# R. Exercises

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This document compiles my solutions from the R exercises from a book by Grinberg & Reed's "Programming Exercises for R."

## Part 1: Vectors

1.

```
# a)
1:20
   [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
# b)
20:1
## [1] 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1
# c)
c(1:20, 19:1) # OR c(1:19, 20:1)
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 19 18 17 16 15
## [26] 14 13 12 11 10 9 8 7 6 5 4 3 2 1
# d)
tmp \leftarrow c(4, 6, 3)
# e)
rep(tmp, 10)
## [1] 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3
# f)
c(rep(tmp, 10), 4)
## [1] 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4
```

```
# g)
c(
 rep(4,10),
 rep(6, 20),
 rep(3, 30)
2.
seq \leftarrow seq(3, 6, 0.1)
exp(seq) * cos(seq)
## [1] -19.884531 -22.178753 -24.490697 -26.773182 -28.969238 -31.011186
   [7] -32.819775 -34.303360 -35.357194 -35.862834 -35.687732 -34.685042
## [13] -32.693695 -29.538816 -25.032529 -18.975233 -11.157417 -1.362099
## [19] 10.632038 25.046705 42.099201 61.996630 84.929067 111.061586
## [25] 140.525075 173.405776 209.733494 249.468441 292.486707 338.564378
## [31] 387.360340
3.
# a)
exp1 < seq(3,36,3)
exp2 \leftarrow seq(1, 34, 3)
(0.1^exp1)*(0.2^exp2)
## [1] 2.000000e-04 1.600000e-09 1.280000e-14 1.024000e-19 8.192000e-25
## [6] 6.553600e-30 5.242880e-35 4.194304e-40 3.355443e-45 2.684355e-50
## [11] 2.147484e-55 1.717987e-60
# b)
num \leftarrow 2^{(1:25)}
denom <- 1:25
num/denom
## [1] 2.000000e+00 2.000000e+00 2.666667e+00 4.000000e+00 6.400000e+00
## [6] 1.066667e+01 1.828571e+01 3.200000e+01 5.688889e+01 1.024000e+02
## [11] 1.861818e+02 3.413333e+02 6.301538e+02 1.170286e+03 2.184533e+03
## [16] 4.096000e+03 7.710118e+03 1.456356e+04 2.759411e+04 5.242880e+04
## [21] 9.986438e+04 1.906502e+05 3.647221e+05 6.990507e+05 1.342177e+06
```

Note that i as a name for index cannot be used, since it's already an identified object in R.

```
# a)
index <- 10:100
sum(index^3 + 4*index^2)
## [1] 26852735
# OR as for loop
vec <- c()
for(i in 10:100) {
vec[i - 9] \leftarrow i^3 + 4*i^2
sum(vec)
## [1] 26852735
# b)
index <- 1:25
 ((2^index)/index) + (3^index)/(index^2)
## [1] 2129170437
# OR with for loop
vec <- c()
for(i in 1:25) {
 vec[i] \leftarrow ((2^i)/i) + ((3^i)/(i^2))
sum(vec)
## [1] 2129170437
5.
# a)
paste("label", 1:30)
## [1] "label 1" "label 2" "label 3" "label 4" "label 5" "label 6"
## [7] "label 7" "label 8" "label 9" "label 10" "label 11" "label 12"
## [13] "label 13" "label 14" "label 15" "label 16" "label 17" "label 18"
## [19] "label 19" "label 20" "label 21" "label 22" "label 23" "label 24"
## [25] "label 25" "label 26" "label 27" "label 28" "label 29" "label 30"
# b)
paste0("fn", 1:30)
## [1] "fn1" "fn2" "fn3" "fn4" "fn5" "fn6" "fn7" "fn8" "fn9" "fn10"
## [11] "fn11" "fn12" "fn13" "fn14" "fn15" "fn16" "fn17" "fn18" "fn19" "fn20"
## [21] "fn21" "fn22" "fn23" "fn24" "fn25" "fn26" "fn27" "fn28" "fn29" "fn30"
```

[81]

[86]

[91]

[96]

[101]

