

Global value chains and the transmission of price shocks

First draft version

Marion Cochard* Guillaume Daudin[†] Violaine Faubert[‡] Antoine Lalliard[§]
Christine Riffart[¶]

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Abstract

Firms' participation in global value chains strengthens cross-country linkages via trade in intermediate inputs. In this paper, we build on two sectoral world input-output datasets to assess the role of global input-output linkages in the propagation of price shocks // exchange rate shocks // in the international economy. We examine the increasing integration of the European economies since the adoption of the common currency and investigate whether the shortening of global value chains in the wake of the Great Recession has changed the propagation of global price shocks. We provide evidence that, following an appreciation of the domestic currency, the direct effect of global price shocks, i.e. the effect resulting from the share of imported final and intermediate goods in domestic consumption, explains the bulk of the propagation of global shocks to domestic consumer prices. By contrast, we find a limited role for the additional transmission of lower domestic input prices to other sectors of the domestic economy and other countries occurring during subsequent production cycles. Finally, building on sectoral data, we examine which sectors experience higher spillovers from global price shocks.

JEL Classification: C67, E31, F42, F62

Keywords: input-output linkages, spillovers, global value chains, cost-push inflation, euro area

1 Introduction

Trade liberalization and lower transportation and communication costs facilitated the fragmentation of production beyond national borders. As a result, firms' participation in global value chains strengthens cross-country linkages via trade in intermediate inputs. Because of imported intermediate goods, fluctuations in the prices of imports that are themselves driven by exchange

*Banque de France, Sciences Po, OFCE. E-mail: marion.cochard@banque-france.fr

[†]PSL, Université Paris-Dauphine, Sciences Po, OFCE. E-mail: gdaudin@mac.com

[‡]Banque de France. E-mail: violaine.faubert@banque-france.fr

[§]Banque de France. E-mail: antoine.lalliard@banque-france.fr

[¶]Sciences Po, OFCE. E-mail: christine.riffart@ofce.sciences-po.fr

rate movements affect the domestic cost of production and, ultimately, domestic consumer prices. As global value chains contribute to explaining the transmission of macroeconomic shocks across countries, a better understanding of trade spillovers has become paramount. In this paper, we build on the World Input-Output tables (WIOT hereafter) to investigate how production linkages give rise to nominal spillovers. We examine the extent to which domestic consumer prices react to changes in imported intermediate and final goods. We pay particular attention to euro area countries. The euro area is indeed more involved in global production chains than other large economies, such as the United States and China (ECB, 2016) and has been less affected by global value chains shortening than other countries in the years following the Great Recession. Building on sectoral data from the World InputOutput Database, we examine which sectors experience higher spillovers from global inflationary shocks.

To preview our findings, we find that...

The remainder of the paper is organized as follows. Section 2 briefly describes the related literature. Section 3 presents the methodology and the data sources. Section 4 presents the impact of an exchange rate shock on consumer prices. Section 5 examines which of the subcomponents of consumer prices experience higher spillovers from global inflationary shocks. Section 6 provides some concluding remarks and avenues for future research.

We improve on the literature on various respects. First, while most of the literature focuses on production prices, we examine the role of input-output linkages in propagating shocks to consumer prices. Secondly, we analyze how sectoral inflation reacts to global inflationary shocks by examining the main components of consumer prices (manufacturing goods, services, food and energy). We draw on the World Input-Output Database to examine which sectors experience higher spillovers from global inflationary shocks.

Thirdly, we provide evidence that, following an appreciation of the domestic currency, the direct effect of global inflationary shocks, i.e. the contribution of first-round effects on imported final and intermediate goods in domestic consumption, explains the bulk of the propagation of global shocks to domestic prices. By contrast, we find a limited role for the additional transmission of lower domestic input prices to other sectors of the domestic economy and other countries occurring during subsequent production cycles.

GD Interestingly, this limited role is additive rather than multiplicative. It adds from 0.02 to 0.04 to the price elasticity

PEUT-ÊTRE We assess whether results are robust to the use of different databases (WIOD versus OECD-ICIO).

2 Related literature

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A recent literature examines whether trade in intermediate inputs is an important source of inflation synchronization across countries. Auer et al. (2017) document that the cross-border propagation of cost shocks through input-output linkages contributes substantially to synchronizing producer price inflation across countries, combining data on sectoral domestic and international input trade from the World Input Output Database (WIOD) and producer price indices. By contrast, exchange rate movements and the degree of pricing-to-market are found to

play no role in synchronizing inflation across countries. Antoun de Almeida (2016) show that the cross-border sectors pairs which trade more intensively with each other in intermediate inputs display higher PPI inflation correlation, indicating price spillovers along the global supply chain.

Our research is also related to the literature on exchange rate pass-through, in particular in an environment where intermediate inputs account for a large share of imports. For instance, Goldberg and Campa (2010) show that imported intermediate inputs are the dominant channel through which changes in import prices pass to CPI inflation.

2.1 The Input-Output model applied to a shock on production costs.

The widely known Leontief's production model (or I-O model) studies the impact of a demand shock in a domestic economy (Leontief, 1951). The trade in value-added analysis reconciles international trade statistics with national I-O tables, and thus allows Leontief's analysis to be extended to an international context. A number of studies (Hummels et al., 2001; Daudin et al., 2006, 2011; De Backer and Yamano, 2012; Johnson and Noguera, 2012; Koopman et al., 2014; Amador et al., 2015; Los et al., 2016) analyze the value added content of world trade. Some authors focus on Asia (Sato and Shrestha, 2014) or on the euro area (Cappariello and Felettigh, 2015).

Leontief's production model has a dual: the price model. Some studies focus on the consequences of a change in production prices based on an I-O model or a SAM (Social Accounting Matrix) model in developing countries. Leontief's price model is broadly used in multi-sector, single-country macroeconomic models, for example, to measure the effect of a change in energy prices (Bournay and Piriou, 2015; Sharify, 2013). Implicitly, Bems and Johnson (2015) use it as they focus on competitiveness and compute real effective exchange rates weighted by the value-added trade structure to measure the impact of a demand change in value added on value added prices and final expenditure levels. It is at the center of Cochard et al. (2016). Cochard et al. (2016) is an accounting approach to the effect of costs on prices ("cost-push inflation"). Firms' margins are assumed to be fixed. Prices only adjust to absorb cost changes, production techniques are fixed during successive production cycles and inputs substitution (for instance, between countries producing the same goods) is not accounted for, despite variations in relative price. The limitations of this approach are well known (Folloni and Miglierina, 1994). In particular, and although the division of global value chains largely takes place within multinational firms, it assumes a unique pricing system based on market prices and independent of firm strategies. Still, this method provides a measure of the vulnerability of each sector to price or productivity shocks (Acemoglu et al., 2012; Carvalho, 2014). Hence, though unrealistic, it is useful for identifying which countries and sectors are under pressure to adjust their prices when subject to exogenous cost shocks. For instance, it can show which euro area countries benefit most from an appreciation of the euro or whether adopting the euro has increased interdependence between member countries.

3 The PIWIM model

Based on initial work from the OFCE (Observatoire Français des Conjonctures Économiques), we developed a model named «PIWIM» (Push cost Inflation through World Input-output Matrices). This paper makes extensive use of this model.

3.1 Defining a price shock in a I-O model

To identify which countries are most affected by a price shock through value-added and vertical trade flows in international trade, we need a large structural matrix that integrates input flows between sectors, both within each country and between countries. This matrix traces the sectoral and geographical origin of inputs.

The standard I-O model relies on input-output tables registering transactions of goods and services (domestic or imported) at current prices. The I-O tables describe the sale and purchase relationships between producers and consumers within an economy. Each column describes, for each industry j , the intermediate consumption of goods and services from the various sectors. By extension, a "world" I-O table (WIOT hereafter) describe the sale and purchase relationships between producers and consumers in the whole world, differentiating between sectors in different countries. The WIOT has, on its diagonal, the country blocks with flows of domestic transactions of intermediate goods and services between industries. The country blocks outside of the diagonal represent international flows of intermediate goods and services via bilateral sectoral exports and imports.

Define Y the output vector of dimension $(1, N)$, \mathcal{A} the matrix of technical input coefficient of dimension (N, N) , and R the vector of factor incomes of dimension $(1, N)$. N is equal to the product of the number of countries (I) and the number of sectors (J).

Output is equal to the sum of factor incomes and intermediary consumption. Thus:

$$Y = (y_1 \dots y_N) = (y_1 \dots y_N) \begin{pmatrix} a_{11} & \dots & a_{N1} \\ \vdots & a_{n,n'} & \vdots \\ a_{1N} & \dots & a_{NN} \end{pmatrix} + (r_1 \dots r_N) = Y\mathcal{A} + R$$

Assuming no inputs substitution between industries or countries (i.e. assuming that technical coefficients are fixed), we can derive a price equation under the assumption of complete cost pass-through.

Define $y_n = p_n * q_n$, with p_n the price and q_n the quantity of product from country n and normalize quantity such as $q_n = 1$.

Define P the vector of production prices of dimension $(1, N)$ and V the vector of factor income of dimension $(1, N)$ needed to produce one unit of good in each sector. Then $P = P\mathcal{A} + V$.

Suppose an exogenous input price shock occurs. Firms face a change in their costs, which they pass on directly to production prices to keep their factor income constant. Define $\Delta^0 P$ the shock vector of dimension $(1, N)$ computed as the difference between the original price vector

P^0 and the new vector P^1 . Then:

$$\Delta^0 P = P^1 - P^0 = C,$$

with C the shock vector of dimension $(1, N)$ that contains the direct effect of the shock on output prices.

The price increase is passed on to the country-specific industries that use shocked products as intermediate consumptions. The higher the reliance on shocked inputs, the higher the increase in production prices.

In a first step, the direct impact of the shock on each country-specific industry's output prices amounts to $\Delta^1 P = C\mathcal{A}$.

In a second step, the shock is passed on all country-specific industries using these shocked inputs in their production processes. For k production cycles, the increase in production prices amounts to $\Delta^k P = C\mathcal{A}^k$.

As the technical coefficients are smaller than 1, the effect of the initial shock on input prices eventually wears out. The overall effect of the shock is equal to the sum of the initial shock and all the increases that occurred during the successive production cycles. The total effect of the shock on prices, S , is equal to $S = C(I + \mathcal{A} + \mathcal{A}^2 + \dots + \mathcal{A}^k + \dots) = C(I - \mathcal{A})^{-1}$, with $(I - \mathcal{A})^{-1}$ the inverse of Leontief's matrix; S is a vector $(1, N)$ composed of the elements s_{ij} measuring the total effect of the shock on the output price of sector j in country i .

