## Google Summer of Code 2012 - Sympy

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  - States as Vectors
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# What is Sympy

- A Python library for symbolic mathematics
- Has a goal of becoming a full featured Computer Algebra System
- Written entirely in Python and does not require external libraries

[1]: http://sympy.org/en/index.html

# Sympy 0.7.1 - Features

Core Capabilities

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- Other Modules
  - Polynomials
  - Calculus
  - Solving Equations
  - Discrete Math
  - Matrices
  - ....
  - Physics
    - Mechanics
    - Quantum: Quantum Mechanics, Qubits, Quantum Gates etc.
    - ( GSOC 2012 : Density Operator)

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- Printing
  - LATEX, MathML etc

```
$ cd sympy
$ ./bin/isympy
IPython console for SymPy 0.7.1 (Python 2.7.1) (ground types: gmpy)
These commands were executed:
>>> from future import division
>>> from sympy import *
>>> x, y, z, t = symbols('x y z t')
>>> k, m, n = symbols('k m n', integer=True)
>>> f, q, h = symbols('f q h', cls=Function)
Documentation can be found at http://www.svmpv.org
In [1]: (1/cos(x)).series(x, 0, 10)
Out[1]:
        5*x 61*x 277*x
1 + - + - + - + - + 0(x**10)
        2.4
              720
                    8064
```

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Matrices are created as instances from the Matrix class:

```
>>> from sympy import Hatrix
>>> Matrix([[1,0], [0,1]])
[1 0]
[0 1]
```

you can also put Symbols in it:

```
>>> from sympy import *
>>> x, y = symbols('x,y')
```

You can integrate elementary functions:

```
>>> integrate(6*x**5, x)
6
x
>>> integrate(sin(x), x)
-cos(x)
>>> integrate(log(x), x)
x*log(x) - x
>>> integrate(2*x + sinh(x), x)
2
x + cosh(x)
```

#### LaTeX printing

```
>>> from sympy import Integral, latex
>>> from sympy.abc import x
>>> latex(x**2)
x^(2)
>>> latex(x**2, mode='inline')
$x^(2)$
>>> latex(x**2, mode='equation')
\text{begin(equation)}x^(2)\text{end(equation)}
>>> latex(x**2, mode='equation')
\text{begin(equation)}x^(2)\text{end(equation)}
>>> latex(1/x)
\text{begin(equation*)}x^(2)\text{end(equation*)}
>>> latex(1/x)
\text{frac(1)}{x}
>>> latex(Integral(x**2, x))
\text{int x^(2)\,dx}
```

# Sympy - Quantum Module

Informally, in quantum mechanics, *states* in a closed system are represented as linear combination of a set of basis vectors,

State: 
$$\left[\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \end{pmatrix} + \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix}\right]$$

where

 $\left(\frac{1}{\sqrt{2}}\right)^2 = 0.5$  gives the probability of observing either state.

### Mixed States

Say we have 2 states, given by

$$State_1: \frac{1}{\sqrt{2}} \left( \begin{smallmatrix} 1 \\ 0 \end{smallmatrix} \right) + \frac{1}{\sqrt{2}} \left( \begin{smallmatrix} 0 \\ 1 \end{smallmatrix} \right)$$

with  $Pr(State_1) = \frac{1}{3}$ 

$$State_2: \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

with  $Pr(State_2) = \frac{2}{3}$ 

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$$State_2: \frac{1}{\sqrt{2}} \left( \begin{smallmatrix} 1 \\ 0 \end{smallmatrix} \right) - \frac{1}{\sqrt{2}} \left( \begin{smallmatrix} 0 \\ 1 \end{smallmatrix} \right)$$

with  $Pr(State_2) = \frac{2}{3}$ 

Represented as

$$((\mathit{state}_1, p_1), (\mathit{state}_2, p_2)....(\mathit{state}_n, p_n))$$

This representation becomes quite cumbersome.



# **Density Matrices**

Density  $\mathsf{Matrix}(\rho)$  given by  $\mathsf{sum}$  of outer products of each of these states

$$\rho = \sum_{i=1}^{n} p_i(state_i).(p_i(state_i))^*$$

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This gives us a nice matrix.

- Helps in representation
- Used to evaluate various properties about systems in mixed states

# GSoC 2012 - Project Goals

- Methods to declare density matrices
- Extend operators for time dependent states
- Way to use these objects in equations representing quantum circuits
- Integrate with current eval() functions to work with other quantum expressions

## Tools/Workflow

- Python 2.7
- IPython as interactive python shell
- Emacs powered with python-mode, pymacs and pyrope
- git and github

### live.sympy.org

