

# Almanac

**Generic Field Level Inference for Full-Sky Cosmological Fields  
and Angular Power Spectra**

**Dr. Arthur Loureiro @ German Centre for Cosmological Lensing  
(Oskar Klein Centre, Stockholm University & Imperial College London)**

# The Almanac Team



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Universiteit  
Leiden



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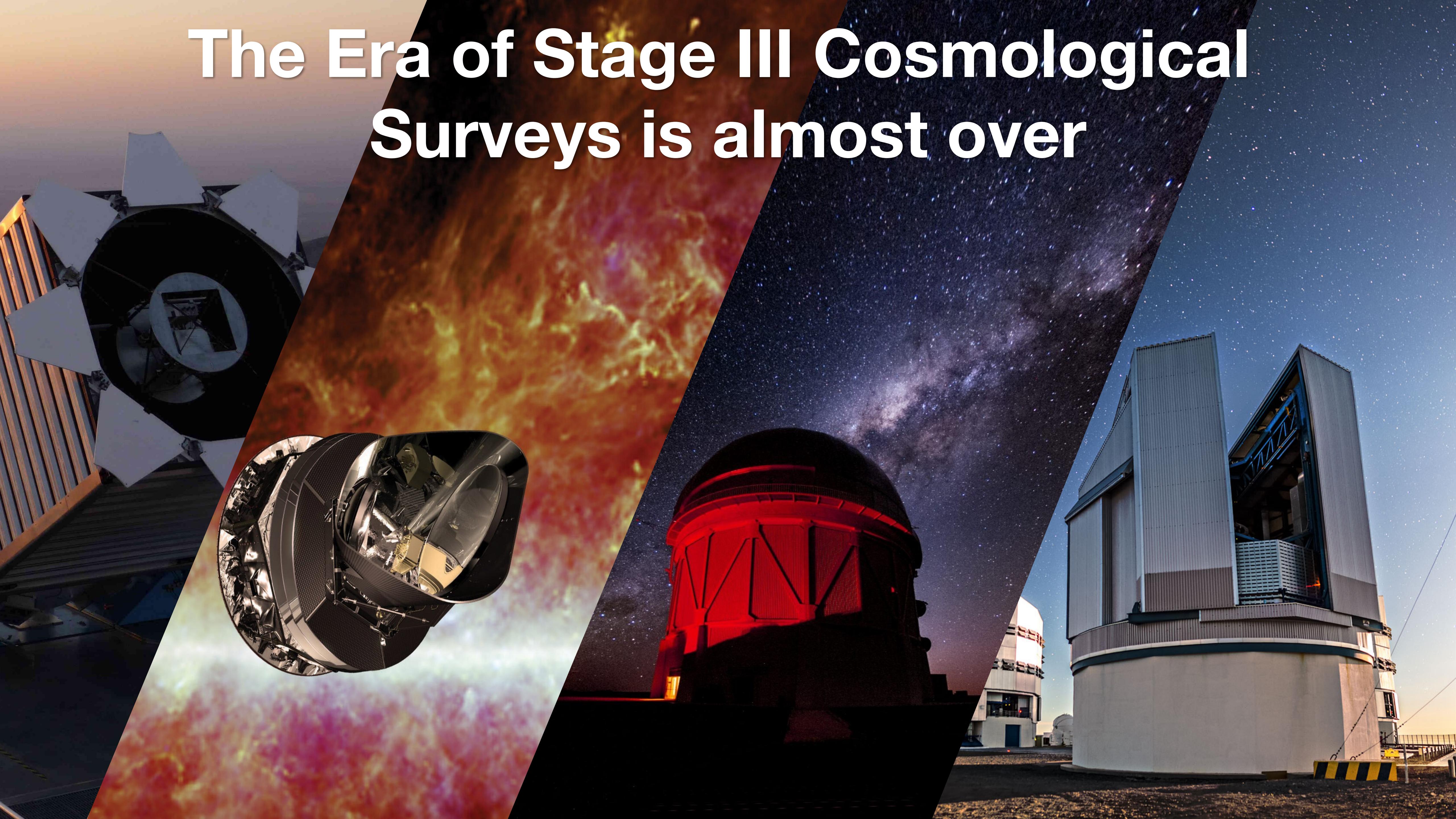


+ Javier S. Lafaurie

# **1. Observational Cosmology**

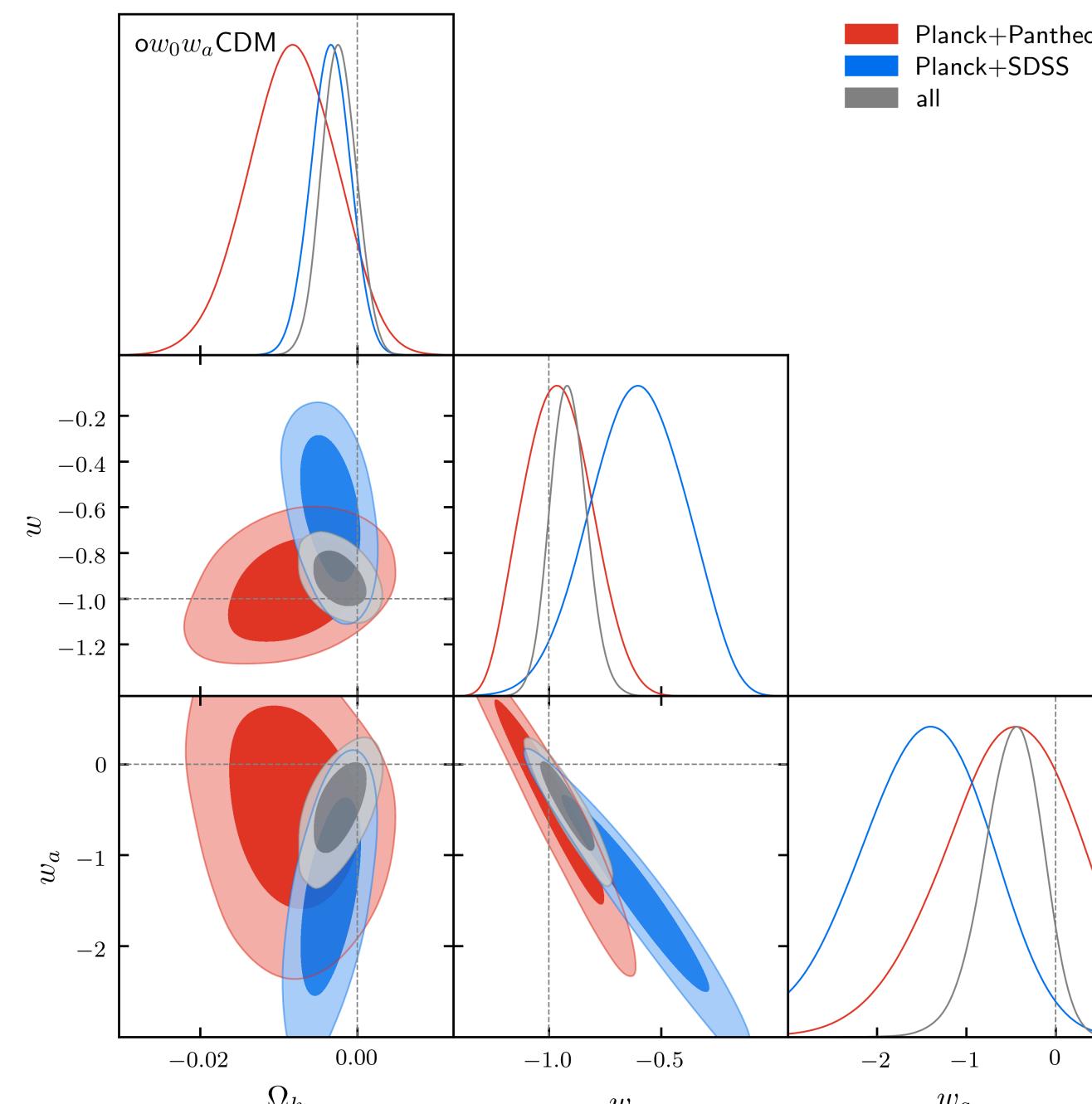
## **Where are we, and where are we going?**

# The Era of Stage III Cosmological Surveys is almost over

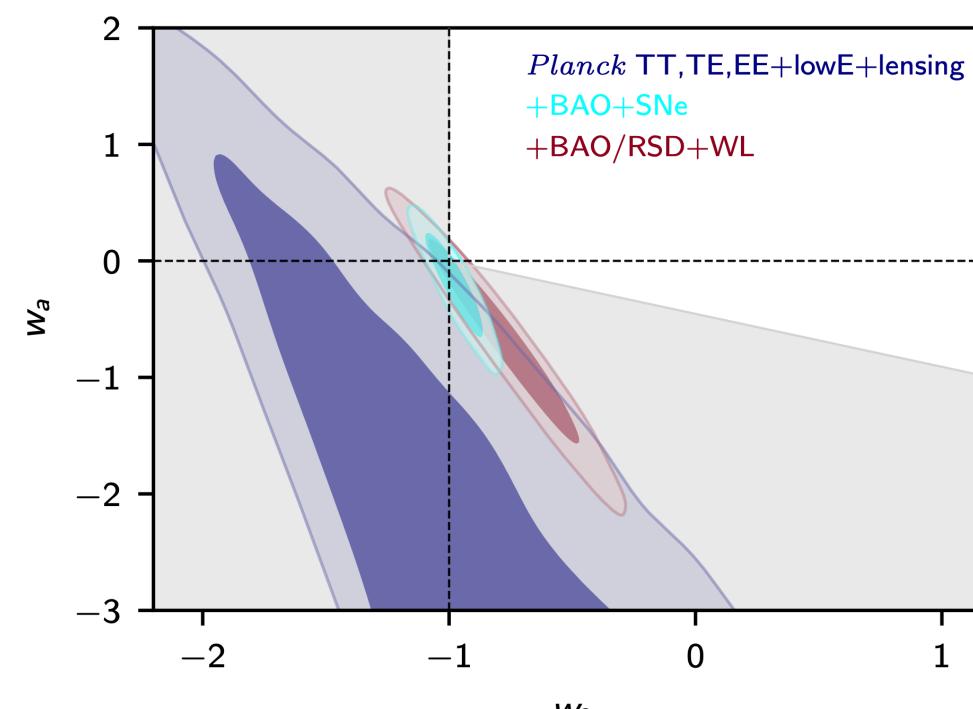


# Stage III Surveys

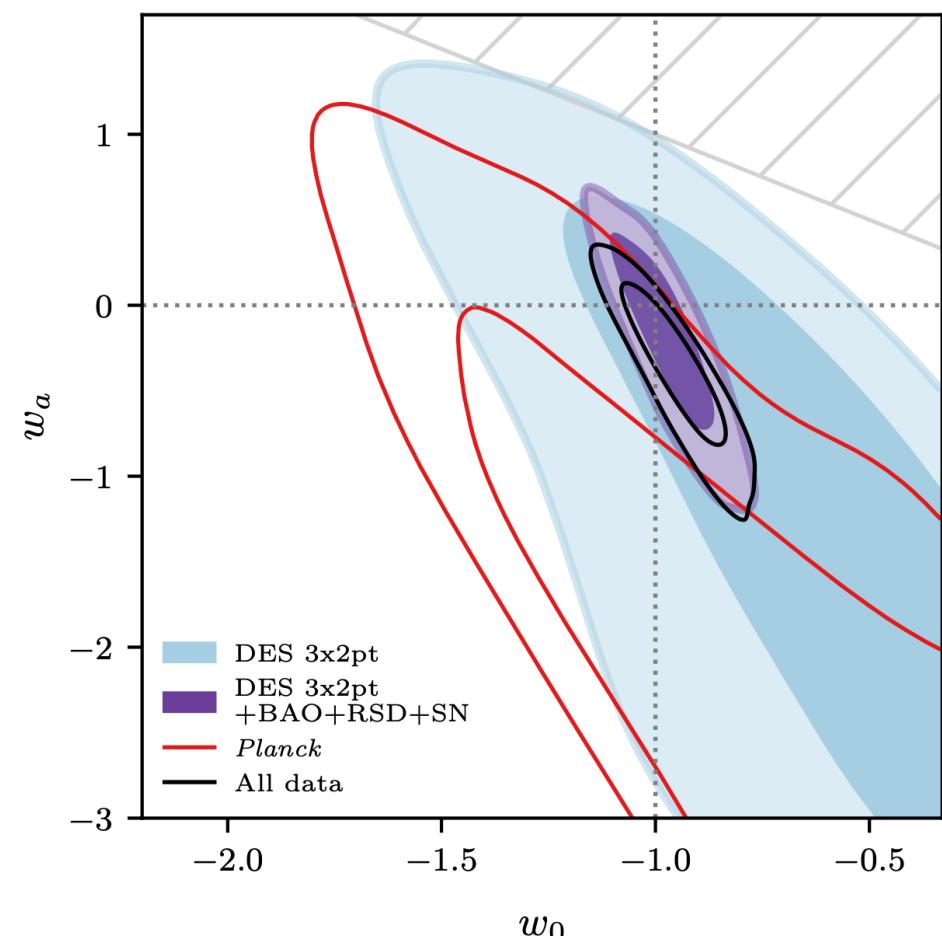
“It’s  $\Lambda$ CDM whether you like it or not...”



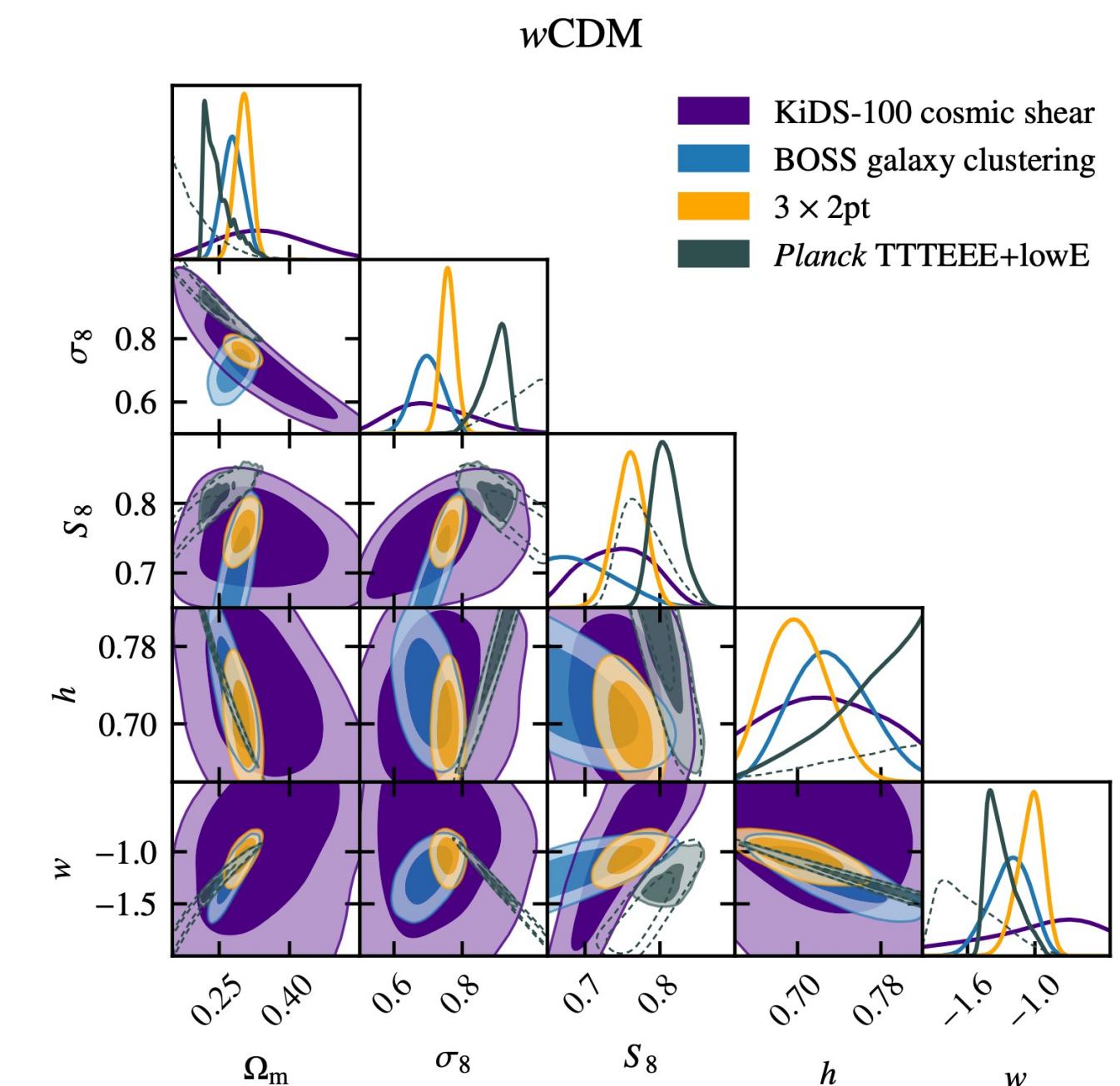
eBOSS Collaboration  
(Alam et al. 2021)



Planck Collaboration, 2018



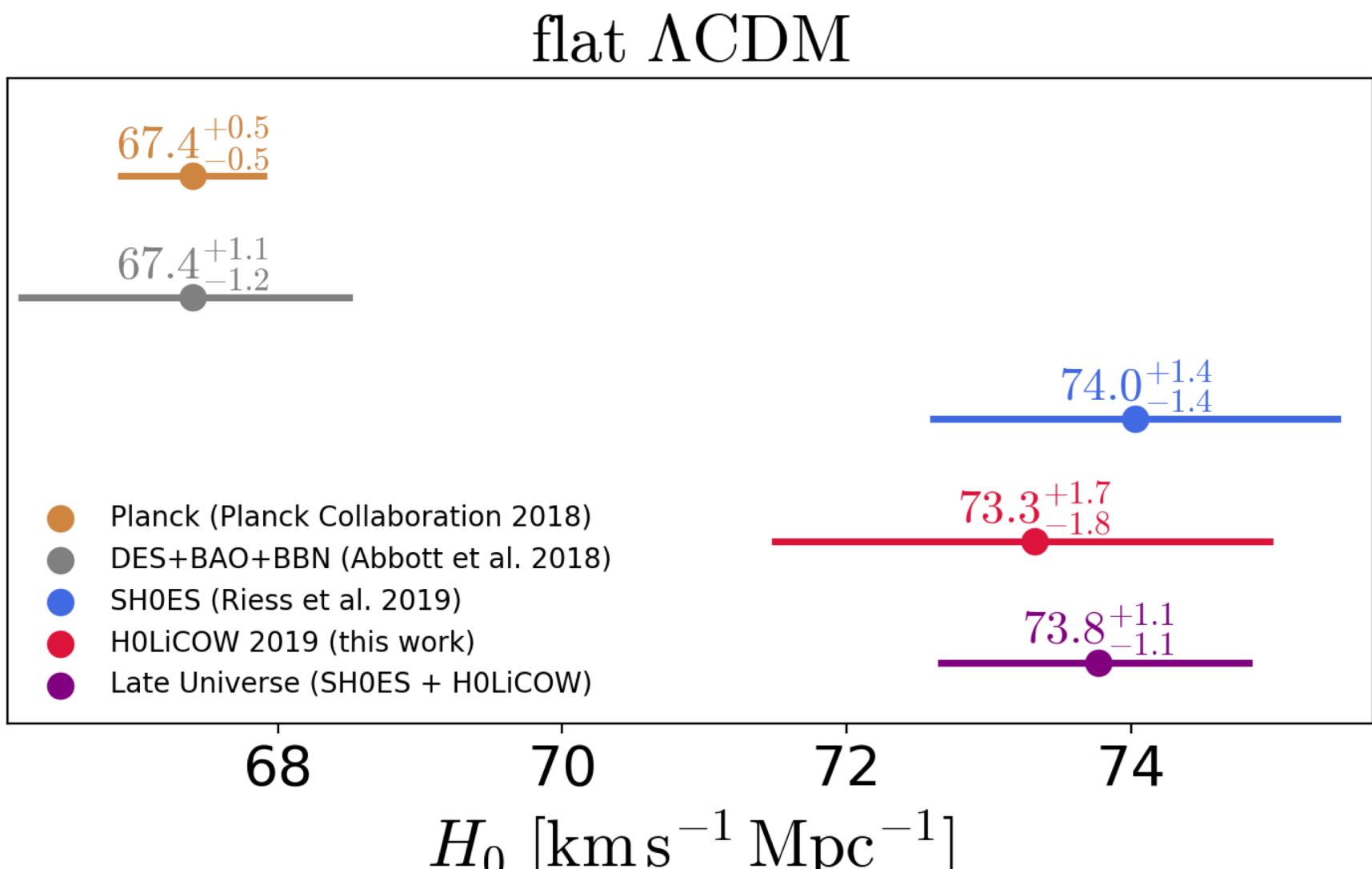
Dark Energy Survey, 2022



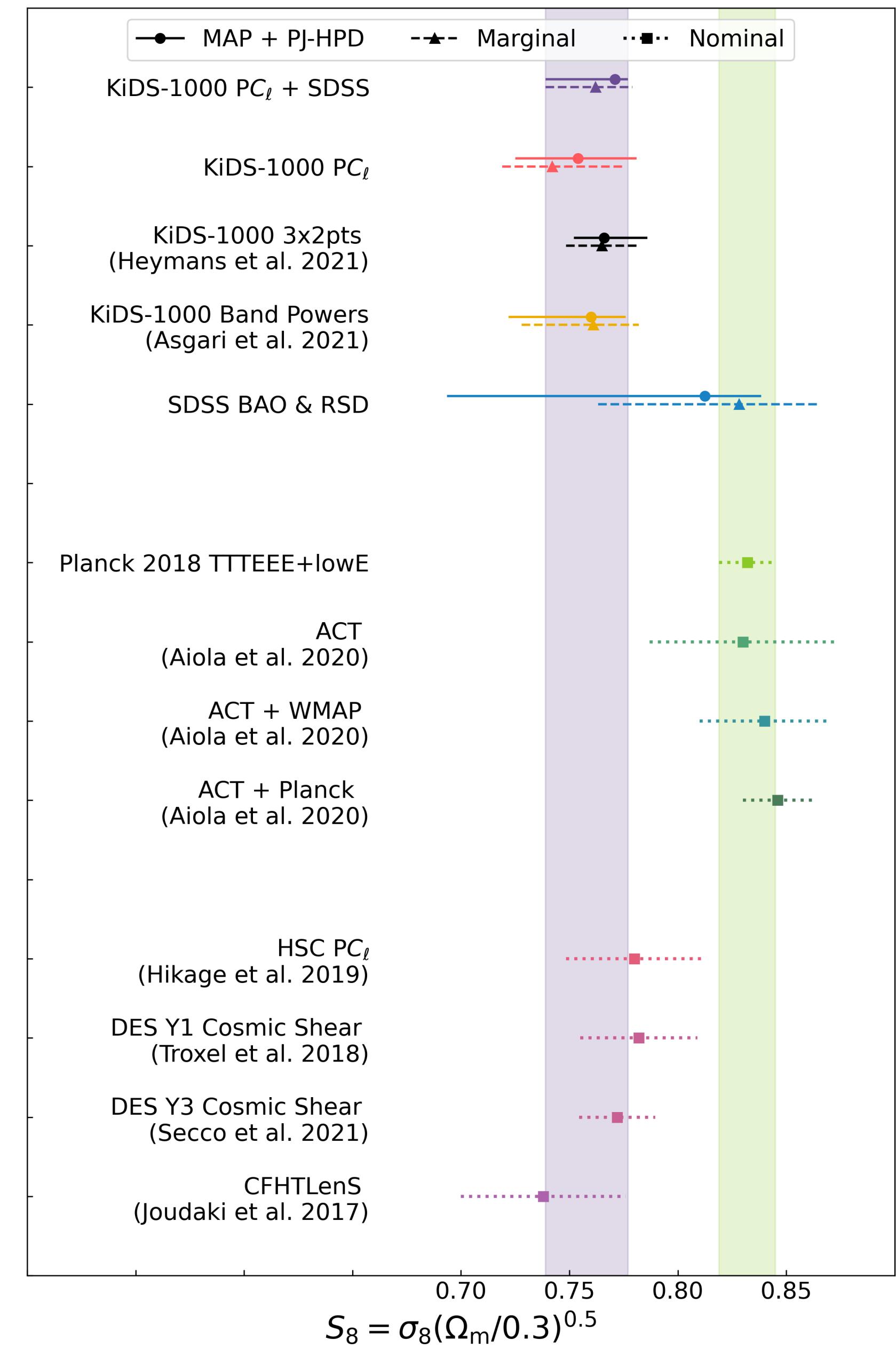
KiDS Collaboration  
(Tröster et al., 2020)

# Stage III Surveys

“It’s  $\Lambda$ CDM whether you like it or not...”  
OR NOT



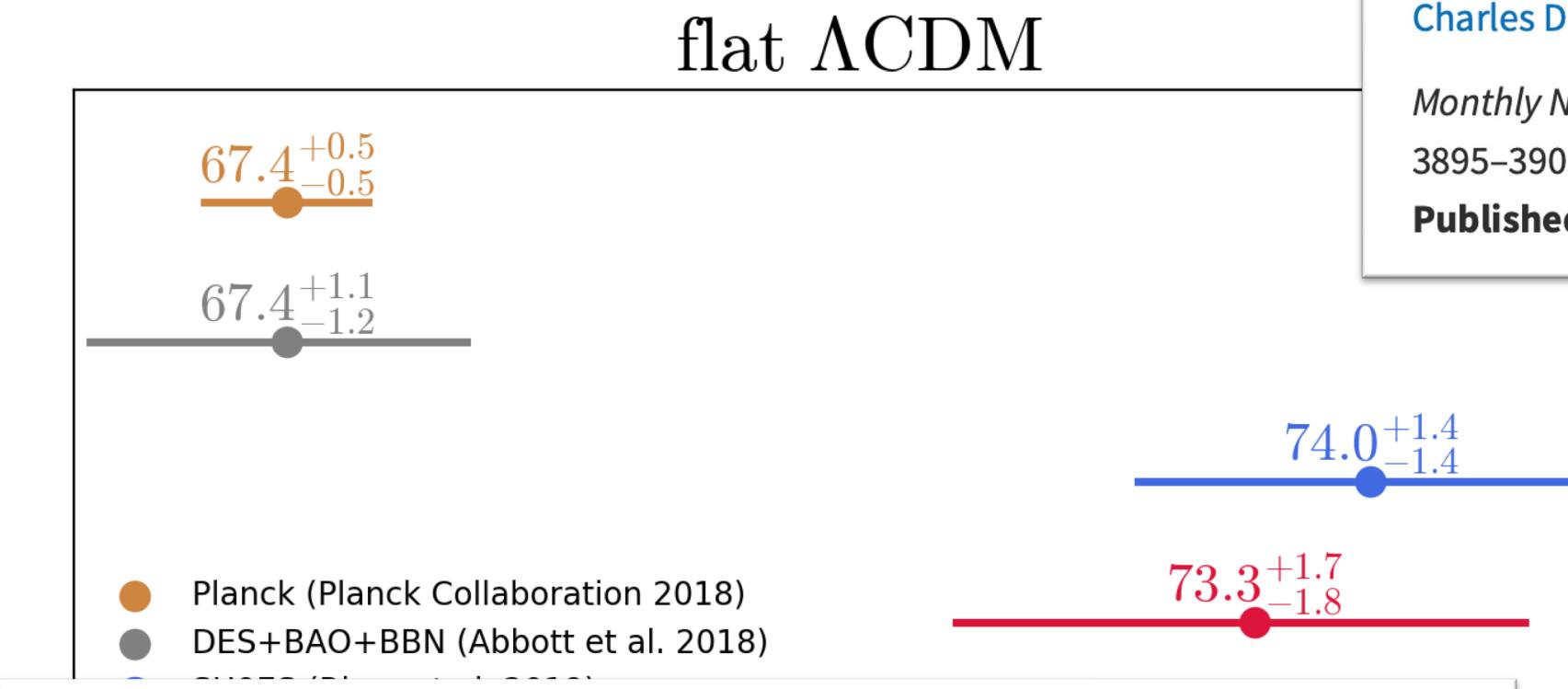
Wong et al. 2019



Loureiro et al., A&A (2022)

# Stage III Surveys

“It’s  $\Lambda$ CDM whether you like it or not...”  
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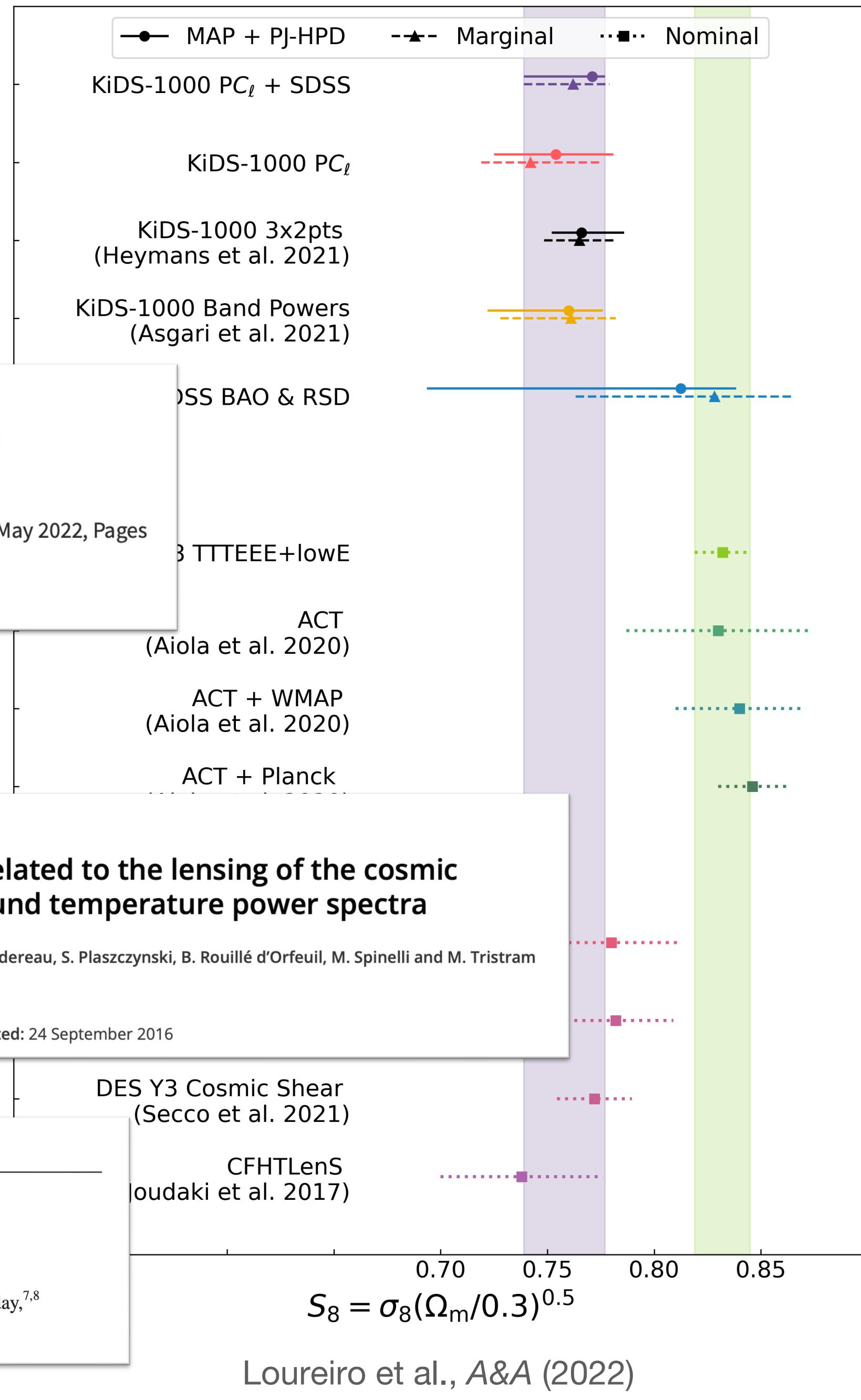
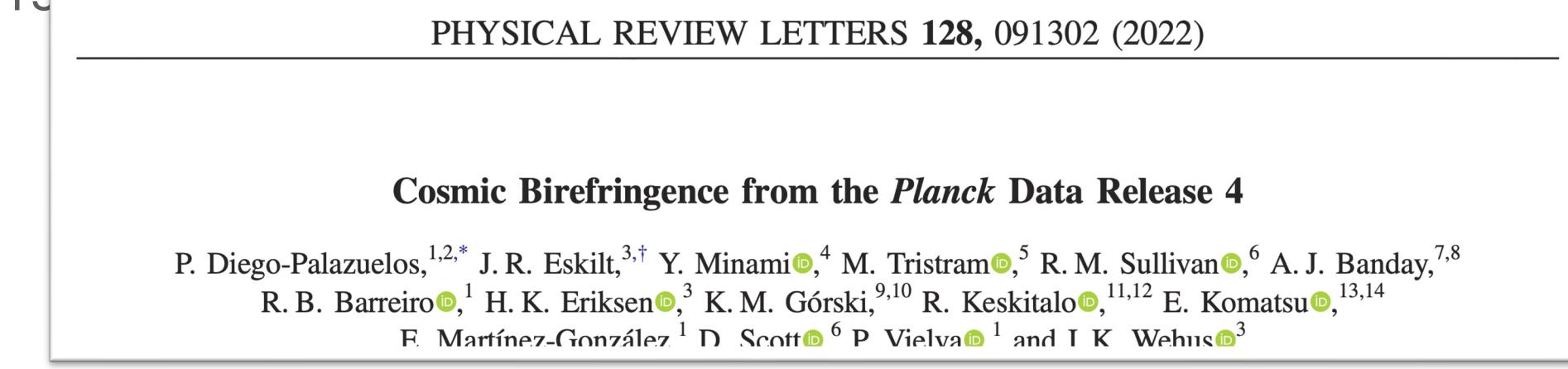
Article | Published: 04 November 2019

**Planck evidence for a closed Universe and a possible crisis for cosmology**

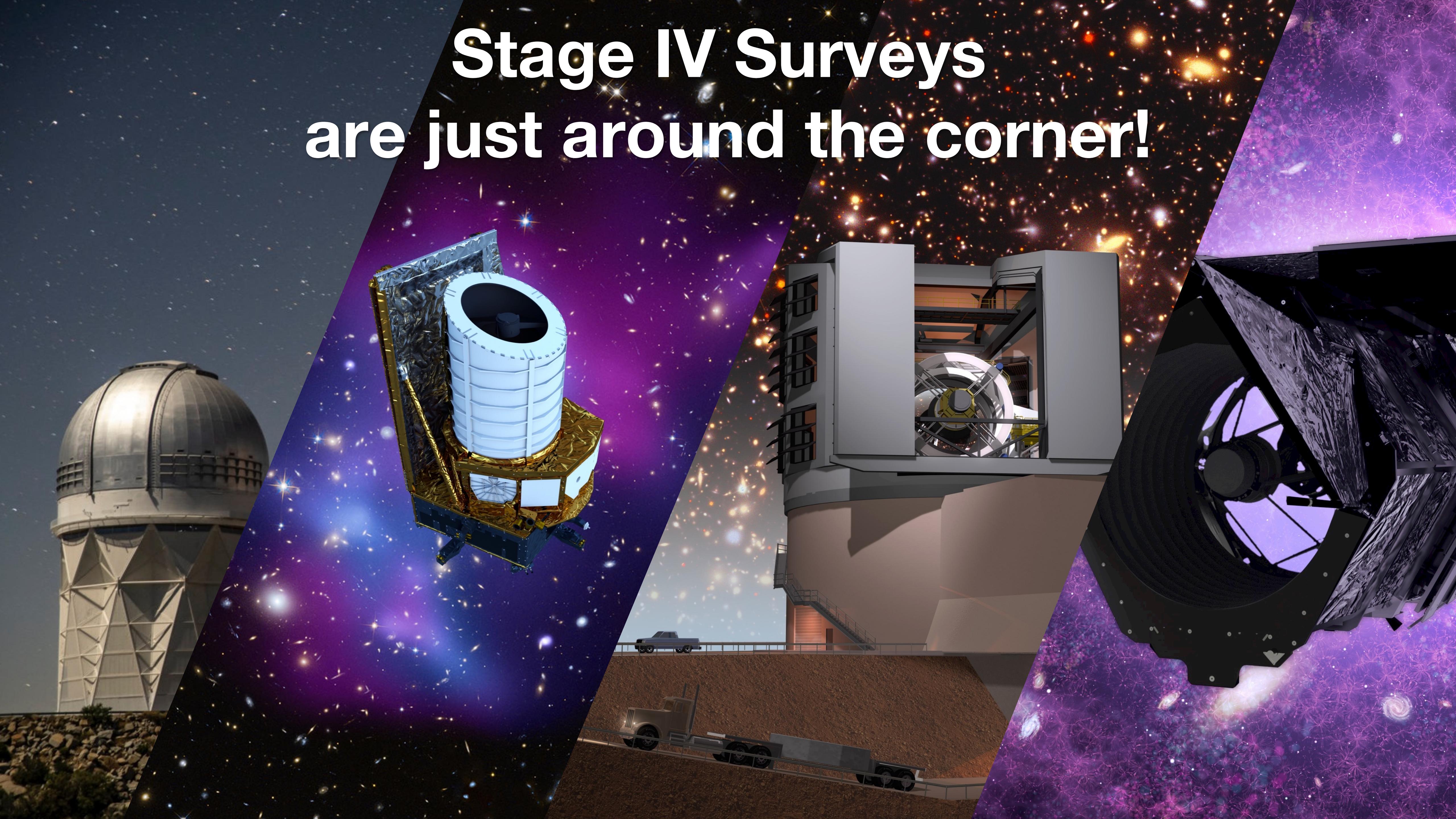
Eleonora Di Valentino, Alessandro Melchiorri & Joseph Silk