3.2 The choice of WIOD

The world input-output tables are an extension of the national input-output tables. Input-output tables measure the relationships between the producers of goods and services (including imports) within an economy and the users of these goods and services (including exports). The national tables specify, in line, for each industry, the use of the product as intermediate or final use. In a national table, final use includes exports alongside domestic final uses. Exports are not a final use in world input-output tables. They show by which foreign industry a product was produced, and which foreign industry or final user uses the exports of a given country. For example, world input-output tables enable us to identify how much international trade is associated with the consumption of a particular final product.

Aggregating national input-output tables in world input-output tables is challenging for many reasons. For example, national input-output tables vary widely in terms of detail and scope, and are therefore not fully consistent. Furthermore, the availability of year-specific national input-output tables is limited, especially for developing economies. Other issues exist.

Two datasets including a time dimension for world input-output tables are available: (i) the World Input Output Database (WIOD) and (ii) the OECD-ICIO database TiVA.

The World Input Output Database (WIOD) The World Input Output Database (WIOD) contains time series of inter-country input-output tables from 2000 to 2014. It provides "World Input-Output Tables" that reconcile national input-output tables (or supply-use tables) with bilateral trade statistics derive the final symmetric world input-output table. The WIOD covers

43 countries, of which 28 belongs to the European Union and 15 are other major countries that cover, in total, around 85% of world GDP. They contain annual information for 56 industries, comprising primary, manufacturing goods and services sectors. Therefore, for each year a full country-sector input-output matrix traces the importance of a supplying industry in one country for an industry in another country. The values in WIOTs are expressed in millions of U.S. dollars; market exchange rates were used for currency conversion (Timmer et al., 2015). GD CORRIGER LA RÉFÉRENCE

Table 1 shows the economies included in the WIOD.

Europe	Austria, Belgium, Bulgaria, Croatia, Cyprus, Czech Republic, Denmark, Estonia, Finland, France, Germany, Greece, Hungary, Ireland, Italy, Latvia, Lithuania, Luxembourg, Malta, Netherlands, Norway, Poland, Portugal, Romania, Slovakia, Slovenia, Spain, Sweden, Switzerland, United Kingdom
North America	Canada, United States
Latin America	Brazil, Mexico
Asia-Pacific	Australia, China, India, Indonesia, Japan, Korea, Taiwan
Other	Russia, Turkey

Table 1: **Economies included in the World Input-Output Database**

The Statistics on Trade in Value Added (TiVA) database The TiVA database is compiled by the OECD and the WTO. It builds on the OECD harmonized individual country input-output tables to provide matrices of inter-industrial flows of goods and services in current prices (USD million), for 64 economies (i.e. 35 OECD Countries, 28 non-OECD economies and the Rest of the world) and 34 industries, covering the years 1995 to 2011. Table 2 shows the economies included in the TiVA database.

Europe	Austria, Belgium, Bulgaria, Croatia, Cyprus, Czech Republic, Denmark, Estonia, Finland, France, Germany, Greece, Hungary, Iceland, Ireland, Italy, Latvia, Lithuania, Luxembourg, Malta, Netherlands, Norway, Poland, Portugal, Romania, Slovakia, Slovenia, Spain, Sweden, Switzerland, United Kingdom
North America	Canada, United States
Latin America	Argentina, Brazil, Chile, Colombia, Costa Rica, Mexico (differentiating between "three Mexico"), Peru
Asia-Pacific	Australia, Cambodia, China (differentiating between "four China"), Hong Kong SAR, India, Indonesia, Japan, Korea, Malaysia, New Zealand, Philippines, Singapore, Taiwan, Thailand, Viet Nam
Other	Brunei, Israel, Morocco, Russia, Saudi Arabia, South Africa, Tunisia, Turkey

Table 2: **Economies included in the TiVA Database**

Major differences between the WIOD and TiVA databases The WIOD and TiVA databases have a number of distinguishing characteristics (see Timmer et al. (2015) for details). The most relevant difference for our analysis relates to the treatment of imports by use category. National input-output statistics provide the use of products by industries and final consumers, but the country of origin of products is unknown. Therefore, one has to breakdown product

import statistics by category of use in the construction of world input-output tables.

The TiVA database relies on the so-called "import proportionality assumption". The domestic input-output tables show transactions between domestic industries. As a complement to these tables, supplementary tables break down total imports by user (industry and the different categories of final demand). Some countries provide these import tables in conjunction with their input-output tables, but in other cases they are derived by the OECD. Mexico and China benefit from a special treatment, but for the other countries the main assumption used is that the share of imports in any product consumed directly as intermediate consumption or final demand (except exports) is the same for all end-uses (the "proportionality assumption")¹.

Various studies have found that this assumption can be misleading, as import shares vary significantly across end-uses. Feenstra and Jensen (2012) find that shares of imported materials may differ substantially across U.S. industries. Based on Asian input-output tables, Puzzello (2012) finds that the proportionality assumption understates the use of foreign intermediate inputs. It is likely to be particularly binding for developing countries, as the import content of exports is usually higher than the import content of products used for domestic consumption.

To address this issue, the WIOD database uses bilateral trade statistics to derive import shares for three end-use categories (intermediate use, final consumption and investment) by mapping detailed six-digit products international trade statistics based on product descriptions (Dietzenbacher et al., 2013).

To sum up, the WIOD includes information on bilateral industry-specific input use, whereas such information exists only in imputed form in TiVA. Therefore, we focus on the WIOD database in our analysis².

3.3 Nominal exchange rate shock

We implement an exchange rate shock using the WIOD databases described above. The appreciation of a currency against other currencies leads, for the shock-stricken country, to a fall in the domestic-currency price of its imports and an increase in the foreign-currency price of its exports. We focus on the disinflationary impact of this shock on the shock-stricken country though we also estimate, conversely, its inflationary impact on countries that directly and indirectly consume, through third countries linkages, inputs from the shock-stricken country.

However, this shock cannot be analyzed applying the method described in 3.1 because the value of the price, besides depending of the nationality of the input-providing sector, also depends on the nationality of the input-using sector. Suppose a world with two countries *A* and *B*, each having its own national currency, and a currency for international transactions, the dollar. Assuming a 100% appreciation of the currency of country *A* against the other two currencies, the production prices of country *A* expressed in dollars would double compared to those of country *B* expressed in dollars. Country *B* pays more for its imports of inputs, in dollars as well as in national currency, since the exchange rate of the currency of Country *B* against the dollar has not changed. Conversely, the imported input prices in country *A* remain constant in dollar terms, since production prices of country *B* have not changed and fall by half once expressed in national currency.

¹See <http://www.oecd.org/sti/ind/49894138.pdf> for details.

²Results obtained with the TiVA database are available on request.

We assume that producers have no margin behavior and pass through the exchange rate shock fully on to their production prices. The change in the prices of imported goods is therefore transmitted to all domestic prices, both directly and through inter-industry linkages. These upward (downward) movements for country B (country A) affect all input prices in each of the countries.

The effects of the shock spread over multiple production cycles. At the end of this process, the overall impact of the shock in dollar terms is equal, for the shocked country A , to the rise in production prices due to the exchange rate shock, minus direct and indirect decreases (via interindustry linkages in the country), in national currency and then converted back into dollar terms, in the prices of inputs imported from B and disseminated to all branches. The overall impact on production prices in dollar terms in country A is therefore lower than the initial exchange rate shock. For country B , the final impact is to the cumulative direct and indirect effects of higher prices of inputs imported from country A and disseminated to all industries.

In a global economy composed of I countries, each with J sectors, the appreciation of a country's currency i against all other currencies translates into a rise in country i 's prices in dollars. The production price of each sector will vary in dollar terms by: $c_{\i in the shock-stricken country i and 0 in other countries.

Hence, for each sector j in country i :

$$\Delta^0 p_{\$ij} = p_{\$ij}^1 - p_{\$ij}^0 = c_{\$ij} = c_{\i$

And for each sector j in country k ($k \neq i$),

$$\Delta^0 p_{\$kj} = p_{\$kj}^1 - p_{\$kj}^0 = c_{\$kj} = 0$$

To simplify, initial output prices for each sector are normalized to 1 and exchange rates to 1:1. A 100% appreciation in the exchange rate of a currency against other currencies therefore corresponds to an absolute shock of +1, with production prices in the shock-stricken country rising from 1 to 2 dollars.

The appreciation affects producers through changes in relative prices between countries and, therefore, through changes in input prices traded between the shock-stricken country i and other countries.

Consider first the direct impact (in absolute terms) on other countries of the rise in imported input prices from shocked country i . For any sector l of a country k ($k \neq i$), the increase in the producer price depends directly on the quantity of inputs imported from the shock-stricken country i , weighted by the variation in level of the price of inputs in dollars (i. e. the exchange rate shock):

$$\Delta^1 p_{\$kl} = c_{\$}^i * a_{kl,i1} + \dots + c_{\$}^i . a_{kl,ij} + \dots + c_{\$}^i . a_{kl,iJ} = \sum_{j=1}^J c_{\$}^i . a_{kl,ij} = c_{\$}^i . \sum_{j=1}^J a_{kl,ij} \quad (1)$$

With $a_{kl,ij}$ the quantity of inputs from the country i 's sector j needed to develop a production

unit for the country's k sector l .

For the shocked country, the shock has a disinflationary effect on domestic production prices. In national currency, the production prices of imported inputs fall in each sector by $c^i = -\frac{c_{\$}^i}{1+c_{\i , or by 0.5 with $c_{\$}^i = 1$.