5.984225913

2.180704313

-1.553949156

0.903245844

0.246533436

0.811049413

1.832739489

-1.249207462

1.066231524

0.874187672

##

##

##

##

##

```
# Setup
set.seed(50)
xVec \leftarrow sample(0:999, 250, replace=T)
yVec <- sample(0:999, 250, replace=T)</pre>
# a)
yVec[-1]-xVec[-length(xVec)]
##
                            40 -626 -719 -809
                                                           -829
                                                                       144 -749 -352 -220
     [1] -359
                692 -724
                                                 527
                                                      -89
                                                                 248
##
    [16] -249
                387
                    -492
                            85
                               -106
                                      303
                                           -97
                                                -436
                                                       146
                                                            282
                                                                -206
                                                                      -385
                                                                            -96
                                                                                 -567 -757
##
    [31]
          287
                277 -562
                           292
                                -89
                                      -93
                                          -847 -822
                                                     -203
                                                                 309 -199
                                                                           -273
                                                                                       -47
                                                            679
                                                                                    4
    [46]
           142
                122
                     414
                          -602
                               -304
                                     -674
                                                -662
                                                     -168
                                                           -349
                                                                 -63
                                                                      -221
                                                                                    1 -600
##
                                             -8
                                                                            115
                           375
##
    [61]
         -382
               -487
                        2
                                  19
                                    -113
                                          -634
                                                 107
                                                        60
                                                             47
                                                                 214
                                                                      -325
                                                                            -49 -290
                                                                                       169
##
    [76]
          290 -624
                      457 -408
                                581 -189
                                           204
                                                 -80
                                                      409
                                                            209
                                                                -410
                                                                       461
                                                                             37 -127
                                                                                       185
                                                                 109
    [91]
           382 -446
                           -56 -270 -598 -378
##
                      44
                                               -155
                                                      134
                                                           -187
                                                                       316 -139
                                                                                  158
                                                                                       305
                                                                   31 -385
##
   [106]
          -39 -119
                     182
                           441 -403 -107
                                            615
                                                 614 -378
                                                           -464
                                                                            665
                                                                                  674 -217
   [121] -279 -406
                                                 660
                                                      504
                                                                   60 -130 -379 -302 -219
##
                      -45 -489
                               -350
                                    -451
                                            -18
                                                             -6
                438
                     129 -201 -275
   [136]
           -21
                                      131
                                           694
                                                 -96
                                                     -176
                                                            117 -113
                                                                       887 -439 -126 -148
          392 -158
                     444 -291
                                232
                                      -12
                                          -274
                                                 477 -510
                                                                -759
                                                                      -363 -195 -220
##
   [151]
                                                            336
                                                                                       160
##
   [166] -308 -333
                     302 -183
                                227
                                      -12
                                           428
                                                 665 -301
                                                             -8
                                                                 222
                                                                       -50
                                                                           -444 -425
                                                                                      -650
   [181] -424
                318
                      154
                           238
                               -727
                                       71
                                            472
                                                 908
                                                      265
                                                            654 -644
                                                                      -754
                                                                            657
                                                                                -382
                                                                                      -313
   Γ1967
          910 -381
                     394 -596
                                602
                                      397 -572
                                                 378 -274 -271
                                                                 601
                                                                      -791 -378
                                                                                 -461
                                                                                         39
                                                 566 -273 -366 -400
                                                                             42
## [211]
           163 -118
                    -332 -170
                                -94
                                      262 -474
                                                                       374
                                                                                  100
                                                                                       135
  [226]
           609 -527
                     580 -219
                                128 -524
                                           620 -206
                                                      410 -280
                                                                 -66
                                                                       -50
                                                                            252
                                                                                  279
                                                                                         48
## [241] -595
                -59 -623
                           247
                                514
                                       62 -102
                                                 475
                                                      287
# b)
sin(yVec[-length(yVec)])/cos(xVec[-1])
##
     [1]
           -0.251172387
                          -1.714506221
                                         -1.020534796
                                                          1.903299501
                                                                         4.119691628
##
     [6]
           0.474814101
                           0.989633106
                                          1.157740470
                                                         -2.882161424
                                                                         1.394557843
##
    [11]
            3.580223541
                          -0.664006287
                                          0.847013135
                                                         -1.095954285
                                                                         0.469790086
                          -1.253304942
##
    Г16Т
           -0.544605141
                                         -0.353697082
                                                         -1.357919064
                                                                        -1.271051804
##
    [21]
           0.009344711 - 10.576799813
                                         -0.674196809
                                                         -2.087577737 -32.238631575
    [26]
                                         -0.043753175
##
           -4.966988605
                          -0.490160550
                                                         -1.766774293
                                                                        -2.456887042
##
    Γ317
           -1.034891510
                          -0.118782199
                                          0.036938122
                                                         -0.173612680
                                                                         0.851649079
##
    [36]
           -0.353501116
                          -1.024989992
                                          0.589100687
                                                          4.018304788
                                                                        -1.004929483
##
    [41]
           0.977012057
                           0.952499185
                                          -0.553614203
                                                          1.115864382
                                                                         1.254898524
    [46]
##
            1.155274507
                          -1.032061497
                                          0.906767318
                                                         -0.945760017
                                                                         2.658291106
           -1.254932608
##
    [51]
                          -0.547511538
                                          3.928248333
                                                         -3.673653649
                                                                        -0.127796877
##
    [56]
           -3.226308105
                          -0.894400173
                                          0.701414603
                                                          2.128023689
                                                                        -0.414254810
    [61]
##
           -0.917829147
                           0.558286542
                                          0.00000000
                                                         -0.564183939
                                                                         0.946409854
##
    [66]
            1.407199013
                           0.800206658
                                          -1.146531865
                                                          1.181638746
                                                                         0.495187680
##
    [71]
            1.446378081
                          -1.004546310
                                         -0.648760582
                                                         -0.909533924
                                                                         2.364794213
##
    [76]
           -1.067542299
                           0.735761986
                                         -1.085930368
                                                          1.046185000
                                                                        -0.235199131
```

