

COSMOLOGY FROM WEAK LENSING ALONE AND IMPLICATIONS FOR THE HUBBLE TENSION

Based on arXiv:2104.12880

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UNIVERSITY OF EDINBURGH



WHO AM I?

Post-doc at the Institute for Astronomy, University of Edinburgh.

Recent work:

- *Weak lensing and galaxy clustering analysis techniques*
- *Gravitational wave source populations, primordial black holes*

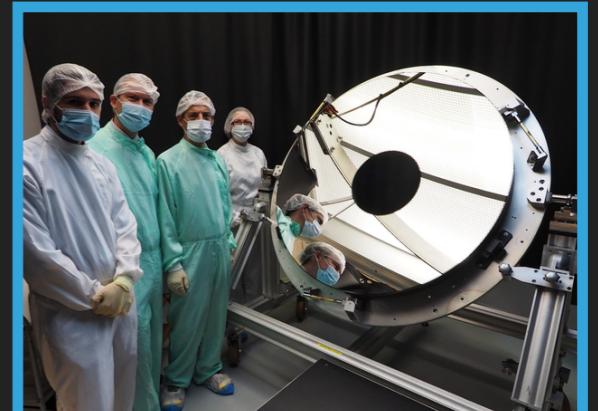
Less recent work:

- *21cm intensity mapping, CMB lensing, relativistic effects in cosmology, non-linear modelling, ...*



Member of ESA *Euclid* Consortium:

- Co-lead of Weak Lensing Estimators Work Package and Pre-Launch Key Project
- Euclid UK Coordination Group

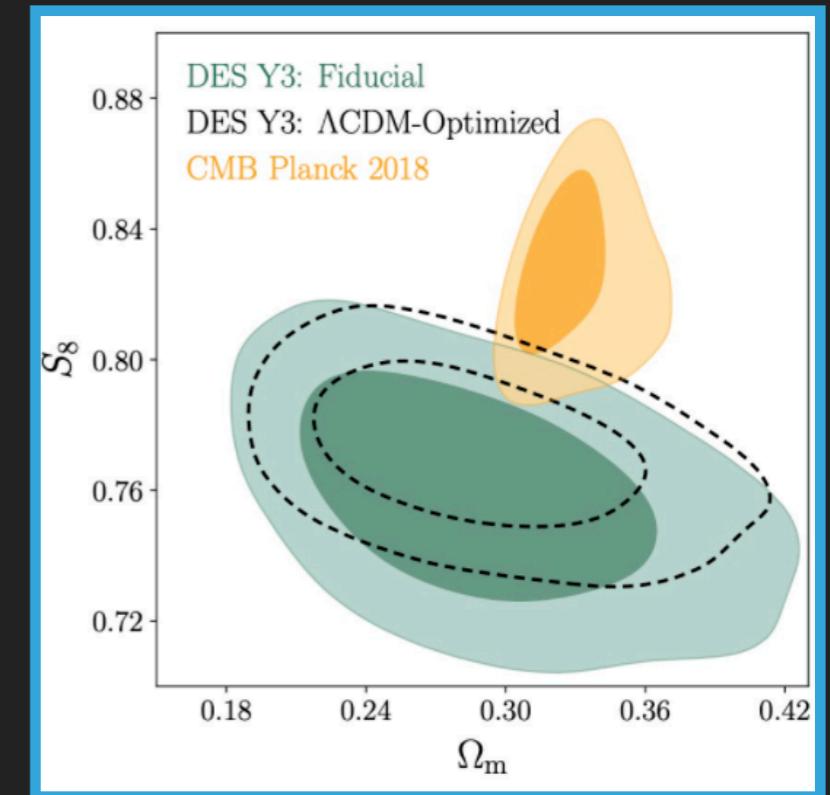


OUTLINE OF THIS TALK

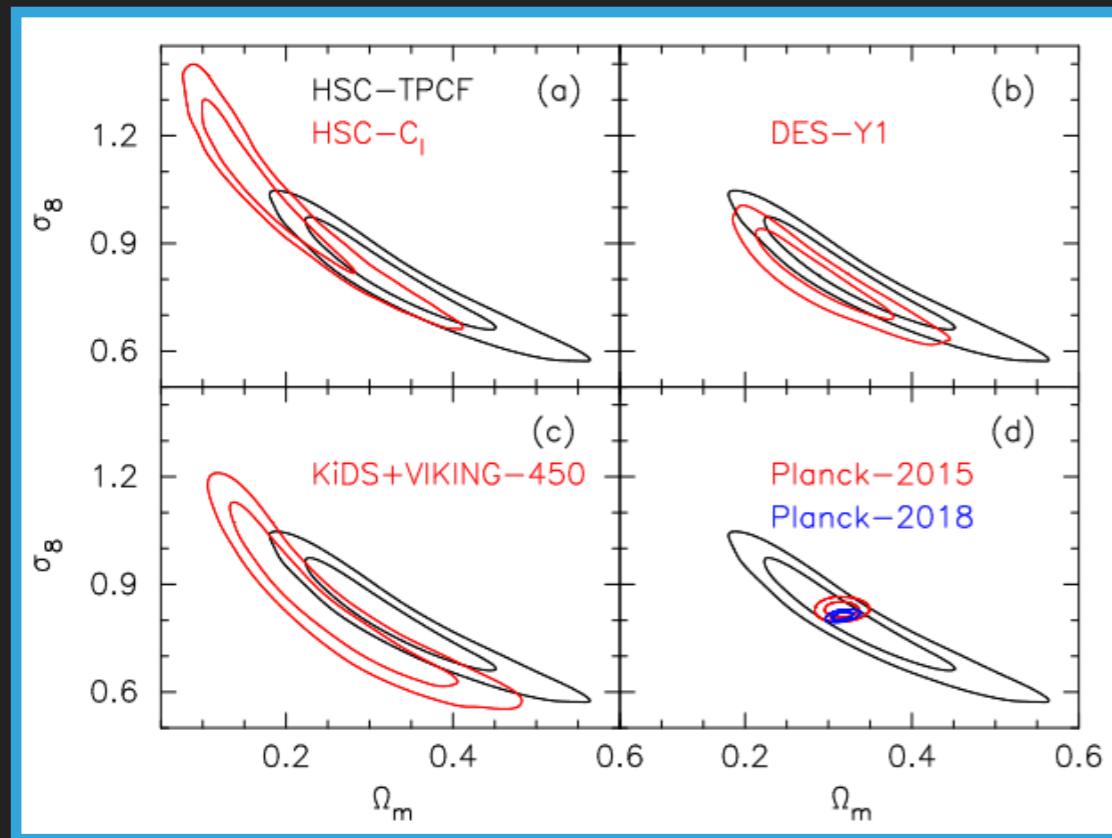
- CURRENT STATE OF COSMIC SHEAR COSMOLOGY
- WHAT DOES WEAK LENSING TELL US ABOUT THE UNIVERSE?
- WHAT DOES WEAK LENSING NOT TELL US ABOUT THE UNIVERSE?
- WHAT CAN WEAK LENSING TELL US ABOUT THE HUBBLE CONSTANT?

LATEST RESULTS FROM COSMIC SHEAR

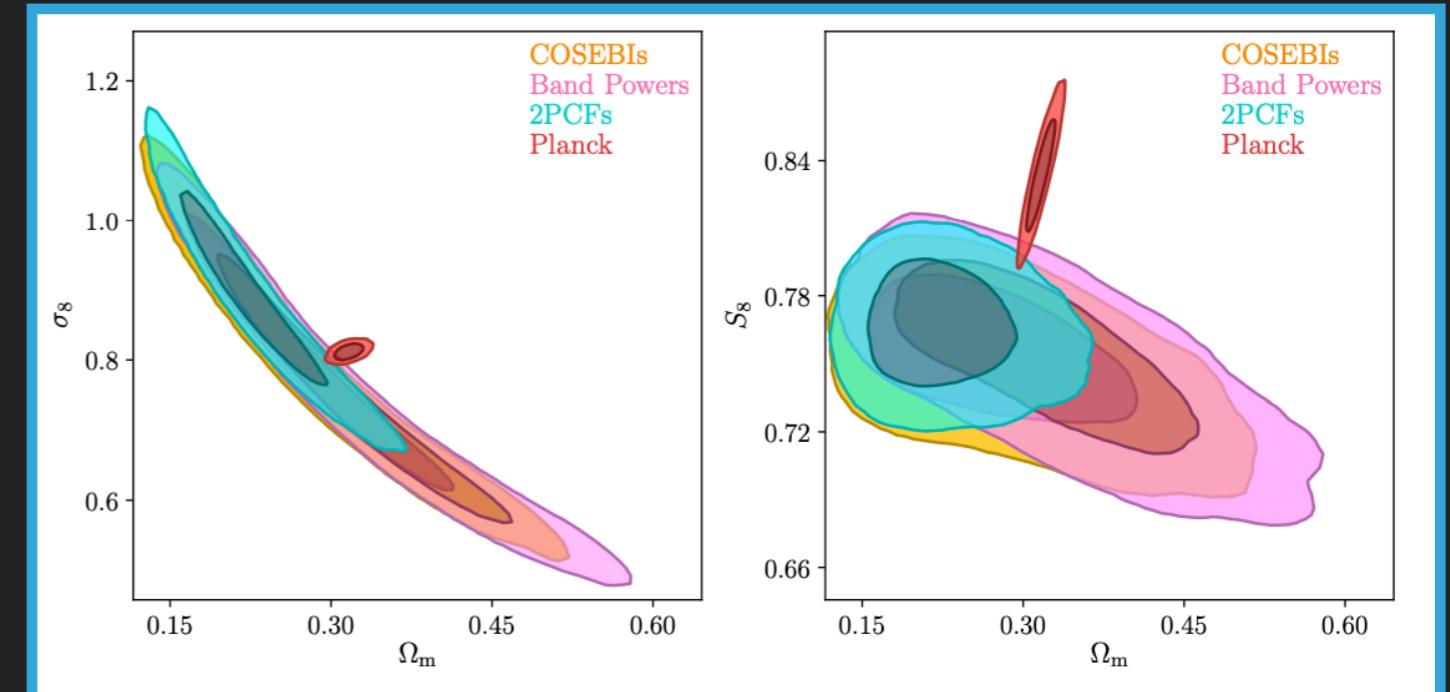
$$S_8 \propto \sigma_8 \Omega_m^{0.5}$$



DES Collaboration, Amon et al. 2021



HSC Collaboration, Hamana et al. 2019
(Erratum 2022)



