

INTERNATIONAL TRANSPORT COSTS: NEW FINDINGS FROM MODELING ADDITIVE COSTS*

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Abstract

This paper investigates the pattern of international transport costs over time, using information contained in the US imports flows from 1974 to 2019. First, we document the importance of the per-unit component of transport costs. It represents between one-third and one-half of overall transport costs. Second, allowing for time-varying per-unit costs, we find that the downward trend in international transport costs comes from the reduction in “pure” transport costs over time, with trade composition effects playing a minor role. In both aspects, our results point to the importance of the additive component in accounting for international transport costs.

JEL classification: F10, N70, R40

Keywords: Transport costs estimates, non-linear econometrics, period 1974-2019, additive costs, trade composition effects

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1 Introduction

Trade costs are central to international economic analysis. In particular, they are known to be a major obstacle to international economic integration and international trade flows. Defined as the costs associated with the exchange of goods across national borders, trade costs are usually split between transaction costs, policy costs, time costs and transport costs *per se*. Many argue that the latter have substantially decreased with technological advance in transportation, infrastructure development and new communication technologies. However, several empirical evidence suggest that transport costs remain large and deserve attention.¹ In addition, progress in transportation techniques (which reduces the constant-dollar cost of transport) should be compared with technical progress in production (which reduces the constant-dollar cost of production) to get a clear picture of the evolution of the transport costs burden. The latter also depends on whether the cost is in proportion of the value of goods traded (hence does not distort relative prices) or a cost per unit traded (the additive form conversely affecting relative prices). If a complex task, having a clear view of the international transport cost burden is of key importance, since the answers to several important (both academic and policy) economic questions depend in large part on how much distance-based costs affects trade, such as, among others, the dynamics of agglomeration, the profitability of outsourcing or the gains from trade liberalization. The main contribution of the paper is to bring new insights on this issue.

Our paper contributes to the literature by providing a thorough empirical investigation of international transport costs over time based on US imports flows from 1974 to 2019. Importantly, our empirical setting carefully distinguishes between multiplicative and additive transport costs, which proves to be key in the characterization of international trade patterns. While most of the international trade literature has modeled trade costs as an ad-valorem tax equivalent (i.e. as a constant percentage of the producer price per unit traded, part of the “iceberg cost” hypothesis in Samuelson’s (1954) terminology Samuelson (1954)),² a recent strand of the empirical literature points to the existence of an additive component, that is, a cost per unit traded (see, among others, Irarrazabal et al. (2015), or Martin (2012)). Based on US sectoral data, our own estimates also point out the importance of additive costs in international transport costs. Contributing one step further, we provide estimates of the size of both additive and ad-valorem transports costs by sector (at the 3-digit level) and country of origin on a yearly basis over 1974-2019 and by transport mode (air or maritime transport).

Our results may be summarized in two main new findings. First, additive transport costs are quantitatively sizable. On average over 1974-2019, the additive cost is estimated

¹Anderson & Van Wincoop (2004) find that around 30% of international trade costs are attributable to transport costs. Equivalently, international transportation costs represent a 21% markup over production costs. Further, the sizable elasticity of trade with respect to freight costs obtained by Behar & Venables (2011) (around -3) testifies to the impact of transport costs on trade flows. Disdier & Head (2008), among others, point out that distance as an incompressible cost is still a very important determinant of trade flows.

²Strictly speaking, the “iceberg cost” includes both the ad-valorem dimension of trade cost and the fact that these costs are paid in terms of the good that is traded. As this last element is irrelevant in our case, we use the terms “iceberg” and “ad-valorem” interchangeably, as is commonly done in the literature.

to be **1.8% and 2.9% A AJUSTER** of the export price in air and vessel transport respectively (at the 3-digit classification level). This is slightly lower than our estimates for the ad-valorem component (**2.5% and 3.2% for air/vessel** respectively on average over the period). Put differently, additive costs represent between **one-third and almost one-half** of the overall transport costs. To the best of our knowledge, our paper is the first to provide such an extensive quantitative measure of both ad-valorem and additive costs in total transport costs. This represents a valuable insight for calibrating related international trade or business cycle models. We also provide an empirical assessment of what standard international trade models lose by skipping additive transport costs. Quantitatively, the omission of the additive term leads to overestimate the ad-valorem component by roughly a **factor 2**. Further, the goodness of fit is systematically better when the additive component is included in the regression, even when taking into account the removed degree of freedom.

Second, we find that the main source of the downward trend in overall transport costs comes mainly from the reduction of transport cost *per se*, , by roughly **50% in air shipping and 60% in vessel shipping over 1974-2013**.³ Specifically, trade composition effects have only limited influence in accounting for the downward trend of international transport costs, and when they matter (in maritime transport), composition effects amplify the reduction of pure transport costs. This contrasts with the conclusion obtained by Hummels (2007) yet also on US import flows. Hummels (2007) finds that total transport costs have decreased in both air and maritime shipment, but less so than “pure” transport costs, because trade composition effects have partly offset the pure transport costs decrease, thereby attenuating the overall downward trend in transport costs. Importantly, we show that the difference of results can be attributed to the new method of modeling the additive component that we offer. Allowing the share of additive costs to vary across time, products and country partners (rather than being constant as in Hummels, 2007), turn out to be key in the decomposition of underlying sources of the decrease of overall transport costs observed over the period.

In both aspects, our results point to the importance of the additive component in accounting for international transport costs. In this respect, it contributes to the literature that challenges the dominant role of iceberg costs in international trade (even in the case of ice transport, see Bosker & Buringh, 2018). As shown by Alchian & Allen (1964), the relative price of two varieties of some goods will depend on the level of additive trade costs. In this context, the relative demand for more expensive/higher-quality product goods increases with trade costs (“shipping the good apples out”). This is consistent with the empirical findings by Hummels & Skiba (2004), who estimate the elasticity of freight rates with respect to price to be well below unity.⁴ Recent empirical studies based on micro-level data also provide strong empirical support for the role of additive costs

³Throughout the paper, we refer to “pure” or “*per se*” transport costs changes as the changes over time in the transport costs for a given product/country partner, ie excluding trade composition effects (i.e. changes over time in the baskets of imported goods and/or the origin countries).

⁴Also, their estimates imply that doubling freight costs increases average free alongside ship (fas) export prices by 80% to 141%, consistent with high-quality goods being sold in markets with high freight costs.

(i.e. cost per unit exported) in international trade costs.⁵ If in empirical support for additive trade costs, these papers yet do not allow for a quantitative measure of these cost (neither for the ad-valorem costs). One important contribution of the paper is to provide quantitative estimates of both type of transport costs.⁶

Closely related to our paper is the work by Irarrazabal et al. (2015), which develops a structural framework for inferring relative additive trade costs from firm-level trade data. Implementing their methodology on Norwegian firm-level export data for the year 2004, they find that, for the median shipment, additive costs (in Norwegian crowns) amount to 6% of the export price multiplied by the ad-valorem cost (also expressed in Norwegian crowns). Our results share in common with Irarrazabal et al. (2015) the important role of the additive component of international trade costs. Yet, our paper complements their findings in two main respects. First, while our study covers a narrower set of trade costs focused on transport costs, their data and their empirical approach only allows the identification of the ratio of the additive cost to the export price multiplied by the ad-valorem cost; by contrast, our estimation strategy enables us to uncover separately both values of the ad-valorem and the additive costs. From this, we can rebuild the ratio in similar terms to them, thereby gaining in generality in this respect. While Irarrazabal et al. (2015) find that, for an export price multiplied by the ad-valorem cost of 100 USD, 6 USD are paid in additive trade costs, our results point to a value paid in additive transport costs of **2.8 USD for maritime shipping and 1.5 USD for air transport for 2004**. This comparison of results suggests that between **a third and a half of the additive trade costs** are attributable to the transport sector (depending on the transport mode). Second, we exploit exhaustive information about the imports flows of the US over a wide time-span from 1974 to 2019. In this respect, our results deliver a broader view of the magnitude of additive costs in international trade over time. In particular, we show that the modeling of additive costs is of critical importance in determining the underlying sources of the trends patterns of international transport costs observed over the last fifty years.

Big Picture. Our results have important implications for both international trade and international macroeconomics models. Beyond the positive aspect, several recent papers also point out the normative implications of additive trade costs.⁷ These results suggest that important welfare gains can be achieved by reducing additive trade costs. On the same token, as additive costs distort relative prices, they are very likely to affect the

⁵Based on a firm-product-level database of French exporters, Martin (2012) finds that firms charge higher unit values for exports to more remote countries, supporting the importance of additive costs. Using transaction-level trade data from Colombia, ? estimates that the transport cost elasticity varies greatly across industries, with a value of 0.8 for the average industry, in contrast with the iceberg specification.

⁶On top of the previously cited papers about additive costs, our paper also relates to Kropf & Sauré (2016), who estimate the size and shape of per-shipment costs based on Swiss data, and to Alessandria et al. (2010) or Hornok & Koren (2015a,b), who point out the role of per-shipment costs (among which, administrative costs) in generating some “lumpiness” in international trade transactions.

⁷Sorensen (2014) extends Melitz (2003)’s seminal model of international trade by including additive trade costs, in addition to the ad-valorem component. A key analytical result is that the welfare gain from a reduction in trade barriers is higher for a decrease in additive costs than a decrease in ad-valorem costs, due to the alteration of relative prices in a heterogeneous-firms trade framework. This is confirmed by Irarrazabal et al. (2015)

international transmission of shocks in international business cycles models. In both fields yet, not much progress has been made in quantifying such gains. One potential reason is the lack of an empirical characterization of the additive component of trade costs (the one exception being Irarrazabal et al., 2015). The quantitative results we provide in the paper allow making one step in filling that gap. **To develop.**

The paper is built as follows. First, we estimate the values of international transport costs annually throughout the period 1974-2013 by transport mode, explicitly distinguishing between the additive and the ad-valorem components. Section 2 reports the mean values of the transport costs estimated over the period (by transport mode). Relying on these estimation results, we then provide a decomposition of the transport costs trend patterns, between what arises from changes in the trade composition (by product and/or partner country), and what is attributable to changes in transport costs *per se*. Section 3 is devoted to this analysis, while Section 4 checks the robustness of our results to the separability assumption and the weighting scheme. Section 6 concludes.

2 Estimating international transport costs

2.1 Data

Our analysis of transportation costs consists of exploiting the difference between commodity-level export and import prices, as in Hummels (2007). The database we use to construct our measure of transport costs comes from the US annual “Imports of Merchandise” provided by the US Census Bureau, spanning 1974 to 2019 (details on the database provided in Appendix A). We first use customs values, quantities and freight costs to recover free alongside ship (fas) and cost-insurance-freight (cif) prices, by good, country of origin and transportation mode.⁸ More precisely, the (unit) fas price is computed as the total “customs value” in the US trade statistics divided by the shipping weight, both items being conditional to the transport mode; in other words, it is the price for one kg of the goods net of transportation costs, by transport mode.⁹ The cif price is then computed as the sum of the customs value and freight charges, once again divided by the shipping weight. Our dependant variable is finally computed as the ratio of the cif price divided by the fas price. By construction higher than 1, the variable provides a measure of transport costs as a proportion of the goods’ price, an ad-valorem equivalent. This is

⁸The related literature commonly refers to the fob (free on board) price rather than the fas price. The fas price means that the seller must transport the goods all the way to the dock, close enough to be reached by the crane of the ship it will be transported in. It is also the seller’s responsibility to clear the goods for export. The FOB price means that the seller is obligated to bring the goods all the way to the port, clear the goods for export, and see that they are loaded onto the ship nominated by the buyer. Once the goods clear the railing of the vessel, the buyer assumes the risk. Note that this term is used exclusively for maritime and inland waterway transport. While both terms are closely related, the US Foreign Trade Statistics reports fas prices.

⁹One might be concerned by the fact that unit prices are calculated as the value divided by the shipping weight, rather than to the quantity of goods. This is due to the fact that in the Census data, information on the quantity of goods is not mode-specific. We yet provide a robustness check where unit values are built as the ratio between value and quantity of goods per observation, on a specific sub-sample restricted to US imports flows that only use one single transport mode. **See Section XXX.**

quite a standard and widespread strategy, as emphasized by Anderson & Van Wincoop (2004).

Obviously, this dataset has limitations. First, it restricts our analysis to the study of international *transport* costs, as our measure of the cif-fas price gap only covers freight, insurance and handling costs. It is thus silent about the other dimensions of international trade costs. Second, in terms of transport costs *per se*, our measure omits the “indirect” costs related to the time value of goods on their way to their export market (including holding cost for the goods in transit, inventory cost due to buffering the variability of delivery dates, preparation costs associated with shipment size, etc.). In this respect, this dataset embraces only a partial view of international transport barriers. However, it is also clear that these direct transport costs do represent a sizable share of trade costs. According to Anderson & Van Wincoop (2004), the 21% markup over production costs coming from transport costs includes both directly measured freight costs (11%) and “indirect” costs that amount to a 9% tax equivalent. Further, the evidence summarized in Anderson & Van Wincoop (2004) points to the persisting importance of direct transport costs, especially compared to other trade barriers. They remain more important than, e.g., policy barriers (8% tax equivalent), language barrier (7%) or information cost (6%).¹⁰

Exploiting this dataset also has three advantages. First, it comes from a single, homogenous and trustworthy customs source. This limits the measurement error bias. Based on customs declarations, the US Imports Database inventories all imports (both values and quantities), by country of origin, to the United States at the HS 10-digit level, with a concordance code to the SITC coding system. In addition, the database reports information regarding freight, insurance and handling expenditures by transportation mode, land/ocean (or “vessel”) and air. We will make use of this to highlight potential differences in the dynamics of transport costs across transportation mode. Second, this dataset provides both the import price and the export price for the same good (for a given origin country). This is highly valuable, as it gives us a direct measure of international transport costs (at the country/sector level), from which we can estimate separately the *levels* of both the iceberg costs and of the additive costs, in contrast to e.g. Irarrazabal et al. (2015). Third, this dataset is available over a long time span, which enables us to analyze the trend patterns of international transport costs over the period 1974-2019.¹¹

As detailed below, the use of a non-linear estimator triggers computational limitations that limit the level of possible detail, especially when covering a long period of time. This drives us to estimate international transport costs at the 3-digit classification level, exploiting heterogeneity between products at the SITC-5 classification level. We ensure the robustness of these results by conducting two types of alternative estimates: *i*, within each 3-digit sector, exploiting heterogeneity between HS-10 products. Notice that this can

¹⁰In his survey, Hummels (1999) mentions several papers which all indicate that transport costs pose a barrier similar in size to, or larger than tariffs. In the same vein, Limao & Venables (2001) highlight the importance of infrastructures for trade costs in general, through their impact on transport costs.

¹¹Note that, as mentioned by Lafourcade & Thisse (2011), our transport costs measures are based on actual trade flows, i.e. ignoring those flows that did not happen because of presumably prohibitive transport costs. In light of this, the estimated values that we obtain can be viewed as the lower bounds of the “potential” transport costs.

be done from 1989 onwards for which HS-10 data are available; *ii*, running the estimation at the 4-digit sector level (still with 5-digit products) for some selected years. The selected years for the 4-digit level estimations are: 1974, 1977, 1981, 1985, 1989, 1993, 1997, 2001, 2005, 2009, 2013. Comparing different levels of aggregation is useful to check differences and the presence of biases precisely due to aggregation. However, we obtain no substantial difference between the results obtained for the benchmark 3-5 sector-product classification levels and those considering either the 3-10 and 4-5 ones (See Appendix C. **ONLINE? IN TEXT? ADD** Depending on the year, this leaves us with around 200 3-digit sectors, from around 200 countries of origin.

2.2 Estimating transport costs: empirical specification

Estimation strategy Starting from the observed transport costs, we decompose the respective sizes of their two sub-components, ad-valorem and additive transport costs. From this, we can deduce the share of the additive component in total transport costs, which also interprets as the elasticity of transport costs with respect to the unit price (in absolute value), as we show below.

Our starting point relates the import price (at the entry gate) of a given good as equal to the export price (at the export gate) plus freight charges. Specifically, denoting by p the price per kg of goods paid by the importer (import, or cif price), \tilde{p} the (per kg) export (or fas) price and f the shipping charge per kg shipped, we have: $p = \tilde{p} + f$. As in Hummels (2010), assume the shipping charges may depend on the price \tilde{p} according to the functional form $f = \tilde{p}^{1-\beta} X$, where X represents all other elements of transport costs (such as distance, port quality, etc.). The link between the import, export prices and shipping charges is hence given by:

$$p = \tilde{p} + f \Leftrightarrow p = \tilde{p} + \tilde{p}^{1-\beta} X$$

Defining transport costs $TC \equiv \frac{p - \tilde{p}}{\tilde{p}}$, we then obtain:

$$TC \equiv \frac{p - \tilde{p}}{\tilde{p}} = \tilde{p}^{-\beta} X \quad (1)$$

From Equation (1), it is straightforward that β is equal to the elasticity of transport costs to the unit price (in absolute value):

$$\frac{\partial TC}{\partial \tilde{p}} \frac{\tilde{p}}{TC} = -\beta \quad (2)$$

From Equation (1), we can identify a first polar case where $\beta = 0$. Shipping charges are proportional to the fas price, such that $p = \tilde{p}(1 + X)$: Only ad-valorem costs apply. At the other extreme, the case $\beta = 1$ corresponds to shipping costs being independent of the unit price, with the cif price the sum of the unit price and the shipping cost: Transport costs are fully additive. This suggests that, the closer β to 1, the more prevalent additive costs in total transport costs. One can analytically show that β is indeed equal to the

share of additive costs in total transport costs.

To do so, start from the link between the link between cif, fas prices and transport costs by explicitly decomposing between the ad-valorem and the additive costs as:

$$p = (1 + \tau)\tilde{p} + t \quad (3)$$

$$\Leftrightarrow p = (1 + \tau)\tilde{p} + \tilde{t}\tilde{p} \quad (4)$$

with $\tau \geq 0$ the ad-valorem cost and $t > 0$ the additive shipping charge per kg transported (Equation (3)). Notice that we can rewrite the additive cost as a function of the cost per USD shipped $\tilde{t} \equiv \frac{t}{\tilde{p}}$, as in Equation 4. Starting from Equation (4), the elasticity of transport costs to the unit price \tilde{p} can be shown to be equal to:¹²

$$\begin{aligned} \frac{\partial TC}{\partial \tilde{p}} \frac{\tilde{p}}{TC} &= \frac{-\frac{t}{\tilde{p}}}{\tau + \frac{t}{\tilde{p}}} \\ &= \frac{-t}{\tau + t} \end{aligned} \quad (5)$$

Comparing Equations (1) and (5), it is straightforward that the unit price-elasticity of transport costs (in relative terms) is also equal to the share of additive costs in total transport costs.

While many in the related literature provide an indirect measure of additive costs by estimating the elasticity of freight charges to the unit price (Hummels & Skiba, 2004, ?), thereby relying on Equation (2), we propose an alternative route. Based on Equation (4), we exploit our dataset to obtain explicit measures of both transport costs components τ and t (or \tilde{t}). From this, we can deduce the price-elasticity of transport costs as the share of additive costs in total transport costs through Equation (5).

Obtaining the estimated equation Let us denote i the origin country, and k the product (at the 5-digit level in our benchmark estimate), for each year-mode specific flow. For sake of reading convenience, we skip the year and transport-mode dimensions in the notations. Transforming the above equation (4) as the percentage change in prices induced by transportation (and get rid of the kg unit), we get the following baseline specification underlying our estimation:

$$\frac{p_{ik}}{\tilde{p}_{ik}} - 1 = \tau_{ik} + \frac{t_{ik}}{\tilde{p}_{ik}} \quad (6)$$

We follow Irarrazabal et al. (2015) by considering that i) both ad-valorem and additive costs are separable between the origin country (i) and the product (k) dimensions, and ii) this separability is in a multiplicative way for the former and an additive way for the latter. In other words, τ_{ik} and t_{ik} from Equation (6) are written as:¹³

¹²See Appendix XXX for a formal demonstration.

