

Homework 2B

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Problem explanation

- Create all the game results that yield the maximum or minimum points (D) of a team with the Cth largest scores
- In other words, Maximize or minimize the Cth ranking's score
- Given inputs are:
 - A: points given for a Win
 - B: points given for a Tie
 - C: target ranking which needs to be maximized / minimized
 - D: 0 (minimum) or 1 (maximum)

Solution explanation

- Focus on half of the matrix only (upper right division from the diagonal)
- Including the diagonal for the X's

Solution explanation

- Maximum:
 - Have a tie score for C th ranking and above (To replace all losses of the C th ranking with ties)
 - Win $20 - C$ games and tie $C - 1$ games
- Minimum:
 - Have a tie score for C th ranking and below (To eliminate any wins for C)
 - Solve for maximum for $(C - 1)$ ranking
 - Lose $C - 1$ games and tie $20 - C$ games

Solution explanation

- To simplify the code, both the maximum and minimum will apply
- For maximum, maximum code will apply to C , and minimum to $C + 1$
- For minimum, minimum code will apply to C , and maximum to $C - 1$

Solution explanation

```
1  #include <stdio.h>
2
3  int main()
4  {
5      int a, b, c, d;
6      char results[20][20];
7      int num_of_ties;
8      int i, j;
9
10     scanf("%d%d%d%d", &a, &b, &c, &d);
11
12     for(i = 0; i < 20; i++)
13     {
14         //num of ties for the rankings for > / >= c
15         if(d == 1)
16             num_of_ties = c;
17         else
18             num_of_ties = c - 1;
19
20         for(j = i; j < 20; j++)
21         {
22             //diagonal is X
23             if(i == j)
24             {
25                 results[i][j] = 'X';
26             }
27             //have C - 1 number of ties
28             else if(num_of_ties - 1 - i > 0)
29             {
30                 results[i][j] = 'T';
```

```
31                 results[j][i] = 'T';
32                 num_of_ties--;
33             }
34             //for minimum, everything else is a tie
35             else if(i >= num_of_ties)
36             {
37                 results[i][j] = 'T';
38                 results[j][i] = 'T';
39             }
40             //remaining are wins
41             else
42             {
43                 results[i][j] = 'W';
44                 results[j][i] = 'L';
45             }
46         }
47     }
48
49     for(i = 0; i < 20; i++)
50     {
51         for(j = 0; j < 20; j++)
52         {
53             printf("%c", results[i][j]);
54         }
55         printf("\n");
56     }
57 }
```

Solution explanation

- A: points for Wins
- B: points for Losses
- C: target ranking
- D: 0 (minimum) or 1 (maximum)
- results: result matrix
- num_of_ties: number of ties of the winners
- i, j: iteration variables

```
1  #include <stdio.h>
2
3  int main()
4  {
5      int a, b, c, d;
6      char results[20][20];
7      int num_of_ties;
8      int i, j;
9
10     scanf("%d %d %d %d", &a, &b, &c, &d);
11
```

Solution explanation

- For loop:
- Fill up the results matrix with W, L, T, X

```
12 for(i = 0; i < 20; i++)
13 {
14     //num of ties for the rankings for > / >= c
15     if(d == 1)
16         num_of_ties = c;
17     else
18         num_of_ties = c - 1;
19
20     for(j = i; j < 20; j++)
21     {
22         //diagonal is X
23         if(i == j)
24         {
25             results[i][j] = 'X';
26         }
27         //have C - 1 number of ties
28         else if(num_of_ties - 1 - i > 0)
29         {
30             results[i][j] = 'T';
31             results[j][i] = 'T';
32             num_of_ties--;
33         }
34         //for minimum, everything else is a tie
35         else if(i >= num_of_ties)
36         {
37             results[i][j] = 'T';
38             results[j][i] = 'T';
39         }
40         //remaining are wins
41         else
42         {
43             results[i][j] = 'W';
44             results[j][i] = 'L';
45         }
46     }
47 }
```


Solution explanation

- 'i' For loop:
- If $D = 1$ (max)
 - Apply max to c
- If $D = 0$ (min):
 - Apply max to $c - 1$

```
12  for(i = 0; i < 20; i++)
13  {
14      //num of ties for the rankings for > / >= c
15      if(d == 1)
16          num_of_ties = c;
17      else
18          num_of_ties = c - 1;
19  }
```