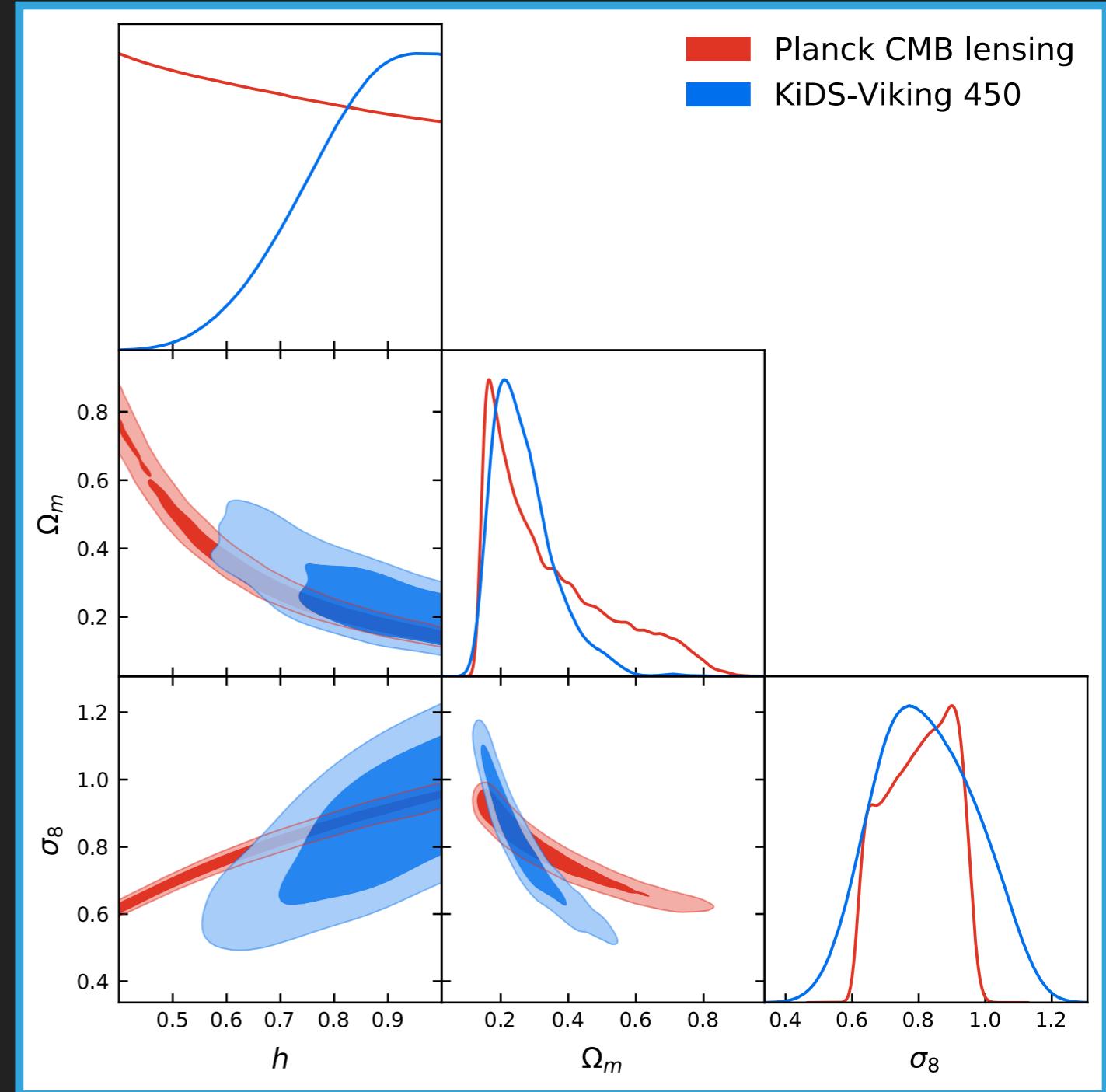
KiDS Collaboration, Asgari et al. 2020

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

Constrain well the combination

$$S_8 \propto \sigma_8 \Omega_m^{0.5}$$

Poor constraints on almost every other parameter combination



COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

We understand this!



CMB lensing

Constrain well **two** of the combinations

$$\begin{aligned}\sigma_8 h^{-0.5} \\ \Omega_m^{0.6} h \\ \sigma_8 \Omega_m^{0.25}\end{aligned}$$

Small-scale amplitude

Peak in the matter power spectrum (in projection)

Amplitude and shape

Do we understand this?



Galaxy weak lensing

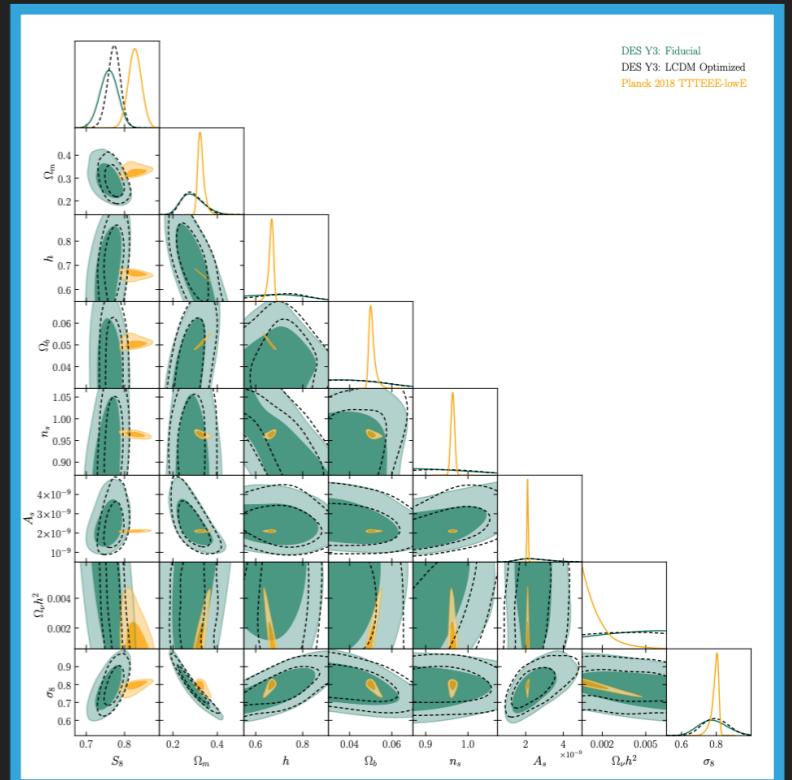
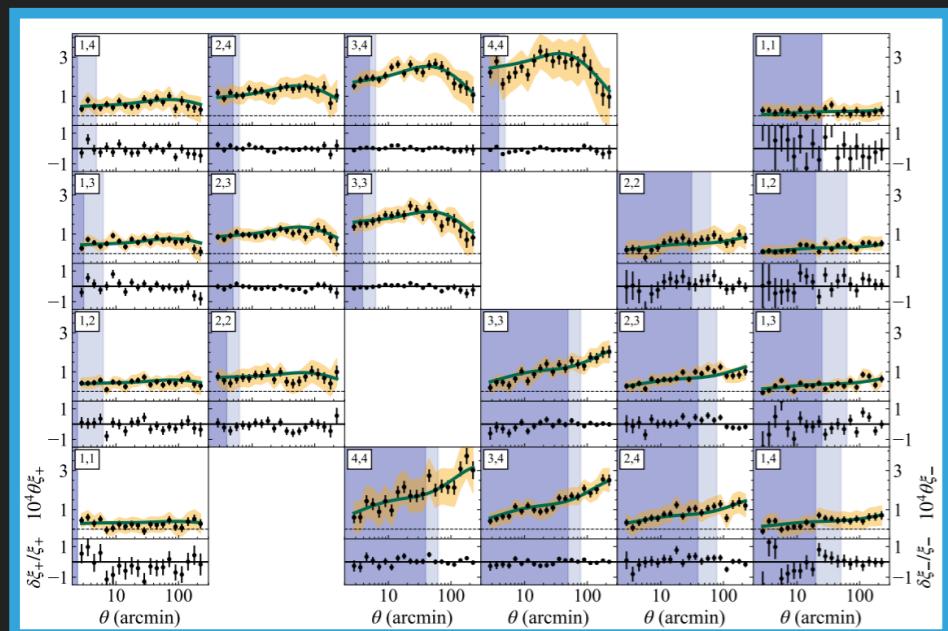
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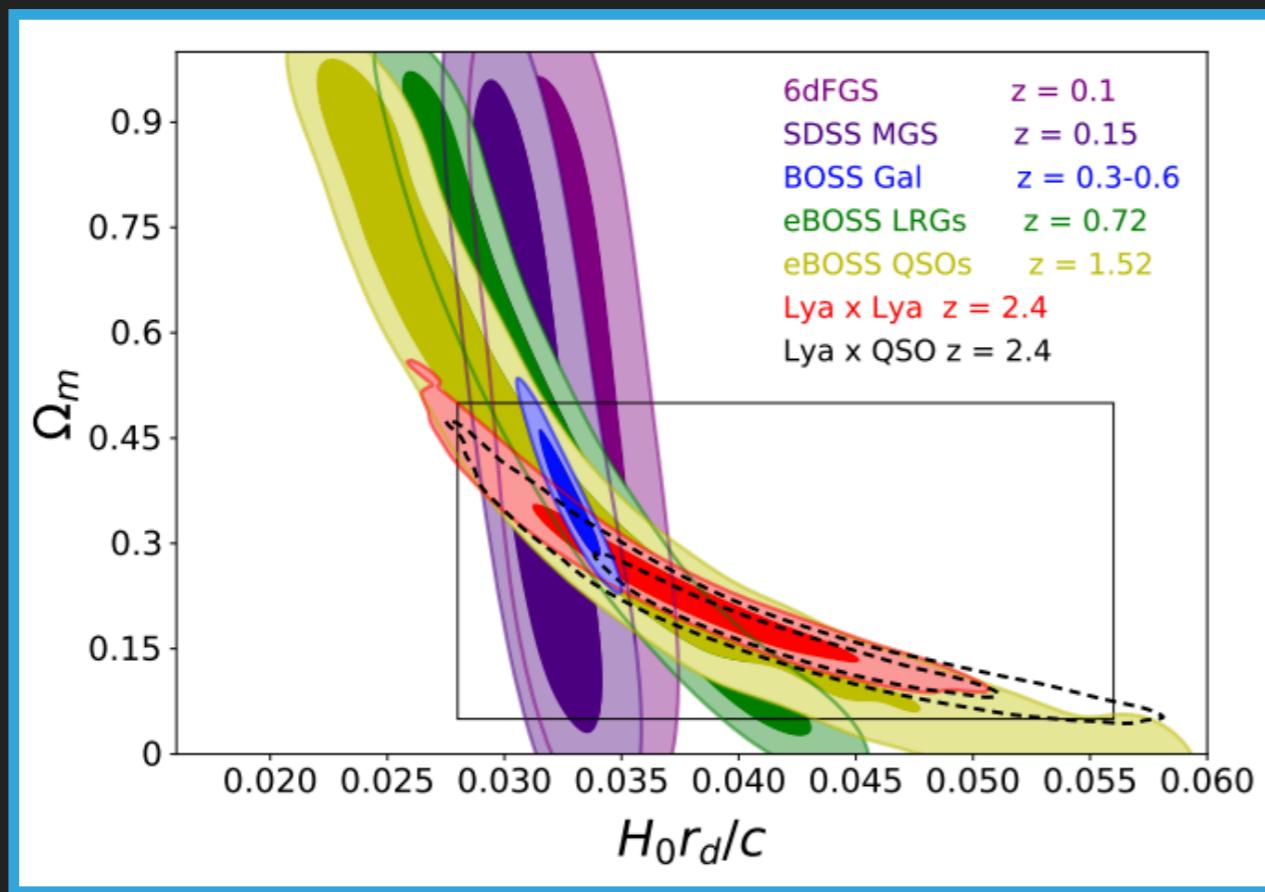
WHY IS IT IMPORTANT TO UNDERSTAND WHERE PARAMETER INFORMATION COMES FROM?

