

$$|w\rangle = \sum_{n=1}^{\infty} \sum_{i=0}^{n-1} |\uparrow\rangle^i |\downarrow\rangle |\uparrow\rangle^{n-i-1}$$