

1. *Probability boot camp*

- (a) *Prove Markov's inequality: $Pr[X \geq c] \leq E[X]/c$*

The formula for the probability of a continuous random variable X with probability density function $f(x)$ is

$$Pr[x_1 \leq X \leq x_2] = \int_{x_1}^{x_2} f(x)dx$$

And the formula for the expected value of a continuous random variable X with probability density function $f(x)$ is

$$E[x_1 \leq X \leq x_2] = \int_{x_1}^{x_2} xf(x)$$

so for $Pr[X \geq c]$ we have

$$Pr[X \geq c] = \int_c^{\infty} f(x)dx$$

and since X is a nonnegative random variable we have

$$E[X] = \int_0^{\infty} xf(x)dx$$

- (b) *Prove Chebyshev's inequality*
(c) *Show that for any discrete random variables $X, X', E[X] = E[E[X|X']]$.*
(d) *Prove by induction that $E[X_t] = 0$.*