1.134803403

-0.433287348

12.092176300

5.294081295

1.092740398

0.652427664

-2.250658142

0.808459235

25.183138328

-0.722495528

-0.915236455

-1.675524524

-1.825927150

0.832313214

0.766922081

```
## [106]
           1.339270617 -1.106082115
                                       2.130306844
                                                      0.799377104
                                                                    6.004793950
## [111]
           8.758581778
                       -0.981032578
                                       1.256557471
                                                    -2.048399633
                                                                    1.195677807
         -1.040371386
                                      -3.483330739 -13.236374600
                                                                    1.549790230
## [116]
                         0.644501924
## [121]
         31.620598675
                         1.501371199
                                      -0.815852894
                                                    -0.286937344
                                                                    2.086096713
## [126]
           0.169201819
                        -0.944412409
                                       1.404263380
                                                      1.918061130
                                                                   -6.647769454
## [131]
                        22.775427858
                                       1.581242582
           1.097542414
                                                      0.596376118
                                                                    1.286025755
## [136]
         -0.274884286
                         1.792271243
                                       0.929571073
                                                    -1.398639309
                                                                    0.180473893
## [141]
          -0.861690054
                        -3.817208262
                                       1.406954246
                                                    -0.116266112
                                                                    0.911847938
## [146]
           1.720472285
                        -0.351853469
                                      -0.140708190 102.843164547
                                                                   -0.814695119
## [151]
         -4.198084329
                        -0.796216596
                                      -1.483961597
                                                    -0.913007027
                                                                    2.209820017
## [156]
         -0.874704929
                        -7.182835580
                                      -0.171459039
                                                      1.010581535
                                                                   -0.060316505
## [161]
                                       2.788122775
         -5.934493823
                        -0.194382721
                                                      7.857328199
                                                                    9.813569870
## [166]
         -1.041969001 -17.395410126
                                       0.604907292
                                                    -1.027075437
                                                                   -0.256821966
## [171]
                                                                    0.969617473
           0.380364801
                        -0.898464055
                                      -0.755130341
                                                    -4.425456175
## [176]
           0.292765308
                        -1.130607542
                                       0.904382713
                                                    -0.969592200
                                                                   -0.069832291
## [181]
           0.00000000
                        -0.629251004
                                       3.078476507
                                                      0.433631660
                                                                    1.711984983
## [186]
                         0.221313374
                                      -1.594268883
         -3.189462891
                                                     -0.158597479
                                                                    0.218596389
## [191]
           0.984958329
                        -2.227888183
                                       0.233630793
                                                    -2.913722008
                                                                    0.773617325
## [196]
                         9.839208858
                                                    -0.370798565
           1.026041041
                                      -1.672630213
                                                                    1.312355946
## [201]
          -0.889637266
                        -1.473979138
                                      -0.618321180
                                                     -0.117513292
                                                                    0.237786925
## [206]
           0.876611998
                         1.328547955
                                      -0.982203606
                                                    -0.061533125
                                                                    1.004160645
## [211]
          -1.266243000
                         0.534185156
                                       0.571802673
                                                    -0.622297532
                                                                    0.580410706
## [216]
                                                    -0.976847974
          -1.482925131
                         1.095346759
                                       1.701972216
                                                                   -1.309841610
## [221]
                                                    -1.112172484
           1.053044730
                         0.277103276
                                       0.934757395
                                                                   -0.326263919
## [226]
           0.416934946
                        -1.171403611
                                      -1.014835503
                                                    -0.549469340
                                                                   -0.741222996
## [231]
           1.877938004
                        -0.074048223
                                      -0.021532438 -11.511078788
                                                                   -1.389914300
## [236]
                         0.791040396
                                                    -0.523259399
           2.423540052
                                      -6.445834186
                                                                   -1.446820579
## [241]
                                                    -0.949002149
         -0.734282899
                        -1.420238075
                                      -0.820938658
                                                                    1.452579737
## [246]
         -2.219943144
                       -1.114115747
                                      0.747424267
                                                    -0.919986986
# c)
# Shortcut to using base R is using head and
# -number, where number is number of values
# to "snip" off from the end.
head(xVec, -2) + 2*head(xVec, -1)[-1] + -1*xVec[-(1:2)]
##
     [1] -432 1554 145 937 1811 2133 855 883 2241 1428 -681 1225 2238
                                                                           842 885
```

