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GCCL SEMINAR

2021-07-30

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# MEASURING THE GROWTH RATE USING SMALL-SCALE CLUSTERING IN EBOSS

**WHAT DO YOU MEAN “SMALL-SCALE”?**

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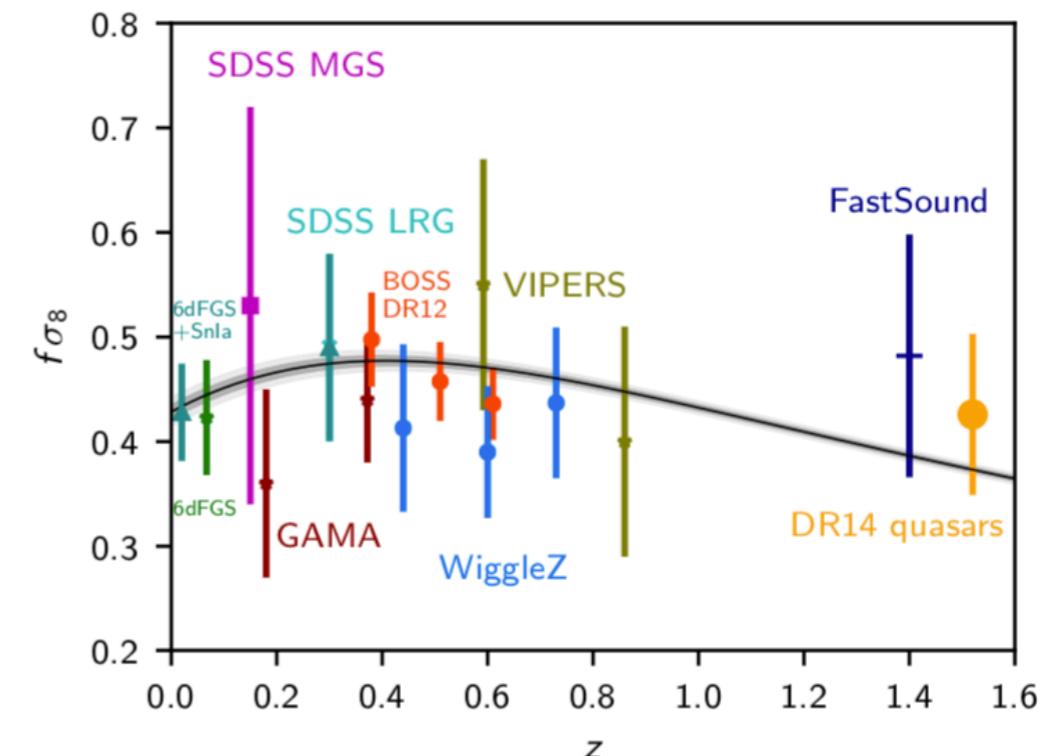
**INTRODUCTION**

# THE GROWTH RATE

- ▶ Theories of dark energy or modified gravity affect the growth of structure, parameterized by  $f\sigma_8$
- ▶  $f$  is the logarithmic growth rate of density fluctuations

$$f(\Omega_m) = \frac{d \ln D}{d \ln a} \quad ; \quad D \propto \delta_+$$

- ▶  $\sigma_8$  is the rms variance of density fluctuations in a sphere of radius 8  $h^{-1} Mpc$



Constraints on the growth rate from various galaxy redshift surveys. Planck TT,TE,EE+lowE+lensing shown in black with 68% and 95% confidence ranges. (Planck Collaboration et al. 2018)

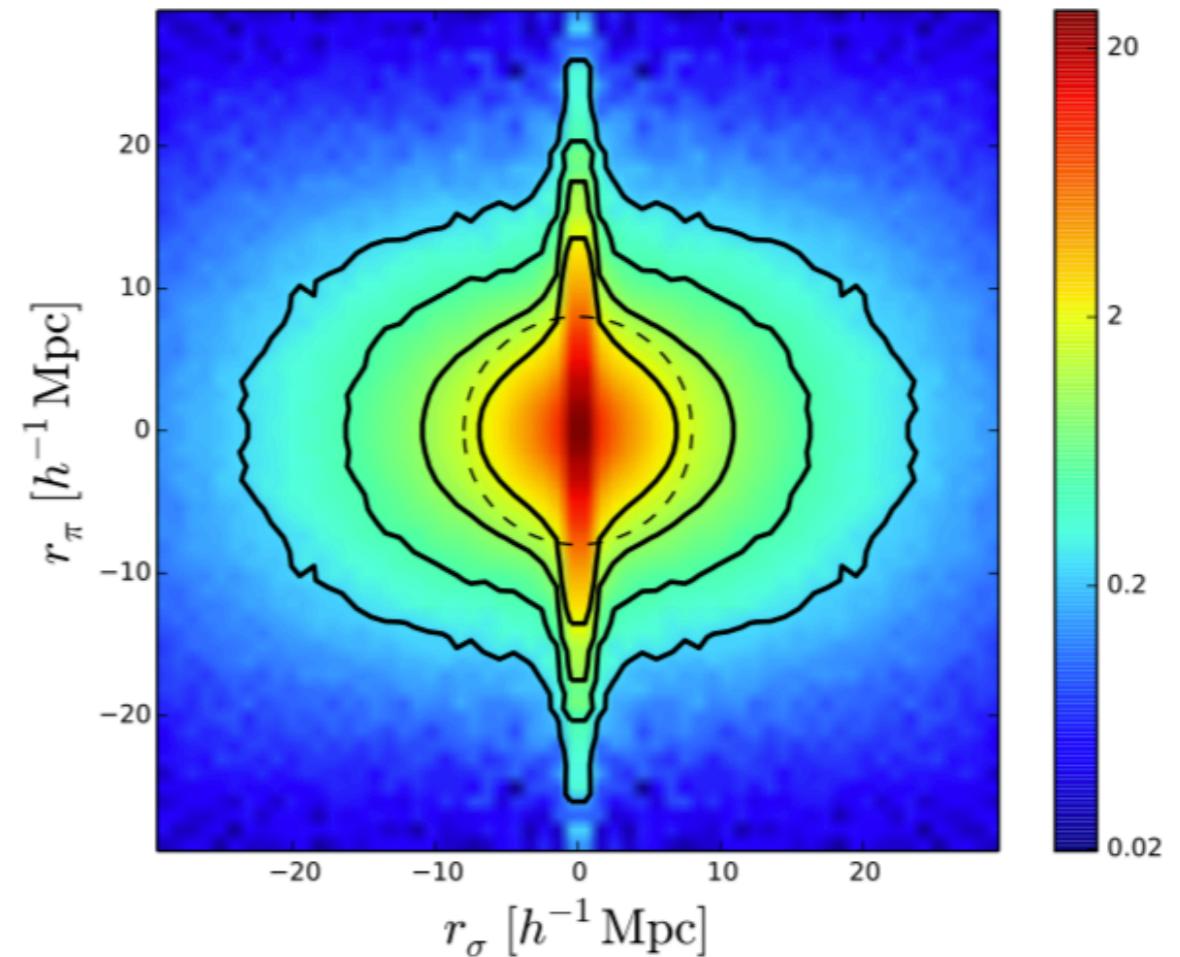
# REDSHIFT SPACE DISTORTIONS

- ▶ Peculiar velocities shift the position of galaxies in redshift space:

$$\nabla \cdot \mathbf{v}_p = -aHf\delta_m$$

$$\delta_g^s(\mathbf{k}) = (b + f\mu^2)\delta_m^r(\mathbf{k})$$

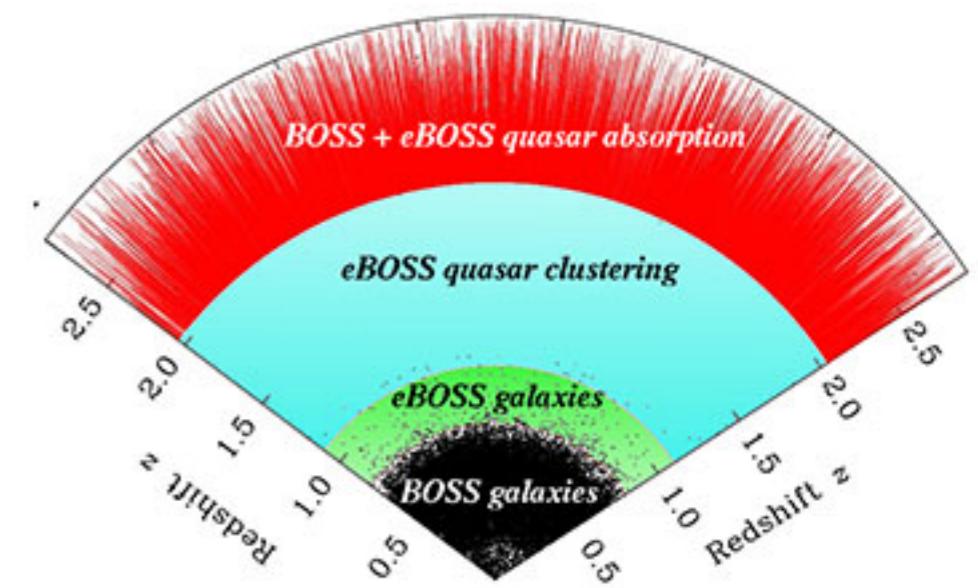
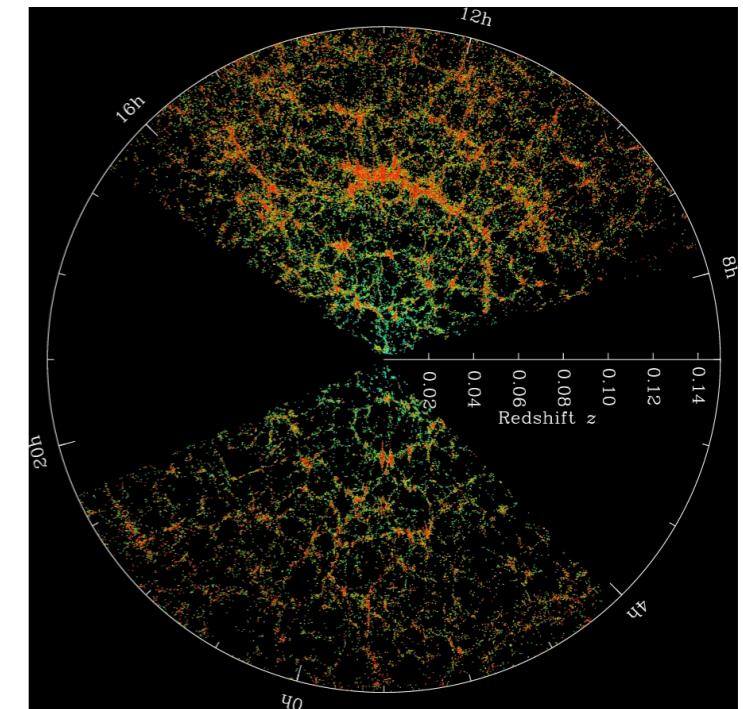
- ▶ In the linear regime ( $>40 h^{-1}\text{Mpc}$ ) gives a direct constraint on  $f\sigma_8$
- ▶ Below  $\sim 40 h^{-1}\text{Mpc}$  need to model non-linearities using N-body simulations



2D correlation function in separation parallel (y-axis) and perpendicular (x-axis) to the line of sight.  
(Reid et al. 2014, 1404.3742)

# EXTENDED BARYON OSCILLATION SPECTROSCOPIC SURVEY (EBOSS)

- ▶ Spectroscopic surveys convert redshifts to distances assuming the Hubble flow
- ▶ The Baryon Oscillation Spectroscopic Survey (BOSS) observed 1.5 million Luminous Red Galaxies (LRG) in the redshift range ( $0.1 < z < 0.7$ )
- ▶ The extended BOSS (eBOSS) observed an additional 300 000 high redshift ( $0.6 < z < 1.0$ ) LRGs, as well as ELG and QSO



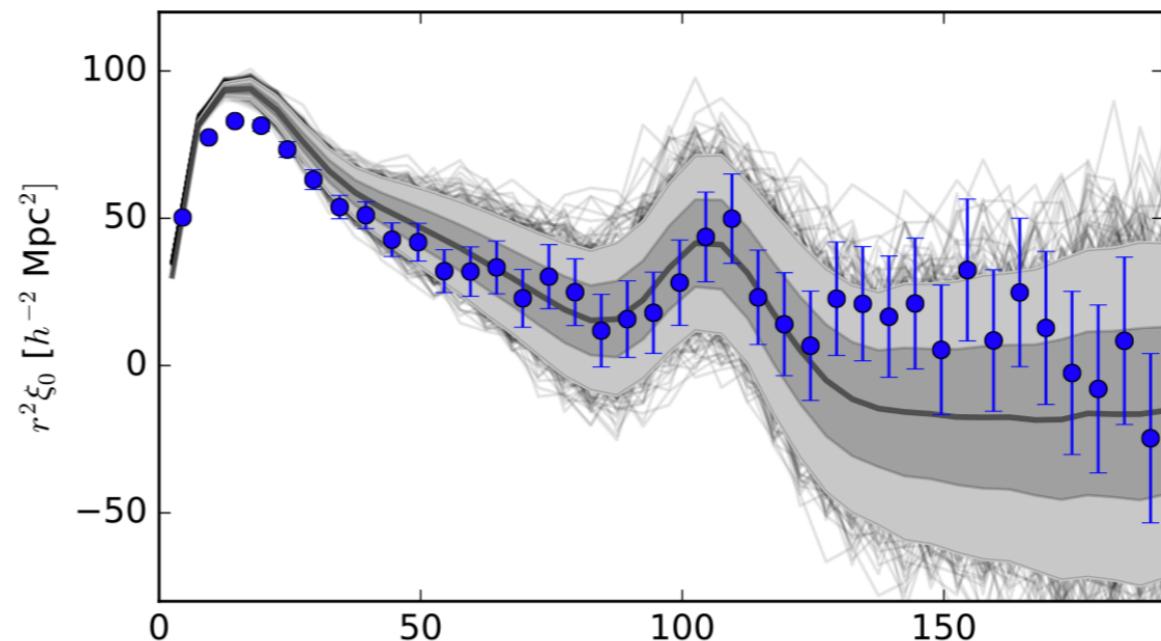
# CORRELATION FUNCTION

- Excess probability of finding another galaxy at a given separation relative to if they followed a Poissonian distribution

$$\xi(r_{\parallel}, r_{\perp}) = \frac{DD(r_{\parallel}, r_{\perp}) - 2DR(r_{\parallel}, r_{\perp})}{RR(r_{\parallel}, r_{\perp})} + 1$$

$$w_p(r_{\perp}) = 2 \int_0^{r_{\parallel, \text{max}}} dr_{\parallel} \xi(r_{\parallel}, r_{\perp})$$

