# Experiments, Distributions, and Simulation

#### 2023-01-10

## Question 12.1

I currently work at a B2B technology company specializing in conversational analytics. From a a business perspective, experiment design is important when building generalized models (or studies) that span across industries. If we just took the data "as-is", the results of the model would not be valid, and could even be misleading! Some of the resons why a poorly designed study would yield biased results are listed below:

- 1. Some companies have volumne that is orders of magnitude higher than others (Fortune 500 vs startup)
- 2. Different industries have vastly different service structure (Bank vs Hardware Store)
- 3. Sales interactions are very different from Customer Service interactions
- 4. Some businesses are seasonal, some are cyclical, some are uniform
- 5. Etc

In order for our model to be valid, we need to ensure we control for as many biased and confounding factors as we can, while still keeping meaningful features. To do this, techniques like Stratification, Blocking, Randomization, and Weighting are applied.

## Question 12.2

In this section, we explore the concept of factorial design with the goal of reducing a set of 10 binary features into 16 options to be shown in a survey. We first note that, in this case, Full Factorial design is impractical given that there are 1024 possible feature combinations  $(2^{10})$ .

```
library(FrF2)
homeFeat = FrF2(16, 10, default.levels = c('Yes', 'No'))
homeFeat
```

```
##
        Α
##
               No
           No
                    No Yes Yes
                                 No
                                    Yes
                                         No
                                             Yes
      Yes Yes Yes Yes
                        No
                            No
                                 No
                                     No
                                        Yes
                    No Yes
                            No Yes Yes Yes
               No Yes Yes Yes
                                 No
      Yes
           No
                                     No Yes
                                              No
      Yes Yes
               No
                    No
                        No Yes Yes Yes
                                              No
##
       No
           No Yes Yes
                        No Yes Yes Yes
                                          No
                                              No
## 7
       No Yes Yes
                    No Yes Yes
                                 No
                                              No
               No Yes Yes
       No Yes
                            No Yes
                                    Yes
                                         No
                                              No
## 9
      Yes
          Yes
               No Yes
                        No Yes Yes
                                     No
                                          No
## 10 Yes Yes Yes
                        No
                    No
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           No Yes Yes Yes
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                        No Yes Yes
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       No Yes
              Yes Yes Yes
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       No Yes
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                    No Yes
                             No Yes
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       No
           No
               No Yes
                        No
                             No
                                 No Yes Yes Yes
## class=design, type= FrF2
```

## Question 13.1

In this section we give a pair of examples of data that is expected to follow some common distributions.

- 1. Binomial
  - a. Throwing a pair of dice e.g P(sum > 6)
  - b. Drawing cards from a deck e.g P(drawing a Spade)
- 2. Geometric
  - a. Baby gender e.g P(boy after having 2 girls)
  - b. Shooting a basketball e.g P(making 1st try)
  - NOTE: The same data can be framed as a Binomial or a Geometric problem! It depends on the question.
- 3. Poisson
  - a. Website visitors per hour e.g P(105 visitors if  $\lambda$ =100)
  - b. Number of credit card applications per day e.g P(1000 applications if  $\Lambda$ =500)
- 4. Exponential
  - a. Ticket purchases e.g P(50 days prior)
  - b. Demand for a new videogame e.g P(50k sold)
- 5. Weibull
  - a. Lifetime of electronics e.g P(screen lasting 10000 hours)
  - b. Car Maintenance e.g P(breakdown within 6 months)
  - NOTE: Again, the same data can be framed in different ways! The Weibull distribution can, in fact, transform into a Normal or an Exponential distributions with the right parameters!

## Question 13.2

In this section we simulate a 2-step airport queue. The goal of the simulation is to find the number of Service representatives and the number of Self-serve scanners to keep the long term wait time under 15 minutes.

Here is as snippet of how the simulation system works:

- P1 arrives at t = [0.16500462]
- P2 arrives at t = [0.17214336]
- P3 arrives at t = [0.37305445]
- P1 time in ServiceQueue = [0.8528443]
- P1 time in ScanQueue = [0.87501753]
- P1 leaves at [1.04002215]
- P4 arrives at t = [1.10415736]
- P5 arrives at t = [1.66829429]
- P2 time in ScanQueue = [1.21356498]
- P2 leaves at [2.25358713]
- P6 arrives at t = [2.3361185]
- P3 time in ScanQueue = [0.50517184]
- P3 leaves at [2.75875897]

The code below shows how we can accomplish such a simulation in Python. Key results for t=120 (2 hours) are shown below:

- 1. 1 rep, 1 scanner = 45.83 minute wait
- 2. 2 rep, 2 scanner = 35.67 minute wait
- 3. 5 rep, 5 scanner = 3.5 minute wait
- 4. 4 rep, 4 scanner = 14.4 minute wait

For this set of runs, it looks like 4 reps and 4 scanners give us the best balance of resources vs wait time. Obviously, these results are not fully optimized, but it gives us an idea of what to expect.

```
from random import uniform
import simpy
import numpy as np
import pandas as pd
from scipy.stats import uniform
from scipy.stats import expon
# Parameters
serviceRep_count = 4
pCheck_count = 4
pArrival_time = .2
repService_time = .75
Sim_Time = 100
in_system = []
def p_arrival(env, serviceRep_count, pCheck_count):
    # Assign counts to passengers
   p_counter = 0
   while True:
       # Exponential generator for arrivals
      next_p = expon.rvs(scale = pArrival_time, size = 1)
       # Wait for next person to arrive
      yield env.timeout(next_p)
      arrival_time = env.now
      p_counter += 1
       env.process(pServiceQueue(env, serviceRep_count, p_counter))
       env.process(pScanningQueue(env, pCheck_count, p_counter, arrival_time))
def pServiceQueue(env, serviceRep_count, p_number):
    with service_line.request() as req:
       yield req
        # Exponential distribution for the service process
        serviced = expon.rvs(scale = repService_time, size = 1)
       yield env.timeout(serviced)
       time_service = serviced
def pScanningQueue(env, pCheck_count, p_number, arrival_time):
    with scan_line.request() as req:
       yield req
        # Uniform distribution for the service process
       scanned = uniform.rvs(.5, 1, size = 1)
       yield env.timeout(scanned)
       time_scan = scanned
       departure_time = env.now
       system_time = departure_time[0] - arrival_time[0]
        in_system.append(system_time)
```

```
# Start environment
env = simpy.Environment()
# define resources
service_line = simpy.Resource(env, capacity = serviceRep_count)
scan_line = simpy.Resource(env, capacity = pCheck_count)
## defining the FULL arrival process
env.process(p_arrival(env, service_line, scan_line))
## run the simultion
## <Process(p_arrival) object at 0x1a93d1d84c0>
env.run(until = Sim_Time)
#Wait time
avg_delay = np.mean(in_system)
print('The average delay in system is {}'.format(avg_delay))
```

## The average delay in system is 7.991436413895146