Nature Astronomy 4, 196–203 (2020) | Cite this article

Wong et al. 2019



# Stage IV Surveys are just around the corner!

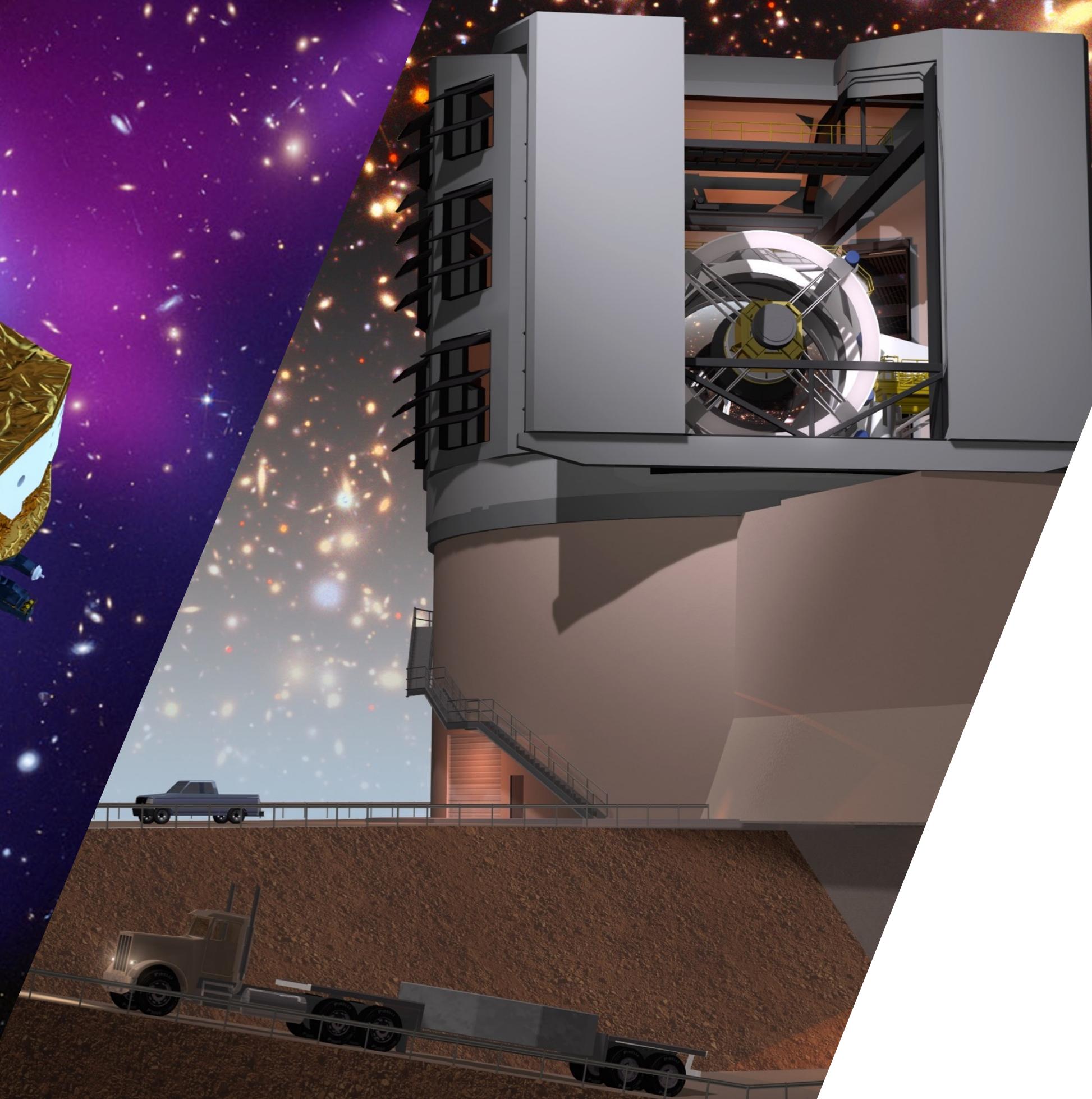


- ~ 2 Billion galaxies for Weak Lensing
- ~ 50 Million galaxies for Galaxy Clustering
- Photometric and Spectroscopic
- $15\ 000 \text{ deg}^2$
- Up to redshift of ~ 2
- Launch: 2023

# Euclid



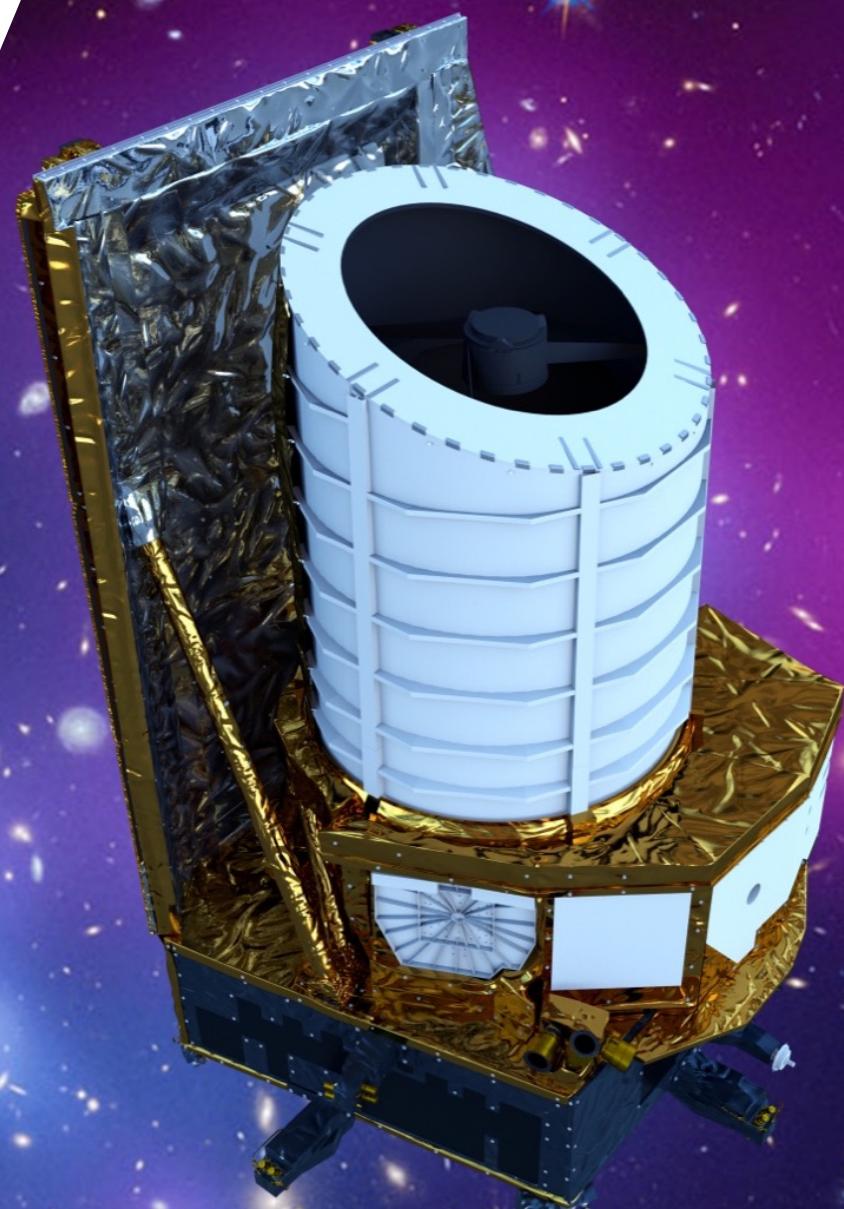
# LSST



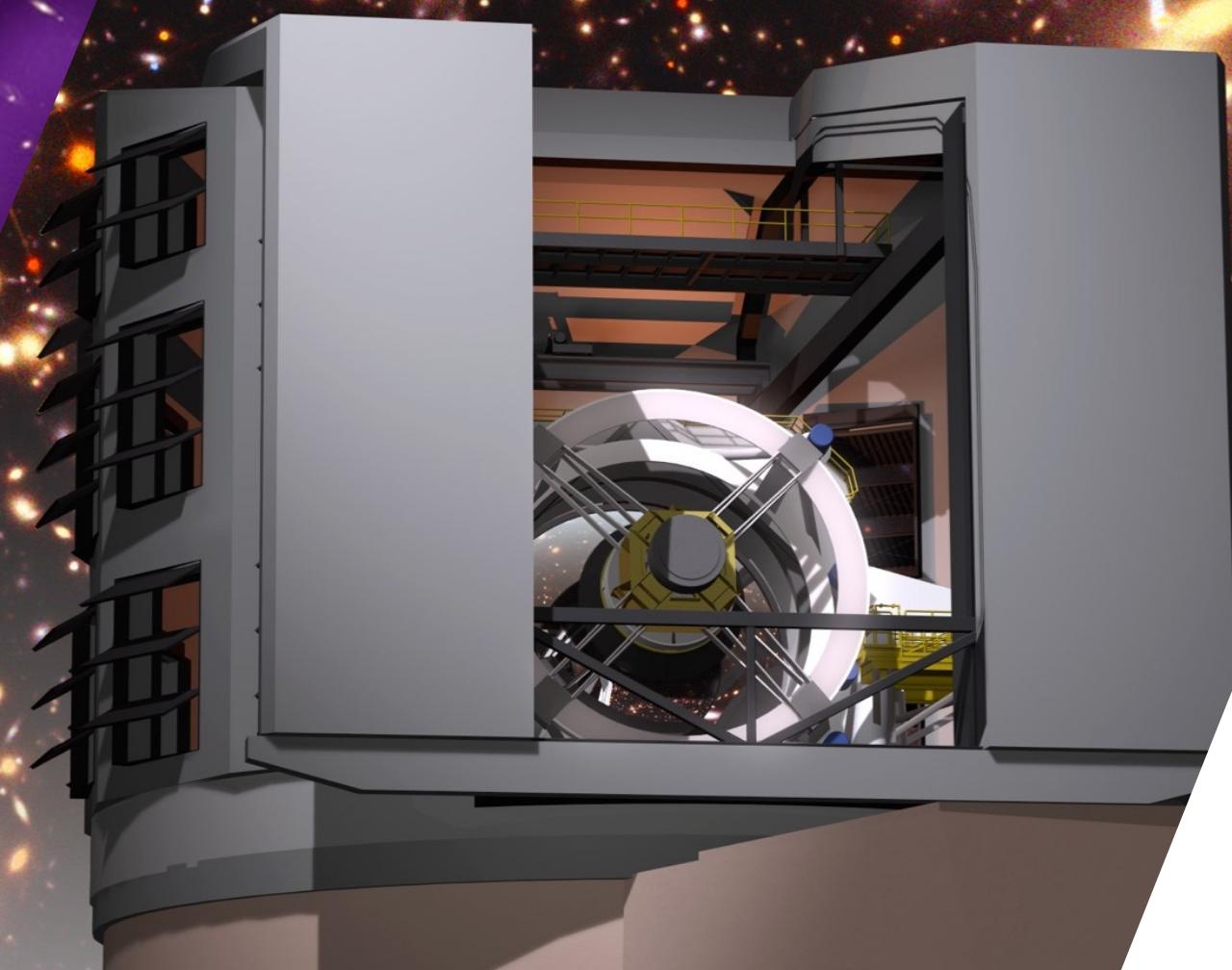
- ~ 20 Billion photometric galaxies
- ~  $10^5$  Supernovae
- Six bands (ugrizy)
- $18\ 000 \text{ deg}^2$
- Up to redshift of ~ 1.2
- First Light: 2023

- ~ 2 Billion galaxies for Weak Lensing
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# Euclid



# LSST



- ~ 20 Billion photometric galaxies
- $\sim 10^5$  Supernovae
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- $18\ 000 \text{ deg}^2$
- Up to redshift of ~ 1.2
- First Light: 2023

Both will be amazing for Weak Lensing



The background features a vibrant, abstract illustration of a telescope. The telescope's body is white with a black lens, set against a dark background with pink and blue swirling patterns. A green ribbon-like shape flows from the telescope towards the right. The sky is filled with various symbols: pink diamonds, red crosses, blue squares, and white stars. In the foreground, there is a grid of binary code (0s and 1s) on a blue background. To the right, a vertical color bar shows a gradient from purple to red.

Exploring Stage-IV data will require the next generation of data analysis techniques, breaking away from outdated assumptions such as sky-flatness, gaussianity, etc.

# **1. Weak Lensing**

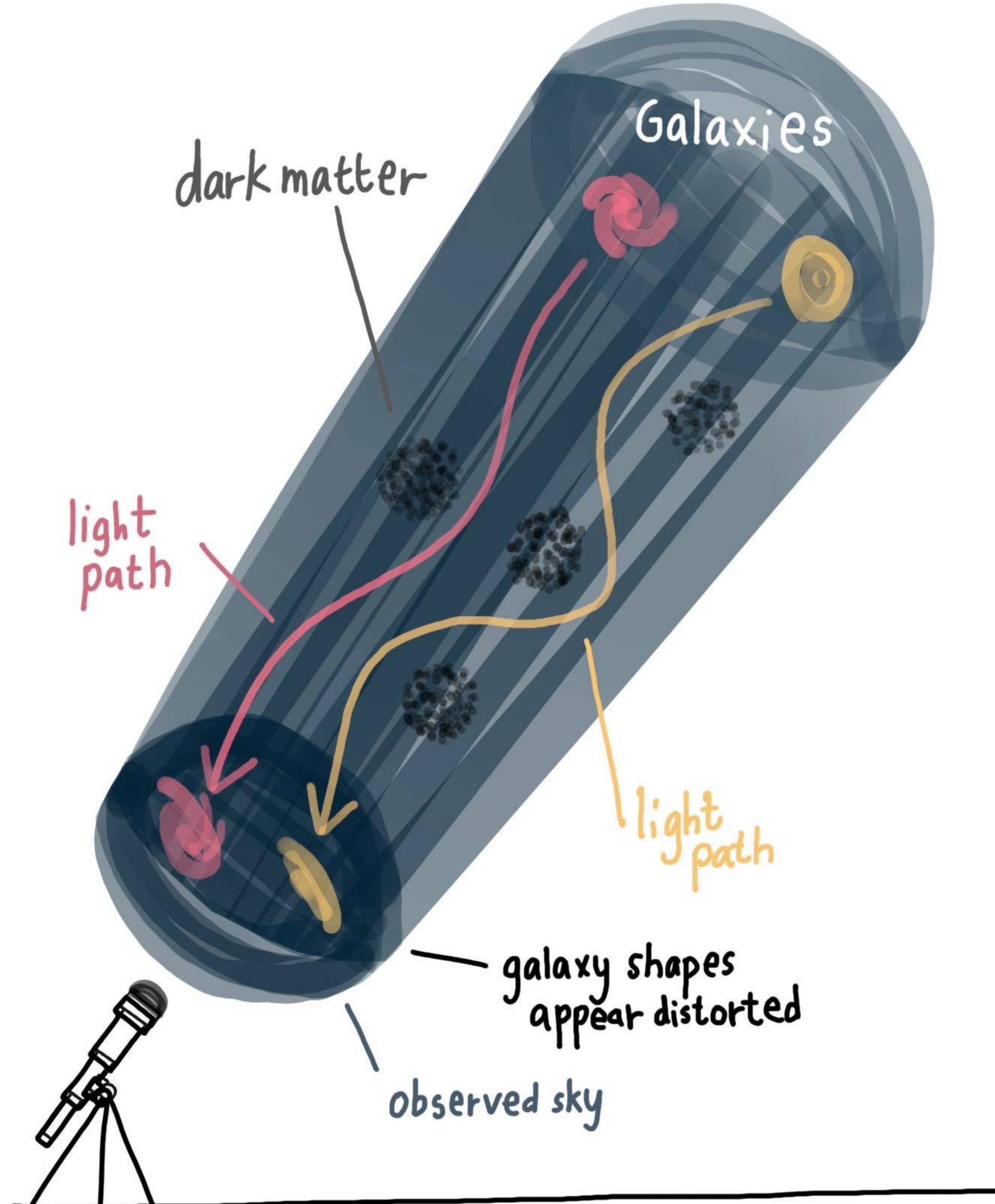
**A speed-run**

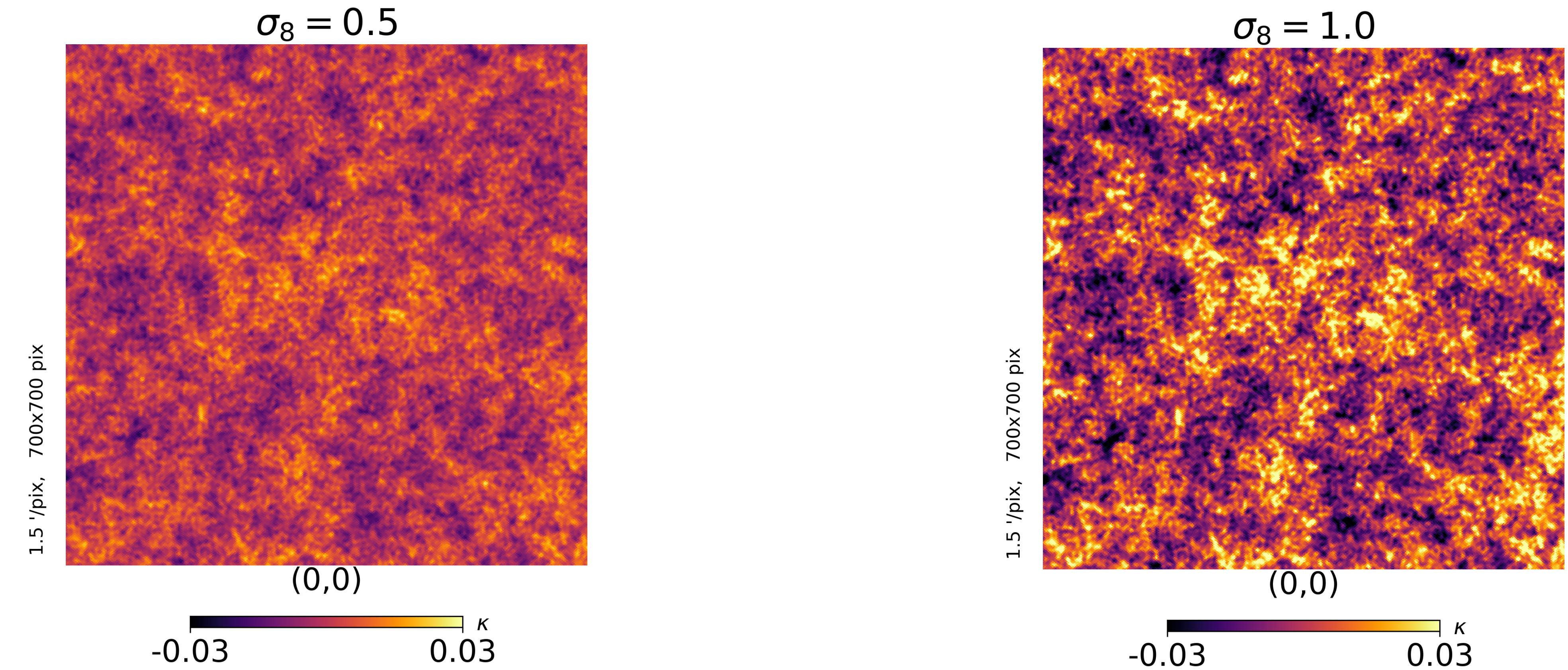
# Weak Lensing (mandatory slide!)

We can probe the growth of structures in the universe using weak gravitational lensing

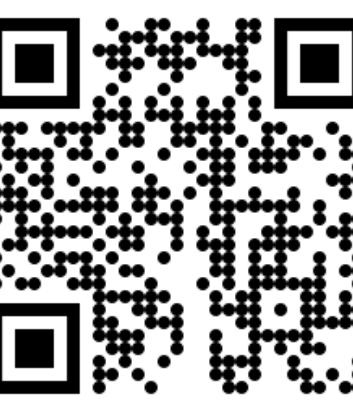
$$S_8 = \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{1/2}$$

as well as the distribution of matter along the line-of-sight.





# The amplitude of matter density fluctuations



# Weak Lensing Theory Speed-run

- The mapping between the lensing source's true angular position and the observed angular position is  $\theta_{s,i} \approx A_{ij}\theta_{\text{obs},j}$ , with

$$A_{ij} = \delta_{ij} - \partial_i \partial_j \tilde{\Psi}$$

where

$$\tilde{\Psi}(\chi_s, \hat{n}) = 2 \int_0^{\chi_s} d\chi \frac{f_K(\chi_s - \chi)}{f_K(\chi) f_K(\chi_s)} \Psi(\chi, \hat{n})$$



Newtonian  
Grav. Potential

- From these, we can define the Weak Lensing observables (in harmonic space):
  - Convergence:

$$\kappa_{\ell m} = -\frac{1}{2} \ell(\ell + 1) \tilde{\Psi}_{\ell m}$$

- Shear:

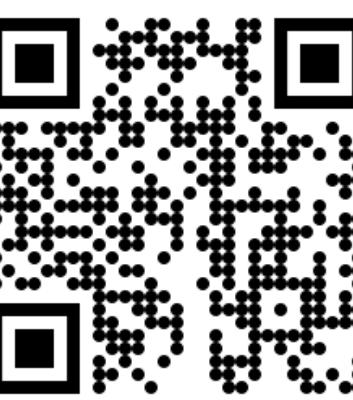
$$\gamma_{\ell m} = \frac{1}{2} \sqrt{(\ell - 1)\ell(\ell + 1)(\ell + 2)} \tilde{\Psi}_{\ell m}$$

- Since shear is a spin-2 field it can be decomposed into  $E$ - and  $B$ -modes

$$E_{\ell m} = -\frac{1}{2} \int d\Omega [\gamma(\hat{n}) {}_{+2}Y_{\ell m}^*(\hat{n}) + \gamma^*(\hat{n}) {}_{-2}Y_{\ell m}^*(\hat{n})]$$

and

$$B_{\ell m} = \frac{i}{2} \int d\Omega [\gamma(\hat{n}) {}_{+2}Y_{\ell m}^*(\hat{n}) - \gamma^*(\hat{n}) {}_{-2}Y_{\ell m}^*(\hat{n})].$$



# Weak Lensing Theory Speed-run

- The mapping between the lensing source's true angular position and the observed angular position is  $\theta_{s,i} \approx A_{ij}\theta_{\text{obs},j}$ , with

$$A_{ij}$$

where

$$\tilde{\Psi}(\chi_s, \hat{n}) = 2$$

**WELL, YOU KNOW IT...**

- From these, we can define the Weak Lensing observables (in harmonic space):
  - Convergence:

$$1) \frac{1}{\ell(\ell+1)(\ell+2)} \tilde{\Psi}_{\ell m}$$

it can be  
nodes

$$E_{\ell m} = -\frac{1}{2} \int d\Omega [\gamma(\hat{n}) {}_{+2}Y_{\ell m}^*(\hat{n}) + \gamma^*(\hat{n}) {}_{-2}Y_{\ell m}^*(\hat{n})]$$

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Newtonian  
Grav. Potential

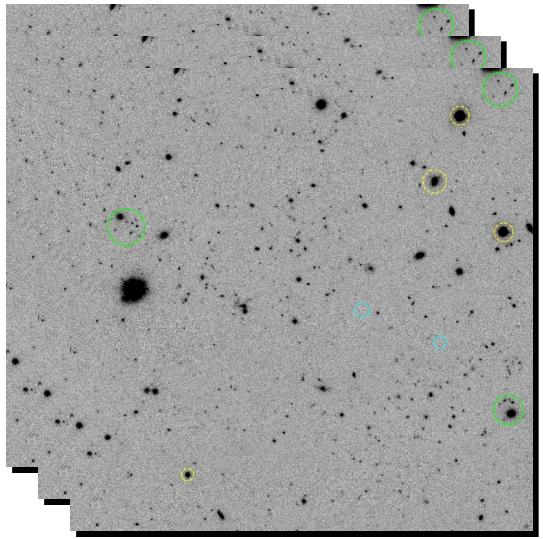
## **2. Field Level Inference**

**What is it, and Why do we care?**

# “Vintage” Cosmology

## Ex: Weak Lensing Surveys

Galaxy Shapes

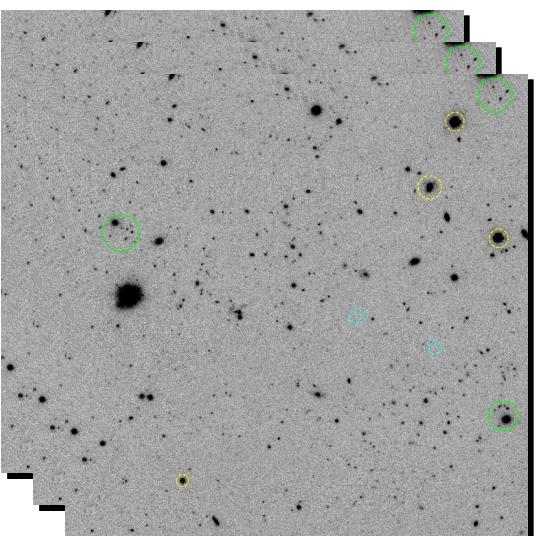


Kannawadi et al. 2018

# “Vintage” Cosmology

## Ex: Weak Lensing Surveys

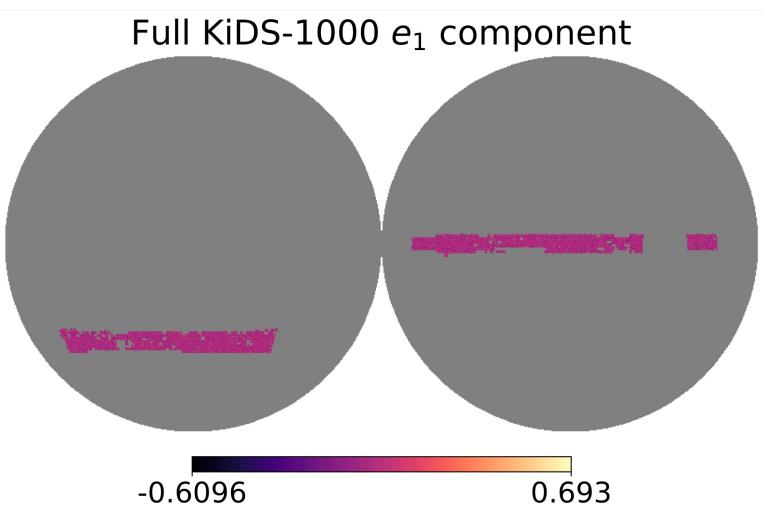
Galaxy Shapes



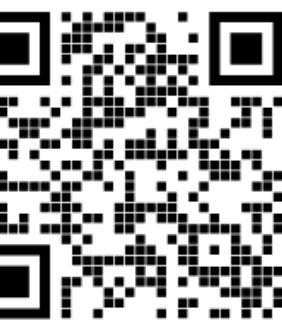
Kannawadi et al. 2018



“Estimator”

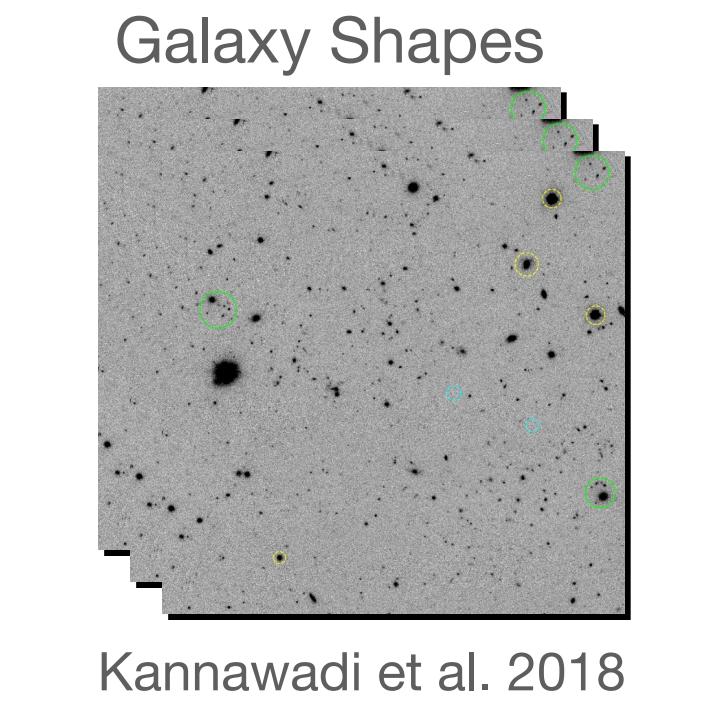


Galaxy shear maps

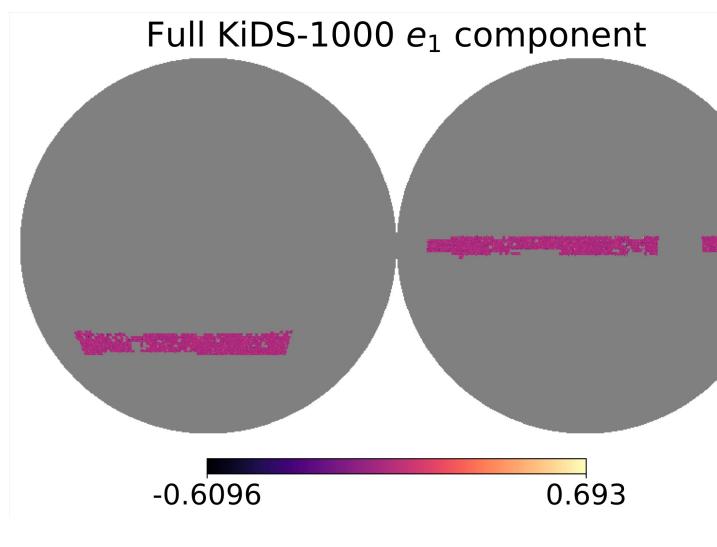


# “Vintage” Cosmology

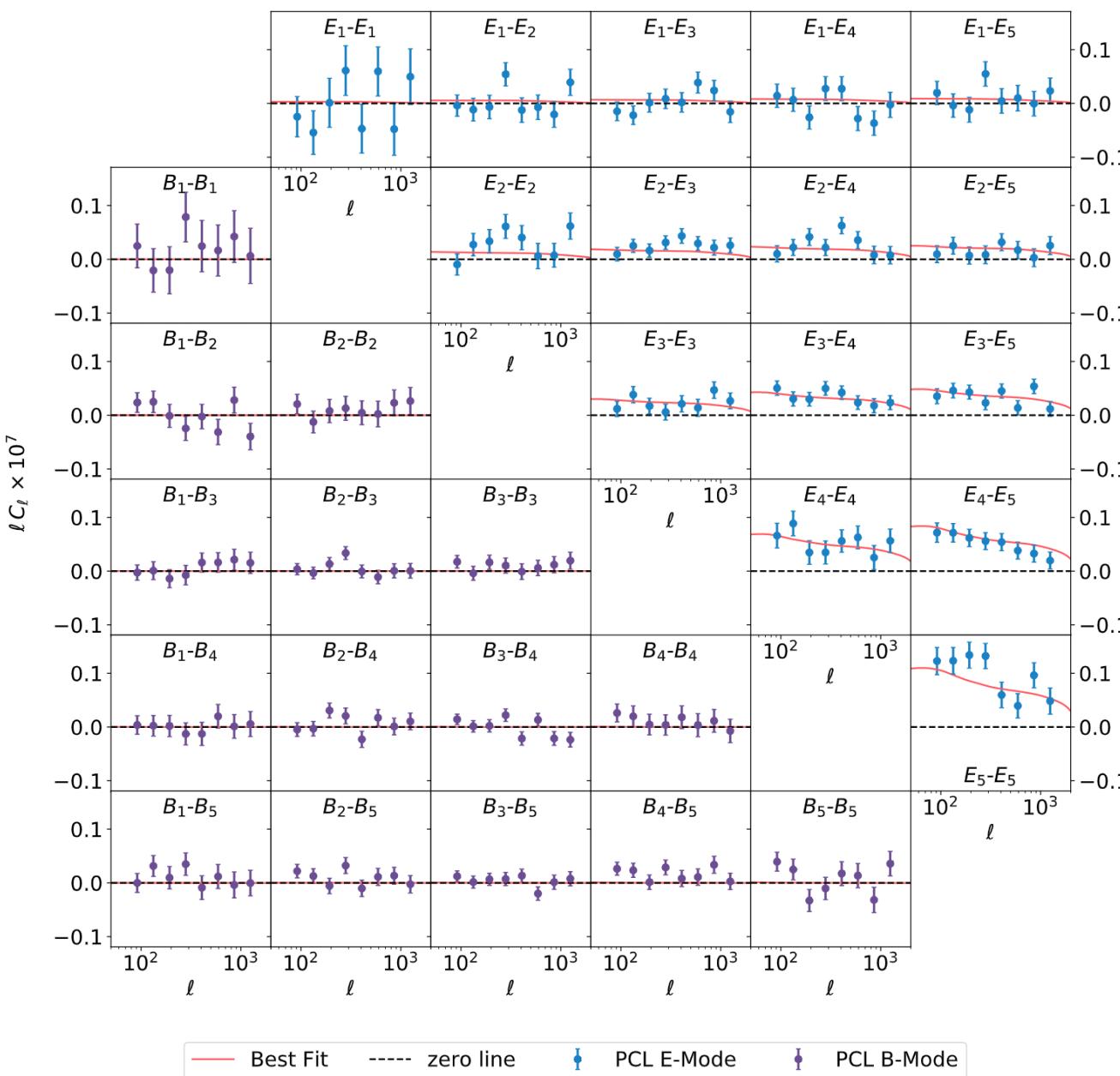
## Ex: Weak Lensing Surveys



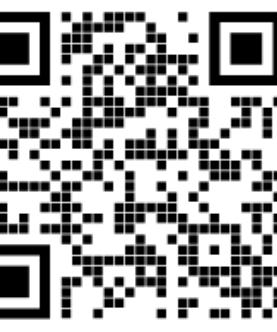
“Estimator”



Galaxy shear maps



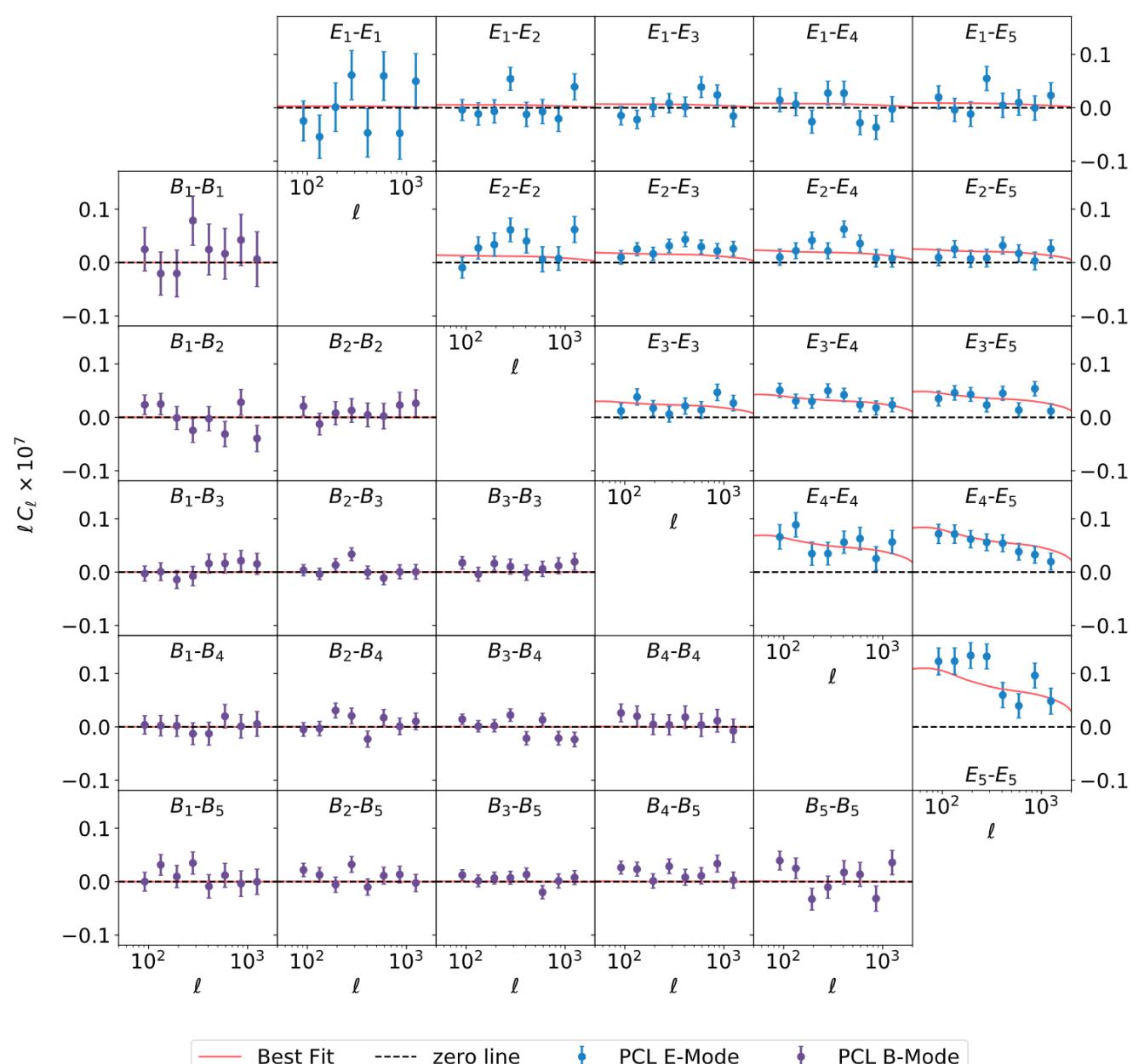
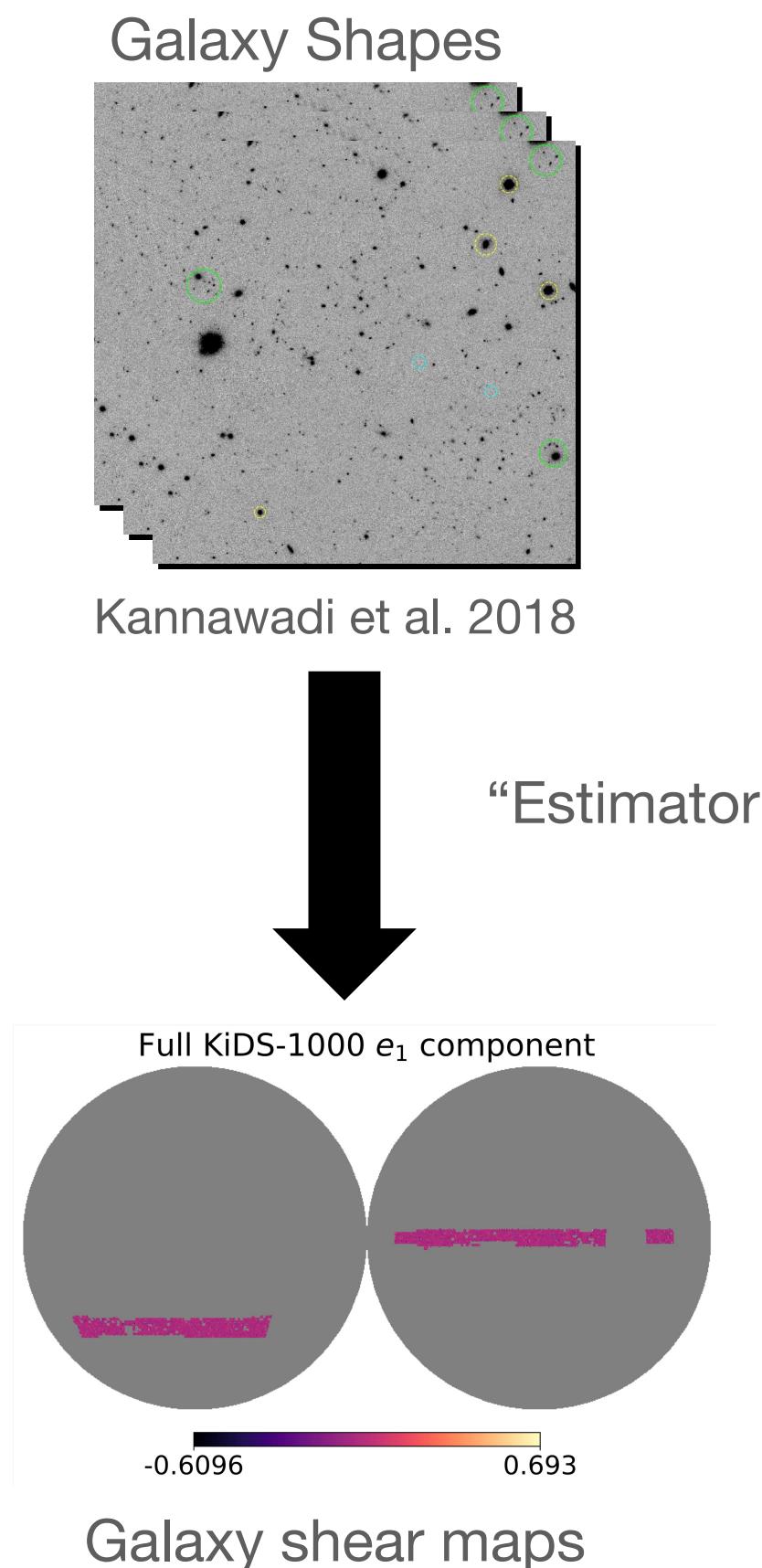
Estimator