I) A sanity check on parameter posteriors

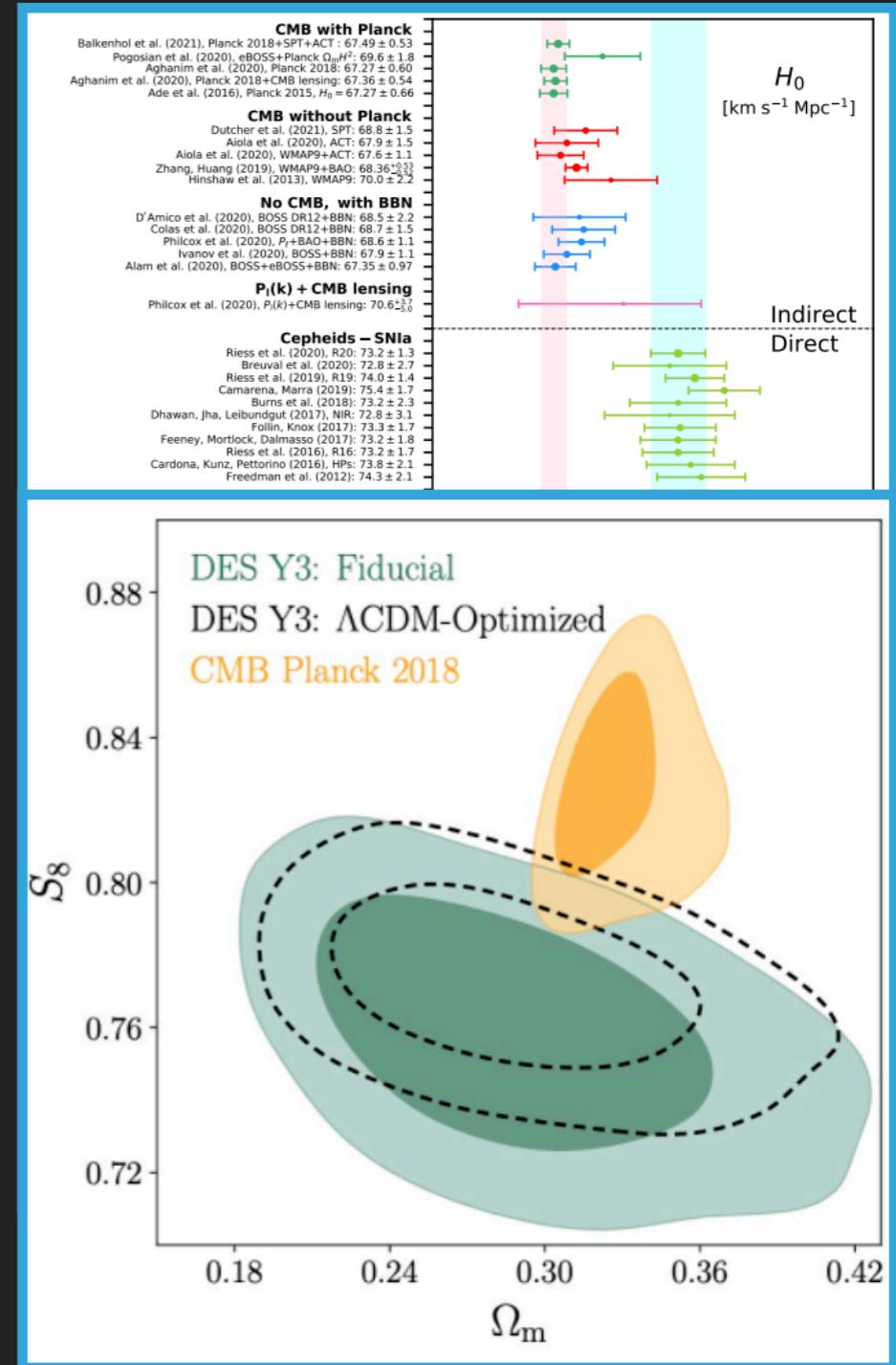


WHY IS IT IMPORTANT TO UNDERSTAND WHERE PARAMETER INFORMATION COMES FROM?

2) Lambda-CDM may need modifying



Cuceu et al. 2019



Di Valentino et al. 2021, Amon et al. 2021

QUESTIONS

- 1) Where does parameter information come from in weak lensing? Why are some parameter combinations constrained well and some not so well?
- 2) *Tensions*: Why does weak lensing tell us about $S8$ and not $H0$?

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

$$C_{\ell}^{\gamma\gamma} = \frac{9}{4} \Omega_m^2 H_0^4 \int_0^{z_s} \frac{dz}{H(z)} \left[\frac{r(z_s) - r(z)}{r(z_s)} \right]^2 (1+z)^2 P_m \left(\frac{\ell}{r(z)}; z \right)$$

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Gravitational potential gradients cause deflection.
Gradients in the deflection cause shear.

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Shear distortions are the net effect of many small deflections along the photon path

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$$\sim \frac{\Omega_m^2}{\ell^3} \int_0^{z_s} \frac{dz}{H(z)/H_0} \left[\frac{r(z_s) - r(z)}{r(z_s)} \right]^2 (1+z)^2 [H_0 r(z)]^3 \Delta_m^2 \left(\frac{\ell}{r(z)}; z \right)$$

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$F(z; \Omega_m) \approx F(z)$ for low-redshift lenses

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

$$C_\ell^{\gamma\gamma} \sim \ell^{-3} \Omega_m^2 \int_0^{z_{\max}} dz F(z) \Delta^2 \left(k/H_0 = \frac{\ell}{z}; z \right)$$

$$\Delta^2(k) \equiv \frac{k^3}{2\pi^2} P_m(k)$$

The dimensionless matter power spectrum with k in h/Mpc units

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Physically: lensing introduces no new length scales on top of those already present in the matter distribution.

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

$$C_\ell^{\gamma\gamma} \sim \ell^{-3} \Omega_m^2 \int_0^{z_{\max}} dz F(z) \Delta^2 \left(k/H_0 = \frac{\ell}{z}; z \right)$$

Usual hand-wavy argument:

$$\begin{aligned} \Delta^2 &\sim \sigma_8^2 \\ \implies C_\ell &\sim \sigma_8^2 \Omega_m^2 \end{aligned}$$

i.e. gets the dependence wrong!

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

$$C_\ell^{\gamma\gamma} \sim \ell^{-3} \Omega_m^2 \int_0^{z_{\max}} dz F(z) \Delta^2 \left(k/H_0 = \frac{\ell}{z}; z \right)$$

More precise: Jain & Seljak 1997

$$\xi_+(\theta) \sim \sigma_8 \Omega_m^\alpha$$

Using linear theory and the
Peacock & Dodds 1996 formula
for the non-linear $P(k)$

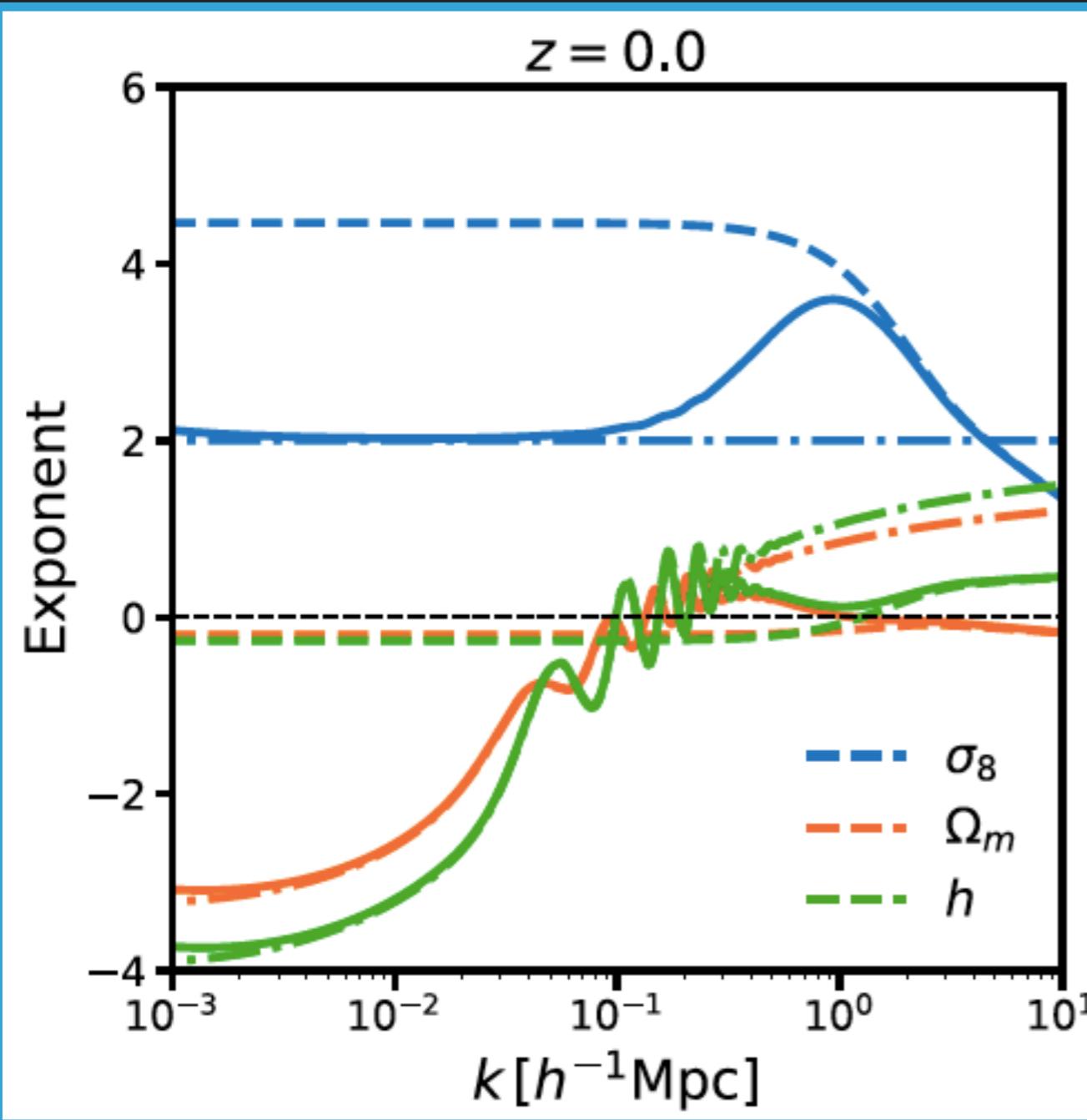
$$\alpha \lesssim 0.5 \quad \theta \lesssim 2'$$

$$\alpha \approx 0.7 \quad \theta > 10'$$

See also: Kaiser 1992, Villumsen 1996,
Bernardeau, van Waerbeke, Mellier 1997

PARAMETER SENSITIVITY IN THE HALO MODEL

$$\lim_{k \rightarrow 0} \Delta_{1H}^2(k) = \frac{(k/h)^3}{2\pi^2} \frac{h^3}{\bar{\rho}^2} \int_0^\infty M^2 n(M) dM$$



$$\lim_{k \rightarrow 0} \Delta_{1H}^2(k) \propto (k/h)^3 \sigma_8^{4.3}$$

Most of the contribution to the 1-halo amplitude at $z=0$ comes from Lagrangian scales around $8 \text{ Mpc}/h$.

$$\Delta^2(k/h) \sim \sigma_8^\alpha \Omega_m^\beta h^\gamma$$

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

$$C_\ell^{\gamma\gamma} \sim \ell^{-3} \Omega_m^2 \int_0^{z_{\max}} dz F(z) \Delta^2 \left(k/H_0 = \frac{\ell}{z}; z \right)$$

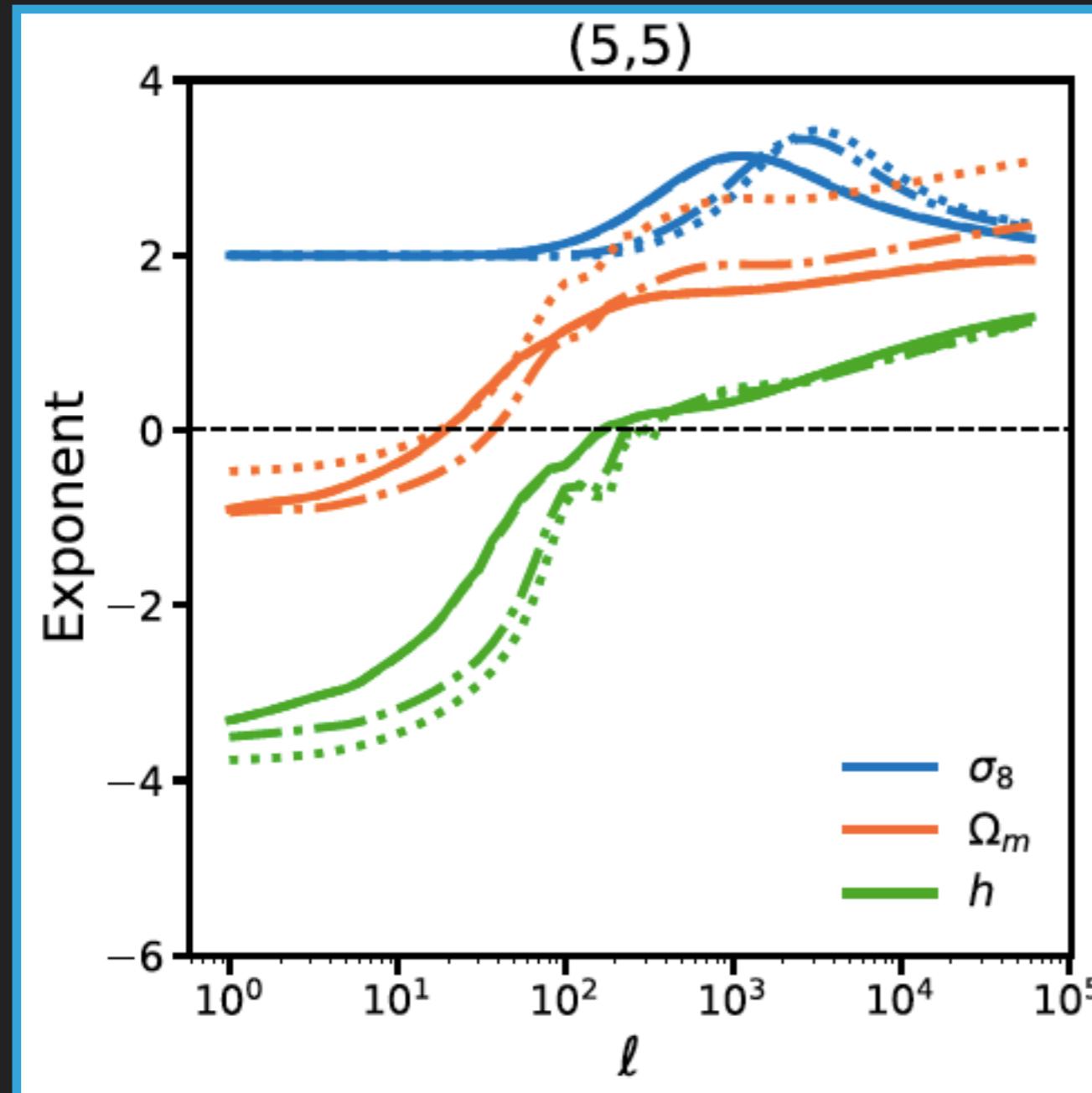
$$\lim_{k \rightarrow 0} \Delta_{1H}^2(k) \propto (k/h)^3 \sigma_8^{4.3}$$

$$\implies C_\ell^{\gamma\gamma} \propto \Omega_m^2 \sigma_8^{4.3} \sim S_8^4$$

On quasi-linear and 1-halo scales, h -dependence drops out completely and dependence is entirely on S_8

(Not perfect due to baryon smoothing, finite-redshift effects, 1-halo shape effects, etc.)