¹³Notice that, given the magnitude or order of transport costs, assuming an additive or a multiplicative form for country/product fixed effects does not make a substantial difference since, for small values (as

$$1 + \tau_{ik} = (1 + \tau_i)(1 + \tau_k) \quad (7)$$

$$t_{ik} = t_i + t_k \quad (8)$$

As a result, our underlying structural equation is specified as:

$$\frac{p_{ik}}{\tilde{p}_{ik}} - 1 = (1 + \tau_i)(1 + \tau_k) - 1 + \frac{t_i + t_k}{\tilde{p}_{ik}}$$

The ratio $\frac{p_{ik}}{\tilde{p}_{ik}}$ has a lower bound of one, since by construction, the import price p cannot be lower than the export price ($p_{ik} \geq \tilde{p}_{ik}$). Taking into account this constraint in the estimate implies that the error term should be always positive. We ensure that this constraint is fulfilled by specifying the error term as follows:

$$\frac{p_{ik}}{\tilde{p}_{ik}} - 1 = \left((1 + \tau_i)(1 + \tau_k) - 1 + \frac{t_i + t_k}{\tilde{p}_{ik}} \right) \times \exp(\epsilon_{ik})$$

where ϵ_{ik} follows a normal law centered on 0. Considered in logs, the above equation becomes:

$$\ln \left(\frac{p_{ik}}{\tilde{p}_{ik}} - 1 \right) = \ln \left((1 + \tau_i)(1 + \tau_k) + \frac{t_i + t_k}{\tilde{p}_{ik}} - 1 \right) + \epsilon_{ik} \quad (9)$$

Since Equation (9) is non-linear, it cannot be estimated using standard linear estimators. All estimates are thus performed using non-linear least squares.¹⁴ Yet, the use of a non-linear estimator triggers computational limitations that limit the level of possible detail, especially when covering a long period of time. Confronted with this trade-off, we estimate international transport costs at the 3-digit level as our benchmark classification, even though data series are available at a more disaggregated product level ($k = 5$ in our benchmark estimates). This amounts to making the additional assumption, that all 5-digit products k in a 3-digit sector s share the same structure of costs.^{15,16}

we generally obtain), we have $\tau_i + \tau_k \simeq (1 + \tau_i) \times (1 + \tau_k) - 1$ and $t_i + t_k \simeq (1 + t_i) \times (1 + t_k) - 1$. We also provide a robustness analysis to the separability assumption. Given the much higher number of fixed effects to estimate, we run this robustness check on a sub-sample of goods/origin countries. See Section 4 for a detailed presentation of this robustness check.

¹⁴The basis of the method is to approximate the model by a linear one and to refine the parameters by successive iterations. The intuitive criterion for convergence is that the sum of squares of residuals does not increase from one iteration to the next. See Wooldridge (2001) for more details.

¹⁵One way to gauge the relevance of this assumption is to provide a decomposition variance exercise on the observed cif-fas price. As reported in Appendix B.3, the share of the observed variance that is accounted for by the between-sectors (s) variance is roughly similar to the between-product (k) variance.

¹⁶One may object that we could preserve the estimation at the 5-digit level by running an OLS estimation on the equation taken in level, i.e. on the basis of Equation (6), specifying the error term additively. This would not solve the problem though, for three main complementary reasons. First, at the 5-digit level the number of fixed effects to include in the estimation would be more than 430,000 (with 216 countries and 2,029 products), making the estimation computationally extremely burdensome, even in OLS. Imposing Equations (7) and (8) to reduce the number of fixed effects would drive us back to the non-linearity issue for fixed effects. Second, making the error term (specified as following a normal law centered on 0) enter Equation (6) additively implies negative values for some of the estimated residuals $\hat{\epsilon}_{ik}$, which is inconsistent with the constraint that $\frac{p_{ik}}{\tilde{p}_{ik}} > 1$. Third, estimating the equation in level does not eliminate the fact that it is non-linear by nature, as long as there are additive costs to estimate (see Equation (6) for $t_{ik} \neq 0$).

This drives us to estimate a modified version of Equation (9), specified as:

$$\ln \left(\frac{p_{ik}}{\tilde{p}_{ik}} - 1 \right) = \ln \left((1 + \tau_i)(1 + \tau_{s(k)}) - 1 + \frac{t_i + t_{s(k)}}{\tilde{p}_{ik}} \right) + \epsilon_{ik} \quad (10)$$

where τ_i , $\tau_{s(k)}$, t_i and $t_{s(k)}$ are the parameters to be estimated, i.e., fixed effects specific to each origin country i and sector s (at the 3-digit classification level), and ϵ_{ik} the residual centered on 0.¹⁷ To eliminate the potential influence of outliers, we exclude 5% of the upper and lower tails of the distribution in the regression variables. These cut-offs are aimed at eliminating reporting or coding errors. We estimate Equation (10) for each year over the period 1974-2013, for each of the transportation modes reported (air or vessel), on a sectoral-origin country basis (i, s) . Depending on the year considered, this leaves us with around 800 fixed effects to estimate by transport mode at the 3-digit level.

stop here

As mentioned in the Introduction, one contribution of the paper is to provide a careful estimation of international transport costs, which decomposes into both an additive and an ad-valorem component. In this respect, our paper relates to the recent literature about the importance of additive costs in accounting for international trade costs (Irrarrazabal et al., 2015, among others). We contribute to this issue by adopting the following strategy. For each year and transport mode, we estimate two models. In Model (a), additive costs are excluded, transport costs being modeled as iceberg costs only (Equation (11)). In this case, the estimated equation simplifies as:

$$\ln \left(\frac{p_{ik}}{\tilde{p}_{ik}} - 1 \right) = \ln (\tau_i \times \tau_{s(k)} - 1) + \epsilon_{ik}^{ice} \quad (11)$$

Under Model (b), transport costs are decomposed in the two additive and ad-valorem dimensions (Equation (10)). From this, we compare the fitting properties and the explanatory power of both models to evaluate the importance of modeling the additive component.¹⁸

After estimating Equation (10), we can rebuild a measure of each component, $\hat{\tau}_{is(k)}^{adv} = \hat{\tau}_i \times \hat{\tau}_{s(k)}$ for the ad-valorem cost and $\hat{t}_{is(k)} = \hat{t}_i + \hat{t}_{s(k)}$ for the additive cost, that are country-sector specific, by year and transport mode. When assuming iceberg costs only

¹⁷Note that, strictly speaking, the exact equation that we estimate is the following:

$$\ln \left(\frac{p_{ik}}{\tilde{p}_{ik}} - 1 \right) = \ln \left(\sum_i \alpha_i^\tau \mathbb{1}_i \times \sum_{s(k)} \alpha_{s(k)}^\tau \mathbb{1}_{s(k)} + \frac{\sum_i \alpha_i^t \mathbb{1}_i + \sum_{s(k)} \alpha_{s(k)}^t \mathbb{1}_{s(k)}}{\tilde{p}_{ik}} - 1 \right) + \epsilon_{ik}$$

After proceeding to the estimation, we uncover the estimated values of the transport costs components τ_i , $\tau_{s(k)}$, t_i , $t_{s(k)}$ from the obtained coefficients α_z^x for $x = \tau, t$ and $z = i, s(k)$ (by year and transport mode). For reading convenience, we adopt a lighter expression of this equation by resorting to the notations of τ_i , $\tau_{s(k)}$ and t_i , $t_{s(k)}$ as a short-cut.

¹⁸One may object that a comprehensive study of the structure of transport costs should also include the third model with only additive costs. This has driven us to estimate this model as well, in which case the estimated equation is written according to: $\ln \left(\frac{p_{ik}}{\tilde{p}_{ik}} - 1 \right) = \ln \left(\frac{t_i + t_{s(k)}}{\tilde{p}_{ik}} \right) + \epsilon_{ik}^{add}$. The main result that emerges is that the model with additive costs only is dominated (in terms of quality of fit properties) by the model with multiplicative costs only (Equation (11)), which is itself dominated by the complete model (Equation (10)), anticipating further results. More details of these results are given in the Online Appendix.

(Equation (11)), we proceed similarly to get $\hat{\tau}_{is(k)}^{ice} = \hat{\tau}_i \times \hat{\tau}_{s(k)}$. In this case, notice that the equation could be estimated relying on a linear form. To preserve comparability of the results, we keep the same non-linear estimation method in both cases. Similarly, as Irarrazabal et al. (2015), we take the average over the sector-country dimension, using the values of each trade flow (*is*-specific) over total yearly trade as a weighting scheme. We thus recover a “synthetic estimate” of each type of transport cost: $\hat{\tau}^{ice}$ for Model (a), $\hat{\tau}^{adv}$ and \hat{t} for Model (b), for each year and transportation mode. These results are reported in Section 2.3.

2.3 The importance of the additive component

Quantification The first step of the analysis consists of providing a quantification of the magnitude of transport costs over time (by transport mode), distinguishing whether the additive component t_{ik} is excluded or included in the estimated equation (Equation (10) or (11)). This allows us to provide estimates for the size of both the ad-valorem and the additive components of transport costs, and assess whether additive costs represent a sizable component of the latter. These results constitute our first original contribution to the literature. We also provide diagnostic tests about the goodness-of-fit measures, which confirm the empirical relevance of adding the additive component in the estimation (see results in Appendix B.2).

Table 1 reports a summary of our results. It displays the mean and median values of each type of transport costs (either ad-valorem estimated alone or estimated along with additive costs), as well as the associated standard deviation, averaged over the period 1974-2013, for estimation driven both at the 3- and 4-digit sectorial level for different specifications and data. The top panel reports the results for a specification based on ad-valorem costs estimated alone (Model (a), based on Equation (11)), while the intermediate panel presents estimates for a specification involving both ad-valorem and multiplicative components (Model (b), based on Equation (10)). Finally, the bottom panel reports the same set of descriptive statistics, but for the actual cif/fas ratio in our data.^{19,20}

Table 1 calls for two types of comments. The first type is of statistical order. As displayed in Table 1, estimated mean values are systematically higher than medians, by around one percentage point. This result is not surprising, given that our key variable is by nature bounded to 0; therefore, outliers can only be positive, pushing the mean upward compared to the median. One can also note that estimated total costs are systematically higher than observed costs, by 0.5 to 1 percentage point. This is first due to the fact that observed data are *de facto* trade-weighted (i.e. by the weight of each good in total trade) while our estimates are based on simple arithmetic means within sector and country.

¹⁹In Appendix B, we report similar results for a sample of years, for both transport modes, at the 3- and 4-digit classification level. Results for all years (available at the 3-digit level) are reported in the Online Appendix, available on the authors’ webpages.

²⁰We present the estimation results for air transport at the 3-digit level, removing the year 1989, as the results reveal the presence of strong outliers that bias the estimates of transport costs upwards this particular year. Overall results (over the whole period) are not substantially affected if this year is included. This can be seen in the results detailed year by year in the Online Appendix, available on the authors’ webpages.

Table 1: Transport costs estimates: summary

Mean value over 1974-2013				
# digit	3 digits		4 digits	
Mode	Vessel	Air (**)	Vessel	Air
Model (a) - With only Ad-Valorem Transport Costs ($\hat{\tau}^{ice} - 1$, in %)				
Mean	5.8	5.1	6.0	4.9
Median	5.1	4.2	5.2	3.7
Model (b) - With Additive & Ad-Valorem Transport Costs				
<i>Ad-valorem term ($\hat{\tau}^{adv} - 1$, in %)</i>				
Mean	3.2	2.5	3.3	2.4
Median	2.8	1.8	2.8	1.6
<i>Additive term</i>				
<i>In % of the export price (\hat{t}/\tilde{p}, in %)</i>				
Mean	2.9	1.8	2.8	1.9
Median	1.9	0.7	1.7	0.8
<i>In USD per kg traded (\hat{t})</i>				
Mean	0.09	1.12	0.08	2.16
Median	0.07	1.04	0.06	1.06
Data				
<i>Transport costs ($p/\tilde{p} - 1$, in %)</i>				
Mean	5.3	5.0	5.6	3.9
Median	4.3	2.0	4.4	1.9
<i>Export price (\tilde{p}), in USD</i>				
Mean	16.0	6488.4	9.6	6643.6
Median	4.1	142.5	4.1	142.2
# obs.	29279	28207	29317	27680
# origin country	188	191	188	189
# products	230	211	666	567

Notes: Statistics are obtained weighting each observation by its value relative to total trade flows. The additive term is expressed in fraction of fas price. For the 4-digit classification, statistics for observed data have been calculated for the same set of years as used for estimation, i.e. 1974, 1981, 1989, 2001, 2009, 2013. (**): 1989 omitted in 3-digit estimation for air.

	3-digit		4-digit	
	air	ves	air	ves
Data				
# obs.	202,298	171,208	41,994	41,773
# sectors	224	239	637	707
# origin countries	214	213	212	209
<i>Observed transport costs</i>				
Mean (in %)	10.6	6.6	13.7	8.2
Median (in %)	6.0	4.7	7.6	5.7
Std. dev.	15.6	7.2	23.0	9.5
Model (A)				
<i>Multiplicative term ($\hat{\tau}^{ice}$)</i>				
Mean (in %)	3.9	4.6		
Median (in %)	3.0	4.0		
Std. dev.	3.4	2.7		
Model (B)				
<i>Multiplicative term ($\hat{\tau}^{adv}$)</i>				
Mean (in %)	4.3	3.2	5.1	3.9
Median (in %)	3.5	2.6	3.9	3.2
Std. dev.	3.2	2.4	4.4	3.0
<i>Additive term (\hat{t}/\tilde{p})</i>				
Mean (in %)	4.4	2.6	6.4	3.4
Median (in %)	1.4	1.3	2.4	1.6
Std. dev.	16.4	11.3	19.3	7.4
<i>Elasticity of transport cost to price ($\hat{\beta}$)</i>				
Mean (in %)	-0.33	-0.37	-0.41	-0.38
Median (in %)	-0.29	-0.34	-0.39	-0.36
Std. dev.	0.26	0.22	0.28	0.25

Furthermore, Table 1 reports values expressed in percentages (for the observed values, $\frac{p_{ik}}{\bar{p}_{ik}} - 1$, in %), whereas all our estimates are based on log-linearization. Therefore, what matters on the statistical ground is that the mean of our predicted values (based on logarithms) must be equal to the mean of the log-linearized data ($\ln\left(\frac{p_{ik}}{\bar{p}_{ik}} - 1\right)$), which does not necessarily imply equality between values. Descriptive statistics showing that both observed and predicted values do match in logarithms are available upon request to the authors.

Interpretation Coming now to interpretation, two main results emerge from Table 1. First, it provides estimation results about the size of the overall transport costs. Table 1 shows that transport costs amount to around a 6% markup in ocean shipping, and 5% markup in air shipping on average over 1974-2013.²¹ If this seems modest in comparison with the 11% of markup obtained by Anderson & Van Wincoop (2004) over a set of industrialized countries, it stands in line with the results obtained by Hummels (2007) for the US economy.²²

Second, and most importantly, Table 1 provides new quantitative evidence about the size of the additive component of transportation costs. On average over the whole period, for sectors defined at the 3-digit level, additive costs amount to 10 cents (0.1 USD) per kilogram exported in maritime transport, and 1.12 USD per kilogram exported in air transport, indicating that freight rates are much higher in the latter case. Expressed in terms of the export price, the additive costs amount to 2.9% and 1.8% for ocean shipping and air transport respectively. This is slightly lower than the estimates for the ad-valorem component, which is estimated at 3.2% and 2.5% for vessel and air shipping respectively (on average over the period). Put differently, the additive component amounts to 48% of total transport costs in vessel, and 42% in Air. This shows that the per-kg cost dimension is quantitatively sizable. For both transport modes, the omission of the additive term seriously biases the ad-valorem term upward, by roughly 2. Additionally, Appendix B.2 reports quality-of-fit diagnostic tests that confirm the importance of the additive cost component. The goodness of fit is systematically better when the additive component is included in the regression, even when taking into account the removed degree of freedom. An important aspect of these results is also to provide quantitative estimates for the values of both additive and ad-valorem transport costs, which can be very useful for more theoretical approaches needing calibration.

Our estimation results on the size of additive transport costs can be compared to Irarrazabal et al. (2015), the most recent evidence on this question. Based on Norwegian trade data for 2004, Irarrazabal et al. (2015) estimate that additive costs (in Norwegian

²¹Expressed as a markup over production costs, transport costs are equal to $\frac{p-\bar{p}}{\bar{p}}$. Under Model (a) (ad-valorem costs only), making use of the figures reported in Table 1 gives a markup of 5.8% in vessel, and 5.1% in air shipping (considering the mean value over the period). Under Model (b), total transport costs are equal to $\frac{p-\bar{p}}{\bar{p}} = (\tau - 1) + \frac{t}{\bar{p}}$. With $\tau - 1 = 0.032$ and $\frac{t}{\bar{p}} = 0.029$ in vessel (as reported in Table 1), we get a value equal to 6.1% in vessel. A similar calculus gives 4.3% in air transport.

²²Beyond country coverage and time period, another plausible explanation for the difference with Anderson & Van Wincoop (2004), lays in the difference of empirical methodology. Anderson & Van Wincoop (2004)'s estimates are based on standard gravity equations, while ours come from a non-linear estimation of a "structural" decomposition of the difference between export and import prices.

crowns) amount to 6% of export price multiplied by the ad-valorem cost (expressed in Norwegian crowns), i.e. $\frac{t}{\tau p} = 6\%$ expressed in our terminology (with $\tau > 1$, and retaining their estimated weighted mean value, which is the one directly comparable to our own results). One important difference with respect to their work is that we can provide separate estimates for each cost component (additive and ad-valorem). From this, we can rebuild the ratio in similar terms to them, allowing us to gain in generality in this respect. Making use of our estimates for 2004 (see Tables B.1 and B.2 in Appendix B), we thus obtain a ratio $\frac{t}{\tau p} = 2.8\%$ in ocean shipping and 1.5% in air transport. This may seem surprisingly low, in contrast to the 6% obtained by Irarrazabal et al. (2015). This can be accounted for by recalling the difference in the type of dataset - hence, of costs, embraced in each case. While the database of Irarrazabal et al. (2015) allows studying trade costs in general, our database covers a subset made of the monetary international transport costs, as we start from the gap between the import and the export prices (on top of differences due to the country coverage of the two databases). In this respect, our two papers can be used in a complementary fashion to infer the proportion of additive trade costs that are due to international shipment. Irarrazabal et al. (2015)'s results imply that, for an export price multiplied by the ad-valorem cost of 100 USD, 6 USD are paid in additive trade costs. For the same export price multiplied by the ad-valorem cost of 100 USD, our results yield the value of 2.8 (1.5) USD paid in additive transport costs for maritime (air) transport.²³ This comparison of results suggests that between 25% (air) and 47% (vessel) of additive trade costs are attributable to international transport. On top of our results summarized in Table 1, this points to evidence that the additive component represents a quantitative sizable dimension of international transport costs.

Time dynamics Given the time coverage of our database, one may then wonder whether this important part of additive costs we put forward, is a long-lasting, i.e. a structural phenomenon. We investigate this point by reporting the share of additive costs in total transport costs on a yearly basis, in both air and vessel transport, based on the weighted-mean values \hat{t}/\hat{p} and $\hat{\tau}$ (in similar terms as those reported in Tables B.1 and B.2. The corresponding values reported in detailed tables are available in the Online Appendix), as displayed in Figure 1. Each yearly value is obtained as: $\frac{\hat{t}/\hat{p}}{\hat{\tau}-1+\frac{\hat{t}}{\hat{p}}}$, expressed in percent of the export price \hat{p} (at the 3-digit level).

In both transport modes, the additive component appears of sizable importance throughout the period. Confirming the results obtained in Table 1, this suggests that additive costs are neither negligible in magnitude nor an erratic phenomenon. On the contrary, they represent a sizable and structural dimension of international transport costs. If the share of additive costs in total costs roughly amounts to 48% (42%) in vessel (air) transport on average, one can further notice that it varies substantially over time, from a minimum of

²³Also notice that, in both papers, starting from the estimated value of the ratio $\frac{t}{\tau p} = x$, we can rebuild the proportion of additive costs in terms of the import price $\frac{t}{\tau p+t} = \frac{x}{1+x}$. Given our estimates for 2004 ($x = 0.028$ and 0.015 in vessel and air transport respectively), we get a ratio $\frac{t}{\tau p+t}$ equal to 2.7% and 1.4% in each transport mode respectively.

