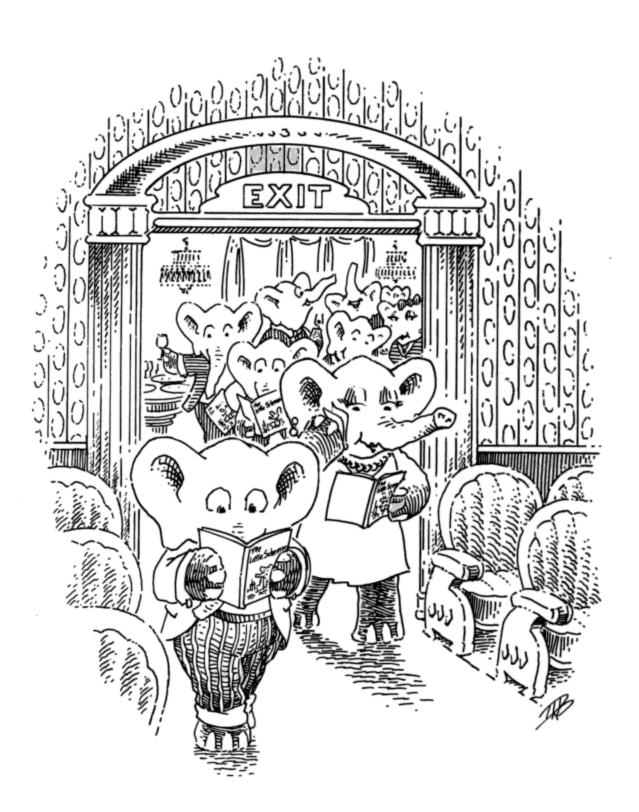
III. TOCOME BECK GO THE STHOTT



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Welcome back.	It's a pleasure.
Have you read The Little LISPer? ¹	#f.
1 Or The Little Schemer.	
Are you sure you haven't read The Little LISPer?	Well,
Do you know about Lambda the Ultimate?	#t.
Are you sure you have read that much of The Little LISPer?	Ab solutely. 1
	1 If you are familiar with recursion and know that functions are values, you may continue anyway.
Are you acquainted with member?	Sure, member? is a good friend.
(define member? (lambda (a lat) (cond ((null? lat) #f) (else (or (eq? a (car lat)) (member? a (cdr lat)))))))	
What is the value of (member? a lat) where a is sardines and lat is (Italian sardines spaghetti parsley)	#t, but this is not interesting.
What is the value of (two-in-a-row? lat) where lat is (Italian sardines spaghetti parsley)	#f.

Are two-in-a-row? and member? related? Yes, both visit each element of a list of atoms up to some point. One checks whether an atom is in a list, the other checks whether any atom occurs twice in a row. What is the value of (two-in-a-row? lat) #t. where lat is (Italian sardines sardines spaghetti parsley) What is the value of (two-in-a-row? lat) #f. where lat is (Italian sardines more sardines spaghetti) Explain precisely what two-in-a-row? does. Easy.

Is this close to what two-in-a-row? should look like?

That looks fine. The dots in the first line should be replaced by #f.

It determines whether any atom occurs

twice in a row in a list of atoms.

What should we do with the dots in the second line?

We know that there is at least one element in *lat*. We must find out whether the next element in *lat*, if there is one, is identical to this element. Doesn't this sound like we need a function to do this? Define it.

Can we now complete the definition of two-in-a-row? Yes, now we have all the pieces and we just need to put them together:

There is a different way to accomplish the same task.

We have seen this before: most functions can be defined in more than one way.

What does two-in-a-row? do when is-first? returns #f

It continues to search for two atoms in a row in the rest of *lat*.

Is it true that (*is-first? a lat*) may respond with #f for two different situations?

Yes, it returns #f when lat is empty or when the first element in the list is different from a.

In which of the two cases does it make sense for two-in-a-row? to continue the search?

In the second one only, because the rest of the list is not empty.

Should we change the definitions of two-in-a-row? and is-first? in such a way that two-in-a-row? leaves the decision of whether continuing the search is useful to the revised version of is-first?

That's an interesting idea.

Here is a revised version of two-in-a-row?

Can you define the function *is-first-b?* which is like *is-first?* but uses *two-in-a-row?* only when it is useful to resume the search?

That's easy. If lat is empty, the value of (is-first-b? a lat) is #f. If lat is non-empty and if (eq? (car lat) a) is not true, it determines the value of (two-in-a-row? lat).

Why do we determine the value of (two-in-a-row? lat) in is-first-b?

If *lat* contains at least one atom and if the atom is not the same as *a*, we must search for two atoms in a row in *lat*. And that's the job of *two-in-a-row?*.

When *is-first-b?* determines the value of (*two-in-a-row? lat*) what does *two-in-a-row?* actually do?