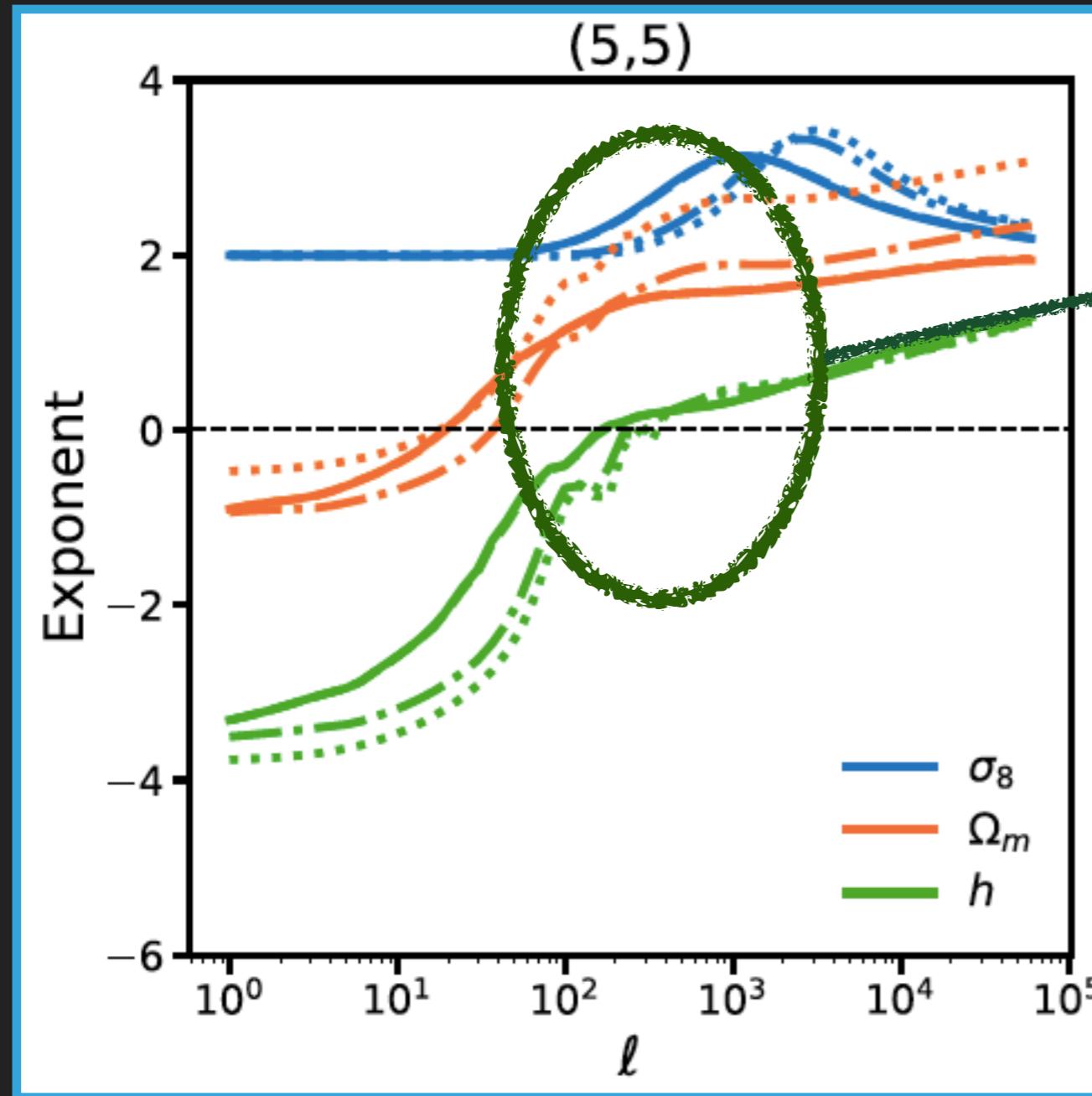
COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING



AH 2021

$$C_\ell \sim \sigma_8^\alpha \Omega_m^\beta h^\gamma$$

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING

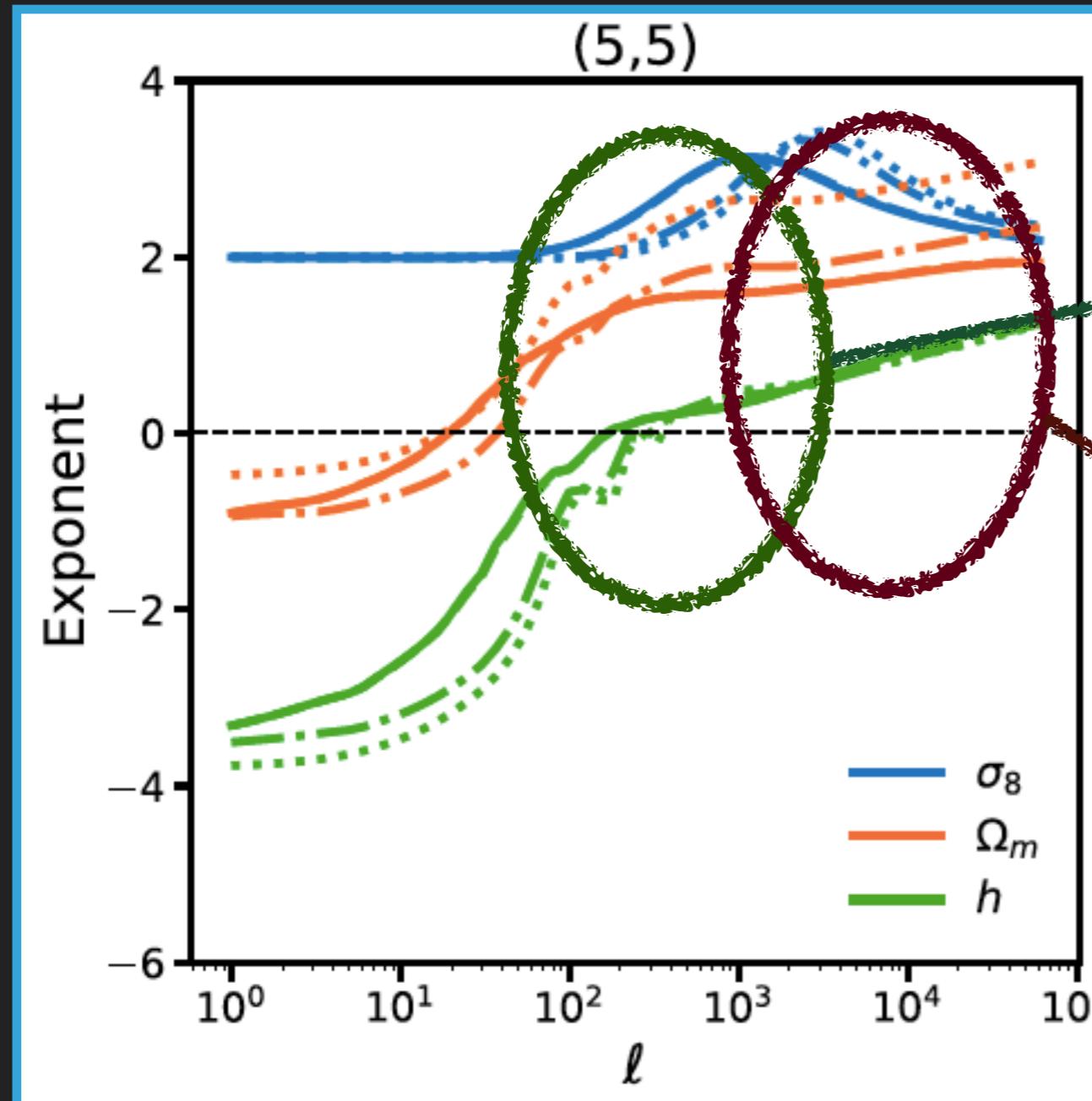


AH 2021

Most of the S/N in current surveys comes from here

$$C_\ell \sim \sigma_8^\alpha \Omega_m^\beta h^\gamma$$

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING



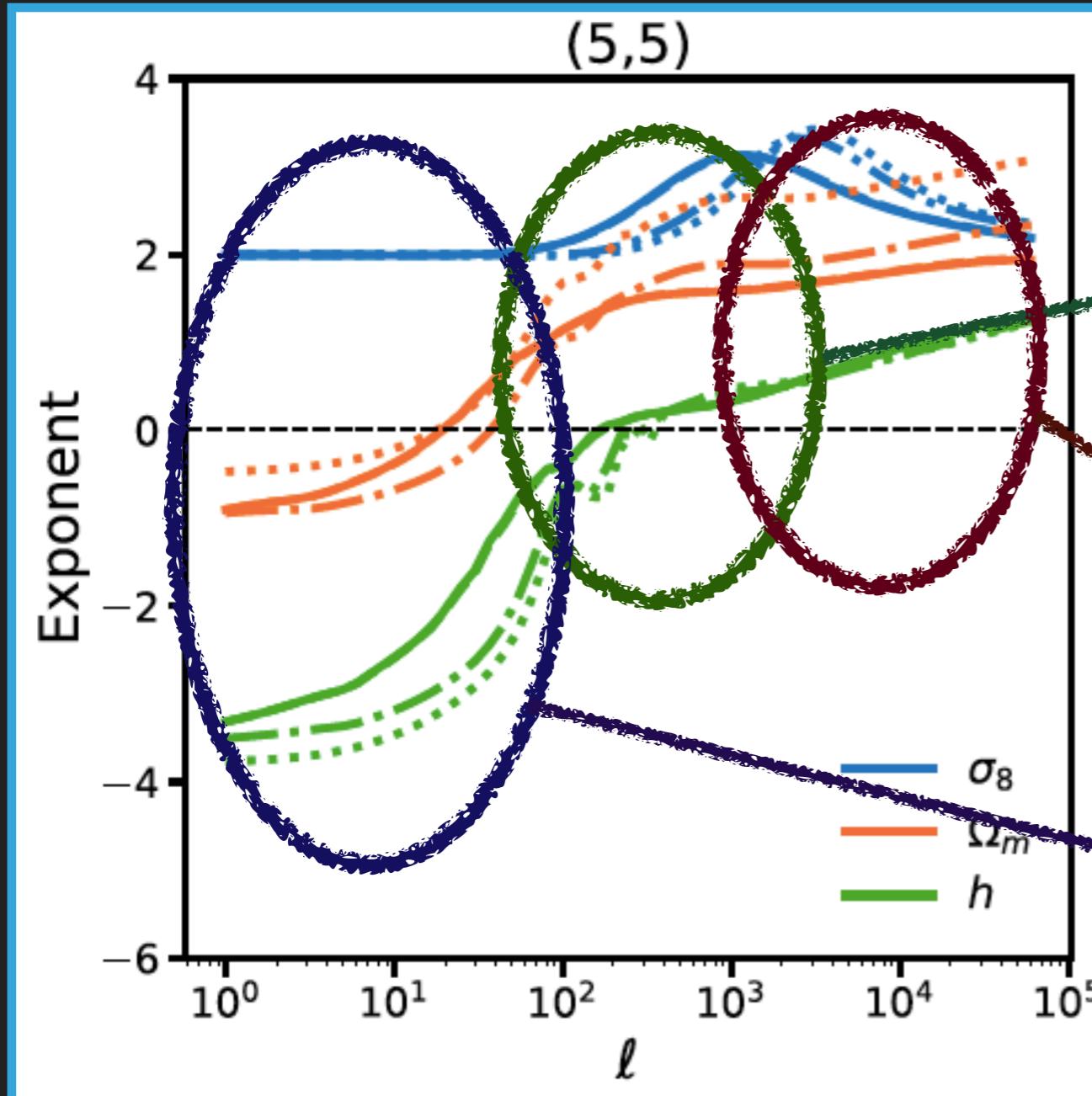
AH 2021

Most of the S/N in current surveys comes from here

Contaminated by baryon feedback!

$$C_\ell \sim \sigma_8^\alpha \Omega_m^\beta h^\gamma$$

COSMOLOGICAL INFORMATION CONTENT OF WEAK LENSING



Most of the S/N in current surveys comes from here

Contaminated by baryon feedback!

