

# QUEUE

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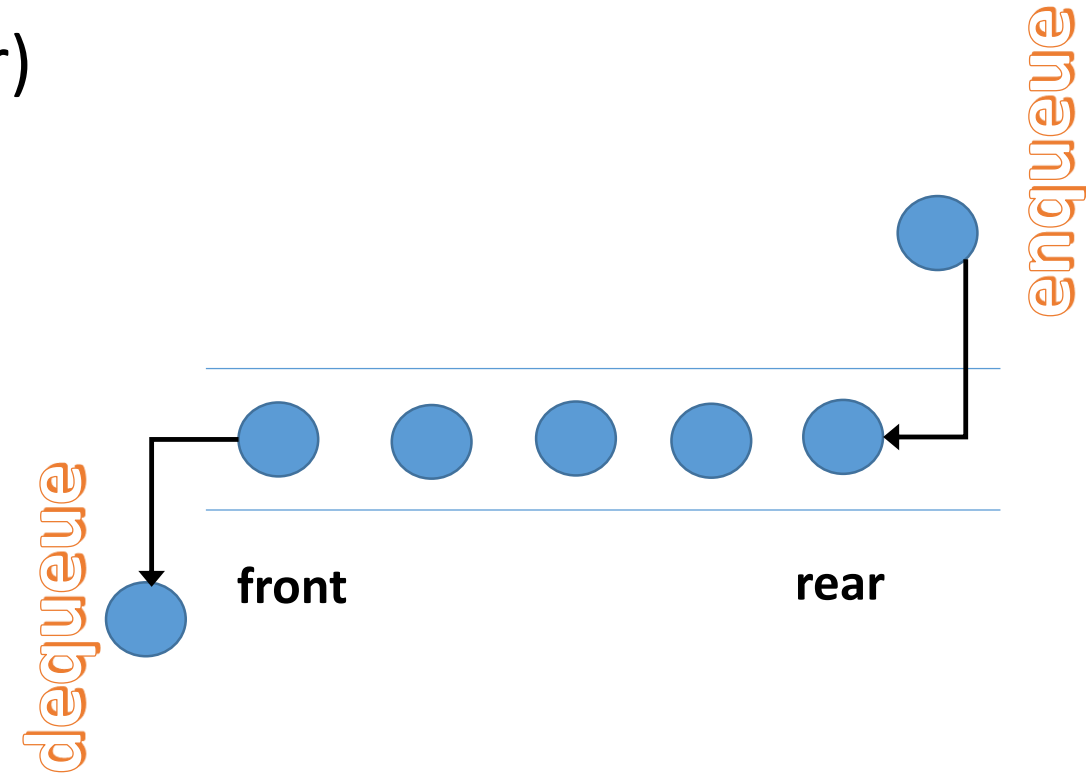
# Queue

- Linear data structure
- Based on the principle of **First-In-First-Out** (FIFO)
  - Data entered first will be accessed first
- Ordered collection of items where an item is inserted at one end called the **rear** and an existing item is removed from the other end, called the **front**
- **En-Queue**: Add items on the Rear end
- **De-Queue**: Remove items from the Front end



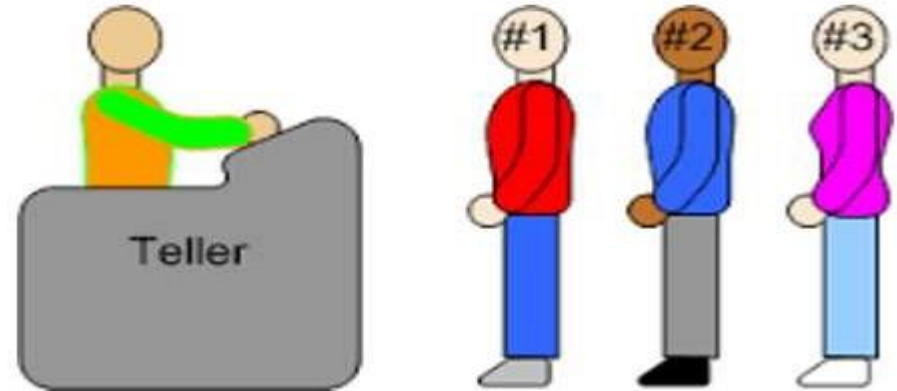
# Operations in an Queue

- Operations performed from both ends
  - Head-tail or front-back.
  - **En-Queue:** insert an item into back (rear) of the queue
  - **De-Queue:** Remove an item from the front of the queue
- People standing at MacDonalds are perfect example of an Queue