Since lat is not empty, it will request the value of (is-first-b? (car lat) (cdr lat)).

Does this mean we could write a function like *is-first-b?* that doesn't use *two-in-a-row?* at all?

Yes, we could. The new function would recur directly instead of through two-in-a-row?.

Let's use the name *two-in-a-row-b?* for the new version of *is-first-b?*

That sounds like a good name.

How would two-in-a-row-b? recur?

With (two-in-a-row-b? (car lat) (cdr lat)), because that's the way two-in-a-row? used is-first-b?, and two-in-a-row-b? is used in its place now.

So what is a when we are asked to determine the value of $(two-in-a-row-b? \ a \ lat)$

It is the atom that precedes the atoms in *lat* in the original list.

Can you fill in the dots in the following definition of two-in-a-row-b?

That's easy. It is just like *is-first?* except that we know what to do when (*car lat*) is not equal to *preceding*:

```
(define two-in-a-row-b?
(lambda (preceding lat)
(cond
((null? lat) #f)
(else (or (eq? (car lat) preceding)
(two-in-a-row-b? (car lat)
(cdr lat)))))))
```

What is the natural recursion in two-in-a-row-b?

The natural recursion is (two-in-a-row-b? (car lat) (cdr lat)).

Is this unusual?

Definitely: both arguments change even though the function asks questions about its second argument only.

Why does the first argument to two-in-a-row-b? change all the time?

As the name of the argument says, the first argument is always the atom that precedes the current *lat* in the list of atoms that *two-in-a-row?* received.

Now that we have *two-in-a-row-b?* can you define *two-in-a-row?* a final time?

Trivial:

Let's see one more time how two-in-a-row? works.

Okay.

(two-in-a-row? lat) where lat is (b d e i i a g)	This looks like a good example. Since lat is not empty, we need the value of (two-in-a-row-b? preceding lat) where preceding is b and lat is (deiiag)
(null? lat) where lat is (deiiag)	#f.
(eq? (car lat) preceding) where preceding is b and lat is (deiiag)	#f, because d is not b.
And now?	Next we need to determine the value of (two-in-a-row-b? preceding lat) where preceding is d and lat is (e i i a g).
Does it stop here?	No, it doesn't. After determining that lat is not empty and that (eq? (car lat) preceding) is not true, we must determine the value of (two-in-a-row-b? preceding lat) where preceding is e and lat is (i i a g).
Enough?	Not yet. We also need to determine the value of (two-in-a-row-b? preceding lat) where preceding is i and lat is (i a g).

And?	Now (eq? (car lat) preceding) is true because preceding is i and lat is (i a g).
So what is the value of (two-in-a-row? lat) where lat is (b d e i i a g)	#t.
Do we now understand how two-in-a-row? works?	Yes, this is clear.
What is the value of (sum-of-prefixes tup) where tup is (2 1 9 17 0)	(2 3 12 29 29).
(sum-of-prefixes tup) where tup is (1 1 1 1 1)	(1 2 3 4 5).
Should we try our usual strategy again?	We could. The function visits the elements of a tup, so it should follow the pattern for such functions: (define sum-of-prefixes (lambda (tup) (cond
What is a good replacement for the dots in the first line?	The first line is easy again. We must replace the dots with (quote ()), because we are building a list.

Then how about the second line?	The second line is the hard part.
Why?	The answer should be the sum of all the numbers that we have seen so far <i>cons</i> ed onto the natural recursion.
Let's do it!	The function does not know what all these numbers are. So we can't form the sum of the prefix.
How do we get around this?	The trick that we just saw should help.
Which trick?	Well, two-in-a-row-b? receives two arguments and one tells it something about the other.
What does two-in-a-row-b?'s first argument say about the second argument.	Easy: the first argument, preceding, always occurs just before the second argument, lat, in the original list.
So how does this help us with sum-of-prefixes	We could define sum-of-prefixes-b, which receives tup and the sum of all the numbers that precede tup in the tup that sum-of-prefixes received.
Let's do it!	(define sum-of-prefixes-b (lambda (sonssf tup) (cond ((null? tup) (quote ())) (else (cons (\(\dip \) sonssf (car tup)) (sum-of-prefixes-b (\(\dip \) sonssf (car tup)) (cdr tup)))))))
Isn't sonssf a strange name?	It is an abbreviation. Expanding it helps a lot: sum of numbers seen so far.