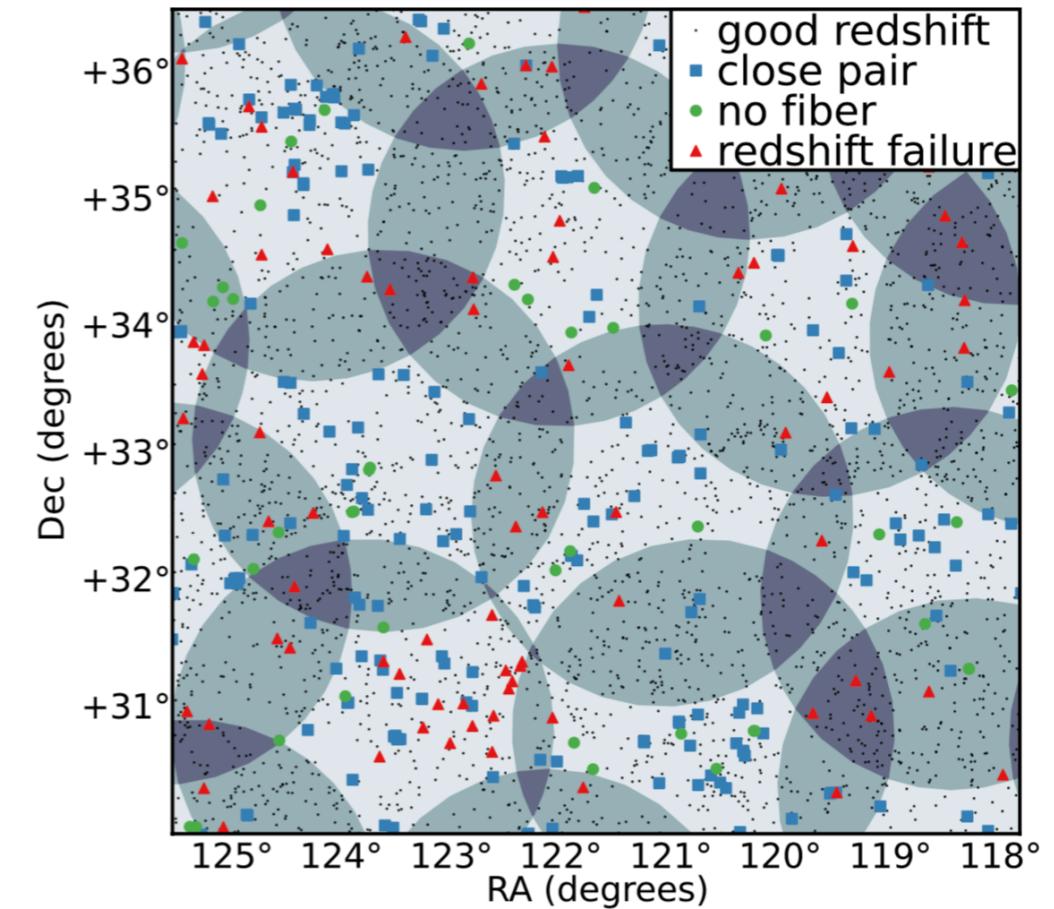
$$\xi_l(s) = \frac{2l+1}{2} \int d\mu_s \xi(s, \mu_s) L_l(\mu_s)$$



Correlation function monopole of the combined BOSS CMASS + eBOSS DR14 (Bautista et al. 2017)

# FIBRE-COLLISION

- ▶ Physical size of fibre prevents targeting two objects within 62"
- ▶ Separation on the sky is correlated with radial separation, leading to a biased sample
- ▶ Commonly corrected using nearest-neighbour weights, which approximately correct issue but perform worse on smaller scales



Result of fibre assignment, Ross et al. 2012

# REID ET AL. 2014 (1404.3742)

## A 2.5% measurement of the growth rate from small-scale redshift space clustering of SDSS-III CMASS galaxies

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2 August 2018

### ABSTRACT

We perform the first fit to the anisotropic clustering of SDSS-III CMASS DR10 galaxies on scales of  $\sim 0.8\text{--}32 h^{-1} \text{ Mpc}$ . A standard halo occupation distribution model evaluated near the best fit Planck  $\Lambda$ CDM cosmology provides a good fit to the observed anisotropic clustering, and implies a normalization for the peculiar velocity field of  $M \sim 2 \times 10^{13} h^{-1} M_{\odot}$  halos of  $f\sigma_8(z = 0.57) = 0.450 \pm 0.011$ . Since this constraint includes both quasi-linear and non-linear scales, it should severely constrain modified gravity models that enhance pairwise infall velocities on these scales. Though model dependent, our measurement represents a factor of 2.5 improvement in precision over the analysis of DR11 on large scales,  $f\sigma_8(z = 0.57) = 0.447 \pm 0.028$ , and is the tightest single constraint on the growth rate of cosmic structure to date. Our measurement is consistent with the Planck  $\Lambda$ CDM prediction of  $0.480 \pm 0.010$  at the  $\sim 1.9\sigma$  level. Assuming a halo mass function evaluated at the best fit Planck cosmology, we also find that 10% of CMASS galaxies are satellites in halos of mass  $M \sim 6 \times 10^{13} h^{-1} M_{\odot}$ . While none of our tests and model generalizations indicate systematic errors due to an insufficiently detailed model of the galaxy-halo connection, the precision of these first results warrant further investigation into the modeling uncertainties and degeneracies with cosmological parameters.

**Key words:** cosmology: large-scale structure of Universe, cosmological parameters, galaxies: haloes, statistics

- ▶ Reid et al. 2014 made a 2.5% measurement of  $f\sigma_8$  using small-scale clustering within the BOSS CMASS sample
- ▶ Found factor of 2.5 improvement in statistical error over large scales
- ▶ Systematics dominated by fixed cosmology modelling and fibre collision effect

**WHAT DO YOU DO BETTER?**

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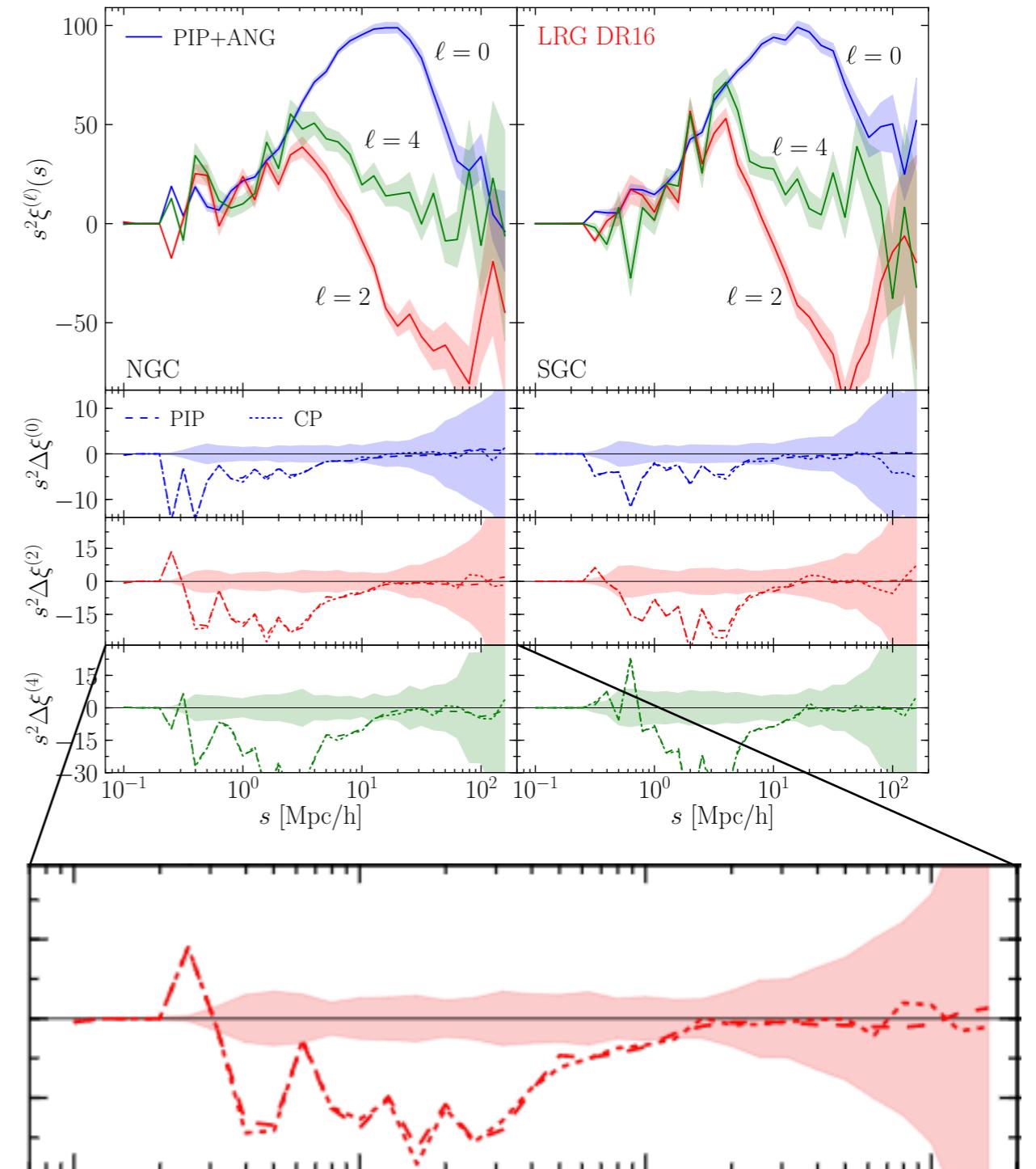
**METHODS**

# PAIRWISE-INVERSE-PROBABILITY WEIGHTING (PIP)

- ▶ Inversely weight pairs by the probability of the pair being observed
- ▶ Combined with angular upweighting (ANG) to correct single-pass regions

$$DD(\vec{s}) = \sum w_{mn}^{\text{PIP}} w_m^{\text{tot}} w_n^{\text{tot}} \times \frac{DD_{\text{par}}(\theta)}{DD_{\text{fib}}^{\text{PIP}}(\theta)}$$

- ▶ See Mohammad et al. 2020 (2007.09005) for details



# HALO OCCUPATION DISTRIBUTION (HOD)

- ▶ Probability distribution  $P(N | M)$  that a halo of mass  $M$  contains  $N$  galaxies
- ▶ Our model separates the occupation of centrals and satellites, and depends on 5 free parameters

$$N_{cen}(M) = \frac{f_{max}}{2} \left[ 1 + \text{erf} \left( \frac{\log_{10} M - \log_{10} M_{min}}{\sigma_{\log M}} \right) \right]$$

$$N_{sat}(M) = \left( \frac{M}{M_{sat}} \right)^\alpha \exp \left( -\frac{M_{cut}}{M} \right) \frac{N_{cen}(M)}{f_{max}}$$

# AEMULUS COSMOLOGICAL EMULATOR

- ▶ Gaussian process based machine learning from N-body simulations to predict galaxy correlation functions to <1% without the need to run additional simulations each step
- ▶ 16 parameter model; 7 wCDM parameters and 9 HOD parameters

wCDM:  $\Omega_m, \Omega_b, \sigma_8, h, n_s, N_{eff}, w$

HOD:  $\log M_{sat}, \alpha, \log M_{cut}, \sigma_{\log M}, f_{max}, v_{bc}, v_{bs}, c_{vir}, \gamma_f$

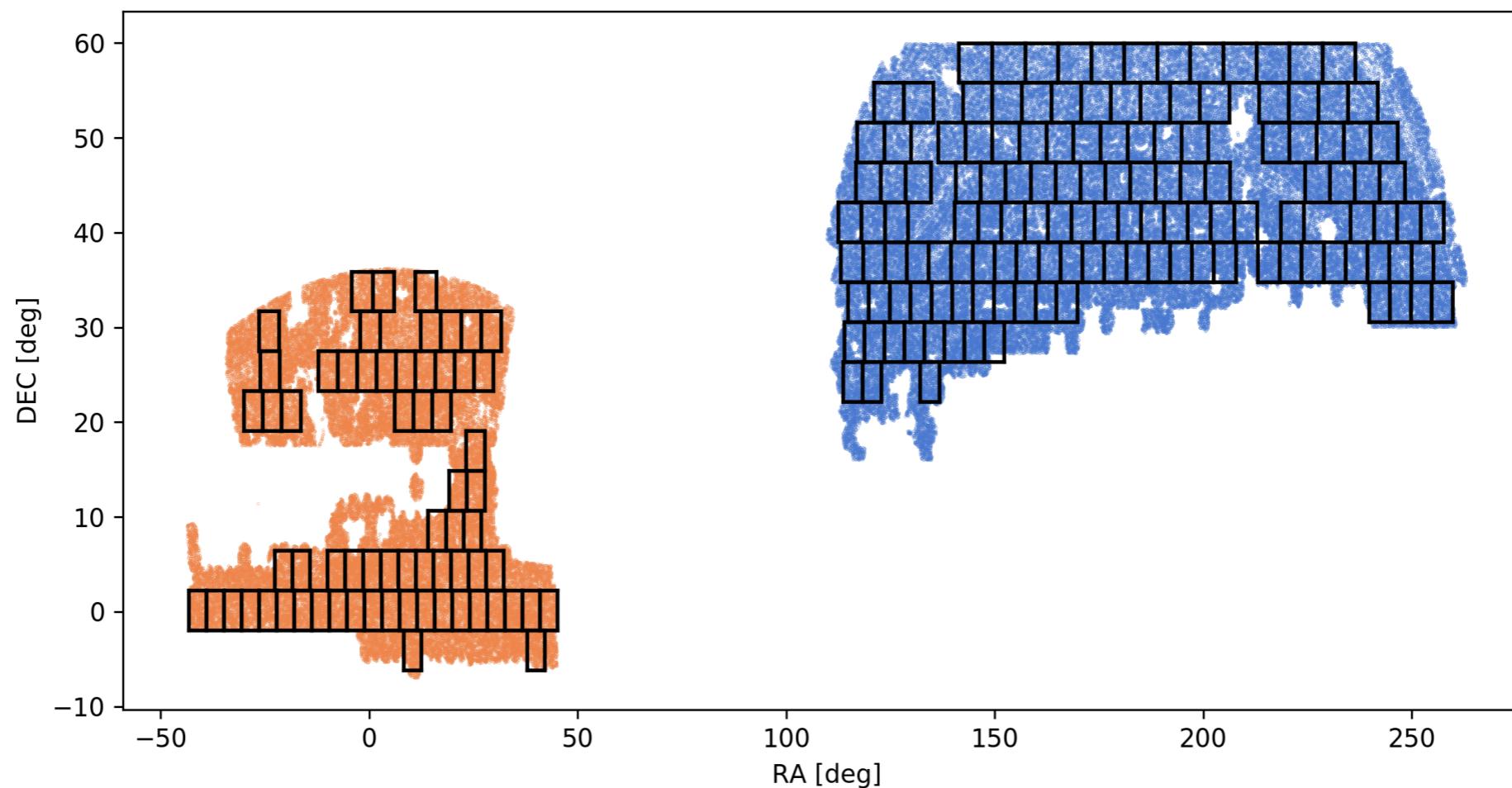
- ▶ In the linear regime a fractional change in  $\gamma_f$  is equal to a fractional change in the linear growth rate,  $f = \gamma_f f_{wCDM}$
- ▶ We keep  $N_{eff}, w$  fixed for a total of 14 free parameters

# JACKKNIFE COVARIANCE MATRIX

- Divide survey into equal area regions, and remove regions with low occupation to ensure all regions contribute approximately equally and are not affected by geometry

$$C_{i,j} = \frac{n-1}{n} \sum_k (\xi_{i,k} - \bar{\xi}_i)(\xi_{j,k} - \bar{\xi}_j)$$

- Rescale covariance matrix by the ratio of  $R_{\text{assigned}}/R_{\text{full}}$  to match effective volume of full sample