This decline then spreads to all domestic-input using sectors. In sector j of the shocked country i , this fall amounts in national currency to:

$$\Delta^1 p_{ij} = \sum_{l=1}^{l=J} c^i \cdot a_{ij,1l} + \dots + \sum_{l=1}^{l=J} c^i \cdot a_{ij,kl} + \sum_{l=1}^{l=J} c^i \cdot a_{ij,pl} = \left(-\frac{c_{\$}^i}{1+c_{\$}^i} \right) \cdot \sum_{\substack{k=1 \\ k \neq i}}^{k=I} \left[\sum_{l=1}^{l=J} a_{ij,kl} \right]$$

This level shock can be converted into dollars:

$$\Delta^1 p_{\$ij} = (1 + c_{\$}^i) \cdot \left(-\frac{c_{\$}^i}{1+c_{\$}^i} \right) \sum_{\substack{k=1 \\ k \neq i}}^{k=I} \left[\sum_{l=1}^{l=J} a_{ij,kl} \right] \quad (2)$$

We therefore know the direct impact of the shock on all input prices of all countries. In matrix notation, we create two matrices that build on the world input-output matrix A defined in 3.1. These two matrices retain only the direct effects of the exchange rate shock on the price of goods imported by the shocked country i and the direct effects of the exchange rate shock on the price of goods imported by the rest of the world from the shocked country i . To formalize the initial impact of the shock on the price of traded goods, we neutralize the impact of an input price shock on the price of domestic inputs as well as on the price of inputs traded between countries that are not shocked.

Let us first look at the shock from the perspective of countries that import inputs from country i .

Let $C_{\i be the vector of change in production prices in dollars following the appreciation of the currency of country i against all other currencies. Hence,

$$C_{\$}^i = (0 \dots 0 \dots c_{\$ij} \dots c_{\$ik} \dots 0 \dots 0)$$

with $c_{\$ij} = c_{\$ik} = c_{\i for all sectors j and k in the shocked country i .

Building on Equation 1, we write the direct impact of the exchange rate shock on the other countries as the product of the shock vector $C_{\i and a matrix \mathcal{B} . \mathcal{B} builds on the large matrix \mathcal{A} of technical coefficients, but only keeps the coefficients of each country's sectoral inputs imported from the shocked country i . The other coefficients are replaced by 0, including those of the block of country i concerning the domestic inputs of the shocked country i . The direct impact of the appreciation of a currency against the dollar on the price of inputs in countries that are not

shocked is equal to $C_{\$}^i \mathcal{B}$ with

$$C_{\$}^i \mathcal{B} = (0 \dots c_{\$}^i \dots 0) \begin{pmatrix} 0 & \dots & 0 \\ a_{11,ij} & 0 & a_{IJ,ij} \\ 0 & \dots & 0 \end{pmatrix} \quad (3)$$

where each $a_{kl,ij}$ element of the line block represents the technical coefficient related to imports of inputs by sector l in country k (with $k \neq i$) from sector j of country i .

Let us now consider the shock from the perspective of the shocked country i .

Define C^i the vector of change in production prices everywhere expressed in country i 's currency, $\left(-\frac{c_{\$}^i}{1+c_{\$}^i}, \dots, 0, \dots, -\frac{c_{\$}^i}{1+c_{\$}^i}\right)$.

From Equation 2, we can write the direct impact for country i of the fall in input prices from the rest of the world. The direct impact corresponds to the product of the shock vector C^i and a matrix $\tilde{\mathcal{B}}$. $\tilde{\mathcal{B}}$ builds on the large matrix \mathcal{A} of which only the country blocks of the inputs imported by country i from other countries have been retained. The other coefficients are replaced by 0, including those of the block of country i concerning the domestic inputs of the shocked country i .

The direct impact of the appreciation of the shocked country i on the price of its inputs corresponds, in national currency, to $C^i \tilde{\mathcal{B}}$ with:

$$C^i \tilde{\mathcal{B}} = \left(-\frac{c_{\$}^i}{1+c_{\$}^i}, \dots, 0, \dots, -\frac{c_{\$}^i}{1+c_{\$}^i}\right) \begin{pmatrix} 0 & \dots & a_{ij,11} & \dots & 0 \\ 0 & & 0 & & 0 \\ 0 & \dots & a_{ij,IJ} & \dots & 0 \end{pmatrix} \quad (4)$$

where each $a_{ij,kl}$ element in the column block represents imports of inputs by sector j in country i from sector l of country k . We can then convert this direct impact in dollars, by multiplying it by the new value of the national currency in dollars, $(1+c_{\$}^i)$. The direct impact of the appreciation of the shocked country i on the price of its inputs corresponds, in dollars, to $\tilde{C}_{\$}^i \tilde{\mathcal{B}}$ with:

$$\tilde{C}_{\$}^i \tilde{\mathcal{B}} = (1+c_{\$}^i) \cdot C^i \tilde{\mathcal{B}} = (-c_{\$}^i \dots 0 \dots -c_{\$}^i) \begin{pmatrix} 0 & \dots & a_{ij,11} & \dots & 0 \\ 0 & & 0 & & 0 \\ 0 & \dots & a_{ij,IJ} & \dots & 0 \end{pmatrix} \quad (5)$$

The direct effect on the world is therefore the sum of these vectors from equations 3 and 5, i. e. $C_{\$}^i \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}$.

An input price shock then spreads to all sectors in all countries via the global intersectoral exchanges transcribed by the matrix of technical coefficients of the large matrix \mathcal{A} . This process will be repeated several times, until the effects are completely exhausted. In the end, the total sectoral effect of the dollar shock is equal to the sectoral shock itself, incremented by changes in input prices due to changes in imported input prices, and by all marginal changes in output prices during the production processes, i. e.:

$$S_{\$}^i = \Delta P_{\$}^i = C_{\$}^i + \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) + \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) \mathcal{A} + \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) \mathcal{A}^2 + \dots + \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) \mathcal{A}^k + \dots$$

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$$S_{\$}^i = C_{\$}^i + \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) * (I - \mathcal{A})^{-1} \quad (6)$$

With $S_{\i the total impact vector composed of the elements $s_{\$kj}^i$ showing the total impact of the shock in the exchange rate of country i on country k 's sector j . Equation 6 gives the absolute evolution of sectoral prices in international currency. The study of this vector is the main objet of Cochard et al. (2016). //

In contrast, this paper focuses on the internal effect of an exchange rate shock. To obtain the absolute evolution of the sectoral prices of the shocked country in national currency, we remove the exchange rate shock in international currency, multiply the balance by the scalar of conversion equal to $\frac{1}{1+c_{\i and add the initial exchange rate shock in national currency.

$$\begin{aligned} S^i &= C^i + \left(\frac{1}{1+c_{\$}^i}\right) * (S_{\$}^i - C_{\$}^i) \\ &= C^i + \left(\frac{1}{1+c_{\$}^i}\right) * \left(C_{\$}^i \cdot \mathcal{B} + \tilde{C}_{\$}^i \tilde{\mathcal{B}}\right) * (I - \mathcal{A})^{-1} \\ &= C^i + \left(\hat{C}_{\$}^i \cdot \mathcal{B} + C^i \tilde{\mathcal{B}}\right) * (I - \mathcal{A})^{-1} \end{aligned} \quad (7)$$

Where $\hat{C}_{\$}^i = \left(0 \dots \frac{c_{\$}^i}{1+c_{\$}^i}, \dots 0\right)$ is the increase in dollar prices of goods from country i used as inputs in all other countries.

S^i represents the overall impact of a shock on prices in each sector of each country expressed in the shocked currency. To transform this number in an average price index, \bar{s}^i , we need to compute a weighted average of the sectoral effects of the shock. This paper focuses on the price of household consumption. Let HC^i be the vector of sectoral shares in country i 's consumption :

$$HC^i = \begin{pmatrix} \frac{hc_{11}^i}{hc^i} \\ \dots \\ \frac{hc_{kj}^i}{hc^i} \\ \dots \\ \frac{hc_{LJ}^i}{hc^i} \end{pmatrix}$$

Where hc_{kj}^i corresponds to household consumption in country i of goods produced by sector j from country k and hc^i represents the total household consumption of country i .

$\bar{s}_i^{i,HC}$ provides the average impact of the shock on the consumer price of country i .

$$\bar{s}_i^{i,HC} = S^i.HC^i = \sum_{\substack{j=1\dots J \\ k=1\dots I}} s_{kj}^i \cdot \frac{hc_{kj}^i}{hc^i} \quad (8)$$

with s_{kj}^i is a coefficient of S^i for country i .

4 The impact of exchange rates fluctuations on consumer prices

4.1 Baseline results

We use the model presented in 3.3 to study the absolute value of $\bar{s}_i^{i,HC}$ following a 100% appreciation of the domestic currency versus all other currencies. When the domestic currency appreciates, domestic prices expressed in domestic currency decrease, as imported inputs and imported consumer goods are cheaper. As our model is linear, the exact value of the shock does not matter: choosing 100% allows us to interpret $\bar{s}_i^{i,HC}$ as an elasticity. As an illustration, using the WIOD database, we find that $\bar{s}_i^{i,HC}$ is equal to -0.055 for the USA in 2011, meaning that a 100% appreciation of the dollar would reduce consumer prices by 5.5%. The following figures report the absolute value of this number (0.055).

Additionally, for Euro area members, we distinguish between the effect of the appreciation of the euro and the effect of the appreciation of a hypothetical national currency. For example, in the case of France, using WIOD in 2011, a 100% appreciation of the euro would lead to a reduction of domestic prices of 7.6%. A 100% appreciation of the hypothetical French national currency would lead a reduction of domestic prices of 12.2%.

Figure 1, shows that, despite their differences, using WIOD or TIVA yields very similar results for consumer prices.

