

Name:

NOTE: This quiz is double sided! Answer the questions in the spaces provided. Show all necessary work. If you have any questions, raise your hand and I will come try to answer.

1. (20 points) In each of the following problems, compute  $\frac{dy}{dx}$ . You may have to use implicit differentiation, and/or logarithmic differentiation. There is no need to simplify.

(a) (5 points)

$$y = e^{2x} \ln(\sin x).$$

$$y' = 2e^{2x} \ln(\sin x) + e^{2x} \frac{\cos x}{\sin x}$$

(b) (5 points)

$$2y^3 + 3xy - x^5 = 40.$$

$$6y^2 y' + 3y + 3xy' - 5x^4 = 0$$

$$y'(6y^2 + 3x) = 5x^4 - 3y$$

$$y' = \frac{5x^4 - 3y}{6y^2 + 3x}$$

product rule  
misuse on  
middle term:

(-2)

forgot a  $y'$

-1

(c) (5 points)

~~Method~~  
Method 1

$$\ln y = \sin x \ln(x)$$

$$\frac{y'}{y} = \cos x \ln x + \frac{\sin x}{x}$$

$$y' = (x^{\sin x}) \left( \cos x \ln x + \frac{\sin x}{x} \right)$$

Forget to multiply by  $y$ ?

-/

$$y = x^{\sin x}$$

Method 2

$$y = e^{\ln x \sin x}$$

$$y' = e^{\ln x \sin x} \left( \cos x \ln x + \frac{\sin x}{x} \right)$$

(d) (5 points)

$$y = \tan^{-1}(\tan^{-1}(x))$$

$$y' = \frac{1}{1+(\tan^{-1}x)^2} \circ \frac{1}{1+x^2}$$

↪ not evaluated  
on inside:

-2?