Figure 1: Share of additive costs (3-digit classification)



30% to a maximum of 60% depending on the year considered. In the next section, we further investigate the importance of the (varying pattern of) additive costs, as regards the determinants of transport costs time trends.

3 Transport costs time trends: the role of the additive component

In this section, we investigate the trend patterns of international transport costs over time, by exploiting the time dimension of our database. This focus is shared with some of the international trade literature, such as Lafourcade & Thisse (2011), Hummels (2007) and Behar & Venables (2011). Specifically, in the same spirit as Hummels (2007) we investigate the underlying sources behind the downward trend of international transport costs, by identifying the respective roles of the reduction in “pure” transport costs and changes in trade composition effects.

3.1 A first look at the trend patterns

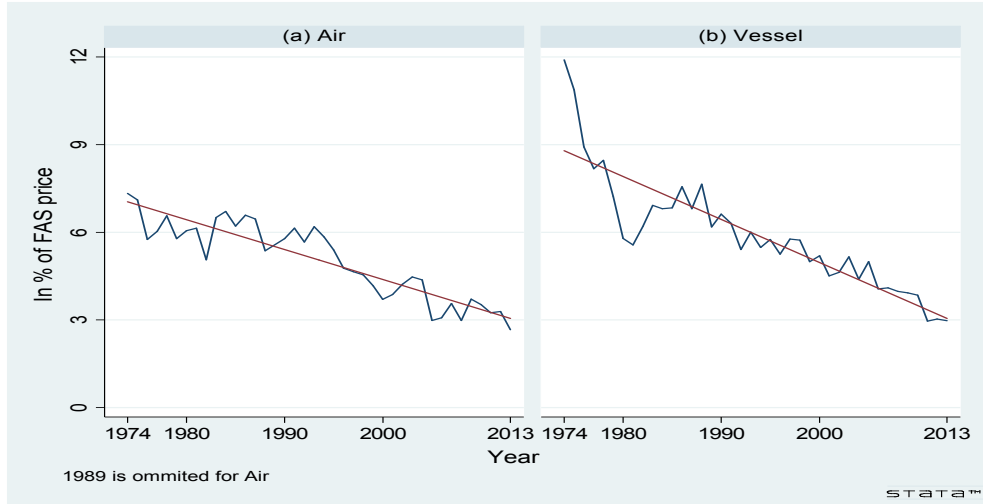
As a first step, Figure 2 displays the evolution of total transport costs over the period, summing the additive and the ad-valorem estimated costs, expressed in percentage of the fas price,²⁴ by transport mode for each year between 1974 and 2013.

As shown in Figure 2, both air and vessel shipping exhibit a downward trend in overall transport costs since 1974, by -2.1% per year for mean air transport costs and -2.0% per year for mean vessel transport costs, implying a 50% decrease in air and a 60% decrease in vessel over the period.²⁵ Using US data, Hummels (1999) found that overall transport cost

²⁴Specifically, we use the yearly values of the estimated transport cost components averaged over the country/product dimensions (at the 3-digit level), corresponding to the numbers reported for each year in detail in the Online Appendix. Each yearly value is obtained as: $\hat{\tau} - 1 + \frac{\hat{\tau}}{p}$.

²⁵One may be puzzled by the high magnitude of estimates for the beginning of the period (until 1980 approximately) for vessel transport. Hummels (2007) finds similar outcomes on tramp prices indexes, and suggests the oil shock as a likely culprit, in a context where technological progress was quicker in aviation than in vessel, allowing a better dampening of oil shocks on air freight rates. In a related manner, one may worry that the strong decrease in transport costs documented in Figure 2 springs from high oil-shock-related transport costs in 1974. However, computing the time trends from 1980 does not dramatically change the picture. The yearly trend from 1980 is -2% for mean air transport costs and -1.6% for mean vessel transport costs. We thus choose to exploit the whole time dimension of our database by taking 1974

Figure 2: Trend in estimated transport costs (yearly mean value)



declined from 6% to 4% of the import value between 1974 and 1996. For the same years, we obtain a total decrease from 6.9% to 4.2% in terms of the export price, on average for air shipping, and from 9.8% to 4.8% for ocean shipping. Overall, our results display trends that are close to those reported by Hummels (1999).

Before making any definite statement, however, it is worth emphasizing that the time trend of international transport costs depends on both the evolution of per product and per partner (“pure”) transport costs and the evolution of the composition of trade. Total transport costs may thus have decreased over time because the share of neighboring countries in total US trade or the share of goods cheaper to transport has increased, independently of any change in transport costs *per se*. As emphasized by Hummels (1999) and Hummels (2007), it is hence necessary to eliminate the composition effects of trade flows to isolate the evolution of pure international transport costs. Specifically, Hummels’s (2007) results underlie the view that trade composition effects partially compensate the reduction in pure transport costs, thereby attenuating the downward trend in overall (observed) transport costs since 1974. Our own results tend to challenge this view, as we further show.

A word on Hummels’ methodology At this point, let us make a brief summary of Hummels’ methodology. He starts from the following specification of the ratio of destination to origin prices modelled as $p_{ikt} = \tilde{p}_{ikt} + \frac{f_{ikt}}{p_{ikt}}$, with f_{ikt} the shipping charge per kg shipped (for a given product k imported from country i in year t). Further, and as in Hummels & Skiba (2004), Hummels (2007) writes the per kg shipping charge as $f_{ikt} = \tilde{p}_{ikt}^{1-\beta} X_{ikt}$, where X_{ikt} represents other costs shifters (distance, port quality, etc.) Accordingly, his transport cost measure TC_{ikt} writes is written as:

as starting date of our time-trend analysis.

$$TC_{ikt} \equiv \frac{p_{ikt} - \tilde{p}_{ikt}}{\tilde{p}_{ikt}} = \tilde{p}_{ikt}^{-\beta} X_{ikt} \quad (12)$$

Notice that β can be interpreted as the elasticity of transport costs to the export price (in absolute value). As such, a value of $\beta = 0$ corresponds to the standard case of “iceberg” costs, in which transport costs are purely ad valorem. At the other extreme, $\beta = 1$ means that all transport costs are additive. Accordingly, the estimated value of β can be interpreted as the share of additive costs in total transport costs. Equation (12) is the baseline specification from which Hummels (2007) decomposes the changes in transport costs over time between trade composition effects and changes in “pure” transport costs, as described in more detail in Appendix D.2. In doing so, Hummels (2007) implicitly assumes β constant across the triplet origin country origin/product/year. Put differently, this means that the share of additive costs in total costs does not vary across these dimensions.

Challenging the β ’s constancy assumption As Figure 1 (based on the yearly estimates of transport costs averaged over the country/sector dimension) suggests, the share of additive costs is rather varying over time, in both transport modes. We investigate this point deeper by reporting the histogram of the distribution of the share of additive costs in total costs. To do so, we start from Equation (6) with the trade costs measure on the left-hand side, from which we deduce the formulae to get the elasticity of transport costs to the export price, i.e. β , according to:

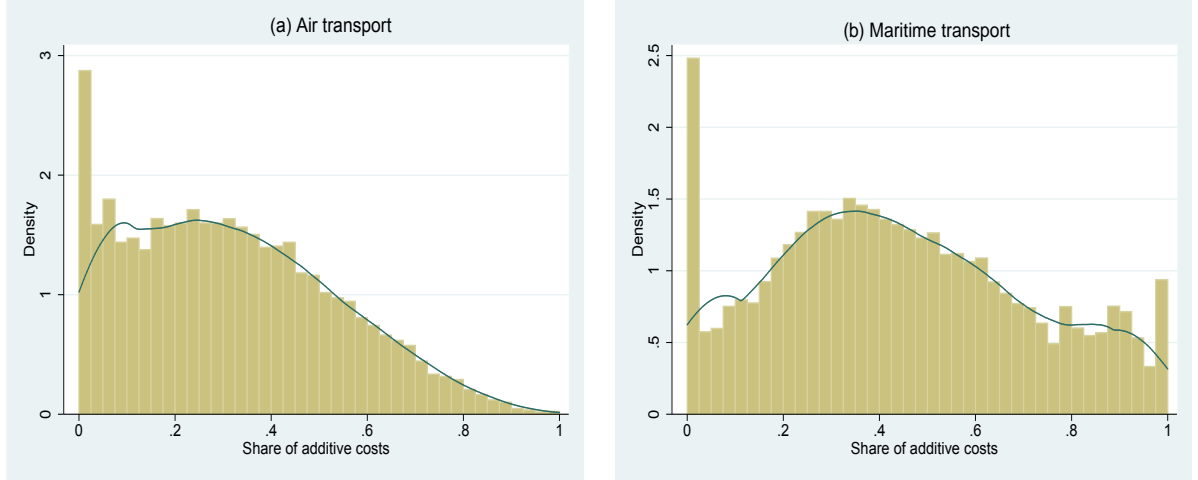
$$\begin{aligned} \beta_{ikt} &\equiv \frac{\partial TC_{ikt}}{\partial \tilde{p}_{ikt}} \frac{\tilde{p}_{ikt}}{TC_{ikt}} \\ &= \frac{\hat{t}_{ikt}/\tilde{p}_{ikt}}{\hat{t}_{ikt}/\tilde{p}_{ikt} + \hat{\tau}_{ikt} - 1}, \end{aligned}$$

making use of our first-stage estimates for both the additive and the ad-valorem components (\hat{t}_{ikt} and $\hat{\tau}_{ikt}$). We can then rebuild the value of the elasticity on a per product-year-country basis. The histogram of the distribution of the estimated β_{ikt} is reported in Figure 3, in panels (a) and (b) for air and maritime transport respectively.

As displayed in Figure 3, for both transport modes the distribution of β_{ikt} over the triplet (year, product, origin country) is smoothly distributed over the interval $[0, 1]$, with a mode of the distribution standing around 0.3-0.4 depending on the transport mode, consistently with our previous findings. This stands in sharp contrast with the assumption made by Hummels & Skiba (2004) or Hummels (2007), which would imply a distribution concentrated on a single point. Rather, this suggests that the elasticity of transport costs to the export price, or equivalently the share of additive costs in total costs, is varying across time, product and country partner.²⁶ In the next section, we shed light on the role of this result in the analysis of the underlying sources of the overall transport costs trend

²⁶We have checked that it is also the case when we look at the distribution over the range of origin countries or products, for a given year. These results are not reported for sake of space, but are available upon request to the authors.

Figure 3: Share of additive costs in total costs: Histogram



Notes: Distribution of β_{ikt} over the triplet (year,product,country), weighted by share of yearly value of flow.

patterns, between trade composition effects and pure transport costs.

3.2 Empirical specification

Based on the above results, we provide a decomposition of the transport costs trends between the trade composition effects and the “pure” transport costs time trends, which explicitly takes into account the varying share of additive costs over time, country partner and product.²⁷ An important contribution of the paper is to show the crucial role of this (empirically relevant) assumption, as it notably modifies the conclusions relative to the role of trade composition effects. We start with the presentation of our estimation strategy before turning to the results.

3.2.1 Estimation strategy

The estimation carried out in Section 2.3 provides us with the additive and ad-valorem measures of international transport costs (Equation (10)), which vary over time, product and origin country (i.e., \hat{t}_{ikt} and $\hat{\tau}_{ikt}$). Starting from these values, for each additive and multiplicative cost component (by transport mode) we extract the pure transport cost measure by the mean of a time fixed effect. Precisely, we extract the changes over time in the pure transport cost dimension by assuming a composition of trade flows by country partner and product that is constant throughout the period, and equal to the one observed in 1974. We conduct the same analysis on an overall transport costs measure, built by combining the two estimated components (additive and iceberg) in a unified measure of transport costs.²⁸ The objective is to obtain six time series, all built as indices with the reference value 100 in 1974: three time series for the unfitted transport costs

²⁷See Appendix D.2 for a detailed comparison of Hummel’s (2007) methodology and ours.

²⁸Note that the unfitted total transport costs are virtually the same as those reported in Figure 2, but reported from another perspective (basis 100 in year 1974).

measures $\{\Gamma_t^{add,raw}, \Gamma_t^{adv,raw}, \Gamma_t^{tc,raw}\}$ (additive, ad-valorem and total cost respectively), and three series for the fitted values $\{\Gamma_t^{add}, \Gamma_t^{adv}, \Gamma_t^{tc}\}$ (additive, ad-valorem and total cost respectively).

One advantage of this method is that it yields measures of transport costs (fitted and unfitted) that are easily comparable between transport modes and transport cost components. For each cost component (additive and ad-valorem) as well as for the total transport cost, comparing the unfitted measure and the fitted measure (composition effects excluded) makes it possible to identify if the decrease observed over the period in the unfitted series is due to trade composition effects (for instance, changes in the country partners, in the type/quality of products traded), or if it is the pure transport costs (for instance, insurance or handling costs) that have reduced over time. We now describe the method to extract these series (with more details provided in Appendix D).

3.2.2 Estimation method for each additive and multiplicative component

We begin by describing the estimation method to extract the fitted and unfitted series for both the additive and the multiplicative components, before turning to the ‘total costs’ series.

Obtaining the “pure” transport costs component series - The empirical strategy to find the fitted transport cost measure (i.e. extracting from trade composition effect) can be described as a two-stage process. First, we decompose the estimated measure in the three product/country/time dimensions, using fixed effects. For the estimated ad-valorem component, we estimate the following equation:

$$\ln(\widehat{\tau}_{ikt}) = \delta + \underbrace{\sum_{i \neq \text{ARG}} \alpha_i \cdot \mathbb{1}_i}_{(a)} + \underbrace{\sum_{s(k) \neq 011} \beta_{s(k)} \cdot \mathbb{1}_{s(k)}}_{(b)} + \underbrace{\sum_{t \neq 1974} \gamma_t \cdot \mathbb{1}_t}_{(c)} + \epsilon_{ikt} \quad (13)$$

where $\mathbb{1}_i$ and $\mathbb{1}_{s(k)}$ represent country and sector fixed effects.²⁹ Equation (13) is estimated using OLS, with a weighting scheme based on the value of each flow in the total value of flows for the relevant year. As for the additive component, given that the sector fixed effect and the country fixed effect are additive rather than multiplicative by construction, we estimate the following equation using non-linear least squares:³⁰

²⁹Throughout the exercise, we consider Argentina, the sector 011 and the first year of our dataset 1974, as references for the country, product and year dummies.

³⁰For sake of notational simplicity, we do not distinguish the coefficients associated with the fixed effects between Equations (13) and (14), even if they are specific to the type of transport costs considered (e.g. the series of γ_t differs from one estimation to the other). Note that we apply the same weighting scheme as for the OLS regression (based on the relative value of the flow).

$$\ln(\widehat{t}_{ikt}) = \ln \left(\delta + \underbrace{\sum_{i \neq \text{ARG}} \alpha_i \cdot \mathbb{1}_i}_{(a)} + \underbrace{\sum_{s(k)} \beta_{s(k)} \cdot \mathbb{1}_{s(k)}}_{(b)} \right) + \underbrace{\sum_{t \neq 1974} \gamma_t \cdot \mathbb{1}_t}_{(c)} + \epsilon_{ikt} \quad (14)$$

As displayed in Equations (13) and (14), we decompose the estimated transport cost component in three elements: the country dimension (Term (a)), the product dimension (Term (b)) and the pure transport costs time trend (Term (c)). Note that Equations (13) and (14) preserve our specification of the ad-valorem and additive costs of Equations (7) and (8), as we consider that the iceberg cost is the product of the country of origin and the goods dimension, while the additive cost is the sum of the two dimensions. Both equations are estimated by transport mode.

In this exercise, we are interested in isolating the change in the time dimension of each transport cost component. This constitutes the second stage of our procedure. As for the ad-valorem component defined in $[1; +\infty]$, from the estimation of Equation (13), we build the variable Γ_t^{adv} , for each year $t \geq 1974$, according to:

$$\Gamma_t^{adv} = 100 \cdot \frac{\bar{\tau}_{1974} \cdot \exp(\gamma_t) - 1}{\bar{\tau}_{1974} - 1} \quad (15)$$

with $\bar{\tau}_{1974} = \exp(\delta + \sum_i \alpha_i + \sum_s \beta_s)$ the mean ad-valorem transport cost in 1974 (see details in Appendix D). In plain words, we measure how these costs have changed over time by blocking the composition of trade flows by product and country partners to the one observed in 1974 (the beginning of our sample).

As for the additive cost defined in $[0; +\infty]$, we build the variable Γ_t^{add} , the reference year being 1974 (ie, with $\gamma_{1974} = 0$) according to:

$$\Gamma_t^{add} = 100 \cdot \exp(\gamma_t) \quad (16)$$

As a result, the two series Γ_t^{adv} and Γ_t^{add} have a straightforward interpretation in percentage changes from the initial value of 100 for $t = 1974$.

Obtaining the unfitted measures - The objective is to find the unfitted transport cost component (additive and multiplicative) built as an index with reference value 100 in 1974, starting from the estimated values previously obtained ($\widehat{\tau}_t$, \widehat{t}_t , for each year t from 1974 to 2013). To do so, we apply the simple formula to get the following indices, for the ad-valorem and the additive cost components respectively:

$$\Gamma_t^{adv,raw} = 100 \times \frac{\widehat{\tau}_t}{\widehat{\tau}_{1974}}, \quad \Gamma_t^{add,raw} = 100 \times \frac{\widehat{t}_t}{\widehat{t}_{1974}}$$

3.2.3 Estimation method for the total transport cost measures

We also build two measures of the “total” transport costs, combining our estimates of the two additive and ad-valorem components, for both the unfitted series and the pure transport cost series (i.e. composition effects excluded). As for each additive and ad-valorem component, the objective is to get a measure of total transport cost changes built as an index starting from the value 100 in 1974. Even if obeying the same logic, we proceed slightly differently for the unfitted and the fitted measures, as we now explain.

Obtaining the unfitted total transport cost index - For each transport mode, we build the total transport cost series based on Equation (6) according to:

$$\widehat{tc}_t^{raw} = \widehat{\tau}_t^{adv} - 1 + \frac{\widehat{t}_t}{\widehat{p}_t}$$

where $\widehat{\tau}_t^{adv}$ and \widehat{t}_t are the average values over the country/sector dimension estimated (conditional on a year and a transport mode), as explained in Section 2. Recall that $\widehat{\tau}_t^{adv} - 1$ measures the ad-valorem transport cost component and $\frac{\widehat{t}_t}{\widehat{p}_t}$ the additive component, both expressed as percentage of the fas price. We then transform this value in an index with base year 1974, applying a similar formula as above (by transport mode):

$$\Gamma_t^{tc,raw} = 100 \frac{\widehat{tc}_t^{raw} - 1}{\widehat{tc}_{1974}^{raw} - 1}$$

Obtaining the fitted total transport cost index - The same logic as above applies to constructing the fitted measure of total transport cost (i.e. composition effect excluded), with one notable exception: Fitted ad-valorem and additive components have not been estimated in value, but extracted and built as indices. In a first step then, we rebuild the fitted measures of each transport cost component in value starting from these indices. For the ad-valorem component, this can be obtained by rewriting Equation (34):

$$\widehat{\tau}_t^{pure,adv} = \frac{\Gamma_t^{adv} (\bar{\tau}_{1974} - 1)}{100} + 1$$

with $\widehat{\tau}_t^{pure,adv} \equiv \bar{\tau}_{1974} \cdot \exp(\gamma_t)$ the yearly value of the pure (fitted) ad-valorem cost. A similar reasoning starting from Equation (36) gives the fitted value for the additive cost component as:

$$\widehat{t}_t^{pure} = \frac{\Gamma_t^{add}}{100}$$

with $\widehat{t}_t^{pure} \equiv \exp(\gamma_t)$ the yearly value of the pure (fitted) additive cost.