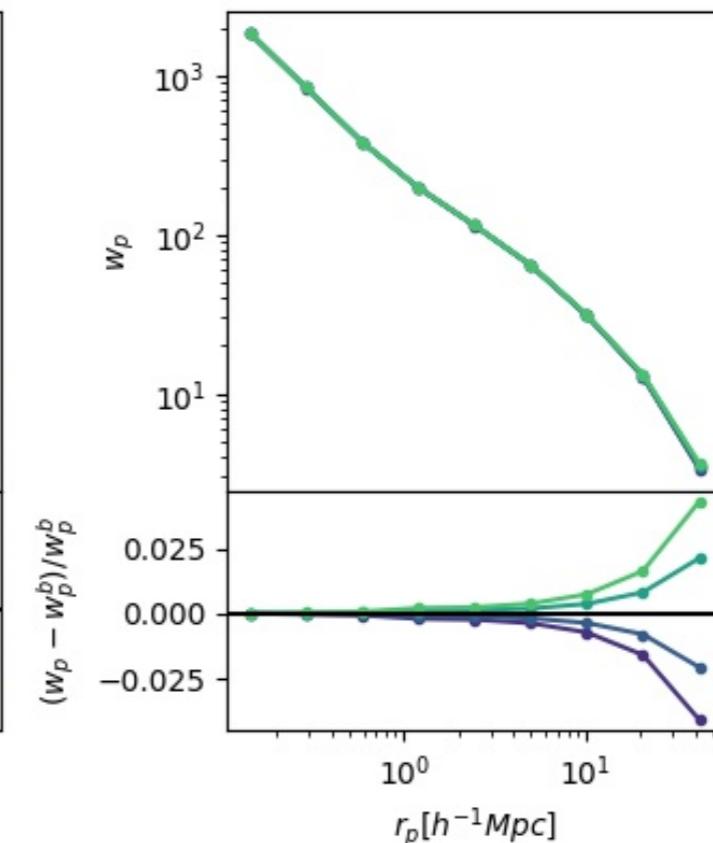
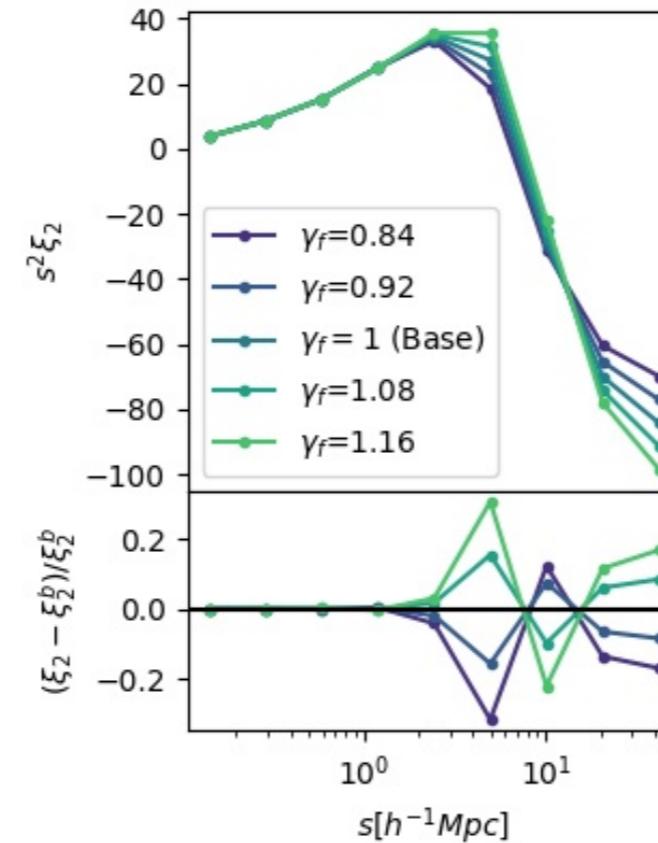
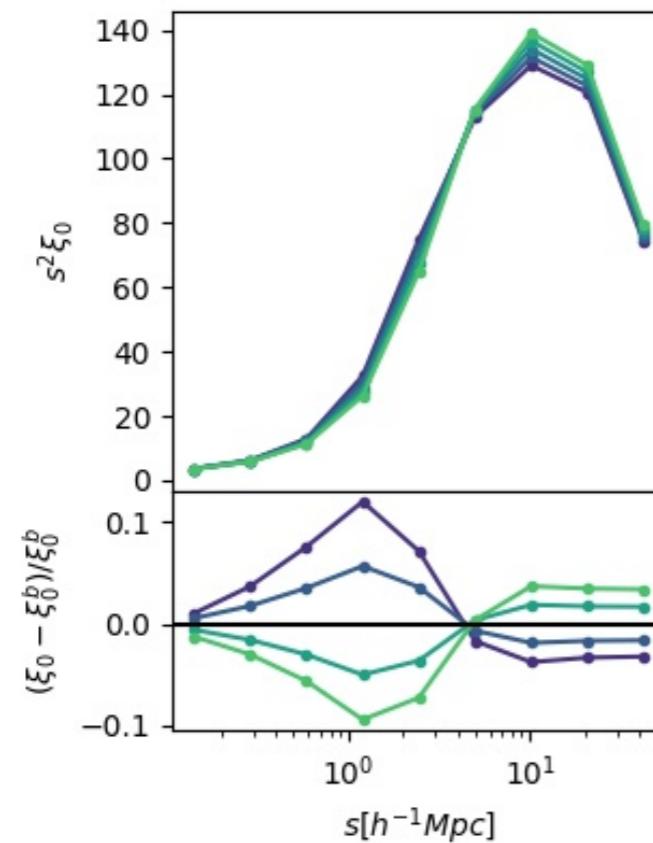
**GREAT. DOES IT WORK THOUGH?**

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**ROBUSTNESS CHECKS**

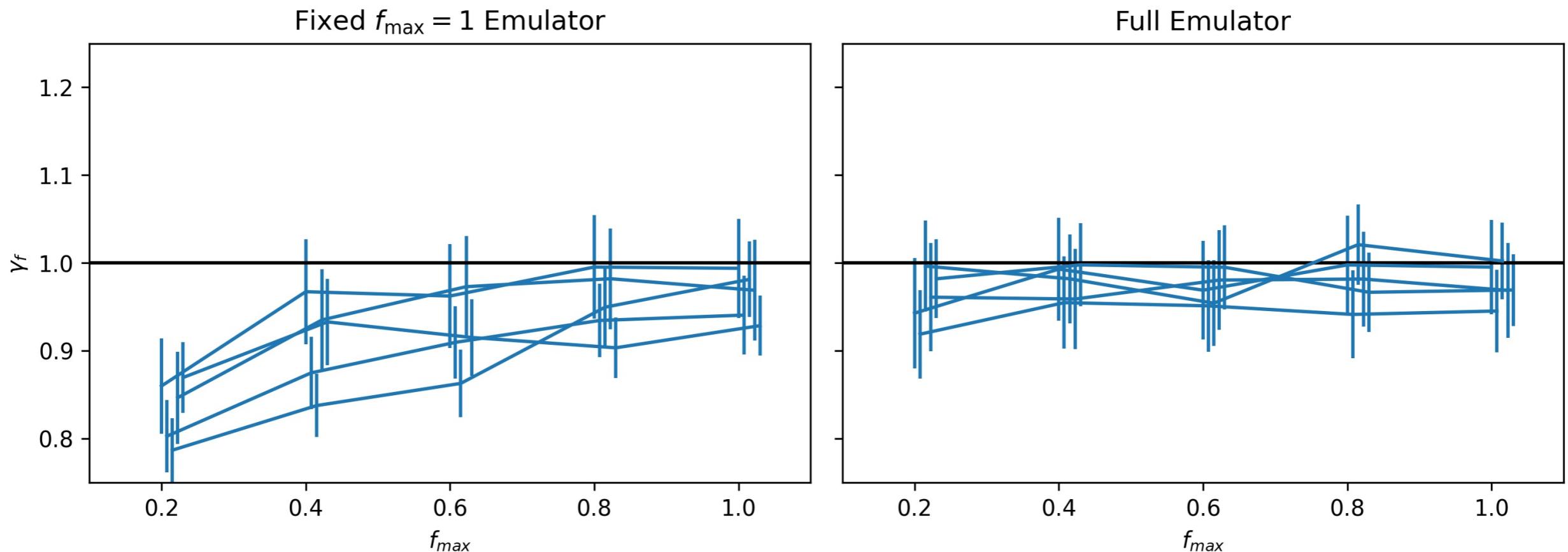
# NON-LINEAR VELOCITIES

- ▶ On linear scales a change in  $\gamma_f$  corresponds to a change in the growth rate, but this is not necessarily true on non-linear scales
- ▶ Identify  $7 h^{-1}\text{Mpc}$  as the transition, so use  $7 < r < 60 \text{ km/s}$  to constrain  $f\sigma_8$ , and  $\gamma_f$  as a test of  $\Lambda\text{CDM}$  using  $0.1 < r < 60 \text{ km/s}$



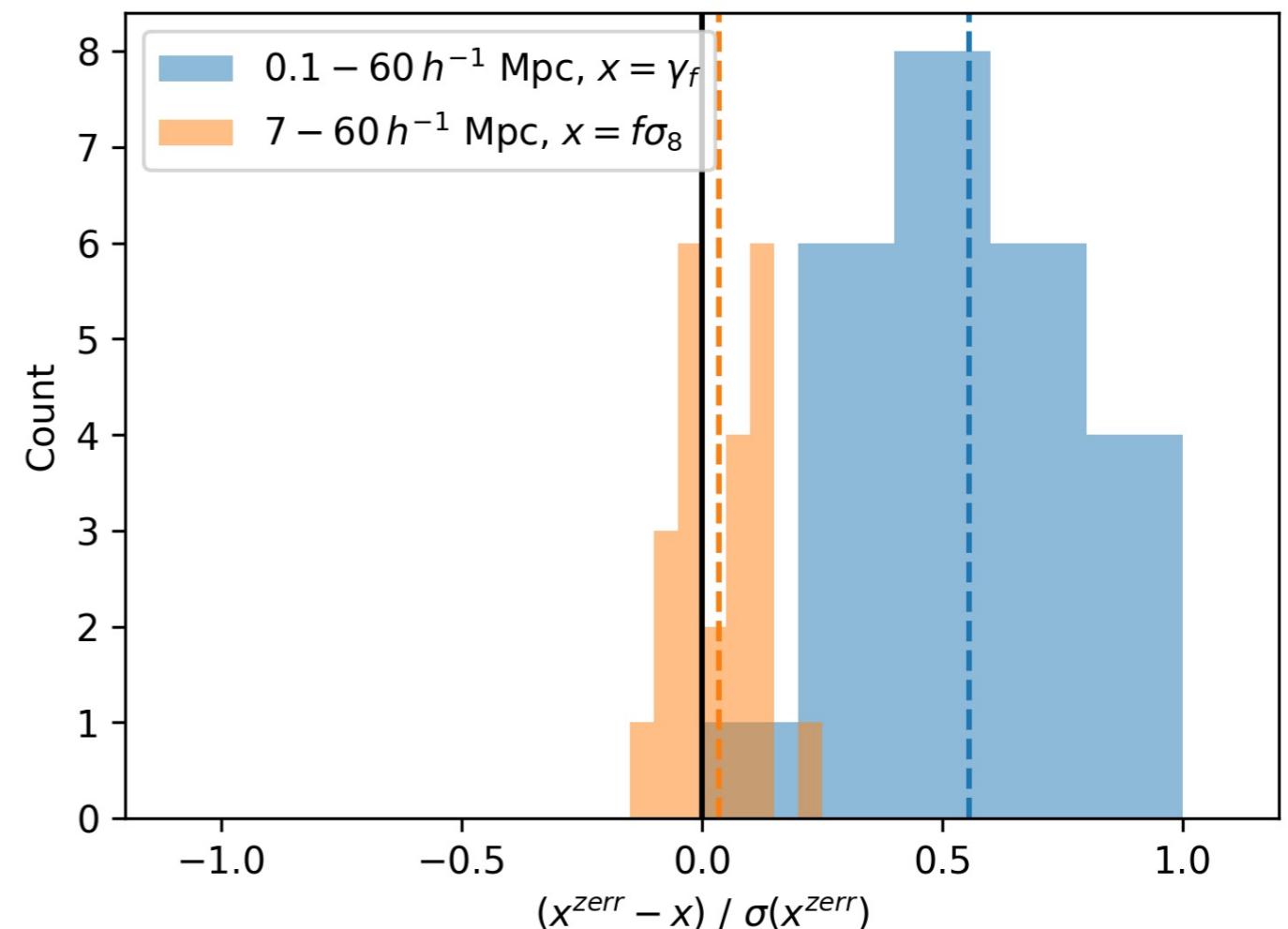
# GALaxy SELECTION

- ▶ eBOSS is targeted using magnitude cuts, so some bright galaxies are excluded
- ▶ Without  $f_{max}$  the HOD model assumes all high mass halos contain a central galaxy, so that the model sample is more highly biased than the data sample

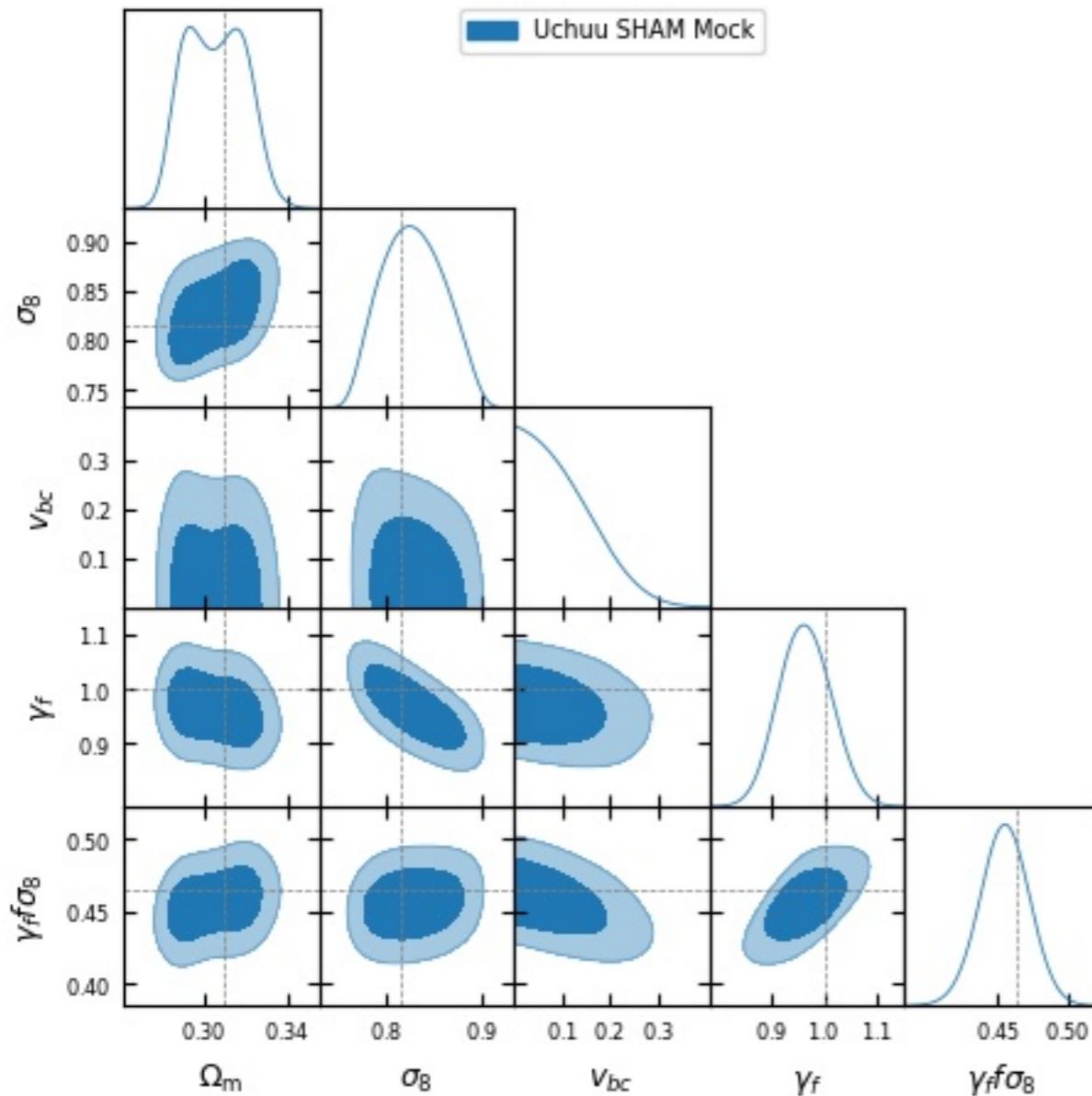


# REDSHIFT UNCERTAINTY

- ▶ The eBOSS sample has a redshift uncertainty well fit by a Gaussian of width  $\sigma = 91.8$  km/s, giving a mean offset of 65.6 km/s
- ▶ On non-linear scales the redshift uncertainty is similar to the halo velocities, giving a degeneracy with  $\gamma_f$
- ▶ Correcting this bias would increase our tension with  $\Lambda$ CDM



# MOCK TESTING



- ▶ Tested full pipeline using a SHAM mock
- ▶ Using a different galaxy-halo connection model shows that the HOD parameterization is robust
- ▶ Recovered the expected value of  $\gamma_f$