To go further, $\bar{s}_i^{i,HC}$ is broken down by origin: imported consumer goods on the one hand and domestic consumer goods on the other hand. The price of domestic goods is affected because of imported inputs. E.g., we can define

$$\bar{s}_i^{i,HC} = \bar{s}_{i,imp}^{i,HC} + \bar{s}_{i,dom}^{i,HC} = S^i.HC^{i,dom} + S^i.HC^{i,imp} \quad (9)$$

$$(10)$$

Where:

$$\begin{aligned} HC^i &= HC^{i,dom} + HC^{i,imp} \\ &= \begin{pmatrix} 0 \\ \dots \\ \frac{hc_{ij}^i}{hc^i} \\ \dots \\ 0 \end{pmatrix} + \begin{pmatrix} \frac{hc_{i1}^i}{hc^i} \\ \dots \\ 0 \\ \dots \\ \frac{hc_{iJ}^i}{hc^i} \end{pmatrix} \end{aligned} \quad (11)$$

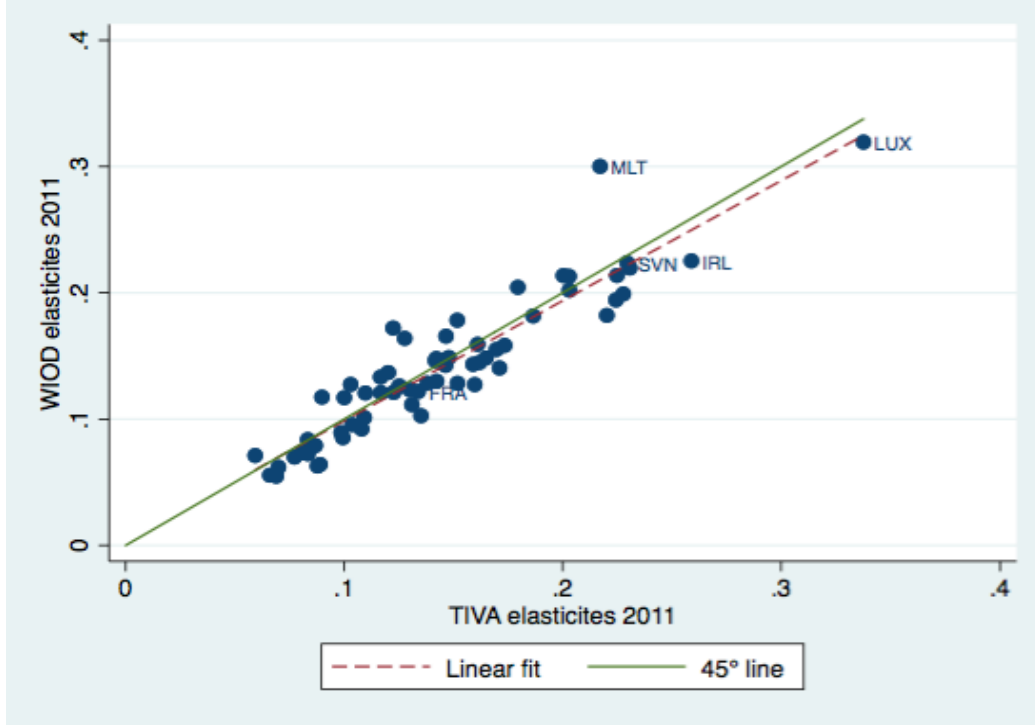


Figure 1: Comparing $\bar{s}_i^{i,HC}$ for WIOD and TIVA, 2011

Source: WIOD and TIVA

For example,

$$\bar{s}_{i,imp}^{i,HC} = \sum_{\substack{j=1 \dots J \\ k=1 \dots I \\ k \neq i}} s_{kj}^i \cdot \frac{hc_{kj}^i}{hc^i} \quad (12)$$

We can then define the contribution of imported consumption goods to an exchange rate shock as $\bar{s}_{i,imp}^{i,HC} / \bar{s}_i^{i,HC} = S^{i,HC^{i,imp}} / S^{i,HC^i}$. We can also define the sensitivity of imported consumption prices as $\frac{S^{i,HC^{i,imp}} / S^{i,HC^i}}{\vec{1}^{i,HC^{i,imp}}}$ where $\vec{1}$ is a horizontal vector of ones. For example, if an appreciation exchange rate reduce household consumption prices by 20%, that household consumption is 50% imported and that imported consumption goods prices evolution cause in a reduction of household consumption prices of 15%, then the contribution of imported consumption goods will be 0.75 ($=.15/.20$) and their sensitivity of 1.5 ($=0.75/0.5$).

GD : PEUT-ÊTRE Y A-T-IL UNE MANIÈRE DE SIMPLIFIER L'EXPRESSION DE LA SENSITIVITÉ, MAIS JE NE VOIS PAS COMMENT FAIRE...

Figure 2 shows, for example, that the contribution of imported consumption is higher than 0.5 in most countries. While imported consumption has a smaller share in total consumption, this is over-compensated by the sensitivity of its prices to exchange rate shocks, as show by the comparison of 4 and 5.

Similar decompositions of the matrix HC^i can be done to analyse the contribution of different sectors. decompose the effect between sectors. That allows the identification of the contribution of different sectors to the inflation shocks in different countries. Figure 3 shows that non-energy industrial goods and services have the highest contribution. Energy is highly sensitive to

exchange rate shocks (see 4 and 5), but its share in consumption is too small for its contribution to the final effect to be large.

4.2 What do we gain from using world input-output matrices?

One might wonder whether using world input-output matrices provided by WIOD or TIVA to compute the effect of exchange rate shocks on household consumption prices is worth the wait (the latest year covered by WIOD is 2014) and the computational complexity. To answer this question, we break down $\bar{s}_i^{i,HC}$ into different elements classified by ease of use and computation. Let us start from equation 7.

$$\begin{aligned}
S^i &= C^i + \left(\hat{C}_{\$}^i \cdot \mathcal{B} + C^i \tilde{\mathcal{B}} \right) * (I - \mathcal{A})^{-1} \\
S^i &= \underbrace{C^i}_{\text{(E1) direct effect through imported consumption goods}} + \underbrace{C^i \tilde{\mathcal{B}}}_{\text{(E2) effect on domestic consumption goods through imported inputs}} + \underbrace{\hat{C}_{\$}^i \cdot \mathcal{B}}_{\text{(E3) effect on imported consumption goods through domestic inputs}} \\
&\quad + \underbrace{\left(\hat{C}_{\$}^i \cdot \mathcal{B} + C^i \tilde{\mathcal{B}} \right) * (I - \mathcal{A})^{-1} * \mathcal{A}}_{\text{(E4) residual}}
\end{aligned} \tag{13}$$

When the shock corresponds to an appreciation of the domestic currency, $E1$ and $E2$ reduce country i 's household consumption prices and $E3$ increases country i 's household consumption prices. Notice that $E1$ and $E2$ are easy to compute with national input-output matrices, whereas world input-output matrices are needed for computing $E3$ and $E4$.

C^i and $\hat{C}_{\i have a large number of zeros. So, we have :

$$\begin{aligned}
\bar{s}_i^{i,HC} &= S^i \cdot HC^i = E1.HC^i + E2.HC^i + E3.HC^i + E4.HC^i \\
&= E1.HC^{i,imp} + E2.HC^{i,dom} + E3.HC^{i,imp} + E4.HC^i
\end{aligned} \tag{14}$$

A first approach to measuring the interest of using WIOD is to compute the share $E1.HC^{i,imp}$, $E2.HC^{i,dom}$, $E3.HC^{i,imp}$ and $E4.HC^i$ in $\bar{s}_i^{i,HC}$. Figure 6 provides the result. $E3.HC^{i,imp}$ is very small, $E1.HC^{i,imp}$ dominates. But, for most countries, $E4.HC^i$ represent between 10% and 30% of $\bar{s}_i^{i,HC}$. That suggests that inverting the WIOD matrixes is indeed useful.

Yet, the relative importance of $E4.HC^i$ might not be too much of an issue if it can be deducted from the easier-to-compute elements of $\bar{s}_i^{i,HC}$. This is suggested by the correlation matrix of $E1.HC^{i,imp}$, $E2.HC^{i,dom}$, $E3.HC^{i,imp}$ and $E4.HC^i$ (see Table ??).

Variables	E1HC	E2HC	E3HC	E4HC
E1HC	1.00			
E2HC	0.74	1.00		
E3HC	-0.09	0.11	1.00	
E4HC	0.36	0.53	0.05	1.00

Table 3: Cross-correlation of $\bar{s}_i^{i,HC}$'s components (WIOD 2014)

$E3.HC^{i,imp}$ does not require inverting a matrix, but it is still quite data-intensive to compute. As a result, we study whether we can deduct $\bar{s}_i^{i,HC}$ from $E1.HC^{i,imp}$ and $E2.HC^{i,dom}$.

Figure 2: Contribution of imported final consumption to the impact of a nominal exchange rate shock (see eq. 12)

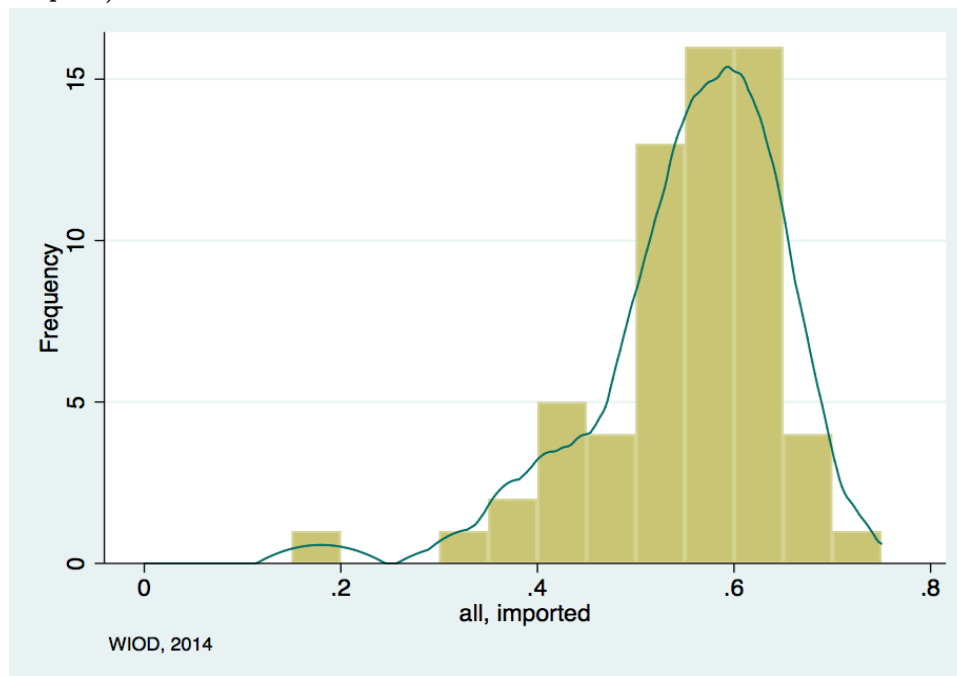


Figure 3: Contribution of sector-specific final consumption to the impact of a nominal exchange rate shock