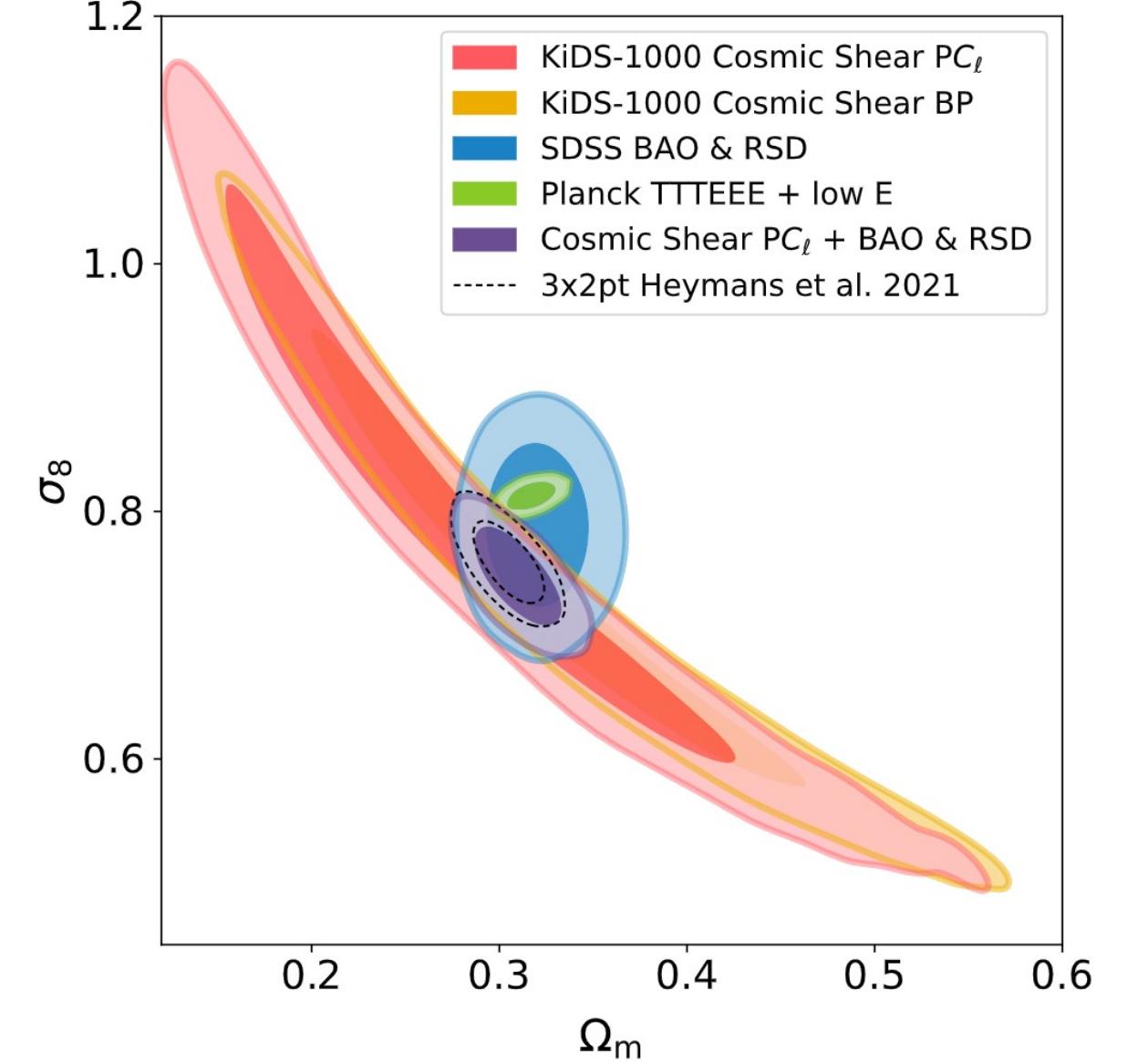
# “Vintage” Cosmology

## Ex: Weak Lensing Surveys

Loureiro et al. 2021 (2110.06947)



Bayesian Inference

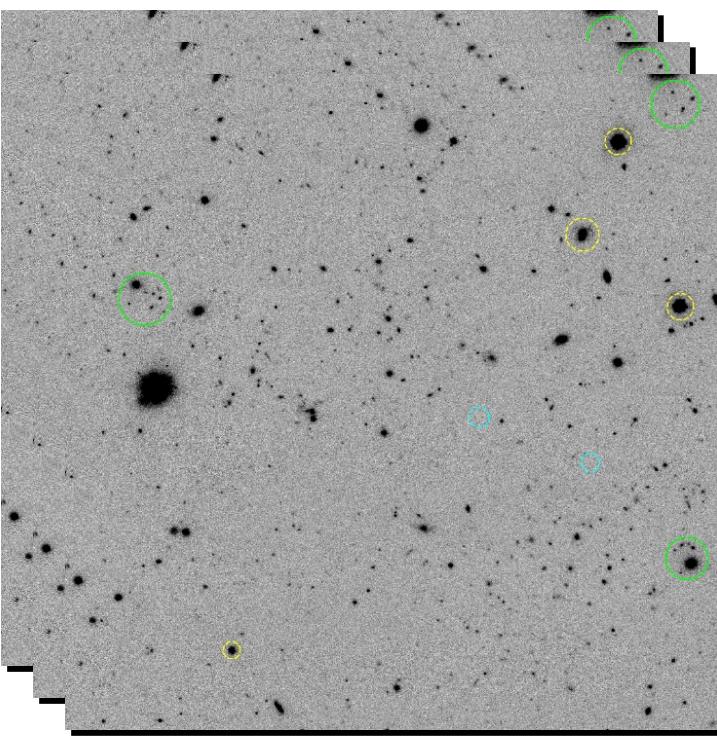


Cosmological Parameters

# Bayesian Hierarchical Cosmology

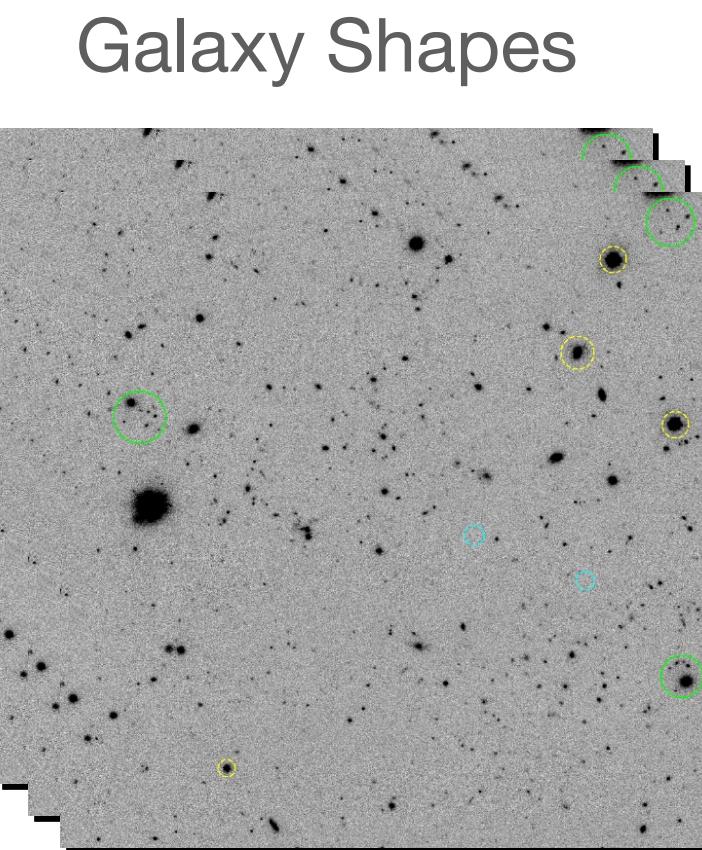
## Ex: Weak Lensing

Galaxy Shapes



# Bayesian Hierarchical Cosmology

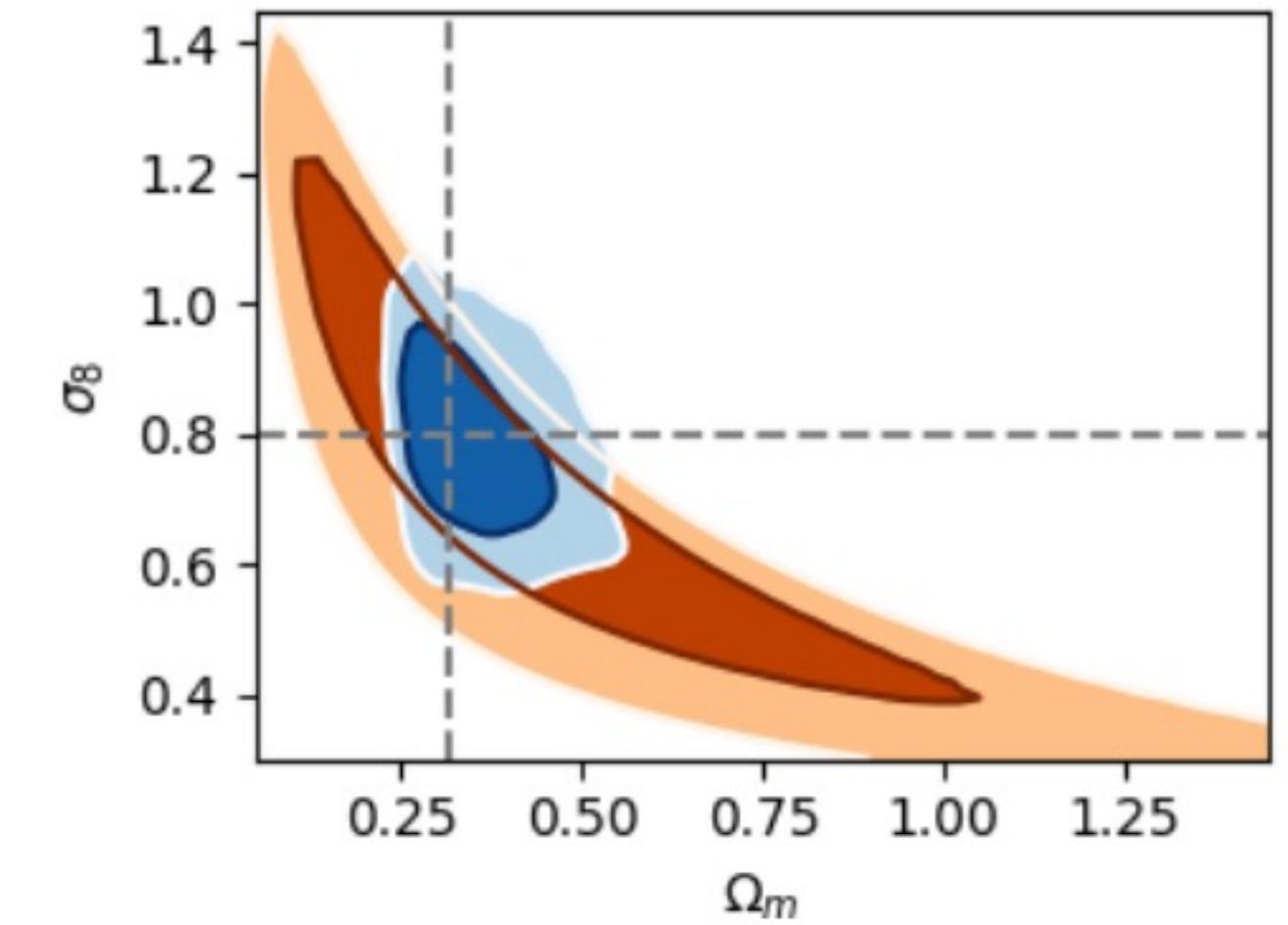
## Ex: Weak Lensing



Hierarchical  
Model



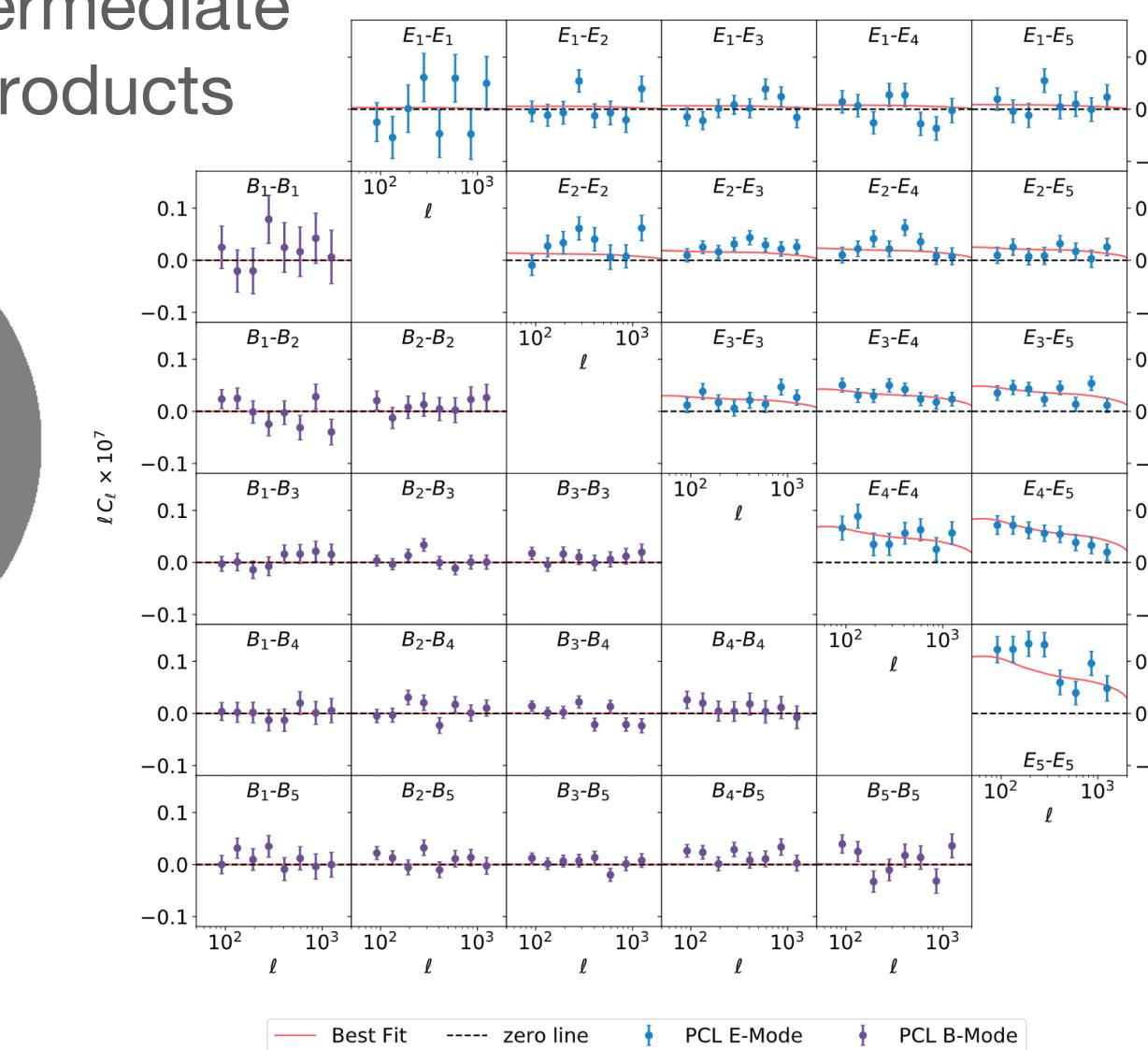
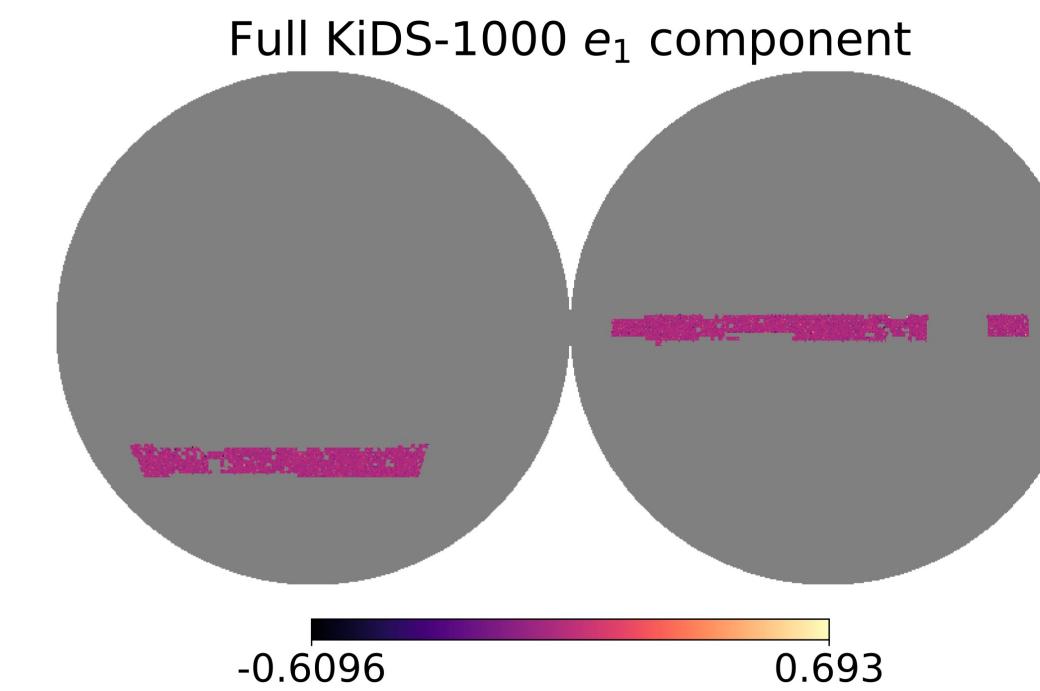
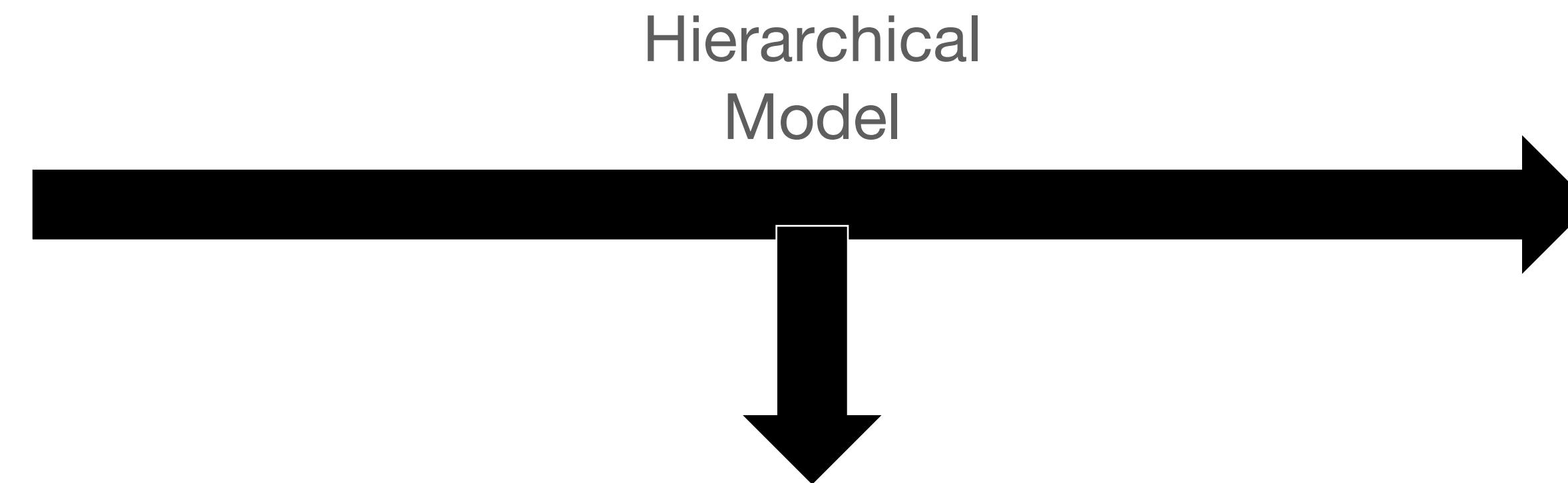
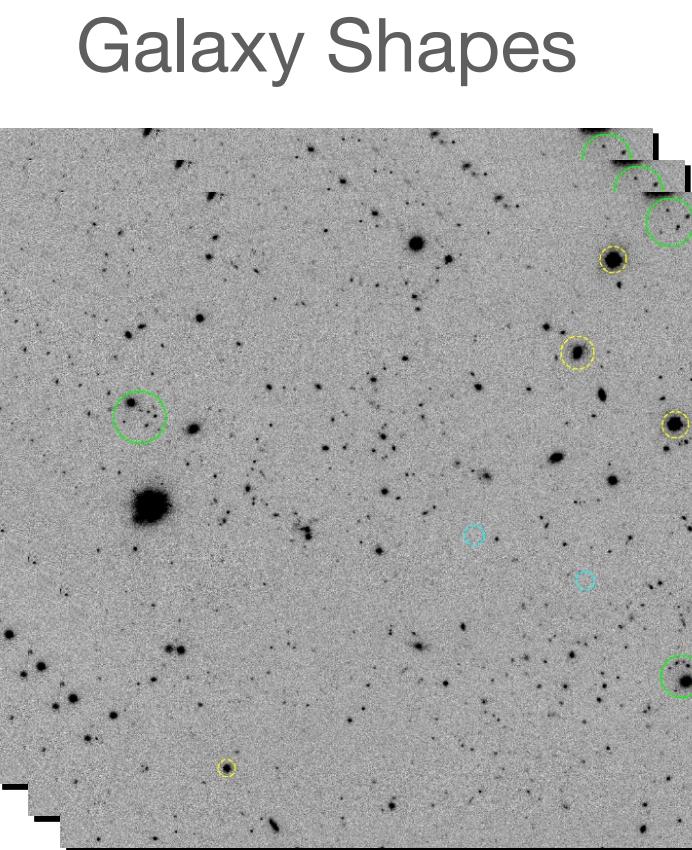
Porqueres et al. 2021(2108.04825)



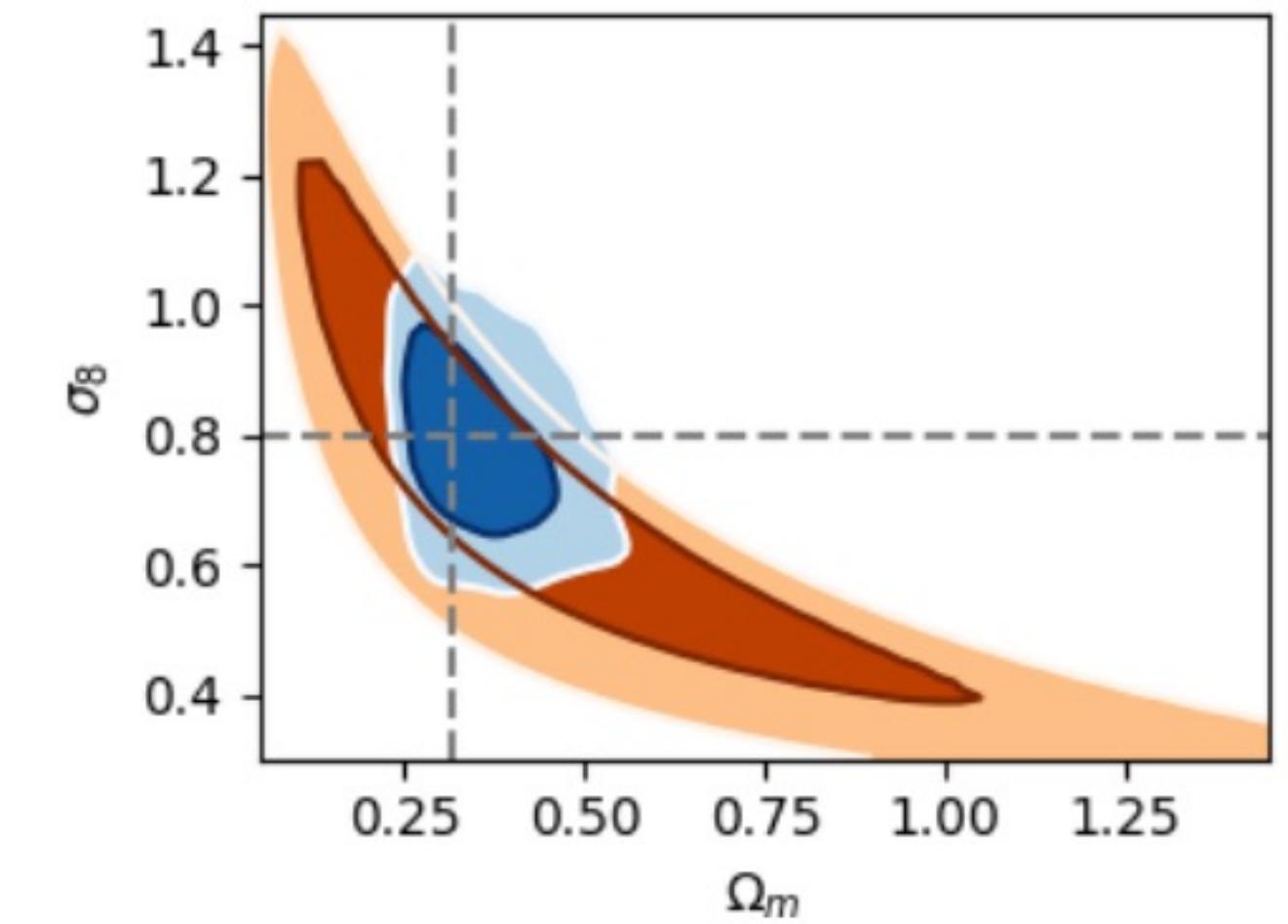
Cosmological Parameters

# Bayesian Hierarchical Cosmology

## Ex: Weak Lensing



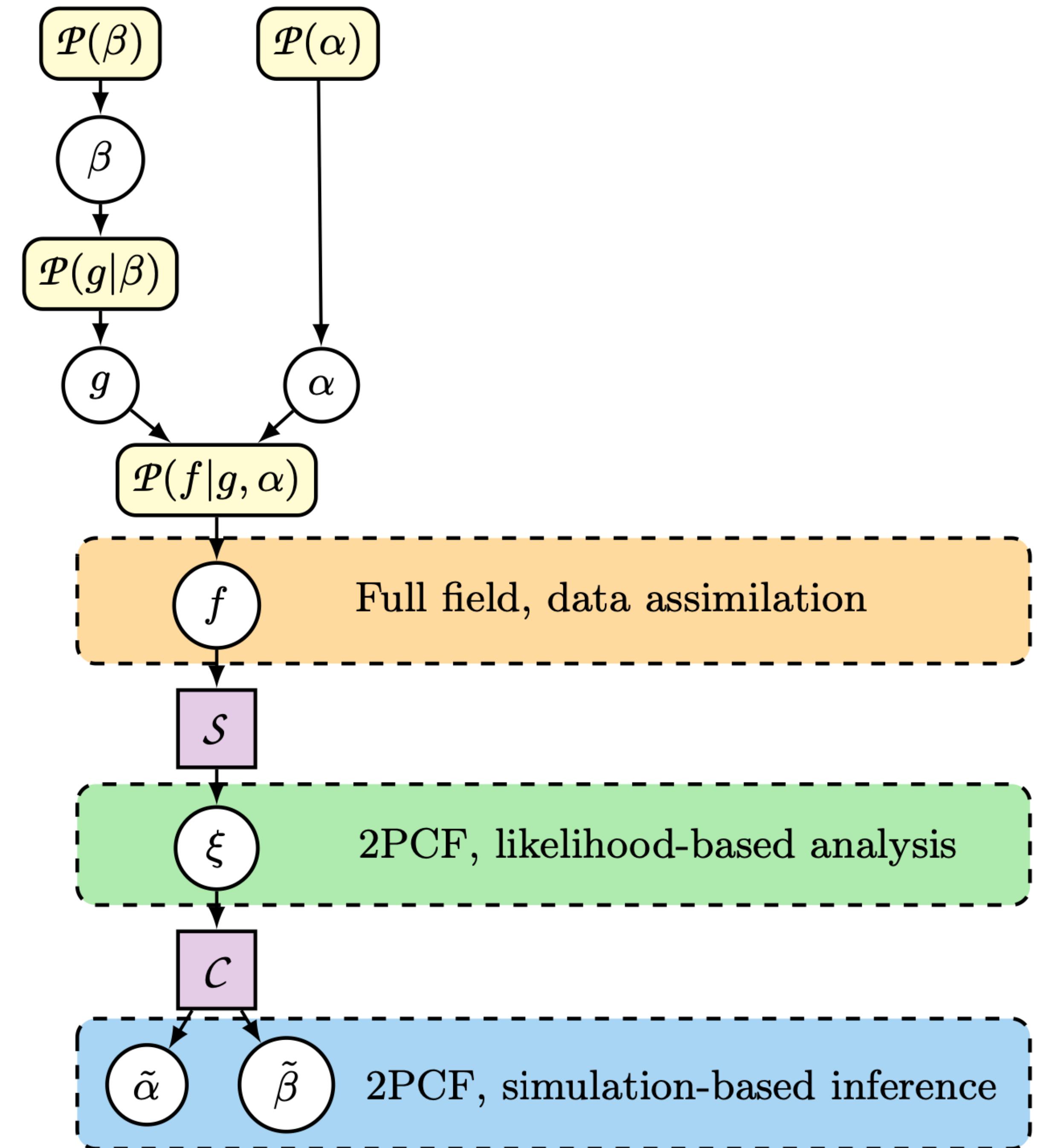
Porqueres et al. 2021(2108.04825)



Cosmological Parameters

# Field Level Inference Compared to other methods

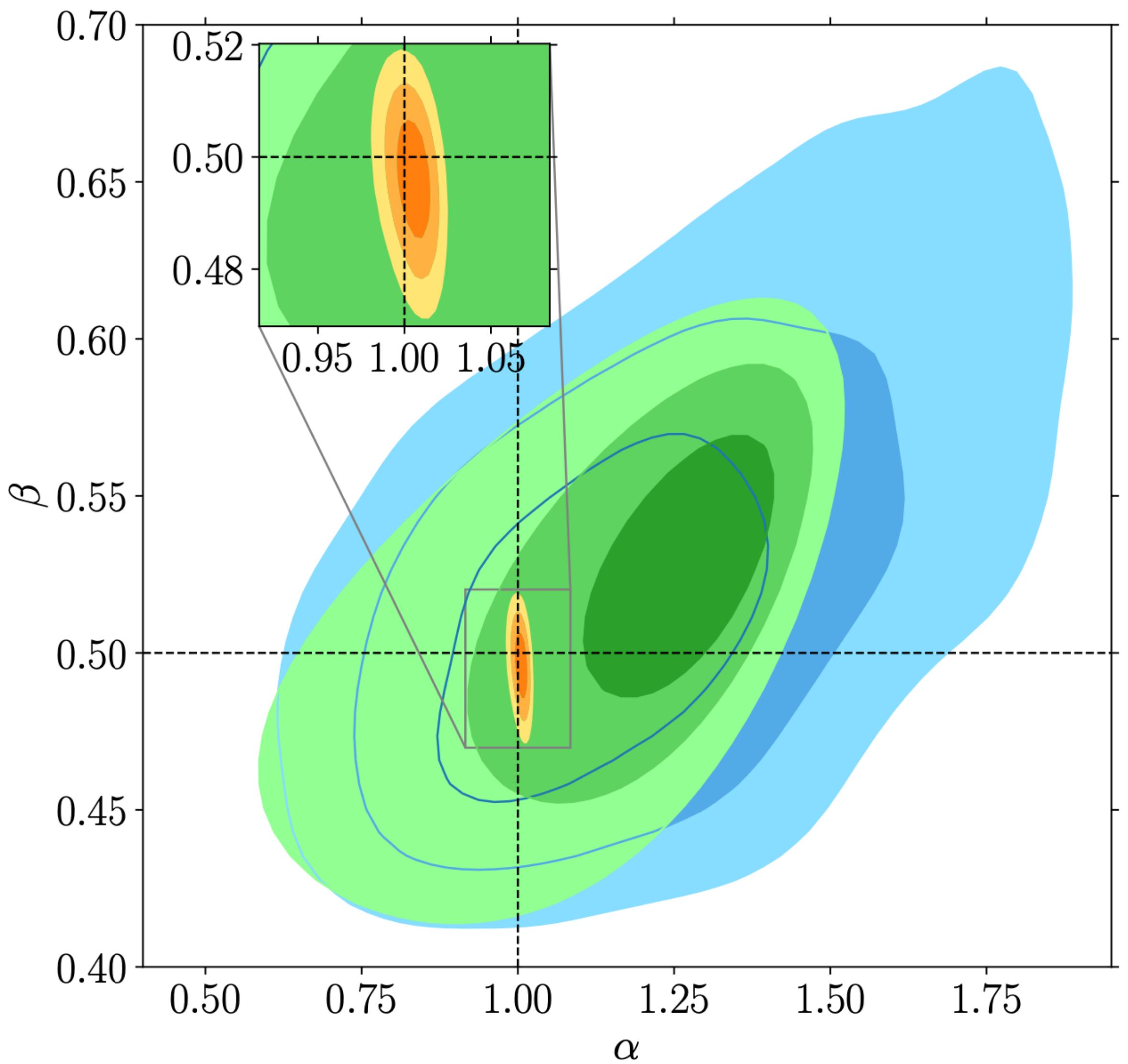
Leclercq & Heavens 2021 (2103.04158)



# Field Level Inference

## Compared to other methods

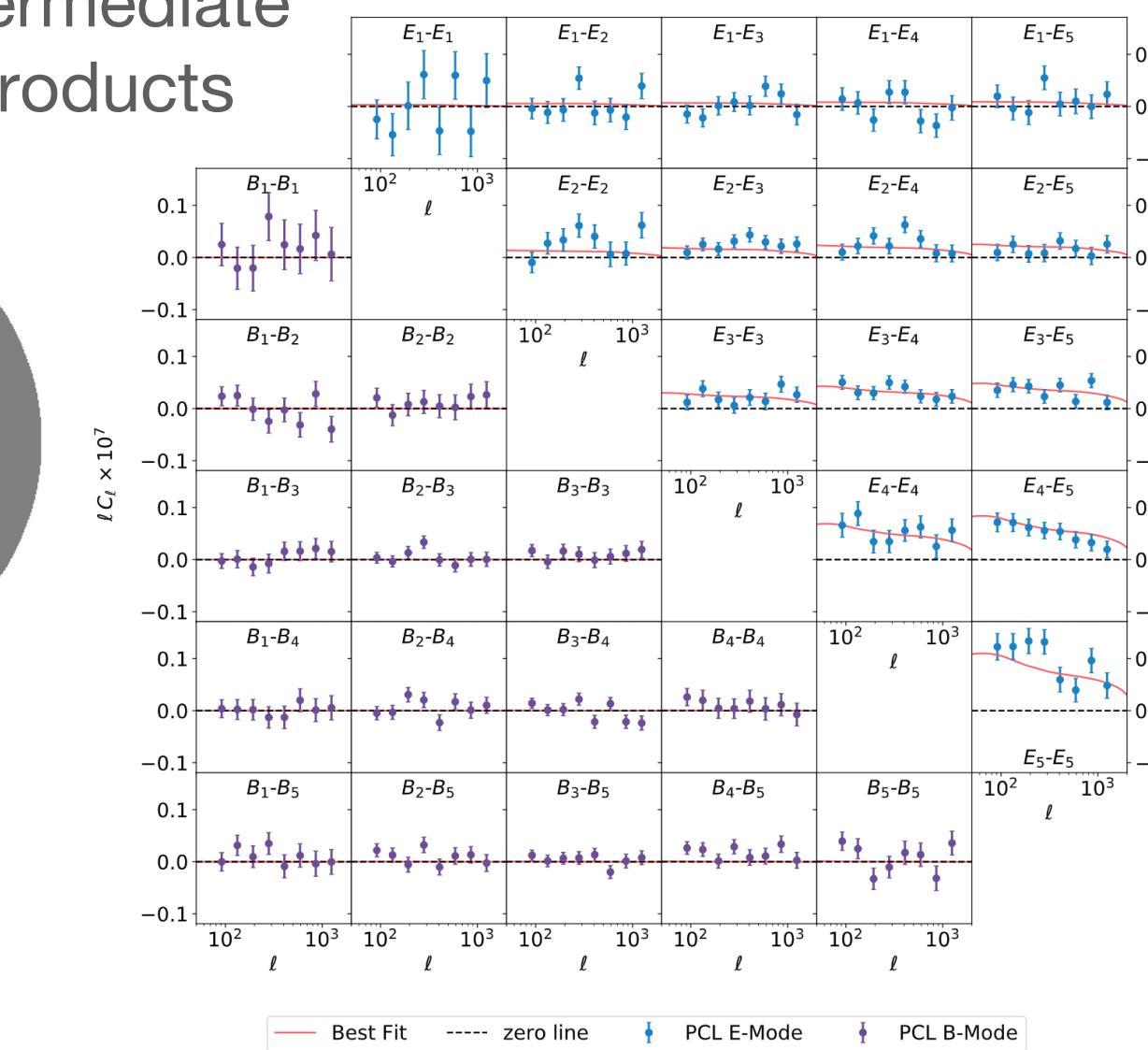
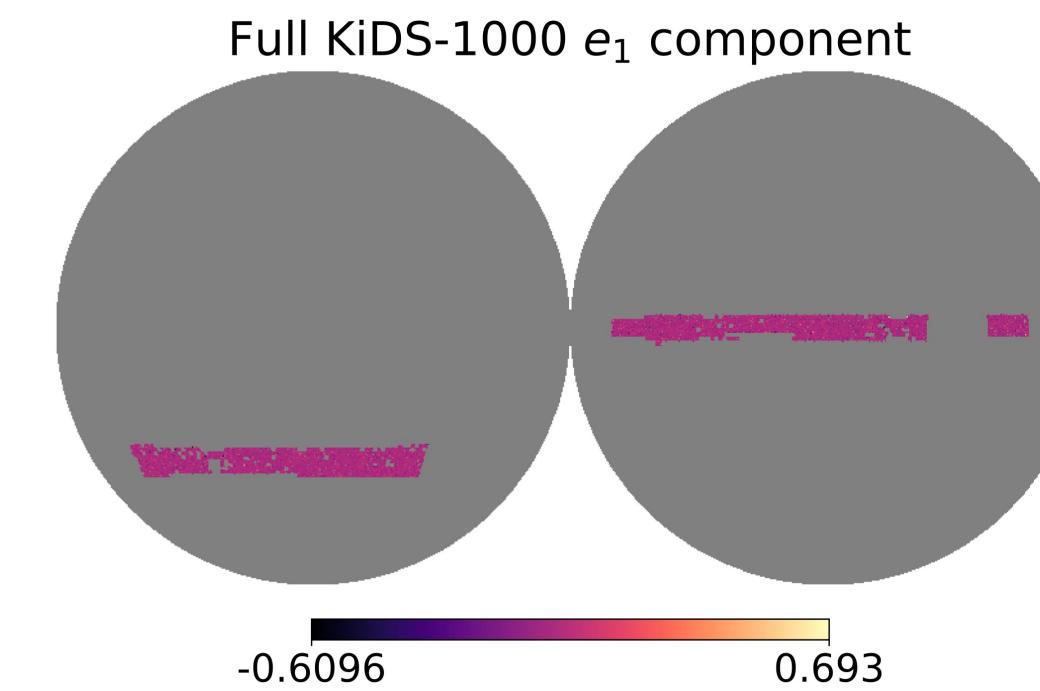
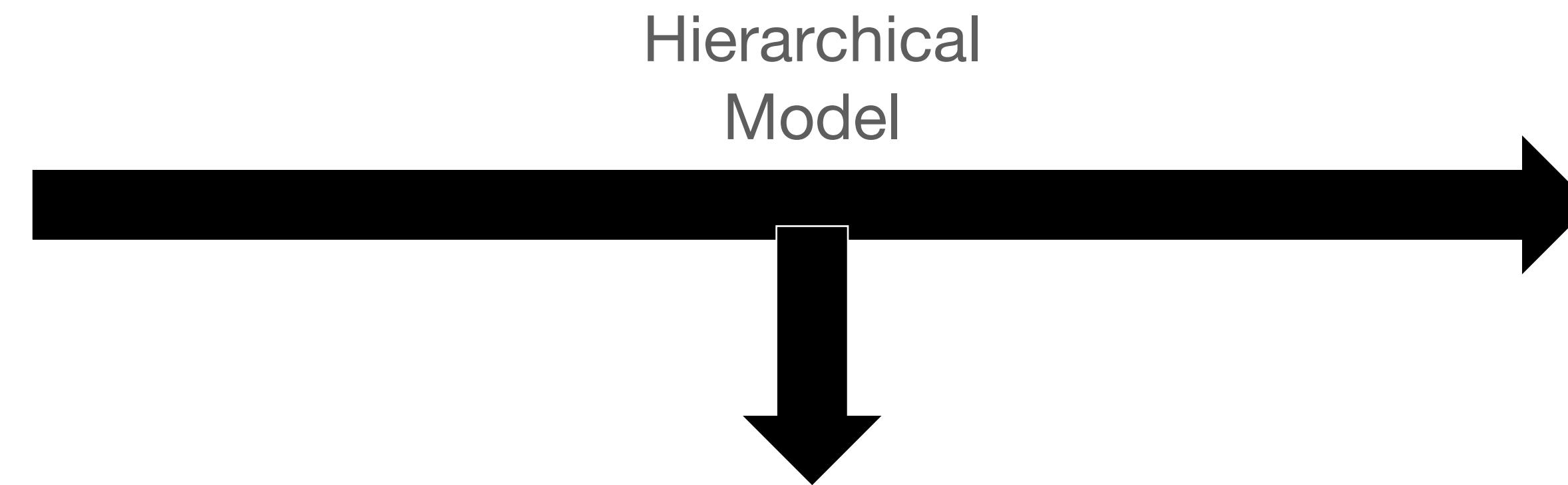
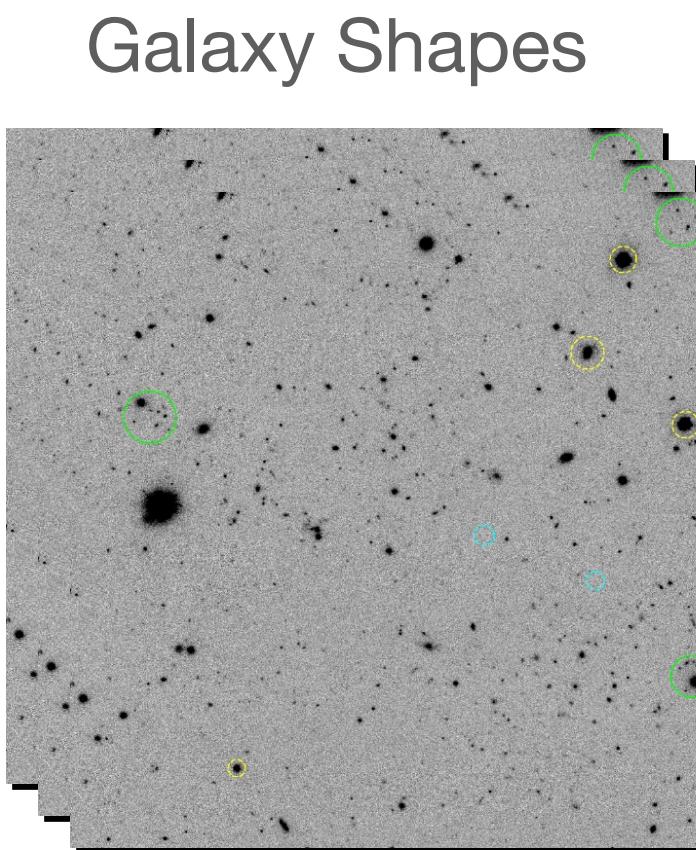
Leclercq & Heavens 2021 (2103.04158)