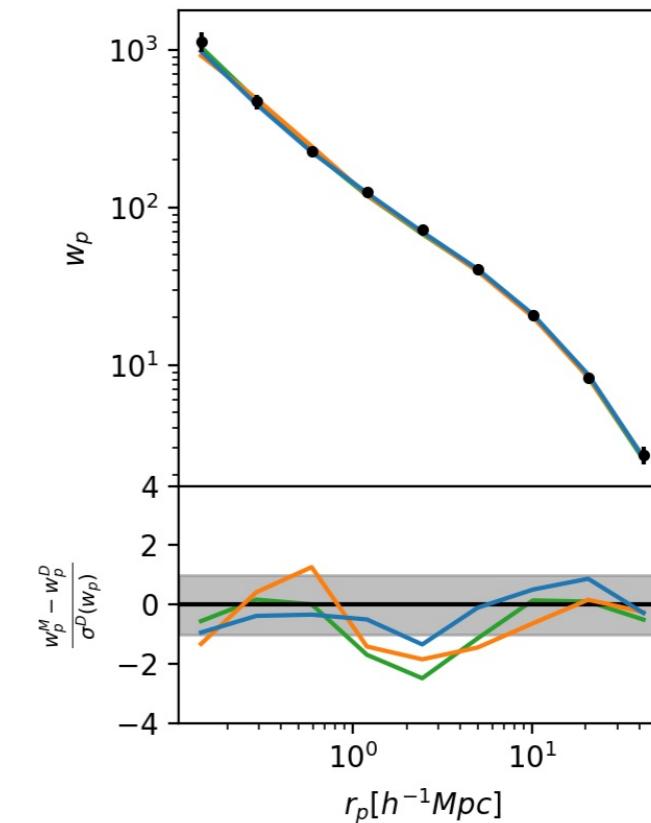
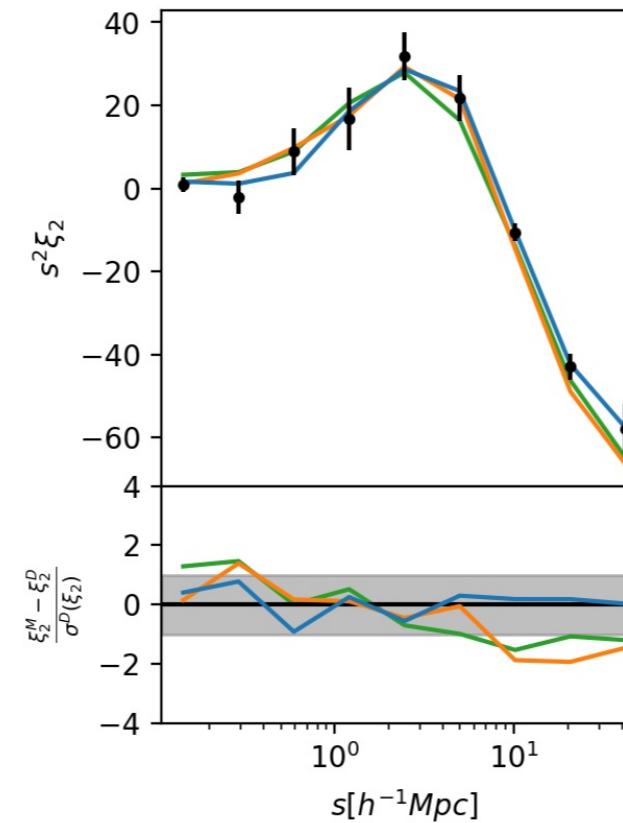
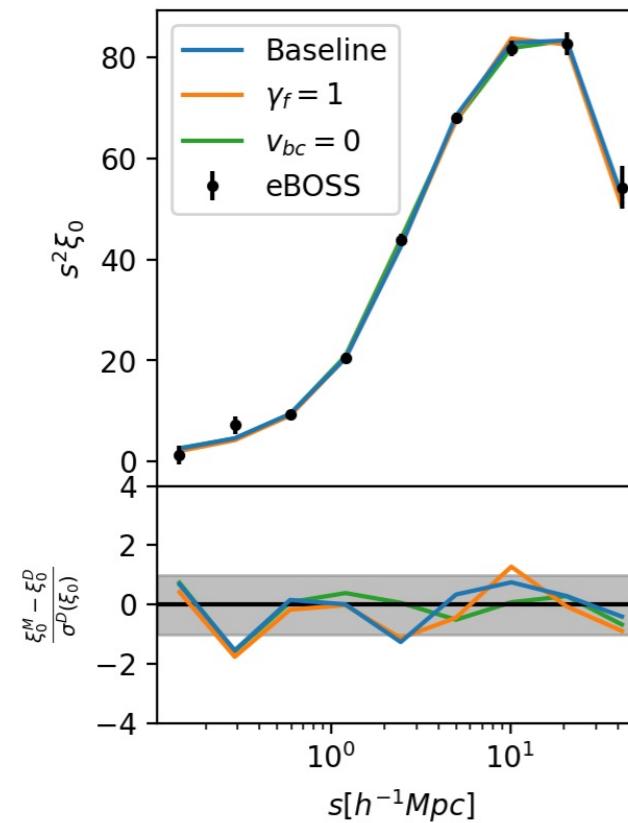
**GET TO THE INTERESTING PART  
ALREADY!**

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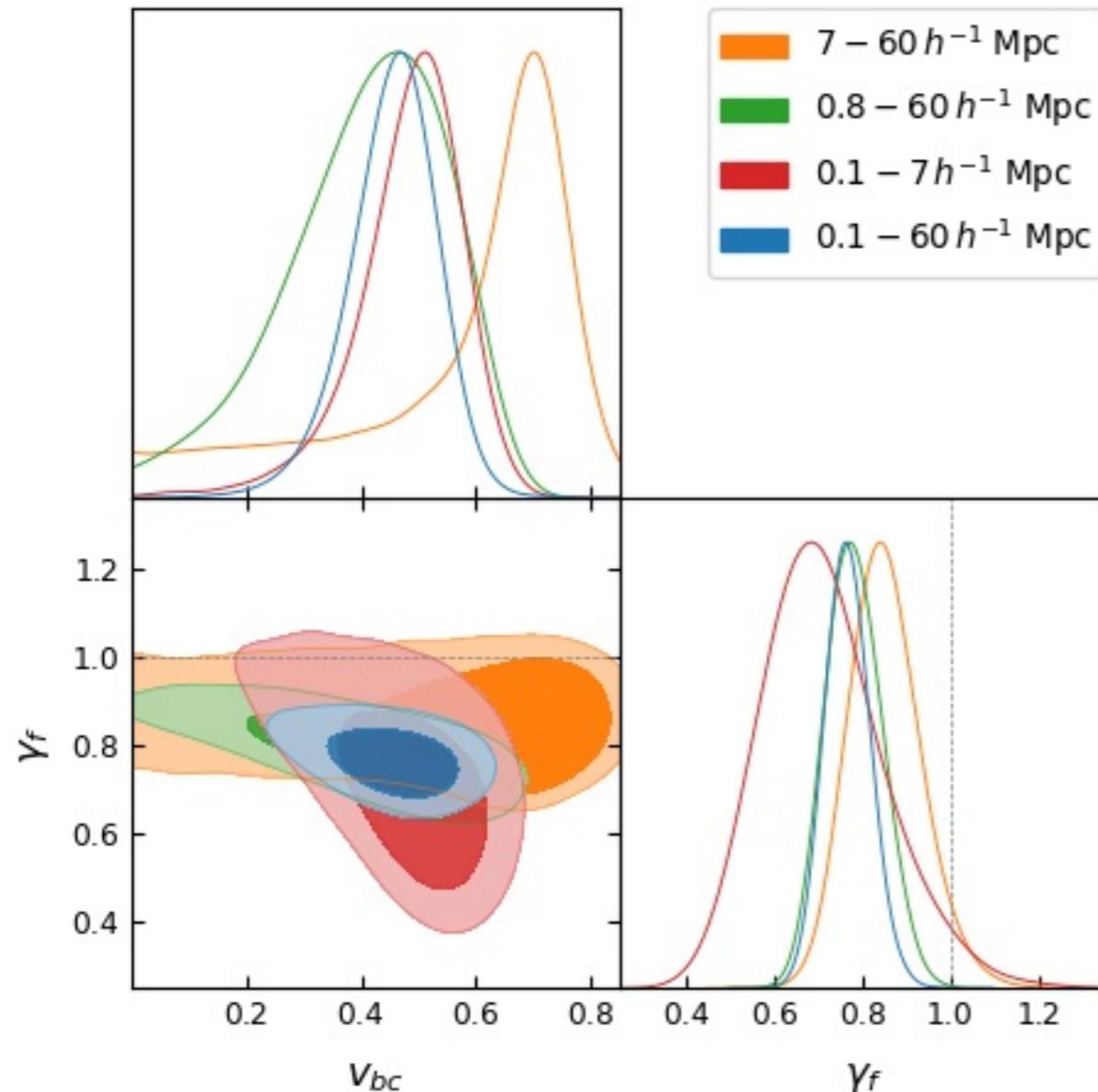
# **RESULTS**

# HEADLINE RESULTS

- ▶ Using  $7 < r < 60 \text{ km/s}$  measure  $f\sigma_8(z = 0.737) = 0.408 \pm 0.038$ ,  $1.4\sigma$  below the Planck2018 expectation and a factor of 1.7 better than the large scales
- ▶ Using  $0.1 < r < 60 \text{ km/s}$  measure  $\gamma_f = 0.767 \pm 0.052$ ,  $4.5\sigma$  below the value for  $\Lambda\text{CDM}$



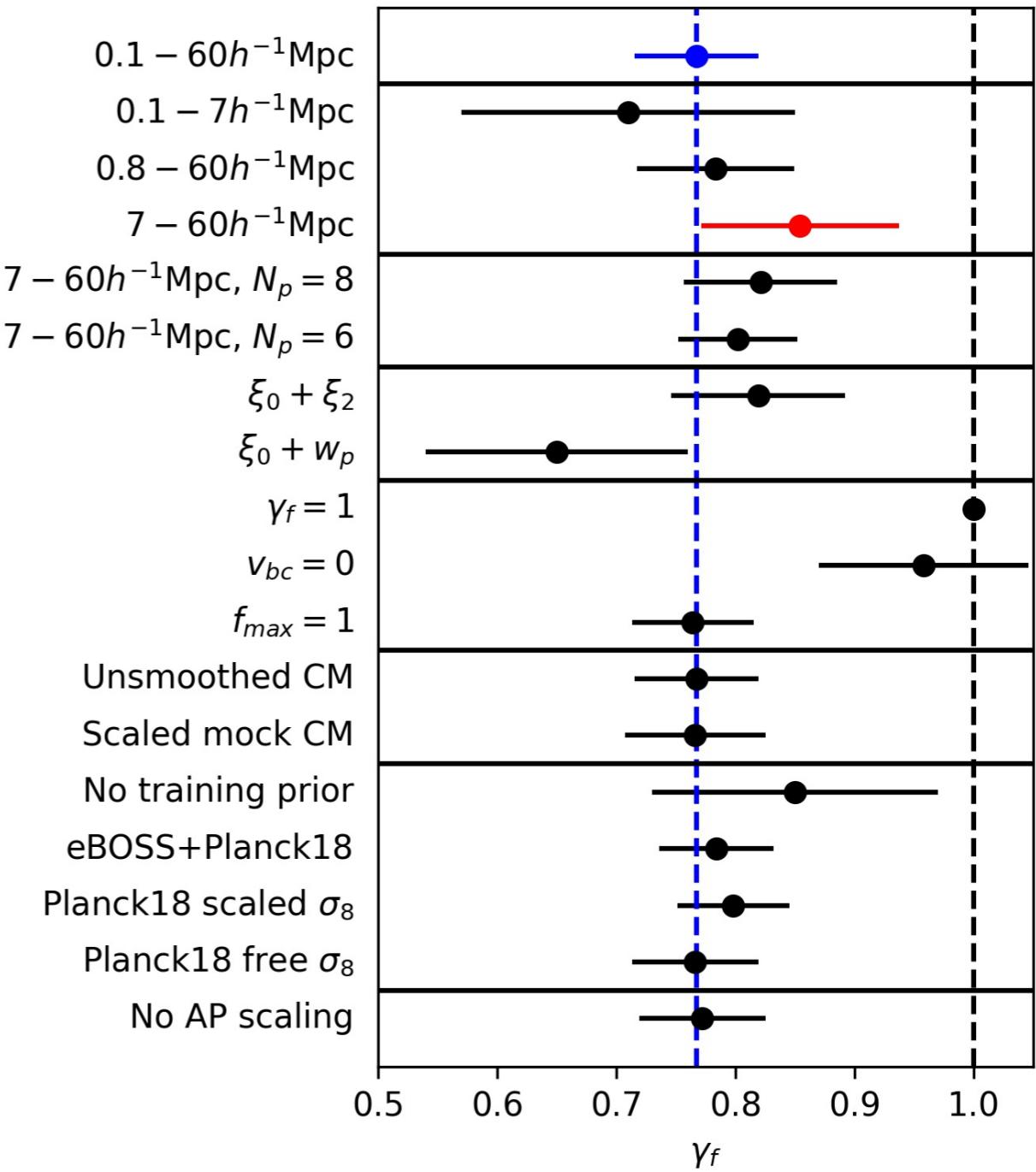
# SCALE DEPENDENCE



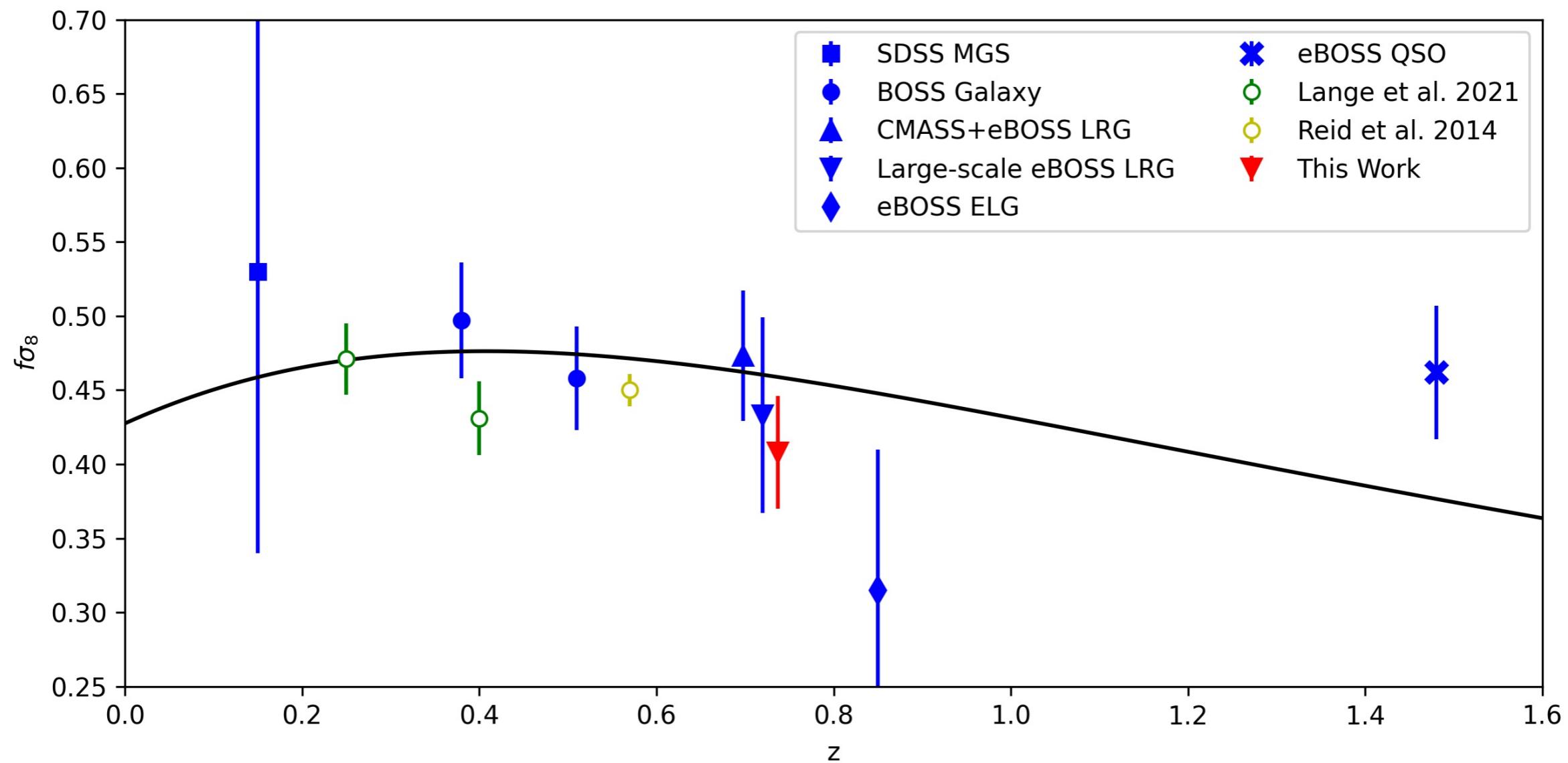
- ▶ Small scales prefer a low value of  $\gamma_f$  and non-zero  $v_{bc}$
- ▶ Large scales prefer a larger value of  $\gamma_f$  and no degeneracy with  $v_{bc}$
- ▶ The non-linear scales drive the stronger tension from all scales

