# Analysis of Algorithms: Data Cleanup Algorithms

Garrett Dancik, PhD Fall 2024

Course Notes: <a href="https://gdancik.github.io">https://gdancik.github.io</a>

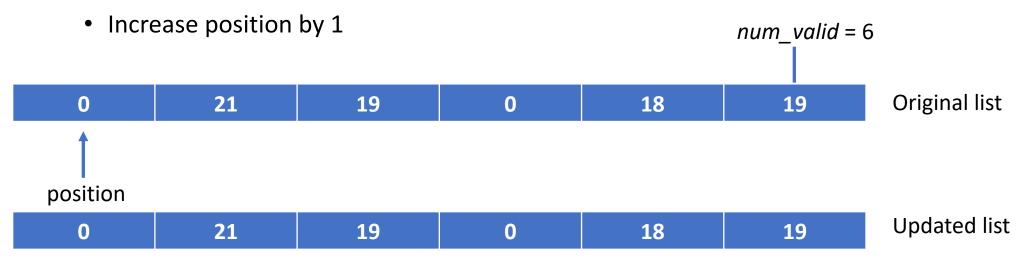
#### What do we mean by Data Cleanup?

- If data contains invalid or missing values, those invalid values should be removed.
  - In a survey, a student does not enter their age (or enters an invalid one)
  - In a survey, a student does not enter their GPA (or enters an invalid one)
- We will assume that missing / invalid values are recorded as 0
- Example data:

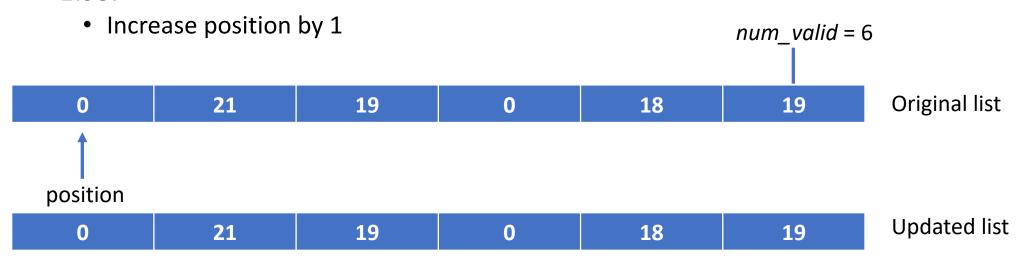


 In this case, we want a list containing only the numbers: 21, 19, 18, and 19

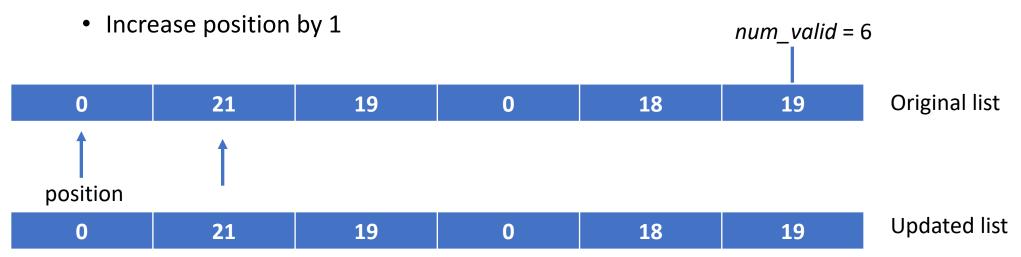
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



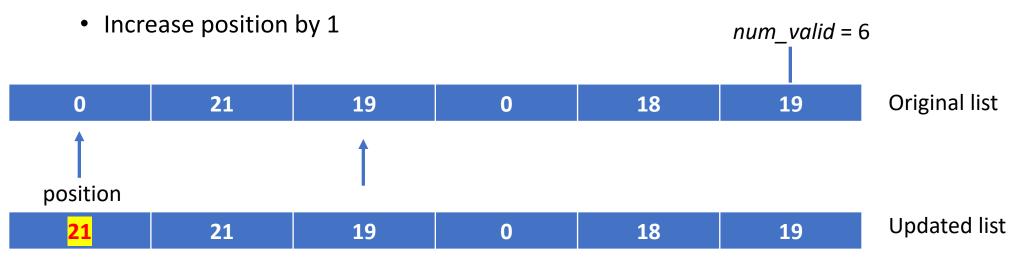
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