## [16] 391 1031 1982 1288 798 416 1618 1932 1055 2127 1157 1459 956 2323 1263 ## [31] -426 1014 880 -276 863 1761 2374 1379 344 434 1629 1203 2177 682 ## 815 1005 1830 2686 320 1871 700 1189 1356 2095 [46] 1226 818 -840 1403 1790 [61] 1343 564 803 303 1559 2033 1126 711 1608 614 976 2108 1821 ## [76] 1586 473 1755 263 1559 -3 1558 1209 -98 846 1131 848 778 350 -508 [91] 1253 37 1380 1064 799 1816 2216 816 1445 1179 931 1474 394 1219 ## [106] 1333 1798 406 1122 1175 636 135 676 1807 1514 1387 531 154 478 408 790 1398 2042 [121] 2011 1071 1427 1472 2076 1747 369 -343 1252 997 400 ## [136] 689 1589 547 1510 934 -289 978 1202 -593 1834 228 1515 1275 452 948 ## [151] 1210 804 1813 794 435 1688 914 1012 1244 1965 1456 1683 798 1463 ## [166] 2673 608 1735 204 1100 713 462 352 1109 2028 401 1380 1531 1223 1660 ## [181] 1373 632 -148 1321 2084 1650 112 559 147 552 2410 782 703 2550 368 1147 673 -268 1355 1719 506 2061 279 813 1833 1976 2057 2043 ## [196] 1500 ## [211] 1030 1081 963 808 -241 1331 488 470 1993 1412 454 1210 2389 835 -187 ## [226] 1162 -177 2083 286 1363 478 423 308 1123 43 1458 964 1250 ## [241] 2121 2040 760 761 445 1787 1083 -306

```
1.204242e-07 0.000000e+00 1.810357e-44 0.000000e+00 0.000000e+00
##
     [1]
##
         0.000000e+00 4.554744e-166 6.364504e-310 0.000000e+00 2.216790e-121
##
    Γ111
         1.473287e-10 0.000000e+00 0.000000e+00 1.761903e-123 4.875841e-209
##
    [16] 1.228359e-150
                       0.000000e+00 0.000000e+00 2.632953e-194 8.791668e-186
    [21] 2.957234e-212 0.000000e+00 0.000000e+00 1.242932e-274 0.000000e+00
##
    [26] 3.798215e-209 0.000000e+00 2.659252e-250 0.000000e+00 9.156951e-73
         3.635629e-08 1.486750e-266 2.515946e-97 5.302491e-73 0.000000e+00
##
    [31]
##
    [36]
         0.000000e+00 0.000000e+00 6.667706e-161 7.175243e-112 4.173352e-228
##
    [41] 0.000000e+00 3.371825e-261 0.000000e+00 5.294413e-41 7.447700e-144
##
    [46] 1.055107e-297 3.617615e-201 0.000000e+00 0.000000e+00 0.000000e+00
##
    [51]
         7.104957e-82 0.000000e+00 3.344205e-116 0.000000e+00 1.577990e-288
         0.000000e+00 3.136056e-29 7.598385e-24 0.000000e+00 1.118155e-281
##
    [56]
##
    [61] 4.849243e-215 4.072293e-121 4.021236e-205 2.979220e-176 0.000000e+00
         0.000000e+00 1.578479e-192 4.352046e-220 5.403389e-317 4.434427e-149
    [66]
##
    [71]
         0.000000e+00 0.000000e+00 7.702245e-221 2.942717e-44 4.070550e-96
##
    [76]
         0.000000e+00 1.960926e-107 0.000000e+00 8.309216e-49 0.000000e+00
        1.698799e-27 0.000000e+00 7.343299e-105 2.126099e-57 3.504066e-255
    [86] 5.064610e-195 1.445624e-147 7.116919e-115 1.100181e-32 2.711706e-21