## ALL FITS

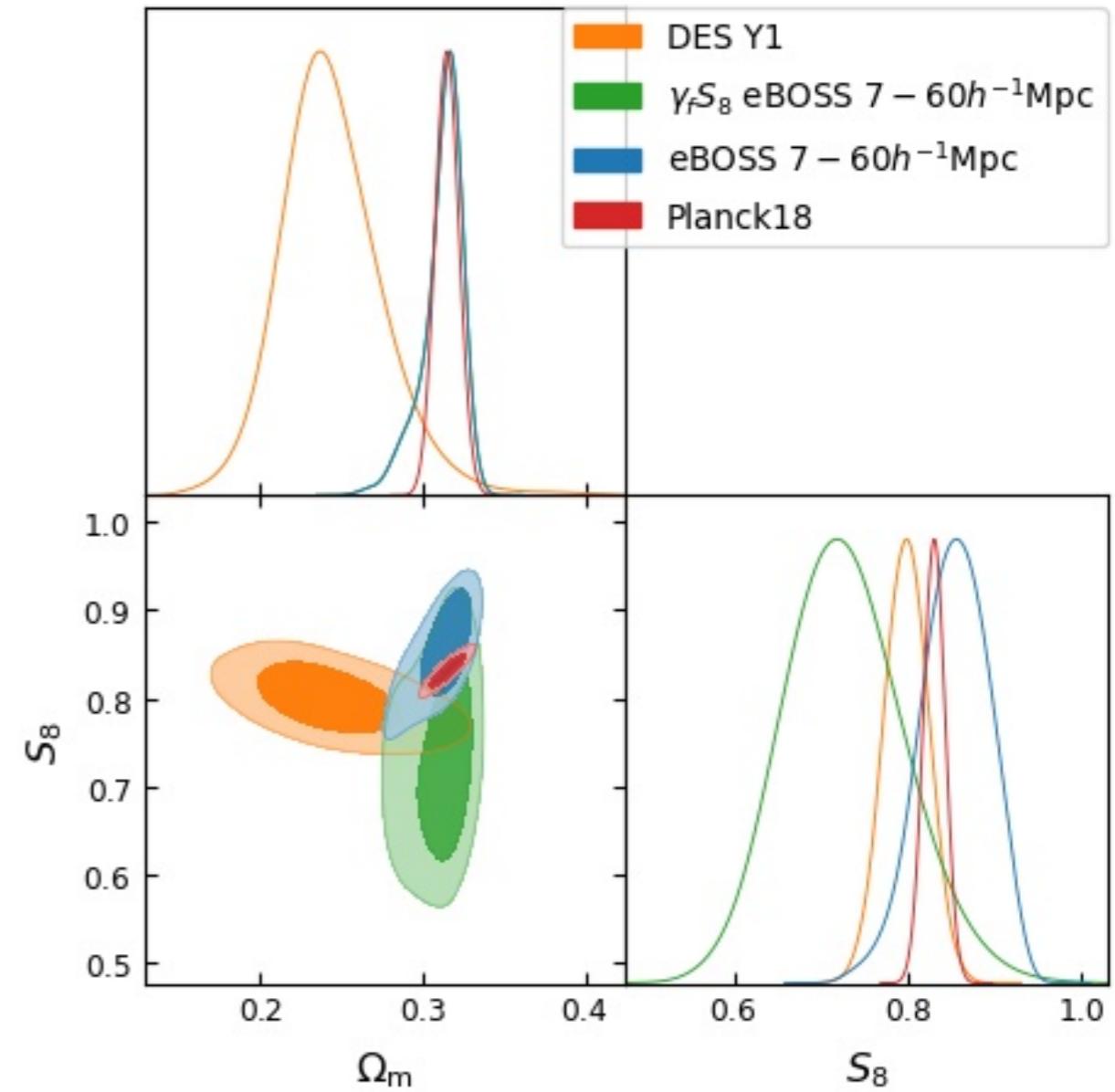
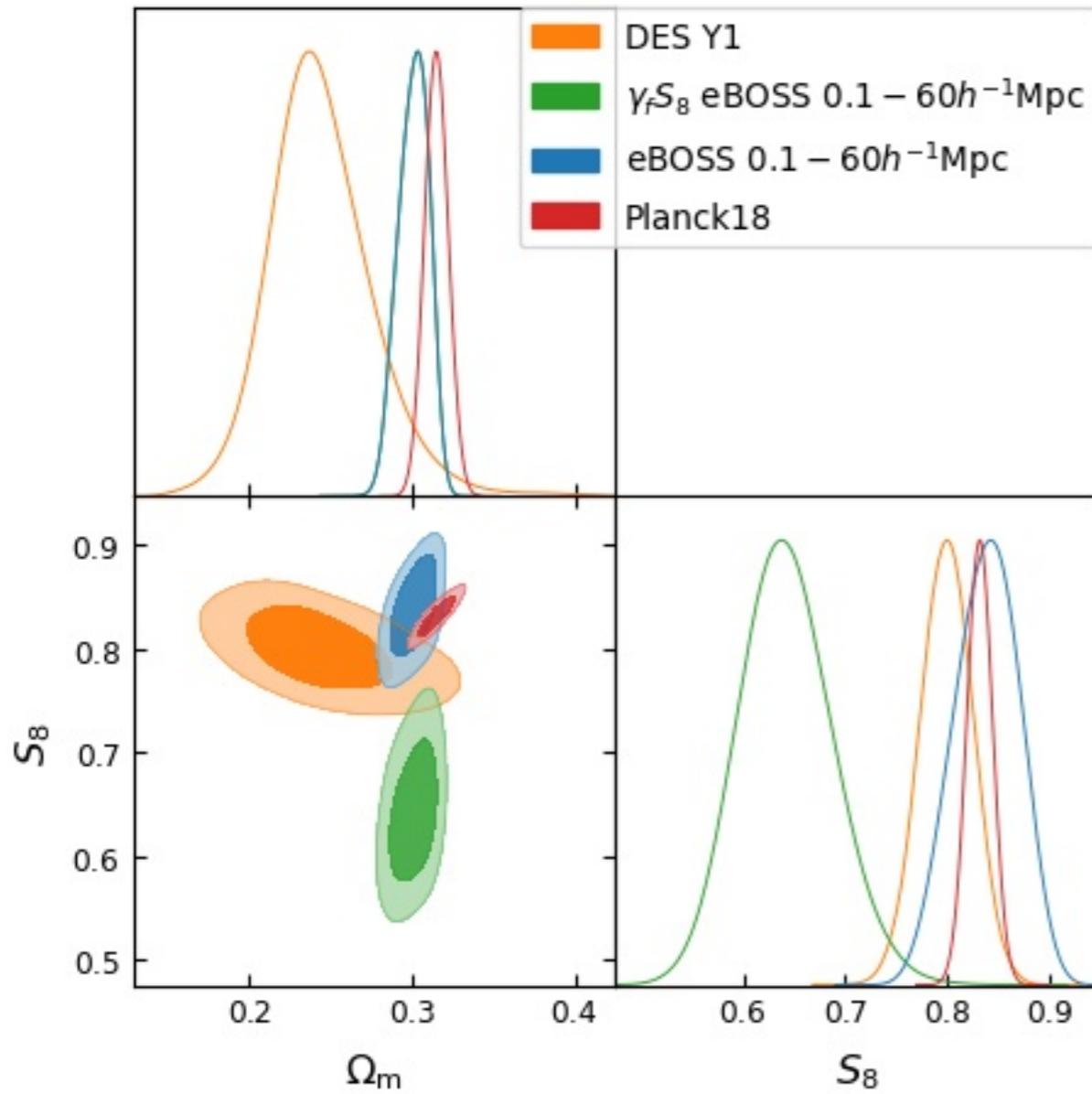
Run	$\gamma_f$	$N_P$	$N_D$	$\chi^2$
0.1 – $60 h^{-1}$ Mpc	$0.767 \pm 0.052$	14	27	14.1
0.1 – $7 h^{-1}$ Mpc	$0.71 \pm 0.14$	14	18	7.8
0.8 – $60 h^{-1}$ Mpc	$0.783 \pm 0.066$	14	18	4.2
7 – $60 h^{-1}$ Mpc	$0.854 \pm 0.083$	14	9	0.36
7 – $60 h^{-1}$ Mpc, 8 parameters	$0.821 \pm 0.064$	8	9	0.74
7 – $60 h^{-1}$ Mpc, 6 parameters	$0.802 \pm 0.050$	6	9	1.8
$\xi_0 + \xi_2$	$0.819 \pm 0.073$	14	18	5.0
$\xi_0 + w_p$	$0.65 \pm 0.11$	14	18	5.4
$\gamma_f = 1$	1	13	27	28.0
$v_{bc} = 0$	$0.958 \pm 0.088$	13	27	22.5
$f_{max} = 1$	$0.764 \pm 0.051$	13	27	16.6
Unsmoothed covariance matrix	$0.767 \pm 0.052$	14	27	14.3
Scaled mock covariance matrix	$0.766 \pm 0.059$	14	27	12.0
No training prior	$0.85 \pm 0.12$	14	27	12.1
eBOSS+Planck18	$0.784 \pm 0.048$	14*	27	18.5
eBOSS+Planck18 scaled $\sigma_8$	$0.798 \pm 0.047$	14*	27	19.1
eBOSS+Planck18 free $\sigma_8$	$0.766 \pm 0.053$	14*	27	18.0
No AP scaling	$0.772 \pm 0.053$	14	27	14.5



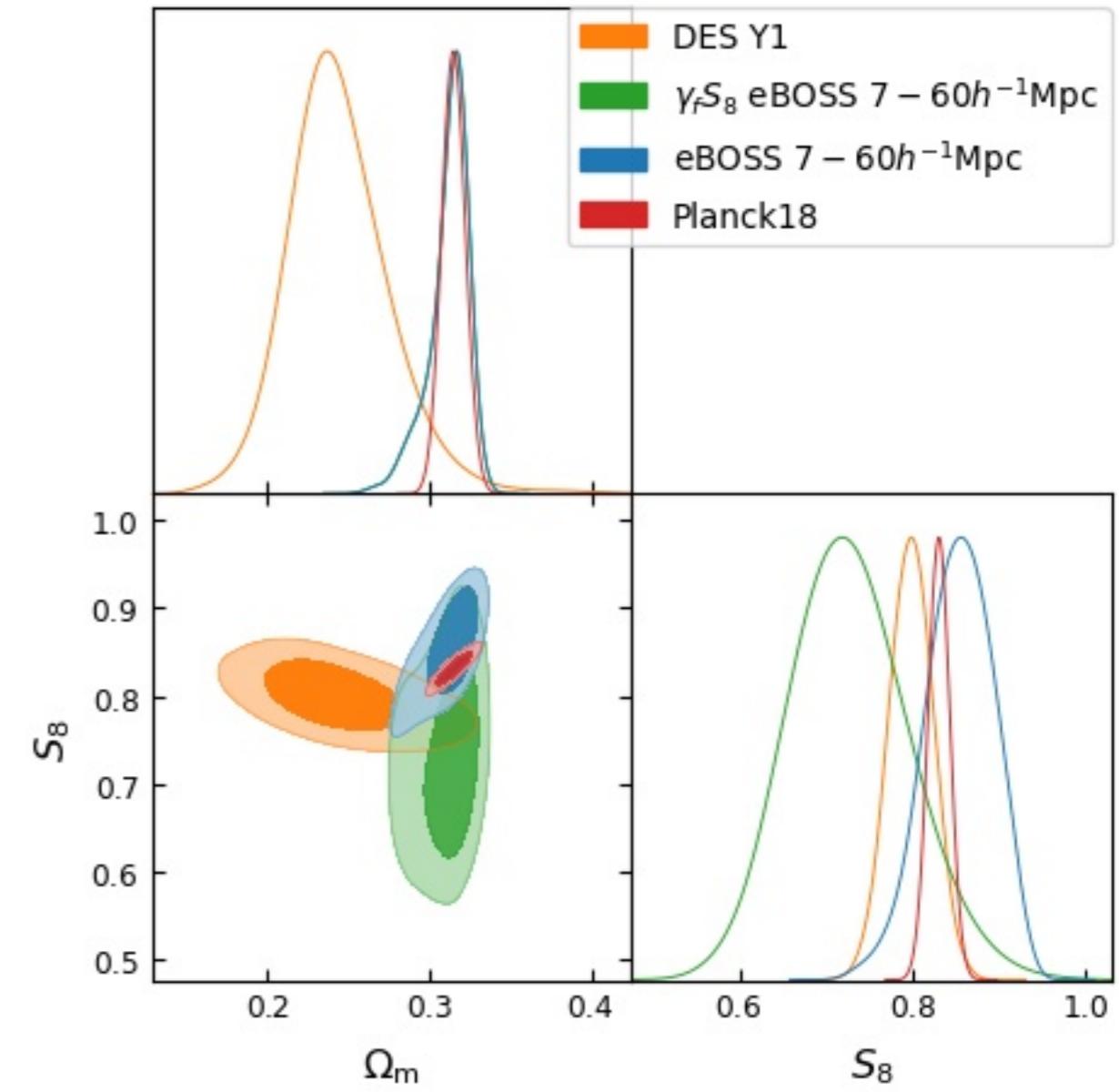
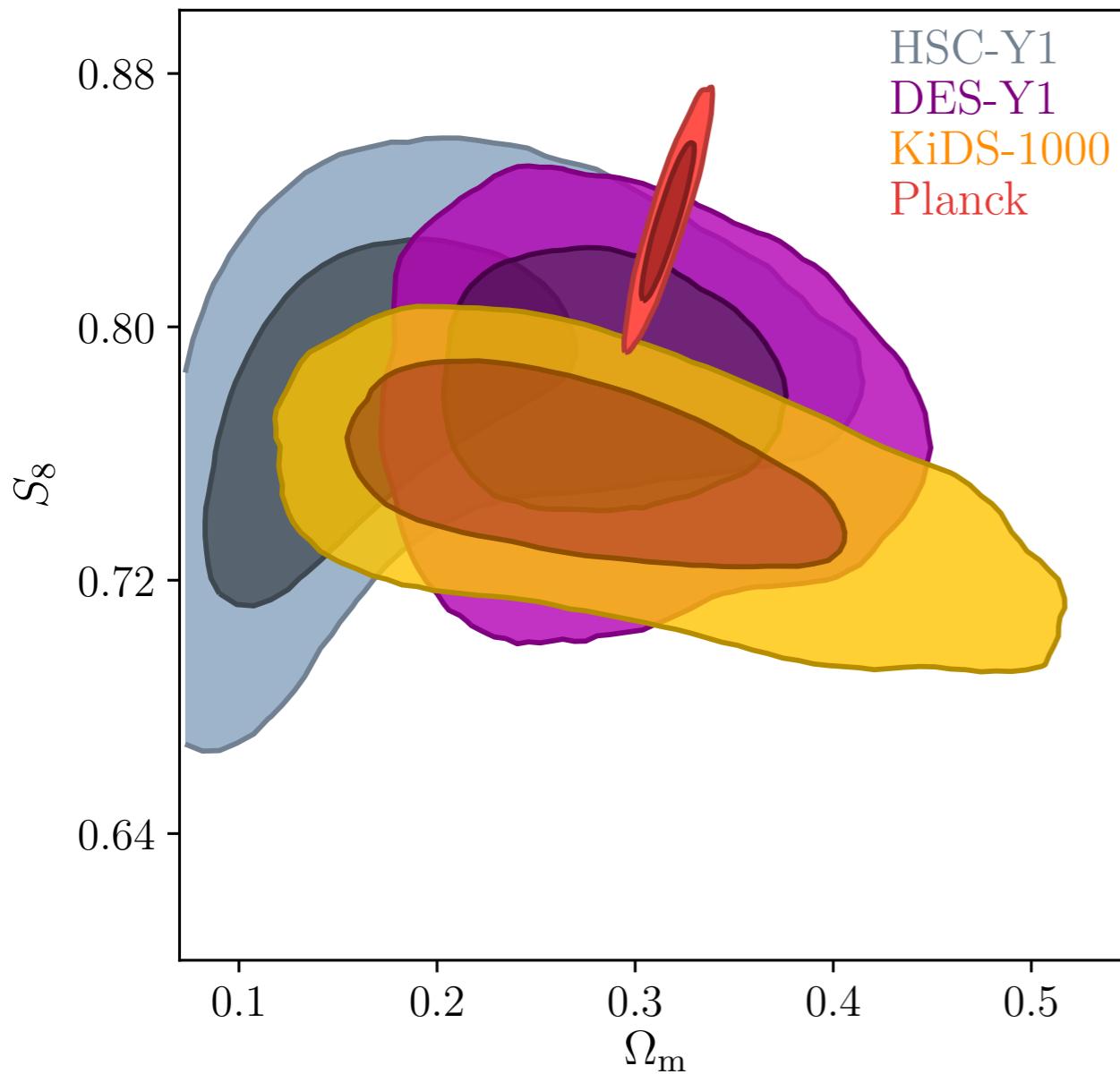
# COMPARISON TO OTHER SDSS RESULTS