What is the value of (sum-of-prefixes-b sonssf tup) where sonssf is 0 and tup is (1 1 1)	Since tup is not empty, we need to determine the value of (cons 1 (sum-of-prefixes-b 1 tup)) where tup is (1 1).
And what do we do now?	We cons 2 onto the value of (sum-of-prefixes-b 2 tup) where tup is (1).
Next?	We need to remember to cons the value 3 onto (sum-of-prefixes-b 3 tup) where tup is ().
What is left to do?	We need to: a. cons 3 onto () b. cons 2 onto the result of a c. cons 1 onto the result of b. And then we are done.
Is sonssf a good name?	Yes, every natural recursion with sum-of-prefixes-b uses the sum of all the numbers preceding tup.
Define sum-of-prefixes using sum-of-prefixes-b	Obviously the first sum for sonssf must be 0: (define sum-of-prefixes (lambda (tup) (sum-of-prefixes-b 0 tup)))

The Eleventh Commandment

Use additional arguments when a function needs to know what other arguments to the function have been like so far.

Do you remember what a tup is?	A tup is a list of numbers.
Is (1 1 1 3 4 2 1 1 9 2) a tup?	Yes, because it is a list of numbers.
What is the value of (scramble tup) where tup is (1 1 1 3 4 2 1 1 9 2)	(1 1 1 1 1 4 1 1 1 9).
(scramble tup) where tup is (1 2 3 4 5 6 7 8 9)	(1 1 1 1 1 1 1 1).
(scramble tup) where tup is (1 2 3 1 2 3 4 1 8 2 10)	(1 1 1 1 1 1 1 1 2 8 2).
Have you figured out what it does yet?	It's okay if you haven't. It's kind of crazy. Here's our explanation: "The function scramble takes a non-empty tup in which no number is greater than its own index, and returns a tup of the same length. Each number in the argument is treated as a backward index from its own position to a point earlier in the tup. The result at each position is found by counting backward from the current position according to this index."
If l is $(1\ 1\ 1\ 3\ 4\ 2\ 1\ 1\ 9\ 2)$ what is the prefix of $(4\ 2\ 1\ 1\ 9\ 2)$ in l	(1 1 1 3 4), because the prefix contains the first element, too.
And if l is $(1 \ 1 \ 1 \ 3 \ 4 \ 2 \ 1 \ 1 \ 9 \ 2)$ what is the prefix of $(2 \ 1 \ 1 \ 9 \ 2)$ in l	(1 1 1 3 4 2).

Is it true that ($scramble\ tup$) must know something about the prefix for every element of tup	We said that it needs to know the entire prefix of each element so that it can use the first element of <i>tup</i> as a backward index to <i>pick</i> the corresponding number from this prefix.
Does this mean we have to define another function that does most of the work for scramble	Yes, because <i>scramble</i> needs to collect information about the prefix of each element in the same manner as <i>sum-of-prefixes</i> .
What is the difference between scramble and sum-of-prefixes	The former needs to know the actual prefix, the latter needs to know the sum of the numbers in the prefix.
What is (pick n lat) where n is 4 and lat is (4 3 1 1 1)	1.
What is $(pick \ n \ lat)$ where n is 2 and lat is $(2\ 4\ 3\ 1\ 1\ 1)$	4.
Do you remember pick from chapter 4?	If you do, have an ice cream. If you don't, here it is: (define pick (lambda (n lat) (cond ((one? n) (car lat)) (else (pick (sub1 n) (cdr lat))))))

Here is scramble-b

```
(define scramble-b

(lambda (tup rev-pre)

(cond

((null? tup) (quote ()))

(else

(cons (pick (car tup)

(cons (car tup) rev-pre))

(scramble-b (cdr tup)

(cons (car tup) rev-pre)))))))
```

A better question is: how does it work?

How do we get scramble-b started?

What does rev-pre abbreviate?

That is always the key to these functions. Apparently, *rev-pre* stands for reversed prefix.

If

tup is (1 1 1 3 4 2 1 1 9 2)
and

rev-pre is ()
what is the reversed prefix of
(cdr tup)

It is the result of consing (car tup) onto rev-pre: (1).

If
tup is (2 1 1 9 2)
and
rev-pre is (4 3 1 1 1)
what is the reversed prefix of
(1 1 9 2)
which is (cdr tup)

Since (car tup) is 2, it is (2 4 3 1 1 1).

Do we need to know what rev-pre is when tup is ()

No, because we know the result of (scramble tup rev-pre) when tup is the empty list.

How does scramble-b work? The function scramble-b receives a tup and the reverse of its proper prefix. If the tup is empty, it returns the empty list. Otherwise, it constructs the reverse of the complete prefix and uses the first element of tup as a backward index into this list. It then processes the rest of the tup and conses the two results together. How does scramble get scramble-b started? Now, it's no big deal. We just give scramble-b the tup and the empty list, which represents the reverse of the proper prefix of the tup: (define scramble (lambda (tup)(scramble-b tup (quote ())))) Let's try it. That's a good idea. The function *scramble* is an unusual Okay. example. You may want to work through it a few more times before we have a snack. Tea time. Don't eat too much. Leave some room for dinner.