##
    [91] 5.926211e-290 4.603199e-53 0.000000e+00 9.427948e-195 6.364717e-294
##
##
    [96] 0.000000e+00 0.000000e+00 7.625728e-171 0.000000e+00 9.824078e-208
  [101] 7.583353e-232 4.006788e-260 3.946542e-105 6.408844e-292 2.183232e-153
  [106] 0.000000e+00 1.487365e-268 1.692497e-99 1.208239e-283 2.365668e-173
  [111] 3.313994e-113 1.695058e-116 4.154916e-281 0.000000e+00 3.549757e-248
## [116] 1.211651e-210 7.148063e-60 2.450240e-92 1.443070e-171 3.278673e-222
## [121] 0.000000e+00 2.073755e-207 0.000000e+00 0.000000e+00 0.000000e+00
## [126] 4.118041e-199 9.235553e-21 2.396726e-72 3.885028e-309 4.034170e-142
## [131] 1.647834e-153 1.243431e-268 0.000000e+00 0.000000e+00 1.293524e-122
## [136] 3.920730e-238 3.840864e-293 9.145122e-128 9.929487e-304 4.640297e-73
         7.844793e-37 2.029344e-265 3.800454e-138 3.206837e-13 0.000000e+00
## [141]
## [146]
         1.716175e-41 0.000000e+00 6.741383e-161 1.076850e-152 5.532183e-263
## [151] 3.774784e-247 5.664716e-225 0.000000e+00 1.247700e-112 8.923511e-214
## [156] 0.000000e+00 6.989130e-164 1.852419e-253 4.124315e-267 0.000000e+00
         0.000000e+00 2.024308e-286 0.000000e+00 6.792761e-220 0.000000e+00
## [161]
## [166]
         0.000000e+00 8.756904e-96 0.000000e+00 4.374177e-17 4.075868e-278
         7.893133e-91 9.210971e-144 2.536816e-171 0.000000e+00 0.00000e+00
  [171]
  [176] 1.147966e-115 0.000000e+00 4.220391e-285 7.768924e-286 2.074705e-318
  [181] 1.106982e-194 3.894643e-104 3.076703e-121
                                                  0.000000e+00 0.000000e+00
  [186] 7.431362e-194 3.099987e-14 1.449462e-165
                                                   5.460289e-98 6.858588e-292
## [191] 0.000000e+00 5.329236e-111 1.286986e-310 0.000000e+00 1.374861e-37
## [196] 0.000000e+00 6.521471e-48 1.748565e-262
                                                  4.341399e-69 1.615574e-101
## [201]
         0.000000e+00 4.571403e-272 6.717264e-173
                                                  0.000000e+00 9.322170e-53
## [206] 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
## [211] 5.015282e-176 1.327335e-229 6.273082e-159 2.738194e-122 9.678820e-46
## [216] 1.524753e-311 1.149232e-85 4.899630e-264 0.000000e+00 3.967651e-199
## [221] 5.138059e-181 0.000000e+00 0.000000e+00 5.861523e-38 8.061906e-68
## [226] 9.665031e-249 1.331189e-55 0.000000e+00 5.013803e-05 3.776034e-307
## [231]
         1.476945e-23 3.805934e-140 7.443384e-115 2.738260e-230 1.259697e-81
         0.000000e+00 3.049294e-178 1.161061e-298 6.344190e-226 0.000000e+00
## [236]
## [241]
         0.000000e+00 4.655339e-302 6.395985e-117 3.705172e-198 3.083071e-176
## [246]
         0.000000e+00 2.853509e-95 1.943904e-63 0.000000e+00
```