# Applications of Queue

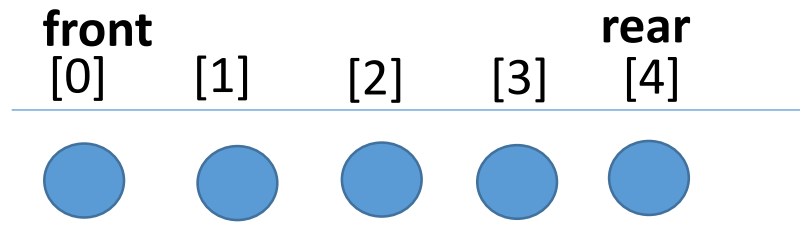
- Checkout line
- Printer/keyboard/mouse etc. queue
- Airport take-off
- Operating system
  - Job Scheduling
  - Multi-programming
- Different types of scheduling algorithms: Round Robin



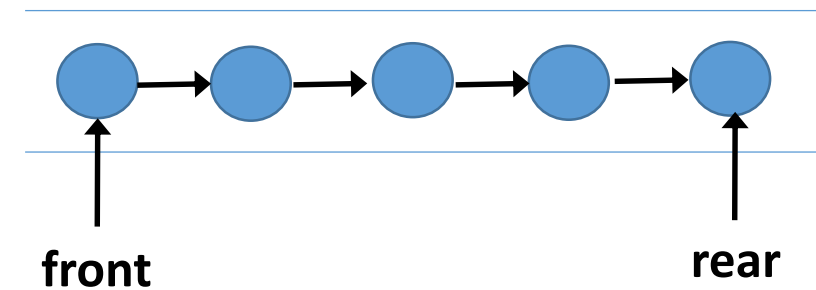
# Queue

- The queue can be implemented into two ways:
  - Using arrays (Static implementation)
  - Using pointer (Dynamic implementation)

## ARRAY / STATIC REPRESENTATION OF QUEUE

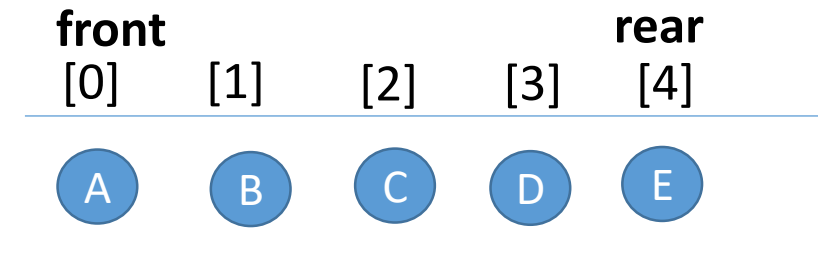
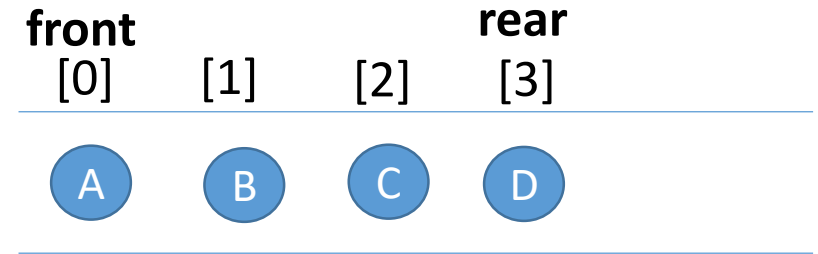


## POINTER / DYNAMIC REPRESENTATION OF QUEUE



# Queue Representation using Array (1/2)

- Let QUEUE be an array
- Two variables: FRONT & REAR
- FRONT contains the location of the element to be removed or deleted
- REAR contains location of the last element inserted



# Queue Representation using Array (2/2)

- The conditions:
  - $\text{FRONT} = \text{NULL}$  indicates empty queue
  - $\text{REAR} = \text{N}-1$  indicates that queue is full

---

**EMPTY**

---

**Front = NULL**

**N = 5**

**front**

[0]

[1]

[2]

[3]

**Rear = N-1**

[4]

A

B

C

D

E

---

# QUEUE OPERATIONS

front

rear  
[0]

A

enqueue (B)

front  
[0]

rear  
[1]

A

B

enqueue (C)

front  
[0]

[1]

rear  
[2]

A

B

C

front  
[0]

[1]

rear  
[2]

A

B

C

dequeue (B)

front  
[0]

rear  
[1]

B

C

A



# Algorithm: Enqueue (1/2)

**ENQUEUE** (QUEUE, REAR, FRONT, ITEM)

QUEUE is an array with N elements;

FRONT is the pointer that contains the location of the element to be deleted;

REAR contains the location of the inserted element; ITEM is the element to be inserted.

