

$$|\text{cat}\rangle = \sum_{n=0}^{\infty} (|\uparrow\rangle^n + |\downarrow\rangle^n)$$