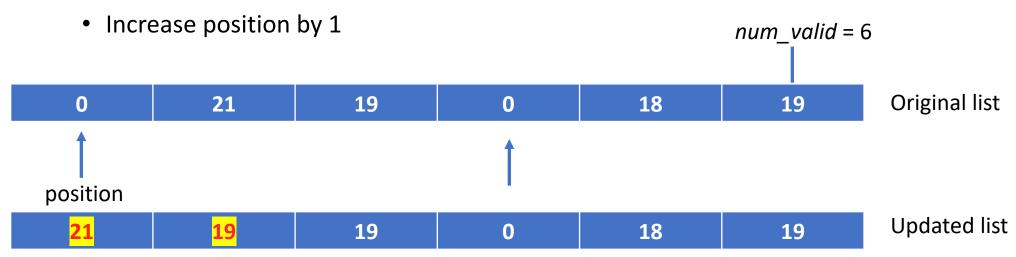
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



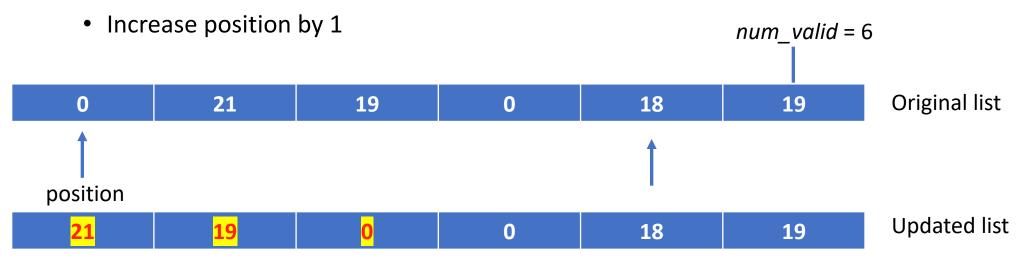
- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., -1:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



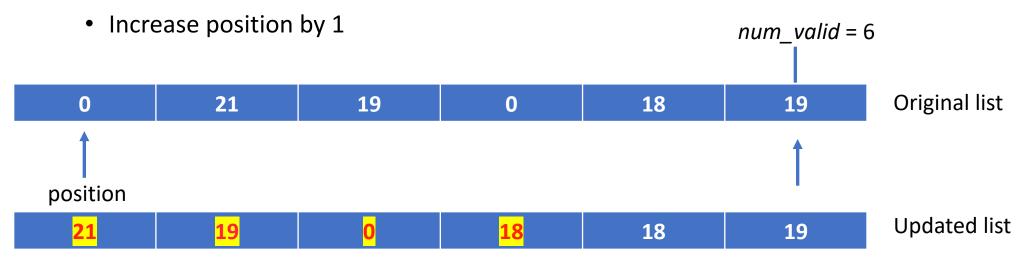
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



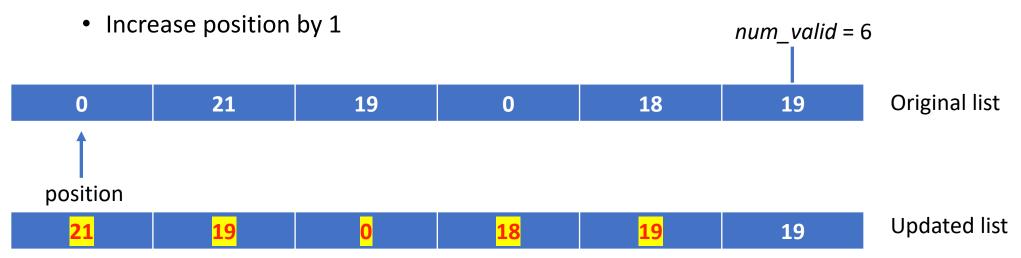
- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



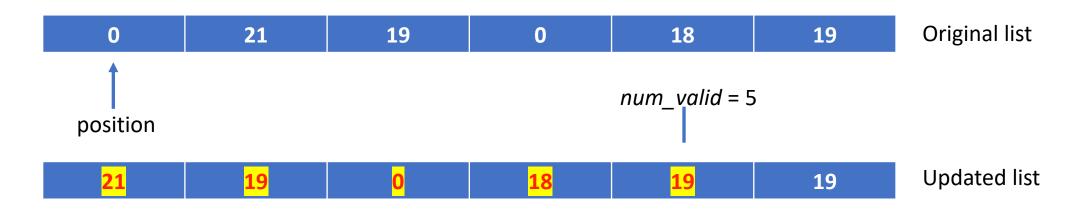
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1



- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All valid numbers to the right of num are shifted 1 position to the left

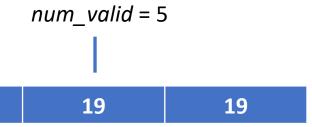
18

0

• Decrease num\_valid by 1

19

- Else:
  - Increase position by 1





21

- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left

18

0

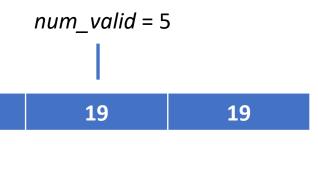
- Decrease num\_valid by 1
- Else:

21

• Increase position by 1

19

position



- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left

position

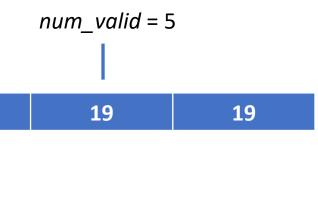
18

- Decrease num\_valid by 1
- Else:

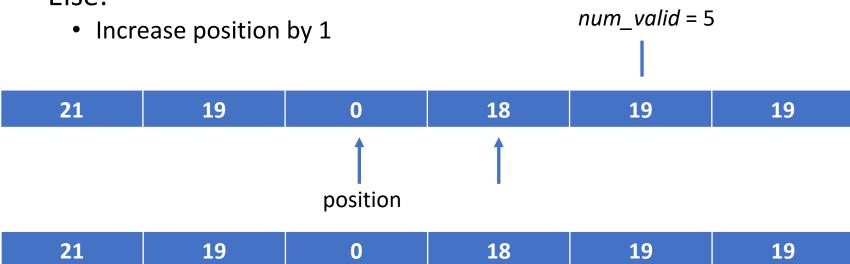
21

• Increase position by 1

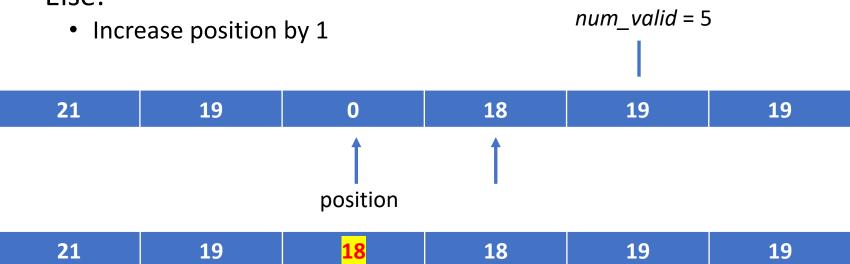
19



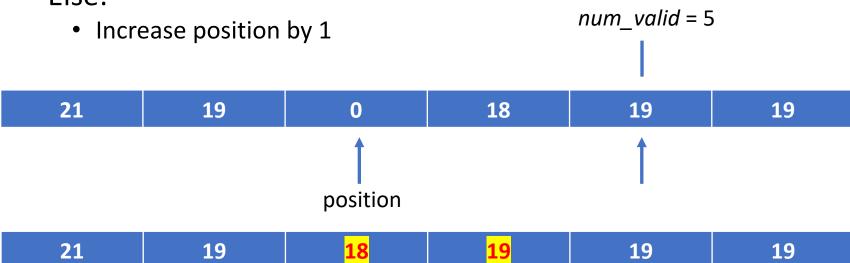
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All valid numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



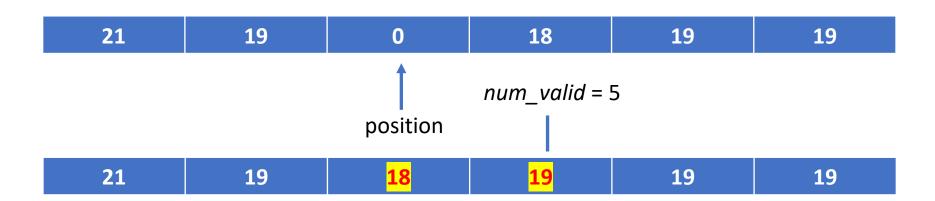
- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



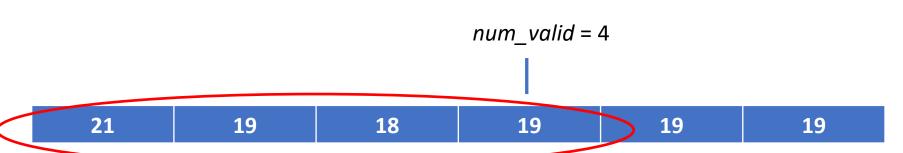
- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:



- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1



- While position <= num\_valid :</li>
  - If *num*[*position*] is invalid, e.g., 0:
    - All valid numbers to the right of num are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1
- The final list, containing 4 valid items, is below:



- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1
- Running time (best case)
  - If *no* numbers are invalid, then the *while* loop is executed n times, where n is the initial size of the list, and the only other operations are the comparison in the *if* statement, and *position* is increased by 1. The running time is  $\theta(n)$ . This is the best case.

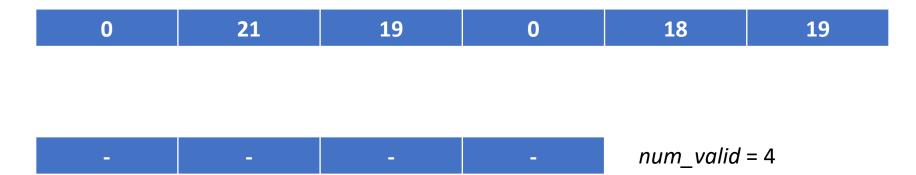
- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All <u>valid</u> numbers to the right of *num* are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1
- Running time (worst case):
  - If *all* the numbers are invalid, then for all *n* passes through the list, n 1 copies (shifts) are made. This is a worst case.
  - The total number of operations in the loop is (ignoring comparisons):
    - For the first position: n + 1 operations: n 1 copies, plus 2 to increase num\_valid and position
    - For the second position: n operations, n-2 copies, plus 2 to increase num\_valid and position
  - The total number of operations is the sum of 1 through n + 1 which equals
    - $n(n+1)/2 + 1 \to \theta(n^2)$

- While position <= num\_valid :</li>
  - If num[position] is invalid, e.g., 0:
    - All valid numbers to the right of num are shifted 1 position to the left
    - Decrease num\_valid by 1
  - Else:
    - Increase position by 1
- Running time:
  - Best case (all entries are valid) is  $\theta(n)$
  - Worst case (all entries are invalid) is  $\theta(n^2)$
  - Average case is also  $\theta(n^2)$
- Space:
  - n (all cases best, worst, and average) (n is required for the original list, plus a few additional variables)

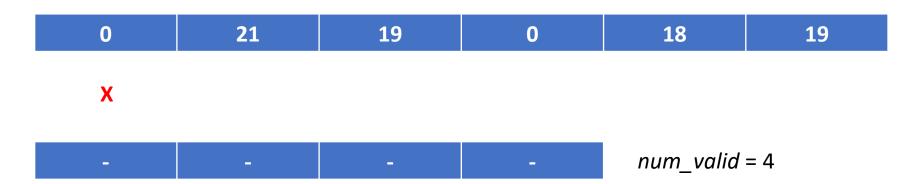
- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



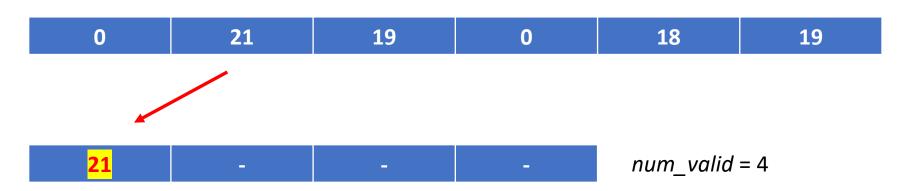
- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase *index* by 1



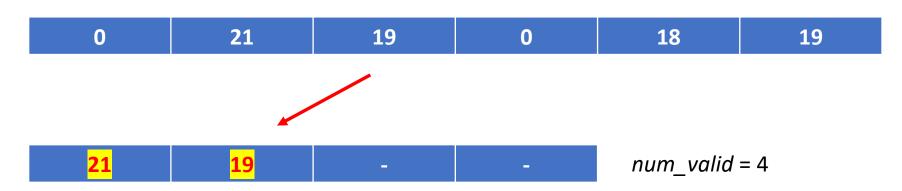
- Find the total number of valid elements in the list, and store in num\_valid
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