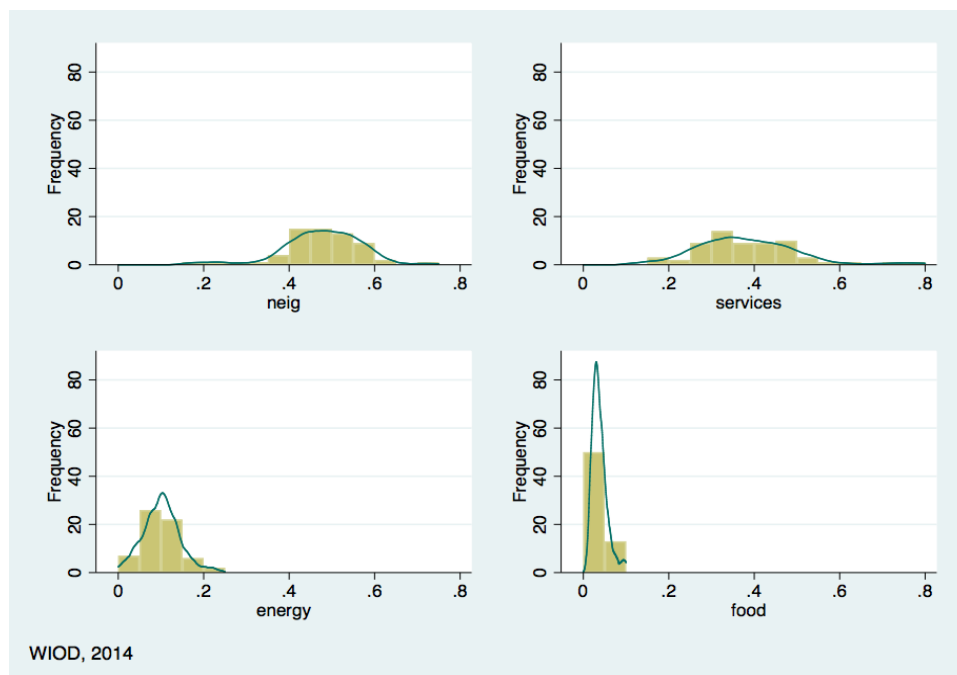


Figure 4: Sensitivity of different domestic sectors to an exchange rate shock

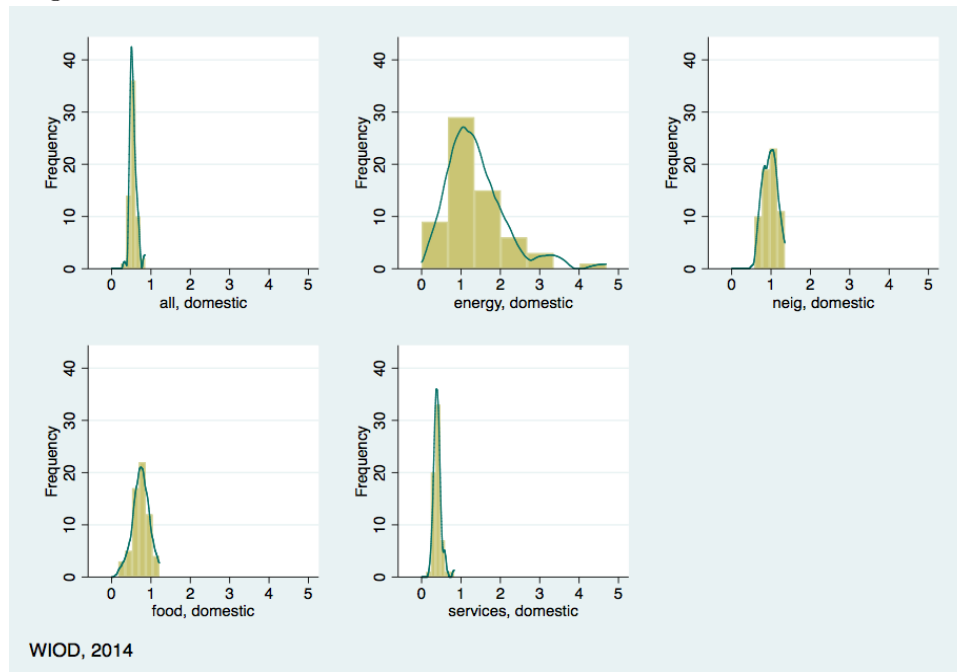
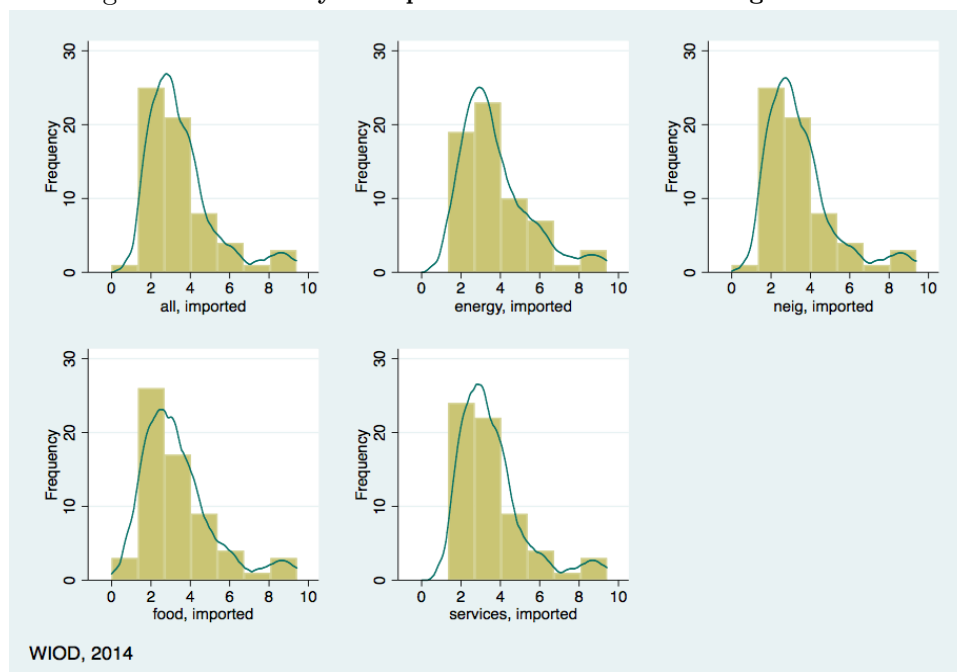


Figure 5: Sensitivity of imported sectors to an exchange rate shock



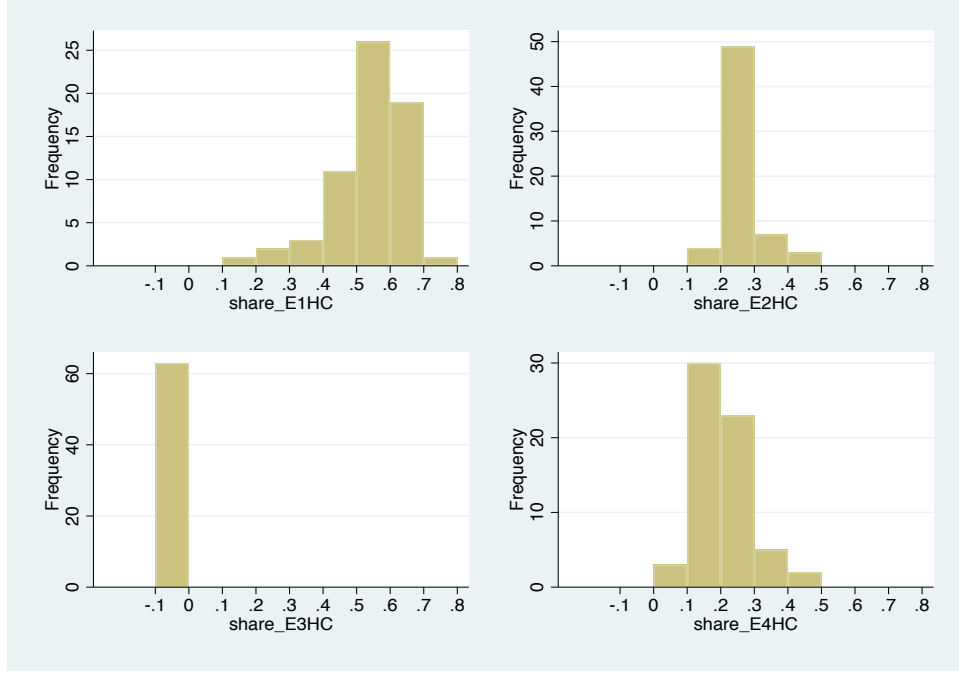


Figure 6: **Decomposition of $\bar{s}_i^{i,HC}$**

Source: WIOD, 2014

Figure 7 depicts the relationship between $\bar{s}_i^{i,HC}$ and $E1.HC^{i,imp} + E2.HC^{i,dom}$. It shows that $E1.HC^{i,imp} + E2.HC^{i,dom}$ is a pretty good predictor of $\bar{s}_i^{i,HC}$ (the R^2 is over 0.98). Excepting to some extent 2009, this relationship is constant through time (see Figure 8 and 9).

$$\bar{s}_i^{i,HC} = \alpha + \beta \left(E1.HC^{i,imp} + E2.HC^{i,dom} \right) + \varepsilon_i \quad (15)$$

The same results stand using the TiVA database (see Figures 10, 11 and 12).