Step 1: if  $REAR = N-1$  then [Check Overflow]

    PRINT “QUEUE is Full or Overflow”

    Exit [End if]

# Algorithm: Enqueue (2/2)

Step 1: if  $REAR = N-1$  then [Check Overflow]

PRINT "QUEUE is Full or Overflow"

Exit

Step 2: if  $FRONT = NULL$  [Check if empty Queue]

$FRONT = -1$

$REAR = -1$

Step 3:  $REAR = REAR + 1$  //[Increment REAR]

$QUEUE[REAR] = ITEM$

//[Copy ITEM to REAR]

Step 4: Return

front, rear

[0]

A

enqueue (B)

front

[0]

rear

[1]

A

B

enqueue (C)

front

[0]

[1]

rear

[2]

A

B

C

# Algorithm: Dequeue (1/2)

**ALGORITHM: DEQUEUE** (QUEUE, REAR, FRONT, ITEM)

QUEUE is the array with N elements; FRONT is the pointer that contains the location of the element to be deleted; REAR contains the location of the inserted element. ITEM will store the element to be deleted.

Step 1: if FRONT = NULL [Check Empty Queue]

    PRINT “QUEUE is Empty or Underflow”

    Exit

[End if]

# Algorithm: Dequeue (2/2)

Step 2:  $ITEM = QUEUE[FRONT]$

Step 3: if  $FRONT = REAR$

[QUEUE has only one element]

$FRONT = NULL$

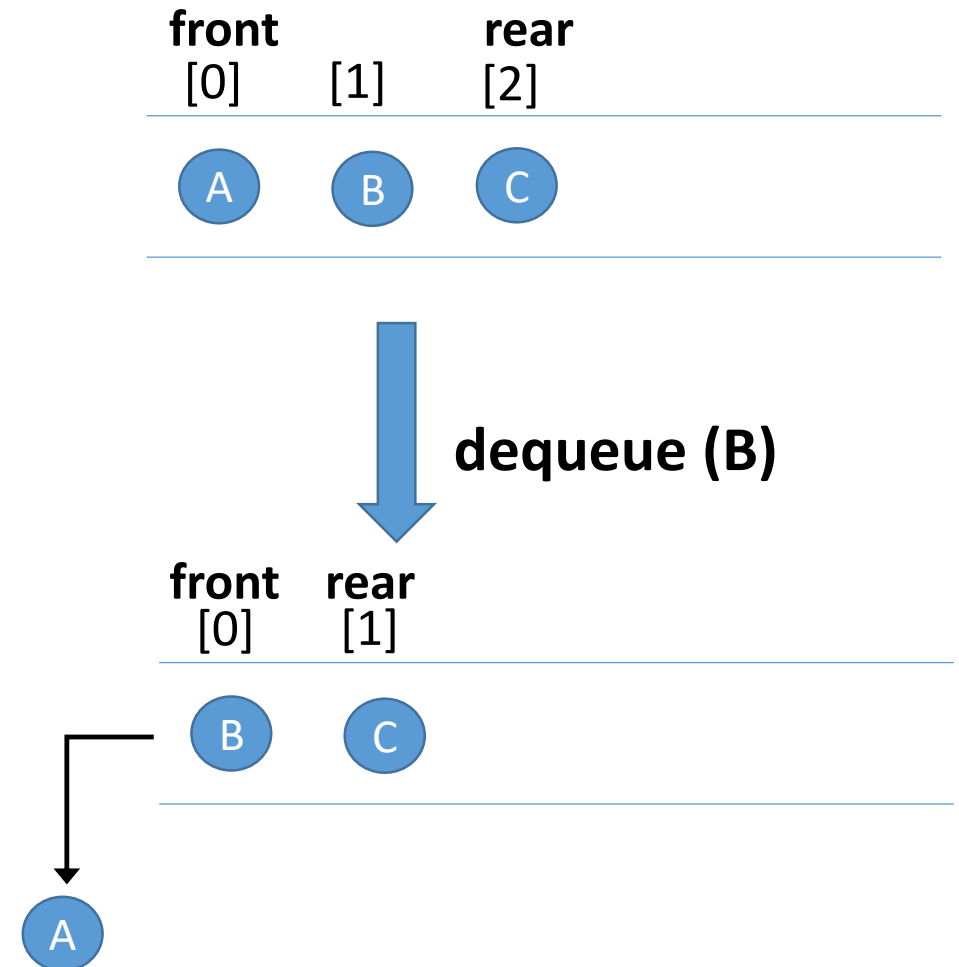
$REAR = NULL$

else

$FRONT = FRONT + 1$

[Increment FRONT pointer]

Step 4: Return



# Array Implementation of Queue

Q    front = NULL  
      Rear = NULL

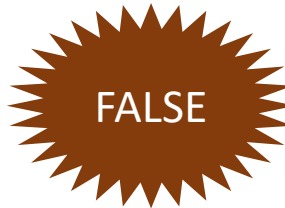
front                  rear  
[0]    [1]    [2]



front,  
rear  
[0]

