Homework 3B

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Problem explanation

• Find a path that minimizes the sum of weights of all points that the path passes

Each path must only have at most 1 zero

Path may not be the shortest path

Problem explanation

- Input:
- 1. Starting and destination point indices
- 2. 10-by-10 matrix; weight being an integer between -100 and 100, or -9999 (-9999 means not included)
- Output:
- 1. The sum of minimum weight
- 2. The series of point indices from starting to destination point including themselves

 Use DFS (Depth First Search) with priority to the smaller values

• During the DFS, branch out to the smallest value in reach

• Each index has at most 4 possible paths to branch out to

 As shown, the orange index has the top, left, bottom, and right index to branch out to



 For the solution, use DFS on the four possible pathways and find the minimum out of the four

The minimum out of the four will be the final answer

Visited_already function:

 Checks whether a certain index has been visited already or not

```
int visited_already(int visited[4][MAX * MAX], int row, int col, int index)
{
   for(int k = 0; k < col; k++)
   {
     if(visited[row][k] == index)
     {
        return 1;
     }
   }
}</pre>
```

- source_row, source_col, dest_row, dest_col: source and destination indices
- matrix: 6 by 6 matrix
- Visited: DFS path for each possible answer
- Sum: each minimum sum
- Zero_count: number of zeroes
- Col_store: number of Indices passed by each DFS

```
int source_row, source_col, dest_row, dest_col;
int matrix[MAX][MAX];
int visited[4][MAX * MAX];
//sum of going to a certain path
//[0 - 3]: up, left, down, right, respectively
int sum[4];
//number of zeroes passed by going to that index
int zero_count = 0;
int col_store[4];
```

- Scan for variables

```
scanf("%d %d %d %d", &source_row, &source_col, &dest_row, &dest_col);
source_row -= 1;
source_col -= 1;
dest_row -= 1;
dest_col -= 1;
//scan for the matrix
for(int i = 0; i < MAX; i++)</pre>
  for(int j = 0; j < MAX; j++)</pre>
    scanf("%d", &matrix[i][j]);
```

- For loop for each pathway
- Insert the source as the first value for each path
- Reinitialize variables

```
for(int i = 0; i < 4; i++)
  int \cdot j = 0;
  zero_count = 0;
  int row = source_row;
  int col = source_col;
  visited[i][j] = source_row * 100 + source_col + 101;
  sum[i] = matrix[source_row][source_col];
  if(matrix[source_row][source_col] == 0)
    zero_count++;
```

- The preparation of each of the four paths

```
- i = 0: up
- i = 1: left
- i = 2: down
- i = 3: right
```

```
if(i == 0 && row > 0)
  row--:
else if(i == 1 && col > 0)
  col--;
else if(i == \cdot 2 \cdot \&\& \cdot row \cdot < \cdot 5)
  row++;
else if(i == 3 & col < 5)
  col++;
```

Start of DFS while loop:

- Insert the next value and sum up
- Minimum value was already decided in the later part of the loop

```
while(1)
{
    visited[i][j] == row * 100 + col + 101;
    int cur_index == visited[i][j];
    int dest_index = dest_row * 100 + dest_col + 101;
    sum[i] += matrix[row][col];
    j++;
```

- If the destination is within reach, approach it directly as the next index

```
if(cur_index - - 100 - == · dest_index)
  row--;
  continue;
else if(cur_index - 1 == dest_index)
  col--:
  continue;
else if(cur_index + 100 == dest_index)
  row++;
  continue;
else if(cur_index + 1 == dest_index)
  col++;
  continue;
else if(cur_index == dest_index)
  break;
```

- Decide the four possible pathways to branch out to every

single time:

- Also making sure each index has not been visited yet

```
int candidates[4][2] = {{9999, 0}, {9999, 0}, {9999, 0}, {9999, 0}};
if(row > 0 && visited_already(visited, i, j, (row - 1) * 100 + col + 101) == 0)
  candidates[0][0] = matrix[row - 1][col];
  candidates[0][1] = (row - 1) * 100 + col + 101;
if(col > 0 && visited_already(visited, i, j, row * 100 + col - 1 + 101) == 0)
  candidates[1][0] = matrix[row][col - 1];
  candidates[1][1] = row \cdot * \cdot 100 \cdot + \cdot col \cdot - \cdot 1 \cdot + \cdot 101;
if(row < 6 && visited_already(visited, i, j, (row + 1) * 100 + col + 101) == 0)
  candidates[2][0] = matrix[row + 1][col];
  candidates[2][1] = (row + 1) * 100 + col + 101;
if(col < 6 && visited_already(visited, i, j, row * 100 + col + 1 + 101) == 0)
  candidates[3][0] = matrix[row][col + 1];
  candidates[3][1] = row * 100 + col + 1 + 101;
```

- Find the minimum value among the possible indices

```
int min_index;
int min = 9999;
for(int k = 0; k < 4; k++)
  if(candidates[k][0] == -9999)
    continue;
  else if(candidates[k][0] == 0 & count == 1)
    continue;
  if(candidates[k][0] < min)</pre>
   min = candidates[k][0];
   min_index = candidates[k][1];
```

- Next row and column values get updated depending on the minimum value and index

- If a zero exists, increase zero_count

- Col_store happens after the while loop and before the next for loop

```
if(min == 0)
{
    zero_count++;
}
row = min_index / 100 - 1;
col = min_index % 100 - 1;
}
col_store[i] = j;
```

- Once for loop for each path is done, compare the sum of

each pathway

- Save the data for the minimum sum and print out its data

```
int min = 9999;
int index;
for(int i = 0; i < 4; i++)
  if(sum[i] < min)</pre>
    index = i;
    min = sum[i];
printf("%d\n", min);
for(int i = 0; i < col_store[index]; i++)
 printf("%d %d\n", visited[index][i] / 100, visited[index][i] % 100);
```

Solution analysis

Pros:

- Consistent
- Efficient due to greedy algorithm application

Cons:

- Quite lacking
- When the destination index is nearby, it will directly approach it
 - This reduces certain possible options that can reduce the sum

Thank you!