Future wide surveys: break degeneracies! (Known for at least ~ 20 years)

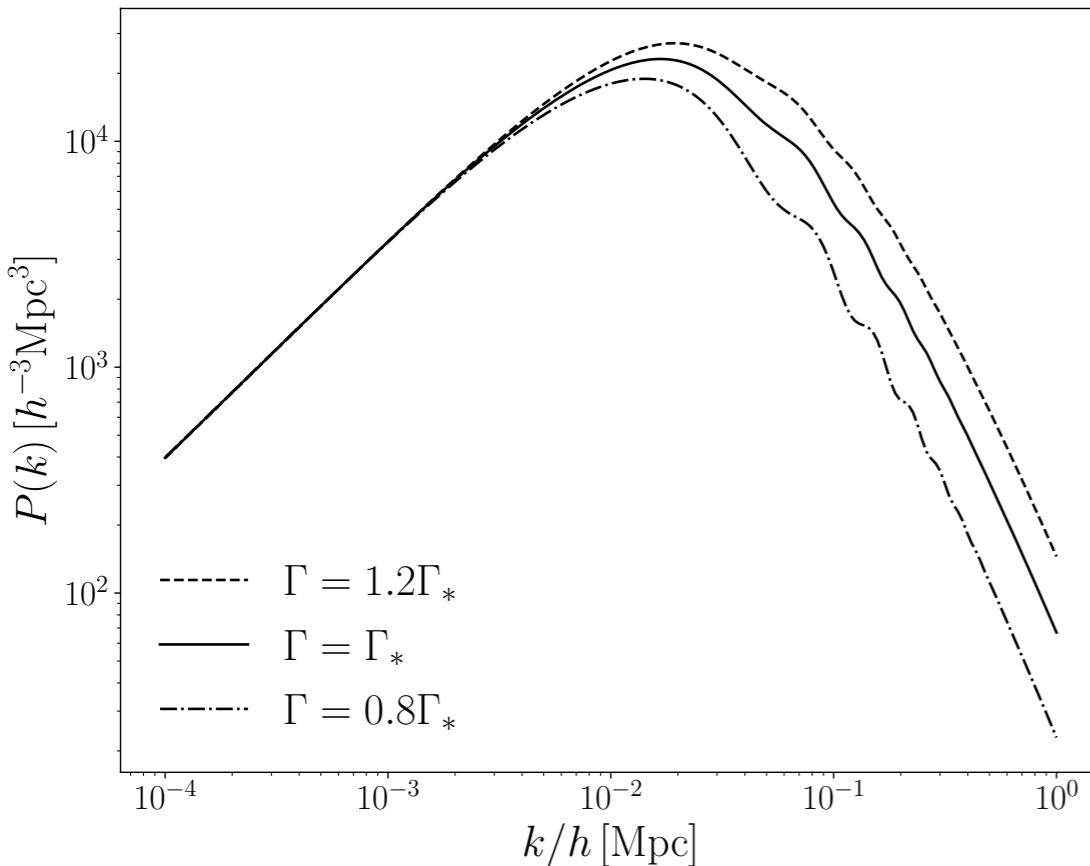
WHY SO INSENSITIVE TO H_0 ?

$$C_\ell^{\gamma\gamma} \sim \ell^{-3} \Omega_m^2 \int_0^{z_{\max}} dz F(z) \Delta^2 \left(k/H_0 = \frac{\ell}{z}; z \right)$$

Fixing Ω_m to keep the lensing pre-factors fixed

$\implies \Gamma \equiv \Omega_m h$ changes

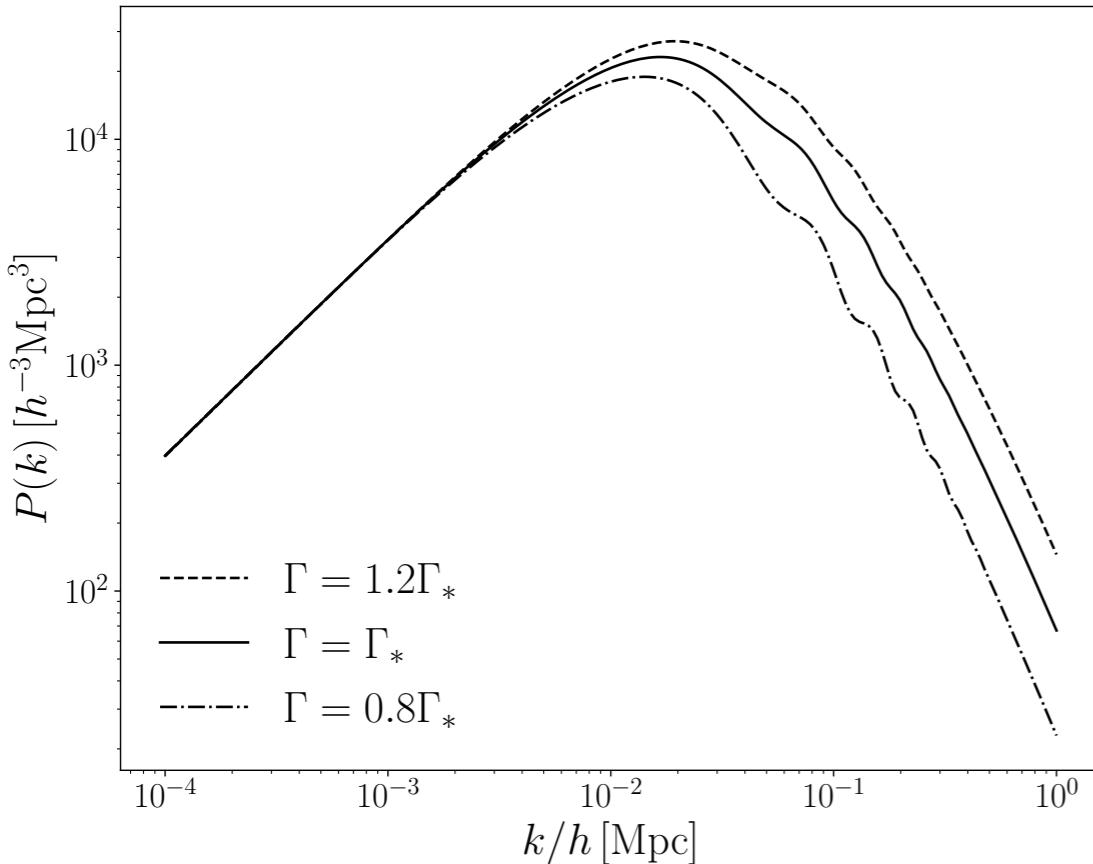
(the horizon scale at matter-radiation equality in h/Mpc units
a.k.a. the “shape parameter”)



WHY SO INSENSITIVE TO H_0 ?

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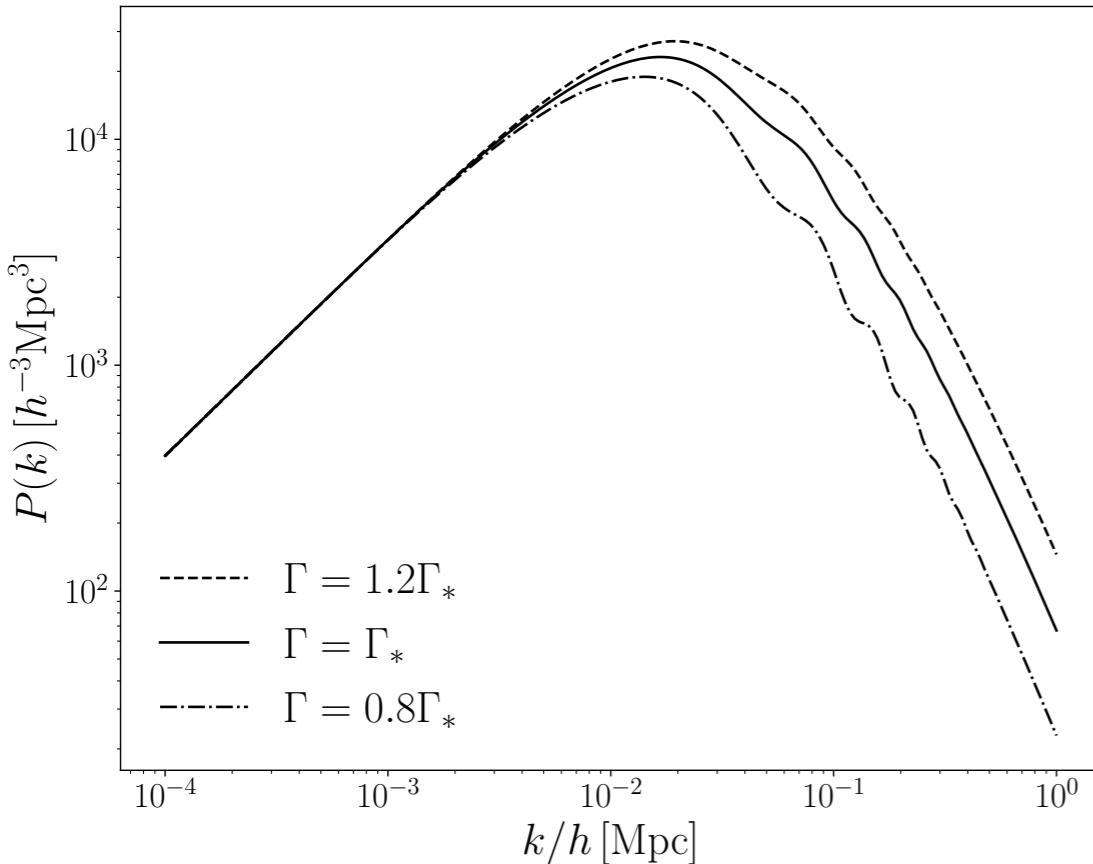
H_0 changes the small-scale amplitude at fixed A_s

But the amplitude is also controlled by Ω_m and A_s or σ_8 .

WHY SO INSENSITIVE TO H_0 ?

