

$$\begin{cases} q(w, x) = a(wx)^2 + bwx \\ y = a(w_0 x)^2 + bw_0 x + \varepsilon \\ \hat{y} = q(w, x) \end{cases}$$

$$\mathcal{L}_i(w) = \frac{1}{2b} \sum_i \left[\varepsilon_i - (q(w, x_i) - q(w_0, x_i)) \right]^2$$

$$\begin{aligned} \partial_w \mathcal{L}_i(w) &= -\frac{1}{b} \sum_i \varepsilon_i q'(w, x_i) + \underbrace{\frac{1}{b} \sum_i (q(w, x_i) - q(w_0, x_i)) q'(w, x_i)}_{= \lim_{b \rightarrow \infty} \partial_w \mathcal{L}(w)} \end{aligned}$$

Show that at w^* st $q(w^*, x) = q(w_0, x) \quad \forall x$

$$p(x) = ax^2 + bx + c = a(x - x_0)^2$$

$$q(w, x) = (wx - w_0 x)^2 = (w - w_0)^2 x^2$$