We then deduce the fitted value of the overall cost according to:

$$\widehat{tc}_t^{pure} = \widehat{\tau}_t^{pure,adv} + \widehat{t}_t^{pure}$$

Last, we transform this (fitted) measure of total transport cost in an index with base

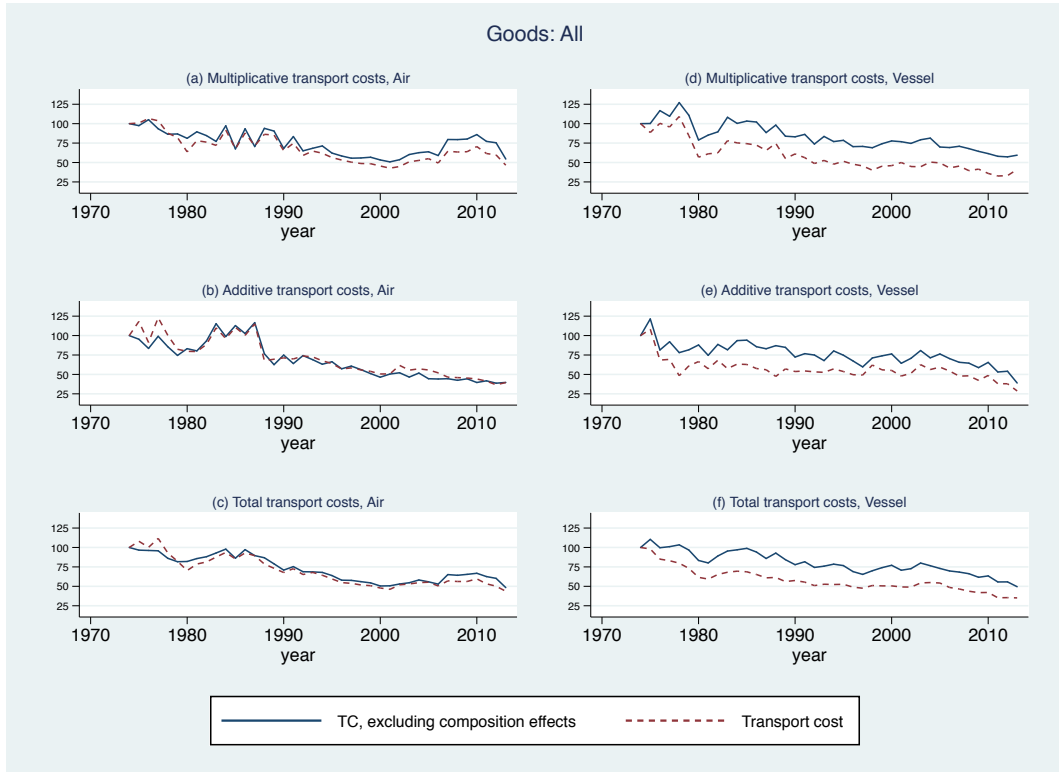
year 1974, applying a similar formula as above (by transport mode):

$$\Gamma_t^{tc} = 100 \frac{\hat{tc}_t^{pure} - 1}{\hat{tc}_{1974}^{pure} - 1}$$

3.3 Characterizing the time trends in transport costs

Figure 4 reports the results for all types of goods.³¹ In panels (a), (b) and (c) we report the time changes of the ad-valorem costs, the additive costs and the total costs respectively, for air transport (starting from the reference value 100 in 1974). Panels (d), (e) and (f) report the results for vessel. In each panel, we report the evolution of transport costs for both the unfitted (plain blue line) and the fitted (dotted red line) measures.

Figure 4: Transport costs (with and without composition effects)



Three main results emerge from Figure 4. First, in accordance with Figure 2, we find that international transport costs have substantially decreased over the period, for both transport modes (Panels (c) and (f)). International transport costs were reduced by 50% between 1974 and 2013 in air shipping, and by 60% in maritime shipping. This stands in line with the related literature (see Hummels, 1999; Lafourcade & Thisse, 2011). Second, the magnitude of the decrease is roughly of the same order for both for the ad-valorem and the additive components (Panels (a), (b), (d) and (e)). Further, the transport cost reduction is much smoother in maritime transport, while air transport shows more volatility in the trend pattern, in particular in the 1980s and the 2000s. Third, and most

³¹In the Online Appendix, we report the results at a more disaggregated level, distinguishing between primary and manufacturing goods.

importantly, we find that composition effects do not play a major role in accounting for the time trend of overall transport costs. Inspecting the panels of Figure 4 for air transport (panels (a) to (c)), we do not find much evidence of a substantial trend difference between the unfitted transport costs measure and the pure transport costs. For all three series (additive, ad-valorem and overall transport costs), the dotted and the plain line follow closely, almost every year throughout the period. Air transport costs were reduced by 50% between 1974 and 2013, which is mainly attributable to a reduction in the transport costs “per se”. Composition effects are stronger in vessel transport, for all three series (Figure 4, panels (d) to (f)): they amplify the reduction in “pure” transport costs at the beginning of the period, in the 1970s (the dotted line is below the plain line, and the gap is increasing). Afterwards, the dotted line remains below the plain line, but the gap between the two remains roughly constant across years, indicating that the amplification effect does not strengthen anymore: the two trends are similar. Considering the raw series (plain line), maritime transport costs have decreased by 60% over the period, which can be decomposed into a 50% decrease in transport costs “per se” (dotted line), and a 10% reduction that comes from composition effects (the difference of the two). This is particularly the case for the multiplicative component (panel (d)).

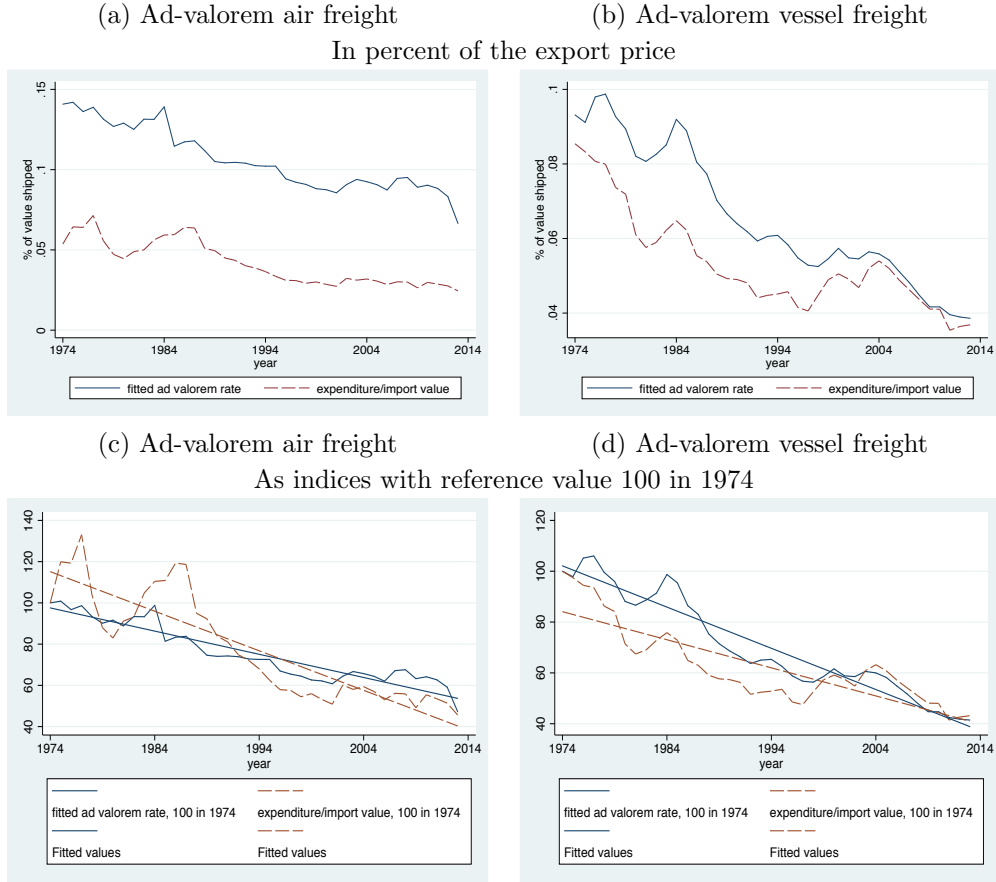
3.4 Time trends in transport costs and the modeling of the additive component

The last results stand in sharp contrast with Hummels (2007), who finds that trade composition effects do matter, as they partially offset the reduction in the pure transport costs for both air and maritime shipping. If anything, we find the opposite result here: Trade composition effects do not matter much in accounting for the downward trend of observed international transport costs, and when they do, they tend to amplify (rather than reduce) the downward pattern. This drives us to investigate this difference further. As we explain in more detail in Appendix D, our empirical strategy differs from Hummels (2007) in one main dimension. Our characterization of the time trends in transport costs starts from our estimates of both the additive and the ad-valorem components (obtained in Section 2.3), as well as for the overall transport cost (rather than the actual cif-fas price gap). Consequently, our methodology lets the ratio between the additive and the ad-valorem components of transport costs vary over the three time-product-partner country dimensions. This turns out to be of primary importance in the disentangling, in the time trend of transport costs, of what comes from the trade composition effects and what comes from changes in the pure transport cost dimension, as we show below.

To establish this point clearly, we replicate the method adopted by Hummels (2007) exposed above on our database (which is the same as his until 2004). The results are reported in Figure 5. The dotted line labeled “expenditure/import value” represents the unfitted measure of transport costs (TC_t in the above terminology) and the plain line labeled “fitted ad-valorem rate” is the measure of “pure” transport costs, i.e. composition effects excluded (\widehat{TC}_t). In Panels (a) (for air) and (b) (for vessel), we report the transport costs measures (fitted and unfitted) expressed as a percentage of the export price, as in

Hummels (2007).³² To ease the interpretation of the trends, we express them as indices with the reference value 100 in 1974, in Panels (c) and (d) for air and vessel respectively.

Figure 5: Characterizing the time trends: applying Hummel’s (2007) method



These results stand in sharp contrast with the ones obtained with our methodology and reported in Figure 4. Applying Hummels (2007) method, we find that the composition effects tend to partly offset the decrease in transport costs in both air and vessel shipping, as the downward trend is of higher magnitude for the fitted rate (plain line) than the unfitted rate (dotted line), especially for vessel (Panel (d)). Yet, this result is overturned when we allow for more flexibility in the role of the additive component, as indicated in Figure 4, Panels (c) and (f).

Assuming a varying share of the additive component over time, product and country partner indeed modifies the decomposition of the trend reduction of transport costs between the one attributable to trade composition effects and the reduction in the “pure” transport costs. In both air and vessel transports, we thus find that this last dimension is the main driver of the reduction in international transport costs observed over time, in particular in air transport. Complementing the findings of Section 2.3, these results highlight the importance of integrating the additive dimension of international transport costs, with the aim here of characterizing their time trends.

³²Unsurprisingly, this accords with Hummels (2007) results, see his Figures 5 (for air) and 6 (for vessel).

4 Robustness analysis

4.1 Robustness to the separability assumption

In this section, we provide a robustness analysis to the separability assumption of country-good fixed effects, which considers (following Irarrazabal et al., 2015) that both the ad-valorem and the additive costs are separable between the origin country (i) and the product ($s(k)$) dimensions. That is, we relax Equations (7) and (8) to model $t_{is(k)}$ and $t_{is(k)}$ (on a yearly/transport mode basis). Yet, this comes at the cost of having to estimate a much larger number of fixed effects (for approx. 200 countries of origin and 200 sectors at the 3-digit level, this means estimating 40,000 versus 400 fixed effects, per year and per transport mode), making the estimation (all the more given our non-linear setting) intractable in practice. This drives us to conduct the analysis on a sub-sample of trade flows, upon which two estimations are conducted (for every year and each transport mode): with the separability assumption (Equations (7) and (8) hold, our baseline case) and without. For each year and transport mode, we select the countries (i) and the products (at the 3-digit level, $s(k)$) that constitute 80% of the total value of trade flows. Table 2 shows a summary of the results, considering the average estimated values over the period (by transport mode).

Table 2: Robustness to the separability assumption (average over the period) - restricted sample

Mean value over 1974-2013				
3 digits				
Mode	Air		Vessel	
Separability	No	Yes (baseline)	No	Yes (baseline)
<i>Additive term</i> (\hat{t}/\hat{p} , in %)				
Mean	1.76	1.96	2.61	2.99
Median	0.65	0.84	1.83	2.23
<i>Ad-valorem term</i> ($\hat{\tau}$, in %)				
Mean	1.04	0.94	2.43	2.40
Median	0.56	0.83	2.06	2.04
<i>Share of additive costs in total costs</i> (in %)				
Mean	62.8	67.5	51.8	55.4
Median	54.1	50.5	47.0	52.2
<i>Diagnostic test</i>				
AIC criteria	4657.60	4654.23	10744.83	10690.80
# observations	2381	2381	2798	2798
# origin country	13.4	13.4	19.8	19.8
# products	25.5	25.5	53	53

Notes: Estimations are performed on a restricted sample, based on the following rule: for each year and transport mode, we select the countries (i) and the products (at the 3-digit level, $s(k)$) that constitute 80% of the total value of trade flows. The additive term is expressed in fraction of fas price. 1989 omitted in 3-digit estimation for air.

Three main comments can be made. First, the subset of large trade flows we are considering (around 8% of the observations of our initial sample, but 80% of the total

value of aggregated trade) involve a higher share of additive costs: between 52% and 67% of total costs on average, versus 40% to 50% on the whole sample. Second, both models provide a similar quality of fit of the regression (once we take into account the number of right-hand-side variables) as the AIC criteria display very close values in both models (conditional on transport mode). Third, the estimated values remain of similar magnitude under both separability and non-separability assumptions, even if one can note that under the separability assumption, the share of additive costs seems slightly biased upward, at least for averages over the period. The picture is reversed for medians.

Before jumping to the conclusion that our results are robust to the separability assumption, however we investigate this comparison deeper on a year-to-year basis, as shown in Figure 6. Specifically, Figure 6 displays the results for air transport in panel (a) and for maritime transport in panel (b). In each case, the estimated values (as well as the fitted regression line) under both separability (baseline) and non-separability are reported, for the additive term (upper panel) and the ad-valorem term (lower panel).

Figure 6: Robustness to the separability assumption (year-to-year basis)



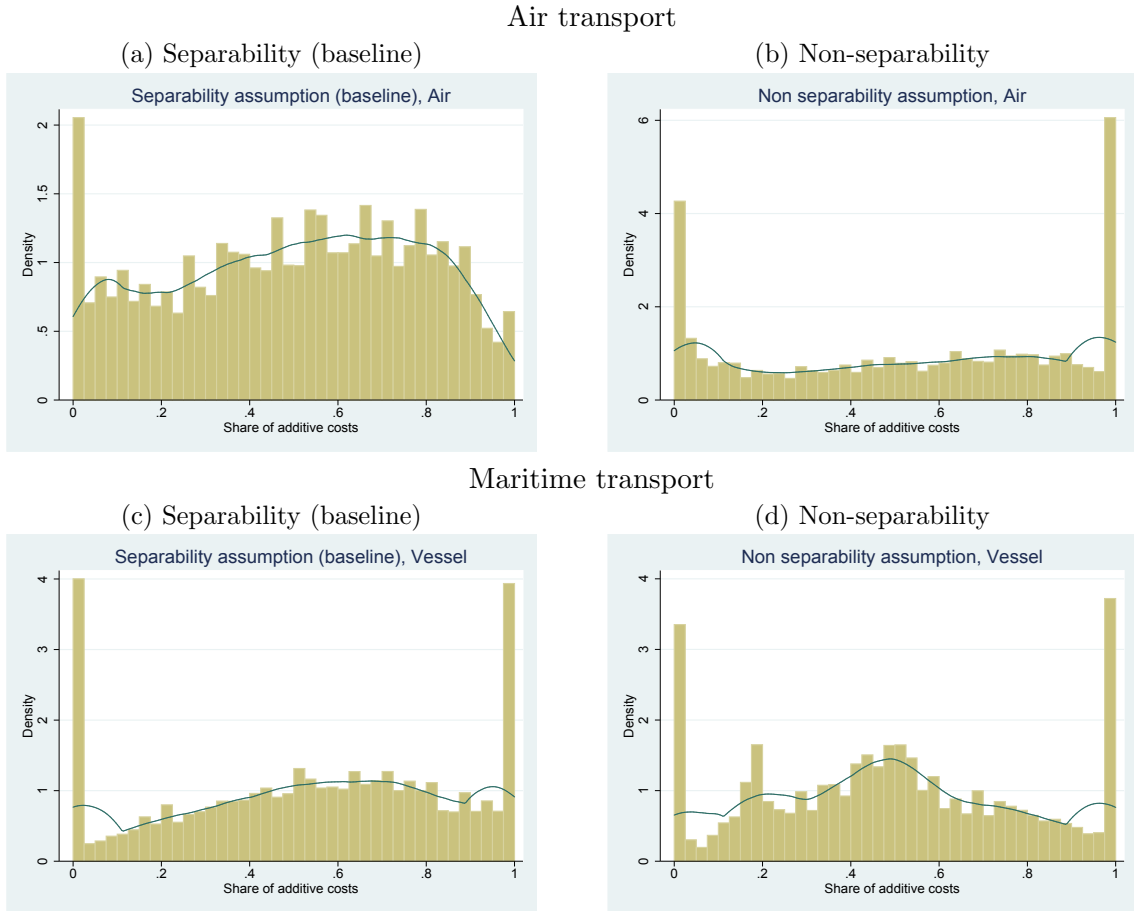
Notes: FE for (country, sector) fixed effects.

In line with Table 2, the results shown in Figure 6 confirm that the separability assumption (retained in our baseline estimation) tends to overestimate the value of the additive cost component (and underestimate the value of the ad-valorem cost). However, they also show that the difference is quantitatively small. Further, and most importantly, whatever the transport mode and for both types of transport costs, the trend patterns

of international transport costs, whether estimated under the separability assumption or not, are very similar. Along with the quality-of-fit diagnosis, this confirms the robustness of our estimation results to this assumption.

As an ultimate check, we investigate whether the varying pattern over time/country of origin/product pointed out in Section 2.3 is also robust to the separability assumption. With this aim, we replicate Figure 3 on the reduced sample for both specifications of separable (baseline) and non-separable fixed costs. Figure 7 shows the histogram of the distribution of the elasticity of transport costs to the export price (β_{ikt} , for air transport (top panel) and for maritime transport (bottom panel) under the baseline specification (Panels (a), (c))) and the non-separability scenario (Panels (b), (c)).

Figure 7: Histogram of the share of additive costs in total costs (restricted sample)



Notes: Distribution of β_{ikt} over the triplet (year-product-country), weighted by share of yearly value of flow.

Similarly, as for the whole sample (Figure 3), for both transport modes the distribution of β_{ikt} over the triplet (year, country of origin, product) appears smoothly distributed over the interval $[0, 1]$, whatever the assumption regarding the specification of fixed effects. Relaxing the assumption that fixed effects are separable between the two country and product dimensions does not alter qualitatively our conclusion, that the elasticity of transport costs to the export price (or the share of additive costs in total transport costs), is strongly varying over time, countries of origin and products. As a consequence, this also

provides an indirect robustness check to the results regarding the trend decomposition provided in Section 3, which establish that the decline of “pure” transport costs is a main reason for the decrease of overall transport costs observed over time.

4.2 Robustness to the weighting scheme

As discussed in Appendix D, one source of difference between our methodology and that of Hummels (2007) concerns the weighting scheme used to obtain the evolution of the pure transport costs over time. In this section, we provide a robustness test to this difference of treatment.

When aggregating the trade cost measure over the product/country (i, k) dimension, Hummels (2007) takes the unweighted average value over the i, k dimension, which implicitly attributes a weight equal to 1 to each flow. Our benchmark specification (at the root of Figure 4) proceeds differently, as each flow is weighted by its relative value in total trade flows observed in 1974. In this section, we check whether this difference of treatment is responsible or not for the difference in results relative to the role of the trade composition effects, which we rather attribute to the modeling of the additive component.

To this aim, we rebuild the fitted values for each of our transport cost measures (ad-valorem, additive and overall) applying the Hummels (2007) weighting scheme (i.e. taking the unweighed average value over the i, k dimension), which we then express as indices, with the reference value 100 in 1974. The results are reported in Figure 8.