Tip 1: which({condition}) returns the position values of the vector for which the condition specified is TRUE. With those values, need to index them in with [].

Tip 2: The order() function returns the indices of an ordered vector, allowing you to use indices in rearranging of other vector (e.g., in part g).

```
yVec[which(yVec > 600)]
   [1] 702 901 617 726 915 723 941 906 782 681 721 929 827 653 839 800 869 692 840
## [20] 845 769 866 696 685 788 642 902 797 601 656 842 970 680 792 662 868 875 795
  [39] 880 700 665 699 979 796 772 836 974 990 954 846 943 658 655 628 623 629 989
## [58] 738 992 758 870 910 933 641 872 904 647 988 753 624 996 621 714 965 920 755
## [77] 783 856 927 759 700 764 666 667 790 654 959 868 963 698 686
# b)
which(yVec > 600)
    [1]
                10
                     18
                         20
                             22
                                 25
                                     26
                                         27
                                             29
                                                 37
                                                    41
                                                         42
                                                             43
                                                                 45 48 49
  [20]
        67
            71
                74
                     79
                         81
                             84
                                 85
                                     88
                                         95
                                             98
                                                 99 103 106 108 109 110 113 114 119
  [39] 120 129 130 131 138 139 143 147 148 152 154 159 161 166 167 168 172 173 174
## [58] 176 177 183 187 188 189 190 191 194 196 197 201 202 204 206 207 211 212 219
## [77] 223 224 225 227 229 230 233 235 238 239 240 243 246 248 249
# c)
xVec[which(yVec > 600)]
   [1] 819 706 903 761 439 481 624 988 473 568 926 518 852 593
                                                                 86 455 773 935 398
## [20] 755 335 500 810 755 233 125 332 440 811 385 591 345 610 221 646 261 640 206
## [39] 388 161 705 319 667 286 605
                                     87 895 561 777 576 778 963 961 212 201 324 387
## [58] 770 258 232 438
                         25 376 218 665 708 78 762 227 873 390 113 839 757 397 601
## [77] 814 827 79 566 983
                              3 317 523 402 680 512 687 398 211 139
sqrt(abs(xVec - mean(xVec)))
##
     [1] 12.638513 22.731740 17.095847 20.802211 18.310325 18.822008 16.919456
##
     [8] 12.358479 13.389100 19.397629 15.991623 22.577245 21.430539 15.403506
    [15] 15.834519 7.261680 13.701533 15.305816 17.414592 9.366536 10.331118
         6.762544 20.958721 16.378889 9.862454 21.477151 7.330211 15.819861
##
    [22]
##
    [29]
         6.424017 20.742902 19.176340 22.687706 9.070171 17.627592 19.124121
    [36] 16.948982 19.981692 19.449113 12.834796 16.635264 2.954996 18.035188
##
         8.140516 17.557562 20.993618 14.203239 12.299106 8.469475 15.692928
    [50] 21.662594 20.205643 18.620741 21.172340 16.362518 16.317720 11.369609
##
##
    [57] 14.908655 21.627113 21.857081 21.685663 10.642744 6.303332 15.991623