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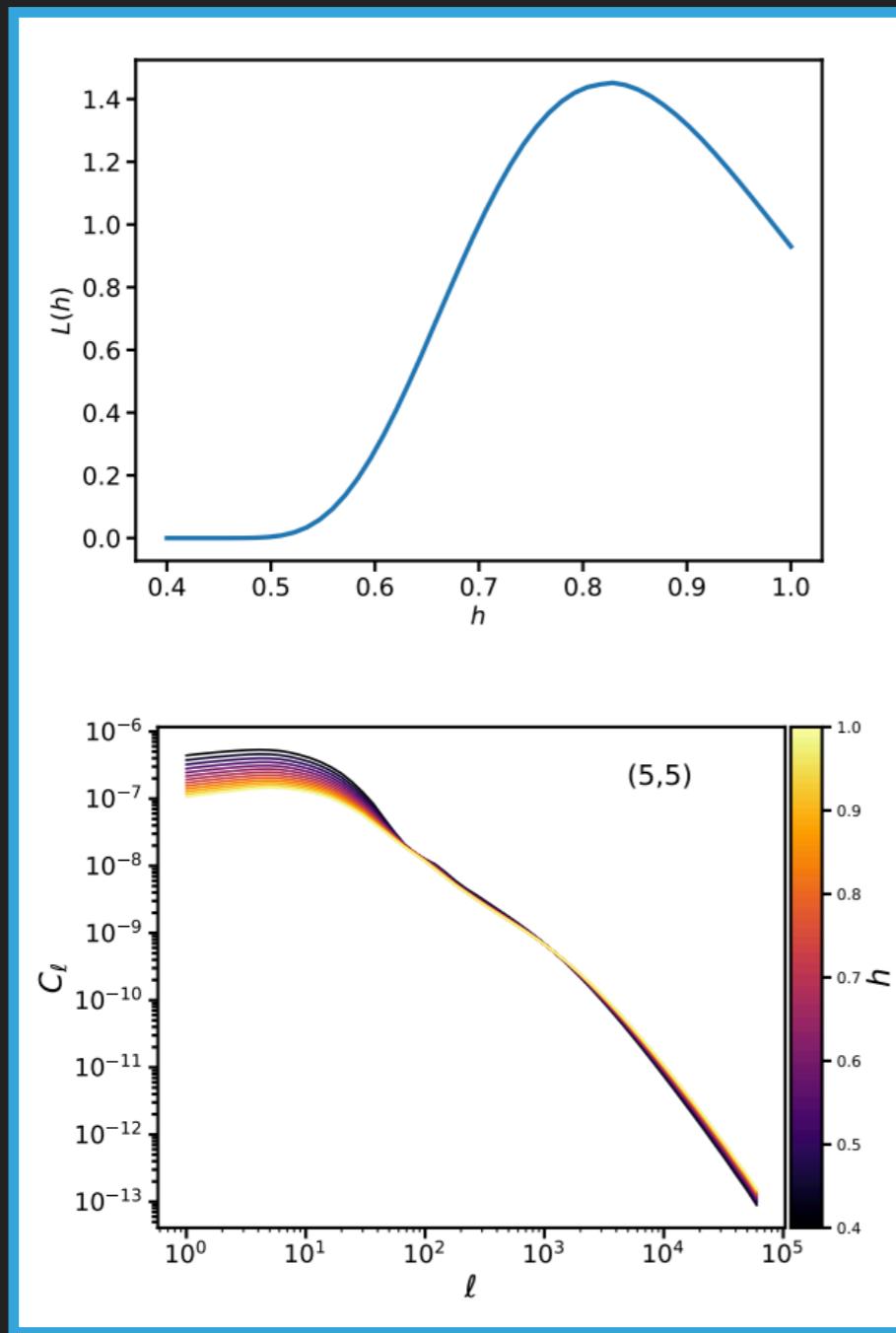
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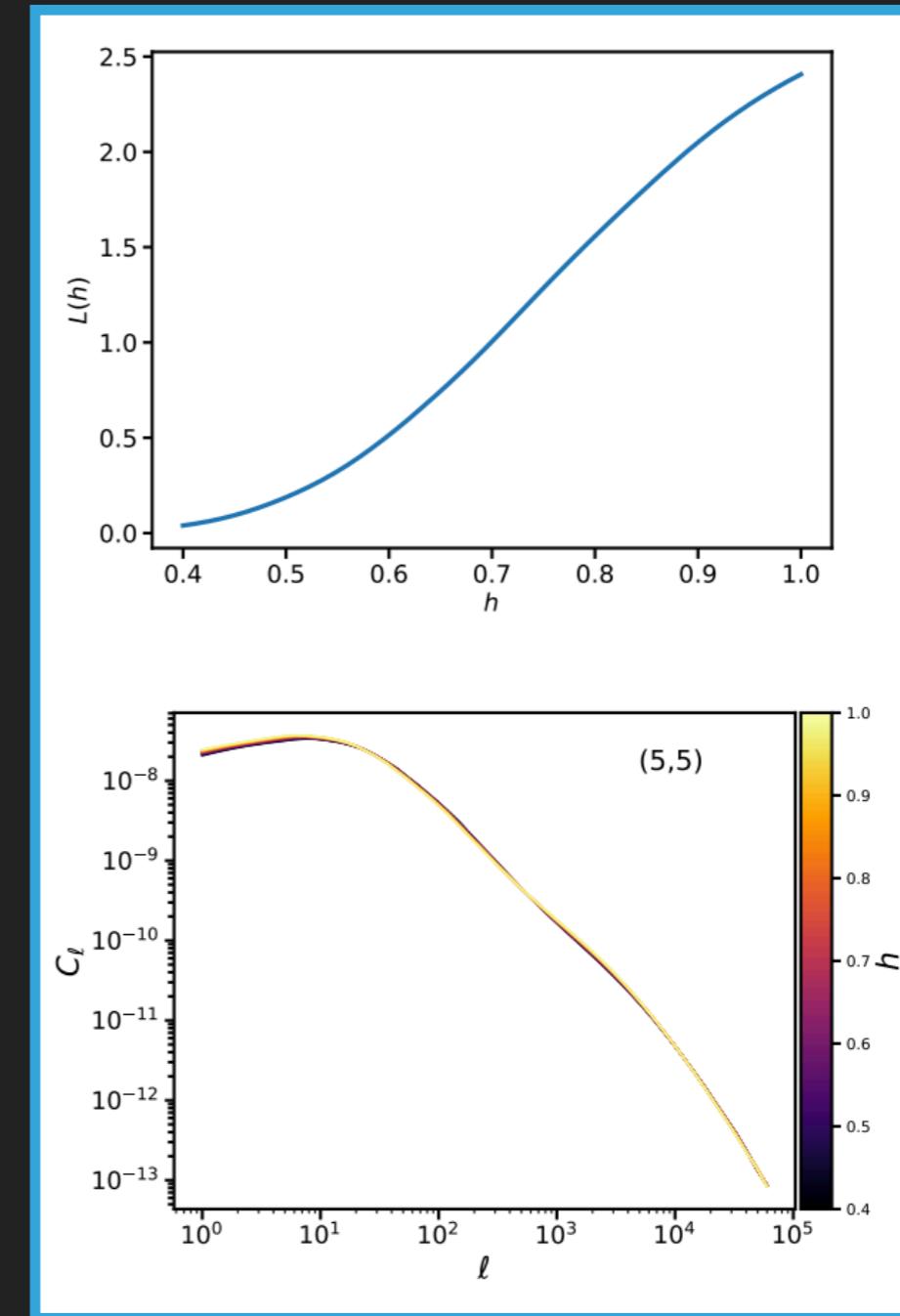
H_0 changes the small-scale amplitude at fixed A_s

Fixing the small-scale amplitude leaves only subtle changes to the shape - not well measured by current surveys!

HO INFORMATION IN KV450

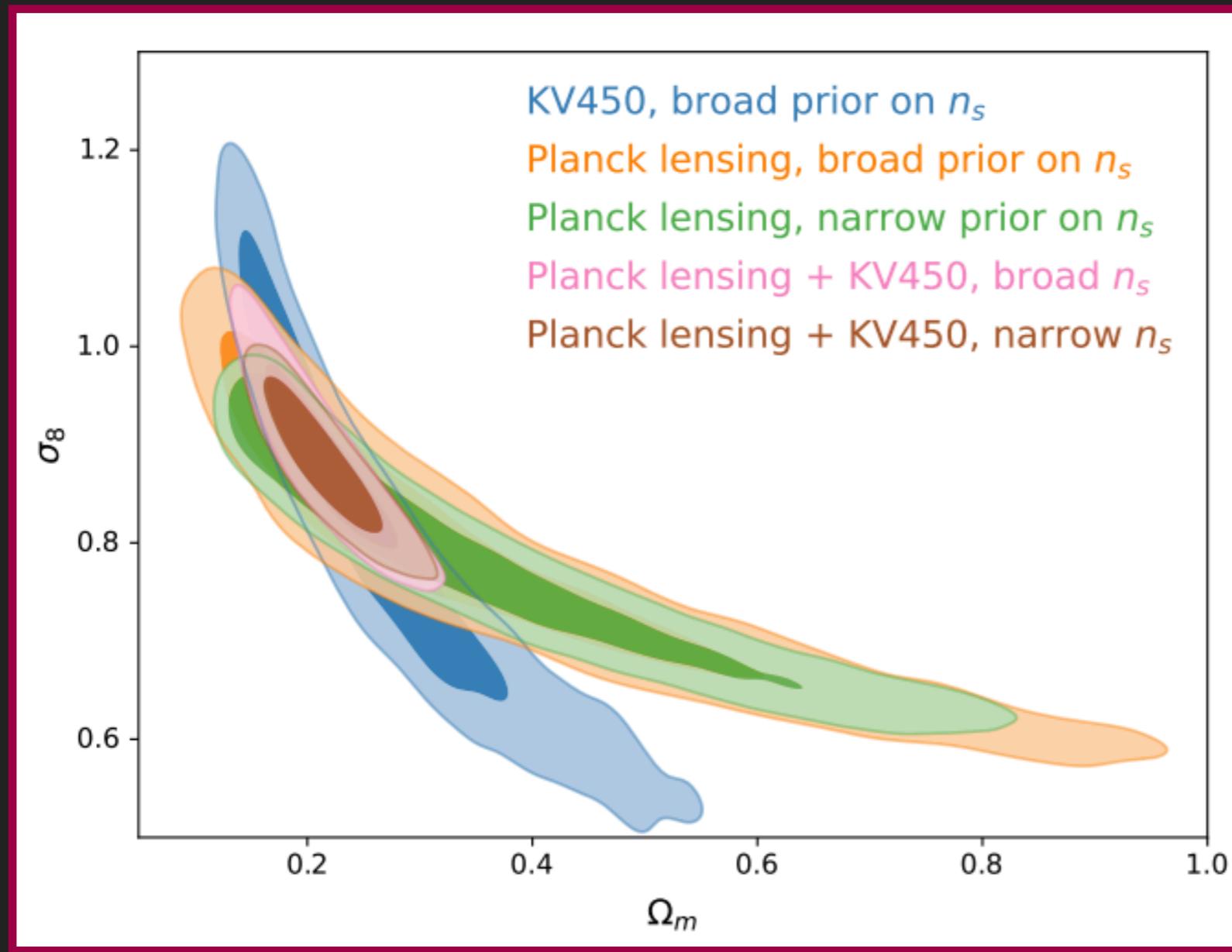


Fixed σ_8 and Ω_m



Fixed S_8 and $\Omega_m h^2$

WHAT *CAN* WEAK LENSING TELL US ABOUT H_0 ?