A

front    rear  
[0]    [1]



front    rear  
[0]    [1]

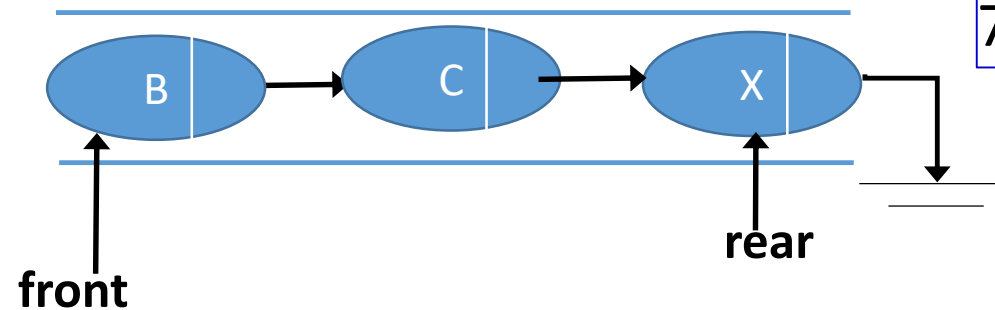
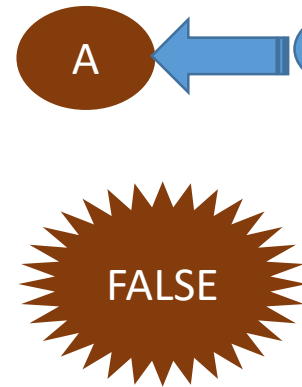
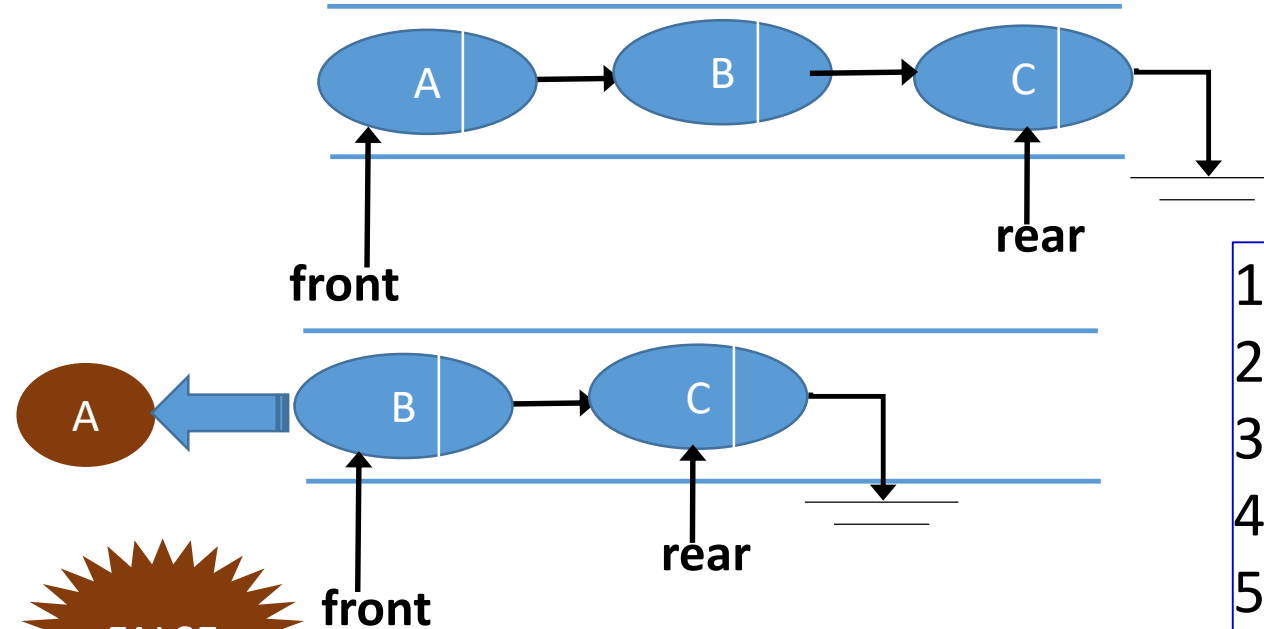
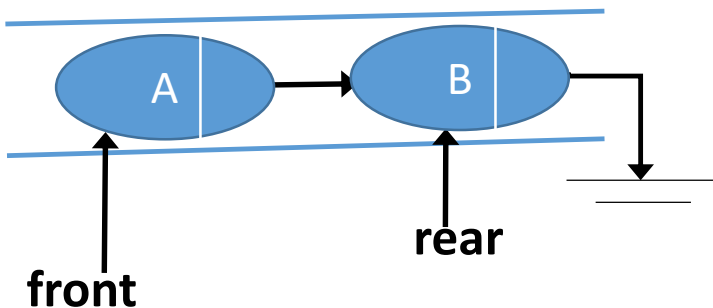
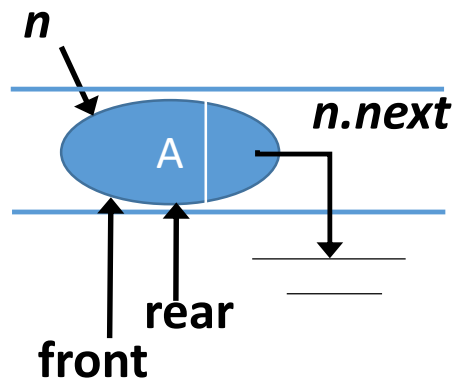
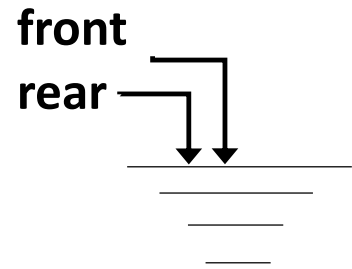