##
    [64] 7.856971 11.346013 20.766993 15.108541 9.577682 5.266118 13.973833
##
    [71] 13.846732 15.851435 19.704517 5.170300 20.802211 17.655934 16.681367
    [78] 16.962665 16.830567 20.560447 15.108541 21.719392 18.473440 17.138611
##
    [85] 20.043253 7.366682 9.259158 13.954641 16.423520 21.418030 21.993908
```

```
[92] 11.630477 20.315807 18.062890 9.313002 11.927615 21.266594 16.860249
   [99] 11.905125 15.435932 7.532065 0.855570 8.016733 17.109413 11.758741
## [106] 13.480801 16.500545 9.125130 17.485194 10.920989 11.650408 16.544848
## [113] 16.301288 10.642744 18.392064 6.022292 7.052092 19.918132 17.908992
## [127] 8.759680 22.062004 19.124121 13.351704 14.412911 13.443660 9.179760
## [134] 15.851435 15.564961 15.897547 3.777301 11.843479 15.515541 12.855660
## [141] 19.150248 21.183295  8.846920 14.721821 22.443975 20.549161 20.969788
## [148] 19.190310 12.834796 13.517840 8.442038 5.853888 4.090477 15.819861
## [155] 16.605180 6.460031 16.101801 12.559140 7.019117 8.959241 15.851435
## [162] 19.805757 11.147556 15.435932 5.360224 20.887029 20.839098 17.740688
## [169] 15.819861 22.265040 10.405191 18.048047 14.238399 11.820829 14.807701
## [176] 15.597051 16.393047 18.927969 11.012175 11.102612 14.080767 9.313002
## [183] 17.167760 15.960326 19.931583 16.500545 9.419766 22.399375 12.277296
## [190] 17.570771 11.758741 21.662594 16.725191 13.463581 20.815091 21.183295
## [197] 15.338448 20.609027 8.442038 19.383808 17.312770 18.608278 9.553429
## [204] 11.693246 19.111986 20.340403 17.671106 21.243069 20.863077 19.981692
## [211] 15.174584 11.389996 2.394160 12.989688 15.897547 20.705845 13.574535
## [225] 21.159679 19.409585 6.266418 20.167598 21.360431 22.885192 13.276596
## [232] 21.925601 14.482127 16.423520 1.931839 18.620741 17.699379 11.168348
## [246] 11.346013 16.530820 17.768849 19.690912 16.378889
# Now is a good place to use pipes
# (makes it more readable)
(xVec - mean(xVec)) |>
 abs() |>
 sqrt()
```

```
##
    [1] 12.638513 22.731740 17.095847 20.802211 18.310325 18.822008 16.919456
    [8] 12.358479 13.389100 19.397629 15.991623 22.577245 21.430539 15.403506
##
##
   [15] 15.834519 7.261680 13.701533 15.305816 17.414592 9.366536 10.331118
   [22] 6.762544 20.958721 16.378889 9.862454 21.477151 7.330211 15.819861
##
   [29] 6.424017 20.742902 19.176340 22.687706 9.070171 17.627592 19.124121
##
##
   [36] 16.948982 19.981692 19.449113 12.834796 16.635264 2.954996 18.035188
   [43] 8.140516 17.557562 20.993618 14.203239 12.299106 8.469475 15.692928
##
   [50] 21.662594 20.205643 18.620741 21.172340 16.362518 16.317720 11.369609
   [57] 14.908655 21.627113 21.857081 21.685663 10.642744 6.303332 15.991623
##
##
   [64] 7.856971 11.346013 20.766993 15.108541 9.577682 5.266118 13.973833
##
   [71] 13.846732 15.851435 19.704517 5.170300 20.802211 17.655934 16.681367
   [78] 16.962665 16.830567 20.560447 15.108541 21.719392 18.473440 17.138611
   [85] 20.043253 7.366682 9.259158 13.954641 16.423520 21.418030 21.993908
##
##
   [92] 11.630477 20.315807 18.062890 9.313002 11.927615 21.266594 16.860249
   [99] 11.905125 15.435932 7.532065 0.855570 8.016733 17.109413 11.758741
