

Part 1: Relational Algebra

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advisor (s_ID, i_ID)      -- s_ID references student(ID), i_ID references instructor(ID)
classroom (building, room_number, capacity)
course (course_id, title, dept_name, credits)
department (dept_name, building, budget)
instructor (ID, name, dept_name, salary)
prereq (course_id, prereq_id)  -- prereq_id references prereq(course_id)
section (course_id, sec_id, semester, year, building, room_number, time_slot_id)
student (ID, name, dept_name, tot_cred)
takes (ID, course_id, sec_id, semester, year, grade)  -- ID references student(ID)
teaches (ID, course_id, sec_id, semester, year)  -- ID references instructor(ID)
time_slot (time_slot_id, day, start_time, end_time)
    
```

1.1 Find the IDs and names of all students who have not taken any course offering before Spring 2009.

$$(\pi_{name, ID}(student)) - (\pi_{name, ID}(\sigma_{year < 2009}(student \bowtie takes)))$$

1.2 Find the course sections taught by more than one instructor without using any aggregate functions

$$\rho_{T1}(ID, course_id, sec_id, semester, year)(teaches)$$

$$\rho_{T2}(ID, course_id, sec_id, semester, year)(teaches)$$

$$\pi_{sec_id}(\sigma_{T1.id \neq T2.id}(T1 \bowtie T2))$$

```

Product (maker, model, type)    -- maker is foreign key to Manufacturer(maker)
                                   -- type is stored as pc, laptop, printer
PC (model, speed, ram, hd, price)
Laptop (model, speed, ram, hd, screen, price)
Printer (model, color, type, price) -- color: true for color printer, false for black/white printer

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2.1 Find the model number and price of all products (of any type) made by manufacturer 'BBB'

$$\begin{aligned}
 & \pi_{model, price}(\sigma_{maker="BBB"}(PC \bowtie Product)) \\
 & \cup \\
 & \pi_{model, price}(\sigma_{maker="BBB"}(Laptop \bowtie Product)) \\
 & \cup \\
 & \pi_{model, price}(\sigma_{maker="BBB"}(Printer \bowtie Product))
 \end{aligned}$$

2.2 Find those hard-disk (hd) sizes that occur in two or more PC's.

$$\begin{aligned}
 & \rho_{PC1(model,speed,ram,hd,price)}(PC) \\
 & \rho_{PC2(model,speed,ram,hd,price)}(PC) \\
 & \pi_{hd}(\sigma_{PC1.hd=PC2.hd \text{ AND } PC1.model \neq PC2.model}(PC1 \bowtie PC2))
 \end{aligned}$$

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Supplier (sid, sname, address)
Part (pid, pname, color)
Catalog (sid, pid, cost)    -- which supplier supplies which part and at which price (cost)

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3.1 Find the names of suppliers who supply some red part.

$$\pi_{sname}(\sigma_{color="red"}(Part \bowtie Catalog \bowtie Supplier))$$

3.2 Find the IDs of suppliers who supply only red parts

$$\pi_{sid}(Supplier) - \pi_{sid}(Catalog \bowtie (\sigma_{color \neq "red"}(Part)))$$

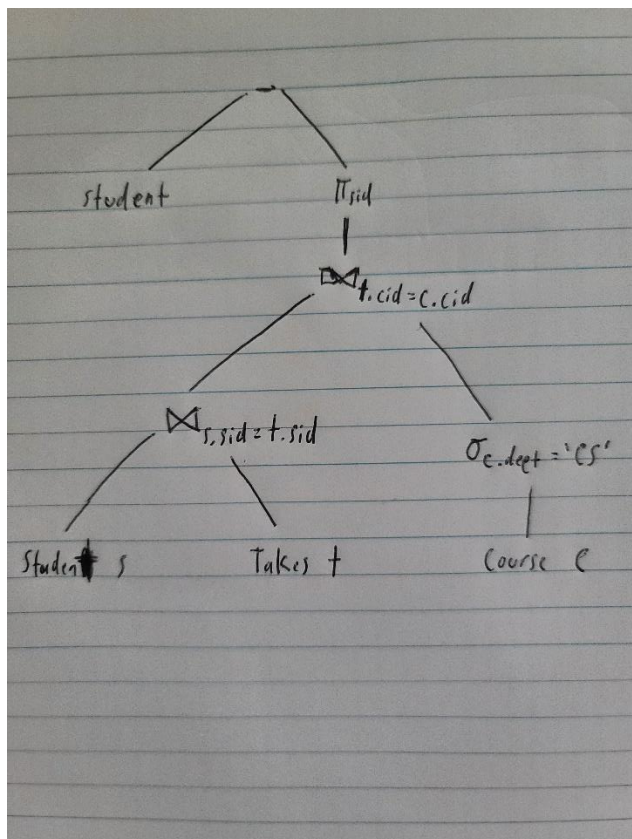
3.3 Find the IDs of suppliers who supply all parts with cost < 20.00