front                  rear  
[0]    [1]    [2]



1. makeQueue(Q)
2. enqueue(A, Q)
3. enqueue(B, Q)
4. enqueue(C, Q)
5. dequeue(Q)
6. isEmpty(Q)
7. enqueue(X, Q)

# Pointer Implementation of Queue



1. makeQueue(Q)
2. enqueue(A, Q)
3. enqueue(B, Q)
4. enqueue(C, Q)
5. dequeue(Q)
6. isEmpty(Q)
7. enqueue(X, Q)

# RECOMMENDED FUNCTIONS

- **Queue()** creates a new, empty queue; no parameters and returns an empty queue
- **enqueue(item)** adds a new item to rear of queue; needs the item and returns nothing
- **dequeue()** removes front item; needs no parameters, returns item, queue is modified
- **isEmpty()** test if queue is empty; needs no parameters, returns a boolean value
- **size()** returns number of items in the queue; needs no parameters; returns an integer

# FOUR Types of Queues

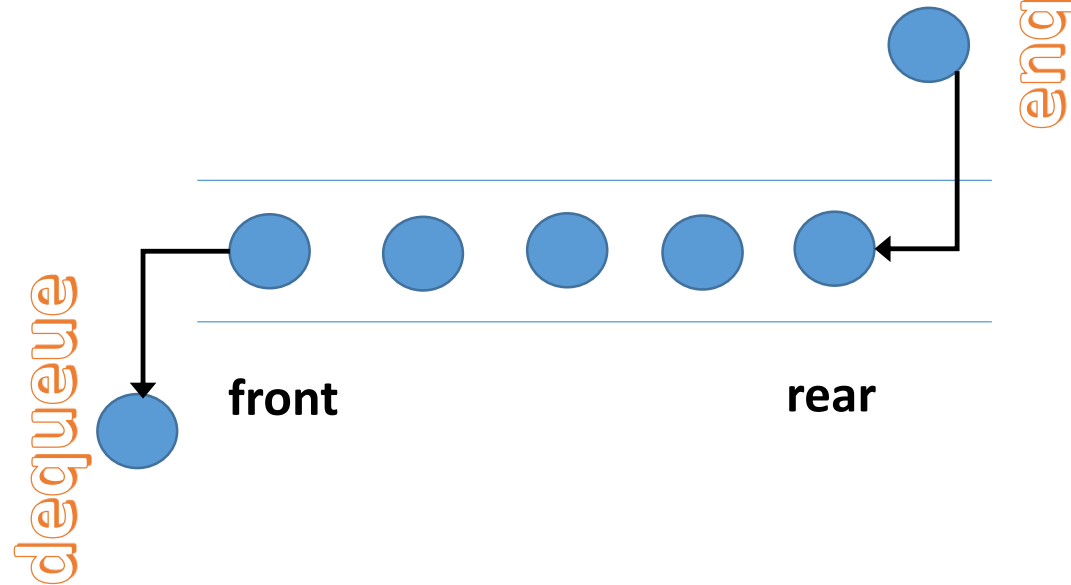
- Simple Queue
- Circular Queue
- Priority Queue
- De-queue ( Double Ended Queue) – not being covered



