1:

INPUT: array size m;Lower limit of value L;Lower limit of value R;whether the values is unique;

OUTPUT: array a

 $a \leftarrow Emptyarray()$

 $n \leftarrow R - L + 1$

 ${f if}$ unique is true ${f then}$

if ln(n+1) < 1 + log((n-m)+1) **then**

for $i \leftarrow 1$ to m do

while u exits in a **do**

 $u \leftarrow rand(L, R)$

end while

append Integer u to a

end for

else

for $i \leftarrow L$ to R do

append i to a

end for

 $a \leftarrow shuffle(a[1, m])$

end if

 ${f else}$

for $i \leftarrow L$ to R do

 $u \leftarrow rand(L, R)$

while u exits in a do

 $u \leftarrow rand(L,R)$

end while

append Integer u to a

end for4

end if

 $\mathbf{return}\ a$

2

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INPUT: Number of nodes of the tree n;
OUTPUT:Pairs Arrays edge
for i \leftarrow 2 to n do
u \leftarrow rand(1,i-1)
v \leftarrow i
edge append \{u, v\}
end for
{\bf return}\ edge
3:
INPUT: Number of nodes of the graph n; Number of edge of the graph m;
OUTPUT:Pairs Arrays edge
for i \leftarrow 2 to n do
u \leftarrow rand(1,i-1)
v \leftarrow i
edge append \{u,v\}
end for
Upper\ limit \leftarrow n*(n-1)/2
if ln(Upper\ limit+1) < 1 + log((Upper\ limit-m)+1) then
for i \leftarrow n to m do
while u = v or edge exits \{u, v\} do
u \leftarrow rand(1, n)
v \leftarrow rand(1, n)
if u > v do
swap(u, v)
end do
end while
edge append \{u, v\}
end for
else
while size(a) < m do
a append \{i, j\} where 1 \le i < j \le n and \{i, j\} not exits in a
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end while
end if
{f return} \ a
4:
INPUT: Number of nodes of the graph n; Number of edge of the graph m;
\mathbf{OUTPUT:}Pairs Arrays edge
for i \leftarrow 2 to n do
u \leftarrow rand(1, i - 1)
v \leftarrow i
edge append \{u, v\}
end for
Upper\ limit \leftarrow n*(n-1)
if ln(Upper\ limit+1) < 1 + log((Upper\ limit-m)+1) then
no\ ring \leftarrow true
for i \leftarrow n to m do
while u = v or edge exits \{u, v\} do
u \leftarrow rand(1, n)
v \leftarrow rand(1, n)
if no \ ring = true and u < v do
swap(u, v)
end if
end while
edge append \{u, v\}
no\ ring \leftarrow false
end for
else
a append \{j, i\} where 1 \le i < j \le n and \{j, i\} not exits in a
while size(a) < m \text{ do}
a append \{i, j\} where \{i, j\} not exits in a
end while
end if
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```
return a
```

5:

INPUT: Number of nodes of the graph n; Number of edge of the graph m; struct Arrays $edge\ with\ value$;

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\mathbf{OUTPUT}: ture \text{ or } false
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 $graph[][] \leftarrow \text{empty Two-dimensional arrays}$

for $\{u, v, w\}$ in edge with value do

$$graph[u][v] = w$$

end for

 $stk \leftarrow \text{empty } stack$

$$st[] \leftarrow \{true\}$$

$$dist[] \leftarrow \{0\}$$

$$cnt[] \leftarrow \{0\}$$

stk push i where $1 \le i \le n$

while $size(stk) \neq 0$ do

 $t \leftarrow \text{the top of } stk$

pop the top of stk

$$st[t] = false$$

for $target \leftarrow 1$ to n do

if graph[t][target] no null and dist[target] > dist[t] + graph[t][target] do

 $dist[target] \leftarrow dist[t] + graph[t][target]$

 $cnt[target] \leftarrow cnt[t] + 1$

if $cnt[target] \ge n$ do

 ${\bf return}\ true$

end if

if st[target] = false do

st[target] = true

push target into stk

end if

end if

end for

```
end while
return false
6:
INPUT: Number of nodes of the graph n; Number of edge of the graph m;
\mathbf{OUTPUT}:Pairs Arrays edge
graph[][] \leftarrow \text{empty array}
for i \leftarrow 2 to n do
u \leftarrow rand(1, i - 1)
v \leftarrow i
edge append \{u, v\}
graph[u][v] = true
end for
set[2] \leftarrow \text{empty array}
function dfs(u, father, color)
append u to set[color]
for j \leftarrow 1 to n do
if graph[u][j] = true and j \neq father do
call dfs(j, u, color \ xor \ 1)
end if
end for
end funtion
call dfs(rand(1, n), 0, 0)
for i \leftarrow n to m do
while u \neq v and \{i, j\} no exits in edge do
u = rand(set[0])
v = rand(set[1])
end while
append \{u, v\} to edge
end for
return edge
```

7:

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INPUT: Number of nodes of the graph n;
OUTPUT:Pairs Arrays edge
top[] = \{0\}
fa[] = \{0\}
graph[][] = 0
for i \leftarrow 2 to n do
u \leftarrow rand(1, i - 1)
v \leftarrow i
edge append \{u, v\}
graph[u][v] = true
end for
function dfs(x, father, grand father)
top[x] = grand\ father
fa[x] = father
link\ son \leftarrow j where j is any one of graph[x][j] = true
call dfs(link\ son, x, grand\ father)
for j \leftarrow 1 to n do
if graph[x][j] = true and j \neq link son do
\mathbf{call}\ dfs(j,x,j)
end if
end for
end function
root \leftarrow rand(1,n)
\mathbf{call}\ dfs(root, 0, root)
vis[] = \{false\}
for i \leftarrow 1 to n do
if vis[top[i]] = false and top[i] \neq i and top[i] \neq fa[i] do
vis[top[i]] = true
append \{i, top[i]\} to edge
end if
end for
```

 ${\bf return} \,\, {\bf edge}$