$$\begin{aligned}
 &\pi_{sid,pid}(\\
 &\quad (Part \bowtie Supplier) \\
 &\quad \bowtie \\
 &\quad ((\pi_{sid}(Part \bowtie Supplier)) \\
 &\quad \quad - \\
 &\quad \quad (\pi_{sid}(\sigma_{cost > 20}(Part \bowtie Supplier)))) \\
 &\quad)
 \end{aligned}$$

Part 2: Cost Estimation

1.1 Write a logical plan (i.e., an RA tree) for the following query.

```
SELECT s.sid
FROM   Student s
WHERE  NOT EXISTS
      (SELECT t.sid
       FROM   Takes t, Course c
       WHERE  s.sid = t.sid
            AND t.cid = c.cid
            AND c.dept = 'CS');
```



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T(R) = 105           // total number of rows in relation R
T(S) = 6 * 106       // total number of rows in relation S
T(T) = 5 * 104       // total number of rows in relation T
V(R,A) = 5 * 104      // number of distinct values of attribute A in relation R
V(R,B) = 3 * 103      // number of distinct values of attribute B in relation R
V(S,B) = 3 * 103      // number of distinct values of attribute B in relation S
V(S,C) = 2 * 104      // number of distinct values of attribute C in relation S
V(T,C) = 2 * 104      // number of distinct values of attribute C in relation T
V(T,D) = 104         // number of distinct values of attribute D in relation T

```

2.1 Estimate the number of tuples returned by $\sigma_{A=4750}(R)$. Show your steps.

1. We know that in regards to selectivity ($\sigma_{A=c}(R)$), we have the form $\frac{1}{V(R,A)}$
2. Thus, we will get $10^5 * \frac{1}{5*10^4}$ which will equal 2

2.2 Estimate the number of tuples returned by the following query. Show your steps.

```

SELECT R.A, S.B, S.C
FROM   R NATURAL JOIN S

```

$$\frac{T(R)*T(S)}{\max\{V(R,B),V(S,B)\}} \rightarrow \frac{(10^5) * (6*10^6)}{\max\{3*10^3, 3*10^3\}} \rightarrow \frac{(10^5) * (6*10^6)}{3*10^3} \rightarrow 200000000$$

2.3 Estimate the number of tuples returned by the following query. Show your steps.

```

SELECT *
FROM   R, S, T
WHERE  R.A = 4750 and R.B = S.B and S.C = T.C and T.D = 1102

```

1. $T(R) * T(S) * T(T) \rightarrow 10^5 * (6 * 10^6) * (5 * 10^4) \rightarrow 3 * 10^{16}$
2. $(3 * 10^{16}) * \left(\frac{1}{V(R,A)}\right) * \left(\frac{1}{\max\{V(R,B),V(S,B)\}}\right) * \left(\frac{1}{\max\{V(S,C),V(T,C)\}}\right) * \left(\frac{1}{V(T,D)}\right)$
3. $(3 * 10^{16}) * \left(\frac{1}{5*10^4}\right) * \left(\frac{1}{3*10^3}\right) * \left(\frac{1}{2*10^4}\right) * \left(\frac{1}{10^4}\right) \rightarrow 1$