# Simple Queue

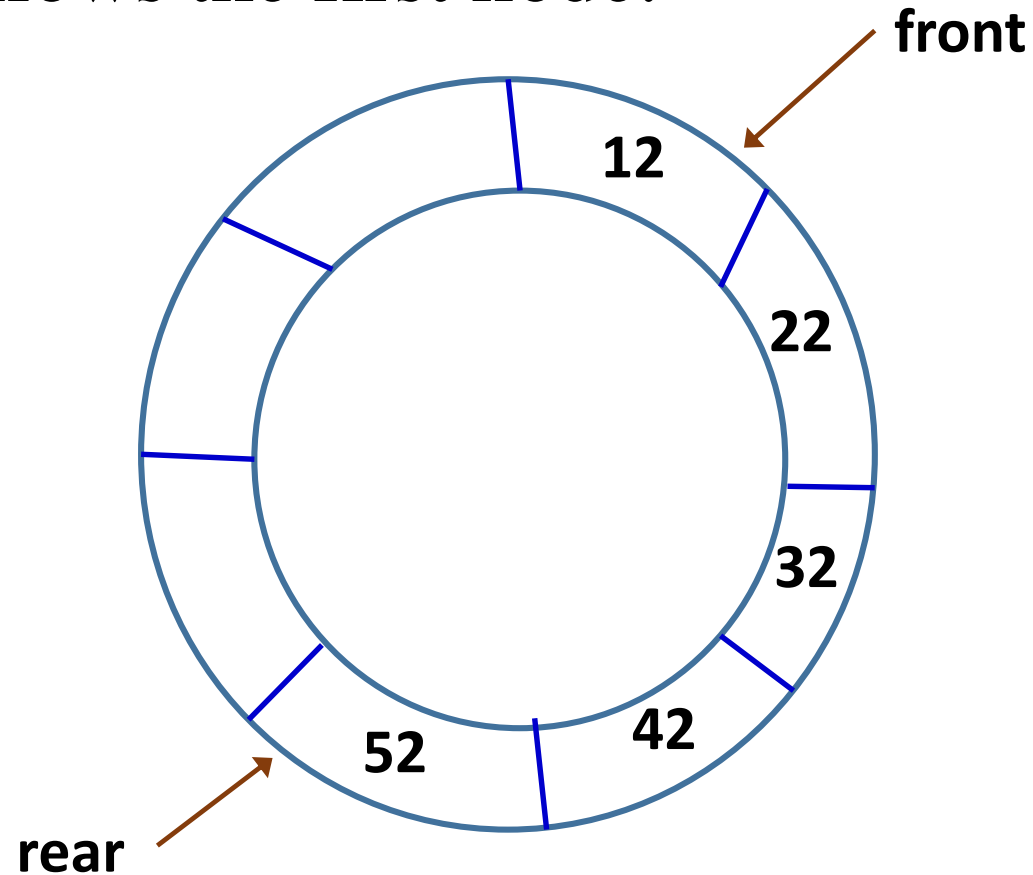
## Simple Queue:

- Insertion occurs at the rear end of the list
- Deletion occurs at the front end of the list.