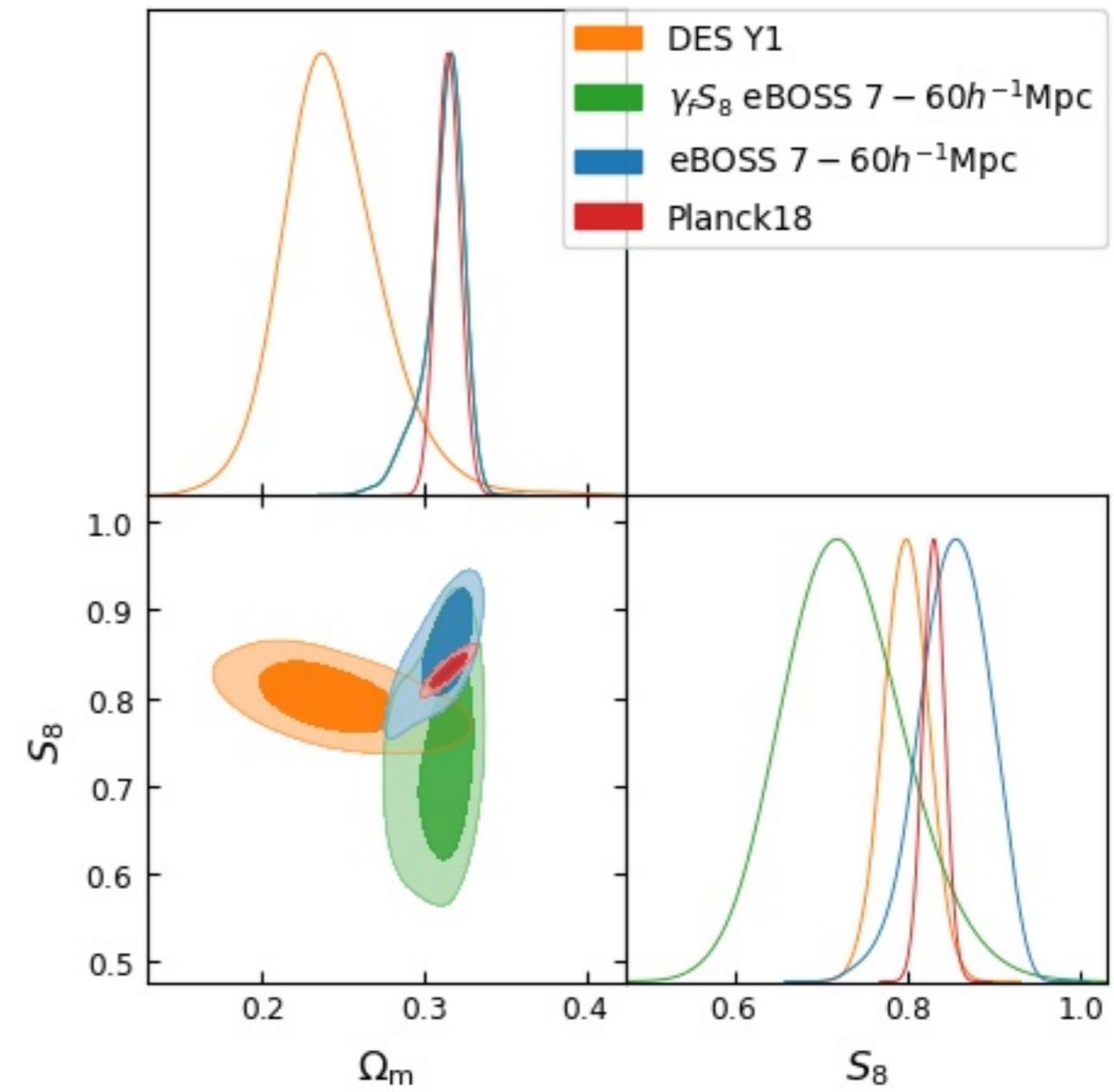
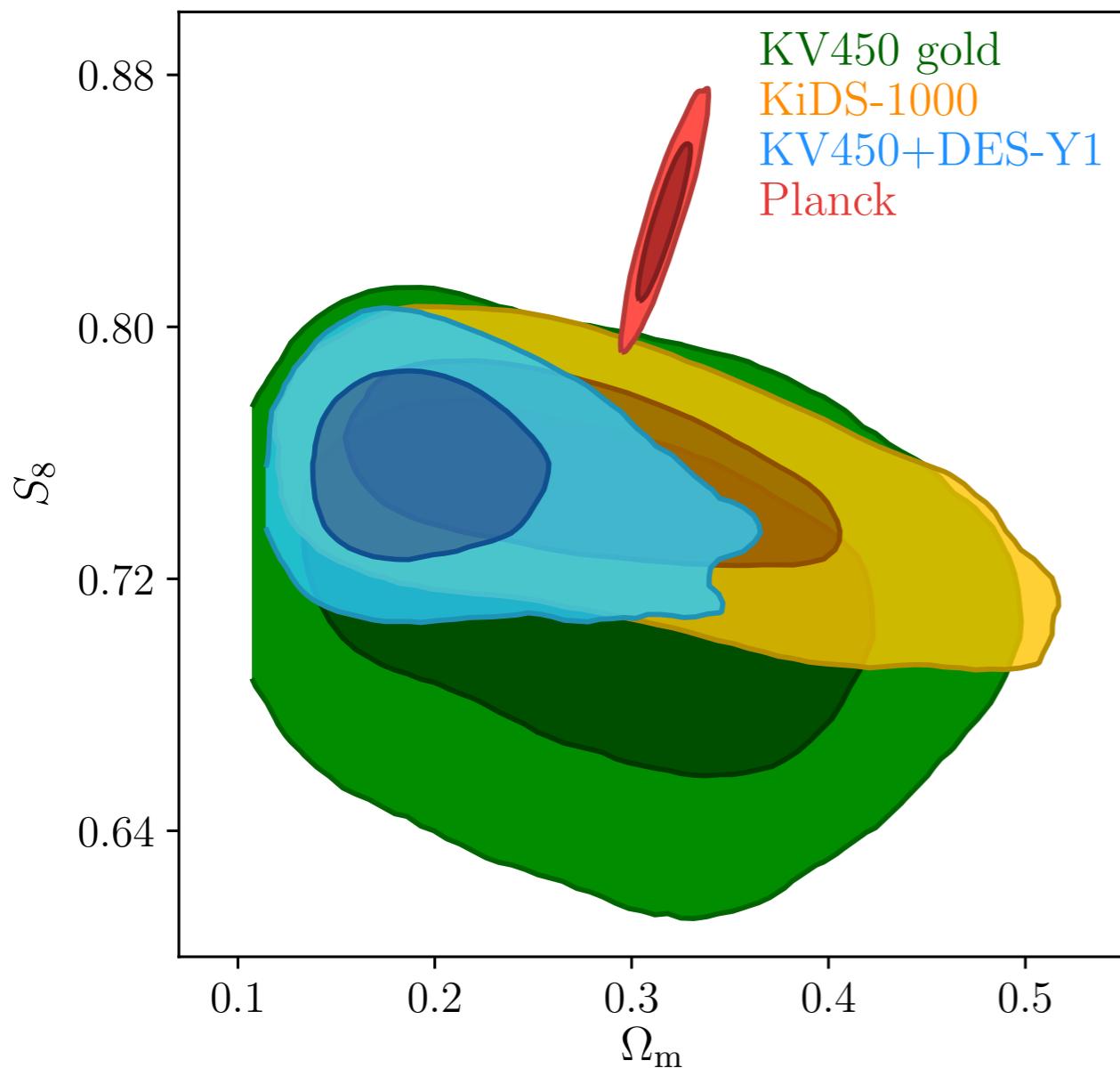
# COMPARISON TO LENSING



# COMPARISON TO LENSING



# COMPARISON TO LENSING



## POTENTIAL IMPROVEMENTS

- ▶ Redshift uncertainty is a significant source of systematic uncertainty, especially at higher redshifts (DESI, Euclid)
- ▶ The uncertainty is limited by the emulator error in many measurement bins
- ▶ We make a conservative separation cut to isolate the linear information, but additional information could be extracted from non-linear scales
- ▶ The source of the tension from non-linear scales is unknown (baryonic physics, HOD model breakdown, new physics?)

## SUMMARY

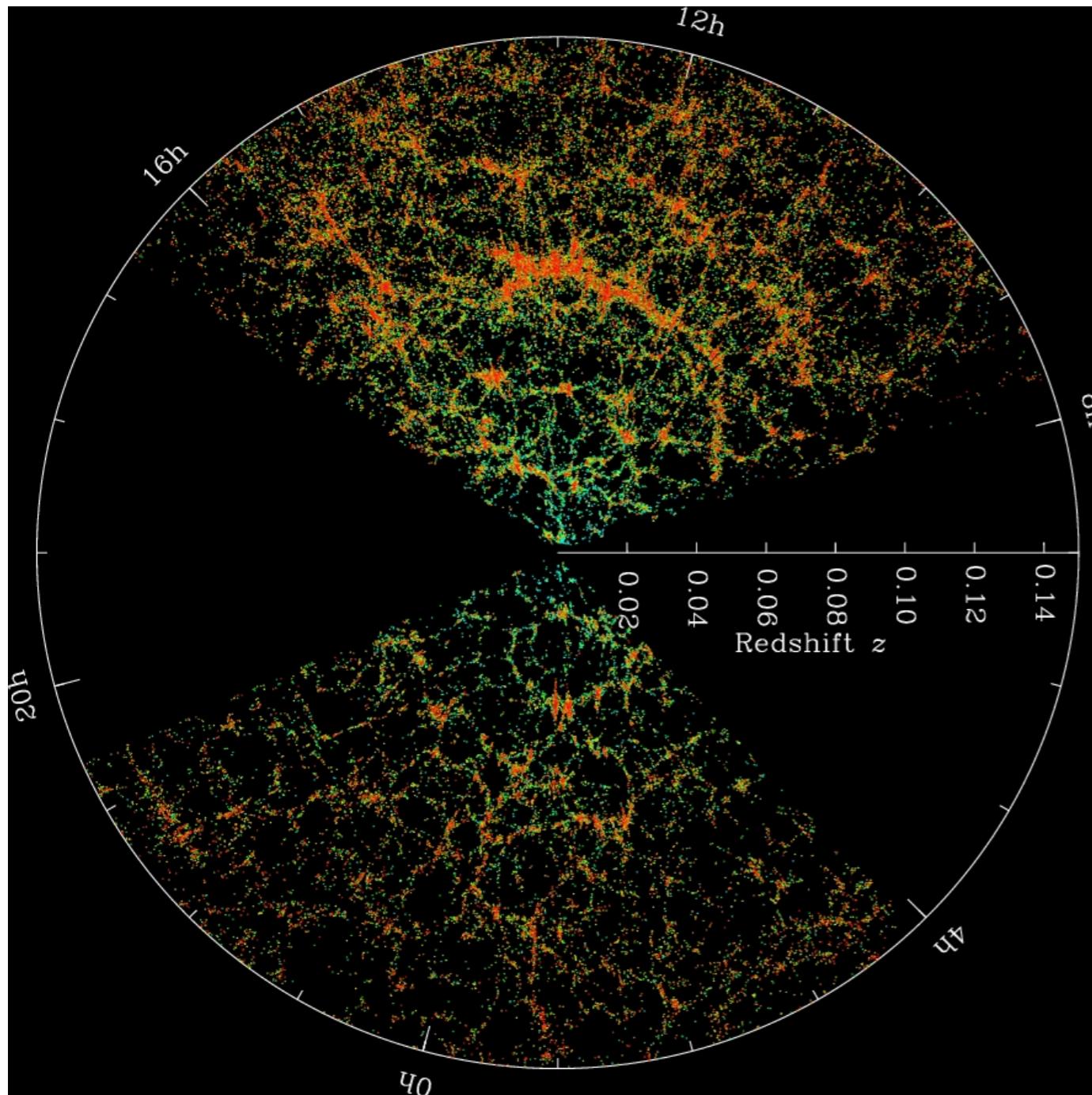
- ▶ We use PIP+ANG weights and Aemulus emulator remove the major systematics of previous analyses
- ▶ Measure  $f\sigma_8(z = 0.737) = 0.408 \pm 0.038$ ,  $1.4\sigma$  below the Planck2018 expectation and a factor of 1.7 better than the large scales
- ▶ Using  $0.1 < r < 60$  km/s find  $4.5\sigma$  tension with  $\Lambda$ CDM
- ▶ Redshift uncertainty, impact of non-linear velocities, and breakdown of HOD model important for future analyses
- ▶ Contact me at **[mj3chapm@uwaterloo.ca](mailto:mj3chapm@uwaterloo.ca)** with additional comments and questions!

**BUT WHAT ABOUT...?**

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**EXTRA SLIDES**

# SPECTROSCOPIC GALAXY SURVEYS

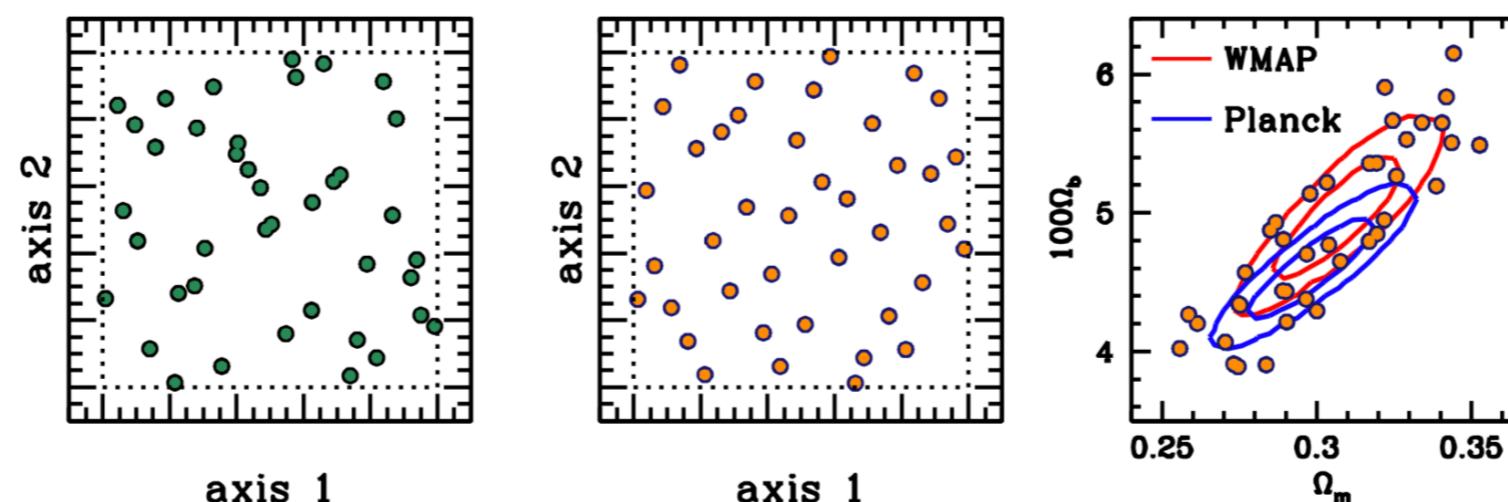


- ▶ Determine redshift from spectra of distant galaxies
- ▶ Redshifts are converted to distances assuming the recession is caused by the expansion of the Universe

$$d_C(z) = c \int_0^z \frac{dz'}{H(z')}$$

# AEMULUS COSMOLOGICAL EMULATOR

- ▶ Gaussian process based machine learning from N-body simulations to predict galaxy correlation functions
- ▶ Latin hypercube efficiently samples cosmological parameter space
- ▶ Results accurate to <1% without the need to run additional simulations each step