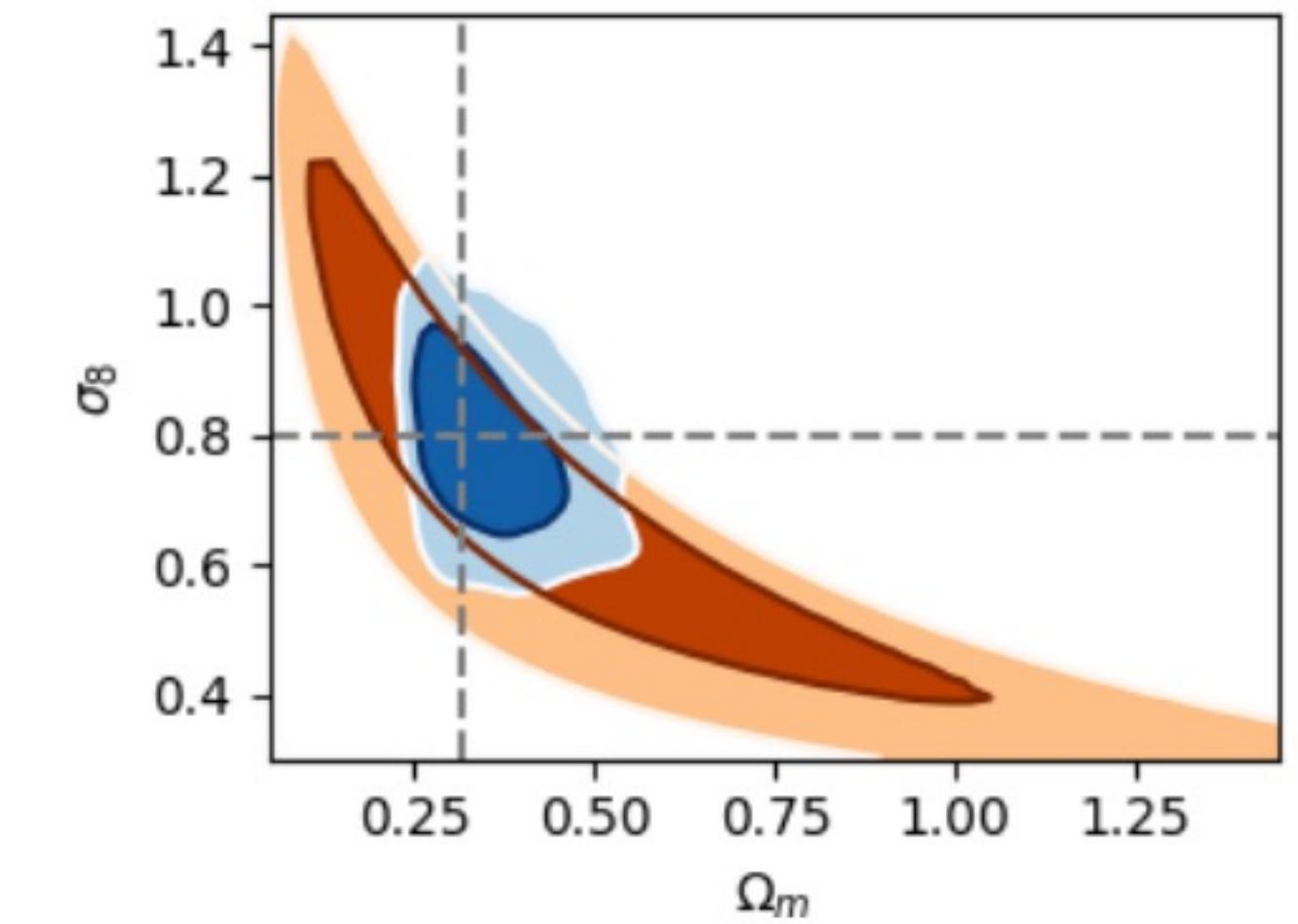
- 2PCF, likelihood-based analysis
- 2PCF, simulation-based inference ( $\varepsilon = 0.05$ )
- Full field, data assimilation

# Bayesian Hierarchical Cosmology

## Ex: Weak Lensing



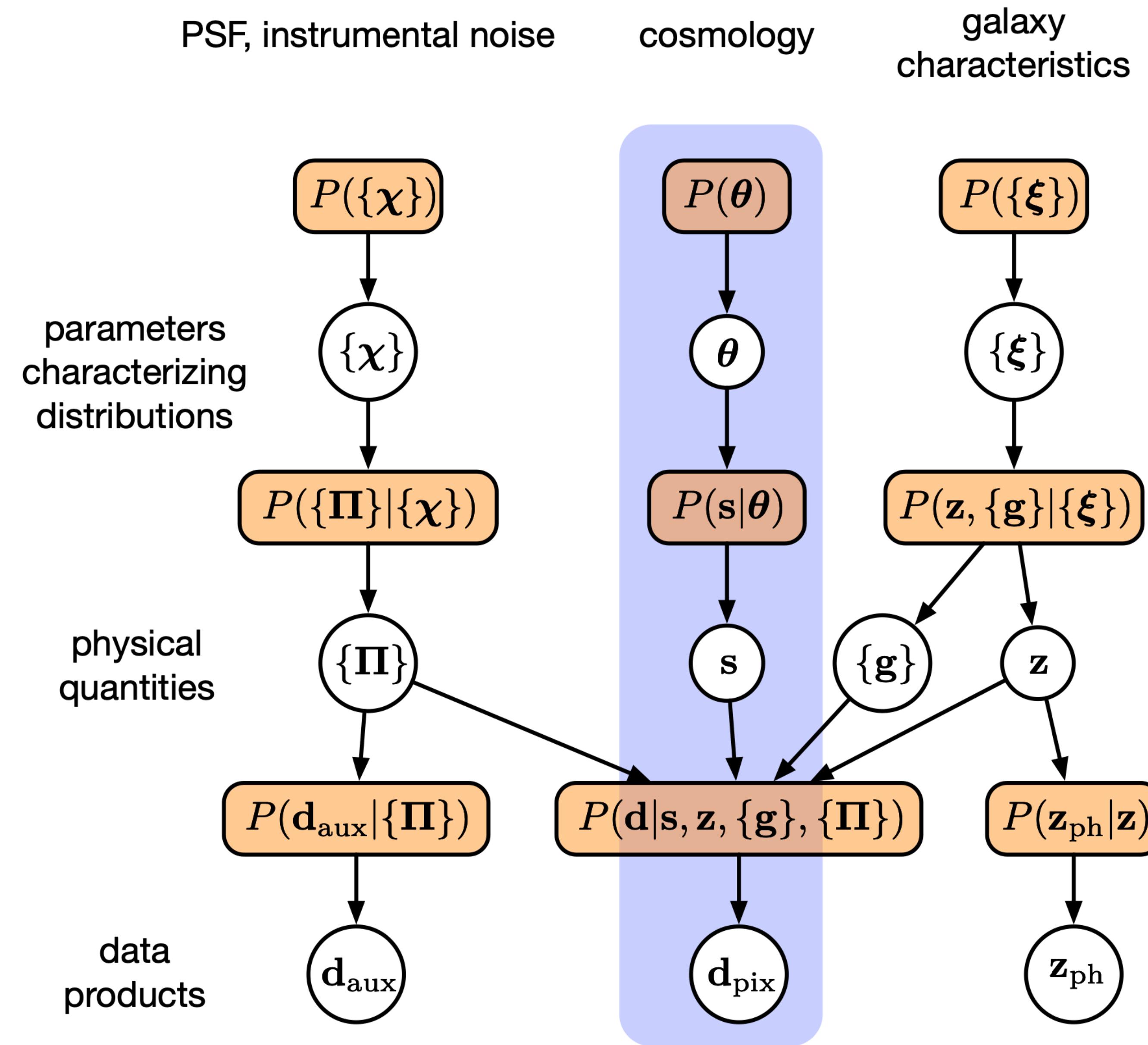
Porqueres et al. 2021(2108.04825)

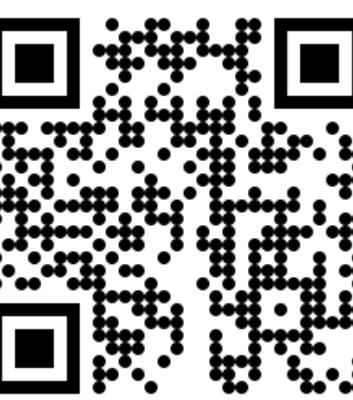


Cosmological Parameters

# Ideal Bayesian Hierarchical Model For Weak Lensing Analysis

Alsing et al. 2015 (1505.078400)





# **3. Almanac**

**Sampling full sky cosmological fields and their power spectra**

# Almanac

## Spin-0 and Spin-2 Cosmological Fields

An arbitrary spin-s field can be represented in the basis of spin-s spherical harmonics

$$f(\hat{n}) = \sum_{\ell m} f_{\ell m} {}_s Y_{\ell m}(\hat{n})$$

With

$$f_{\ell m} = \int d\Omega \ f(\hat{n}) {}_s Y_{\ell m}^*(\hat{n})$$

And covariance

$$C \equiv \langle f_{\ell m} f_{\ell' m'}^* \rangle \delta_{\ell \ell'} \delta_{mm'}$$

# Almanac

## Spin-0 and Spin-2 Cosmological Fields

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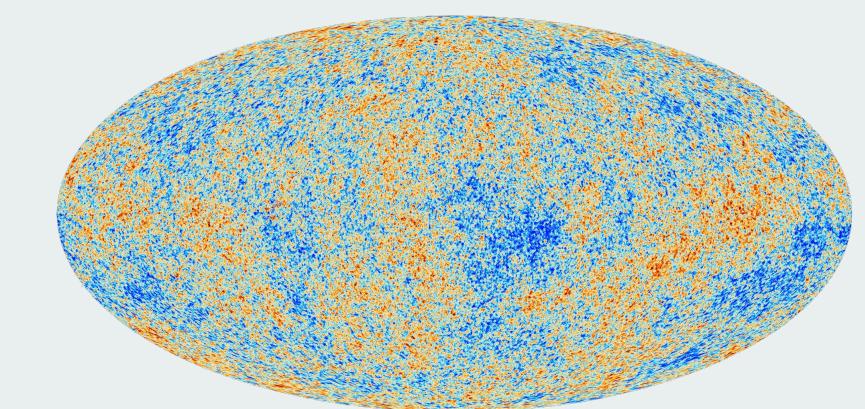
With

$$f_{\ell m} = \int d\Omega f(\hat{n}) {}_s Y_{\ell m}^*(\hat{n})$$

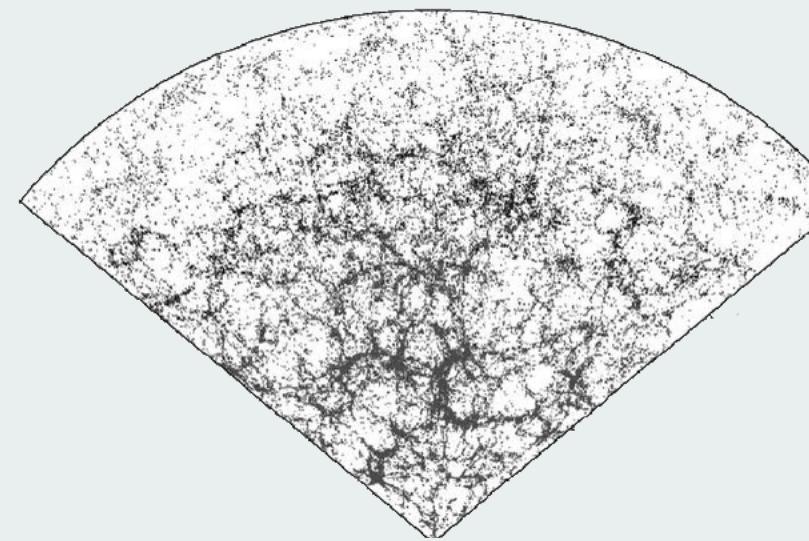
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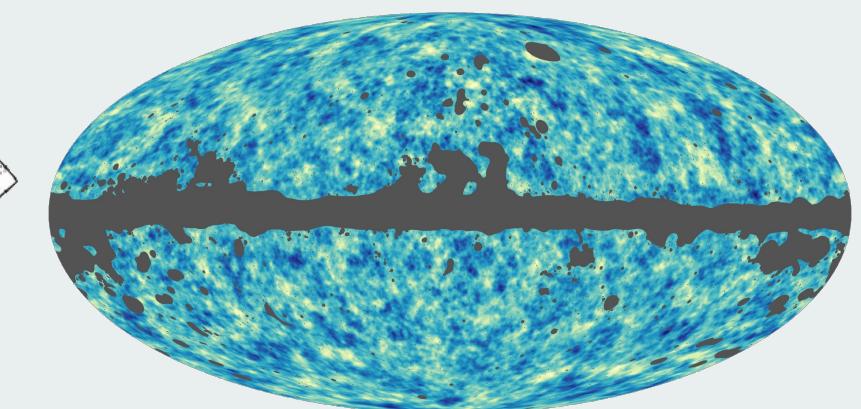
### Spin-0 Fields



CMB Temperature



Galaxy Clustering



Lensing Convergence

# Almanac

## Spin-0 and Spin-2 Cosmological Fields

An arbitrary spin-s field can be represented in the basis of spin-s spherical harmonics

$$f(\hat{n}) = \sum_{\ell m} f_{\ell m} {}_s Y_{\ell m}(\hat{n})$$

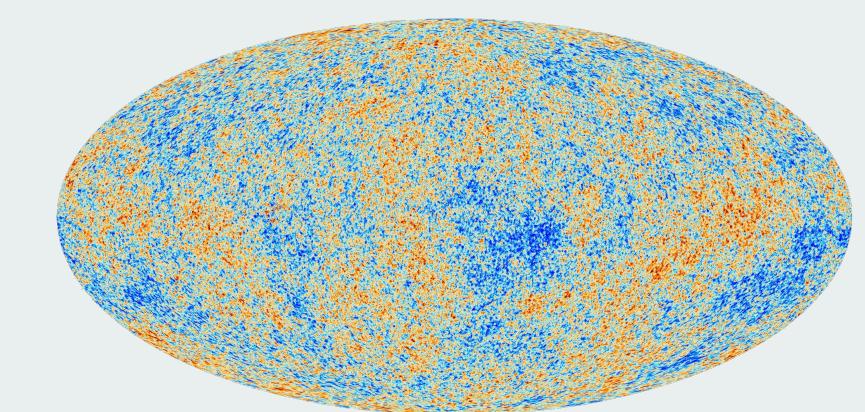
With

$$f_{\ell m} = \int d\Omega f(\hat{n}) {}_s Y_{\ell m}^*(\hat{n})$$

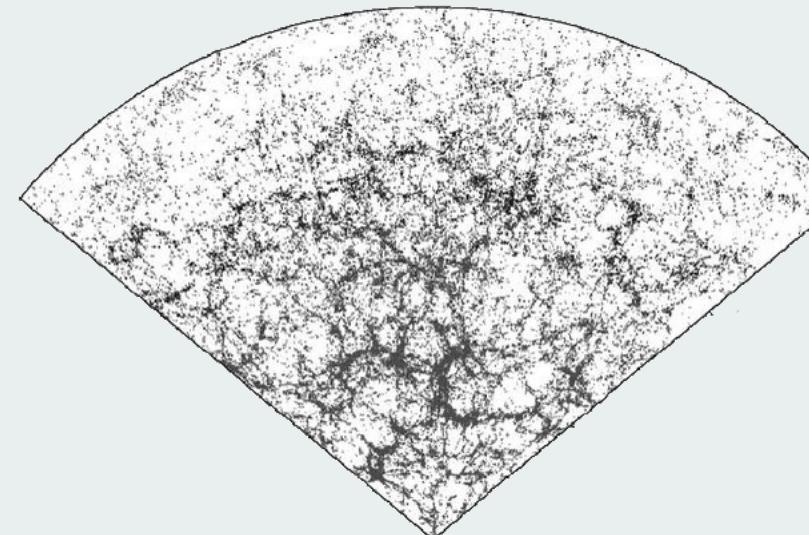
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$$C \equiv \langle f_{\ell m} f_{\ell' m'}^* \rangle \delta_{\ell \ell'} \delta_{mm'}$$

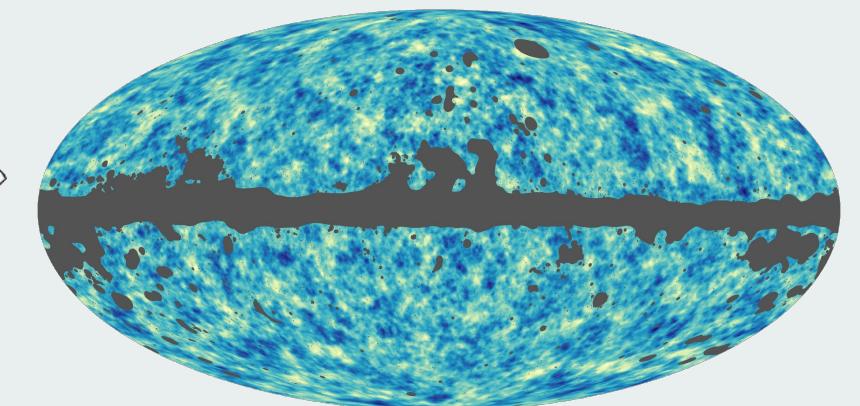
### Spin-0 Fields



CMB Temperature

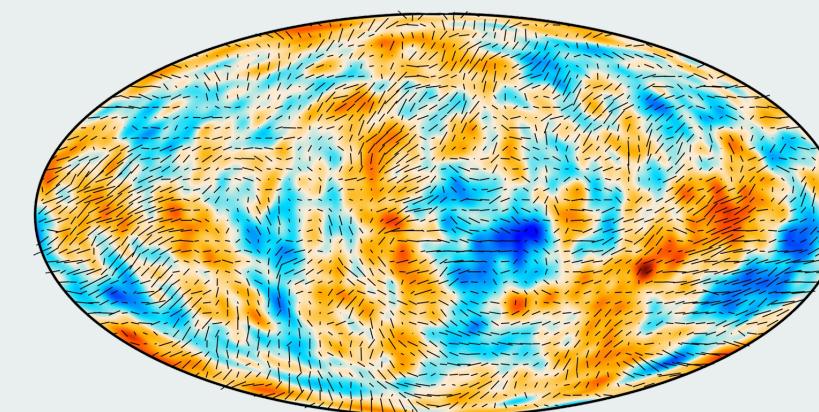


Galaxy Clustering

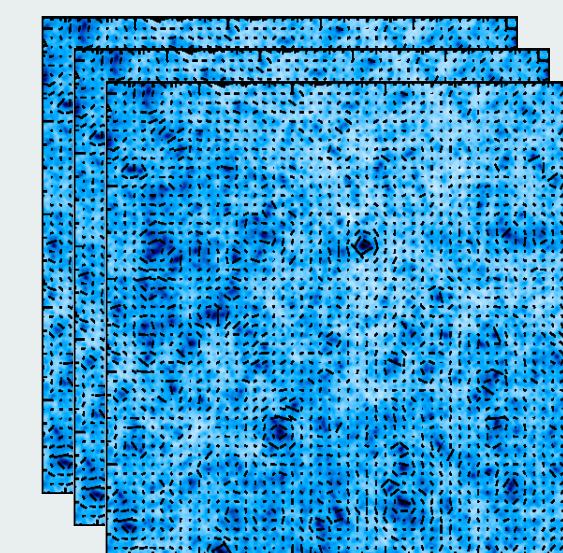


Lensing Convergence

### Spin-2 Fields



CMB Polarisation

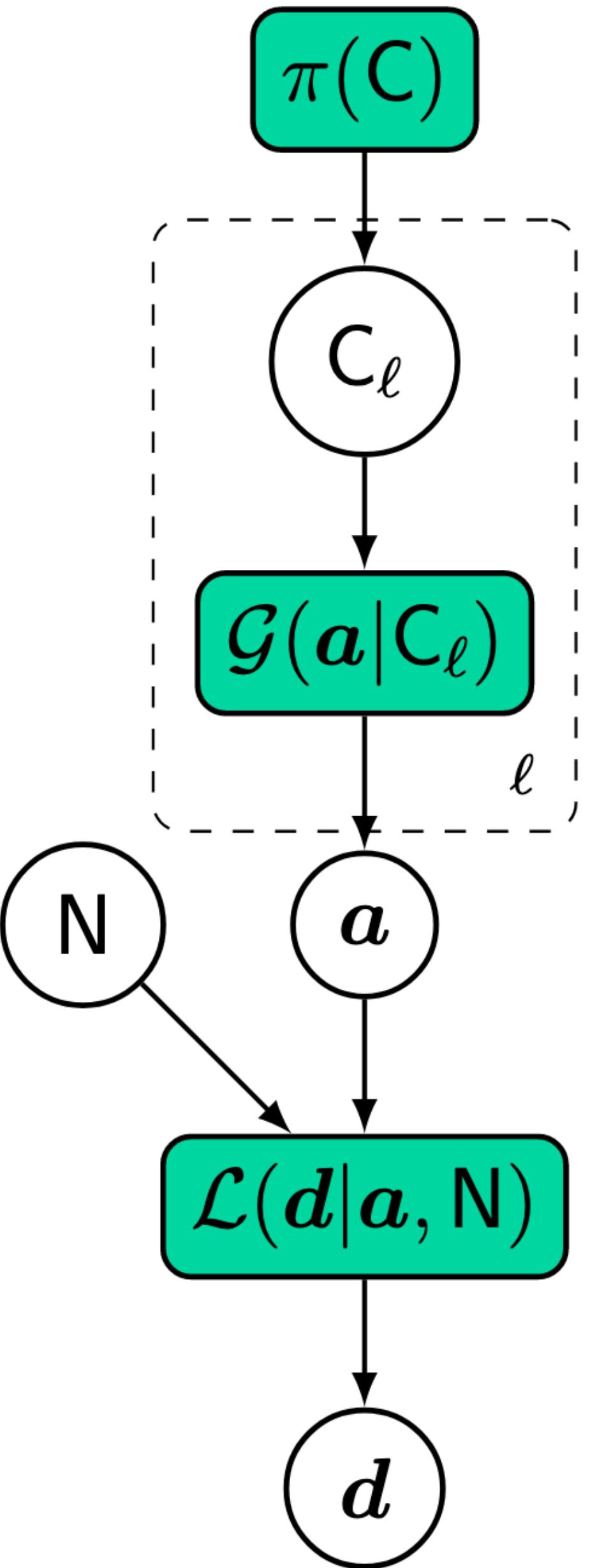


Cosmic Shear

# Almanac

Directed Acyclical  
Graph & posterior

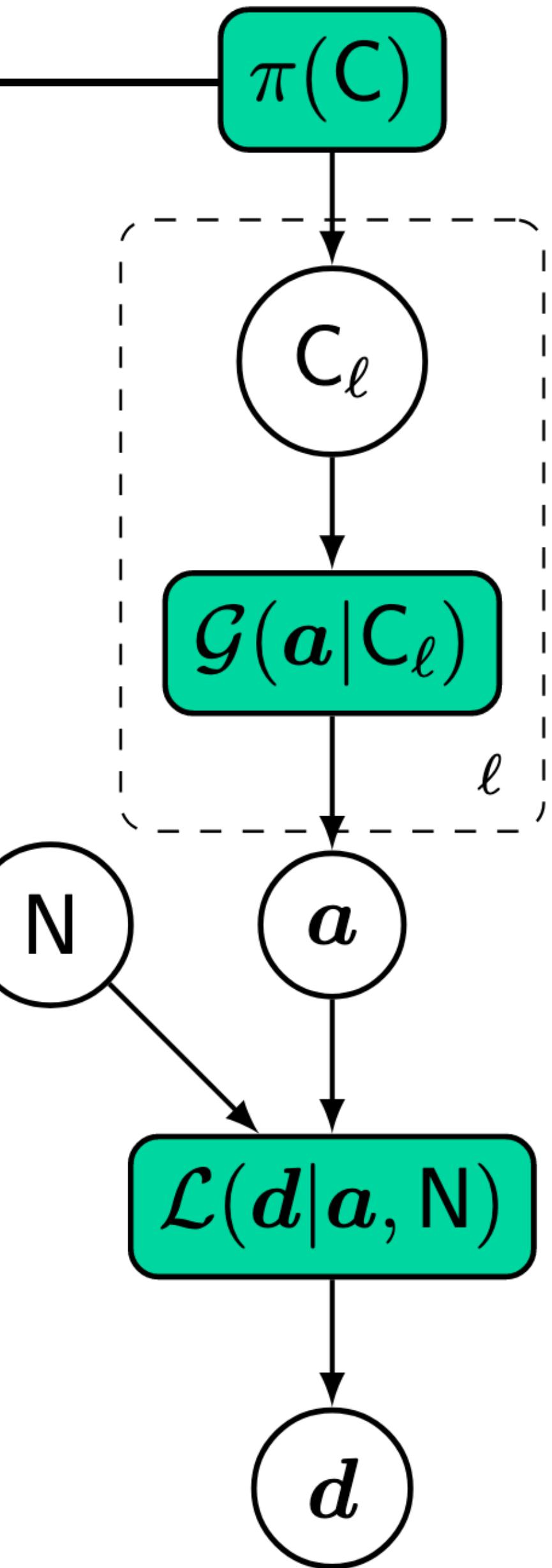
$$\mathcal{P}(C, a | d, N) \propto \mathcal{L}(d | a, N) \mathcal{G}(a | C) \pi(C)$$



# Almanac

Directed Acyclical  
Graph & posterior

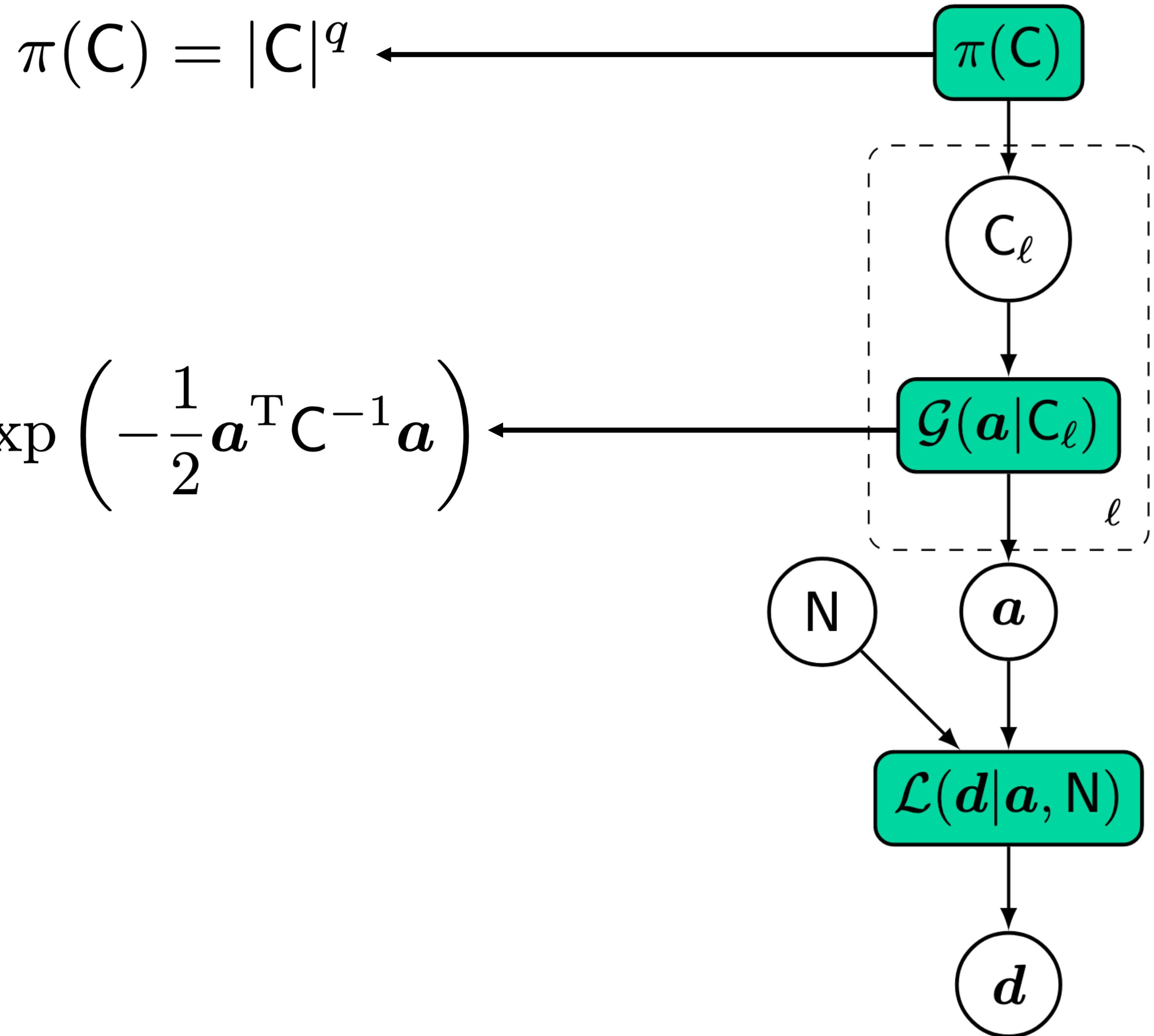
$$\pi(C) = |C|^q$$



# Almanac

Directed Acyclical  
Graph & posterior

$$\mathcal{G}(a|C) = \frac{1}{\sqrt{|2\pi C|}} \exp\left(-\frac{1}{2} a^T C^{-1} a\right)$$



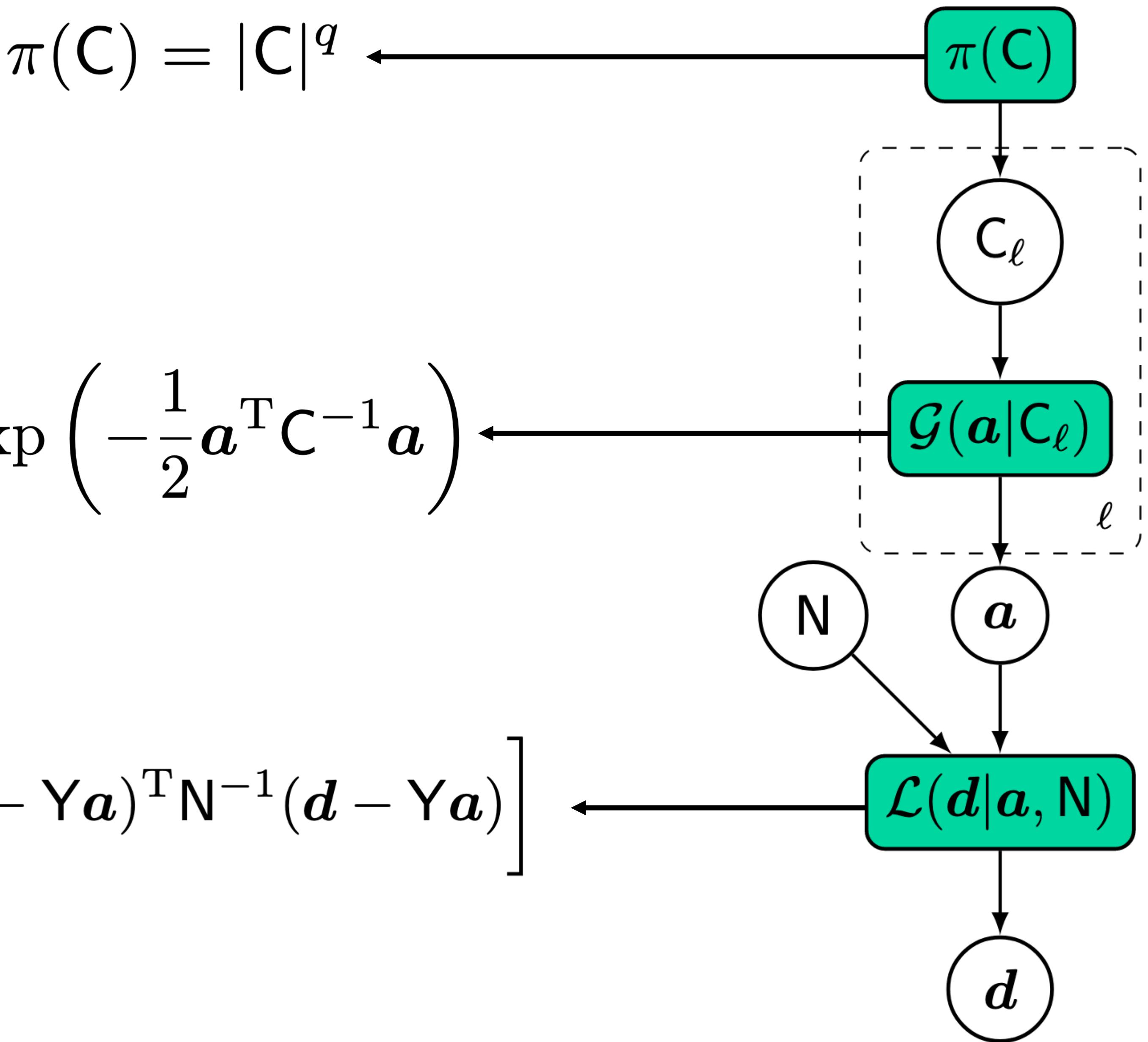
# Almanac

Directed Acyclical  
Graph & posterior

$$\pi(C) = |C|^q$$

$$g(a|C) = \frac{1}{\sqrt{|2\pi C|}} \exp\left(-\frac{1}{2} a^T C^{-1} a\right)$$

$$\mathcal{L}(d|a, N) \propto \exp\left[-\frac{1}{2}(d - Ya)^T N^{-1}(d - Ya)\right]$$