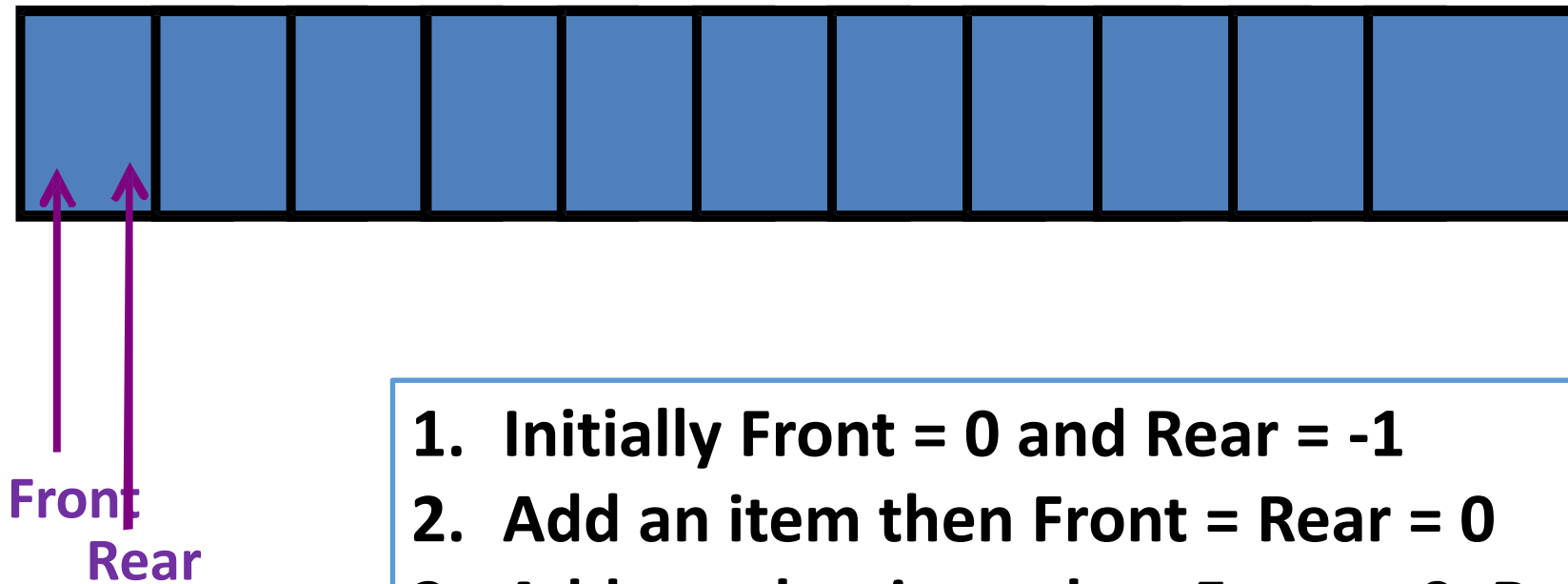


# Circular Queue

**Circular Queue:** All nodes are treated as a circle such that the last node follows the first node.



# Array Implementation: Circular Queue

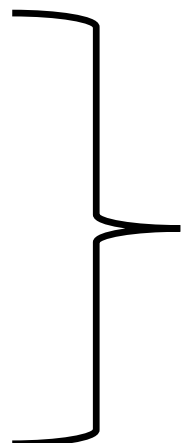


1. Initially  $\text{Front} = 0$  and  $\text{Rear} = -1$
2. Add an item then  $\text{Front} = \text{Rear} = 0$
3. Add another item then  $\text{Front} = 0$ ;  $\text{Rear} = 1$
4. Add three items then  $\text{Front} = 0$ ;  $\text{Rear} = 4$

# Logical Circularity of Queue (1/2)

Addition causes the increment in REAR.

When REAR reaches MAX-1 position then Increment in REAR causes REAR to reach at first position that is 0

If (rear == MAX-1)		rear = ( rear + 1 ) % MAX;
rear = 0		
Else		
rear = rear + 1		

# Logical Circularity of Queue (2/2)

Deletion causes the increment in FRONT.

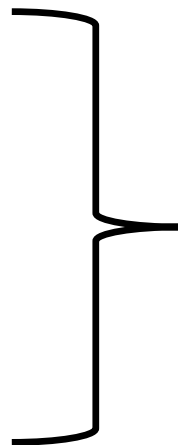
When FRONT reaches the MAX-1 position, then increment in FRONT, causes FRONT to reach at first position that is 0

If (front == MAX-1)

front = 0

Else

front = front + 1



Front = ( front + 1 ) % MAX;

# Drawbacks of Circular Queue

- **Boundary case problem:** Difficult to distinguish full and empty queues
- In circular queue it is necessary that:
  - Before insertion, fullness of Queue must be checked (for overflow)
  - Before deletion, emptiness of Queue must be checked (for underflow)

- **Condition to check FULL Circular Queue**

**If** `(( front == MAX-1) || ( front ==0 && rear == MAX - 1))`

- **Condition to check EMPTY Circular Queue**

**if** `(( front == MAX-1) || ( front ==0 && rear == MAX - 1))`

**To solve the drawback of circular Queue:**

Use **count variable** to hold the current position ( in case of insertion or deletion)

# Circular Queue using count

Operations	Algorithms
Initialize Operation	<b>INIT</b> (QUEUE,FRONT,REAR,COUNT)
<b>Is_Full</b> check	<b>INSERT-ITEM</b> (QUEUE, FRONT, REAR, MAX, COUNT, ITEM)
<b>Is_Empty</b> check	<b>REMOVE-ITEM</b> (QUEUE, FRONT, REAR, COUNT, ITEM)
Insertion operation	<b>FULL-CHECK</b> (QUEUE,FRONT,REAR,MAX,COUNT,FULL)
Deletion operation	<b>EMPTY-CHECK</b> (QUEUE,FRONT,REAR,MAX,COUNT,EMPTY)

# Algorithms

## **INIT(Queue, FRONT, REAR, COUNT)**

1. FRONT = 1
2. REAR = 0
3. COUNT = 0
4. Return

## **FULL-CHECK(Queue, FRONT, REAR, MAX, COUNT, FULL)**

If ( COUNT = MAX ) then

    FULL = true

Otherwise

    FULL = false

Return

## **EMPTY-CHECK(Queue, FRONT, REAR, MAX, COUNT, EMPTY)**

This is used to check queue is empty or not.