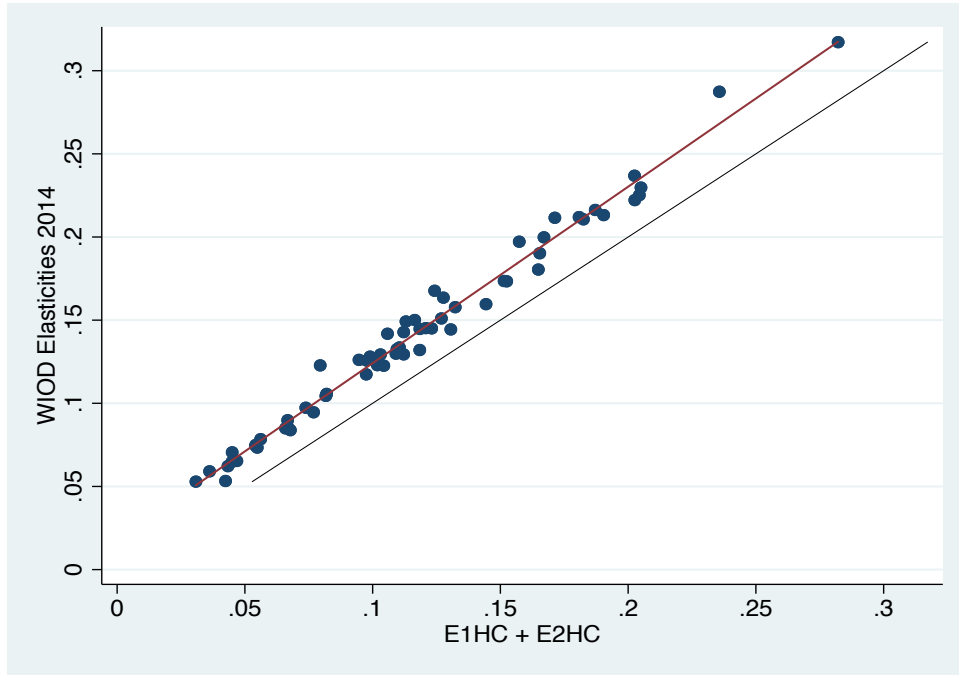


Figure 7: Comparing $\bar{s}_i^{i,HC}$ and $E1.HC^{i,imp} + E2.HC^{i,dom}$

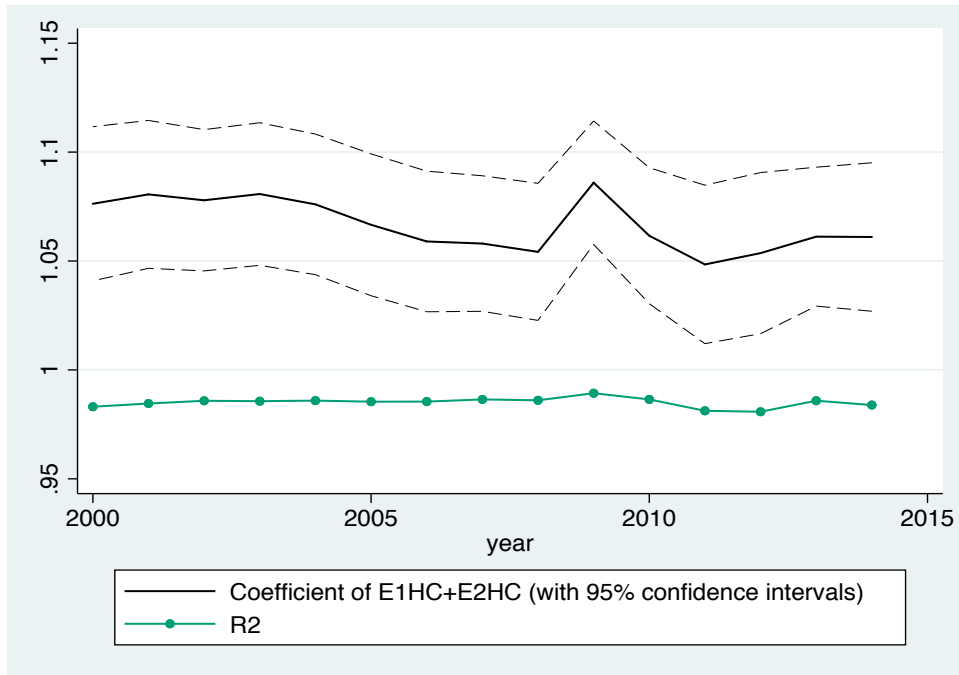


Figure 8: Evolution of β and R^2 through time (WIOD)

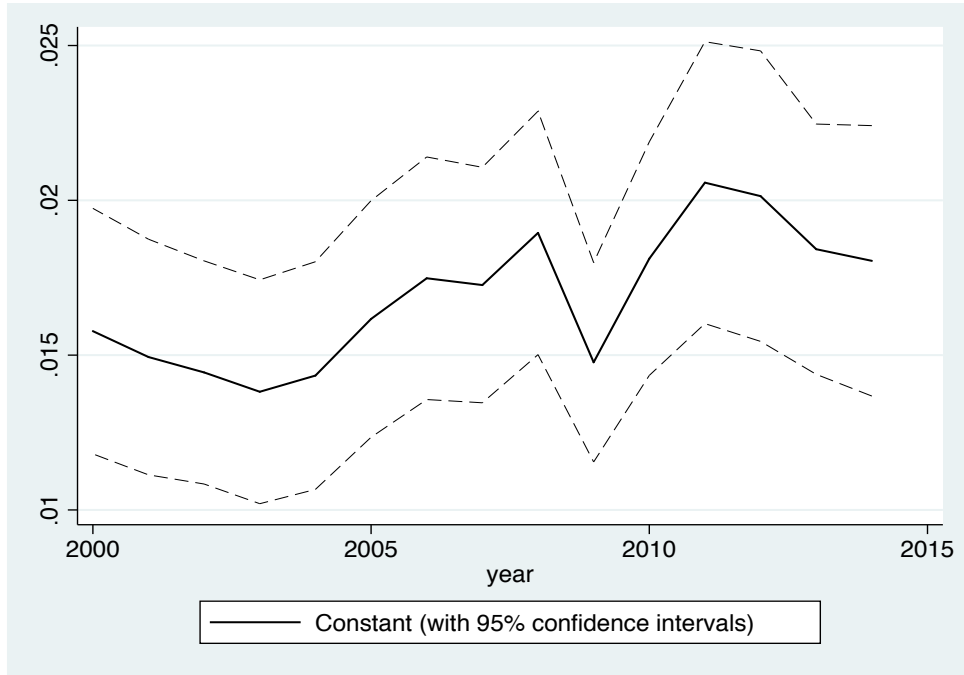


Figure 9: Evolution of α through time (WIOD)

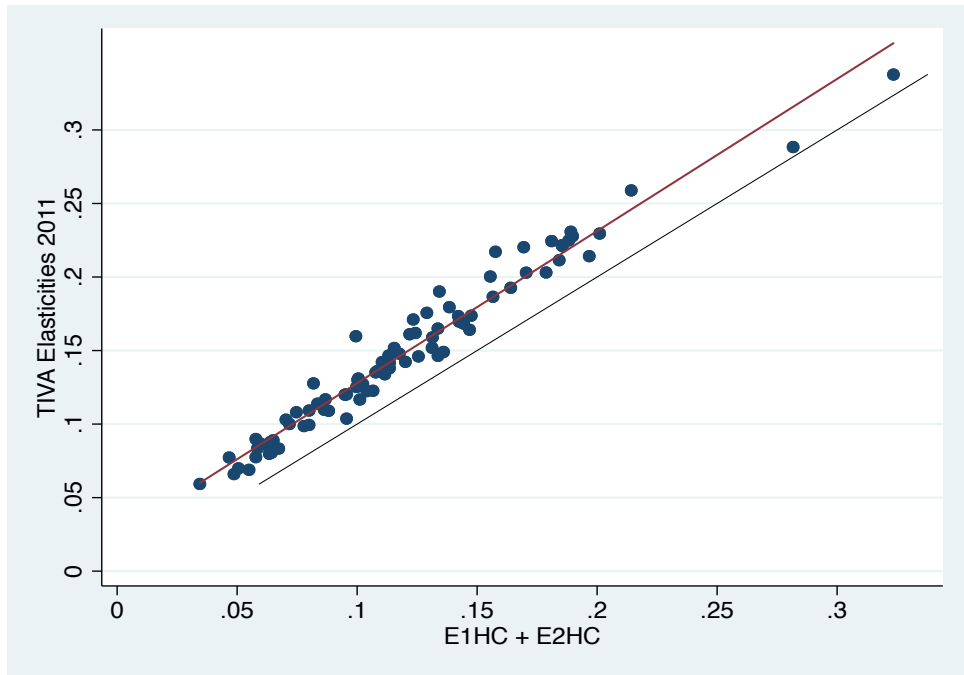


Figure 10: Comparing $\tilde{s}_t^{i,HC}$ and $E1.HC^{i,imp} + E2.HC^{i,dom}$ (TiVA)

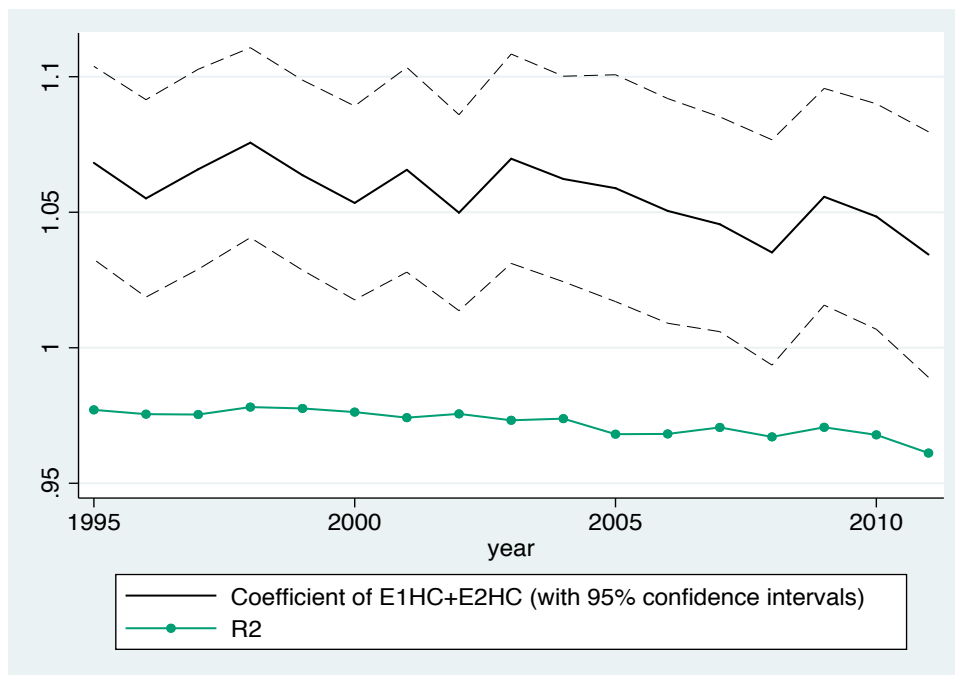


Figure 11: Evolution of β and R^2 through time (TiVA)