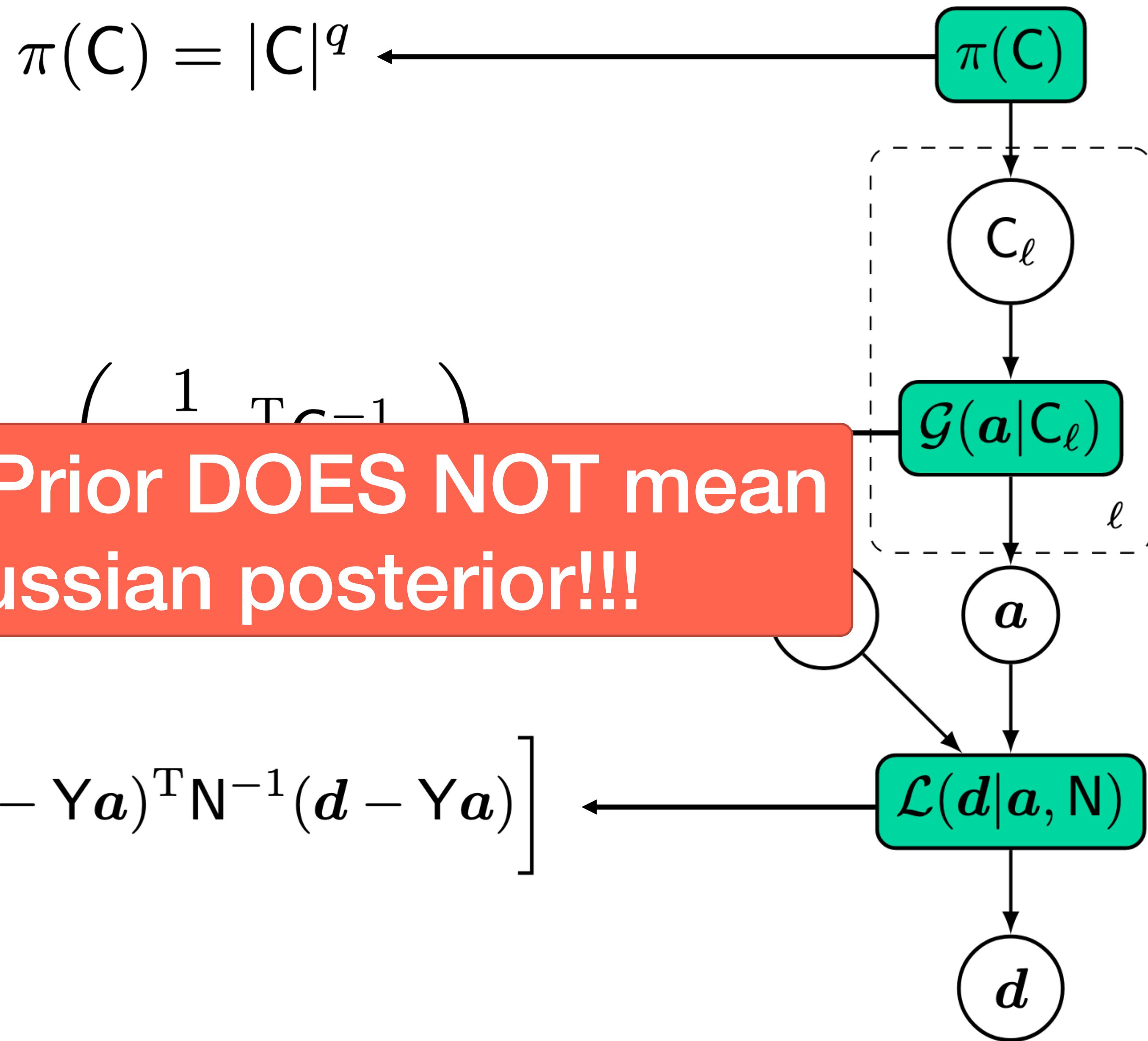
# Almanac

Directed Acyclical  
Graph & posterior

$$\mathcal{G}(a|C) = \frac{1}{\sqrt{\det(\Sigma_C)}} \exp\left(-\frac{1}{2} (a - \mu_C)^T \Sigma_C^{-1} (a - \mu_C)\right)$$

Gaussian Prior DOES NOT mean  
a Gaussian posterior!!!

$$\mathcal{L}(d|a, N) \propto \exp\left[-\frac{1}{2}(d - Ya)^T N^{-1}(d - Ya)\right]$$

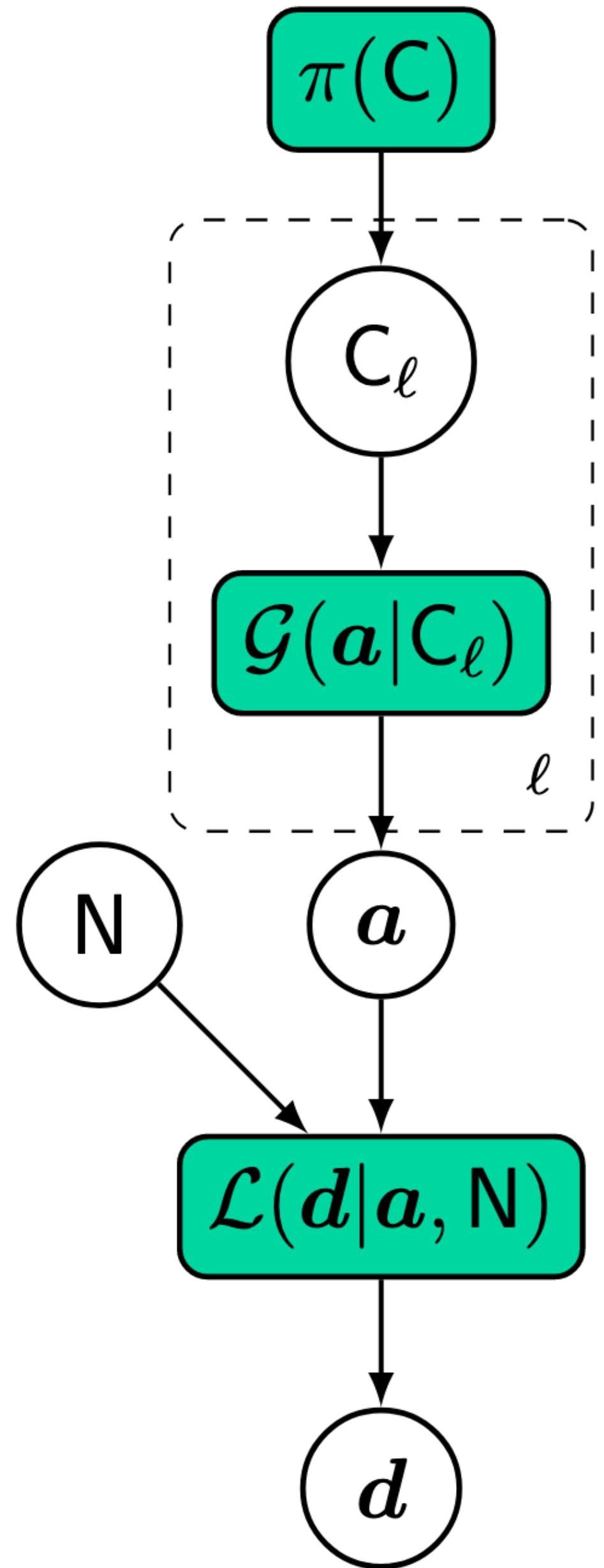


# Almanac

Directed Acyclical  
Graph & posterior

$$\mathcal{P}(C, a | d, N) \propto \mathcal{L}(d | a, N) \mathcal{G}(a | C) \pi(C)$$

$\sim 10^6 - 10^8$  parameters



# **4. Sampling High Dimensional Posteriors**

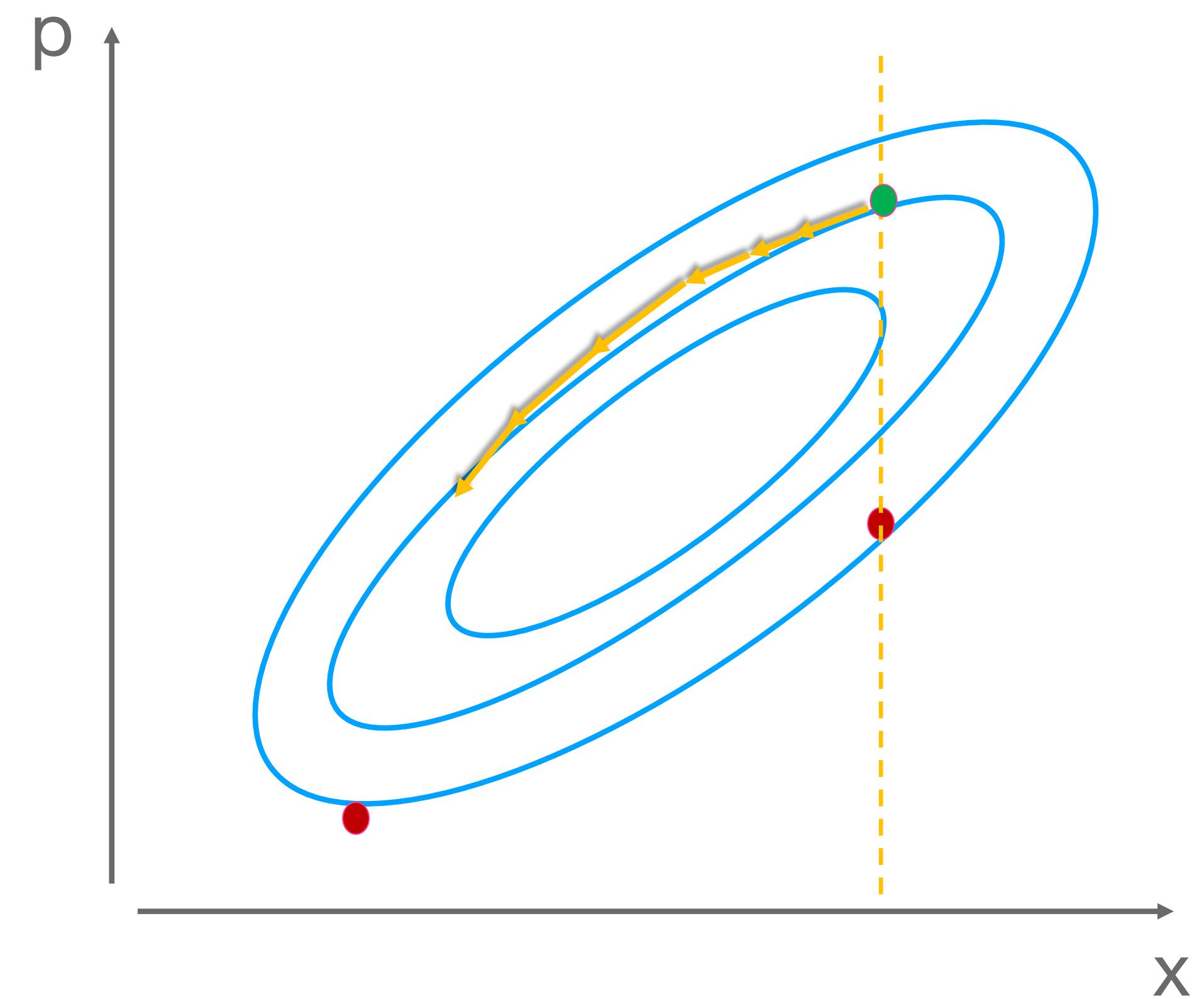
**Coordinate Transformations & the Tuned Hamiltonian Monte-Carlo**

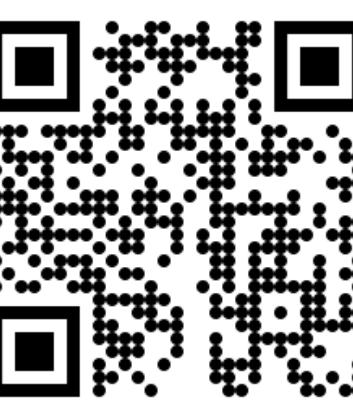
# Hamiltonian Monte Carlo

- Explores the phase space using an analogy with dynamical systems with our parameters being the positions

$$\mathcal{H} = \sum_i^N \frac{p_i^2}{2m_i} + \Psi(\mathbf{a}, \mathbf{C}_\ell)$$

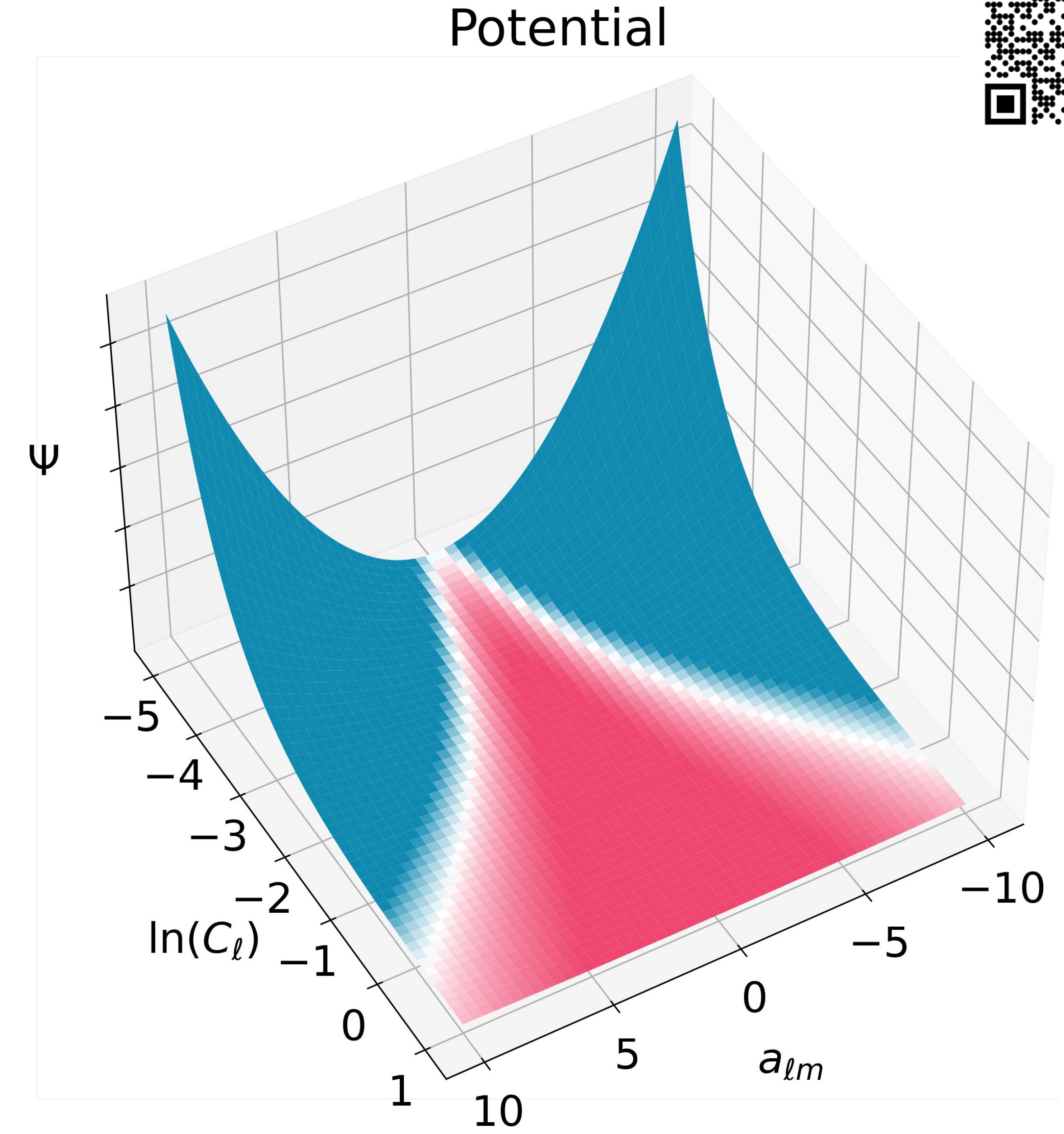
- The potential is related to the posterior:
$$\Psi(\mathbf{a}, \mathbf{C}_\ell) = -\ln p(\mathbf{a}, \mathbf{C}_\ell | \mathbf{d}, \mathbf{N})$$
- Evolves as a dynamical system with the momenta marginalized over

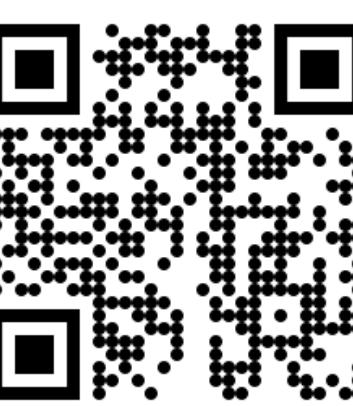




# The sting-ray problem

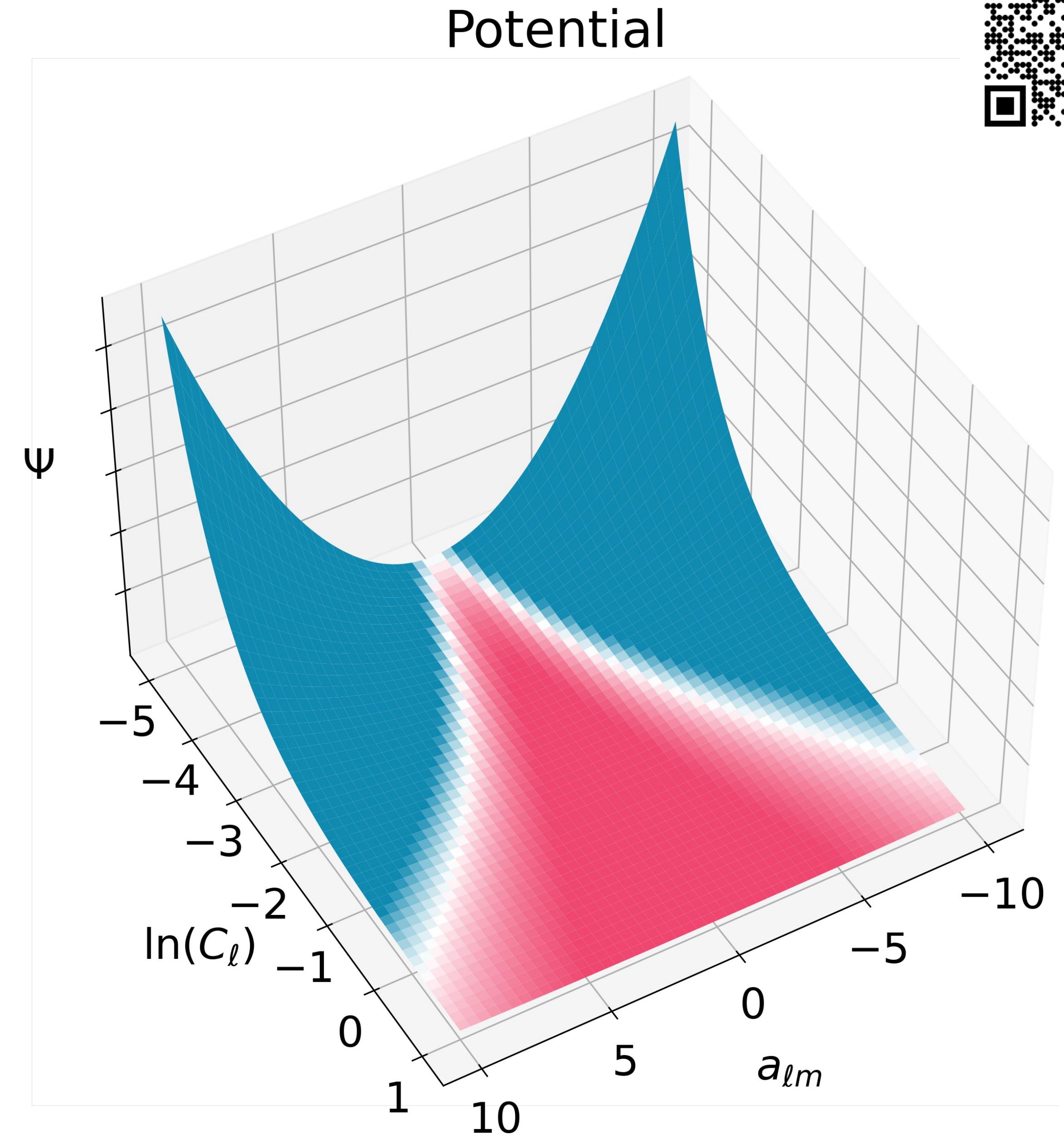
- The C matrix needs to be positive definite

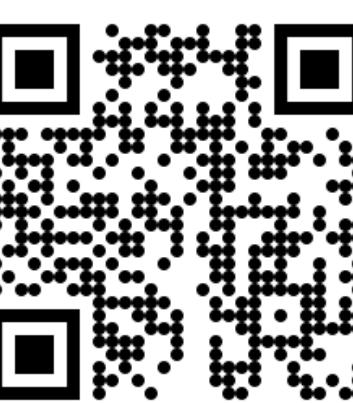




# The sting-ray problem

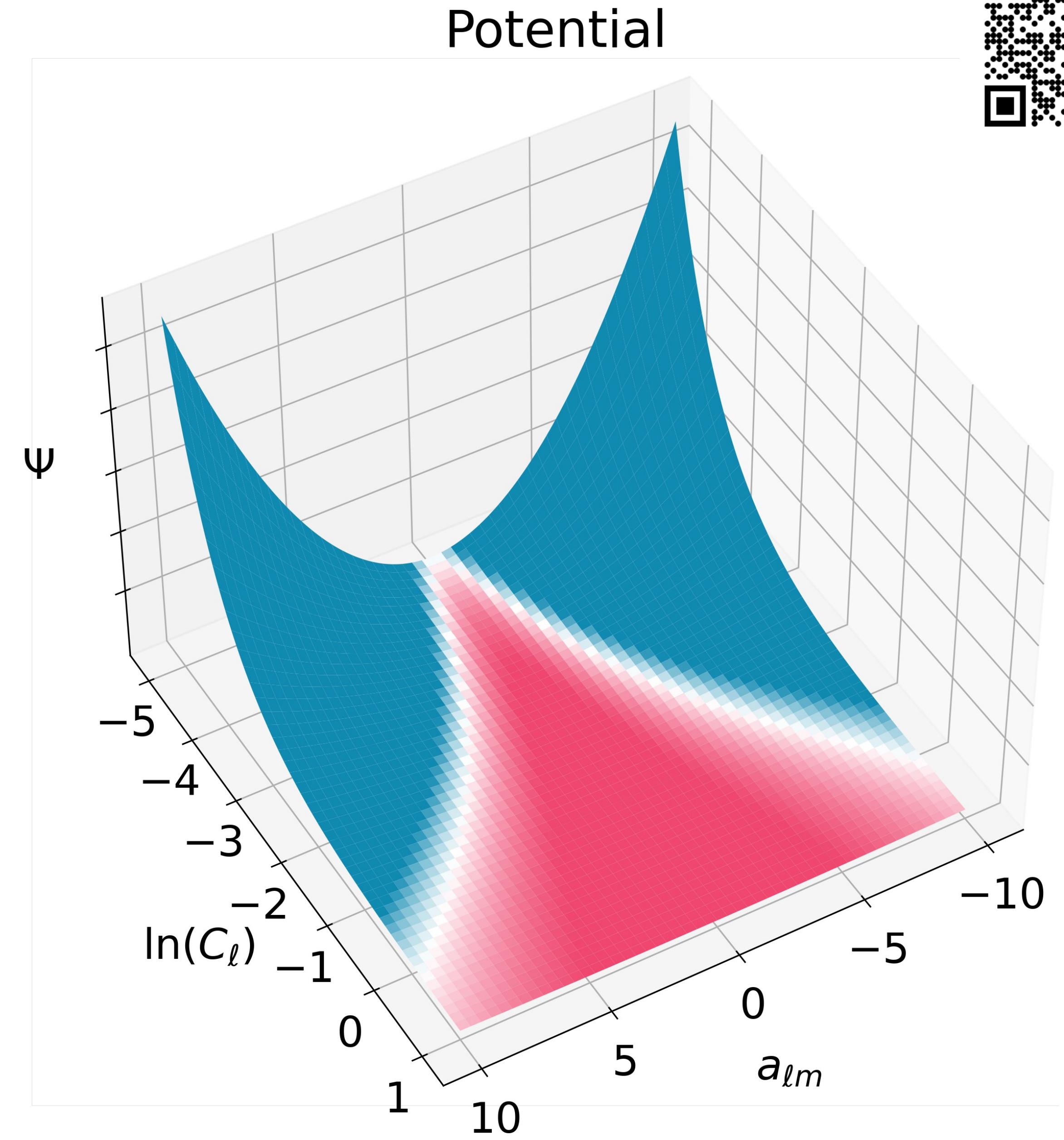
- The C matrix needs to be positive definite
- The most straightforward coordinate system to ensure this is using  $\mathbf{a}$  and  $\mathbf{G} = \ln(\mathbf{C})$ .

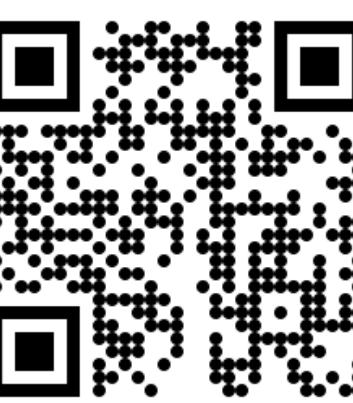




# The sting-ray problem

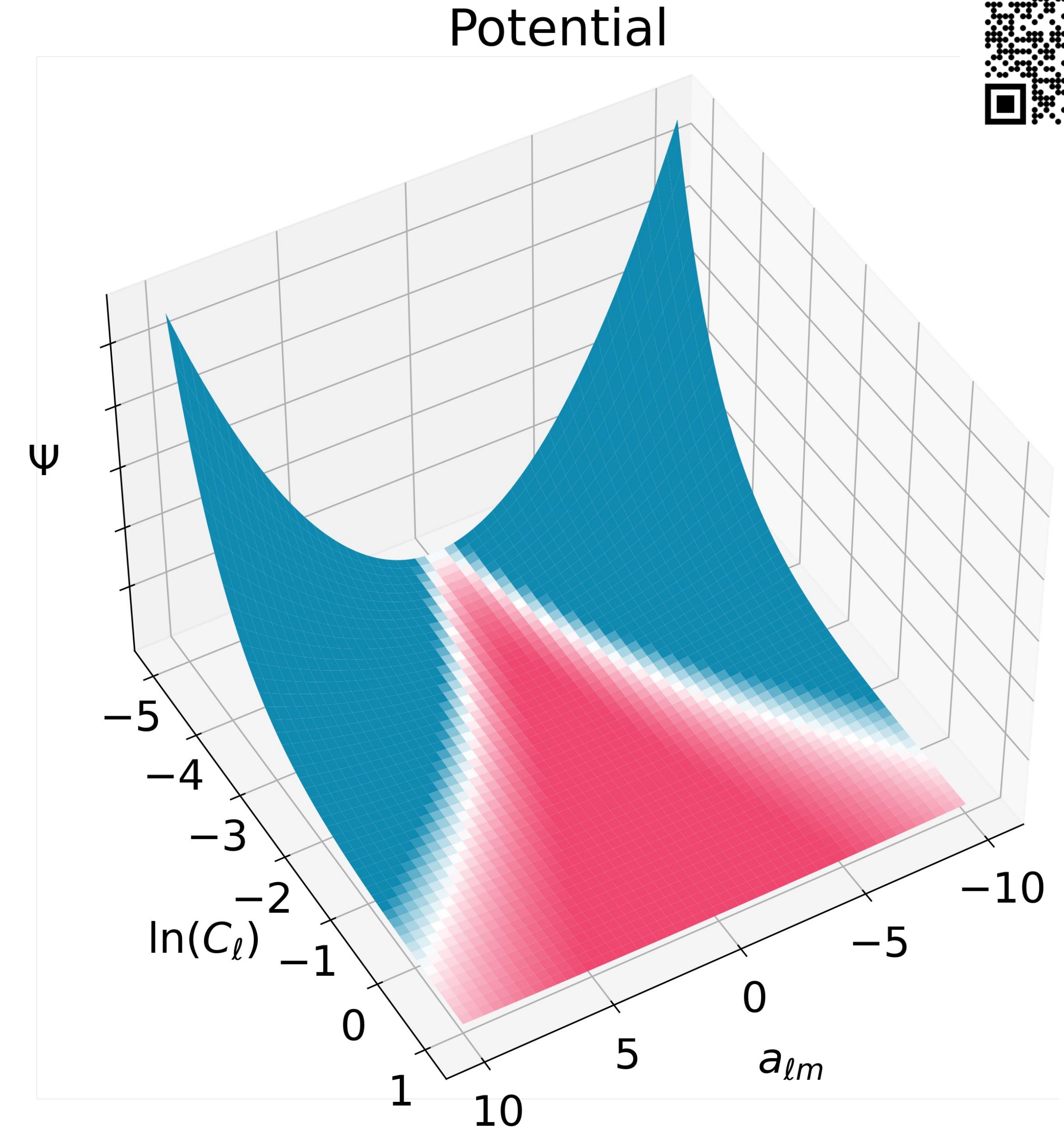
- The C matrix needs to be positive definite
- The most straightforward coordinate system to ensure this is using  $\mathbf{a}$  and  $\mathbf{G} = \ln(\mathbf{C})$ .
- However, we fall into the Sting-Ray (Neil's Funnel) posterior problem

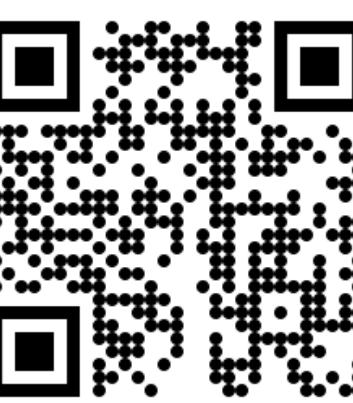




# The sting-ray problem

- The C matrix needs to be positive definite
- The most straightforward coordinate system to ensure this is using  $\mathbf{a}$  and  $\mathbf{G} = \ln(\mathbf{C})$ .
- However, we fall into the Sting-Ray (Neil's Funnel) posterior problem
- Sampler becomes inefficient





# The sting-ray problem: SOLVED

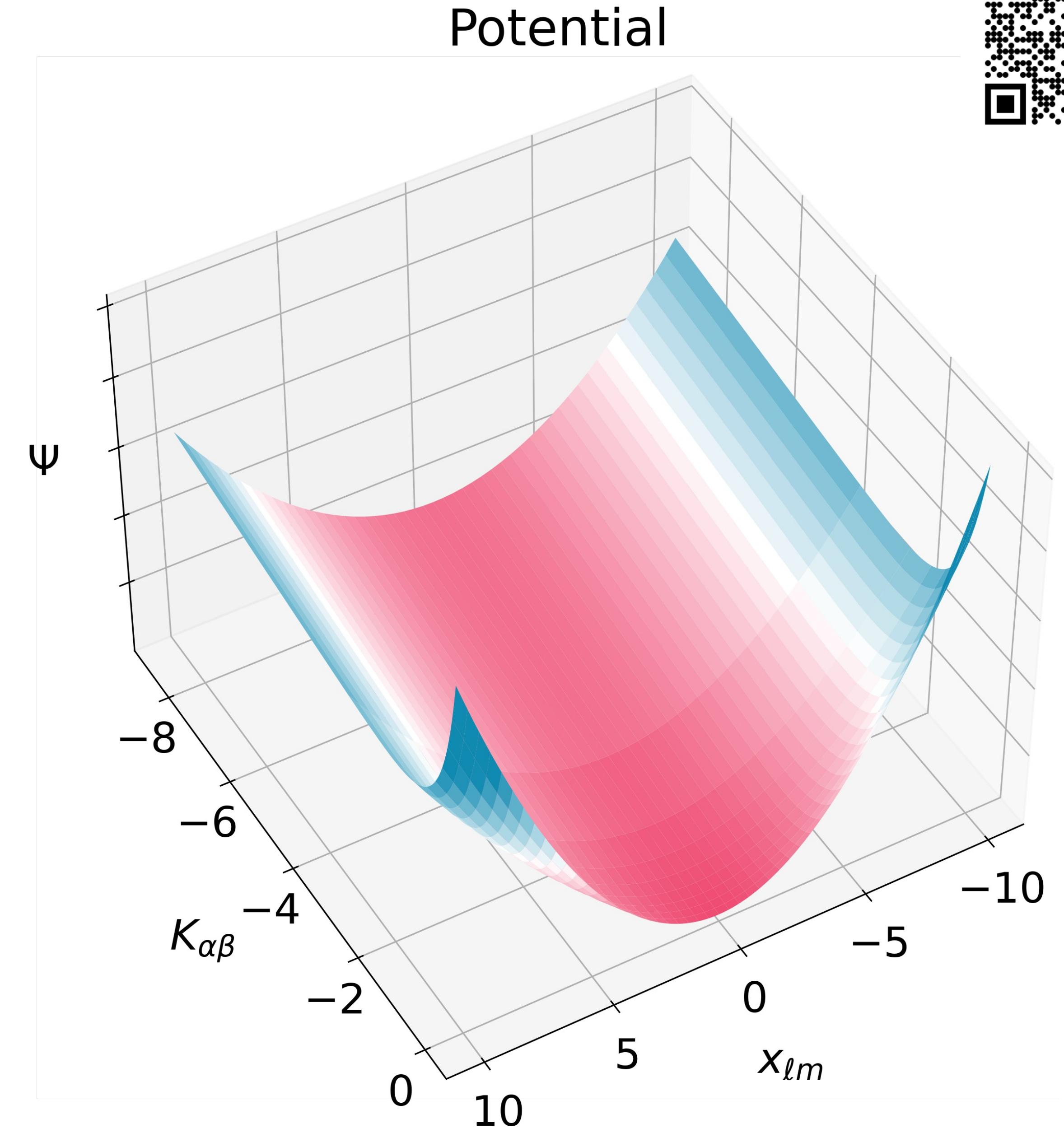
- Rescaling the fields by their standard deviation

$$\mathbf{x} = \mathbf{L}^{-1} \mathbf{a}$$

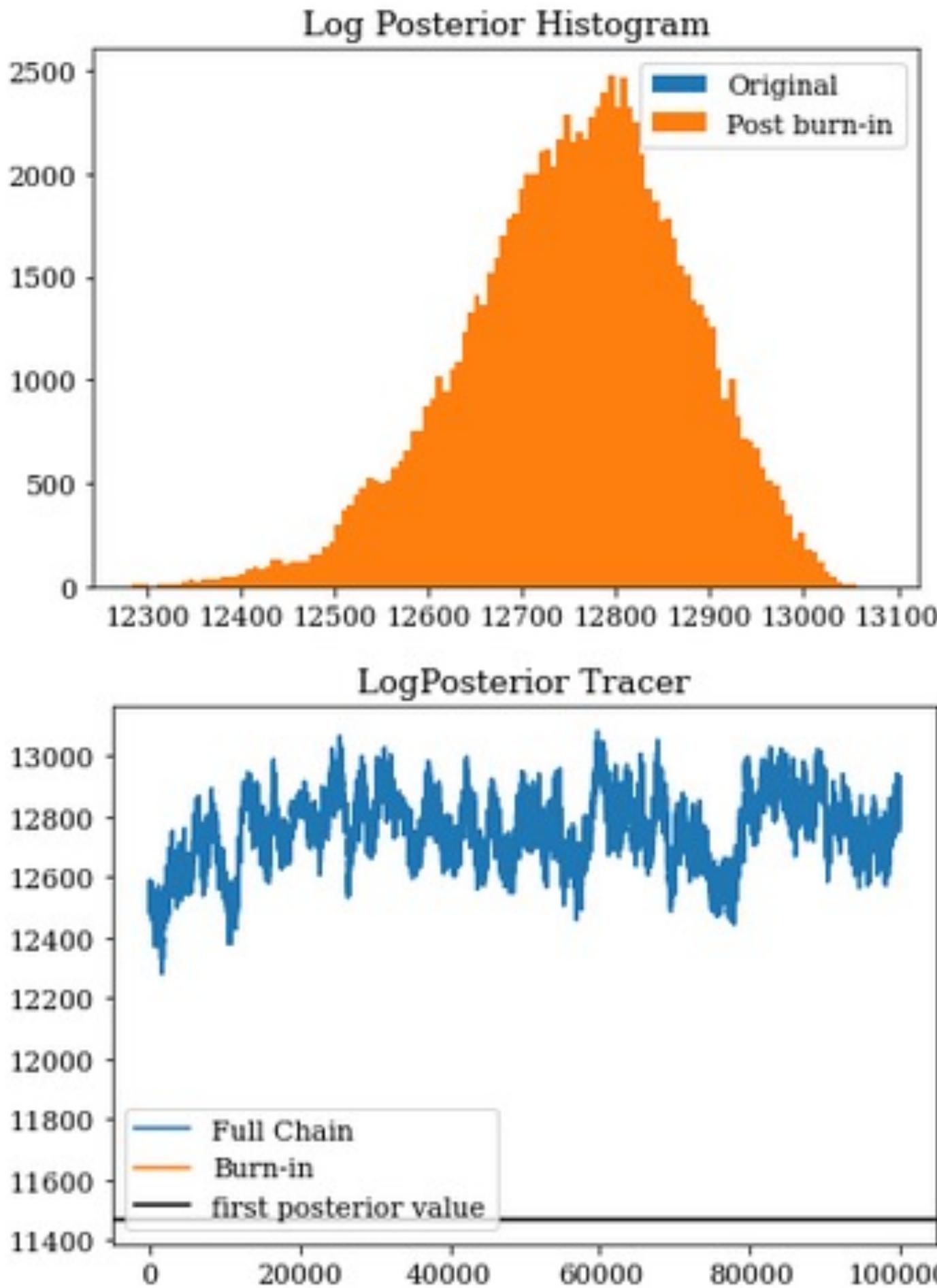
where  $\mathbf{C} = \mathbf{L}\mathbf{L}^T$

- Taking the diagonal-log of the Cholesky decomposed covariance

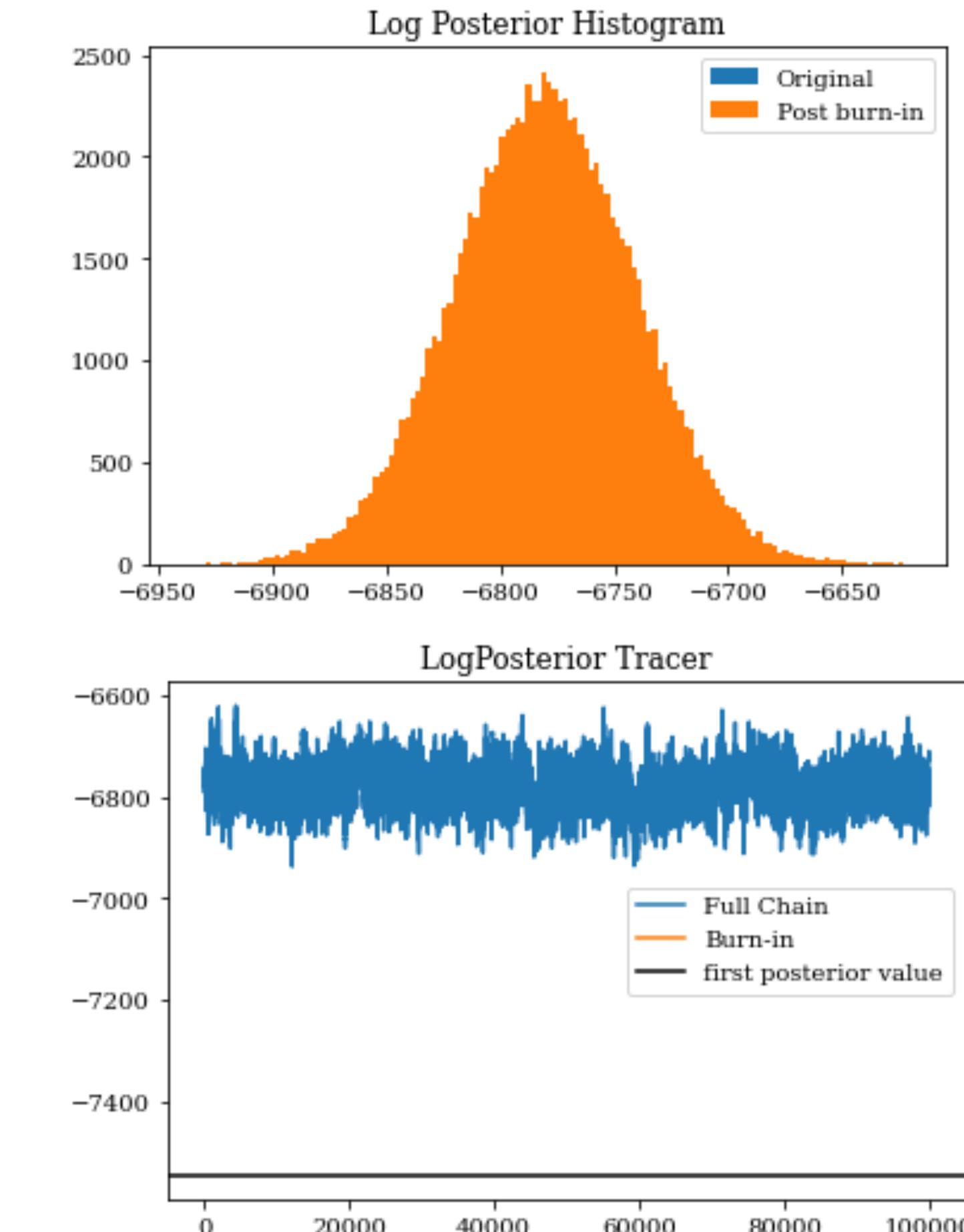
$$K_{\alpha\beta} = \begin{cases} \ln(L_{\alpha\beta}) & \text{if } \alpha = \beta, \\ L_{\alpha\beta} & \text{otherwise.} \end{cases}$$