Figure 8: Transport cost time trends: robustness to the weighting scheme



The comparison of Figure 8 (applying Hummels, 2007’s weighting scheme) and Figure 4 (applying our weighting scheme) prompts two comments. First, differences do show up, in particular for the multiplicative component of air transport. This suggests that the weighting scheme is not innocuous in the time trend decomposition exercise. However, Figure 8 also shows that the composition effects have contributed to strengthen the

decrease in the “ceteris paribus” transport costs in air transport (in Figure 8, panel (a), overall transport costs have decreased more than the fitted component), in accordance with the conclusions drawn from Figure 4, rather than partly offsetting this decline, as argued by Hummels (2007). This confirms that it is the functional form and precisely the modeling of the additive component, rather than the weighting scheme, that is key in understanding the underlying determinants of the overall transport costs time trends, as pointed out in Section 3.

4.3 Endogeneity concerns

One may be concerned that the specification of Equations (10) or (11) might be subject to an endogeneity bias, as the price set by the exporter may vary depending on the transport cost burden. Studies on the pricing-to-market behavior of firms (see Krugman, 1987) show that we cannot exclude that the export price set by the firm (\tilde{p}_{ik}) is partly endogenous to the size of transport costs (for instance, the exporting firm absorbing (part of) the transport costs by reducing the *fas* price). Besides, related concerns may arise from productivity-sorting model in Melitz (2003) or the quality-sorting model in Baldwin & Harrigan (2011): more productive firms and/or firms selling high-quality products will charge higher prices, all other things equal – in our case, for a given country-product pair. In addition, there is also the possibility that bigger firms might impact transport costs, due to their ability of bargaining discounts for larger shipped volumes.

It is true we are not interested in causal inference, since our aim is to provide an accounting breakdown of transport costs between the additive and the multiplicative components. However, the latter can be biased by the aforementioned endogeneity issues since they imply that $\frac{1}{\tilde{p}_{ik}}$ is correlated in one direction on another with residuals ϵ_{ik} . This may ultimately harm the estimation of \hat{t}/\tilde{p} and consequently, $\hat{\tau}$.

Therefore, we propose to compare our main estimates with those stemming from a two-stage least-squares procedure. Put differently, we follow earlier literature (see e.g. Caliendo & Parro, 2015 or Lashkaripour, 2017) by replacing in the right-hand side of Equation (10) \tilde{p} by predicted values stemming from a first-stage equation regressing \tilde{p} on custom duties coming based on tariffs at the product line, together with one-year lagged *fas* prices. Section B.4 in Appendix B provides a full presentation of the theoretical basis for the first-stage equation, as well as first-stage estimates. In particular, it shows that our main instrumental variable displays the right statistical properties, and that we can confidently re-inject the predictions arising from the first-stage equation for \tilde{p}_{ik} on the right-hand side of Equation (10)³³ to produce a 2SLS-type of estimation. Figure 9 below reports our benchmark estimates by transport mode, together with their instrumented counterpart. In all cases, these estimates are very similar, when not identical. This supports that our benchmark estimates do not suffer any substantial biases arising from endogeneity concerns.

³³Note that, since the predictions are expressed in logarithms, they are transformed through the exponential function before their implementation in Equation (10).

Figure 9: Transport cost time trends: robustness to the weighting scheme



5 The role of additive cost: Theoretical insights

Our estimation results drive two main conclusions: First, additive costs constitute a significant part of international transports costs, in both maritime and air transport. Second, the size of international transport costs has decreased since the mid-1970s, in particular in air transport. While the share of additive costs is relatively stable in maritime transport, it has substantially decreased in air transport. **METTRE DES CHIFFRES.**

The question we want to explore is about the implications of such results on theoretical grounds. While the whole bulk of the trade literature investigates the role of trade costs modelled as ad-valorem costs (e.g., iceberg trade costs), not much is said about the role of the additive components. One potential explanation is the lack of empirical estimates about the size of additive costs. Our results may thus usefully palliate this limitation. Specifically, we can make use of our empirical results to answer two questions: First, what does it change to introduce additive costs along with standard iceberg trade costs, in particular regarding the pattern of trade flows? Second, what are the welfare consequences of a reduction in international transport costs, when such a reduction also occurs through a reduction in the additive component? These two key questions (the pattern of trade and the welfare gains of trade liberalization) are overwhelmingly addressed considering ad-valorem trade costs only. Given our empirical results pointing out the importance of additive costs, we explore how additive costs modify the picture. **A MIEUX DIRE.**

5.1 The model

Two papers have explored the role of additive costs on theoretical grounds: Irarrazabal et al. (2015) and Sorensen (2014). As in Sorensen (2014), we investigate the role of additive costs in the trade model of Melitz (2003), considered in its canonical symmetric

two-country version. **discuter de pourquoi on ne retient pas Chaney. Faut-il citer Lashkaripour ici aussi?** This allows to highlight the specificities induced by additive versus the standard iceberg (ad-valorem) costs. In contrast to Sorensen (2014), we make use of our empirical results to quantify the effects of a reduction in international transports costs on both positive and normative dimensions. In accordance with the literature, we focus on steady-state analysis. Since our focus is on the role of additive versus ad-valorem transport costs, we directly present the two-country version of the model, with the two countries (Home and Foreign) being perfectly symmetric.

5.1.1 Households

In each country, the representative household exogenously supplies L units of labour and maximizes utility $\mathcal{U} = \left[\int_{\omega \in \Omega} c(\omega)^{\frac{\sigma-1}{\sigma}} d\omega \right]^{\frac{\sigma}{\sigma-1}}$, with $\sigma > 1$ the elasticity of substitution between varieties. She chooses her consumption $c(\omega)$ of each variety ω within the set Ω of available varieties (made of both domestic and foreign varieties, endogenously defined), subject to her budget constraint: $\int_{\omega \in \Omega} p(\omega)c(\omega)d\omega \leq E$, with $p(\omega)$ the consumer price of variety ω and E nominal expenditures. As standard, the optimal demand function for variety ω is:

$$c(\omega) = \left(\frac{p(\omega)}{P} \right)^{-\sigma} \frac{E}{P}$$

with the associated optimal price index P equal to:

$$P = \left[\int_{\omega \in \Omega} p(\omega)^{1-\sigma} d\omega \right]^{\frac{1}{1-\sigma}} \quad (17)$$

5.1.2 Firms behavior

As in Melitz (2003), firms are in monopolistic competition, each producing a differentiated variety using labor as sole production factor. Both countries being perfectly symmetric, the labor market equilibrium imposes the same wage in both countries, thus considered as the numéraire. Prices and costs are hence expressed in terms of labor. At entry, each firm pays a sunk entry cost f_e and subsequently draws its productivity level φ from a known distribution $G(\varphi)$. Production of q units, a firm should employ $l(q|\varphi) = f + \frac{q}{\varphi}$ units of labor, with f the fixed cost of production. Exporting is subject to an extra fixed cost f_x and variable exporting costs of two types: an ad-valorem cost that depend on the value traded $\tau \geq 1$ and an additive cost depending on the quantity (weight) transported, $t \geq 0$. **Mettre une footnote, unit vs weight.** At each point in time, a firm can be hit by a death shock at the exogenous probability $\delta > 0$. Following Melitz (2003), we solve the problem backwards. First, we solve for the maximizing profit behavior once entered. Second, we determine the entry conditions on the various markets.

Profit-maximizing behaviors Once entered, a firm adopts a pricing-to-market behavior (conditional on exporting) by setting a specific price on each destination market.

On the domestic market, the objective is to maximize profit $\pi_d(\omega)$, taken into account the consumer demand function³⁴:

$$\begin{aligned} \max_{p(\varphi)} \pi_d(\varphi) &= \left(p^d(\varphi) - \frac{1}{\varphi} \right) c(\varphi) \\ \text{s.t.} \quad c(\varphi) &= \left(\frac{p(\varphi)}{P} \right)^{-\sigma} \frac{E}{P} \end{aligned}$$

The optimal pricing behavior yields:

$$p^d(\varphi) = \frac{\sigma}{\sigma - 1} \frac{1}{\varphi}$$

With a CES specification on household's preferences, the firm sets its price as a constant mark-up on marginal cost, which is inversely related to its productivity as for the domestic market.

Conditional on exporting abroad, the profit-maximizing program on the foreign market requires the inclusion of variable international trade costs according to:

$$\begin{aligned} \max_{p^x(\varphi)} \pi_x(\varphi) &= \left(p^x(\varphi) - \frac{\tau}{\varphi} \right) c^x(\varphi) - t c^x(\varphi) \\ \text{s.t.} \quad c^x(\varphi) &= \left(\frac{p^x(\varphi)}{P^*} \right)^{-\sigma} \frac{E^*}{P^*} \end{aligned}$$

where E^* and P^* refer to nominal expenditures and the price index in the foreign country, $c^x(\omega)$ to the demand for variety ω from the Foreign household and $p^x(\omega)$ to the price set by the firm producing the variety ω on the export market. Solving for this yields:

$$p^x(\varphi) = \frac{\sigma}{\sigma - 1} \left[\frac{\tau}{\varphi} + t \right]$$

Similarly as for the Home market, the firm sets a constant markup on its marginal cost, which is still a decreasing function of the firm's productivity φ , but also takes into account both components of trade costs.

Under the assumption of symmetric countries (i.e, implying $E = E^*$ and $P = P^*$), one can deduce the profits on the domestic and export markets ($\pi_d(\varphi)$ and $\pi_x(\varphi)$) respectively

³⁴In a monopolistic set-up, each firm (of productivity φ) is the sole producer of variety ω , implying a one-to-one link between ω and φ , such that we could write $\omega(\varphi)$. For sake of notational simplicity, we omit this link and simply write the consumer demand function as a function of φ directly.

as:

$$\pi_d(\varphi) = \frac{r_d(\varphi)}{\sigma} - f = B\varphi^{\sigma-1} - f \quad (18)$$

$$\pi_x(\varphi) = \frac{r_x(\varphi)}{\sigma} - f_x = B \left[\frac{\tau}{\varphi} + t \right]^{-(\sigma-1)} - f_x \quad (19)$$

$$\text{with } B \equiv \frac{1}{\sigma-1} \left(\frac{\sigma}{\sigma-1} \right)^{-\sigma} P^{\sigma-1} E$$

where $r_d(\varphi)$ and $r_x(\varphi)$ denote the sales revenues on each market. Profits increase with productivity φ , and only sufficiently productive firms are able to cover the fixed costs of operating in a given market. Further, in presence of trade costs, a given firm of productivity φ makes a lower export profit than on its domestic market, conditional on being productive enough to export. This drives us to determine the productivity threshold associated to the entry conditions.

Making use of the firm's first-order pricing conditions, revenues on each local and export market respectively read as:

$$r_d(\varphi) = \left[\frac{1}{\rho} \frac{1}{\varphi} \right]^{1-\sigma} P^{\sigma-1} E \quad (20)$$

$$r_x(\varphi) = \left[\frac{1}{\rho} \left(\frac{\tau}{\varphi} + t \right) \right]^{1-\sigma} P^{\sigma-1} E \quad (21)$$

with $\rho = \frac{\sigma-1}{\sigma}$ inversely related to the markup.

Zero-cutoff profit conditions Given the fixed costs on both the domestic and the export markets, only firms with a productivity above φ^* will serve the domestic market, and those with $\varphi > \varphi_x^*$ will export abroad. The zero cut-off (ZCP) productivity level for successful entry on the domestic and export markets should verify:

$$\begin{aligned} \frac{\pi_d(\varphi^*)}{\delta} = 0 &\Leftrightarrow \frac{r_d(\varphi^*)}{\sigma} - f = 0 \\ \frac{\pi_x(\varphi_x^*)}{\delta} = 0 &\Leftrightarrow \frac{r_x(\varphi_x^*)}{\sigma} - f_x = 0 \end{aligned}$$

with $\frac{\pi_d(\varphi^*)}{\delta}$ the expected profit on each market. Manipulating equations, we get:

$$\begin{aligned} \varphi_x^* &= \frac{\tau}{f_x^{\frac{1}{1-\sigma}} B^{\frac{-1}{1-\sigma}} - t} \\ \varphi^* &= \frac{1}{f^{\frac{1}{1-\sigma}} B^{\frac{-1}{1-\sigma}}} \end{aligned}$$

The two productivity thresholds are accordingly linked according to:

$$\frac{\varphi_x^*}{\tau + t\varphi_x^*} = \varphi^* \left(\frac{f}{f_x} \right)^{\frac{1}{1-\sigma}} \quad (22)$$

Following Melitz (2003) and the subsequent literature, we ensure selection on the export market, i.e. such that $\varphi_x^* > \varphi^*$. Making use of Equation (22), this condition writes down as:

$$\tau + t\phi_x^* \left(\frac{f}{f_x} \right)^{\frac{1}{1-\sigma}} > 1$$

Notice that, due to additive costs ($t > 0$), this condition depends on the general equilibrium of the model (through ϕ_x^*) and cannot be imposed ex-ante by an appropriate restriction on the space parameter. We check this condition holds numerically in solving the model. **A FAIRE ??? JE CROYAIS LE FAIRE MAIS JE NE LE FAIS QUE DANS LE CAS SANS ADDITIFS.**

5.1.3 Aggregation, firm entry and exit

Aggregation The general equilibrium is characterized by a mass M of producing firms in each country associated with a distribution $\mu(\varphi)$ of productivity levels of a subset of $(0, \infty)$. Given the productivity threshold ϕ^* , $\mu(\varphi)$ is equal to the conditional distribution of $g(\varphi)$ on the subset $[\phi^*, \infty)$:

$$\mu(\varphi) = \begin{cases} \frac{g(\varphi)}{1-G(\varphi^*)}, & \text{if } \varphi \geq \varphi^* \\ 0 & \text{otherwise} \end{cases} \quad (23)$$

with $1 - G(\varphi^*)$ the probability of successful entry on the domestic market. Conditional on being active on the domestic market, a subset mass M_x of firms export abroad. $\mu_x(\varphi)$ can be similarly defined as the conditional distribution of productivity on the export market, e.g. on the support $[\varphi_x^*, \infty)$.

Following Melitz (2003), and decomposing the set of available varieties into Ω_d , Ω_x the set of varieties respectively produced at Home and imported, one can rewrite the price index (17) as:

$$\begin{aligned} P &= \left[\int_{\omega \in \Omega_d} p_d^{1-\sigma}(\omega) d\omega + \int_{\omega \in \Omega_x} p_x^{1-\sigma}(\omega) d\omega \right]^{\frac{1}{1-\sigma}} \\ &= \left[\int_0^\infty p_d^{1-\sigma}(\varphi) M \mu(\varphi) d\varphi + \int_0^\infty p_x^{1-\sigma}(\varphi) M_x \mu_x(\varphi) d\varphi \right]^{\frac{1}{1-\sigma}} \end{aligned}$$

Making use of Equation (23), the price index reads as:

$$P = \left[\frac{M}{1-G(\varphi^*)} \int_{\phi^*}^\infty p_d^{1-\sigma}(\varphi) g(\varphi) d\varphi + \frac{M_x}{1-G(\varphi_x^*)} \int_{\varphi_x^*}^\infty p_x^{1-\sigma}(\varphi) g(\varphi) d\varphi \right]^{\frac{1}{1-\sigma}}$$

with $\begin{cases} p_d(\varphi) &= \frac{\sigma}{\sigma-1} \frac{1}{\varphi} \\ p_x(\varphi) &= \frac{\sigma}{\sigma-1} \left[\frac{\tau}{\varphi} + t \right] \end{cases}$

Accordingly, the price index can be rewritten as:

$$P = \left(\frac{\sigma}{\sigma - 1} \right) \left[\frac{M}{1 - G(\varphi^*)} \int_{\varphi^*}^{\infty} \phi^{\sigma-1} g(\varphi) d\varphi + \frac{M_x}{1 - G(\varphi_x^*)} \int_{\varphi_x^*}^{\infty} \left[\varphi \left(\frac{\tau}{\tau + t\varphi} \right) \right]^{\sigma-1} g(\varphi) d\varphi \right]^{\frac{1}{1-\sigma}}$$

Similarly as in the closed-economy case (Melitz (2003)), let us define $\tilde{\varphi}(\varphi^*)$ and $\tilde{\varphi}_x(\varphi_x^*)$ as the weighted average of productivities of the domestic firms, on the domestic market and the export market respectively:³⁵

$$\tilde{\varphi} = \left[\frac{1}{1 - G(\varphi^*)} \int_{\varphi^*}^{\infty} \phi^{\sigma-1} g(\varphi) d\varphi \right]^{\frac{1}{\sigma-1}} \quad (24)$$

$$\tilde{\varphi}_x = \left[\frac{1}{1 - G(\varphi_x^*)} \int_{\varphi_x^*}^{\infty} \left[\varphi \left(\frac{\tau}{\tau + t\varphi} \right) \right]^{\sigma-1} g(\varphi) d\varphi \right]^{\frac{1}{\sigma-1}} \quad (25)$$

Further defining $M_T = M + M_x$ as the total number of varieties accessible to the consumers, it comes that:

$$P = \frac{\sigma}{\sigma - 1} M_T^{\frac{1}{1-\sigma}} \left[\frac{1}{M_T} \left(M \tilde{\varphi}^{\sigma-1} + M_x \left(\frac{\tilde{\varphi}_x}{\tau} \right)^{\sigma-1} \right) \right]^{\frac{1}{1-\sigma}}$$

With $\tilde{\varphi}_T \equiv \left[\frac{1}{M_T} \left(M \tilde{\varphi}^{\sigma-1} + M_x \left(\frac{\tilde{\varphi}_x}{\tau} \right)^{\sigma-1} \right) \right]^{\frac{1}{1-\sigma}}$ the weighted average of firm productivities on the domestic market (including both local producers and foreign producers exporting at Home), the price index can be expressed as:

$$P = M_T^{\frac{1}{1-\sigma}} \frac{1}{\rho \tilde{\varphi}_T} \quad (26)$$

Free-entry condition There is free-entry in the monopolistic industry, imposing that the expected net present value of entry is driven to 0. In the open-economy setting, this condition is given by:

$$\sum_{t=0}^{\infty} (1 - \delta)^t \left(\int_{\varphi^*}^{\infty} \pi_d(\varphi) dG(\varphi) + \int_{\varphi_x^*}^{\infty} \pi_x(\varphi) dG(\varphi) \right) = f_e$$

Defining $\bar{\pi}$ as the average profit conditional to entry, this free-entry condition rewrites as:

$$(1 - G(\varphi^*)) \frac{\bar{\pi}}{\delta} = f_e \quad (27)$$

with $(1 - G(\varphi^*))$ the probability of successful entry. In the open-economy setting, $\bar{\pi}$ can be expressed as:

$$\bar{p}i = \pi_d(\tilde{\varphi}(\varphi^*)) + \rho_x \pi_x(\tilde{\varphi}_x(\varphi_x^*))$$

³⁵In the symmetric two-country model, $\tilde{\varphi}_x(\varphi_x^*)$ also corresponds to the weighted average of productivities of foreign exporters at Home, e.g. associated with the imported varieties.

with $\pi_d(\tilde{\varphi}(\varphi^*)) \equiv \bar{p}_d$ the average expected profit on the domestic market, $\pi_x(\tilde{\varphi}_x(\varphi_x^*)) \equiv \bar{p}_x$ the average expected export profit and ρ_x the probability of exporting (conditional on entry on the domestic market), equal to:

$$\rho_x = \frac{1 - G(\varphi_x^*)}{1 - G(\varphi^*)}$$

Noticing that, from Equation (20), $\frac{r_d(\varphi)}{r_d(\varphi^*)} = \left(\frac{\varphi}{\varphi^*}\right)^{\sigma-1}$ and similarly on the export market, Equations (18) and (19) can be rewritten as:

$$\begin{aligned}\bar{\pi}_d &= \left\{ \left(\frac{\tilde{\varphi}^*}{\varphi^*} \right)^{\sigma-1} - 1 \right\} f \\ \bar{\pi}_x &= \left\{ \left[\left(\frac{\tilde{\varphi}_x^*}{\varphi_x^*} \right) \left(\frac{\tau + t\varphi_x^*}{\tau + t\tilde{\varphi}_x^*} \right) \right]^{\sigma-1} - 1 \right\} f_x\end{aligned}$$

Making use of the above elements, we finally get the zero-cut off profit condition in the open economy with additive costs as:

$$\bar{\pi} = \left\{ \left(\frac{\tilde{\varphi}^*}{\varphi^*} \right)^{\sigma-1} - 1 \right\} f + \frac{1 - G(\varphi_x^*)}{1 - G(\varphi^*)} \left\{ \left[\left(\frac{\tilde{\varphi}_x^*}{\varphi_x^*} \right) \left(\frac{\tau + t\varphi_x^*}{\tau + t\tilde{\varphi}_x^*} \right) \right]^{\sigma-1} - 1 \right\} f_x \quad (28)$$

with $\tilde{\varphi}^*$ and $\tilde{\varphi}_x^*$ given by Equations (24) and (25).

