CFP® Board Provided Formulas (w/ BIF Explanations)

$$V = \frac{D_1}{r - g}$$

Intrinsic Value Formula (Valuation)

Calculates the value of a dividend paying security in dollar terms

D1 = next year's dividend

k = r =the rate of return required by the investor

g = the dividend growth rate or the company growth rate

$$r = \frac{D_1}{P} + g$$

Expected Rate of Return Formula

The rate an investor should expect based on price paid for a security

D1 = next year's dividend

P = market price paid for a security

g = the dividend growth rate or the company growth rate

$$COV_{ij} = \rho_{ij}\sigma_i\sigma_j$$

Covariance

Measures how one security behaves as a direct result of another

σi = standard deviation of security i

 σ j = standard deviation of security j

ρij = correlation between securities i and j

$$\sigma_p = \sqrt{W_i^2 \sigma_i^2 + W_j^2 \sigma_j^2 + 2W_i W_j COV_{ij}}$$

Portfolio deviation formula

Standard deviation for a 2 stock portfolio

Wi = weight of stock 'i'

Wi = weight of stock 'j'

σi = standard deviation of stock 'i'

σj = standard deviation of stock 'j'

COVij = covariance between 'I' and 'j'



$$\beta_i = \frac{COV_{im}}{\sigma_m^2} = \frac{\rho_{im}\sigma_i}{\sigma_m}$$

Beta

Risk as a measure of volatility relative to that of the market σ i = standard deviation of the individual security ρ im = correlation between an individual security and the market σ m = standard deviation of the market

$$\sigma_r = \sqrt{\frac{\sum_{t=1}^{n} (r_t - \overline{r})^2}{n}}$$

Standard Deviation in a Population

Deviation of a single security over a series of periods of return

 σr = standard deviation of results from the expected return

 Σ = summation of all terms

n = number of periods being considered

rt = actual return

 \bar{r} = average return

$$S_r = \sqrt{\frac{\sum_{t=1}^{n} (r_t - \overline{r})^2}{n-1}}$$

Standard Deviation of a Sample

Deviation of a single security over a series of periods of return

Sr = standard deviation of results from the expected return

 Σ = summation of all terms

n = number of periods being considered

rt = actual return

 \bar{r} = average return



$$r_i = r_f + (r_m - r_f)\beta_i$$

Capital Asset Pricing Model

Used to determine a theoretically appropriate required rate of return of an asset

ri = the investor's required rate of return

rf = risk free rate (T-Bill rate serves this end)

rm = return of the market (S&P 500 or some broad index)

 βi = beta of the security being measured for required return

$$\alpha_p = \overline{r_p} - \left[\overline{r_f} + \left(\overline{r_m} - \overline{r_f}\right)\beta_p\right]$$

Jensen Model

Measures the performance of a portfolio manager to the market

 αp = difference of return from amount required by investors

rp = return of the portfolio

rf = risk free rate of return

rm = return of the market

 βp = beta of the portfolio being measured

$$T_p = \frac{\overline{r_p} - \overline{r_f}}{\beta_p}$$

Treynor Ratio

Measures the risk-adjusted performance of a portfolio manager

Tp = Treynor Index

rp = return of the portfolio

rf = risk free rate of return

βp = beta of the portfolio being measured



$$D = \frac{1+y}{y} - \frac{(1+y)+t(c-y)}{c[(1+y)^t - 1]+y}$$

Duration

The length of time the discounted cash flow of a bond remains outstanding

c = rate of interest paid on the coupon

t = number of periods to maturity

n = number of cash flows

i = interest or yield to maturity

y = Yield to Maturity (as a %)

c = rate of interest paid on the coupon

t = number of periods to maturity

$$\frac{\Delta P}{P} = -D \left[\frac{\Delta y}{1+y} \right]$$

Change of Bond Price

The change of price that will occur in a bond as interest rates change

 ΔP = the dollar change in price

P = price of a bond

 $\Delta P/P = \%$ price change of bond

(-D) = the duration in terms of years used as a negative value

 Δy = the % change in interest rates. If they go down this number should be negative

1+y = 1 + yield to maturity

$$IR = \frac{R_P - R_B}{\sigma_A}$$

Information Ratio

Measures return above benchmark divided by standard deviation

Rp = return of a portfolio

Rb = return of a benchmark

 σA = tracking error of active return



$$EAR = (1 + \frac{i}{n})^n - 1$$

Effective Annual Return

Accounts for intra-year compounding

i = interest rate

n = number of periods

$$TEY = r/(1-t)$$

Taxable Equivalent Yield

Return that is required on a taxable investment to make it equal to the return on a tax-exempt investment

r = nominal rate of return

t investor's marginaltax rate (as a decimal)

$$AM = \frac{a_1 + a_2 + a_3 + \dots + a_n}{n}$$

Arithmetic Mean

The average of a set of numerical values, calculated by adding them together and dividing by the number of terms in the set

a = rate of return for given period

n = number of periods

$$S_p = \frac{\overline{r_p} - \overline{r_f}}{\sigma_p}$$

Sharpe Ratio

Measures the risk-adjusted performance of a portfolio in terms of standard deviation

Sp = sharpe Index

 $\bar{r}p = return of the portfolio$

ref = risk free rate of return

σp = standard deviation of the portfolio being measured



$$_{1}R_{N}=[(1+_{1}R_{1})(1+E(_{2}r_{1}))...(1+E(_{N}r_{1}))]^{1/N}-1$$

Rate of return for period N

N = number of periods

1R1 = interest rate for period 1

E(2r1) = expected interest rate for period 2

E(Nr1) = expected interest rate for given period

$$HPR = [(1+r_1) \times (1+r_2) \times ...(1+r_n)] - 1$$

Holding Period Return

The total return received from holding an asset or portfolio of assets over a period of time r = rate of return for given period

n = number of periods

$$\sqrt[n]{(1+r_1)\times(1+r_2)\times...(1+r_n)} - 1$$

Geometric Mean

The central number in a geometric progression, also calculable as the nth root of a product of n numbers

n = number of periods

r = rate of return for given period