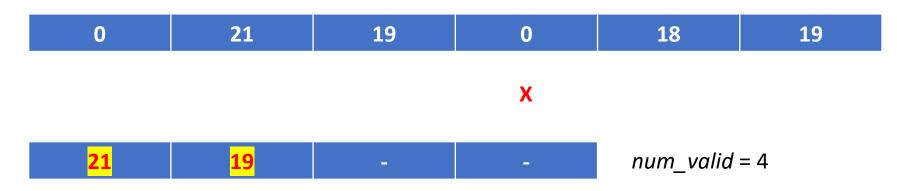
- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



- Find the total number of valid elements in the list, and store in num\_valid
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



- Find the total number of valid elements in the list, and store in num\_valid
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1



- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1

#### • Running time:

- The first step is order *n*, since we need to iterate through all elements in the list to count the number of valid elements. For each element, there is a constant number of operations. (More details for this step are required, but this likely would use a *for* loop).
- The main work then occurs in the *for* loop on the 4<sup>th</sup> line, which is also order *n*. For each element, we either copy it or not, and this is also a constant number of operations for each of the *n* elements.
- The running time is  $\theta(n)$ , in the best, worst, and average cases.

- Find the total number of valid elements in the list, and store in *num\_valid*
- Create an empty list, called copyNum, of length num\_valid
- Set index to 0
- For each num in the original list:
  - If *num* is valid
    - Assign num to copyNum[index]
    - Increase index by 1
- Space (depends on the number of valid elements):
  - Best case: if there are *no* valid elements, then the space only requires the original list, which is *n* (we ignore a few additional variables)
  - Worst case: if *all* the elements are valid, we create an additional copy of the original list. The space requirements are 2*n*.
  - Average case: this depends on the expected number of valid/invalid items, and will be between n and 2n. If the number of valid items is equally likely to be between 0, 1, 2, ...n, then the average space requirement is 1.5n.

#### Converging pointers algorithm

- We keep a *left* and *right* index
  - Set *left* to 0 and *right* to n-1 (index of the last element)
- Set num\_valid to the length of the numbers list
- While left < right</li>
  - If *number[left]* is valid :
    - Increase left by 1
  - Else (number[left] is not valid) :
    - Copy number[right] to number[left]
    - Decrease num\_valid by 1
    - Decrease right by 1
- If number[left] is not valid :
  - Decrease num\_valid by 1



 $num_valid = 6$ 

Item at left is 0, so we copy from right to left, and decrease right and num\_valid by 1.



 $num_valid = 5$ 

Item at left is not 0, so we increase left by 1



 $num_valid = 5$ 

Item at left is not 0, so we increase left by 1



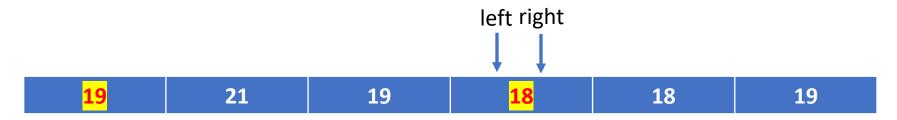
 $num_valid = 5$ 

Item at *left* is not 0, so we increase *left* by 1



 $num_valid = 5$ 

Item at left is 0, so we copy from right to left, and decrease right and num\_valid by 1.



 $num_valid = 4$ 

Item at *left* is not 0 (if it was, we would decrease *num\_valid*).

Once *left* is equal to *right*, we are done

#### Converging pointers algorithm

- While *left < right* 
  - If number[left] is valid:
    - Increase left by 1
  - Else (number[left] is not valid):
    - Copy number[right] to number[left]
    - Decrease num\_valid by 1
    - Decrease right by 1
- If number[left] is not valid:
  - Decrease num\_valid by 1

#### • Running time:

- The main work occurs in the *while* loop. The loop always increases *left* or decreases right, until *left* and *right* are the same. This can only happen n times. All other operations inside the loop are constant, so the running time is  $\theta(n)$ , which is true for the best, worst, and average cases.
- Space: *n* (we need space only for the original list, as well as a few additional terms). This is the most space efficient algorithm

# Data Cleanup Algorithms

	Shuffle-left		Copy over		Converging Pointers	
	Time	Space	Time	Space	Time	Space
Best	$\theta(n)$	n	$\theta(n)$	n	$\theta(n)$	n
Worst	$\theta(n^2)$	n	$\theta(n)$	2n	$\theta(n)$	n
Average	$\theta(n^2)$	n	$\theta(n)$	(n, 2n)	$\theta(n)$	n

• Which algorithm is the *best*?