# Coordinate System comparison



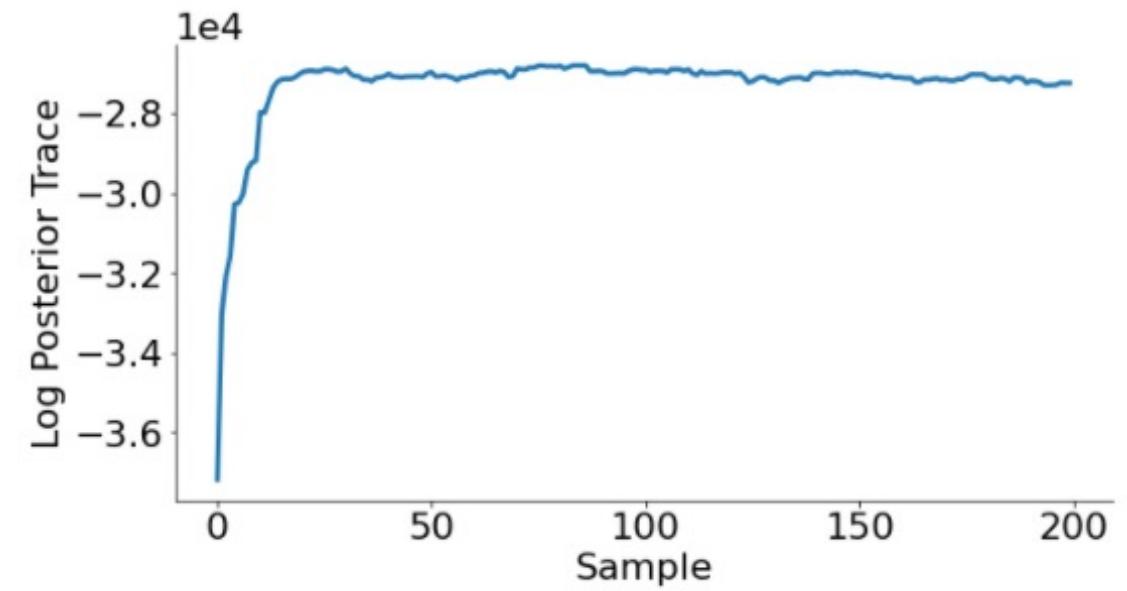
Naïve:  $G_\ell = \log(C_\ell)$  &  $a_{\ell m}$



Cholesky:  $K_{ij}$  &  $x_{\ell m} = L^{-1} a_{\ell m}$

# Tuned HMC

## Three phase tuning



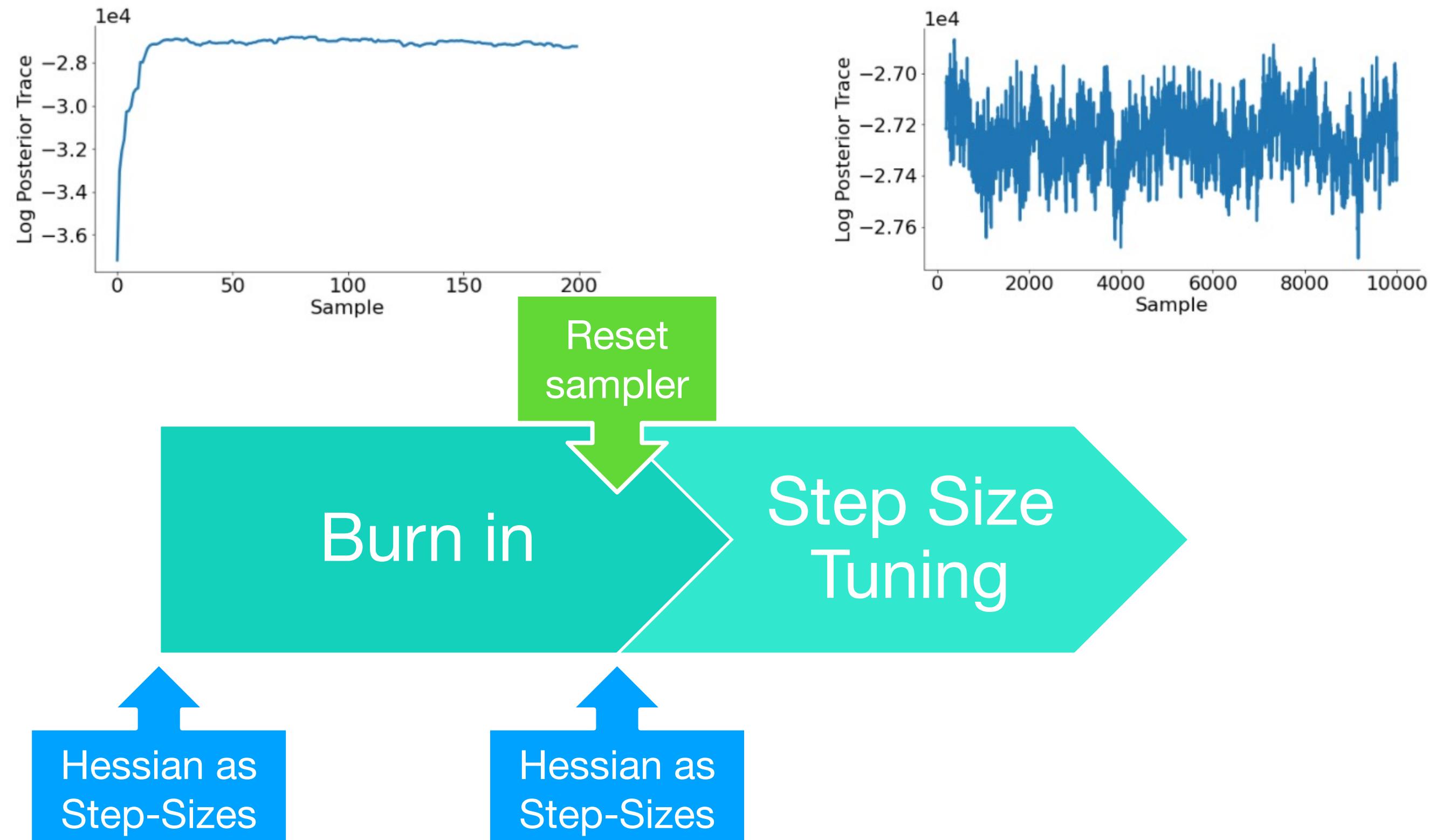
Burn in

Hessian as  
Step-Sizes

$$\mathcal{E} = \eta \left( \frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

# Tuned HMC

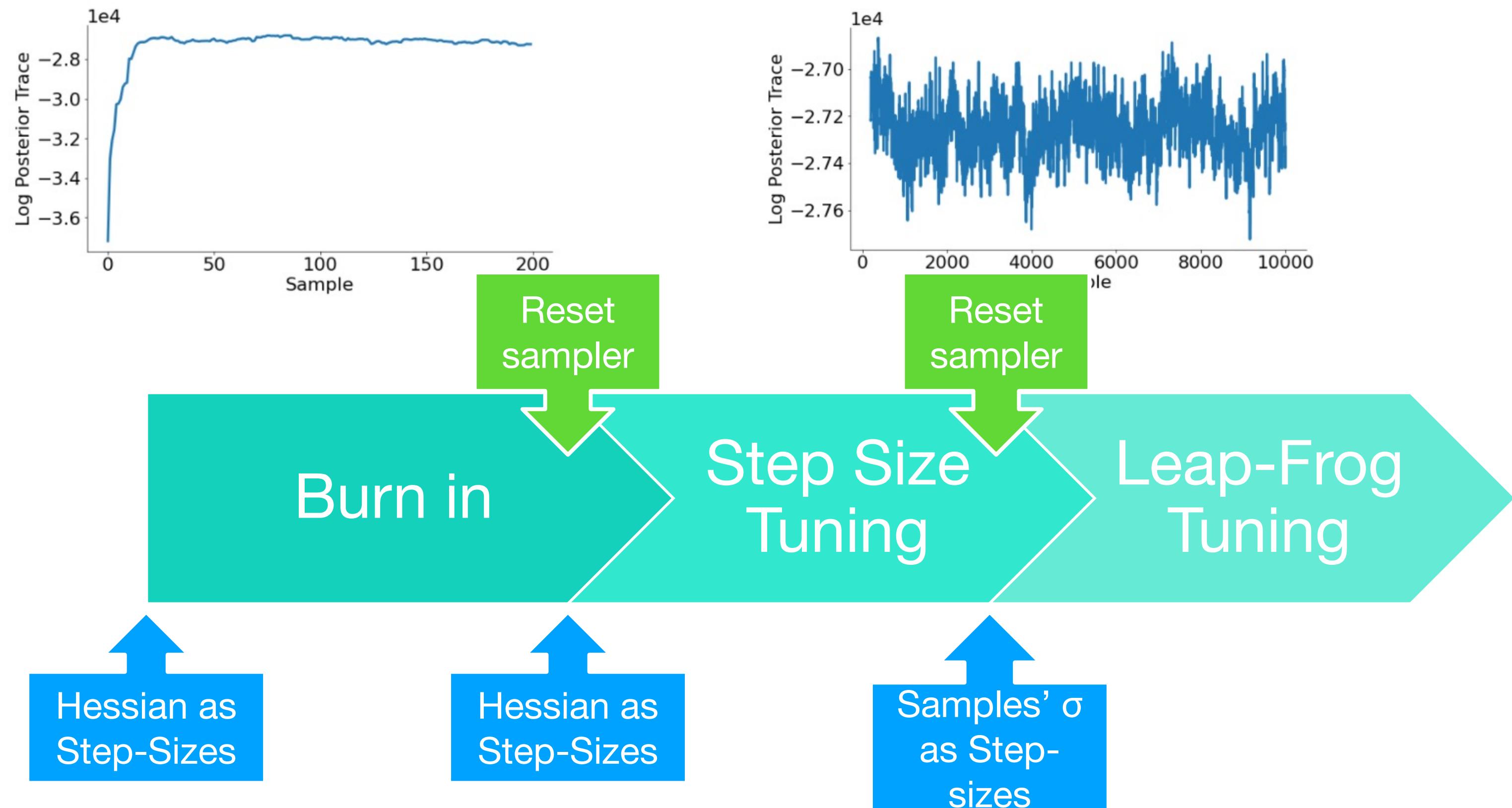
## Three phase tuning



$$\mathcal{E} = \eta \left( \frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

# Tuned HMC

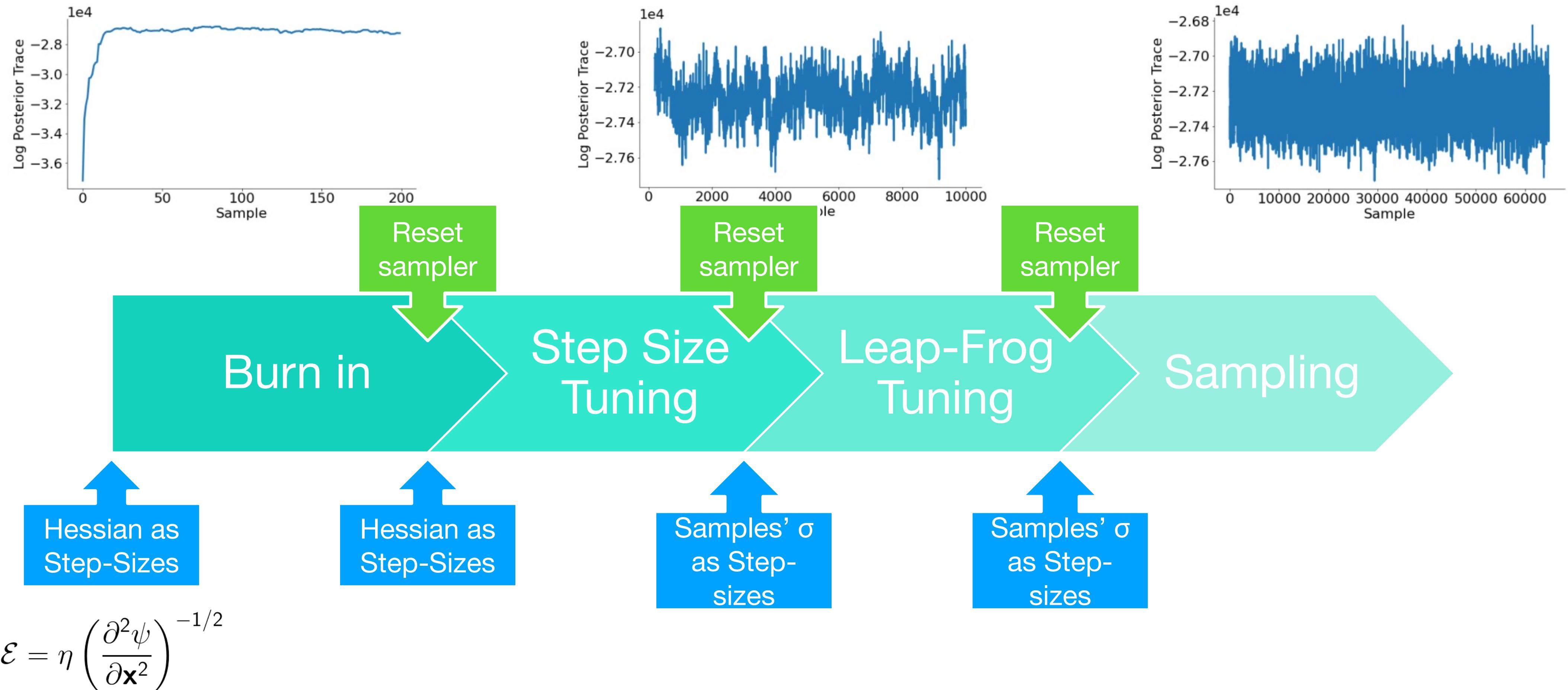
## Three phase tuning



$$\mathcal{E} = \eta \left( \frac{\partial^2 \psi}{\partial \mathbf{x}^2} \right)^{-1/2}$$

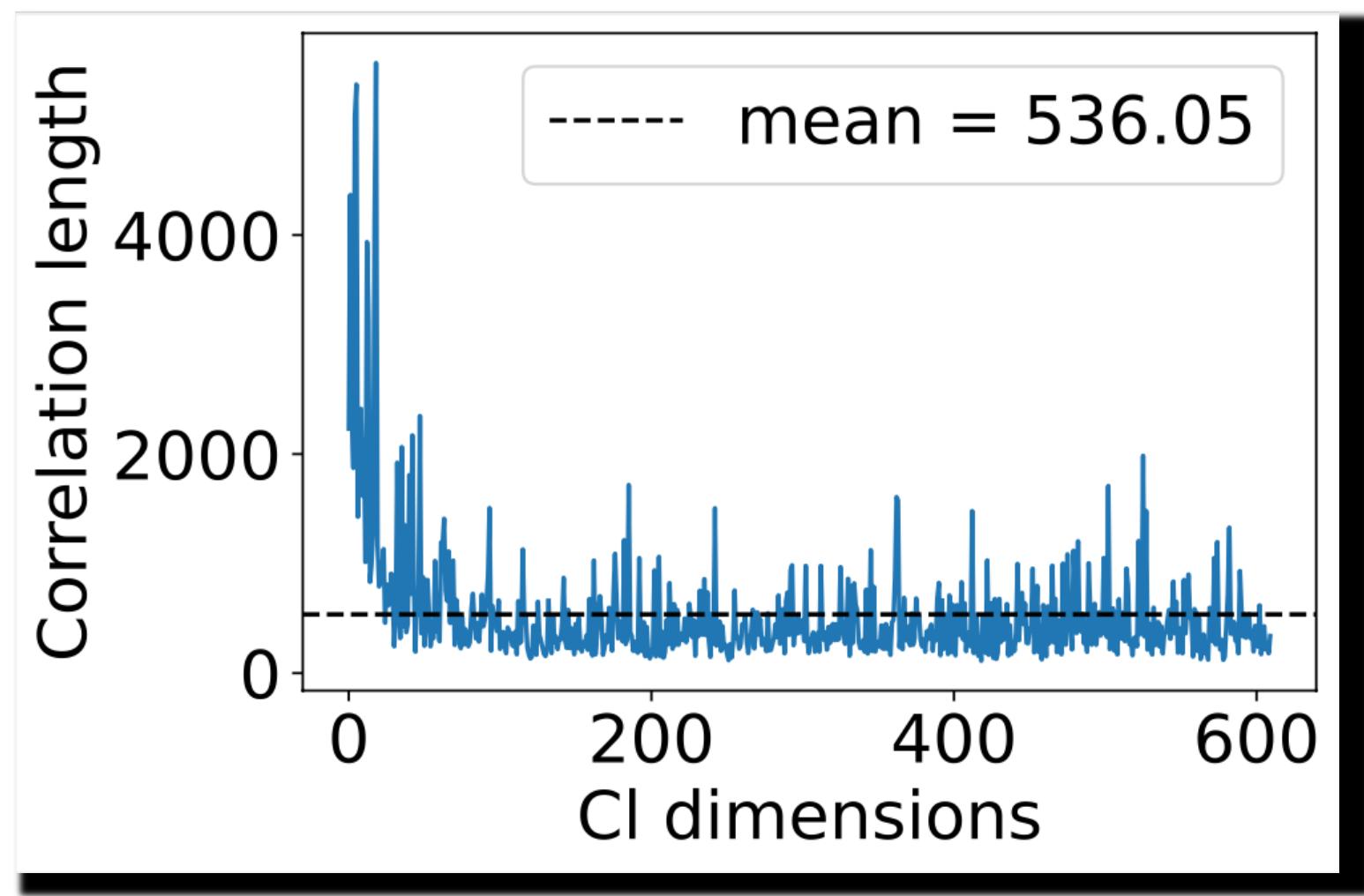
# Tuned HMC

## Three phase tuning

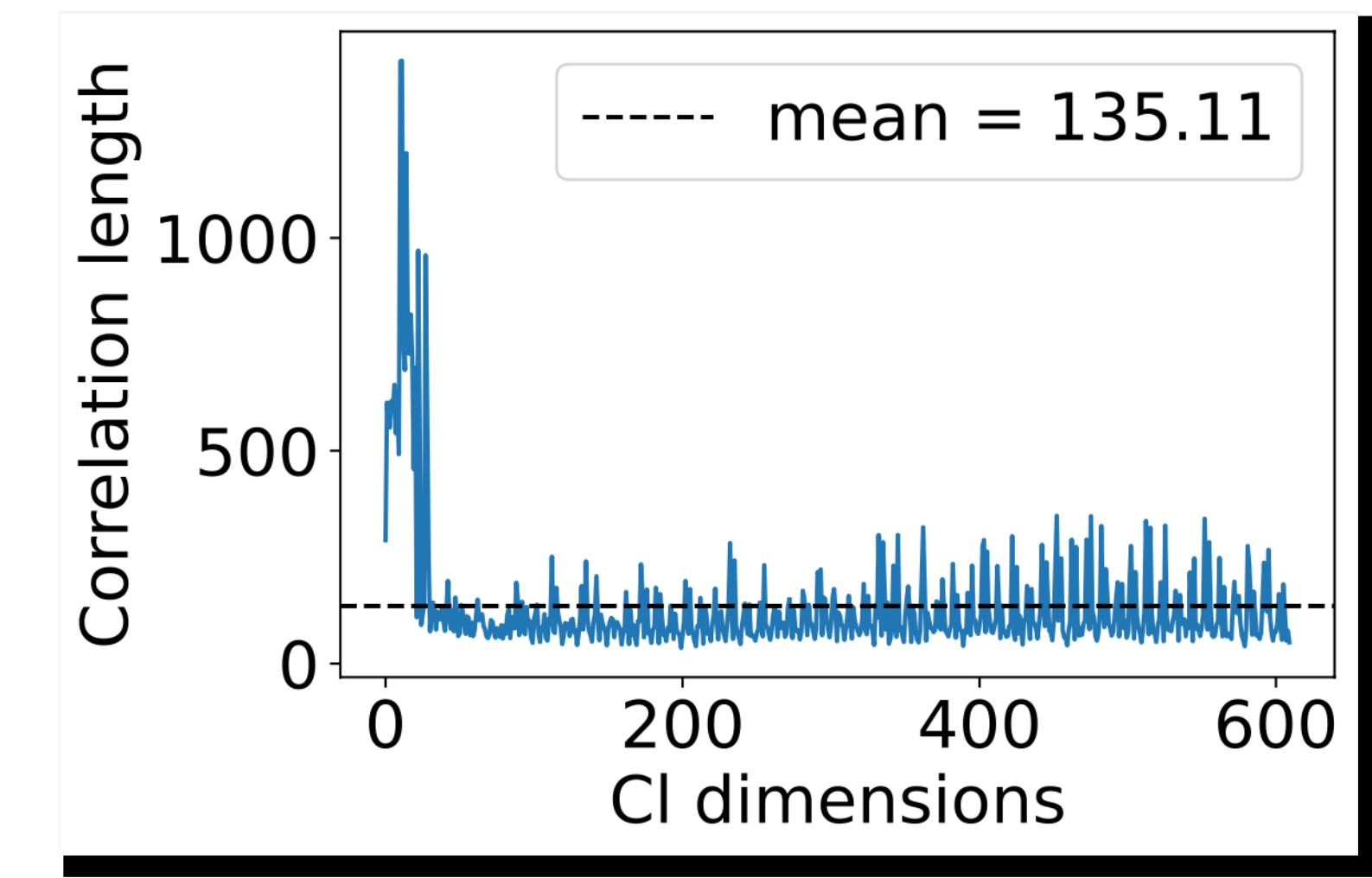


# Tuned HMC

## Three phase tuning



Normal HMC



Tuned HMC

# **5. Applications to Weak Lensing**

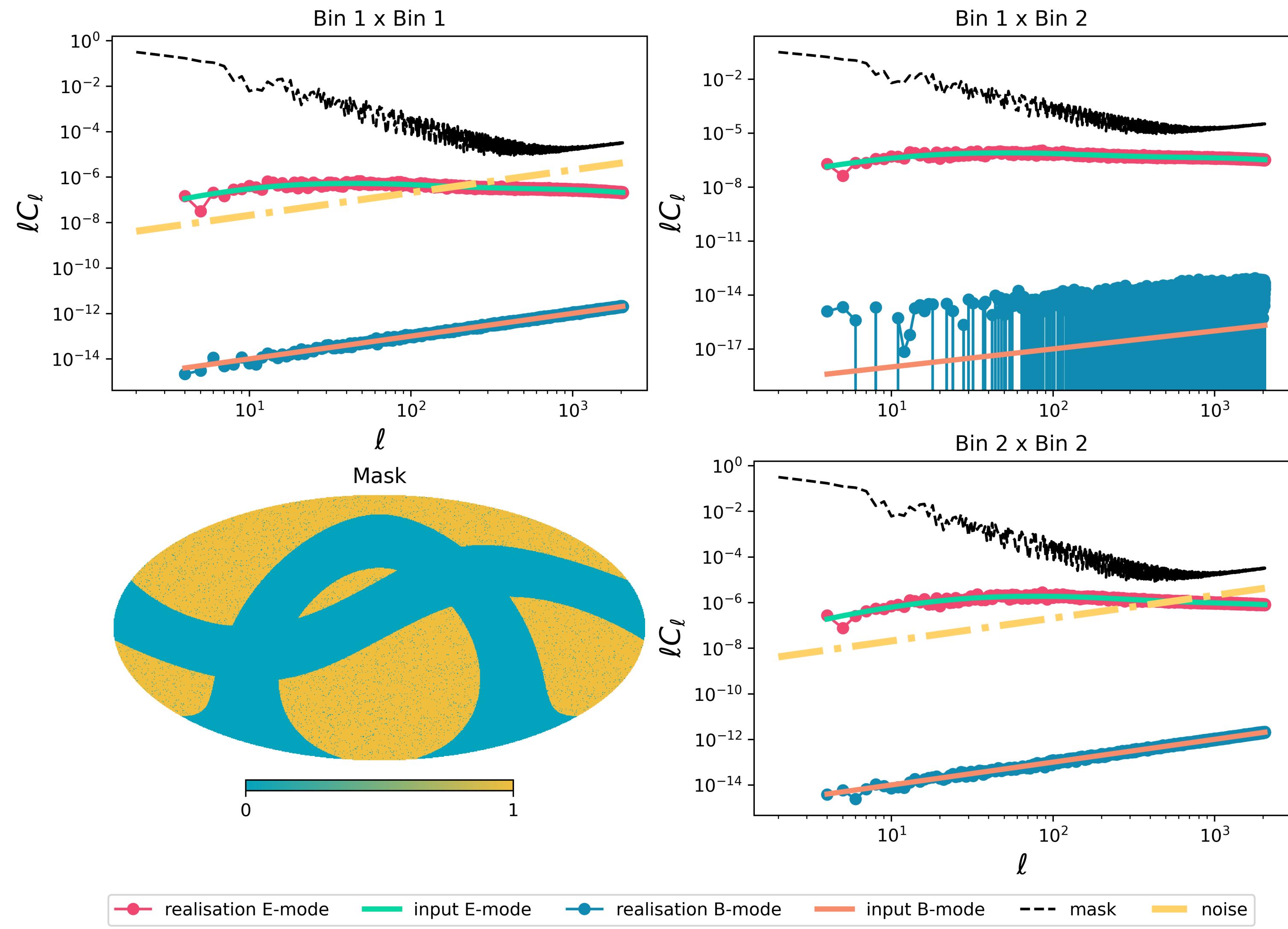
## **Simulated Euclid-like data**



# Weak Lensing

## Euclid-like case

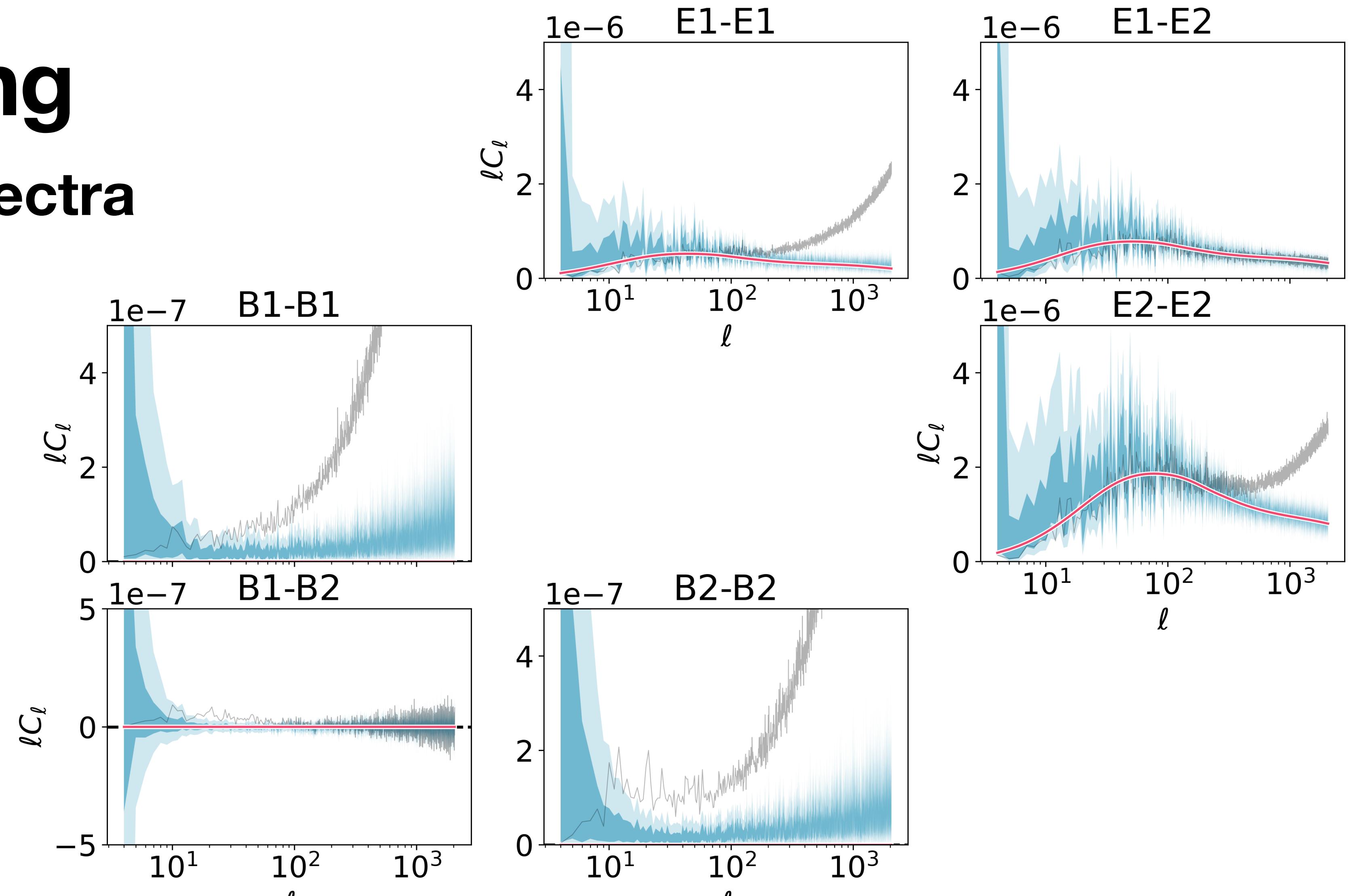
- Two tomographic bins
- Multipoles: 4, 2048
- Nside = 1024 (12.5M pixels)
- 16.8 Million free parameters;  
~20k are  $C_\ell$
- Noise:
  - 3 gals/arcmin<sup>2</sup>/bin
  - $\sigma(e) = 0.28$





# Weak Lensing

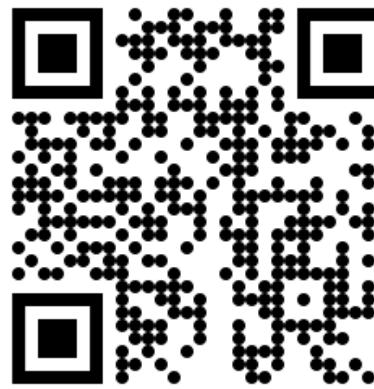
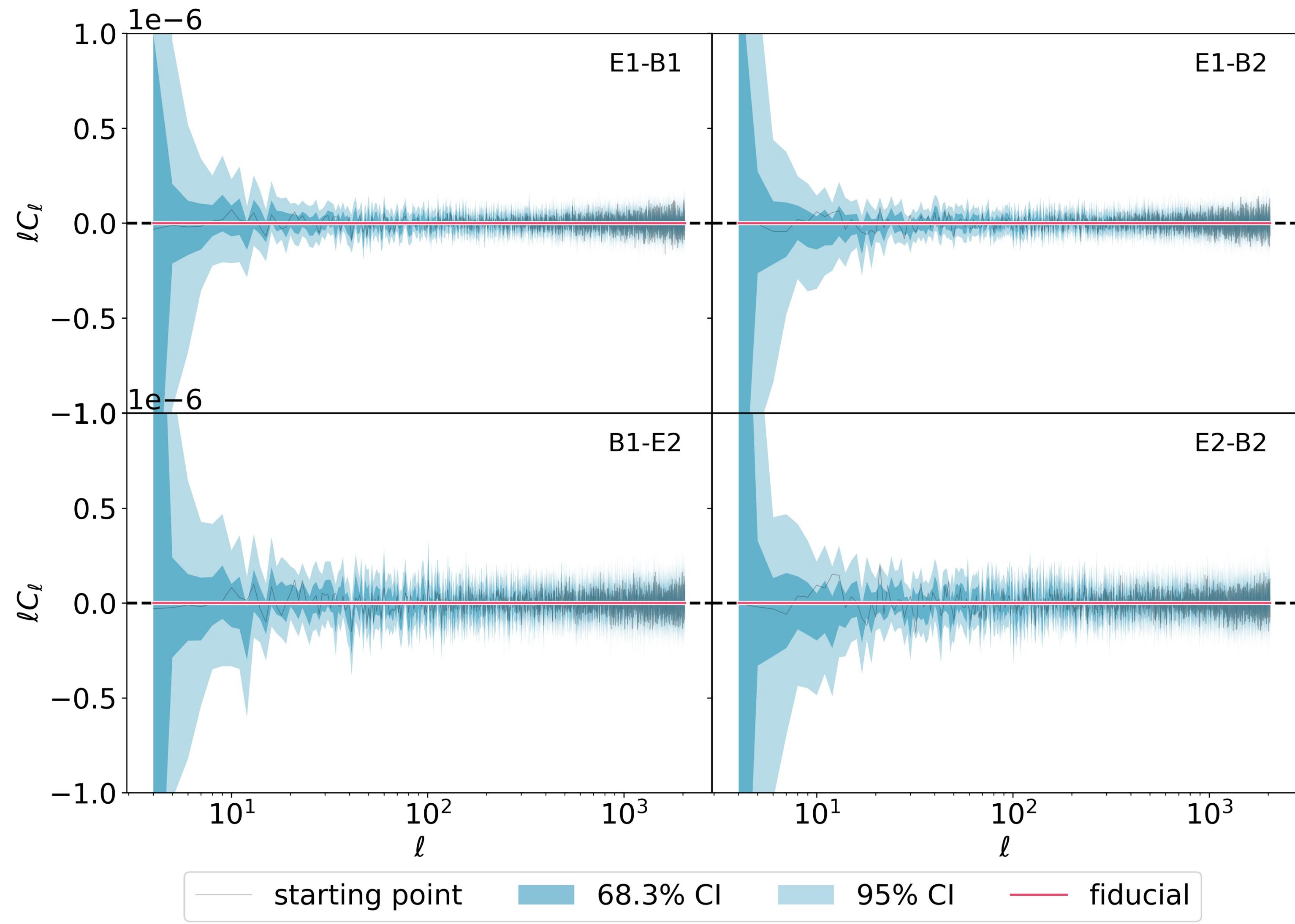
## Angular Power Spectra



starting point      95% CI      68.3% CI      fiducial



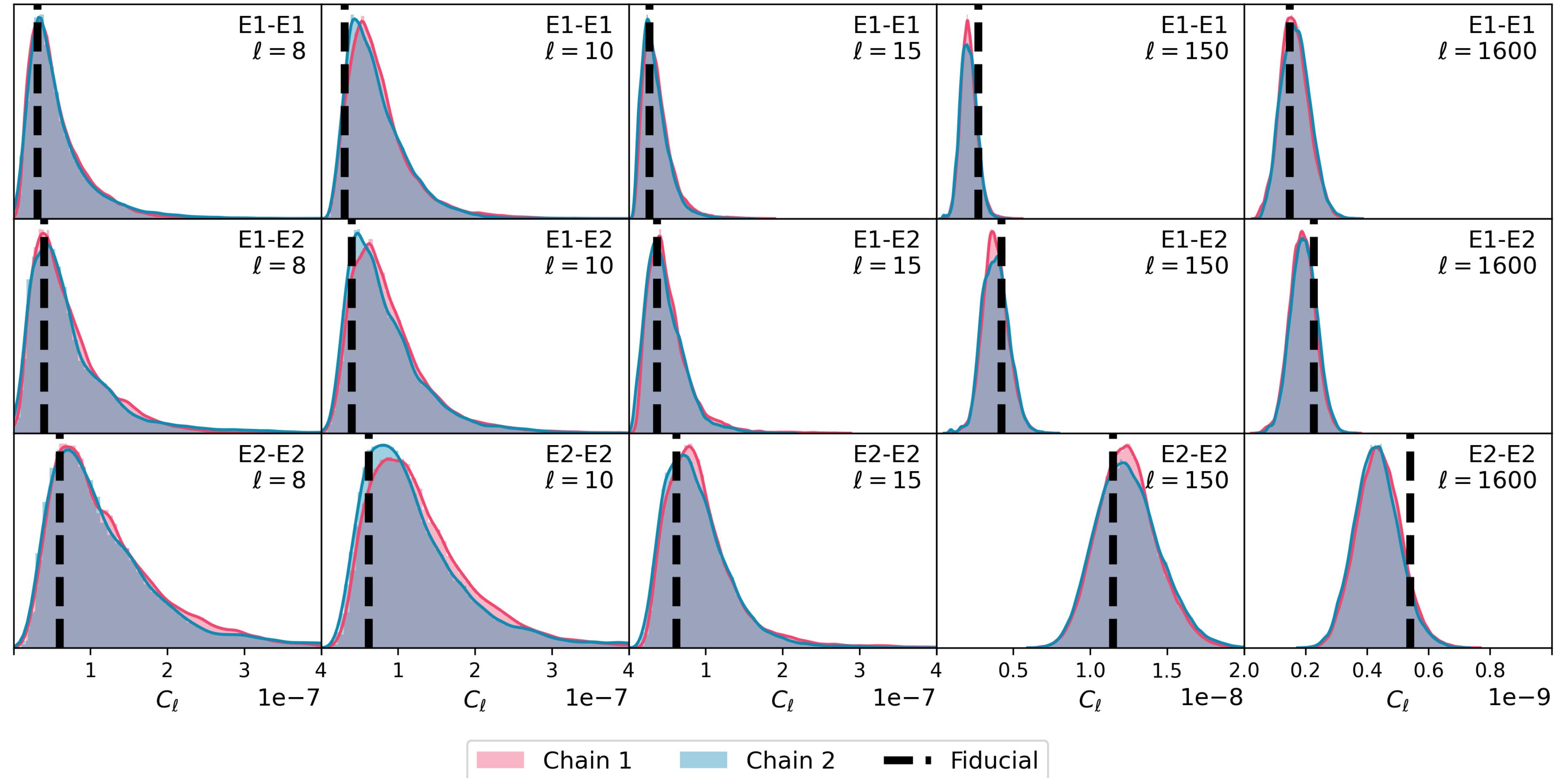
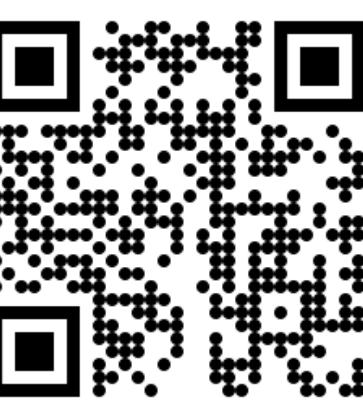
# Weak Lensing Angular Power Spectra