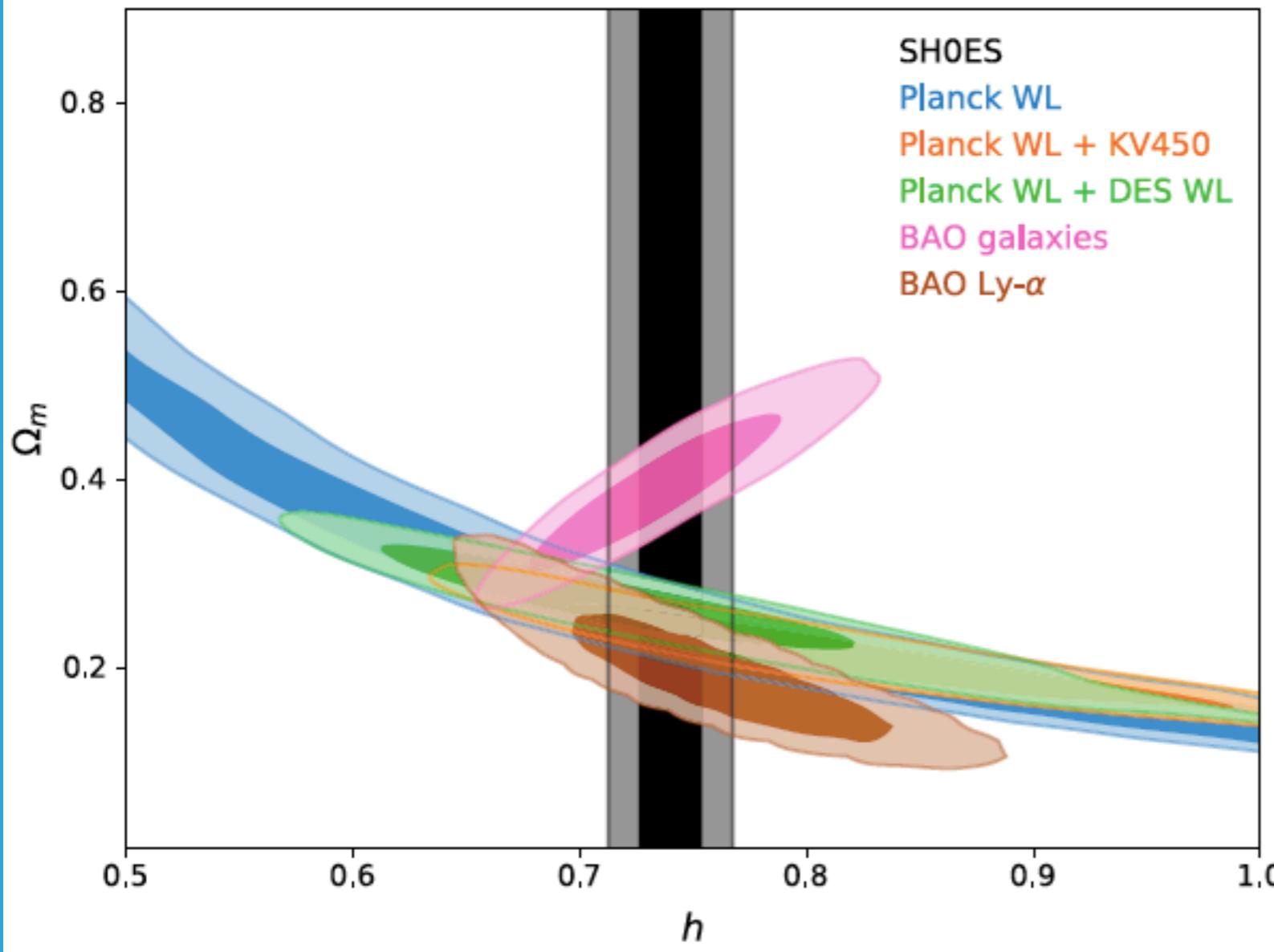
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Combined weak lensing probes give us Ω_m

Combine with BAO+BBN, which give contours in the Ω_m - H_0 plane.

CMB-independent probe of H_0
Addison+ 2013,
Auborg+ 2015 (DES)

WHAT *CAN* WEAK LENSING TELL US ABOUT H_0 ?



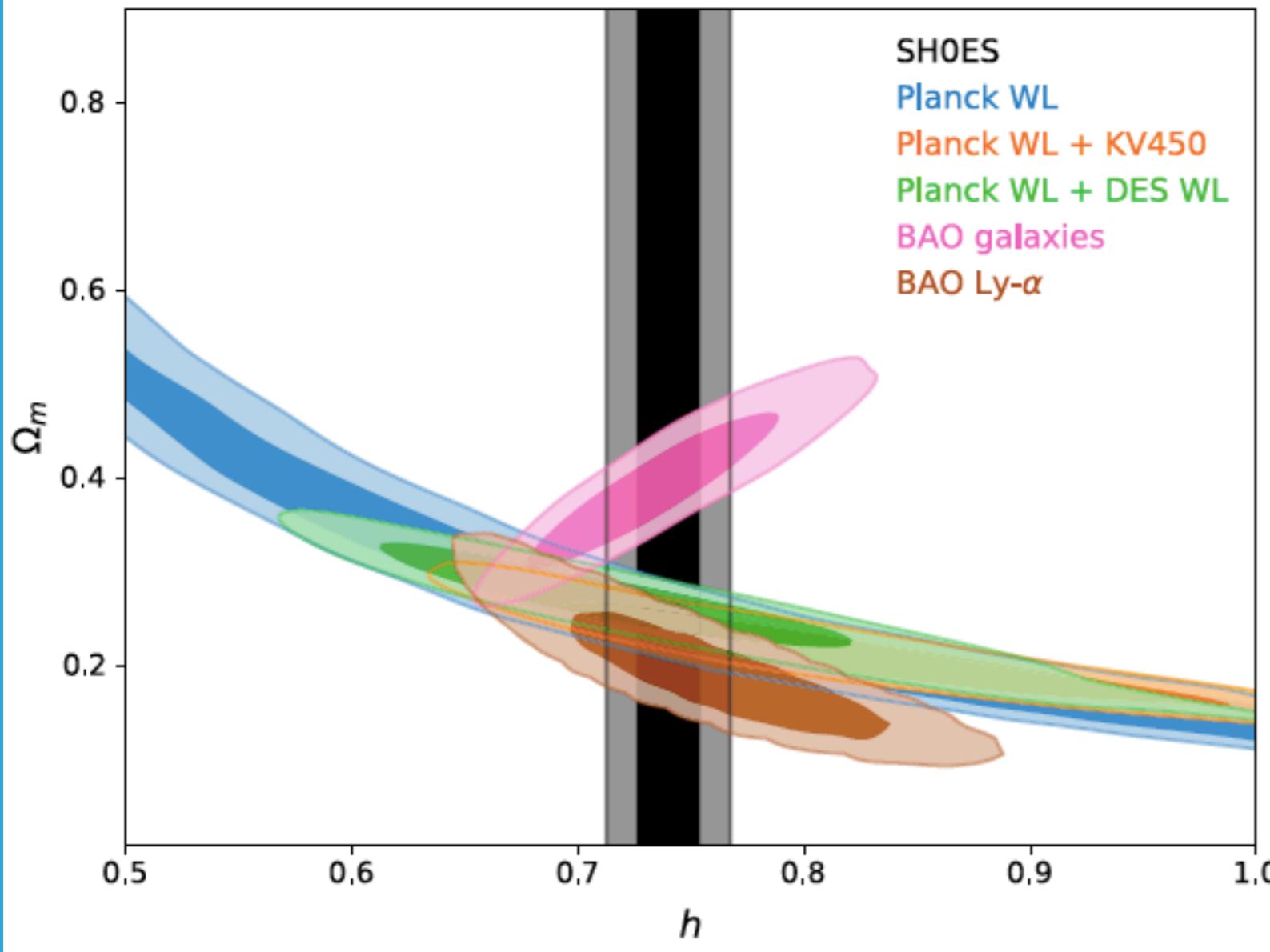
Galaxy lensing adds basically nothing to H_0 from CMB lensing + BAO.

Do get separate Ω_m and σ_8 constraints.

BAO + BBN + WL:

$$H_0 = 67.4 \pm 0.9 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

WHAT *CAN* WEAK LENSING TELL US ABOUT H_0 ?



Galaxy lensing adds basically nothing to H_0 from CMB lensing + BAO.

Do get separate Ω_m and σ_8 constraints.

BAO + ~~BBN~~ + WL:

$$H_0 = 70.0 \pm 6.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

**S8 and nothing else - same
story in ~10 years time?**

NEAR-FUTURE WEAK LENSING SURVEYS



Vera C. Rubin Observatory:
The Legacy Survey of Space and Time (LSST)

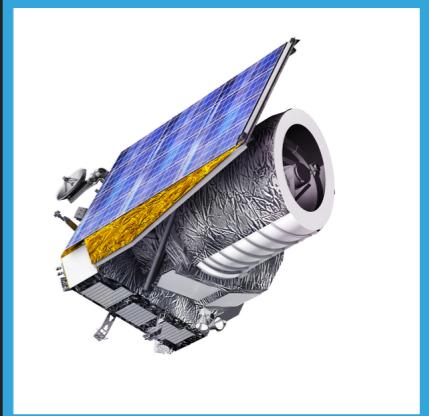
8.4m M1

18,000 sq deg: WL, GC, 3x2pt

$n_{\text{eff}} \approx 30$ galaxies per sq arcmin.



EUCLID



1.2m primary
mirror made
from silicon
carbide.

Two instruments:
Visible light
camera (VIS) and
Near-Infrared
camera (NISP).

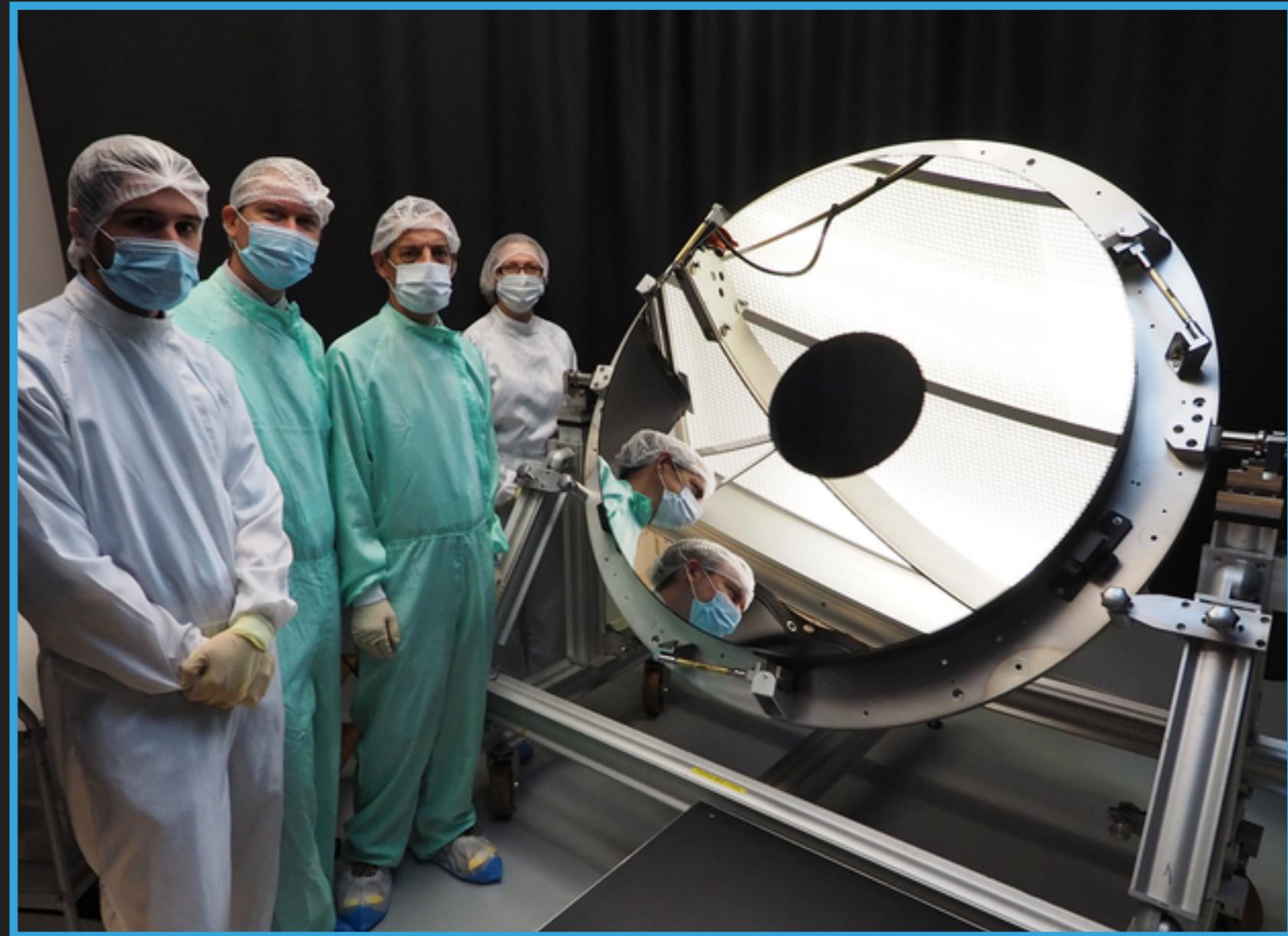
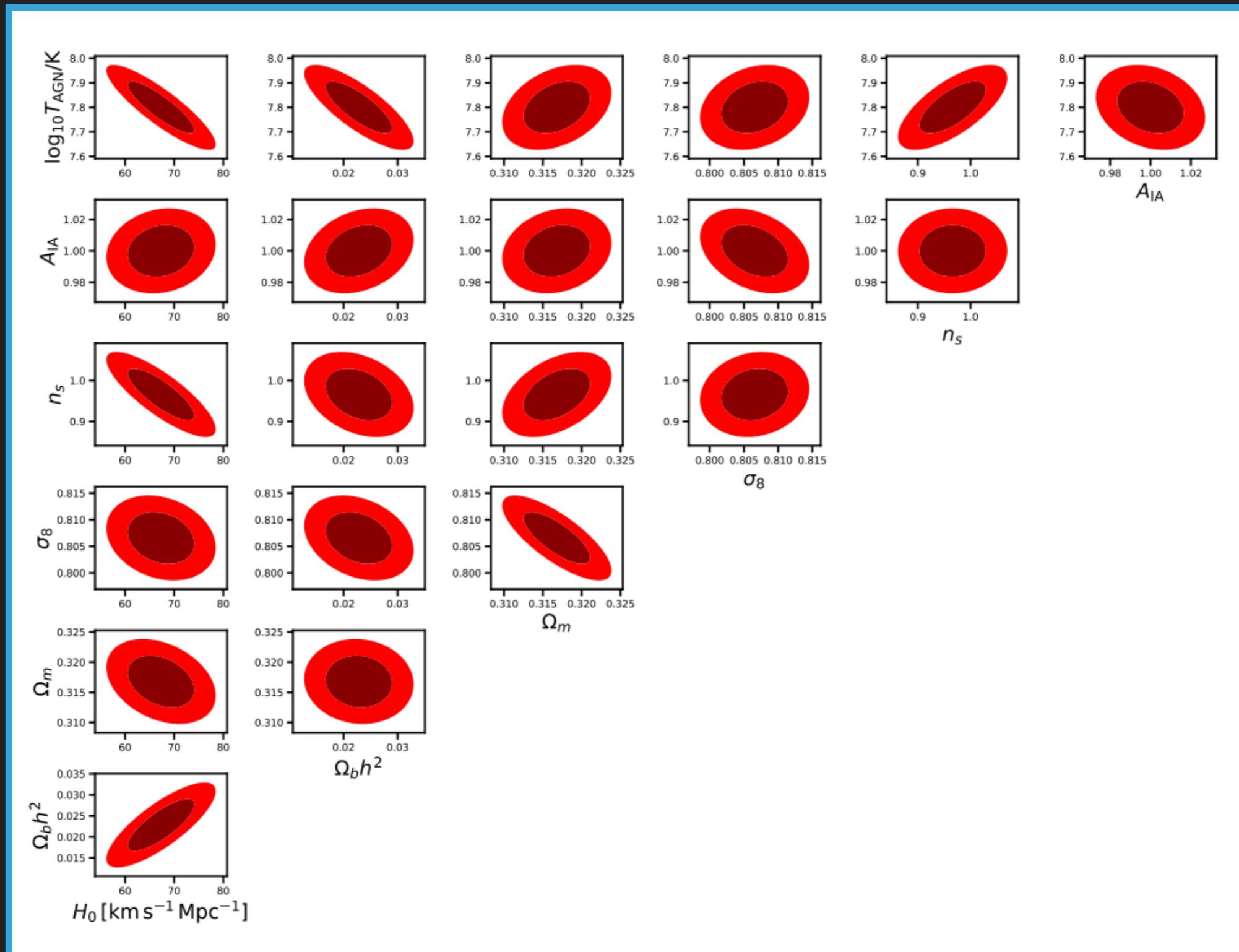