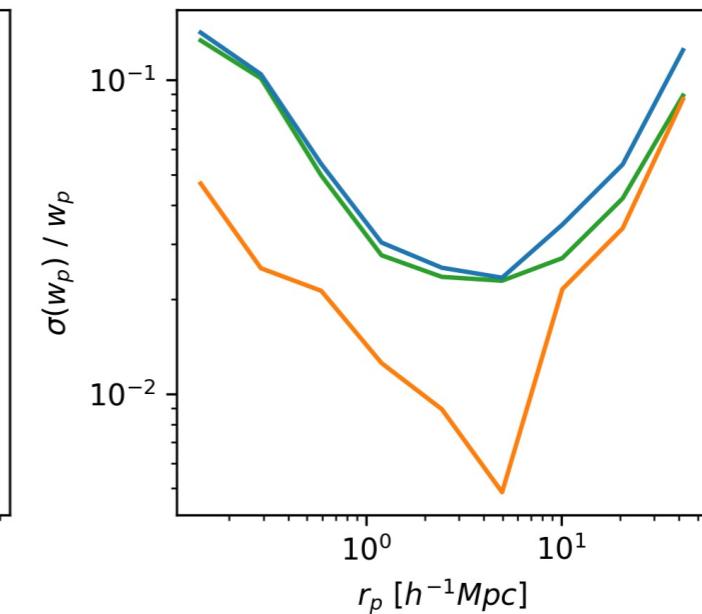
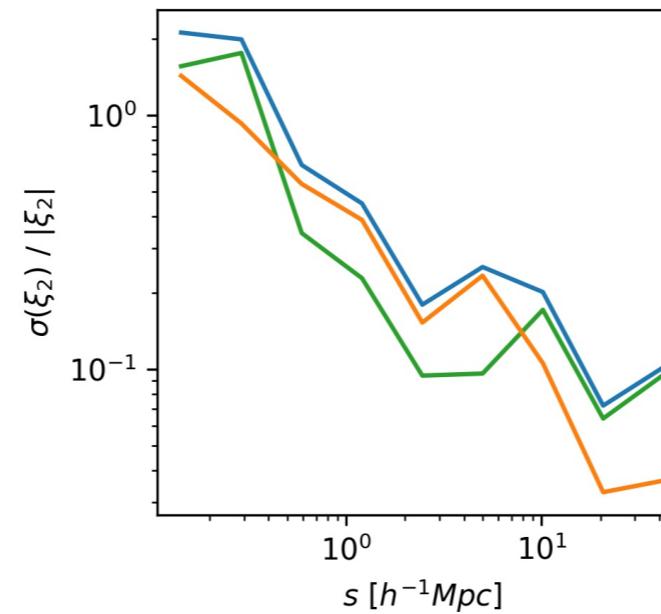
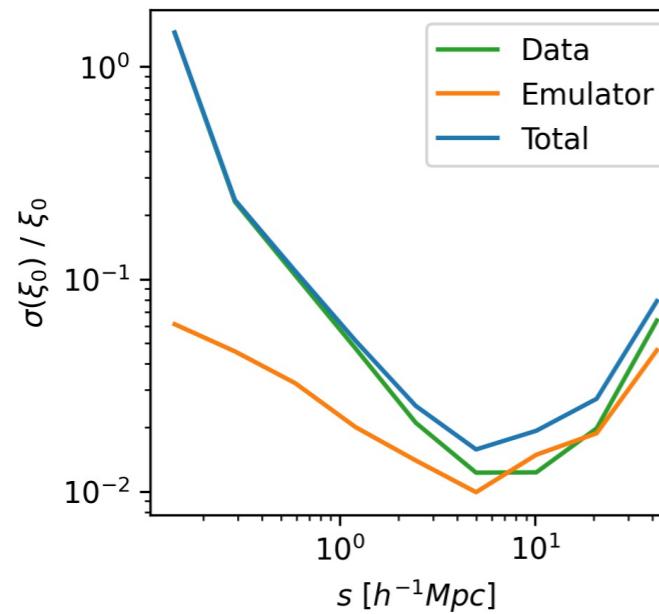
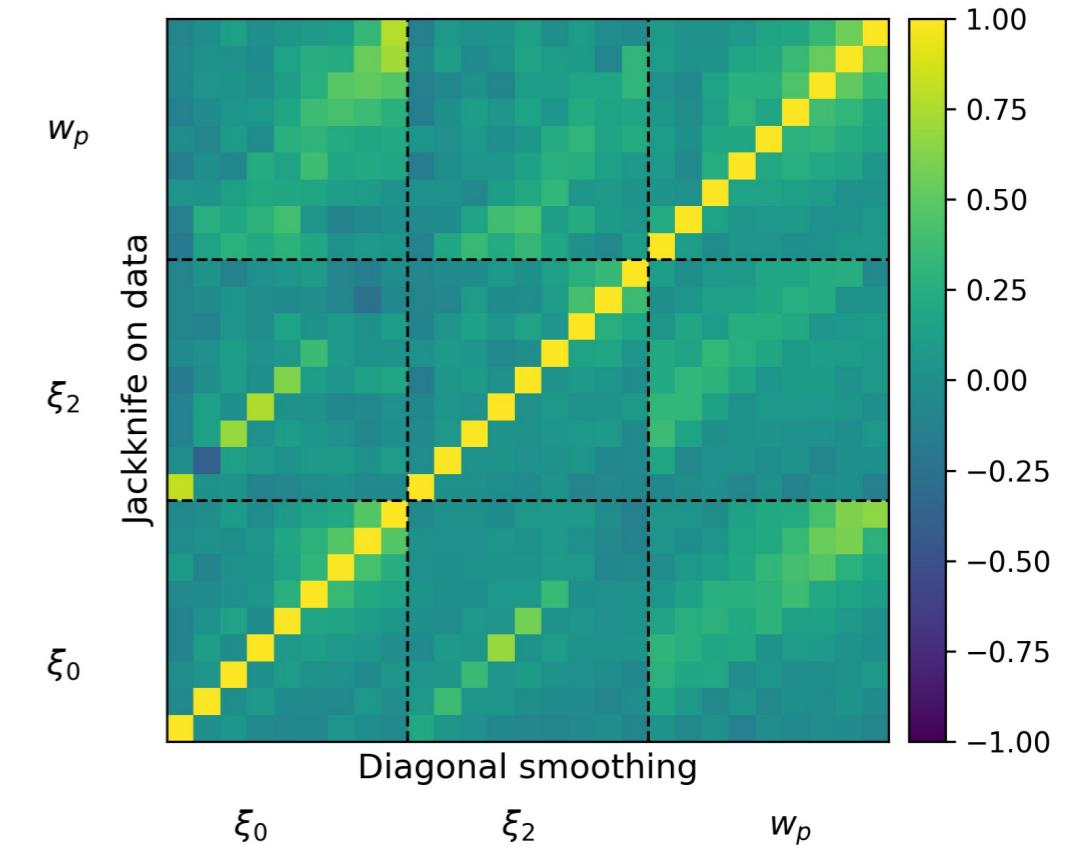
2D Projection of 7D parameter space, DeRose et al. 2018  
(1804.05865)

## JACKKNIFE COVARIANCE MATRIX

1. Choose occupation threshold,  $N_t$ , desired number of regions,  $N_R$ , and estimated region size,  $l$
2. Cover eBOSS footprint with equal area square regions of side length  $l$
3. Remove all regions below occupation threshold ( $N < N_t$ )
4. If number of remaining regions,  $N_r$ , is greater than  $N_R$  proceed to Step 5, otherwise reduce  $l$  and repeat Steps 2-4
5. Remove lowest occupation regions until  $N_r = N_R$

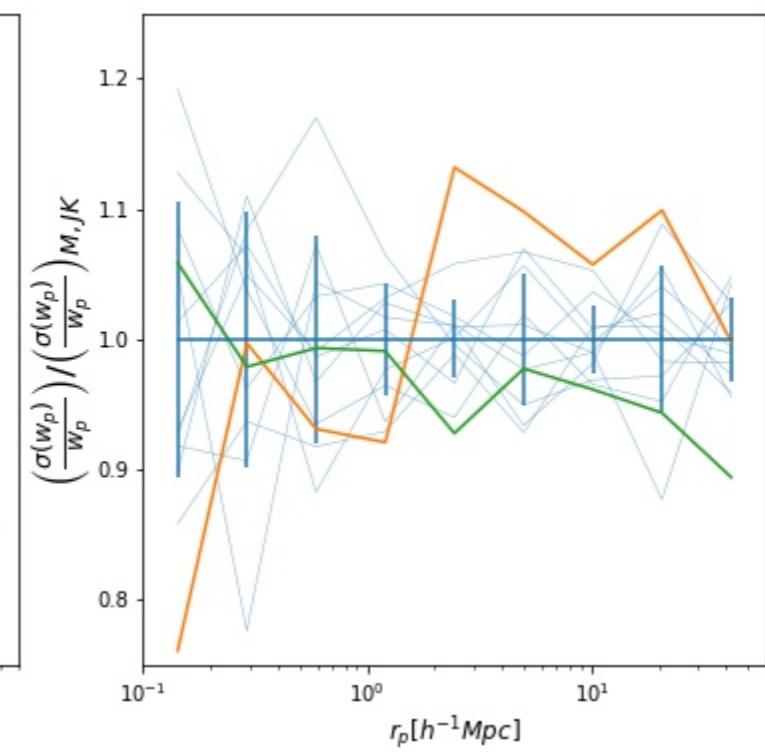
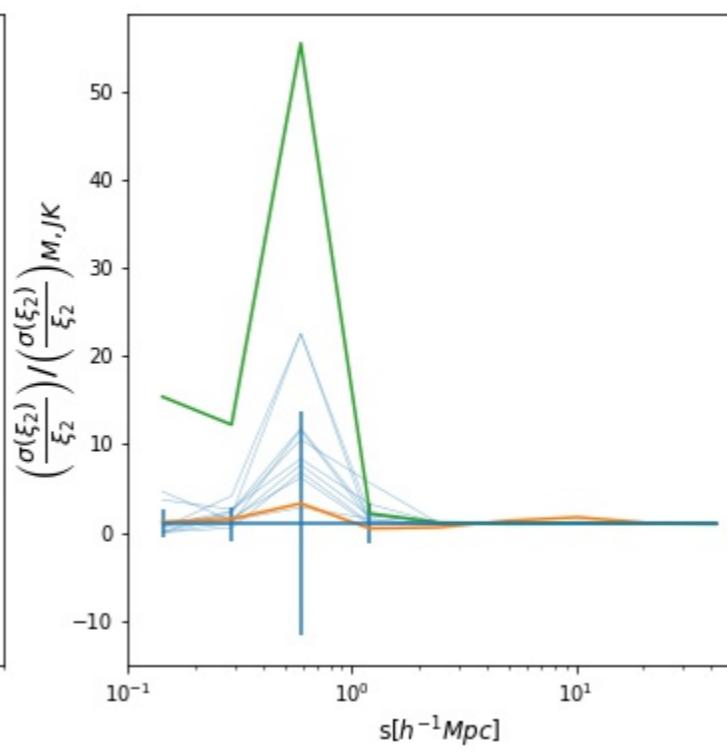
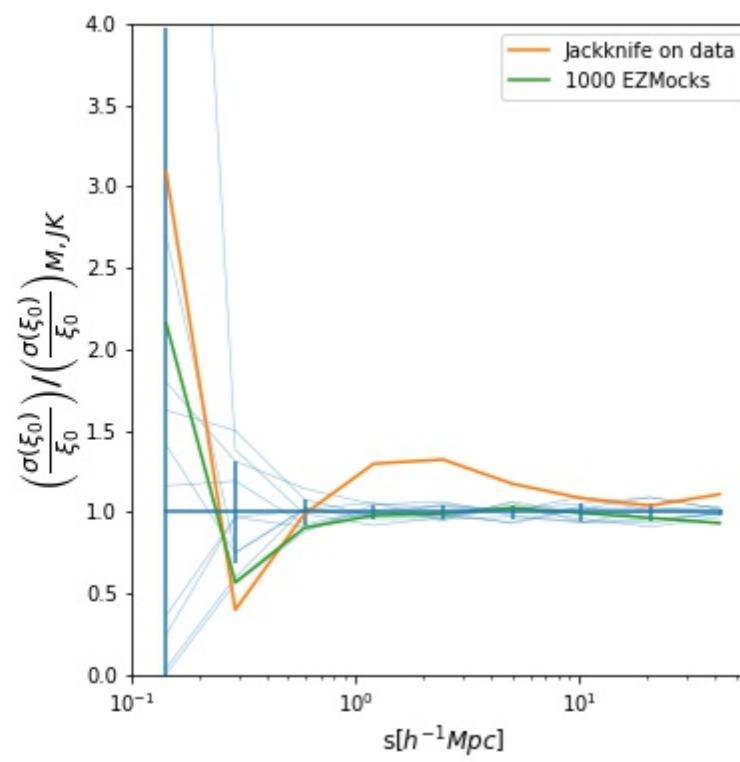
# JACKKNIFE COVARIANCE MATRIX

- ▶ Correlation matrix is highly diagonal so we smooth along the diagonals
- ▶ Combine with emulator error and apply Hartlap factor for final covariance matrix



# JACKKNIFE COVARIANCE MATRIX

- Comparing diagonal elements using relative error and find agreement between data JK, 1000 mocks, and JK on mocks



# AP SCALING

- ▶ Corrects for difference between the true cosmology and the cosmology assumed for distance calculations

$$a_{\perp} = \frac{D_M(z_{\text{eff}})}{D_M^{\text{fid}}(z_{\text{eff}})} \quad , \quad a_{\parallel} = \frac{D_H(z_{\text{eff}})}{D_H^{\text{fid}}(z_{\text{eff}})}$$

$$\xi_0^{\text{fid}}(r^{\text{fid}}) = \xi_0(\alpha r) + \frac{2}{5}\epsilon \left[ 3\xi_2(\alpha r) + \frac{d\xi_2(\alpha r)}{d \ln(r)} \right]$$

$$\xi_2^{\text{fid}}(r^{\text{fid}}) = (1 + \frac{6}{7}\epsilon)\xi_2(\alpha r) + 2\epsilon \frac{d\xi_0(\alpha r)}{d \ln(r)} + \frac{4}{7}\epsilon \frac{d\xi_2(\alpha r)}{d \ln(r)}$$

$$w_p^{\text{fid}}(r_p^{\text{fid}}) = w_p(a_{\perp} r_p)$$

# EXPLORING THE LIKELIHOOD

- ▶ Use Cobaya MCMC sampler to explore the likelihood
- ▶ Use priors slightly larger than training range to detect poorly constrained parameters
- ▶ Test additional cosmological priors restricting parameters using a distance threshold from the training points and Planck2018 constraints