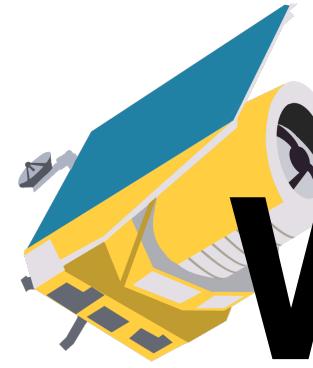




# Weak Lensing

## Angular Power Spectra

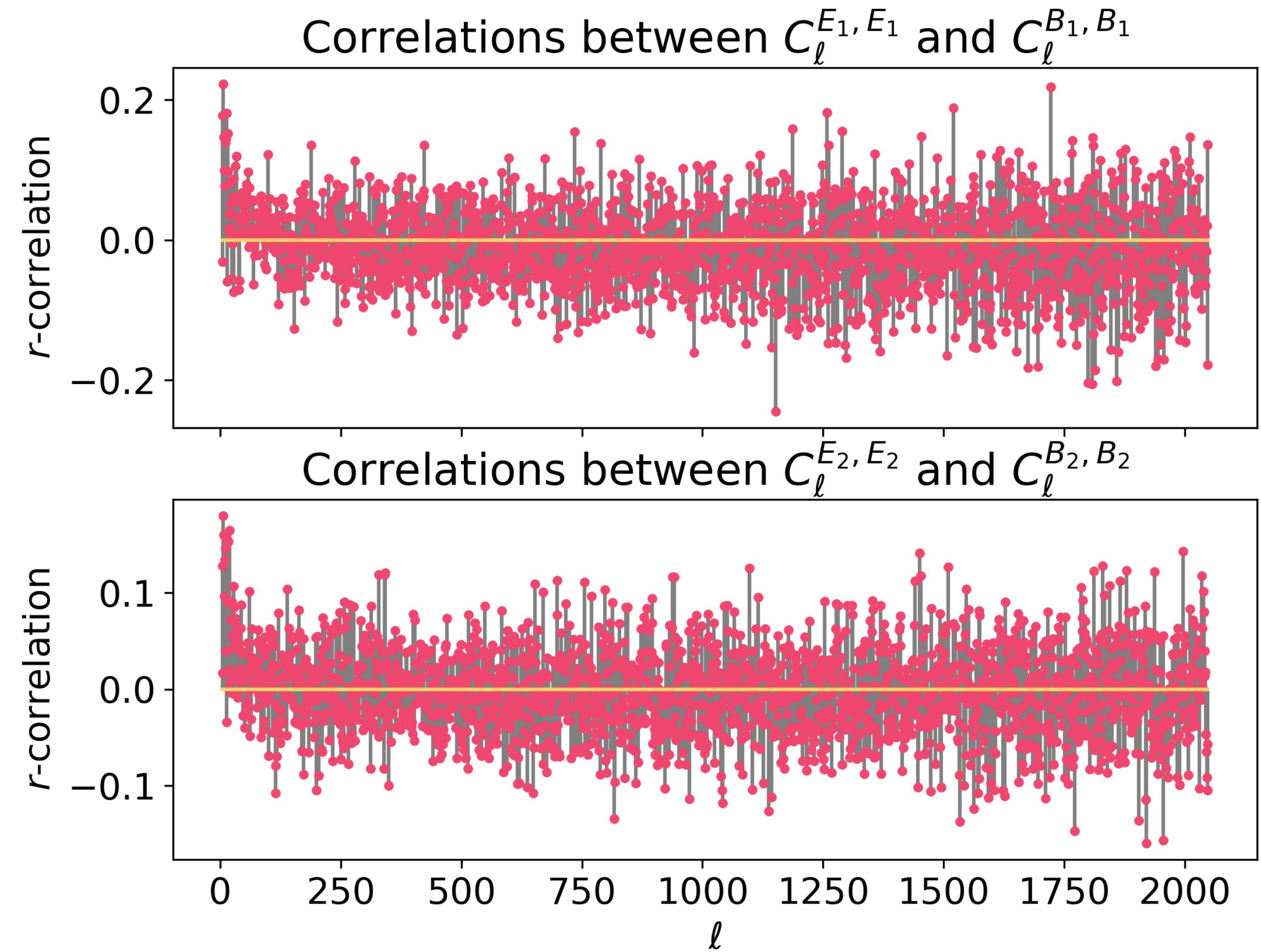
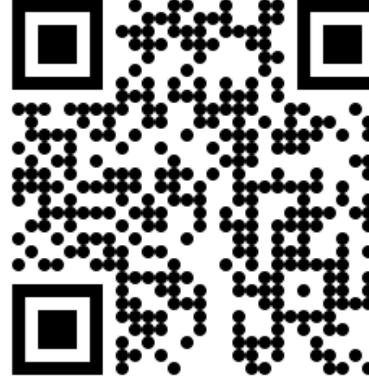




# Weak Lensing

## E/B Correlations

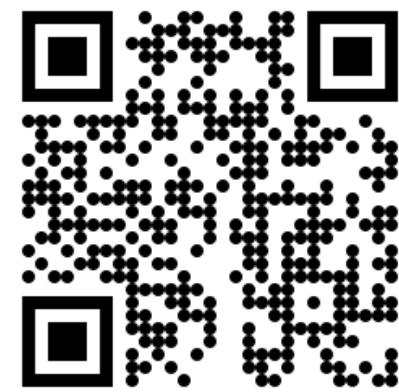
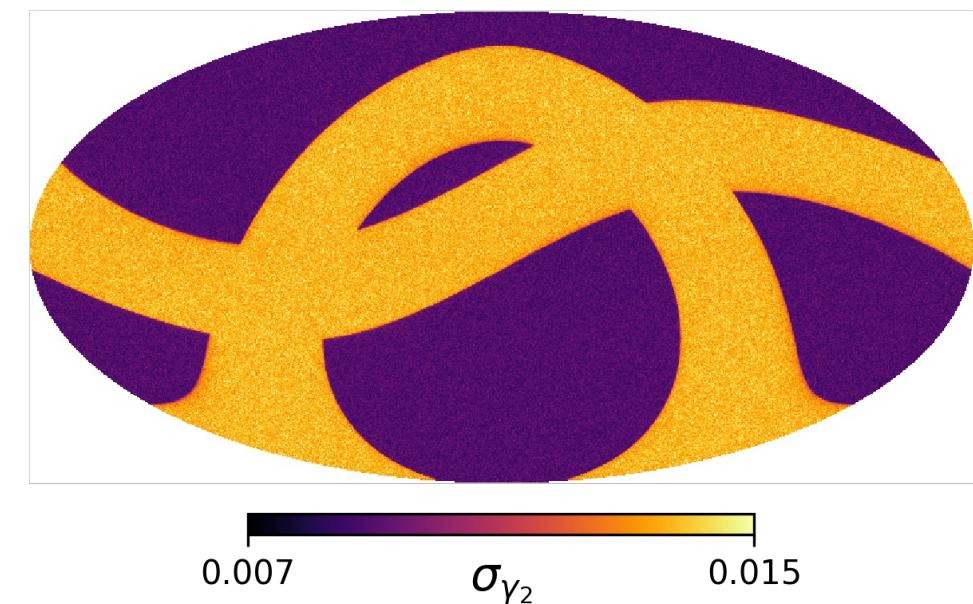
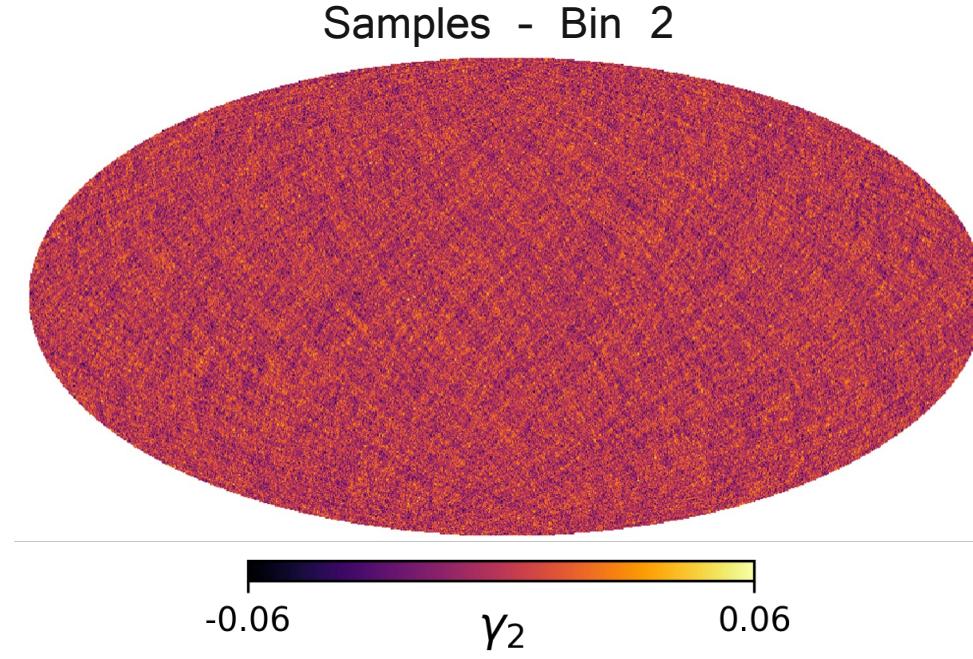
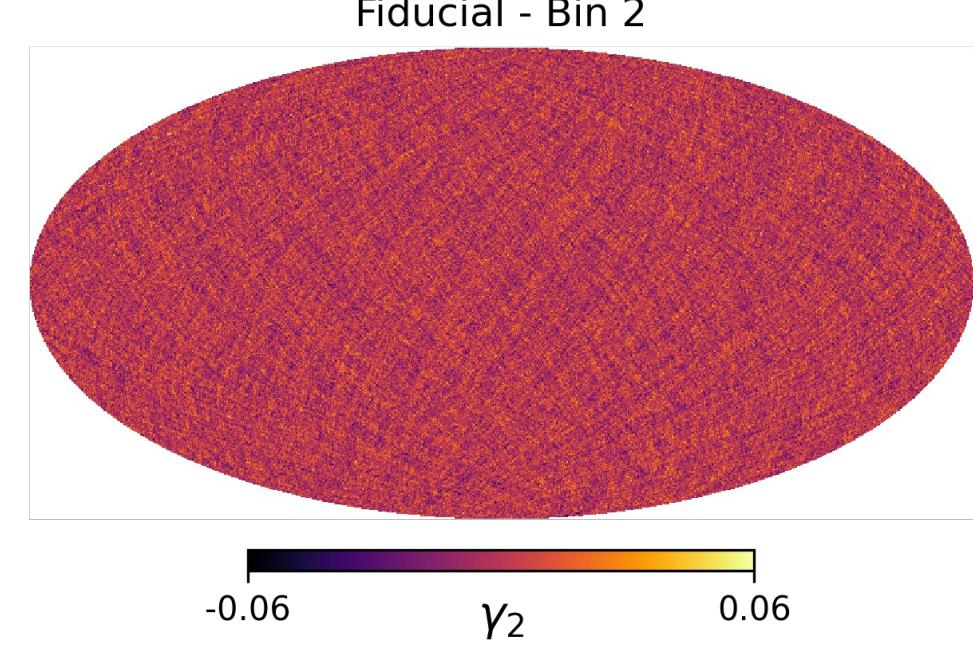
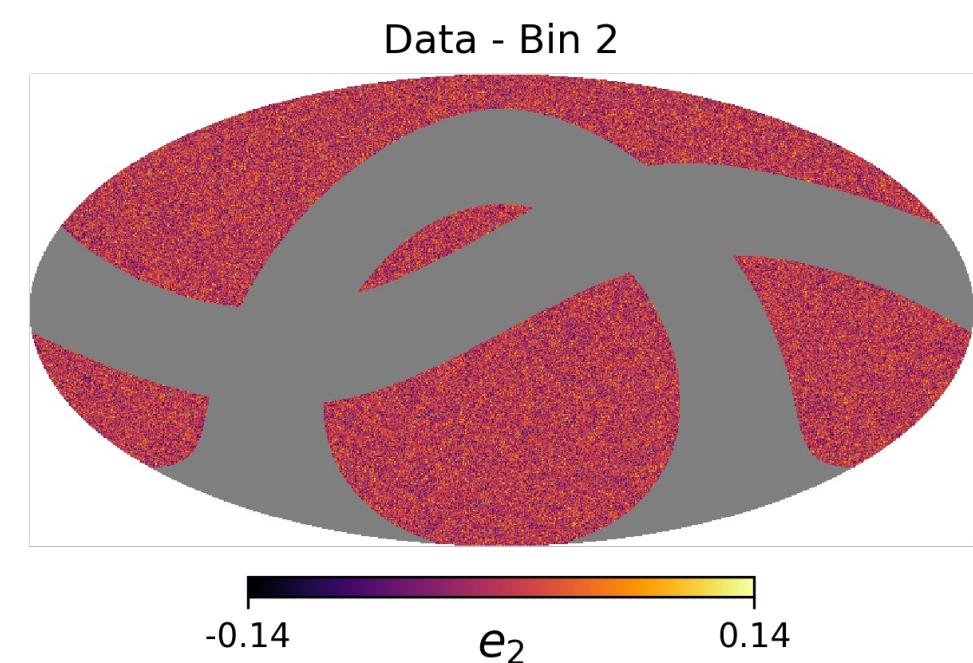
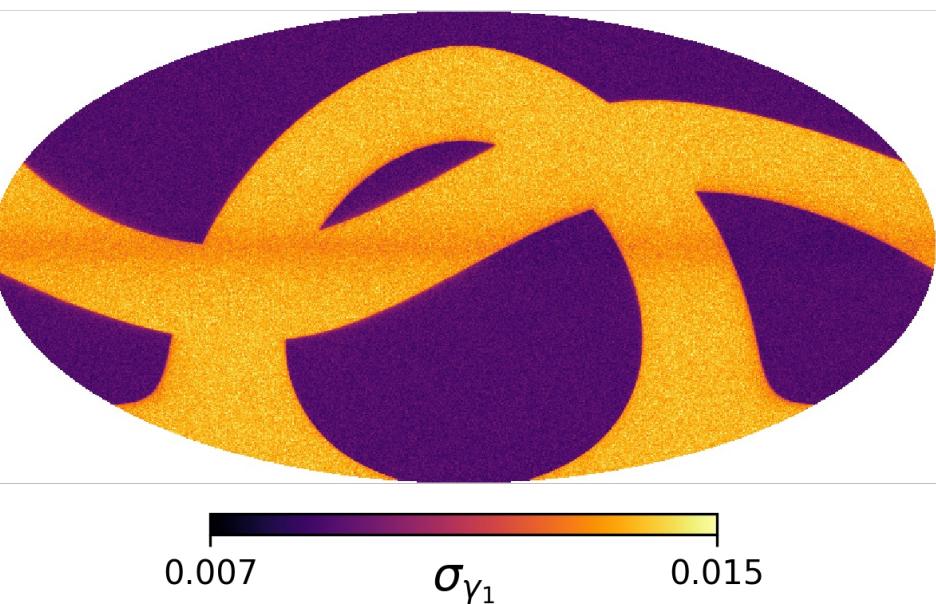
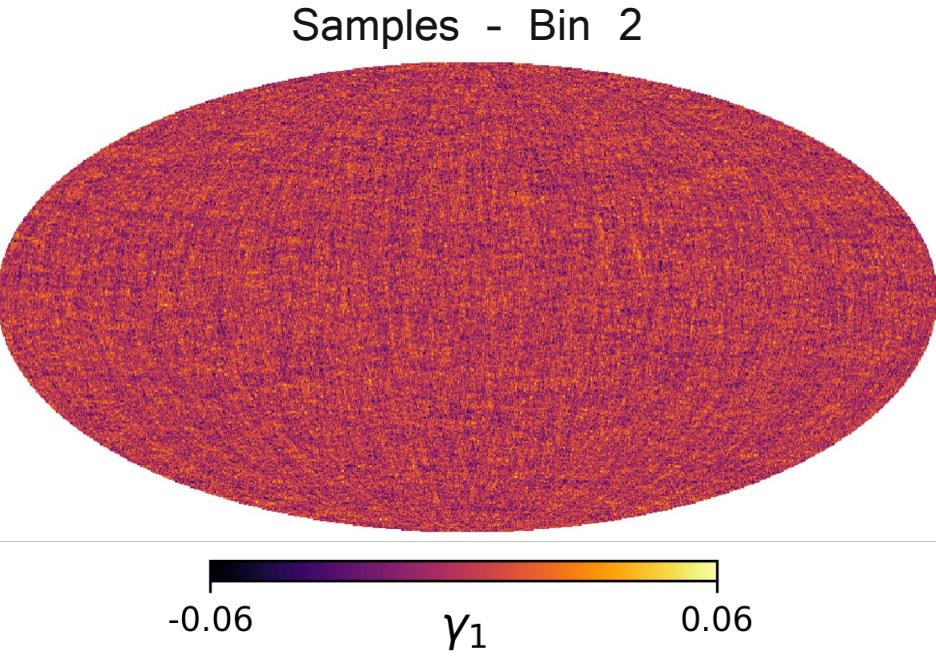
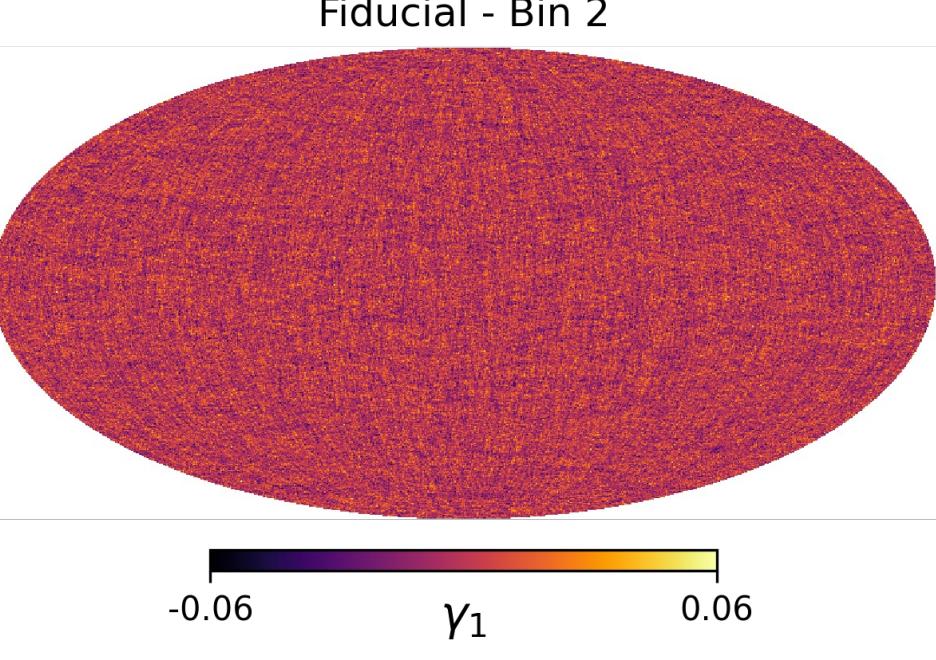
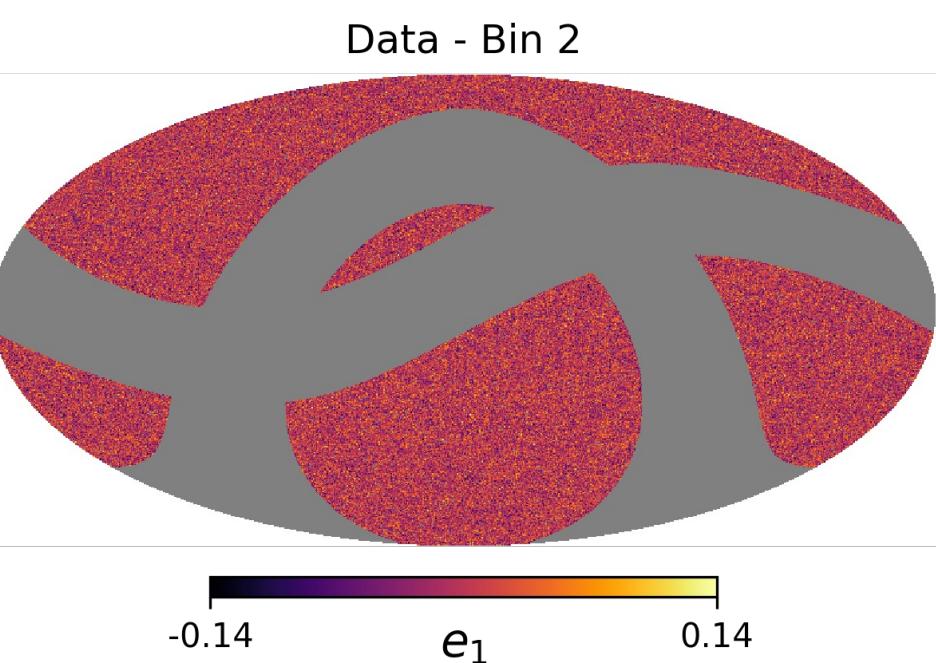
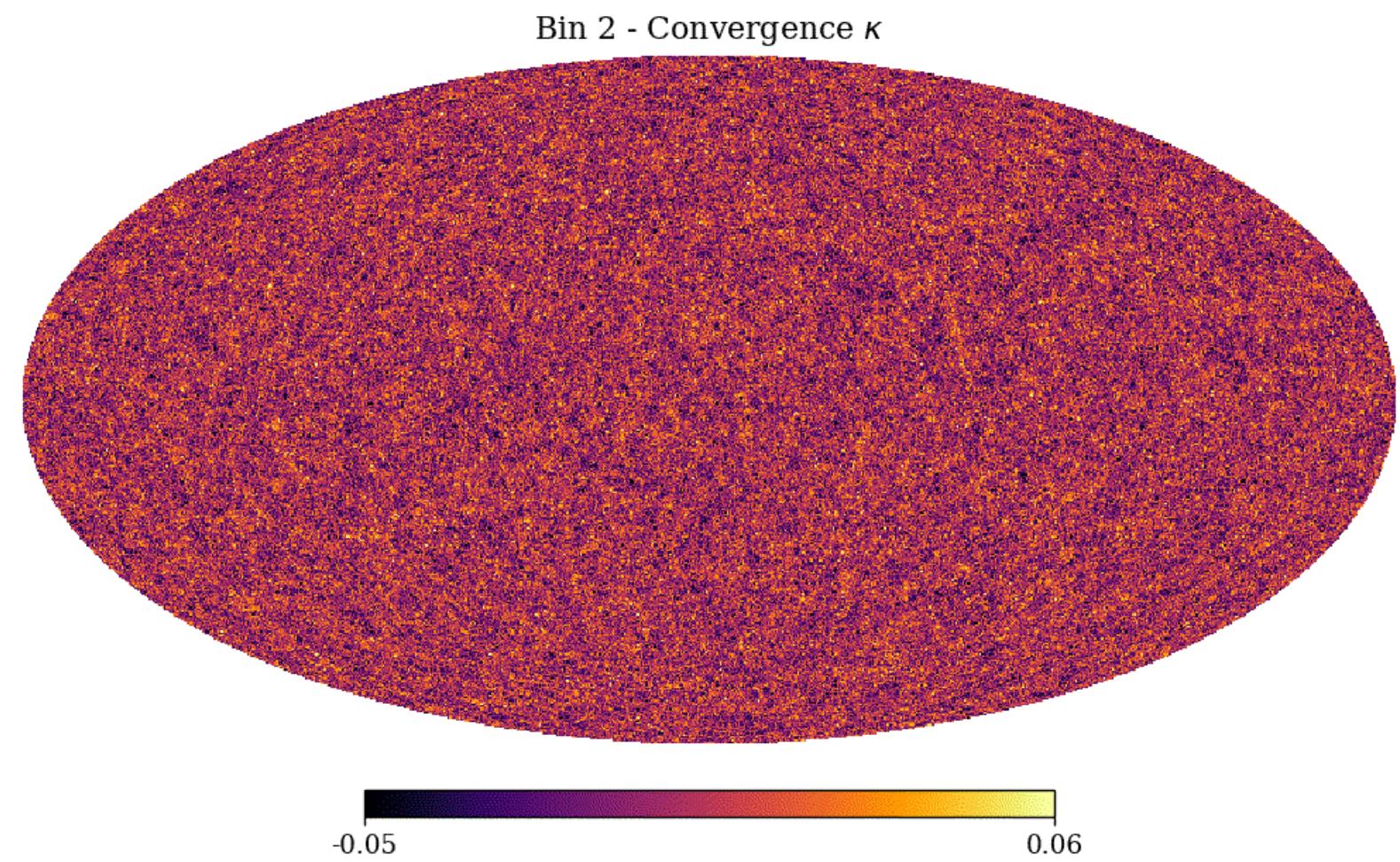
Safe to use the point estimates,  
no E/B leak detected!

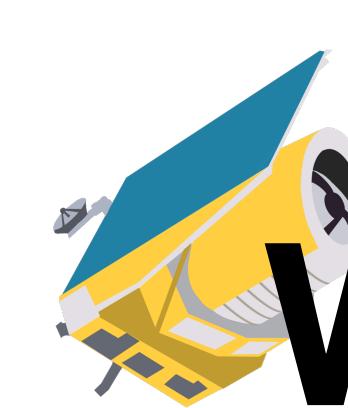




# Weak Lensing

## Inferred shear maps

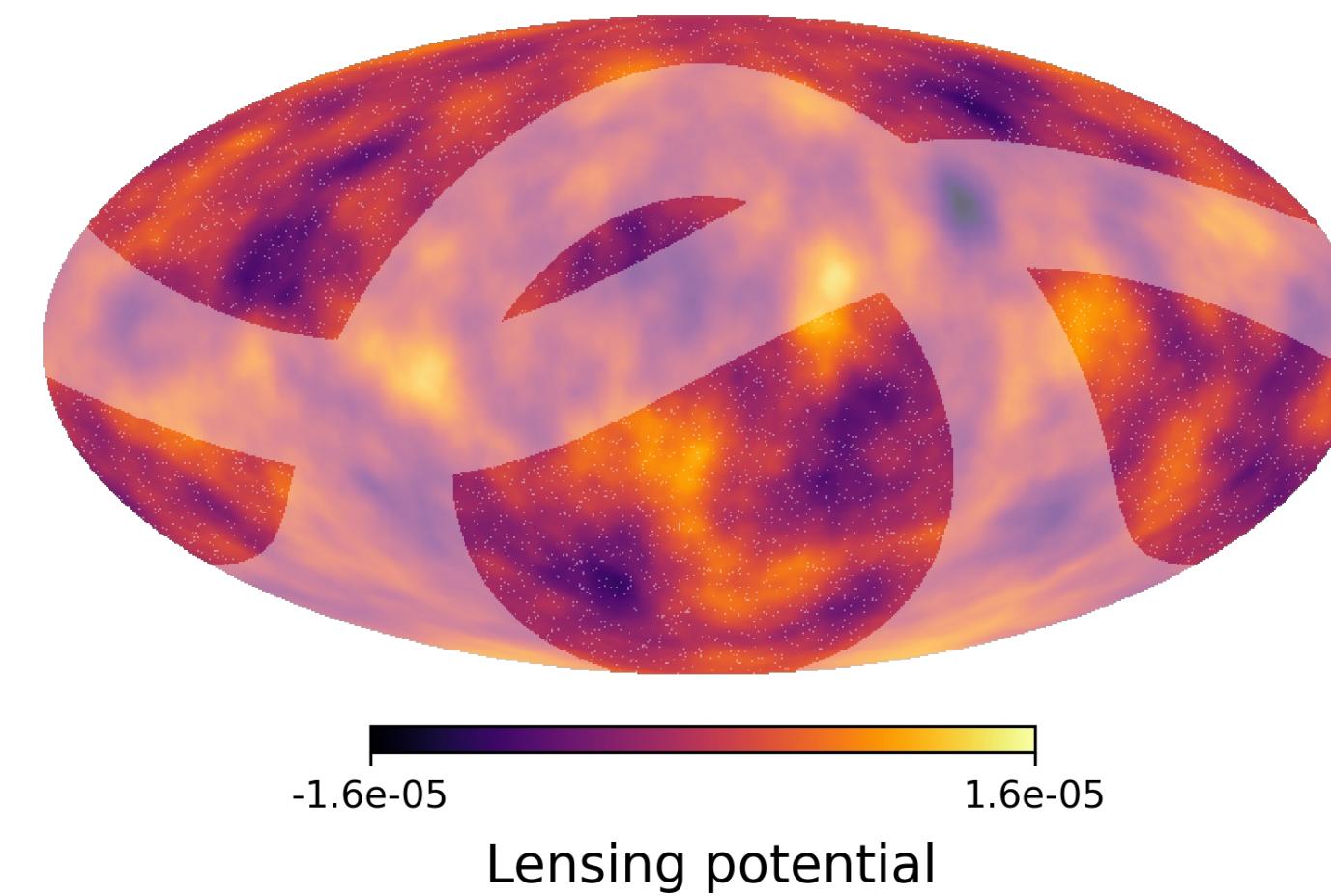




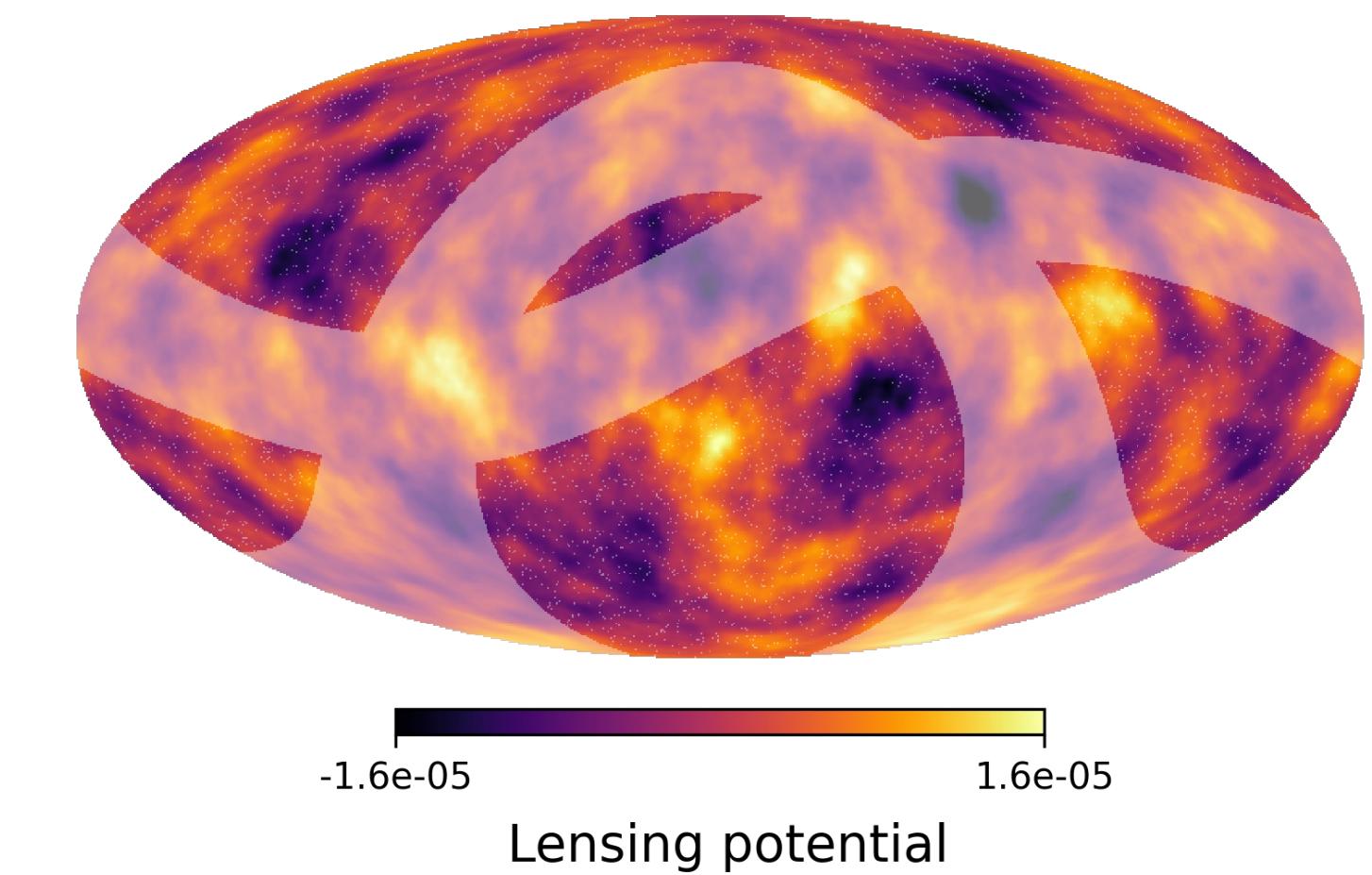
# Weak Lensing

## Reconstructed Lensing Potential

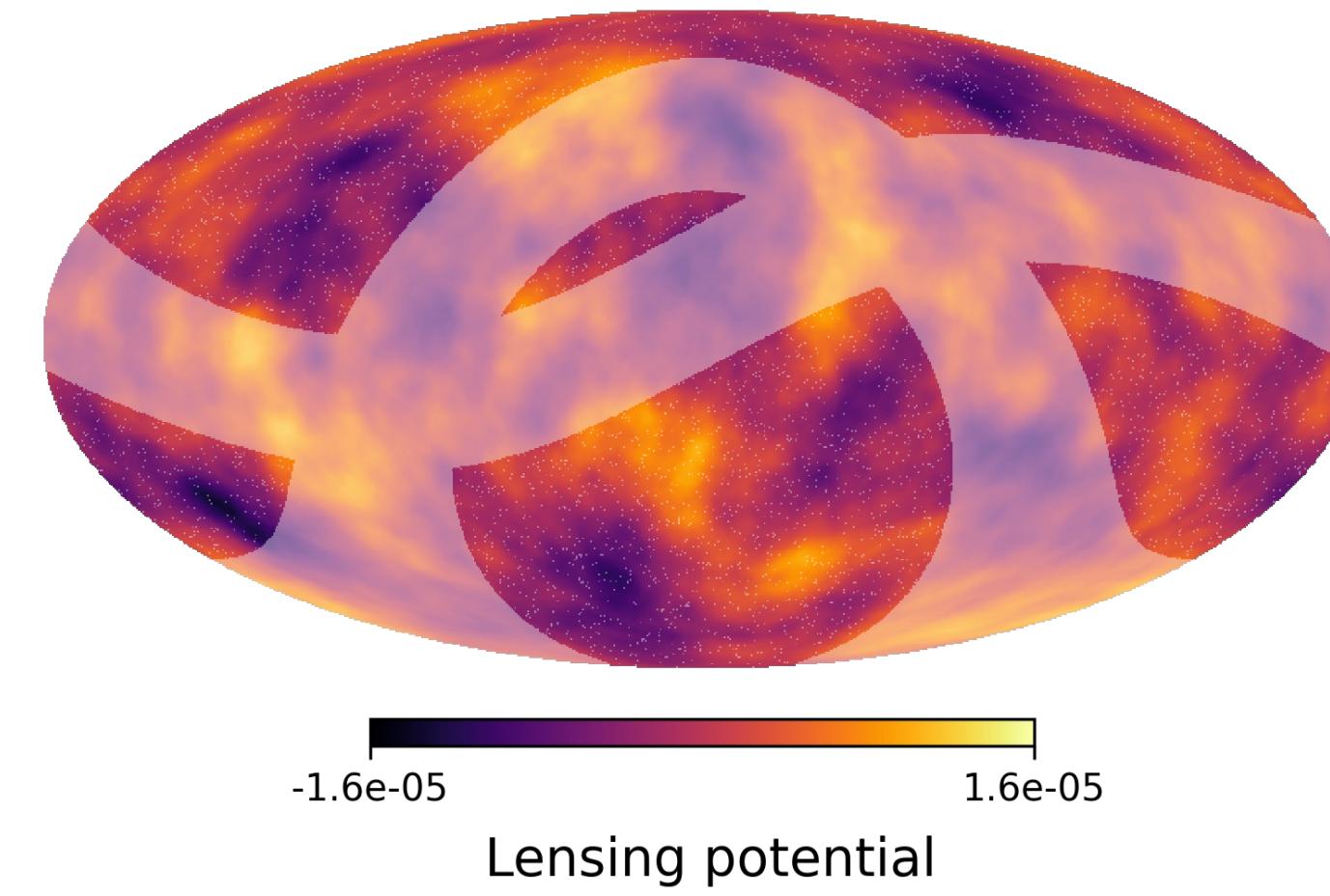
Ground Truth - Bin 1



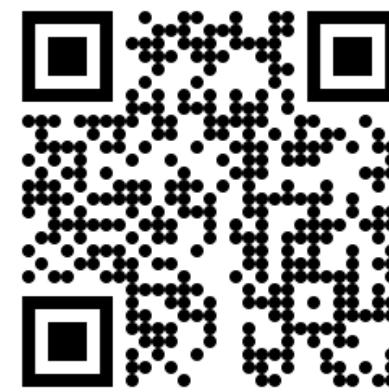
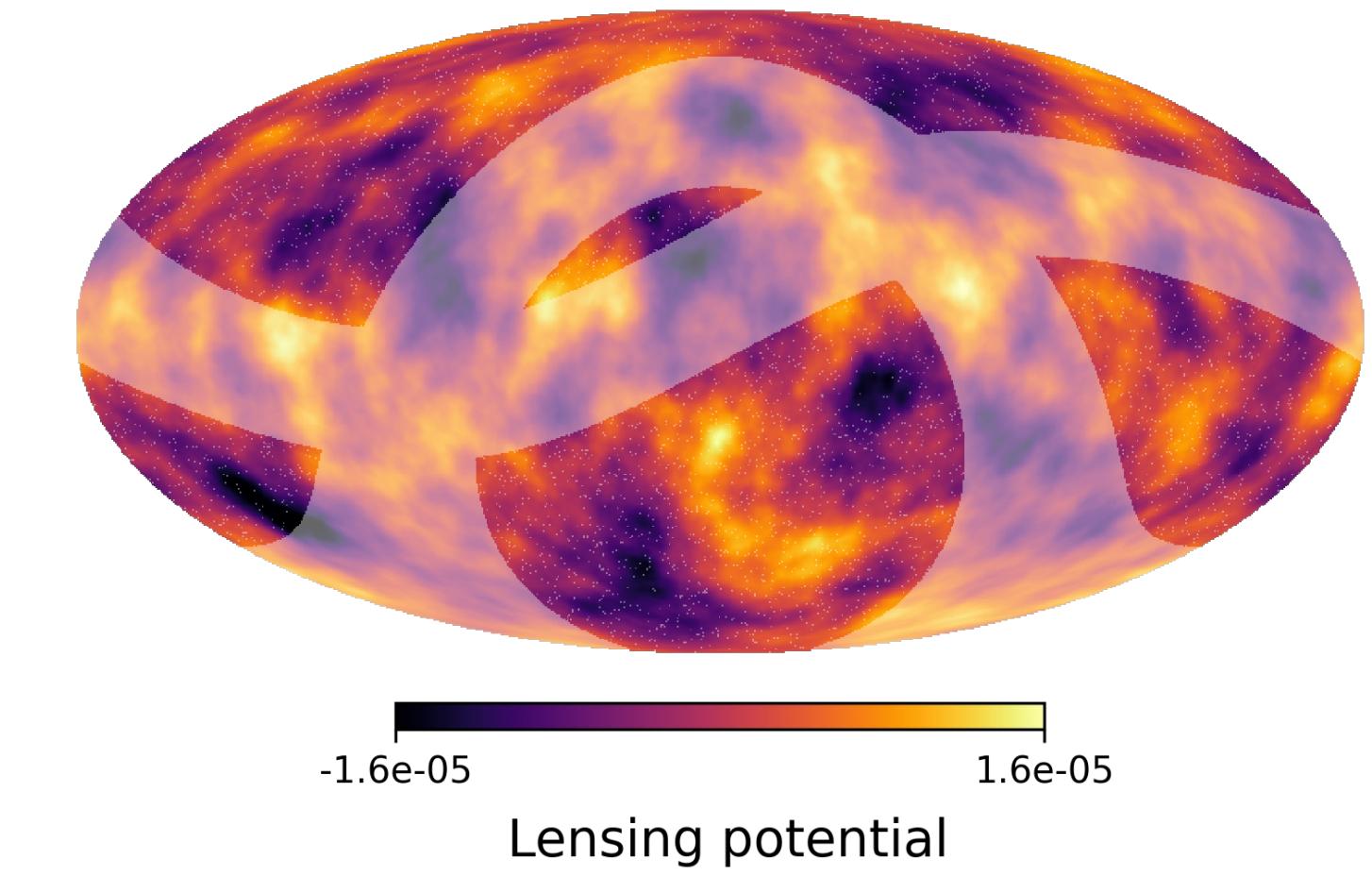
Ground Truth - Bin 2