Summary Equations (24), (25), (28), (22) and (27) determine a system of interdependent equations in five endogenous variables $\{\bar{\pi}, \tilde{\varphi}, \tilde{\varphi}_x, \varphi^*, \varphi_x^*\}$. From this, we can deduce the equilibrium values of the remaining set of variables (as detailed in Appendix E). Specifically, we will study the consequences of additive costs in terms of welfare, which can be shown to be the inverse of the price level as standard in this literature (the price level P being given by Equation (26)).

5.2 Calibration

As standard in this literature (Irrazabal et al. (2015), Melitz fial proofs), the heterogeneity in firm productivity is assumed to be given by a Pareto distribution. In contrast to the standard case with only ad-valorem costs, the model can no longer be solved analytically due to the presence of additive costs (see Appendix E). In this case, we rely on the model's simulations to determine the steady state. This drives us to calibrate the structural parameters of the model. To do so, we rely on values commonly retained in the literature except for the two additive and ad-valorem transport costs, as reported in Table 3.

f such that all firms produce in autarky (i.e., such that $\varphi^{*,a} = \varphi_{\min}$. f_x endogenously revealed such that the initial steady state (with 1974 values of transport costs) implies a share of exporting firms equal to 21%, based on ???, following so the calibration method of Ghironi & Melitz (2005) or Irrazabal et al. (2015).

The calibration of transport costs parameters relies on our empirical estimates. We

Table 3: Calibration (1)

	Value	Reference
σ	4	Irrarrazabal et al. (2015)
f_e	1	Ghironi & Melitz (2005)
f	0.033	Ghironi & Melitz (2005)
f_x	0.09	Share of exporters = 21% (Ghironi & Melitz (2005), Irrarrazabal et al. (2015))
L	1	Arbitrary
δ	0.1	Ghironi & Melitz (2005), Irrarrazabal et al. (2015)
k	4	
φ_{\min}	1	Ghironi & Melitz (2005), Irrarrazabal et al. (2015)

notably illustrate the consequences of trade liberalization by comparing the equilibrium based on the 1974 values of transport costs (at the beginning of our sample), versus those of 2019 (at the very end of our estimation period), in both cases on only ad-valorem transport costs and in the presence of both additive and ad-valorem costs. Calibration of transport costs is displayed in Table 4.

Table 4: Calibration (2)

	Air transport				Maritime transport			
	1974		1974					
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Total TC (% of fas price)	6.2	6.2	2.8	2.8	10.5	10.5	4.1	4.1
τ (in %)	6.2	3.6	2.8	2.2	10.5	5.4	4.1	2.3
t/\tilde{p}_x (in %)	0	2.6	0	0.6	0	5.1	0	1.8

Notes: TC = Transport Costs. In columns (1), (3), (5) and (7) only ad-valorem costs are considered. In Columns (2), (4), (6) and (8), we model both ad-valorem and additive costs. t is calibrated so that the ratio t/\tilde{p}_x from the model matches its empirical target, with $\widetilde{widetilde{dep}}_x^{\text{fas}}$ the average fas price set in place by those domestic firms that export. We theoretically define the export fas price through:
 $p_x = \tau p^{\text{fas}} + t$

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5.3 Trade liberalization: The importance of additive costs

Our empirical results point to two important conclusions: First, additive costs represent a non-negligible part of overall international transport costs. Second, total transport costs are strongly reduced over 1974-2019, and the decrease is particularly marked in the additive component in air transport. We exploit the theoretical implications of these empirical findings in two different ways.

First, we run a comparative statics analysis following a reduction in transport costs based on our estimates in 1974 and 2019, by transport mode. Specifically, we contrast two cases: In the first scenario, the reduction in total transport costs is solely attributable to the ad-valorem component (e.g., contrasting Table 4, Column (3) to (1) for air transport, and Column (7) to (5) for maritime transport); in the second scenario, we rely of the true estimates of transport costs, with the reduction of total transport costs coming from both

additive and ad-valorem components. In this scenario, we contrast Table 4, Column (4) to (2) (Air) and Column (8) to (6) (Vessel). Importantly, we run this comparative statics analysis *ceteris paribus*, notably with the same value of the export fixed cost f_x as in the initial equilibrium (see Table 3).

Second, we take into account the fact that the share of exporting firms has substantially increased since the 21% value estimated by ??? in **YEAR YYY**. According to ???, this share roughly amounts to 35% in ???. This can be matched in the model by resetting the (lower) value of the export fixed cost f_x accordingly. In the second exercise, we thus run a comparative statics analysis where we contrast the 2014 steady states (e.g., with the 2019 transport costs values) with the two dimensions of trade liberalization: the reduction of transport costs (as in the first exercise) and the reduction of the export fixed cost, consistent with the increase in the share of exporters from 21% to 35%.

The results are reported in Table 5, for Air (Columns (1)-(4)) and Vessel (Columns (5)-(8)) respectively. Specifically, we report the change in total transport costs (expressed in percentage points, and based on the raw numbers reported in Table 4), decomposed in its two dimensions (additive and ad-valorem); as well as the welfare change, both in absolute and in relative terms. For each transport mode, the first two columns report the results of reducing transport costs only, maintaining the same value of f_x as in the initial equilibrium (Columns (1)-(2) for Air, (5)-(6) for Vessel), contrasting the case of only ad-valorem costs (Columns (1), (5)) and in presence of transport costs (Columns (2), (6)). In Columns (3)-(4) for Air and (7)-(8), we report the results when both the variable transport costs and the fixed export costs are lower in the final steady state (2019) relative to the initial one (1974).

Table 5: Trade liberalization: The role of additive costs

Mode	Air				Vessel			
Fixed export cost:	Constant f_x		Lower f_x		Constant f_x		Lower f_x	
Reduction in:	τ only	τ and t	τ only	τ and t	τ only	τ and t	τ only	τ and t
ΔTC (in pp)	-3.4	-3.4	-3.4	-3.4	-6.4	-6.4	-6.4	-6.4
$\Delta \tau$ (in pp)	-3.4	-1.4	-3.40	-1.40	-6.4	-3.1	-6.4	-3.1
$\Delta t/\bar{p}_x^{\text{fas}}$ (in pp)	0	-2.0	0	-2.0	0	-3.3	0	-3.3
$\Delta \mathcal{U}$	0.0202	0.0295	0.0362	0.0527	0.035	0.052	0.047	0.064
$\Delta \mathcal{U}/\mathcal{U}$ (in %)	1.2319	1.8187	2.2073	3.2477	2.179	3.295	2.872	4.052

Notes: TC = Transport Costs. The reduction in transport costs is expressed in percentage points.

5.3.1 Reducing international transport costs

In this first exercise, we contrast the effects of a reduction of international transport costs depending on whether this occurs through a reduction in ad-valorem costs only, or a combined reduction in both the additive and the multiplicative components. Accordingly, we focus on the results reported in Table 5, Column (1) versus (2) for Air, Column (5) versus (6) for Vessel.

A first conclusion emerges: Whatever the transport mode (and the magnitude of the

transport costs decrease accordingly), welfare gains are higher when this reduction is made (partly) through a reduction of additive costs. The effect is substantial: In Air transport, the reduction of 3.4 percentage points of transport costs generates a welfare gain higher by 0.58 percentage point when almost 60% of such a reduction occurs through the additive component, rather than when it realizes through a decrease of iceberg costs only. In maritime transport, where the decrease in total transport costs is larger (by 6.4 percentage points), the extra welfare gain amounts to 1.12 percentage points when 50% of the transport cost reduction occurs through the additive component.

6 Conclusion

This paper empirically studies the magnitude of additive costs in international transport costs, by exploiting the differences between the import and the export prices. Using SITC 3 and 4- digit cif-fas unit values taken from the US import database over 1974-2013, we estimate the two components (additive and ad-valorem) of transport costs, by transport mode (air or ocean). Two main findings emerge from our results. First, we provide a quantitative measure of both the additive and the ad-valorem transport costs. We find that additive costs are quantitatively sizable: They amount to 2.8% of the export price unit values for ocean shipping, and 1.8% for air transport. This is slightly lower than the estimated values for the ad-valorem costs, around 2.5% (vessel) and 3.2% (air) as mean values over 1974-2013. Further, modeling the additive component significantly improves the quality of fit of the regression. Second, we show the importance of integrating the additive component in accounting for the time trend of international transport costs. Allowing for a varying share of additive costs in the product/country/time dimension, we find that the decrease of international transport costs observed in the data is mostly attributable to a reduction in the *pure* transport costs, with trade pattern composition effects playing a small role. If anything, trade composition effects have contributed to amplifying the reduction in the pure transport costs in maritime transport. In both aspects, our results highlight the importance of the additive component in accounting for international transport costs.

Our results could be extended in two main ways. On the empirical side, one may want to go deeper into the structural determinants of (pure) transport costs - i.e. identify the respective roles of handling costs, insurance and freight at the root of the gap between export and import prices. On the theoretical side, our results can be used to explore the role of additive costs in shaping international trade flows in an international trade theory perspective and in affecting the international transmission of business cycles. This is left for further research.

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A Data Appendix

The Customs value is the value of imports as appraised by the U.S. Customs and Border Protection in accordance with the legal requirements of the Tariff Act of 1930, as amended. This value is generally defined as the price actually paid or payable for merchandise when sold for exportation to the United States, excluding U.S. import duties, freight, insurance, and other charges incurred in bringing the merchandise to the United States. The term “price actually paid or payable” means the total payment (whether direct or indirect, and exclusive of any costs, charges, or expenses incurred for transportation, insurance, and related services incident to the international shipment of the merchandise from the country of exportation to the place of importation in the United States) made, or to be made, for imported merchandise by the buyer to, or for the benefit, of the seller. In this respect, the “custom value” corresponds to the *fas* price (“free-alongside” price) delivered by the seller. More information is available at: http://www.census.gov/foreign-trade/reference/products/catalog/fl_imp.txt.

The import charges represent the aggregate cost of all freight, insurance, and other charges (excluding U.S. import duties) incurred in bringing the merchandise from alongside the carrier at the port of exportation in the country of exportation and placing it alongside the carrier at the first port of entry in the United States. In the case of overland shipments originating in Canada or Mexico, such costs include freight, insurance, and all other charges, costs and expenses incurred in bringing the merchandise from the point of origin (where the merchandise begins its journey to the United States in Canada or Mexico) to the first port of entry.

The *cif* (cost, insurance, and freight) value represents the landed value of the merchandise at the first port of arrival in the United States. It is computed by adding “Import Charges” to the “Customs Value” (see definitions above) and therefore excludes U.S. import duties.

B Estimation at the 3-digit classification level

B.1 Transport costs estimates: More detailed results

In this section, we report more detailed results for the estimates for international transport costs, by transport mode on a yearly basis, when either additive costs are included in the estimation (Equation (10)) or not (Equation (11)), under our benchmark sectoral classification level (3 digit). Specifically, we complement the results displayed in Table 1 by reporting the estimates of international transport costs for a sample of years over 1974-2013, when the degree of classification retained (s) is at the 3-digit classification level. Table B.1 reports the results for air transport. The results for vessel transport are displayed in Table B.2.

Table B.1: Air: Transport costs estimates, 3-digit level (selected years)

Year	1974	1980	1990	2000	2004	2010	2013
Model (a) - With only Ad-Valorem TC ($\hat{\tau}^{ice} - 1$, in %)							
Mean	6.9	5.4	5.0	3.6	4.0	4.2	3.4
Median	5.4	3.8	4.4	2.5	2.9	3.4	2.9
Model (b) - With Additive & Ad-Valorem TC							
<i>Ad-valorem term ($\hat{\tau}^{adv} - 1$, in %)</i>							
Mean	3.6	2.3	2.4	1.7	1.9	2.6	1.7
Median	2.7	1.6	1.6	1.2	1.4	2.2	1.7
<i>Additive term (\hat{t}/\tilde{p}, in %)</i>							
Mean	2.6	2.0	1.8	1.3	1.5	1.1	1.0
Median	1.1	0.5	0.8	0.5	0.6	0.4	0.5
# observations	14,955	16,118	24,958	35,027	36,990	40,279	39,351

Notes: TC = Transport Costs. Statistics are obtained weighting each observation by its share in trade (mode-dependent). Additive term expressed in fraction of fas price.

Table B.2: Vessel: Transport costs estimates, 3-digit level (selected years)

Year	1974	1980	1990	2000	2004	2010	2013
Model (a) - With only Ad-Valorem TC ($\hat{\tau}^{ice} - 1$, in %)							
Mean	9.8	6.5	5.7	5.1	5.4	4.0	3.6
Median	9.6	5.5	4.6	4.9	5.1	3.6	3.3
Model (b) - With Additive & Ad-Valorem TC							
<i>Ad-valorem term ($\hat{\tau}^{adv} - 1$, in %)</i>							
Mean	5.4	3.1	3.3	2.5	2.7	1.9	2.2
Median	4.9	2.4	2.8	2.1	2.8	1.8	1.8
<i>Additive term (\hat{t}^{add}/\tilde{p}, in %)</i>							
Mean	5.1	3.4	2.7	2.8	2.9	2.5	1.5
Median	2.9	2.3	1.7	2.2	1.9	1.9	0.8
# observations	19,007	17,356	28,383	36,090	37,757	37,748	38,473

Notes: TC = Transport Costs. Statistics are obtained weighting each observation by its share in trade (mode-dependent). Additive term expressed in fraction of fas price.

B.2 Assessing the importance of additive transport costs

In this section, we explore the performances of each type of model (with and without additive costs) in fitting the observed cif-fas prices gap, in order to deliver a more systematic diagnosis of the importance of additive costs. To do so, we rely on several standard measures of fit. The first indicator is through comparing R^2 . However, its use is far from being straightforward when evaluating non-linear estimates. R^2 is based on the underlying assumption that the adjusted model is a linear one. In a non-linear context, R^2 is strictly speaking inappropriate. However, if the error distribution is approximately normal, a standard metric like R^2 remains informative on the quality of adjustment. This leads us to complement the goodness-of-fit diagnosis with three alternative measures. We provide the Standard Error of Regression (SER), which represents the average distance that the observed values fall from the regression line. The smaller the SER value, the better the quality of fit, as it indicates that the observations are closer to the fitted line. We also report the log-likelihood function, and two measures derived, the Akaike Information Criterion (AIC) and the log-likelihood (LL) ratio test. A decrease in the log-likelihood function points to a better quality of fit. However, the likelihood function systematically decreases with the number of parameters included; the AIC criterion allows for correcting this overfitting by including a penalty in the computation of the statistic.³⁶ The preferred model is the one with the minimum AIC value. Finally, the log-likelihood ratio test statistic compares systematically the likelihood of the Unrestricted model (UR , including the additive term, i.e. Equation (10)) and the Restricted one (R , i.e. Equation (11)). The null tested is that the two models are statistically equivalent. Results are reported in Tables B.3 and B.4, for air and vessel respectively, at the 3-digit level.

Tables B.3 and B.4 lead to the same conclusion: The inclusion of the additive term leads to an improvement of the quality of fit, whatever the considered criterion or the transport mode. On average over the whole period, the R^2 doubles when per-kg costs are included for air, and increases by 50% for vessel. Similar qualitative conclusions arise from the comparisons of the standard errors of the regression (SER). Regarding the other criteria, improvements allowed by the inclusion of the additive term are roughly of the same extent across transport modes. Both AIC and log-likelihood statistics decrease with the inclusion of the additive term, and the log-likelihood test unambiguously rejects the null of statistical equivalence of the two models. These results holds whatever the considered year.

For comparison purposes, we provide a similar goodness-of-fit exercise at the 4-digit product level (4-digits), reported in Appendix C, Tables C.3 and C.4. If anything, the quality of fit appears slightly higher when estimations are based on the 4-digit classification. This is especially true for the model restricting transport cost to their ad-valorem dimension, whatever the transport mode considered. When the additive part is taken into account however, the difference in goodness of fit between the 3- and the 4-digit classification level becomes very small, whatever the considered criterion. In other words, if using a more

³⁶Specifically, the AIC stat is equal to $2 \times \text{number of parameters} - 2 \times \text{Likelihood}$, the number of parameters being given by the number of restrictions.

Table B.3: Air: Measures of Goodness-of-fit (3 digits)

Year	1974	1980	1990	2000	2010	2013	Mean stat
R^2							
Model (A)	0.30	0.27	0.25	0.32	0.42	0.34	0.31
Model (B)	0.59	0.65	0.63	0.64	0.51	0.46	0.60
SER							
Model (A)	0.79	0.86	0.81	0.84	0.86	0.92	0.85
Model (B)	0.67	0.71	0.67	0.70	0.79	0.85	0.73
AIC criteria							
Model (A)	35675.0	41171.0	60715.6	87492.6	102297.7	88191.9	70498.1
Model (B)	31387.3	35738.4	52098.9	74954.9	95887.1	80873.7	62285.0
Log-likelihood							
Model (A)	-17530.5	-20253.5	-29977.8	-43341.3	-50746.8	-43692.9	-34888.6
Model (B)	-15125.6	-17263.2	-25393.5	-36788.4	-47277.5	-39751.9	-30508.3
LL ratio	4809.7	5980.6	9168.7	13105.7	6938.6	7882.1	8760.69
Nb of restrictions	355	369	393	426	426	427	402
p-value	0.00	0.00	0.00	0.00	0.00	0.00	0.00

Notes: Model (A) = with only ad-valorem transport costs. Model (B) = with additive & ad-valorem transport costs. SER = Standard Error of regression; AIC = Akaike Information Criterion. R^2 between the log of predicted ratio and the log of the observed ratio. For the LL ratio test, the number of restrictions is equal to the number of parameters estimated, i.e. the number of partner countries plus the number of products. The mean statistics are calculated as the average value over all years.

Table B.4: Vessel: Measures of Goodness-of-fit (3 digits)

Year	1974	1980	1990	2000	2010	2013	Mean stat
R^2							
Model (A)	0.45	0.42	0.46	0.40	0.35	0.34	0.39
Model (B)	0.61	0.58	0.59	0.57	0.49	0.46	0.56
SER							
Model (A)	0.58	0.62	0.59	0.65	0.74	0.76	0.66
Model (B)	0.48	0.53	0.51	0.55	0.66	0.68	0.57
AIC criteria							
Model (A)	33328.8	33010.3	51142.6	71365.9	84789.9	88191.9	57848.6
Model (B)	27331.5	28067.3	43664.7	60475.9	76161.3	80873.7	49682.3
Log-likelihood							
Model (A)	-16287.4	-16129.1	-25169.3	-35263.9	-41998.9	-43692.9	-28534.3
Model (B)	-12985.8	-13353.7	-21171.4	-29491.0	-37418.7	-39751.9	-24151.3
LL ratio	6603.28	5550.96	7995.88	11545.98	9160.56	7882.15	8766.0
nb of restrictions	393	395	411	436	424	427	417
p-value	0.00	0.00	0.00	0.00	0.00	0.00	0.00

Notes: Model (A) = with only ad-valorem transport costs. Model (B) = with additive & ad-valorem transport costs. SER = Standard Error of regression; AIC = Akaike Information Criterion. R^2 between the log of predicted ratio and the log of the observed ratio. For the LL ratio test, the number of restrictions is equal to the number of parameters estimated, i.e. the number of partner countries plus the number of products. The mean statistics are calculated as the average value over all years.

disaggregated classification unsurprisingly adds some statistical precision, this is not to an extent that would disqualify the use of slightly more aggregated data. Further, the same conclusion established at the 3-digit level regarding the significant role of the additive component in fitting international transport costs emerges at the 4-digit level.