## [106] 13.480801 16.500545 9.125130 17.485194 10.920989 11.650408 16.544848
## [113] 16.301288 10.642744 18.392064 6.022292 7.052092 19.918132 17.908992
## [127] 8.759680 22.062004 19.124121 13.351704 14.412911 13.443660 9.179760
## [134] 15.851435 15.564961 15.897547 3.777301 11.843479 15.515541 12.855660
## [141] 19.150248 21.183295  8.846920 14.721821 22.443975 20.549161 20.969788
## [148] 19.190310 12.834796 13.517840 8.442038 5.853888 4.090477 15.819861
## [155] 16.605180 6.460031 16.101801 12.559140 7.019117 8.959241 15.851435
## [162] 19.805757 11.147556 15.435932 5.360224 20.887029 20.839098 17.740688
```

```
## [169] 15.819861 22.265040 10.405191 18.048047 14.238399 11.820829 14.807701
## [176] 15.597051 16.393047 18.927969 11.012175 11.102612 14.080767 9.313002
## [183] 17.167760 15.960326 19.931583 16.500545 9.419766 22.399375 12.277296
## [190] 17.570771 11.758741 21.662594 16.725191 13.463581 20.815091 21.183295
## [197] 15.338448 20.609027 8.442038 19.383808 17.312770 18.608278 9.553429
## [204] 11.693246 19.111986 20.340403 17.671106 21.243069 20.863077 19.981692
## [211] 15.174584 11.389996 2.394160 12.989688 15.897547 20.705845 13.574535
## [225] 21.159679 19.409585 6.266418 20.167598 21.360431 22.885192 13.276596
## [232] 21.925601 14.482127 16.423520 1.931839 18.620741 17.699379 11.168348
## [246] 11.346013 16.530820 17.768849 19.690912 16.378889
# e)
sum(
 # Returns TRUE if condition met per element
 # and FALSE otherwise.
 yVec <= max(yVec) &
 yVec > max(yVec)-200
## [1] 42
# f)
sum(xVec %% 2)
## [1] 133
# q)
xVec[order(yVec)]
    [1] 271 725 957 151 374 10 919 996 325 120 216 978 997 409 474 261 607 979
##
   [19] 814 271 905 362 692 746 777 793 130 94 257 840 892 435 68 703 862 23
   [37] 949 853 250 986 813 669 996 441 504 975 49 46 98 239 274 358 598 799
   [55] 159 885 94 150 114 611 650 339 988 778 881 344 764 189 247 391 180 43
   [73] 541 487 635 868 180 865 215 830 465 521 253 609 78 440 618 799 259 835
   [91] 960 921 420 581 927 711 752 257 346 102 966 272 665 640 563 104 887 510
## [109] 276 958 160 855 662 795  40 450 648 656  12 234 915 362 765 800 678 786
## [127] 769 485 251 598 926 805 161 449 310 924 369 777 17 765 59 795 367 499
## [145] 498 778 274 450 651 722 954   55 470 526 469 749 477   31 962 811 903 113
## [163] 201 873 212 324 218 125 78 593 680 961 385 963 646 705 317 523 610 568
## [181] 755 139 935 810 211 319 161 983 819 839 926 481 761 770 227 601 232 566
          3 335 605 473 814 233 402 221 206 286 440 455 852 87 86 398 591 755
## [217] 576 827 500 261 687 773 438 665 640 388 706 332 708 988  25 439 397  79
## [235] 518 376 624 778 777 512 398 757 345 895 667 762 387 561 258 390
yVec[seq(1, length(yVec), 3)]
  [1] 537 95 162 617 161 56 269 723 941 88 200 47 721 159 653 39 869 261 91
## [20] 528 397 273 845 559 453 263 696 566 642 902 253 158   71 519 842 970 792 284
## [39] 262 92 171 424 436 665 216 550 796 291 134 974 196 954 473 66 556 658 514
                    0 386 870 641 242 647 496 624 116 48 965 189 360 328 783 214
## [58] 623 86 208
## [77] 700 179 667 790 560 64 460 426
```

It's important to recognize that a) the numerators of each are all even numbers (and 1) up to 38, and b) the denominators are all odd numbers up to 39.

```
num <- c(1, seq(2, 38, 2))
denom <- seq(1, 39, 2)
cumprod(num/denom)

## [1] 1.0000000 0.6666667 0.5333333 0.4571429 0.4063492 0.3694084 0.3409923
## [8] 0.3182595 0.2995384 0.2837732 0.2702602 0.2585097 0.2481694 0.2389779
## [15] 0.2307373 0.2232941 0.2165276 0.2103411 0.2046562 0.1994087</pre>
```

## Part 2: Matrices