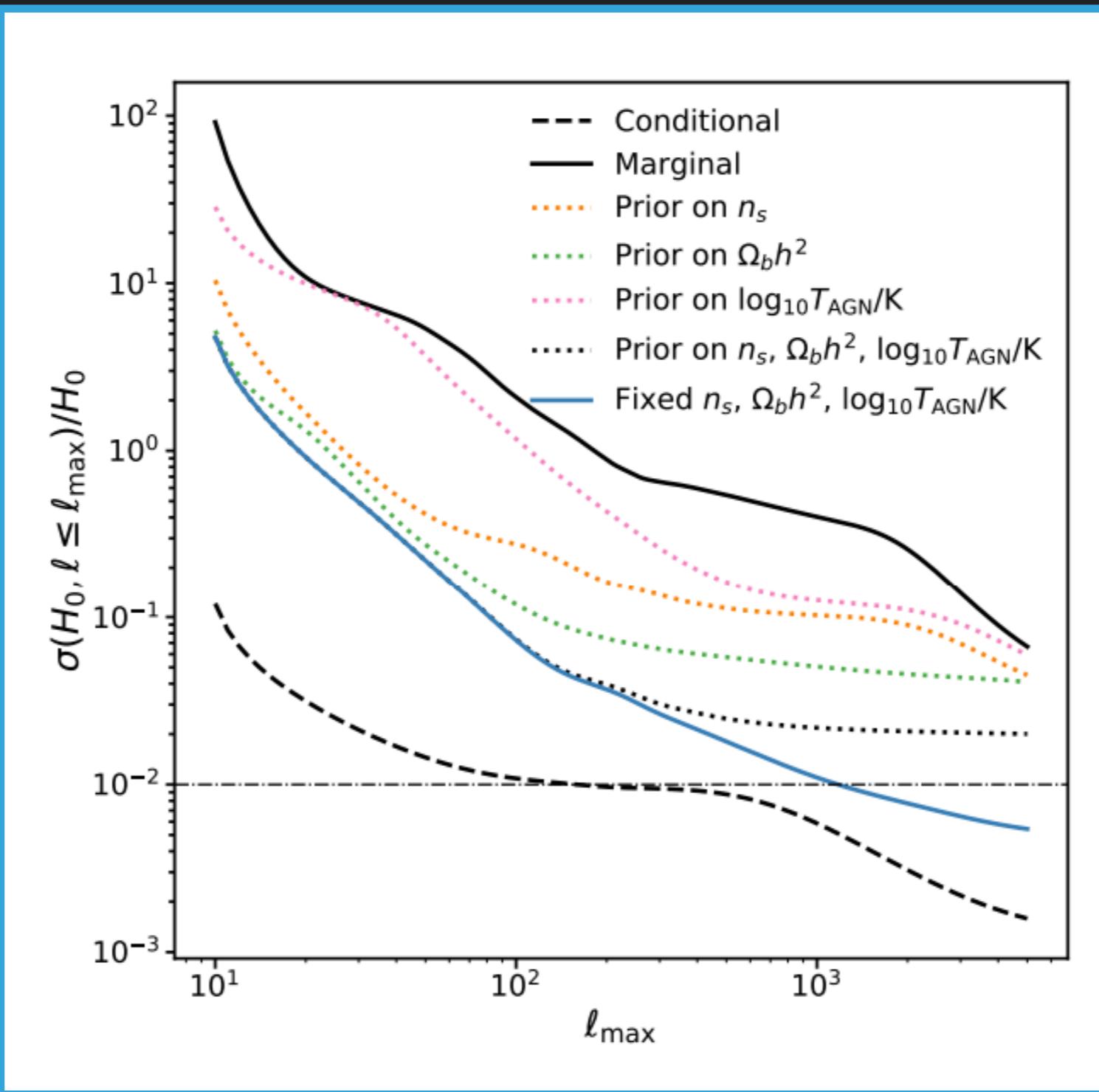
Image credit: ESA

Launch date: 2023

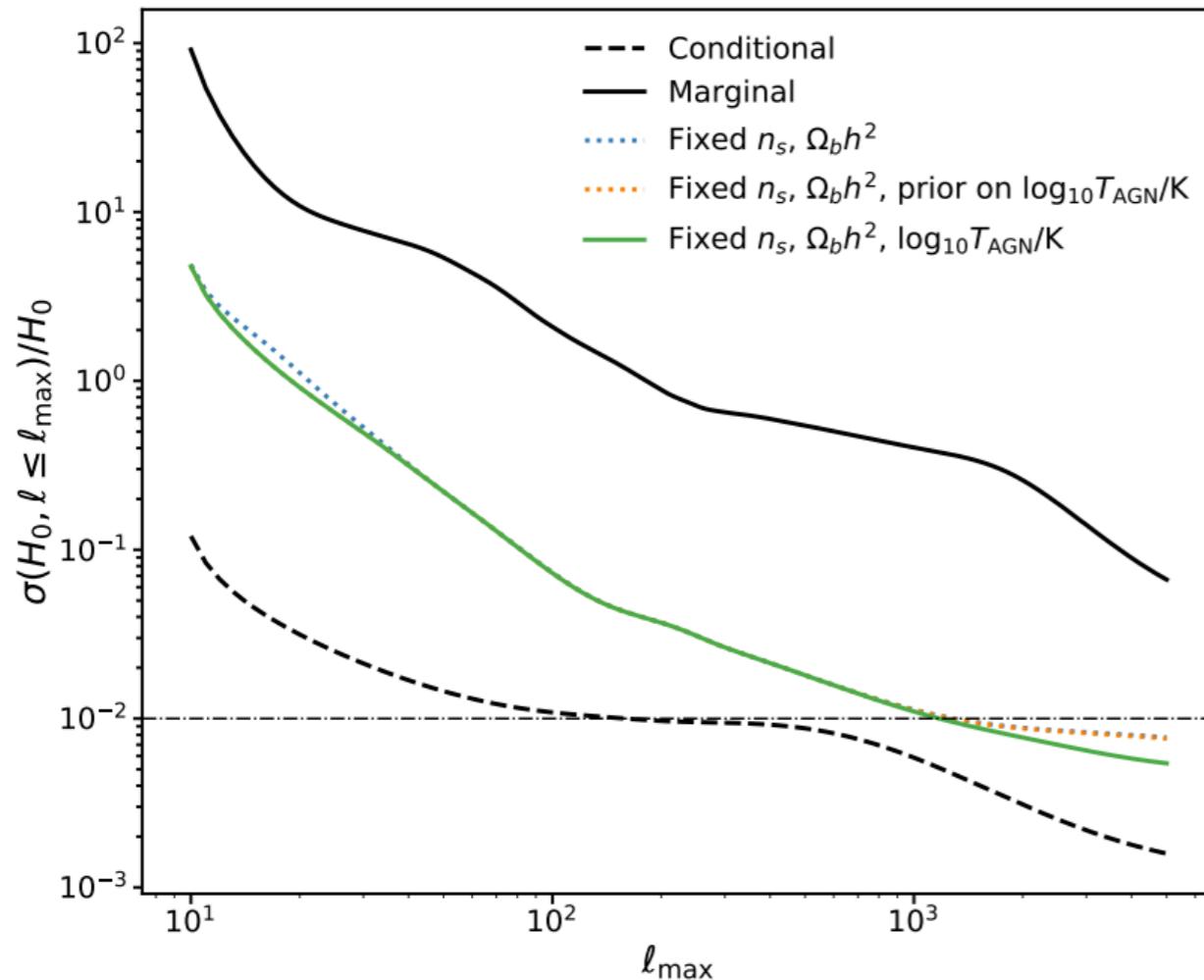
EUCLID-LIKE FORECAST FOR LCDM



EUCLID-LIKE FORECAST ON H_0



EUCLID-LIKE FORECAST ON H_0



AH 2021

For 1% H_0 from lensing
need *at least*:

- to know n_s to current (Planck) precision
- assume BBN
- Use all modes out to $l_{\text{max}}=5000$

H_0 information coming from broadband shape of the power spectrum - many degeneracies!

CONCLUSIONS

- Current lensing surveys alone give good constraint on $S8$ but weak/no constraint on $H0$.
- Have shown why current lensing data constrain $S8$ well and $H0$ poorly, using **analytic arguments** based on the halo model.
- Cleanest probe of $H0$ is the matter-radiation equality scale seen in projection, followed by subtle effects on the shape of the spectrum: partially degenerate with baryon feedback. Looks like Euclid will have a tough job of getting $< 1\%$ $H0$ from lensing alone!

IF YOU ENJOYED THIS, YOU MAY ALSO LIKE...

Astrophysics > Cosmology and Nongalactic Astrophysics

[Submitted on 8 Feb 2022]

The non-Gaussian likelihood of weak lensing power spectra

[Alex Hall](#), [Andy Taylor](#)

arXiv:2202.04095

Theory + simulations paper:

- Derive the leading-order correction to the power spectrum likelihood from non-Gaussianity (non-linearity) in the shear field.
- Provide (first?) rigorous justification for the use of a Gaussian likelihood for power spectra in wide cosmic shear surveys (or 3x2pt).