$$\frac{p_{ik}}{\widetilde{p}_{ik}} - 1 = \tau_{ik} - 1 + \frac{t_{ik}}{\widetilde{p}_{ik}}, \text{ with } \tau_{ik} \ge 1 \text{ and } t_{ik} \ge 0$$
 (1)