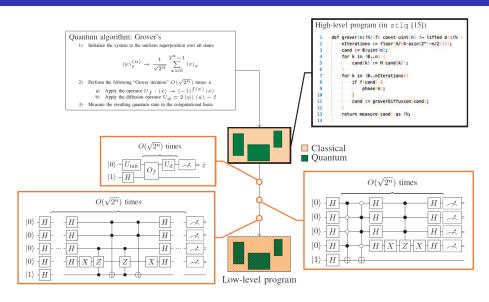


Figure: compilation flow overview



## flexibility

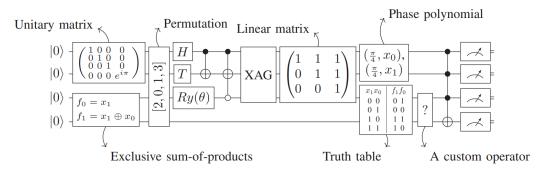


Figure: tweedledum's IR flexibility

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#### synthesis

- pkrm\_synth and pprm\_synth synthesize a particular case of an exclusive-or sum-of-product (ESOP) expression for f
- spectrum\_synth uses the Rademacher-Walsh spectrum of a truth table to generate a circuit
- Ihrs\_synth and xag\_synth are examples of hierarchical synthesis
- a\_star\_swap\_synth and star\_swap\_synth for circuits composed entirely of SWAP operators

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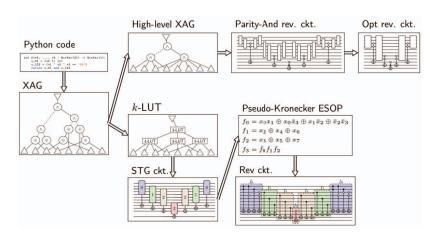


Figure: overview of possible Boolean function synthesis flows

## compilation passes

- utility
- decomposition
- mapping
- optimization

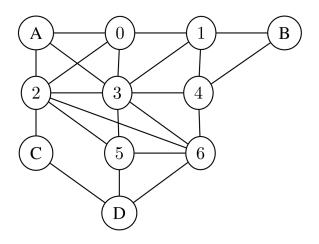


Figure: Zed city as an undirected graph

#### initial state boolean function

#### python implementation of initial function f

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#### python implementation of f

```
def f(v0, \ldots, v6 : BitVec(2)) \rightarrow
   BitVec(1):
  c0 = (v0 != "00)
  c1 = (v1 != ''01) and (v1 != v0)
  c2 = (v2 != "00)  and (v2 != "10)
     and (v2 != v0)
  c3 = (v3 != "00) and (v3 != v0)
     and (v3 != v1) and (v3 != v2)
  c4 = (v4 != "01) and (v4 != v1)
     and (v4 != v3)
  c5 = (v5 != "11)  and (v5 != v2)
     and (v5 != v3)
  c6 = (v6 != "11)  and (v6 != v2)
     and (v6 != v3) and (v6 != v4)
      and (v6 != v5)
  return c0 and c1 and c2 and c3
     and c4 and c5 and c6
```

## hand-optimized python implementation of f

```
def f(v0, ..., v6 : BitVec(2)) ->
   BitVec(1):
   c1 = (v1[0] == v1[1]) and (v3 !=
      v1)
   c023 = ((v0 ^ v2 ^ v3) == "00)
   c4 = (v4 != v1) and (v4 != v3)
   c5 = (v5 != v2) and (v5 != v3)
   c6 = ((v2 ^ v3 ^ v5 ^ v6) == "00)
      and (v6 != v4)
   return c1 and c023 and c4 and c5
   and c6
```

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## result<sup>6</sup>

	Hand-optimized		Non-optimized	
	Qubits	cost	Qubits	cost
IBM's solution	32	5004		
Whit3z solution	32	2474		
XAG-based flow	31	2202	56	4347
XAG-based flow with pebbling	21	4497	30	7737

Table: quality of results for boolean function (hand-optimized and non-optimized), where  $cost = q_1 + 10q_2$ 

<sup>&</sup>lt;sup>6</sup>Bruno Schmitt et al. "From Boolean functions to quantum circuits: A scalable quantum compilation flow in C++". In: 2021 Design, Automation Test in Europe Conference Exhibition (DATE) (2021). DOI: 10.23919/date51398.2021.9474237.

#### disscussion

- lack of quantum computing features
- comparing with isq etc
- the abstract level of quantum computer?

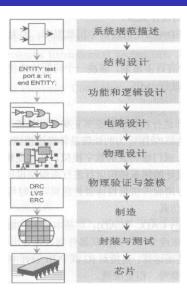


Figure: the main flow of ultra-large scale IC product design

#### references I

- Giulia Meuli et al. "Reversible Pebbling Game for Quantum Memory Management". In: arXiv: Quantum Physics (2019). DOI: 10.23919/date.2019.8715092.
- Giulia Meuli et al. "The Role of Multiplicative Complexity in Compiling Low T-count Oracle Circuits". In: (2019). DOI: 10.1109/iccad45719.2019.8942093.
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- Bruno Schmitt et al. "From Boolean functions to quantum circuits: A scalable quantum compilation flow in C++". In: 2021 Design, Automation Test in Europe Conference Exhibition (DATE) (2021). DOI: 10.23919/date51398.2021.9474237.

Gcc (ISCAS)

#### references II



Mathias Soeken et al. "The EPFL Logic Synthesis Libraries.". In: arXiv: Logic in Computer Science (2022). DOI: null. URL: https://arxiv.org/abs/1805.05121.

# END Thank you