If( COUNT = 0 )

    then EMPTY = true

Otherwise

    EMPTY = false

Return



# Insertion Operation

**INSERT-ITEM( QUEUE, FRONT, REAR, MAX, COUNT, ITEM)**

This algorithm is used to insert or add item into circular queue

If ( COUNT = MAX ) then

    Display “Queue overflow”

    Return

Otherwise

    If ( REAR == MAX ) then

        REAR = 1

    Otherwise

        REAR = REAR + 1

    QUEUE(REAR) = ITEM

    COUNT = COUNT + 1

Return

# Deletion Operation

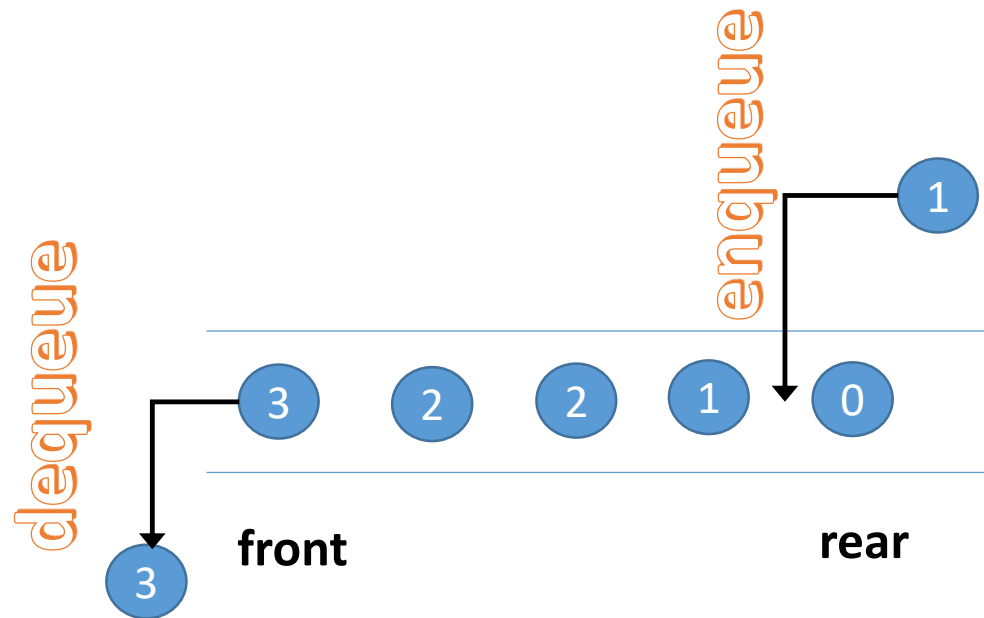
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REMOVE-ITEM( QUEUE, FRONT, REAR, COUNT, ITEM)
```

```
If ( COUNT = 0 ) then  
    Display "Queue underflow"  
    Return
```

```
Otherwise  
    ITEM = QUEUE(FRONT)  
    If ( FRONT = MAX ) then  
        FRONT = 1  
    Otherwise  
        FRONT = FRONT + 1  
        COUNT = COUNT + 1  
    Return
```

# Priority Queue (1/3)

- Each items have some pre-defined priority.
- An element can be inserted or removed from any position depending upon their priority.



Higher Value  
=> Higher priority

# Priority Queue (2/3)

- Stores item into queue with associated priority
- Does not support FIFO (First In First Out)
- It supports the following three operations:
  - **InsertWithPriority**: Insert an item to the queue with associated priority
  - **GetNext**: remove the element from the queue which has highest priority.  
Also know as **PopElement()** or **GetMaximum**
  - **PeekAtNext(optional)**: Get the item with highest priority without removing it

# Priority Queue (3/3)

- Every item has a priority associated with it
- An element with high priority is dequeued before an element with low priority
- If two elements have the same priority, they are served according to their order in the queue
- A typical priority queue supports following operations
  - insert(item, priority):** Inserts an item with given priority
  - getHighestPriority():** Returns the highest priority item
  - deleteHighestPriority():** Removes the highest priority item

# Implementing Priority Queue

- **insert()** Adding an item at end of array in  $O(1)$  time
- **getHighestPriority()** Linearly search the highest priority item in array. This operation takes  $O(n)$  time
- **deleteHighestPriority()** First linearly search an item, then remove the item by moving all subsequent items one position back
- Using Linked List, time complexity of all operations remains same as array.
- The advantage with linked list is deleteHighestPriority() can be more efficient as we don't have to move items

# Some Applications of Queue

1. Modeling and analysis of Computer Networks
2. CPU Scheduling
3. Graph algorithms like Dijkstra's shortest path algorithm, Prim's Minimum Spanning Tree.
4. All queue applications where priority is involved
5. Heap Sort

**Thank you!**