

ATLAS Experiment  
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# Particle Physics An Introduction

Module 1:  
Matter and forces, measuring and counting  
Part 1.2a: Natural units

For those who are unfamiliar with the system of natural units, we will briefly introduce it.

Planck's constant  $\hbar$  and speed of light  $c$ :

$$\begin{aligned}\hbar &\equiv \frac{h}{2\pi} \simeq 1.055 \times 10^{-34} \text{ J s} \\ c &\simeq 2.998 \times 10^8 \text{ m/s}\end{aligned}$$

Units in the international system:

$$\begin{aligned}[\hbar] &= \frac{ML^2}{T} = \frac{\text{kg m}^2}{\text{s}} \\ [c] &= \frac{L}{T} = \frac{\text{m}}{\text{s}}\end{aligned}$$

“Natural“ units:

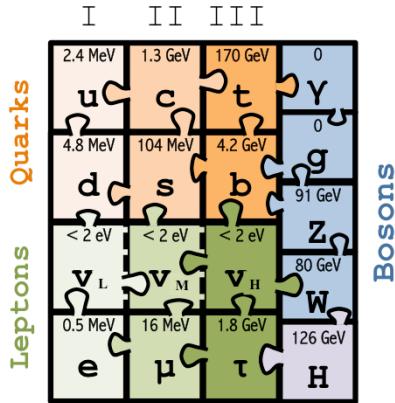
$$\begin{aligned}\hbar = c &\equiv 1 \quad ; \quad [\hbar] = [c] = 1 \\ [e] = [\sqrt{\hbar c}] &= [1] \quad ; \quad \alpha = \frac{\frac{1}{4\pi} \frac{e^2}{\hbar/mc}}{mc^2} = \frac{e^2}{4\pi\hbar c} \simeq \frac{1}{137}\end{aligned}$$

- High energy physics deals with relativistic quantum processes. The scale of the action is thus characterized by Planck's constant  $\hbar$ , the scale of velocities is given by the speed of light  $c$ .
- In the system of natural units, we set  $\hbar = c = 1$ . This means that we define  $\hbar$  as the unit of action, and  $c$  as the unit of velocity. In such a system, 1s is equal to approximately  $3 \times 10^8$  m.
- As an added value, the electric charge is now dimensionless. It often shows up as the fine structure constant  $\alpha$ , which is the electrostatic potential energy of two electrons at unit distance, divided by the mass of the electron. This constant is equal to 1/137 to a good approximation.

Basic unit: electronvolt (eV)  $\equiv$  energy gained by an electron in a potential difference of 1V:

$$[E, M, p] = \frac{ML^2}{T^2} = \text{eV}$$

$$1 \text{ GeV} = 10^9 \text{ eV} \simeq M_p$$



Quantity	Conversion factor	Natural units	IS units
Mass	$1 \text{ kg} = 5.61 \times 10^{26} \text{ GeV}$	GeV	$\text{GeV}/c^2$
Length	$1 \text{ m} = 5.07 \times 10^{15} \text{ GeV}^{-1}$	$\text{GeV}^{-1}$	$\hbar c/\text{GeV}$
Time	$1 \text{ s} = 1.52 \times 10^{24} \text{ GeV}^{-1}$	$\text{GeV}^{-1}$	$\hbar/\text{GeV}$

- The system of natural units is of great practical value, since it eliminates a lot of constants from the equations. It thus makes them less heavy and more easy to understand.
- The basic unit, the electronvolt (eV) is defined as the gain in energy of an electron when it traverses a potential difference of 1V.
- In the system of natural units, the electronvolt is the common unit of energy, momentum and mass.
- A billion of these units corresponds roughly to the mass of the proton,  $M_p$ , and thus sets the natural scale of high energy physics.
- Whenever you want to convert a result to units of the International System, this table can be useful.