B.3 Variance decomposition exercise

In this section, we provide a variance decomposition exercise on the observed cif-fas price gap. Specifically, we determine the share of the observed variance in the ratio $\ln(\frac{p_{ik}}{p_{ik}} - 1)$ that comes from *i*) the between-product variance (at the 5-digit level, k) and *ii*) the between-sector variance (at the 3-digit level, s). The variance decomposition expression at the product level k (5-digit level) is obtained by applying the following formula (by year and transport mode):

$$\underbrace{\sum_{k=1}^K \sum_{i=1}^I (x_{ik} - \bar{x}_g)^2}_{\text{Total variability}} = \underbrace{\sum_k \sum_i (x_{ik} - \bar{x}_k)^2}_{\text{Within-product variability}} + \underbrace{\sum_k (\bar{x}_k - \bar{x}_g)^2}_{\text{Between-product variability}}$$

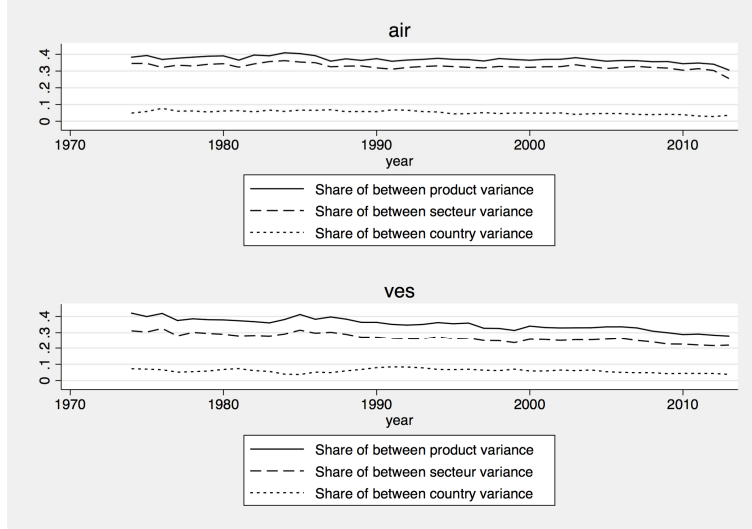
with x the observed cif-fas price gap and \bar{x}_g , \bar{x}_k average values defined as:

$$\bar{x}_g \equiv \frac{1}{n} \sum_{k=1}^K \sum_{i=1}^I x_{ik}, \quad \bar{x}_k \equiv \frac{1}{K} \sum_{k=1}^K x_{ik}$$

with n the total number of observations, K the total number of products and I the total number of country partners. We apply the same variance decomposition exercise at the sector level, in which case the sector s index (at the 3-digit level) replaces the k index (at the 5-digit level). This gives us an alternative way to ensure the robustness of the estimation results to the degree of classification retained to estimate international transport costs. We also determine the share of the observed variance that can be attributed to the between-country variance, adapting the variance decomposition formula written above accordingly. Results are reported in Figure B.1.

Two interesting results emerge from Figure B.1. First, the share of the cif-fas price gap variance that comes from the variance between products (5-digit level) is of the same magnitude of order as the variance between sectors at the 3-digit level. Both account for between 30 and 40% of the total variance in air transport, depending on the years considered. This is also the case for vessel transport, even if the difference between the between-product variance share and the between-sector share is more pronounced (30% for the between-sector vs 40% for the between-product variance at the beginning of the period). This provides an indirect robustness check to the degree of classification we have retained to estimate international transport costs. Second, the variance of the cif-fas price gap that can be attributed to the product (or sector) dimension is much larger than the between-country variance. This holds throughout the period and for both transport modes. This suggests that what primarily matters in international transport costs is

Figure B.1: Variance decomposition (observed cif-fas price gap)



mostly attributable to the product *per se*, rather than to the country where it comes from.

B.4 IV estimates: First stage

We report here the first-stage procedure and estimates underlying the IV estimates reported in section 2.3. We start by detailing the theoretical intuitions behind the first-stage equation. Afterwards, we report the estimates based on 5-digit-product-level data, before moving to the more disaggregate HS10 level for sensitivity checks.

First-stage equation. Our main instrumental variable for the fas price \tilde{p}_{ikt} is the share of tariff duties over the total value imported, at the product line. Tariffs may be considered as a (reasonably) exogenous source of variation for fas prices, i.e., uncorrelated with transport costs changes and mostly independent from firm- or sector-level dynamics. In this respect, considering the predicted part of the fas price related to tariff duties is likely to solve potential endogeneity biases. In other words, tariff shocks should eliminate from the fas price any endogenous component that might be related to transport costs. Note that this strategy has been regularly used in the related literature - see for example Caliendo & Parro (2015) or Lashkaripour (2017).

Denoting as usual i the origin country, k the product at the 5 digit level, we assume that the fas price \tilde{p}_{ik} decomposes in two components, say \bar{p}_{ik} the “firm-specific” price (related to its cost and pricing strategy) and τ_{ik}^d the tax duty (out of the firm’s hands) according to :

$$\tilde{p}_{ikt} = (1 + \tau_{is(k)t}^d)^\alpha (\bar{p}_{ikt})^\beta \quad (29)$$

with $s(k)$ the 3-digit classification as a function of the 5-digit product classification.

We first-differentiate this equation (between t and $t - 1$), with Δ the difference operator

($\Delta \tilde{p}_{ikt} = \tilde{p}_{ikt} - \tilde{p}_{ikt-1}$ and so on):

$$\begin{aligned} \Delta \tilde{p}_{ikt} &= \beta \bar{p}_{ikt-1}^{\beta-1} (1 + \tau_{is(k)t-1}^d) \Delta \bar{p}_{ikt} + \alpha \bar{p}_{ikt-1}^\beta (1 + \tau_{ikt-1}^d)^{\alpha-1} \Delta \tau_{is(k)t}^d \\ \Leftrightarrow \quad \frac{\Delta \tilde{p}_{ikt}}{\tilde{p}_{ikt-1}} &= \beta \frac{\Delta \bar{p}_{ikt}}{\bar{p}_{ikt-1}} \frac{(1 + \tau_{is(k)t-1}^d)^\alpha \bar{p}_{ikt-1}^\beta}{\bar{p}_{ikt-1}^\beta (1 + \tau_{is(k)t-1}^d)^\alpha} + \alpha \frac{\Delta \tau_{is(k)t-1}^d}{1 + \tau_{is(k)t-1}^d} \frac{(1 + \tau_{is(k)t-1}^d)^\alpha \bar{p}_{ikt-1}^\beta}{\bar{p}_{ikt-1}^\beta (1 + \tau_{is(k)t-1}^d)^\alpha} \end{aligned}$$

leading to:

$$\frac{\Delta \tilde{p}_{ikt}}{\tilde{p}_{ikt-1}} = \beta \frac{\Delta \bar{p}_{ikt}}{\bar{p}_{ikt-1}} + \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{ikt-1}^d} \quad (30)$$

Equation (31) brings a first-stage regression model as follows:

$$\frac{\Delta \tilde{p}_{ikt}}{\tilde{p}_{ikt-1}} = \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d} + \gamma_i + \gamma_k + \epsilon_{ik}$$

Or equivalently, taking logs:

$$\Delta \log \tilde{p}_{ikt} = \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d} + \gamma_i + \gamma_k + \epsilon_{ikt}$$

with the LHS being the growth rate of the fas price (between t and $t - 1$). $\frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d}$ is the change in the considered tariff rate, the second and third terms are fixed effects designed to capture changes in the “firm-specific price” \bar{p}_{ik} , ϵ_{ikt} being the residual. Note that, consistently with the second stage, the first stage will be estimated on a year-by-year basis, and will incorporate 3-digit-sector fixed effects. This implies to consider the following functional form of the first-stage equation:

$$\Delta \log \tilde{p}_{ikt} = \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d} + \gamma_i + \gamma_s + \epsilon_{ikt} \quad (31)$$

or equivalently:

$$\log \tilde{p}_{ikt} = \log \tilde{p}_{ikt-1} + \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d} + \gamma_i + \gamma_s + \epsilon_{ikt} \quad (32)$$

Finally, we allow for more flexibility in the empirical set-up, by allowing a variable degree of persistence in the fas price, i.e. by relieving the constraint of a unit parameter on $\log \tilde{p}_{ikt-1}$:

$$\log \tilde{p}_{ikt} = \beta \log \tilde{p}_{ikt-1} + \alpha \frac{\Delta \tau_{is(k)t}^d}{1 + \tau_{is(k)t-1}^d} + \gamma_i + \lambda_{s(k)} + \epsilon_{ikt} \quad (33)$$

Note that in such a formulation, $\log \tilde{p}_{ikt-1}$ appears as a second instrument for $\log \tilde{p}_{ikt}$. The α parameter should fall between -1 and 0 , and has a direct theoretical interpretation in terms of “pricing-to-market” behavior of firms. $\alpha = 0$ corresponds to the case where the considered sector is made of firms not adjusting their fas price to the change in tariff,

that would cancel out the influence of the tariff change on the price paid by the US consumers; this rather corresponds to small firms which do not have enough market power to manipulate their prices following changes in international competition. $\alpha = -1$ is the other polar case: the sector here displays full pricing-to-market, because it involves large firms fully compensating the tariff change through their margin (see Berman et al., 2012). In-between, $\alpha \in]-1, 0[$ corresponds to some variable degree of “pricing-to-market” in the sector, characterized by firms offsetting partly the impact of the tariff change on the fas price by adjusting the producer price in the opposite direction of the tariff change.

As already mentioned, consistently with the cross-section analysis adopted by now, the first-stage equation is estimated on a yearly basis, and implements 3-digit sector fixed effects ($\lambda_{is(k)}$). We then replace the observed series of fas prices in the right-hand side of Equation (10) by the predicted fas prices produced by Equation (33). We now report results based on our main database at the SITC 5-digit level, before replicating the exercise on HS10 digit level, consistently with one major robustness implemented in the paper.

First-stage estimates based on SITC5 data. Here we run Equation (33) on our standard dataset, based on SITC-5 data. Consistently, we will use as instrument 5-digit product-specific tariff rates, as well as the one-year-lagged fas price. Table B.5 reports summary results of these first stage regressions, while Figure B.2 displays year estimates of β and α parameters, together with 5% confidence bands:

Table B.5: Summary Results for First-Stage Regressions

variable	Mean	1 st Quart.	Median	3 rd Quart.	S.D.	Min	Max
$\log \tilde{p}_{ikt-1} (\hat{\beta})$	0.7484	0.7400	0.7551	0.7663	0.0248	0.6616	0.7788
Student $t_{\hat{\beta}}$	157.07	113.24	168.82	191.15	41.23	82.88	208.23
$\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d} (\hat{\alpha})$	-0.6324	-0.8858	-0.6079	-0.3639	0.3962	-1.8353	0.0534
Student $t_{\hat{\alpha}}$	-2.8178	-3.7575	-2.5741	-1.8099	1.6808	-7.3086	0.2280
F-statistic $\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d}$	10.7023	3.2757	6.6260	14.1188	11.4529	0.0008	53.4159

Figure B.2: Yearly estimates of α and β - SITC5

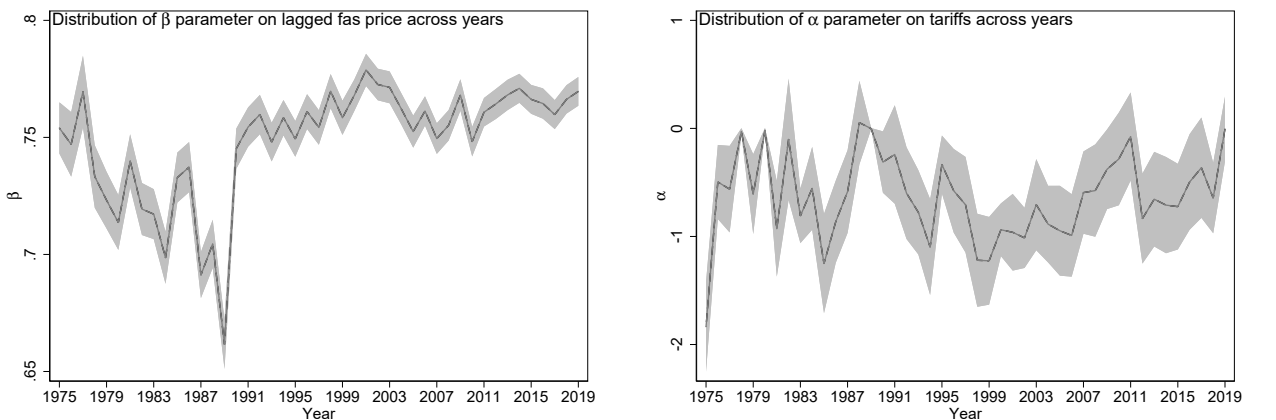


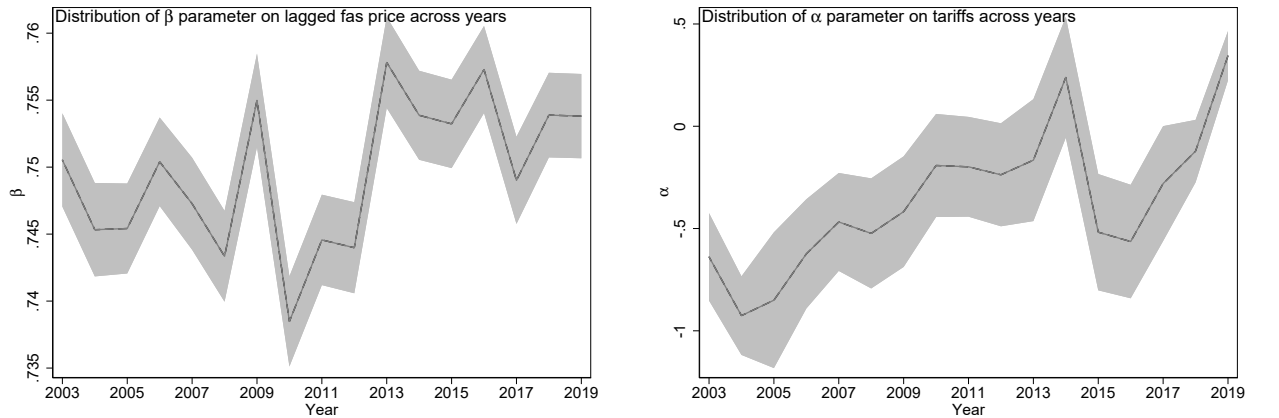
Table B.5 suggests that custom duties variations are a satisfactory predictor of fas prices \tilde{p}_{ik} , with strong significance and the correct, negative sign. The lagged fas price $\log \tilde{p}_{ikt-1}$ displays also the expected positive sign: with a β parameter around 0.75 on average, fas prices exhibit substantial persistence. The F-statistic on the excluded instrument $(\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d} (\hat{\alpha}))$ is on average above 10, the “rule-of-thumb” threshold value recommended by Staiger & Stock (1997) as a test for weak instrumentation. In addition, Figure B.2 shows that most values of the α parameter stand between 0 and -1, as expected, except in a very small number of occasions, corresponding to abrupt fluctuations in oil prices. This is typically the case in 1975, with $\alpha=-1.83$. All in all, these estimates make us confident in the validity of our instrumentation strategy.

First-stage estimates based on HS10 data. Here we replicate our first-stage estimations using HS10 data, available between 2002 and 2019. In addition to one-year-lagged fas price, we use this time HS10-digit product-specific tariff duties. Table B.6 reports summary results of these first-stage regressions, while Figure B.3 presents yearly estimates of β and α parameters, together with 5% confidence bands:

Table B.6: Summary Results for First-Stage Regressions

variable	Mean	1 st Quart.	Median	3 rd Quart.	S.D.	Min	Max
$\log \tilde{p}_{ikt-1} (\hat{\beta})$	0.7496	0.7453	0.7504	0.7539	0.0055	0.7385	0.7578
Student t $\hat{\beta}$	369.81	361.19	366.34	376.77	12.91	352.61	395.33
$\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d} (\hat{\alpha})$	-0.3612	-0.5636	-0.4175	-0.1918	0.3393	-0.9258	0.3448
Student t $\hat{\alpha}$	-2.2505	-3.3518	-2.5489	-1.3144	2.7027	-7.9494	4.7359
F-statistic $\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d}$	11.9399	1.7974	9.0342	14.8620	15.1916	0.8415	63.1932

Figure B.3: Yearly estimates of α and β - HS10



Results are qualitatively very similar to those reported on the longer-time-span, more-aggregated-SITC5 dataset previously reported. The F-statistic on the excluded instrument $(\frac{\Delta \tau_{is(k)t}^d}{1+\tau_{is(k)t-1}^d} (\hat{\alpha}))$ is on average close to 12, slightly higher than in our benchmark. As

previously, Figure B.3 shows that most values of the α parameter stand between 0 and -1, as expected, except in a few years which seem again to coincide with significant fluctuations in oil prices. Interestingly, the value of the α parameter is on average -0.36, lower than in our benchmark on SITC5 data. At this highly disaggregated level, pricing-to-market behavior seems less strong, indicating that the average firm is smaller than its average SITC5 counterpart. In addition, this average value is almost identical to the one found by Fontagné et al. (2018) on French HS6 data between 1995 and 2010 (see the first-stage coefficients in their Table 6), or by Bussiere (2013) on country-level data between 1980 and 2006. In any case, this strengthens our confidence in the validity of our estimation strategy.

C Estimation at the 4-digit level

In this section, we report the estimation results when we retain the 4-digit classification level ($s=4$ -digit).

C.1 Transport cost estimates

Tables C.1 and C.2 report the estimates of both models (with and without additive costs) in air and ocean transport respectively.

Table C.1: Air: Transport costs estimates, selected years, 4-digit level

Year	1974	1981	1989	2001	2009	2013
Model (a) - With only Ad-Valorem TC ($\widehat{\tau}^{ice} - 1$, in %)						
Mean	6.6	5.8	5.2	3.3	3.7	3.2
Median	5.2	4.4	4.1	2.1	2.7	2.6
Model (b) - With Additive & Ad-Valorem TC						
<i>Ad-valorem term ($\widehat{\tau}^{adv} - 1$, in %)</i>						
Mean	3.5	2.6	3.1	1.5	2.1	1.6
Median	2.5	1.7	1.9	1.0	1.7	1.4
<i>Additive term (\widehat{t}/\widehat{p}), in %</i>						
Mean	2.6	2.1	1.7	1.2	1.2	1.0
Median	1.2	0.6	0.6	0.5	0.4	0.4
# observations	14944	16844	25307	35005	38475	39460

Notes: TC = Transport Costs. Statistics are obtained weighting each observation by its share in trade (mode-dependent). Additive term expressed in fraction of fas price.

Table C.2: Vessel: Transport costs estimates, selected years, 4-digit level

Year	1974	1981	1989	2001	2009	2013
Model (a) - With only Ad-Valorem TC ($\widehat{\tau}^{ice} - 1$, in %)						
Mean	9.8	6.1	5.8	5.1	4.2	3.6
Median	9.4	5.1	4.8	4.5	3.8	3.1
Model (b) - With Additive & Ad-Valorem TC						
<i>Ad-valorem term ($\widehat{\tau}^{adv} - 1$, in %)</i>						
Mean	5.4	3.4	2.8	2.8	2.4	2.1
Median	4.9	3.0	2.4	2.5	2.6	1.8
<i>Additive term ($\widehat{t}^{add}/\widehat{p}$), in %</i>						
Mean	4.6	2.6	3.1	2.4	2.1	1.5
Median	2.9	1.3	1.9	1.5	1.3	0.8
# observations	19196	17916	29387	36677	37643	38820

Notes: TC = Transport Costs. Statistics are obtained weighting each observation by its share in trade (mode-dependent). Additive term expressed in fraction of fas price.