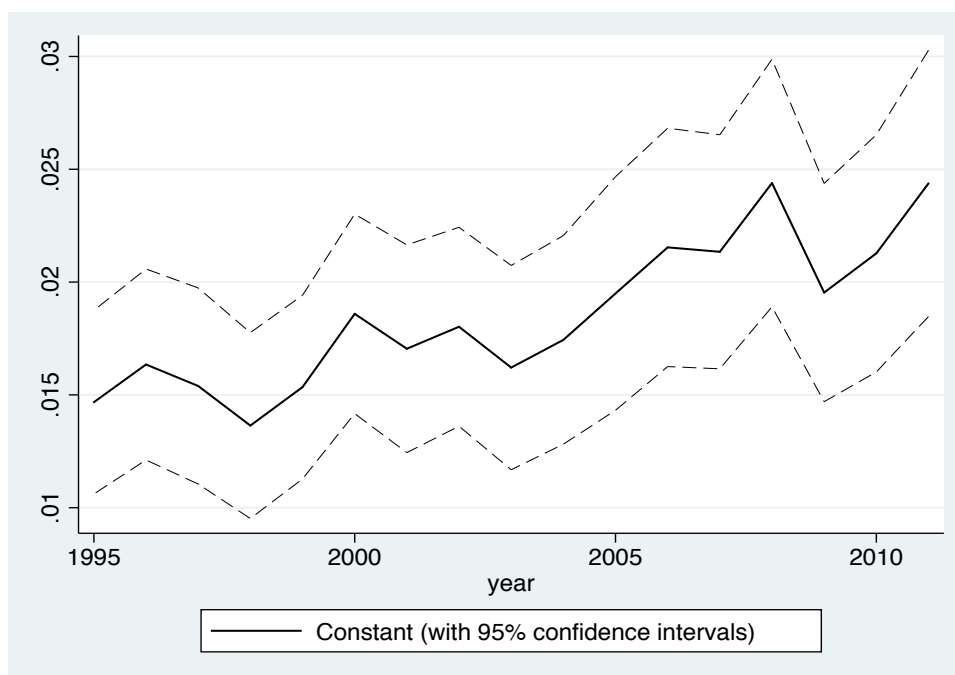


Figure 12: Evolution of α through time (TiVA)

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4.3 The intensity of import in domestic consumption

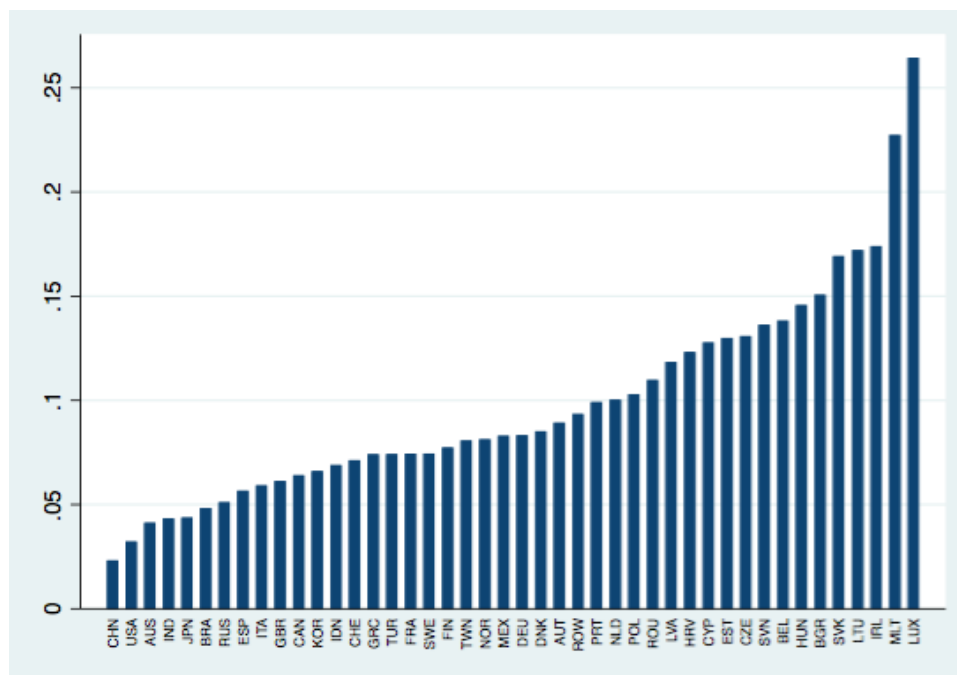


Figure 13: The share of imported intermediate and consumer goods and services in private consumption

Source: WIOD, 2014

Differences in the import intensity across sectors and countries are crucial to our analysis on global nominal spillovers. In this section, we present some stylised facts about the import intensity in domestic consumption. Using data from the WIOD, we define the import intensity of private consumption as the share of imported intermediate and final goods and services in total consumption.

Figure 13 depicts the import intensity of household consumption in 2014. Not surprisingly, small countries, such as Malta, Luxembourg and Ireland, have the highest import intensity (above 15%), while larger countries, such as Japan, the U.S. and Australia, display a much lower ratio of import intensity.

How has the import intensity of private consumption changed over time? In the Euro area, Figure 14 shows that the import intensity of consumption increased in most member states over the last decade. Following the adoption of the euro, the intensity of import increased between 2000 and 2007 in all countries except the southern economies (Spain, Portugal and Greece). In the years following the Great Recession, the import intensity of consumption kept expanding in the two largest economies of the area (Germany, France), but receded in the countries stricken by the sovereign-debt crisis (Spain, Italy, Portugal and Greece).

Outside of the euro area, Figure 15 shows that the import intensity of consumption has broadly expanded since 2000. In all countries, except China, Croatia, Indonesia and Russia, the import

intensity was higher in 2014 than it was in 2000. In China, it declined somewhat following the 2008-2009 crisis, reflecting global value chains shortening. In Russia, the intensity of import has been decreasing over the last two decades.

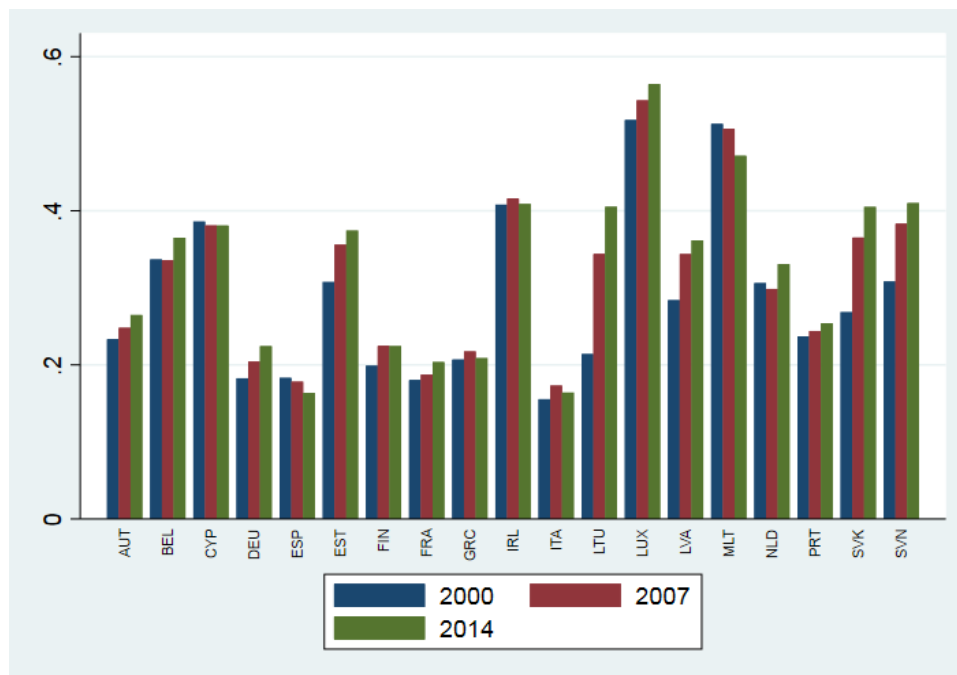


Figure 14: Evolution of the intensity of import in household consumption in the euro area

Source: WIOD

4.4 The reaction of domestic consumer prices to changes in import prices

In this section, we evaluate how domestic consumer prices react to changes in prices of imported intermediate and final goods, the latter being caused by exchange rate fluctuations. We are interested in (i) the direct effect of global inflationary shocks, defined as the share of imported final and intermediate goods in domestic consumption (i.e. the import intensity in domestic consumption defined in Section 4.3) and (ii) the total effect. The latter depends both on the direct effect and on the additional transmission of lower domestic input prices to other sectors of the domestic economy as well as to other countries which occurs during subsequent production cycles.

How much of domestic consumer prices' reactions to changes in import prices is explained by the direct effect? Figure 16 depicts how much of the total impact of a change in import prices is explained by the import intensity of household consumption. In other words, Figure 16 represents the ratio of the direct effect to the total effect. In all countries, the direct effect accounts for more than 60% of the total impact in 2014. For the whole cross-section, the coefficient of correlation between the total and the direct effect is close to unity in 2014.