Solution explanation

- 'j' For loop:
- if case: diagonals = 'X'
- 1st else if case: Ties for the rankings above c
- 2nd else if case: Ties for the rankings below c
- else case: W for the max cases, L for the min cases

```
for(j = i; j < 20; j++)
{
    //diagonal is X
    if(i == j)
    {
        results[i][j] = 'X';
    }
    //have C - 1 number of ties
    else if(num_of_ties - 1 - i > 0)
    {
        results[i][j] = 'T';
        results[j][i] = 'T';
        num_of_ties--;
    }
    //for minimum, everything else is a tie
    else if(i >= num_of_ties)
    {
        results[i][j] = 'T';
        results[j][i] = 'T';
    }
    //remaining are wins
    else
    {
        results[i][j] = 'W';
        results[j][i] = 'L';
    }
}
```

Solution explanation

- Example for 5 by 5
- Input: 3 1 2 1
- For $c = 2$ and $d = 1$, number of ties needed $= c - 1 = 1$

Solution explanation

- If cases: Fill diagonal with X

X				
	X			
		X		
			X	
				X

Solution explanation

- 1st else if case: since max case, fill ties of ranks above c inclusive ($\geq c$)

X	T			
T	X			
		X		
			X	
				X

Solution explanation

- 1st else if case: since max case, fill ties of ranks above c inclusive ($\geq c$)
- Since there can be no more ties, move on to the next

X	T			
T	X			
		X		
			X	
				X

Solution explanation

- 2nd else if case: Fill up ties for all the ranks below c

X	T			
T	X			
		X	T	T
		T	X	T
		T	T	X

Solution explanation

- Else case: Fill up all the blanks in the upper left half with 'W' and the lower half with L

X	T	W	W	W
T	X	W	W	W
L	L	X	T	T
L	L	T	X	T
L	L	T	T	X

Solution explanation

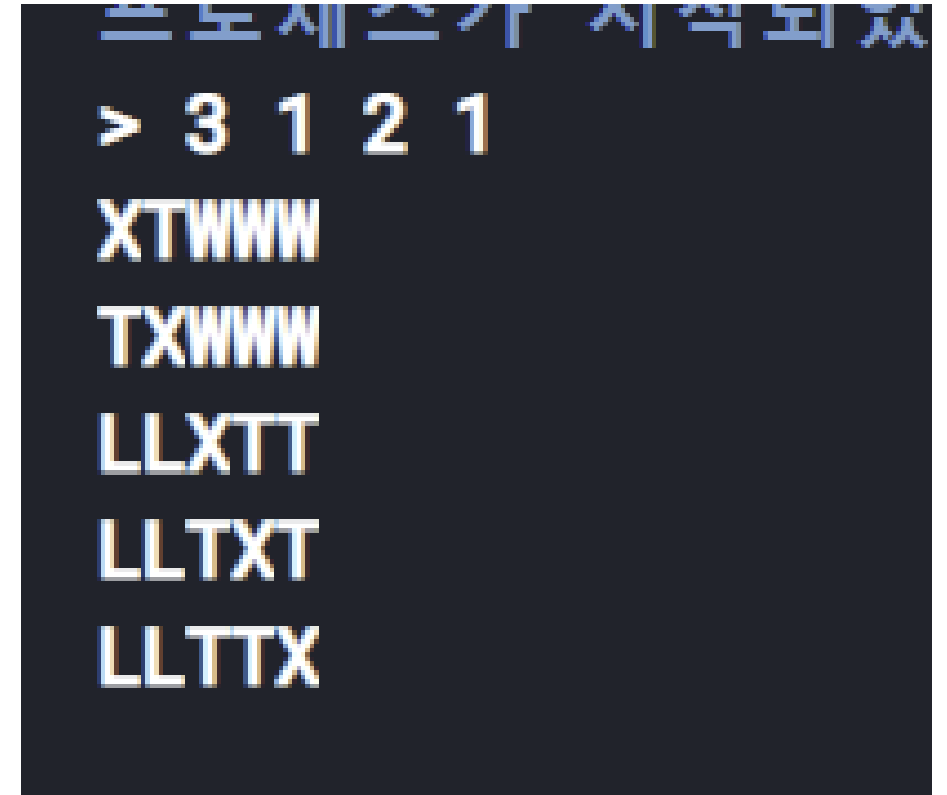
- Result Matrix

X	T	W	W	W
T	X	W	W	W
L	L	X	T	T
L	L	T	X	T
L	L	T	T	X

Solution explanation

- Result Matrix

X	T	W	W	W
T	X	W	W	W
L	L	X	T	T
L	L	T	X	T
L	L	T	T	X



Solution analysis

- Main Idea was to simplify the code by using the nested for loop for half of the matrix only
- Time Complexity: $O(n \log(n))$

Solution analysis

- Pros: reduces complexity by only solving for half of the matrix to calculate the remaining half
 - Resulting matrix is easy to interpret due to a huge tie for both max and min
- Cons: No diversity in results
 - All of the results are technically set from the beginning

Thank you!