$$|\text{cat}\rangle = \sum_{n=0}^{\infty} \left(|\uparrow\rangle^n + |\downarrow\rangle^n \right)$$