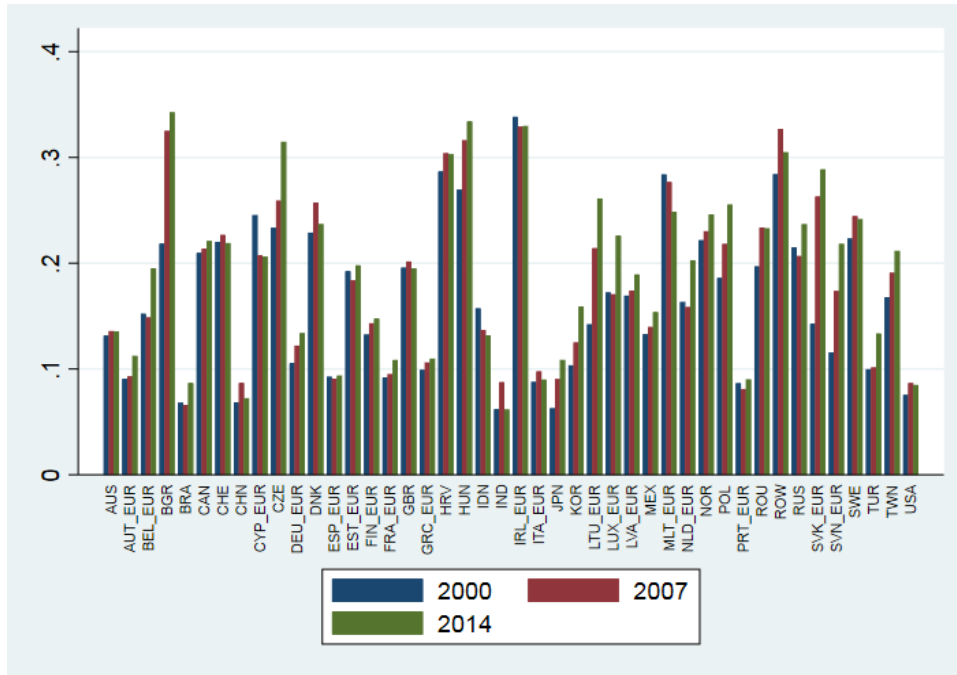


Figure 15: Evolution of the intensity of import in household consumption

Source: WIOD

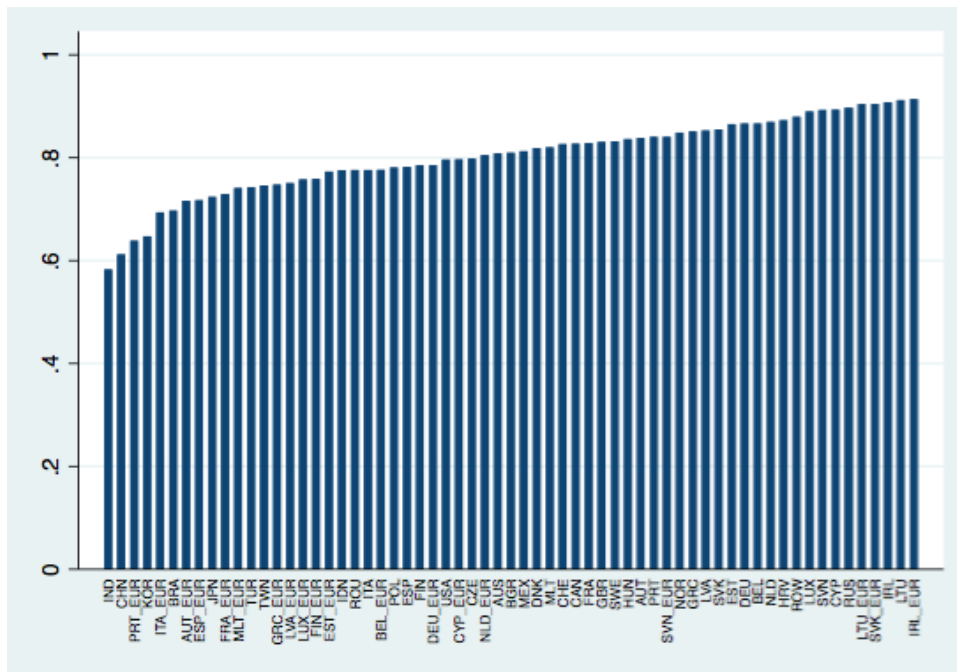


Figure 16: Ratio of direct to total effect of domestic consumer prices reactions to changes in import prices

Source: WIOD, 2014

5 The impact of exchange rates fluctuations on the main components of consumer prices

Differences in the intensity of import use across sectors In this section, we investigate the import intensity of consumption at the sectoral level. We run the following sectoral regressions (Equation 16) for each sector j .

$$S_j^{HC} = \beta_j I + c_j + \varepsilon \quad (16)$$

with S^{HC} the impact of the devaluation shock on consumer prices, for each country i , and I the vector of country-specific and sector-specific import intensity of consumption.

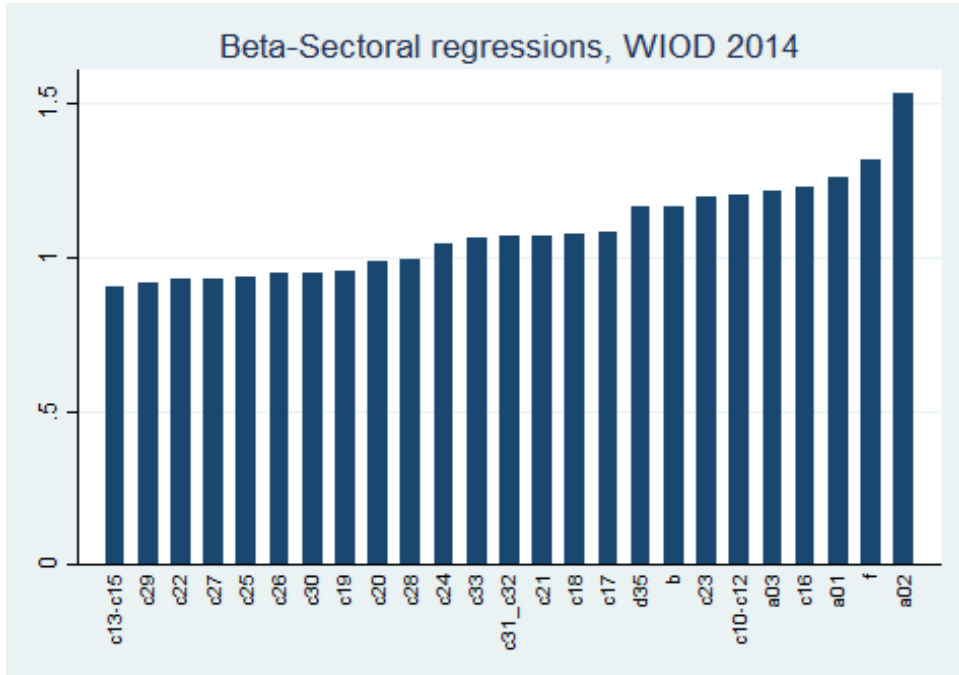


Figure 17: Consumer prices elasticity to an exchange rate shock: a sectoral analysis

Source: WIOD, 2014.

6 Conclusion

Real integration through the supply chain matters for domestic price dynamics in the euro area.

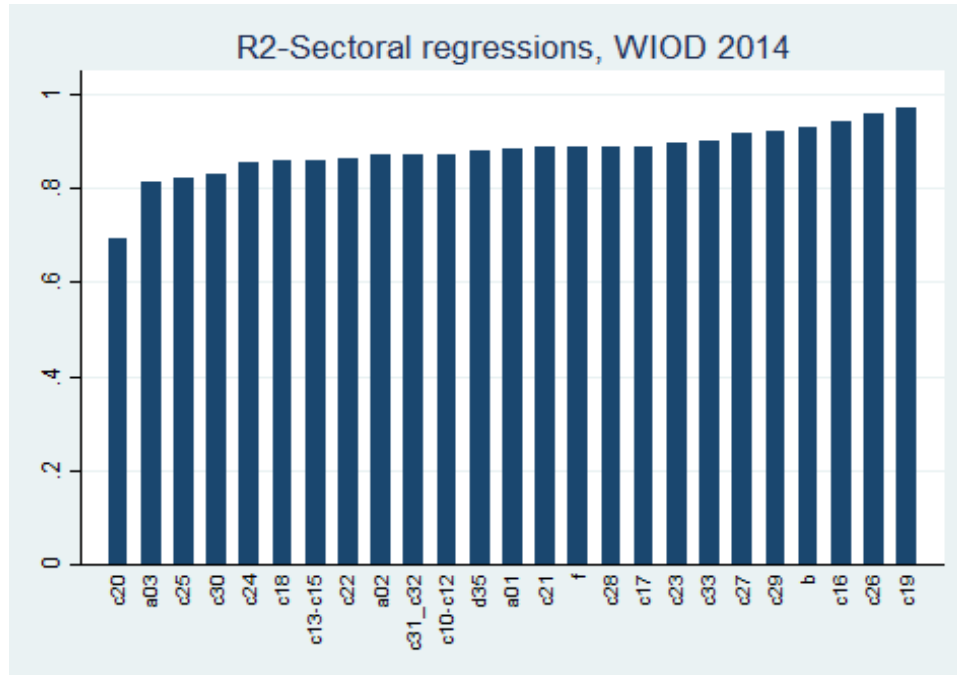


Figure 18: Sectoral analysis: R2

Source: WIOD, 2014.

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Appendix

A01	Crop and animal production, hunting and related service activities
A02	Forestry and logging
A03	Fishing and aquaculture
B	Mining and quarrying
C10-C12	Manufacture of food products, beverages and tobacco products
C13-C15	Manufacture of textiles, wearing apparel and leather products
C16	Manufacture of wood and of products of wood and cork, except furniture; articles of straw and plaiting materials
C17	Manufacture of paper and paper products
C18	Printing and reproduction of recorded media
C19	Manufacture of coke and refined petroleum products
C20	Manufacture of chemicals and chemical products
C21	Manufacture of basic pharmaceutical products and pharmaceutical preparations
C22	Manufacture of rubber and plastic products
C23	Manufacture of other non-metallic mineral products
C24	Manufacture of basic metals
C25	Manufacture of fabricated metal products, except machinery and equipment
C26	Manufacture of computer, electronic and optical products
C27	Manufacture of electrical equipment
C28	Manufacture of machinery and equipment n.e.c.
C29	Manufacture of motor vehicles, trailers and semi-trailers
C30	Manufacture of other transport equipment
C31-C32	Manufacture of furniture; other manufacturing
C33	Repair and installation of machinery and equipment
D35	Electricity, gas, steam and air conditioning supply
E36	Water collection, treatment and supply
E37-E39	Sewerage and other waste management services
F	Construction
G45	Wholesale and retail trade and repair of motor vehicles and motorcycles
G46	Wholesale trade, except of motor vehicles and motorcycles
G47	Retail trade, except of motor vehicles and motorcycles
H49	Land transport and transport via pipelines
H50	Water transport
H51	Air transport
H52	Warehousing and support activities for transportation
H53	Postal and courier activities
I	Accommodation and food service activities
J58	Publishing activities
J59-J60	Motion picture, video and television programme production; programming and broadcasting activities
J61	Telecommunications
J62-J63	Computer programming, consultancy; information service activities
K64	Financial service activities, except insurance and pension funding
K65	Insurance, reinsurance and pension funding, except compulsory social security
K66	Activities auxiliary to financial services and insurance activities
L68	Real estate activities
M69-M70	Legal and accounting activities
M71	Architectural and engineering activities; technical testing and analysis
M72	Scientific research and development
M73	Advertising and market research
M74-M75	Other professional, scientific and technical activities; veterinary activities
N	Administrative and support service activities
O84	Public administration and defence; compulsory social security
P85	Education
Q	Human health and social work activities
R-S	Other service activities
T	Activities of households as employers; producing activities of households for own use
U	Activities of extraterritorial organizations and bodies

Table 4: **Industries in WIOD**