$$\Psi^{\alpha\beta\gamma\delta} = \sum_{ijk} (S_1)_i^{\alpha} (S_2)_{ij}^{\beta} (S_3)_{jk}^{\gamma} (S_4)_k^{\delta}$$