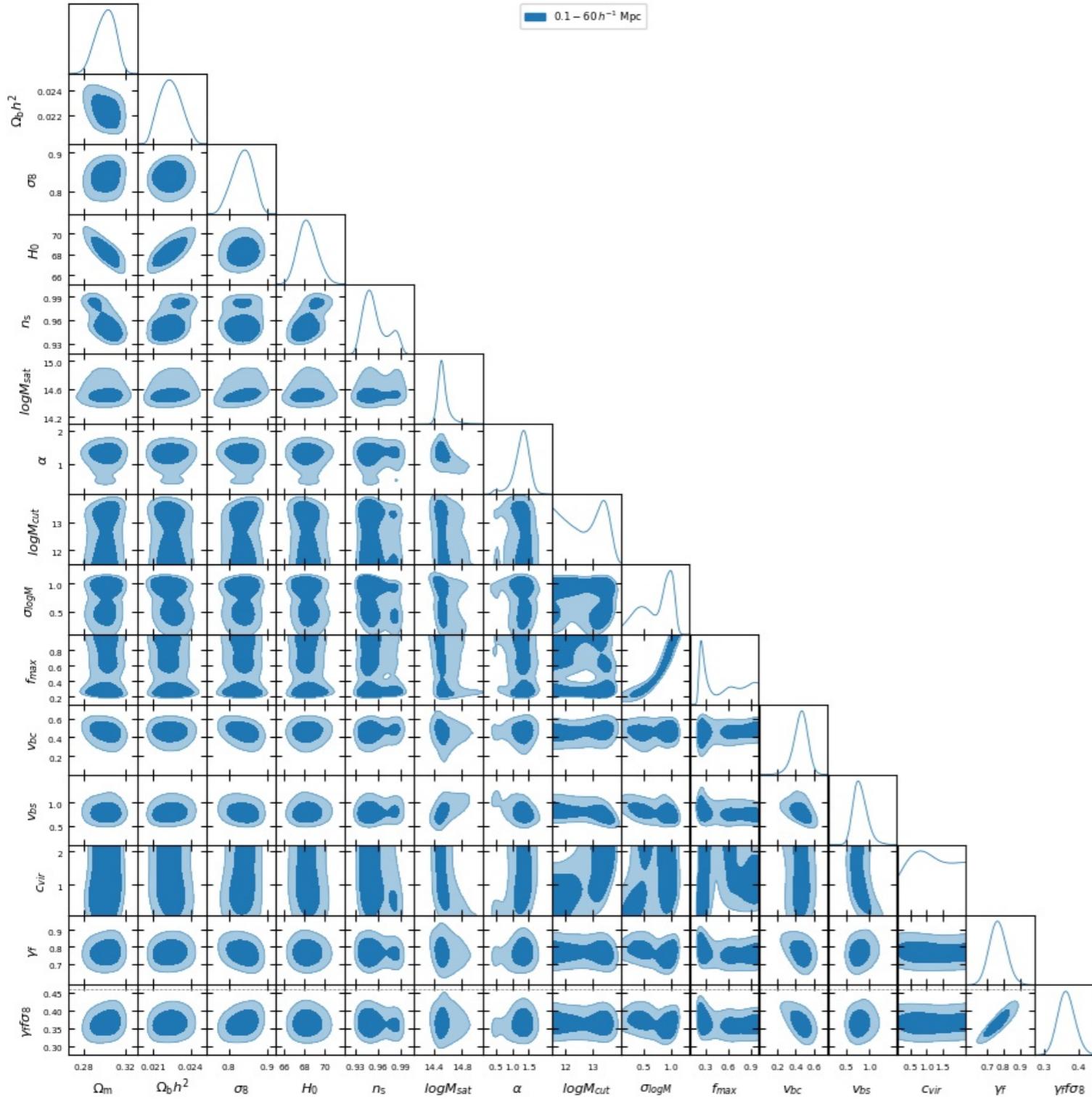
Parameter	Training Range	Prior Range
$\Omega_m$	[0.255, 0.353]	[0.225, 0.375]
$\Omega_b h^2$	[0.039, 0.062]	[0.005, 0.1]
$\sigma_8$	[0.575, 0.964]	[0.5, 1]
$h$	[0.612, 0.748]	[0.58, 0.78]
$n_s$	[0.928, 0.997]	[0.8, 1.2]
$N_{\text{eff}}$	[2.62, 4.28]	3.046
$w$	[-1.40, -0.57]	-1
$\log M_{\text{sat}}$	[14.0, 16.0]	[13.8, 16.2]
$\alpha$	[0.2, 2.0]	[0.1, 2.2]
$\log M_{\text{cut}}$	[10.0, 13.7]	[11.5, 14]
$\sigma_{\log M}$	[0.1, 1.6]	[0.08, 1.7]
$v_{\text{bc}}$	[0, 0.7]	[0, 0.85]
$v_{\text{bs}}$	[0.2, 2.0]	[0.1, 2.2]
$c_{\text{vir}}$	[0.2, 2.0]	[0.1, 2.2]
$\gamma_f$	[0.5, 1.5]	[0.25, 1.75]
$f_{\text{max}}$	[0.1, 1]	[0.1, 1]

## UCHUU

- ▶ Large, high resolution simulation with Rockstar halos
- ▶  $L_{box} = 2000 \text{ Mpc}/h, 12800^3$  particles,  $3.27 \times 10^8 M_{\odot}/h$
- ▶ Created HOD and SHAM mocks for robustness checks

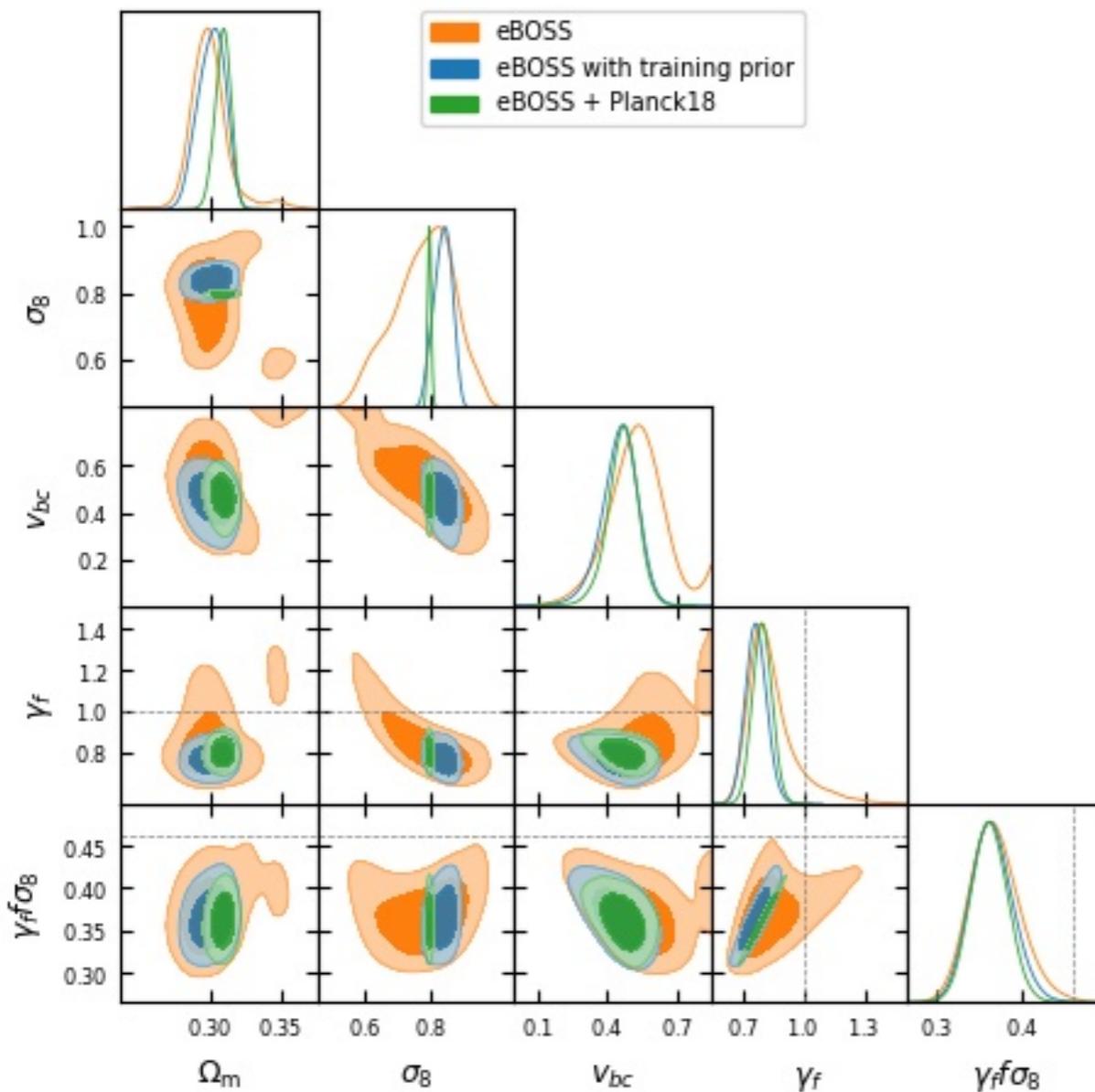


# HEADLINE RESULTS



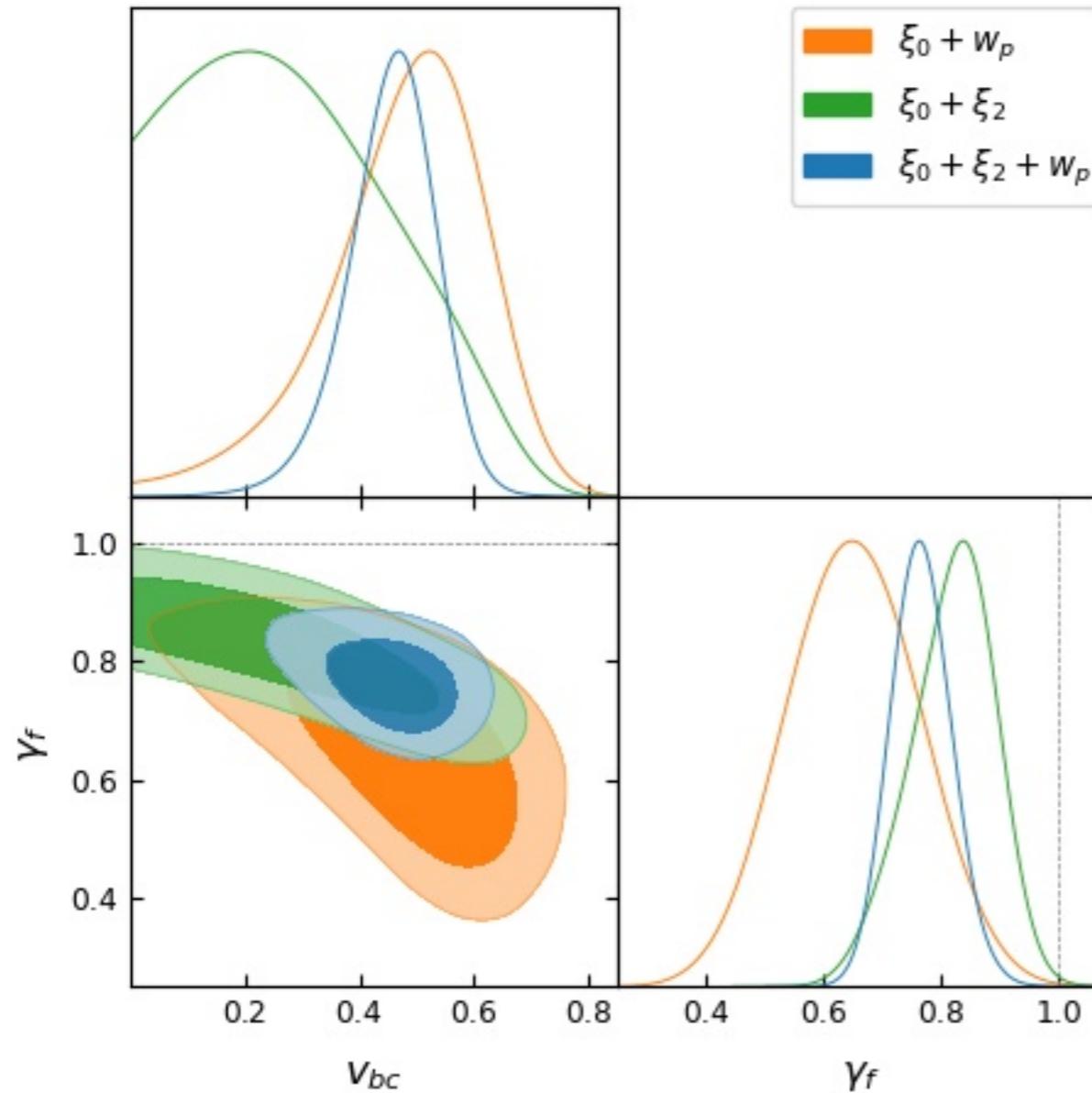
- ▶ All well-constrained parameters are within the training range
- ▶ All cosmological parameters consistent with Planck2018
- ▶ Close to Gaussian constraints on parameters of interest

# TESTING COSMOLOGICAL PRIORS



- ▶ Aemulus training prior restricts cosmological parameters to well trained region
- ▶ Tested combined fit with Planck2018 TT+EE+TE+lensing likelihoods
- ▶ Find consistent constraints in all cases

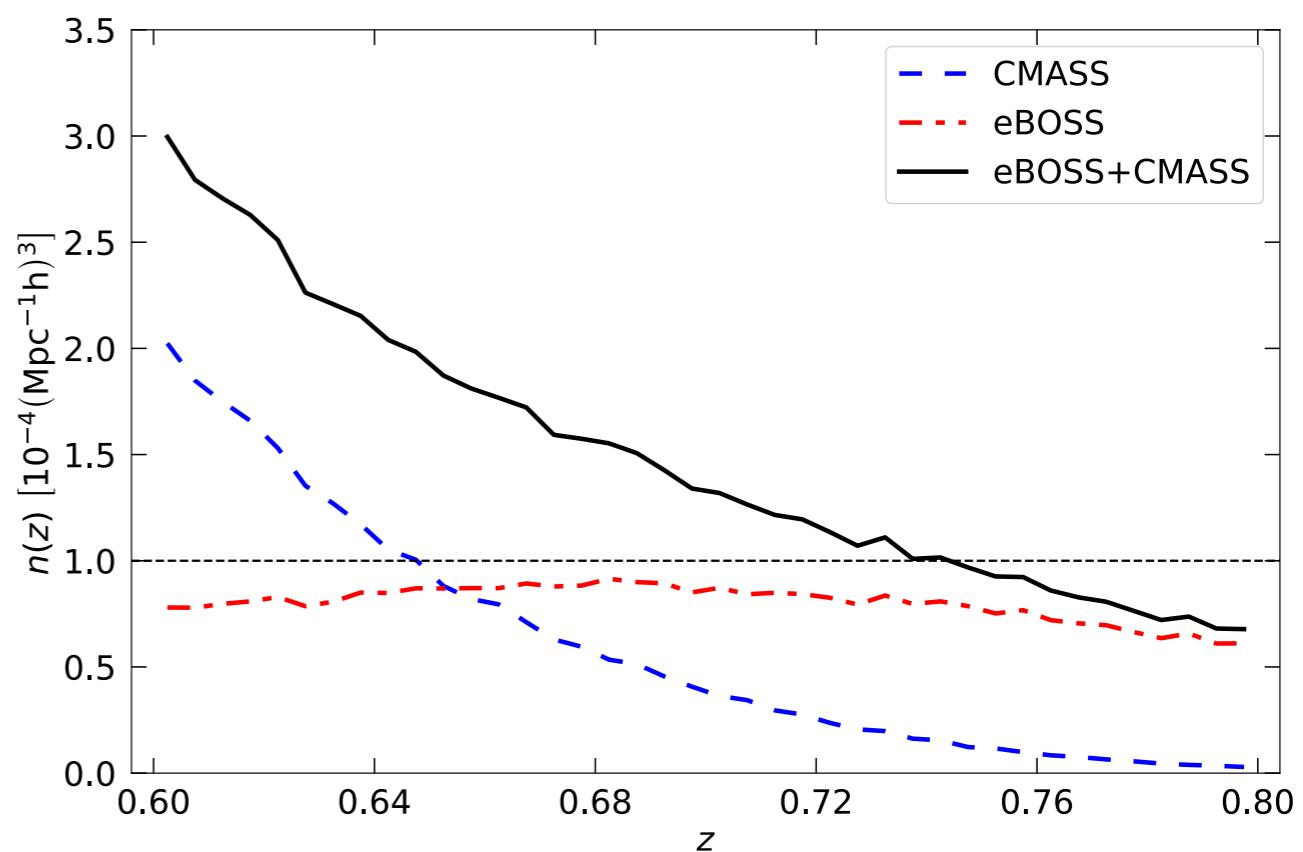
# MEASUREMENT DEPENDENCE



- ▶ Monopole and projected correlation function more strongly prefer non-zero  $v_{bc}$  and low  $\gamma_f$
- ▶ Multipoles prefer larger  $\gamma_f$  along degeneracy with  $v_{bc}$
- ▶ Combined fit occupies the overlap region

## CMASS+EBOSS

- ▶ Additionally fit to a combined BOSS CMASS+eBOSS sample between  $0.6 < z < 0.8$
- ▶ Adding CMASS increases the number of objects and completeness, but skews  $n(z)$
- ▶ HOD formalism assumes single population for entire sample



## CMASS+EBOSS