C.2 Goodness-of-fit tests at the 4-digit level

We now report the goodness-of-fit exercise (conducted by transport mode) at the 4-digit product classification level (for the selected years). The results are reported in Tables C.3 (for air) and C.4 (for vessel).

Table C.3: Air: Measures of goodness of fit, 4-digit level

	Year					
	1974	1981	1989	2001	2009	2013
R²						
Model (a)	0.48	0.49	0.50	0.50	0.45	0.35
Model (b)	0.63	0.66	0.65	0.66	0.54	0.45
SER						
Model (a)	0.8	0.9	0.83	0.87	0.88	0.93
Model (b)	0.67	0.74	0.69	0.80	0.80	0.86
Log-likelihood						
Model (a)	-17505.6	-21813.5	-30960.6	-44067.6	-49375.6	-53197.9
Model (b)	-14895.8	-18589.9	-26553.5	-37297.9	-45747.6	-49899.1
AIC criteria						
Model (a)	36243.1	44966.9	63417.1	89747.2	100317.13	107963.7
Model (b)	31873.6	39495.8	55777.1	77439.9	94059.1	102224.3
Test LL						
2×(ll(UR) -ll(R))	5219.5	6447.1	8814.1	13539.4	7256.0	6597.5
# restrictions	640	698	778	833	824	818
p-value	0.00	0.000	0.00	0.00	0.00	0.000

Notes: Model (a) = with only ad-valorem transport costs. Model (b) = with additive & ad-valorem transport costs. R^2 between the log of predicted ratio and the log of the observed ratio. The number # of restrictions is equal to the number of parameters estimated, i.e. the number of partner countries plus the number of products.

Table C.4: Vessel: Measures of goodness of fit, 4-digit level

	Year					
	1974	1981	1989	2001	2009	2013
R²						
Term I only	0.50	0.45	0.47	0.41	0.37	0.35
Terms A & I	0.66	0.62	0.62	0.58	0.51	0.46
SER						
Model (a)	0.58	0.64	0.61	0.0.72	0.79	0.82
Model (b)	0.48	0.53	0.51	0.61	0.69	0.75
Log-likelihood						
Model (a)	-16460.1	-16951.6	-26771.4	-39008.3	-43888.9	-47161.6
Model (b)	-12743.65	-13546.9	-21752.8	-33281.0	-39078.9	-43399.2
AIC criteria						
Model (a)	34464.2	35491.2	55272.9	79800.7	89459.8	95987.2
Model (b)	28271.3	29877.8	46595.6	69743.9	81155.7	89692.4
Test LL						
2×(ll(UR) -ll(R))	12385.80	11226.8	17354.7	20113.5	16608.2	12589.6
# restrictions	797	814	881	910	886	874
p-value	0.000	0.000	0.000	0.000	0.000	0.000

Notes: Model (a) = with only ad-valorem transport costs. Model (b) = with additive & ad-valorem transport costs. R^2 between the log of predicted ratio and the log of the observed ratio. The number # of restrictions is equal to the number of parameters estimated, i.e. the number of partner countries plus the number of products.

D Eliminating the composition effects: more details

In this section, we explain in more detail the method employed to eliminate the country and product dimensions of the estimated transport cost.

D.1 More on our methodology

D.1.1 Additive and ad-valorem transport costs: excluding the composition effects

In this section, we detail our methodology to extract the time trend in the pure (or fitted) transport cost component, for both the ad-valorem and the additive component.

For the ad-valorem component - Consider first the multiplicative transport cost component. Rewriting Equation (13) by taking the exponential, we get:

$$\hat{\tau}_{ikt} = \exp \left(\delta + \sum_{i \neq \text{AFG}} \alpha_i \cdot \mathbb{1}_i + \sum_{k \neq 011} \beta_k \cdot \mathbb{1}_k \right) \cdot \exp \left(\sum_{t \neq 1974} \gamma_t \cdot \mathbb{1}_t \right) \cdot \exp(\epsilon_{ikt})$$

Based on this equation, we deduce after estimation that:

$$\begin{cases} \text{For the year 1974:} & \hat{\tau}_{is74} = \exp(\delta + \alpha_i + \beta_s), \\ \text{For any year } t > 1974: & \hat{\tau}_{ist} = \exp(\delta + \alpha_i + \beta_s) \times \exp(\gamma_t) \end{cases}$$

From this, we obtain the following recursive link: $\hat{\tau}_{ist} = \hat{\tau}_{is74} \exp(\gamma_t)$. Given that $\tau > 1$, we can rewrite to get the percentage change between year 1974 and any year $t > 1974$:

$$\Gamma_{ist} = 100 \cdot \frac{\hat{\tau}_{ist} - 1}{\hat{\tau}_{is74} - 1} = 100 \cdot \frac{\hat{\tau}_{is74} \exp(\gamma_t) - 1}{\hat{\tau}_{is74} - 1}$$

As such, the index of transport costs in year t (relative to the reference year 1974) Γ_{ist} only depends on the cost observed in 1974 and the time trend. At this stage though, it remains specific to a product-origin country pair. Next step is to build the index Γ_t^{adv} such that:

$$\Gamma_t^{adv} = 100 \frac{\bar{\tau}_{1974} \cdot \exp(\gamma_t) - 1}{\bar{\tau}_{1974} - 1} \quad (34)$$

that is, Equation (15) with $\bar{\tau}_{1974} = \exp(\delta + \sum_i \alpha_i + \sum_k \beta_k)$ the mean (ad-valorem) transport cost in 1974.

For the additive component - After estimating Equation (14), we can rebuild the additive component according to:

$$\begin{cases} \text{For the year 1974:} & \hat{t}_{is74} = \delta + \alpha_i + \beta_s, \\ \text{For any year } t > 1974: & \hat{t}_{ist} = (\delta + \alpha_i + \beta_s) \cdot \exp(\gamma_t) \end{cases}$$

From this, we deduce the recursive link: $\hat{t}_{ist} = \hat{t}_{is74} \times \exp(\gamma_t)$. Given the constraint $t > 0$, we then obtain the percentage change from 1974 from:

$$\Gamma_{ist}^{add} = 100 \frac{\hat{t}_{ist}}{\hat{t}_{ik74}} = 100 \exp(\gamma_t) \quad (35)$$

Note that it is independent of the product-origin country pair. We can thus rewrite the time-trend series for the additive transport cost component as:

$$\Gamma_t^{add} = 100 \exp(\gamma_t) \quad (36)$$

D.2 Comparing with Hummels (2007)

In this section, we investigate the difference of results with Hummels (2007) regarding the importance of the composition effects in characterizing the time trends of international transport costs. In order to do so, we start from the empirical specification implemented by Hummels (2007) (also making use of Hummels' Stata codes provided on his webpage³⁷), to better identify the precise points of difference between our estimation strategies.

Let us start from Hummels' (2007) quotation (p. 146) according to which (for air), the “*unadjusted measure of ad valorem air shipping costs [is] the aggregate expenditures on air shipping divided by the value of airborne imports*”. From this, we get the “raw” ad-valorem measure of transport costs as the ratio between the imported total value and the exported total value ($(p_{ikt} - \tilde{p}_{ikt})q_{ikt}/\tilde{p}_{ikt}q_{ikt}$), the mean yearly value being obtained by weighting each flow by its value in total trade flows (ie, yielding the observed aggregate value of τ_t for air).

Consider now the “fitted ad-valorem rate”. Hummels (2007) uses “*a regression in which the dependent variable is the ad-valorem air freight cost in logs for commodity k shipped from exporter i ³⁸ at time t . The independent variables include a separate intercept for each exporter-commodity shipped, the weight/value ratio in logs for each shipment, and year dummy variables*”. With the value of the shipment equal to $\tilde{p}_{ikt}q_{ikt}$, and denoting the air freight cost as TC_{ikt} , we can formulate the above sentence according to the following equation (suppressing the transport mode index to alleviate notation):

$$\begin{aligned} \ln TC_{ikt} &= \delta + \beta \ln \frac{q_{ikt}}{\tilde{p}_{ikt}q_{ikt}} + \sum_{i,k} \alpha_{ik} \cdot \mathbb{1}_{ik} + \sum_t \gamma_t \cdot \mathbb{1}_t + \epsilon_{ikt} \\ \Leftrightarrow \ln TC_{ikt} &= \delta + \beta \ln \frac{1}{\tilde{p}_{ikt}} + \sum_{i,k} \alpha_{ik} \cdot \mathbb{1}_{ik} + \sum_t \gamma_t \cdot \mathbb{1}_t + \epsilon_{ikt} \end{aligned} \quad (37)$$

where TC_{ikt} is measured by the ratio between (air) charges, i.e. $(p_{ikt} - \tilde{p}_{ikt})q_{ikt}^{fas}$ and the value of the shipment, i.e. $\tilde{p}_{ikt}q_{ikt}^{fas}$, or equivalently : $TC_{ikt} = \frac{p_{ikt} - \tilde{p}_{ikt}}{\tilde{p}_{ikt}}$.

After estimating Equation (37), Hummels (2007) uses the predicted value of the regression,

³⁷<http://www.krannert.purdue.edu/faculty/hummelsd/research/jep-transport-cost-data.php>

³⁸To be consistent with our notations, we change the country subscript from j (Hummels, 2007 terminology) to i (our terminology).

denoted \widehat{TC}_{ikt} , to obtain the unweighted average in the product/origin country dimension i, k , that is \widehat{TC}_t , to be compared to the unfitted ad-valorem rate TC_t (by transport mode).

What are the main differences with our estimation strategy? Five points may be underlined. First, Hummels (2007) obtains the fitted ad-valorem rate in one step (considering the observed export-import price gap on the left-hand side of Equation (37)), while we use our two-step approach to extract the fitted transport cost (ie, composition effect excluded) from the (already estimated) unfitted rate. However, this is a slight difference, as in both cases it ultimately amounts to taking the predicted value of Equation (37) (which eliminates the changes specific to the origin country/product/year triplet). Second, in contrast to us, Hummels (2007) does not purge his measure of the fitted ad-valorem rate by the country-sector fixed effects. This is not likely to make a substantial difference, however, as these fixed effects are by nature constant over time. Accordingly, they only amount to a scale effect.

A third difference is that we separate the country-product fixed effects ($\sum_{i,k} \alpha_{ik} \cdot \mathbb{1}_{ik}$ in Equation (37)) into two separate components (origin country and product dimensions). As discussed in Section 4, this is constrained by the number of fixed effects to estimate. However, we do not view this as the major cause of difference between our two methods, as can be inferred from the robustness analysis on this point in Section 4.

Fourth, we differ in the weighting scheme retained to obtain the yearly value of the fitted transport cost (in the terms of Hummels (2007) method, the switch from \widehat{TC}_{ikt} to \widehat{TC}_t , Equations (15) and (16) in our case). Hummels (2007) takes the unweighted average value over the i, k dimension, which implicitly attributes a weight equal to 1 to each flow. We proceed differently, as we weight each flow by its relative value on total trade flows observed in 1974. This choice is made for two reasons. First, this weighting scheme does not overweight the small flows in value. Second, the 1974 weighting scheme makes sense as the starting point of our time trend analysis. However, we ensure that our results are not sensitive to an alternative weighting scheme, by building the average fitted transport costs rate as in Hummels (2007), as reported in Section 4.

One last difference remains to be commented, concerning the way the additive component of international transport costs is treated. As we show below, it turns out to be key in accounting for the difference of results with Hummels (2007). Coming back to Equation (37), it can be shown that it encompasses the two extreme cases of only ad-valorem costs ($\beta = 0$) and only additive costs ($\beta = 1$), as also pointed out in Hummels & Skiba (2004). Rewriting Equation (37) in a simpler form as:

$$\ln TC_{ikt} \equiv \ln \left(\frac{p_{ikt} - \tilde{p}_{ikt}}{\tilde{p}_{ikt}} \right) = \Delta_{ikt} - \beta \ln \tilde{p}_{ikt}$$

with $\Delta_{ikt} \equiv \sum_{i,k} \alpha_{ik} \cdot \mathbb{1}_{ik} + \sum_t \gamma_t \cdot \mathbb{1}_t$ agglomerates the various fixed effects for reading clarity.

Under the first polar case with $\beta = 1$, it becomes:

$$\begin{aligned} \ln \left(\frac{p_{ikt} - \tilde{p}_{ikt}}{\tilde{p}_{ikt}} \right) &= \Delta_{ikt} - \ln \tilde{p}_{ikt} \\ \Leftrightarrow \ln(p_{ikt} - \tilde{p}_{ikt}) &= \Delta_{ikt} \end{aligned}$$

Equivalently, we can write:

$$\begin{aligned} p_{ikt} &= \tilde{p}_{ikt} + \exp(\Delta_{ikt}) \\ \Leftrightarrow p_{ikt} &= \tilde{p}_{ikt} + t_{ikt} \end{aligned}$$

with t_{ikt} appropriately defined. This exactly corresponds to the case of additive costs only.

In the second polar case with $\beta = 0$, Equation (37) becomes:

$$\begin{aligned} \ln \left(\frac{p_{ikt} - \tilde{p}_{ikt}}{\tilde{p}_{ikt}} \right) &= \Delta_{ikt} \\ \Leftrightarrow \ln \left(\frac{p_{ikt}}{\tilde{p}_{ikt}} - 1 \right) &= \Delta_{ikt} \\ \Leftrightarrow \frac{p_{ikt}}{\tilde{p}_{ikt}} &= \exp(\Delta_{ikt}) + 1 \end{aligned}$$

that is,

$$p_{ikt} = \tau_{ikt} \tilde{p}_{ikt}$$

with τ_{ikt} appropriately defined.

This exactly corresponds to the case of ad-valorem transport costs only.

As noted by Hummels & Skiba (2004), $0 < \beta < 1$ represents the elasticity of freight costs to the export prices, increasing with the relative weight of the additive component in international transport costs. By estimating Equation (37) with a constant β , Hummels (2007) assumes that the share of additive costs does not vary over time, country partner or product. This is an important difference with our method, as we measure transport costs by explicitly allowing for an additive component that varies in the three dimensions (i.e. allowing for a varying β across time, country partner and product). To establish this point clearly, we replicate the method adopted by Hummels (2007), outlined above, on our database (which is the same as his until 2004). The results are reported in Figure 5.

E More on the model

E.1 Solving the general equilibrium

Following Melitz (2003) and the subsequent literature, denoting M_e the mass of prospective entrants and ρ_e the probability of successful entry (equal to $1 - G(\varphi^*)$, considering only

steady-state equilibrium needs to verify the entry-exit flow equilibrium condition:

$$rho_e M_e = \delta M$$

Given the wage normalization, total revenue in each country should be such that: $E = L_p + \Pi$, with L_p the number of workers of the productive sector and Π total profits. Labor market equilibrium further requires: $L = L_p + L_e$ with $L_e = f_e M_e$ as sunk entry costs are paid in terms of labor. Combining this with the free-entry condition (27), we obtain that $\Pi = L_e$: Total profits in the productive sector are used to pay the entry sunk costs. Making use of this, we obtain that aggregate income in each country is equal to its labor endowment: $E = L$.

Further, total revenue can be expressed as the product of the average sales and the mass of active producers, according to: $E = M\bar{r}$, with \bar{r} average sales. Similarly as for profits, it can be expressed as the sum of average sales on each local and foreign market:

$$\bar{r} = r_d(\tilde{\varphi}(\varphi^*)) + \rho_x r_d(\tilde{\varphi}_x(\varphi_x^*))$$

with the (conditional) probability of export $\rho_x = \frac{1-G(\varphi_x^*)}{1-G(\varphi^*)}$ and average sales on each market which can be shown to be:

$$\begin{aligned}\bar{r}_d &= \left(\frac{\tilde{\varphi}^*}{\varphi^*}\right)^{\sigma-1} \sigma f \\ \bar{r}_x &= \left(\frac{\tilde{\varphi}_x^*}{\varphi_x^*}\right)^{\sigma-1} \left(\frac{\tau + t\varphi_x^*}{\tau + t\tilde{\varphi}_x^*}\right)^{\sigma-1} \sigma f_x\end{aligned}$$

Given selection on the export market, the mass of domestic exporters depends on that of domestic active firms according to: $M_x = \rho_x M$. In the symmetric equilibrium, the total mass of available varieties is then: $M_T = M + M_x = (1 + \rho_x)M$.

E.1.1 Summary

Equations (24), (25), (28), (22) and (27) determine a system of interdependent equations in five endogenous variables $\{\bar{\pi}, \tilde{\varphi}, \tilde{\varphi}_x, \varphi^*, \varphi_x^*\}$. We can deduce the equilibrium values of the remaining set of variables $\{P, M_T, M, M_x, \tilde{\varphi}_T, \bar{r}\}$ by recursively solving the following set of equations:

$$\begin{aligned}
\bar{r} &= \left(\frac{\tilde{\varphi}^*}{\varphi^*} \right)^{\sigma-1} \sigma f + \frac{1 - G(\varphi_x^*)}{1 - G(\varphi^*)} \left(\frac{\tilde{\varphi}_x^*}{\varphi_x^*} \right)^{\sigma-1} \left(\frac{\tau + t\varphi_x^*}{\tau + t\tilde{\varphi}_x^*} \right)^{\sigma-1} \sigma f_x \\
M &= \frac{L}{\bar{r}} \\
M_x &= \frac{1 - G(\varphi_x^*)}{1 - G(\varphi^*)} M \\
M_T &= \left(1 + \frac{1 - G(\varphi_x^*)}{1 - G(\varphi^*)} \right) M \\
\tilde{\varphi}_T &= \tilde{\varphi}_T \equiv \left[\frac{1}{M_T} \left(M \tilde{\varphi}^{\sigma-1} + M_x \left(\frac{\tilde{\varphi}_x}{\tau} \right)^{\sigma-1} \right) \right]^{\frac{1}{1-\sigma}} \\
P &= M_T^{\frac{1}{1-\sigma}} \frac{\rho}{\tilde{\varphi}_T}
\end{aligned}$$

E.2 With a Pareto distribution

As in most of the related literature (Irrarrazabal et al. (2015), **Melitz final proofs**, ...), we adopt a Pareto distribution for firm productivity heterogeneity, with the density and the cumulative functions respectively written as:

$$\begin{aligned}
g(\varphi) &= k \varphi_{\min}^k \varphi^{-(k+1)} \\
G(\varphi) &= 1 - \left(\frac{\varphi_{\min}}{\varphi} \right)^k
\end{aligned}$$

With the Pareto distribution, the system of Equations (24), (25), (28), (22) and (27) can be rewritten as a system of four equations in four endogenous variables: $\{\bar{p}i, g(\varphi_x^*), \varphi_x^*, \varphi^*\}$ as given by:

$$\bar{\pi} = \frac{\sigma - 1}{k - (\sigma - 1)} f + (\varphi^*)^k f_x \left[k \left(\frac{\tau}{\varphi_x^*} + t \right)^{\sigma-1} \left[1 + (k(\varphi_x^*)^k g(\varphi_x^*))^{\frac{1}{\sigma-1}} \right]^{1-\sigma} - (\varphi_x^*)^k \right] \quad (38)$$

$$g(\varphi_x^*) = \int_{\varphi_x^*}^{\infty} \varphi^{\sigma-1-(k+1)} (\tau + t\varphi)^{1-\sigma} d\varphi \quad (39)$$

$$\frac{\varphi_x^*}{\tau + t\varphi_x^*} = \varphi^* \left[\frac{f}{f_x} \right]^{\frac{1}{1-\sigma}} \quad (40)$$

$$\bar{\pi} = \delta f_e \left(\frac{\varphi^*}{\varphi_{\min}} \right)^k \quad (41)$$

Notice that, in the absence of additive costs ($t = 0$), Equation (39) rewrites as:

$$g(\varphi_x^*) = \tau^{1-\sigma} \left[\frac{(\varphi_x^*)^{-(k-(\sigma-1))}}{k - (\sigma - 1)} \right]$$

The system of Equations (38)-(41) thus simplifies to be solved recursively with a full analytical solution. This is no longer the case in the presence of additive costs, and we

have to rely on the model's simulations to obtain the general equilibrium of the model for a given calibration of the deep parameters.