Typical Sample Map from Almanac- Bin 1



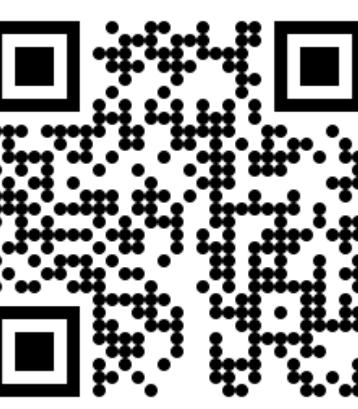
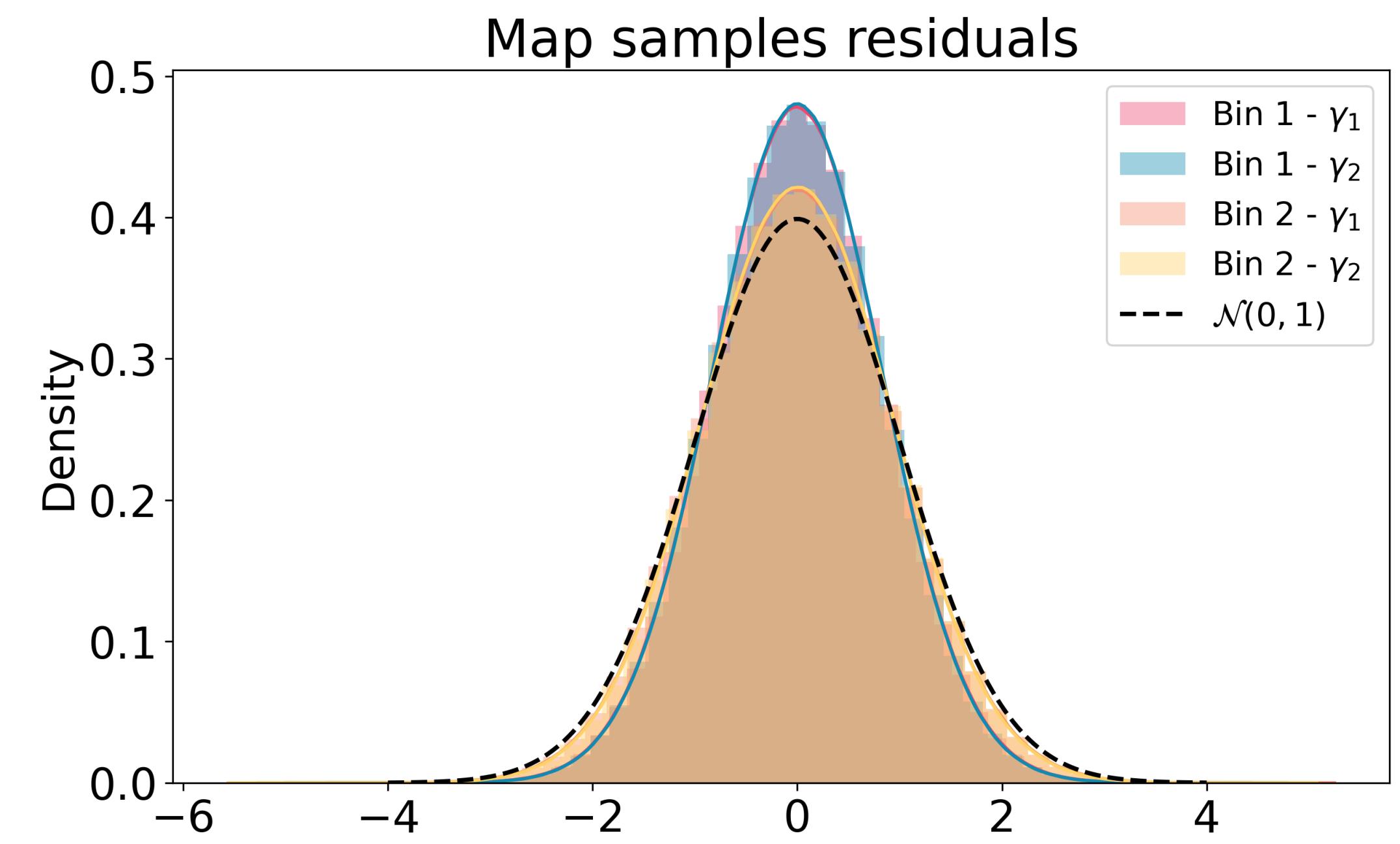
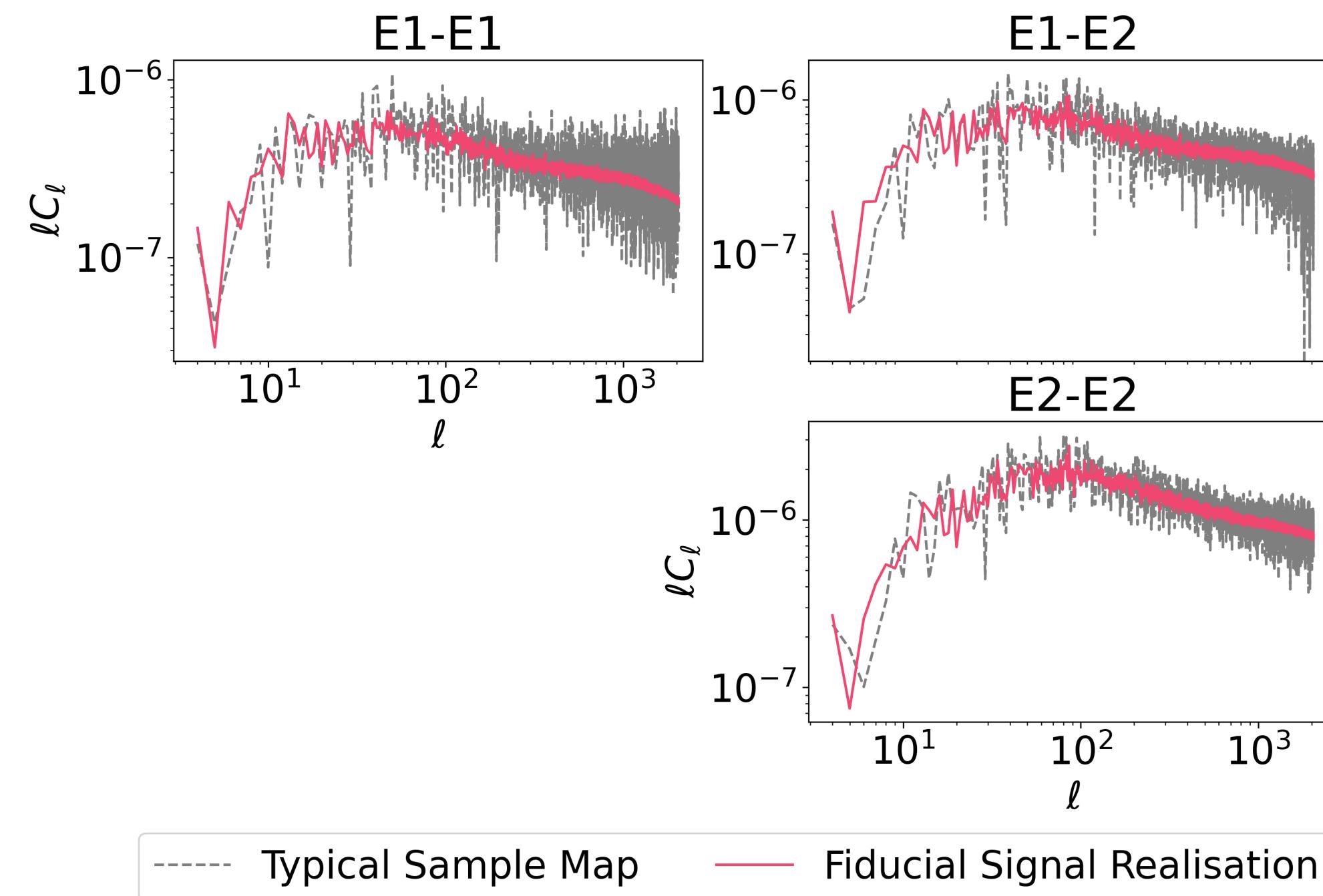
Typical Sample Map from Almanac - Bin 2





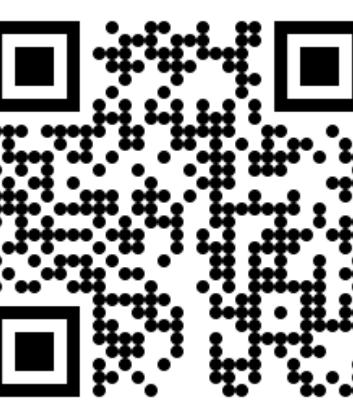
# Weak Lensing

## Map consistency check



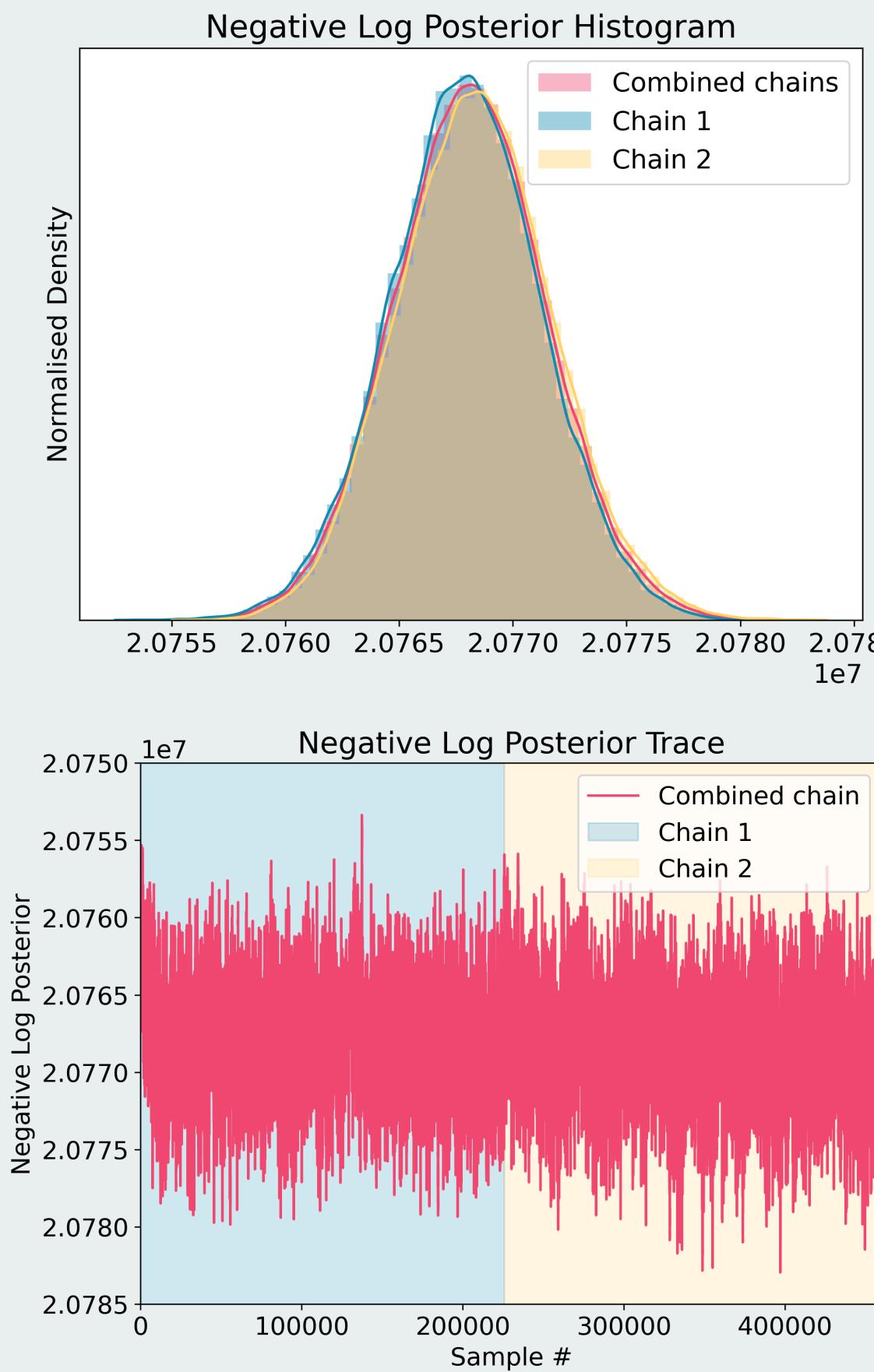
# **6. Convergence Testing**

**All diagnostics we carried out...**

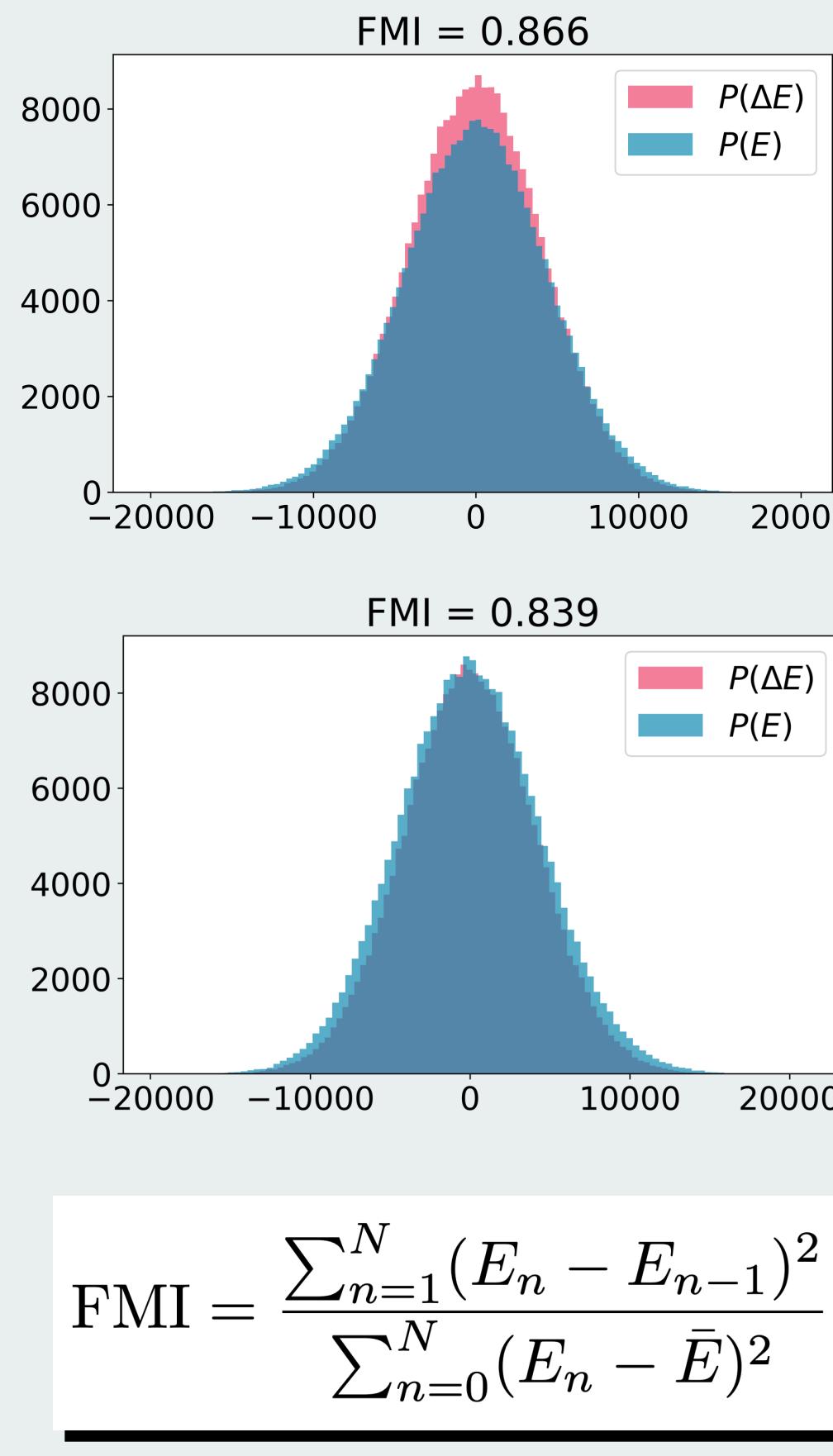


# Convergence Diagnostics

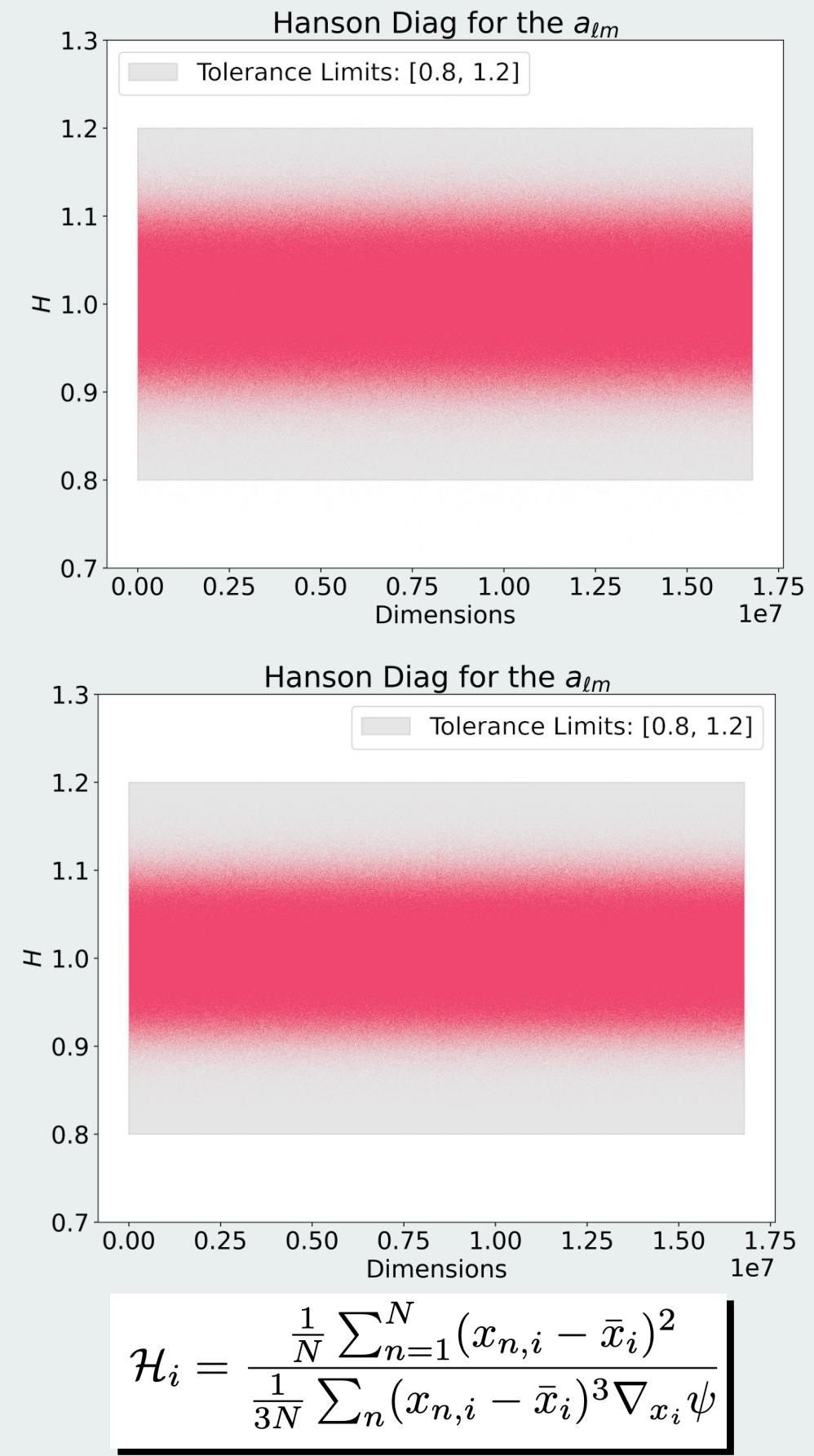
## Posterior Trace Analysis



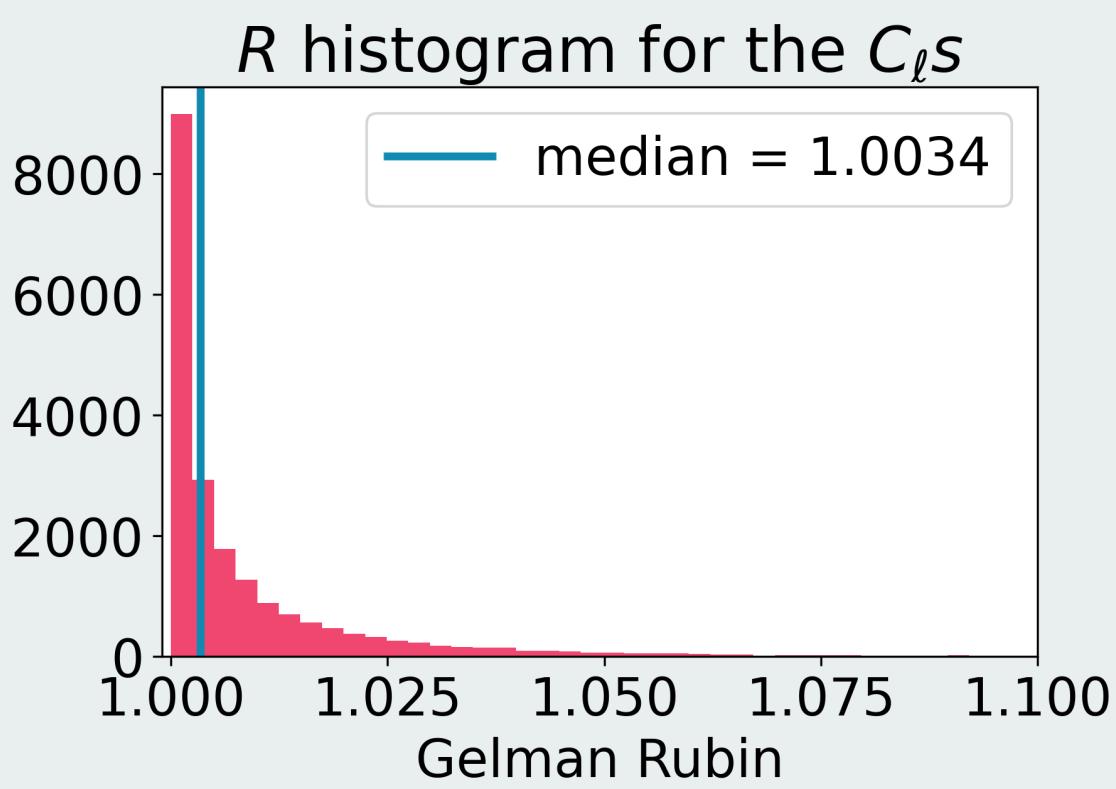
## Fraction of Missing Info



## Hanson Diagnostics



## Gelman Rubin Test

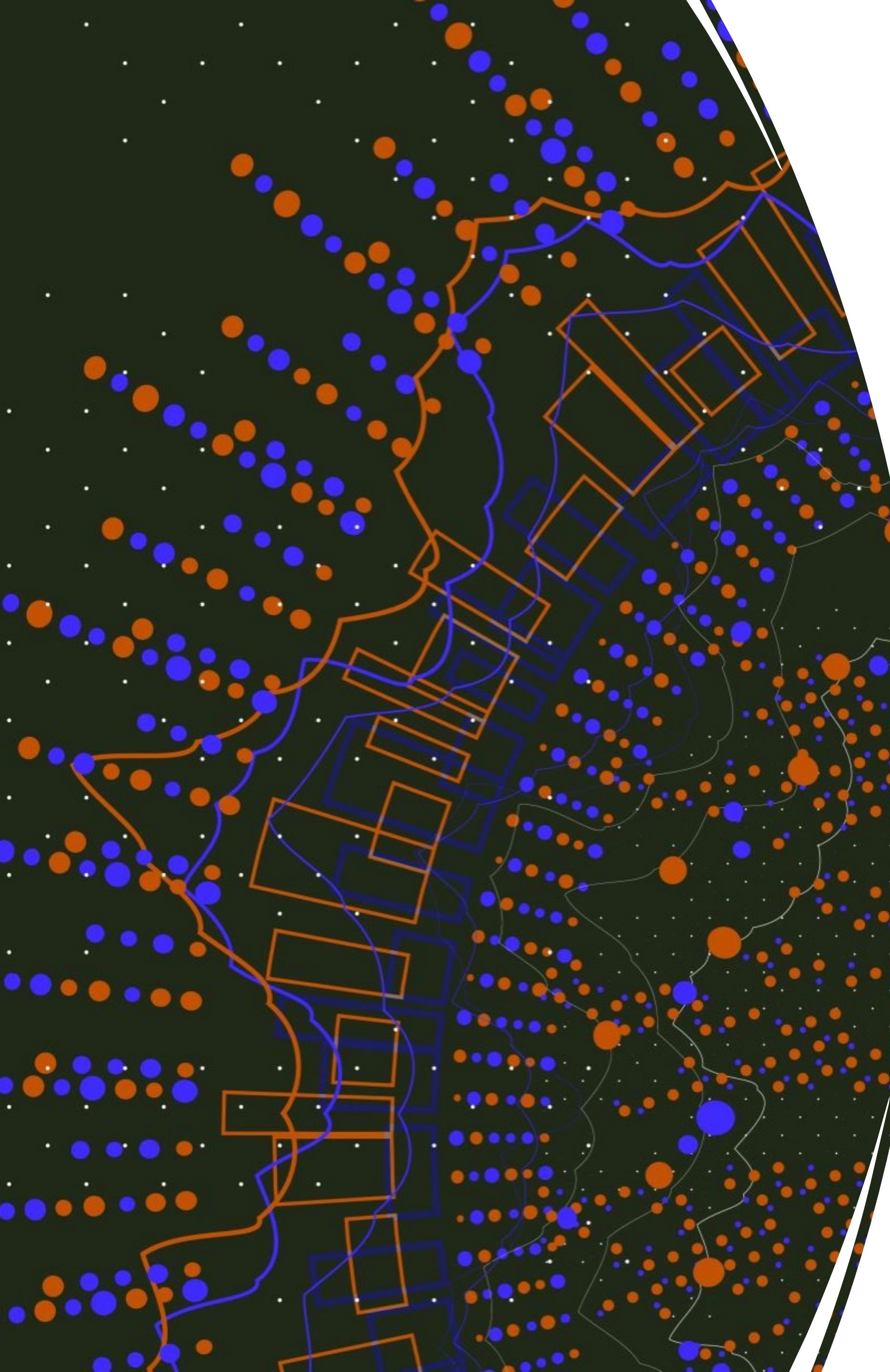
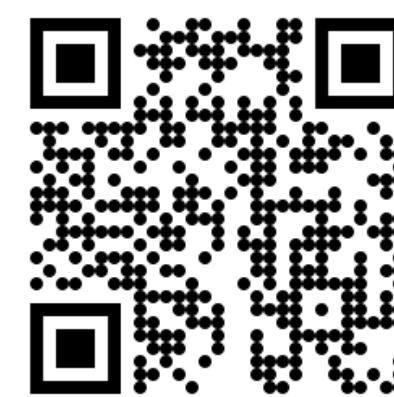


## Correlation Length

Chain 1: 3042  
Chain 2: 2585  
Total samples:  $2.25 \times 10^5$   
Effective sample size: 165

# **7. Conclusions & Next Steps**

**What we achieved and where are we going from here?**



# Summary

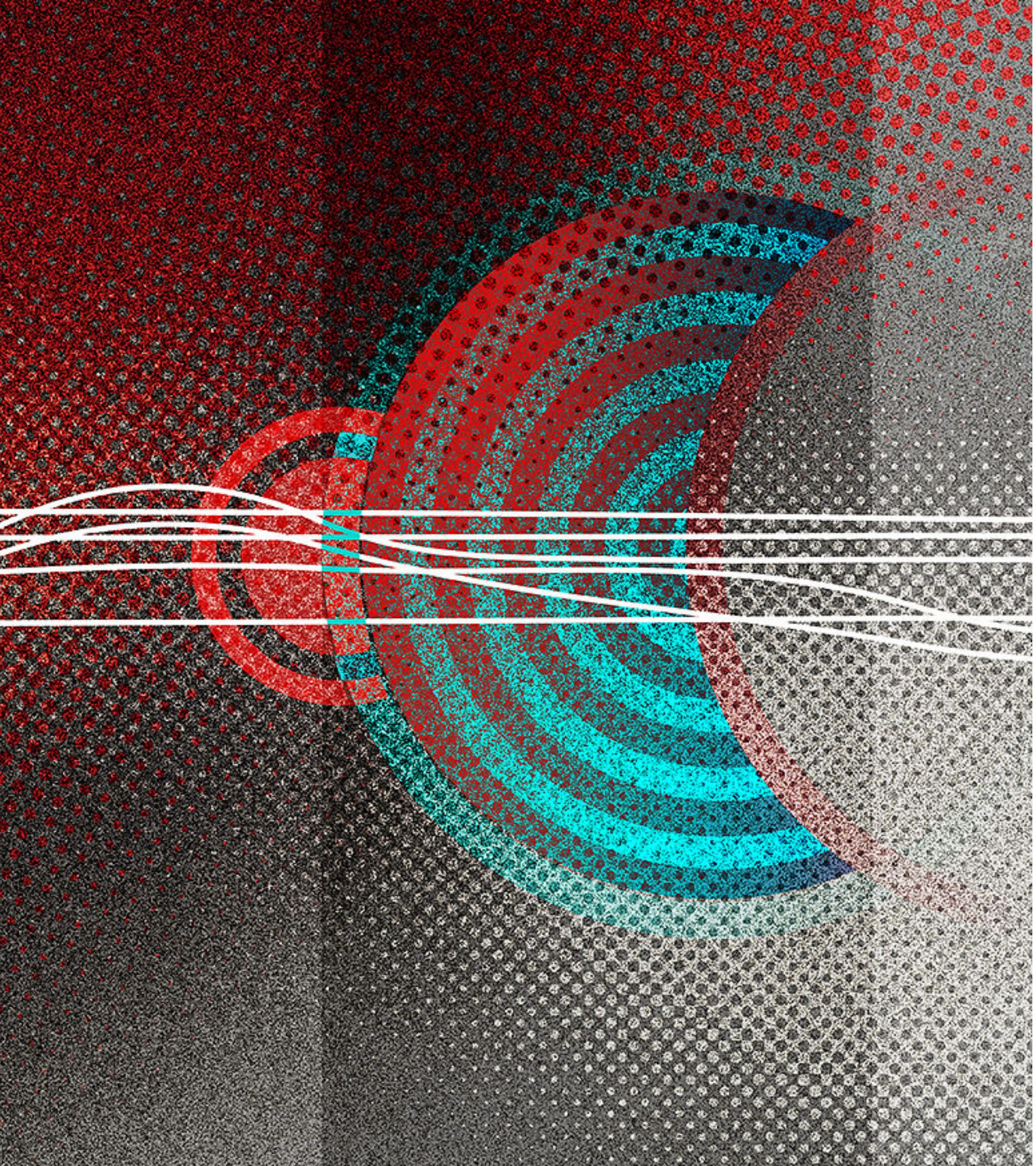
- Next Gen Surveys require Next Gen Cosmological Analysis
- Field Level Inference is an optimal way to extract cosmological information for upcoming cosmological surveys
- Almanac can recover the full sky posterior of high-resolution maps and angular power spectra ( $l_{\text{max}} = 2048!$ )
- We retain the ability to perform systematic contamination checks: EB “leakage”, B-modes, and more
- We can optimally (by construction) infer the largest scales accessible in Euclid/LSST, including their full marginalised posterior
- We can now also infer (aka have an educated guess) mass maps where surveys will not even observe!

## Next:

- A background paper on our new sampler with applications to CMB simulations is on the way.
- Applications to Stage III Survey Data
- Cosmological analysis from point estimates (by Javier Lafaurie)
- Cosmological analysis using normalising flows
- Primordial non-gaussianities with Weak Lensing Fields

# Thanks!

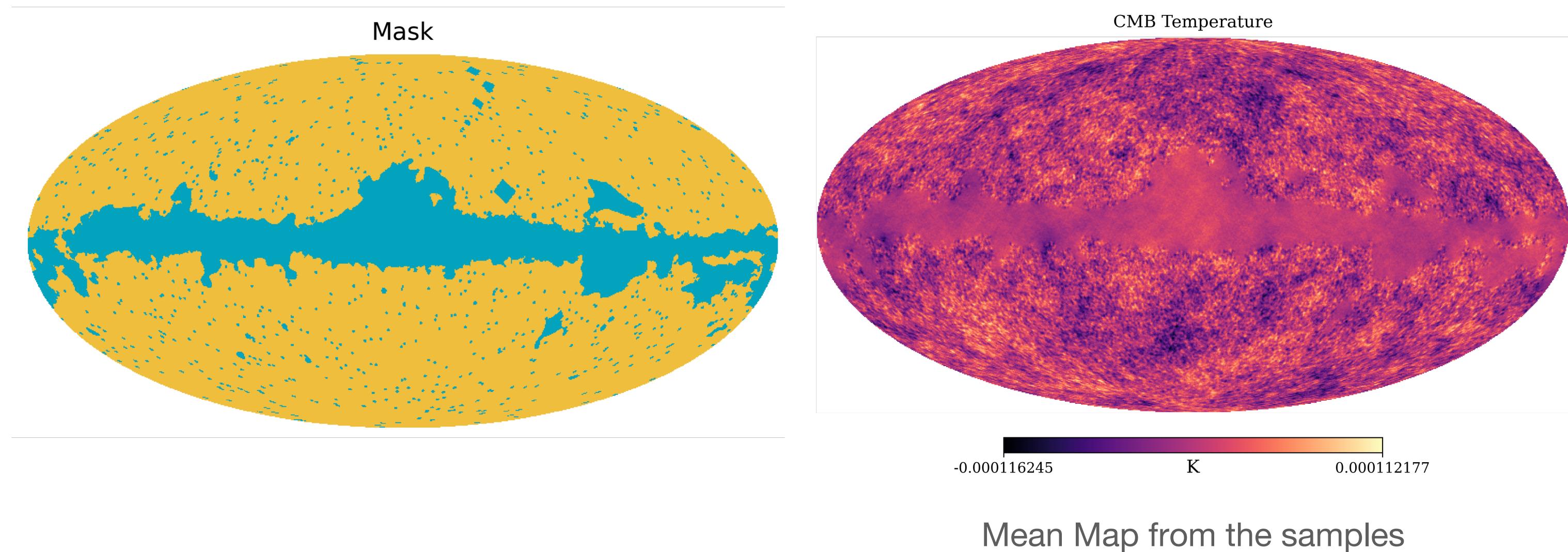
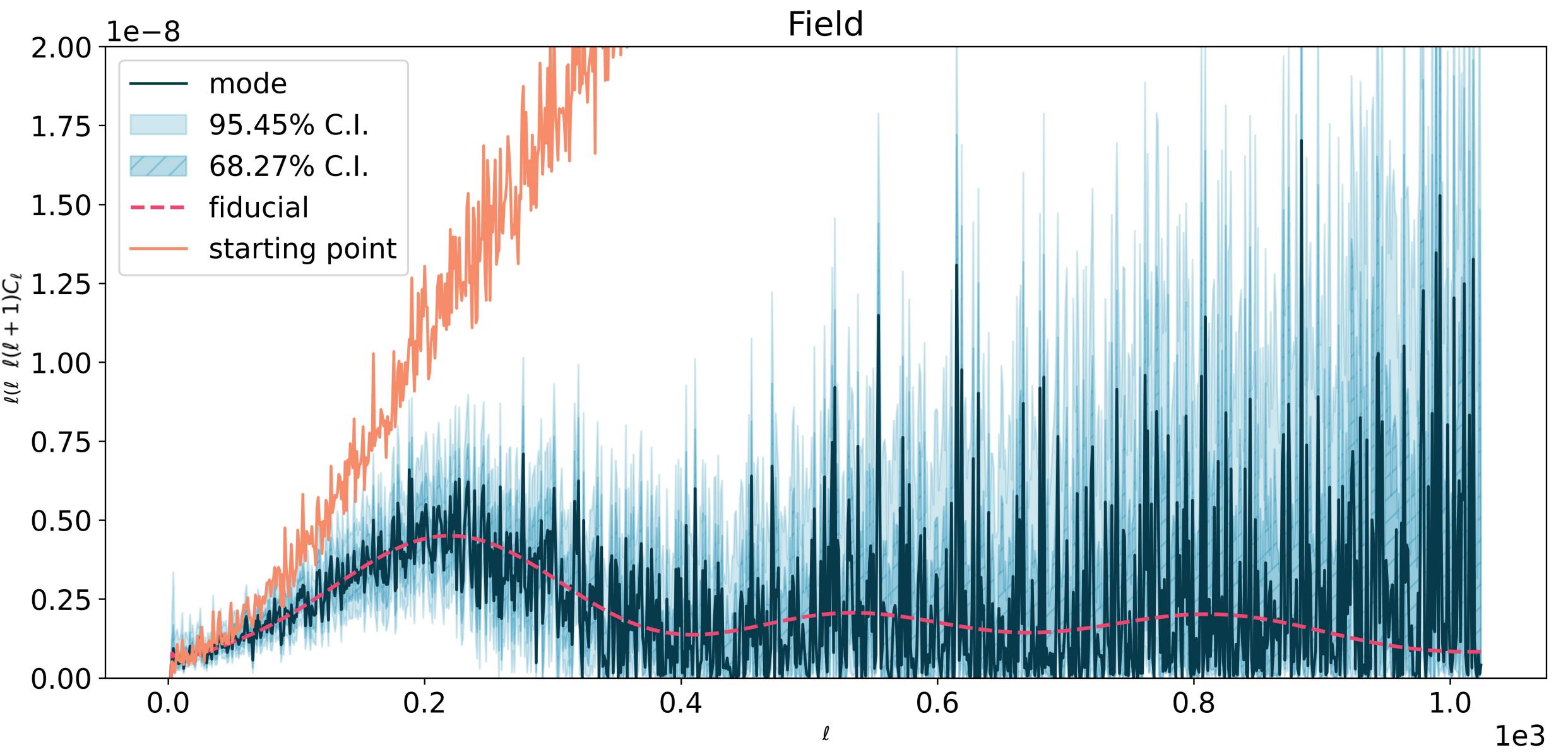
[arthur.loureiro@fysik.su.se](mailto:arthur.loureiro@fysik.su.se)



# CMB Temperature

## Low Signal-to-noise case

- Temperature-only
- Single channel simulation
- Multipole range: 2, 1024
- Nside: 512 (3.14M pixels)
- Noise level:  $1\text{e}-6 \text{ K/pixel}$
- WMAP-Like Mask



# CMB Polarisation

## Mid Signal-to-noise

- Polarisation only, no EB-cross
- Single channel simulation
- Multipole range: 2, 1024
- Nside: 512 (3.14M pixels)
- Noise level: 2e-6 K / pixel
- WMAP-Like Mask

