Here is the function finite-lenkth which returns its argument's length, if it has one. If the argument doesn't have a length, the function returns false.

```
(define finite-lenkth

(lambda (p))

(letcc infinite

(letrec

((C (lambda (p \ q))

(cond

((same? p \ q)

(infinite #f))

((null? (q) 0)

((null? (kdr \ q)) 1)

(else

(+ (C (sl \ p) (qk \ q))

2)))))

(qk (lambda (x) (kdr (kdr \ x))))
```

 $(sl\ (\mathbf{lambda}\ (x)\ (kdr\ x))))$

(add1 (C p (kdr p))))))))

(cond

(else

((null? p) 0)

Bon appétit.

Guy's Favorite Pie

```
(define mongo
(kons (quote pie)
(kons (quote à)
(kons (quote la)
(kons (quote mode)
(quote ()))))))
(set-kdr (kdr (kdr (kdr mongo))) (kdr mongo))
```

We see you have arrived here.	Let's continue.
What is the value of (deep 6)	(((((((pizza)))))).
Here is deep again.	Yes, this is our friend.
(define deep (lambda (m)	
How did you determine the value of (deep 6)	The value is determined by answering the single question asked by deep.
What is the question asked by deep	The question is (zero? m). If deep's argument is zero, the value of (deep m) is pizza. If it is not, we need to determine the value of (deep (sub1 m)) and cons its value onto the null list.
What is the answer to (zero? 5)	Why are we doing this? We practiced this kind of thing in chapter 2.
So do you remember these questions?	Sure do.
When (deep 0) returns the value pizza, how many cons steps do we have to pick up to find out what the value of (deep 6) is?	Six.

And they are?

Simple,

we need to:

- 1. cons the pizza onto ()
- 2. cons the result of 1 onto ()
- 3. cons the result of 2 onto ()
- 4. cons the result of 3 onto ()
- 5. cons the result of 4 onto ()
- cons the result of 5 onto ().

And if *deep*'s task had been to make a mozzarella pizza, what steps would we have had to do then?

We just use mozzarella and do whatever we needed to do before:

- 1. cons the mozzarella onto ()
- 2. cons the result of 1 onto ()
- 3. cons the result of 2 onto ()
- 4. cons the result of 3 onto ()
- 5. cons the result of 4 onto ()
- 6. cons the result of 5 onto ().

How about a Neapolitan?

Perhaps we should just define the function six-layers and use it to create the pizzas we want:

But what if we had started with (deep 4)

Then we would have had to define four-layers to create these special pizzas.

That will help.	You mean what we saw isn't all there is to it?
Not even half.	Okay. Let's see more.
That's what we shall do. Here is a first layer: (define toppings)	This use of (letcc) is different from anything we have seen before. ¹
(define deepB (lambda (m) (cond ((zero? m) (letcc jump (set! toppings jump) (quote pizza))) (else (cons (deepB (sub1 m)) (quote ()))))))	1 L: This is impossible in Lisp, but Scheme can do it.
How is it different?	To begin with, the value part of (letcc) has two parts.
Have we seen this before?	Yes, (let) and (letrec) sometimes have more than one expression in the value part.
What else is different about (letcc)	We don't seem to use $jump$ the way we used hop in chapter 13.
True. What does $deepB$ do with $jump$	It seems to be remembering $jump$ in $toppings$.
What could it mean to "remember jump"?	We don't even know what jump is.
What was $deep$ when we asked for the value of $(deep 9)$	Easy: deep was the name of the function that we defined at the beginning of the chapter.

So what was hop when we asked for the value of (hop (quote ())) in chapter 13?	We said it was a compass needle. Could hop also be a function?
What would be the value of (deepB 6)	No problem: ((((((pizza)))))).
And what else would have happened?	We would have remembered <i>jump</i> , which appears to be some form of function, in <i>toppings</i> .
So what is (six-layers (quote mozzarella))	(((((((mozzarella)))))).
What would be the value of $(toppings \ e)$ where e is mozzarella	Yes, it would be ((((((mozzarella)))))).
And what about $(toppings \ e)$ where e is cake	((((((cake)))))).
(toppings (quote pizza)) would be ((((((pizza)))))) right?	After mozzarella on cake, nothing's a surprise anymore.
Just wait and see.	Why?
Let's add another layer to the cake.	Easy as pie: just cons the result onto the null list.
Like this: $(cons\ (toppings\ m)\ (quote\ ()))$ where m is cake	That should work, shouldn't it?
You couldn't possibly have known!	It doesn't. Its value would be ((((((cake)))))).

```
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```

```
Let's add three slices to the mozzarella:
                                                  ((((((mozzarella)))))), same as above. Except
   (cons
                                                  that we get mozzarella pizza instead of cake.
     (cons
       (cons (toppings (quote mozzarella))
         (quote ()))
       (quote ()))
     (quote ()))
                                                  We haven't told you yet, but here is the
Can you explain what happens?
                                                  explanation:
                                                   "Whenever we use (toppings \ m) it forgets
                                                    everything surrounding it and adds exactly
                                                    six layers of parentheses."
Suppose we had started with (deep B 4)
                                                  Then toppings would be like the function
                                                  four-layers but it would still forget.
                                                  Yes!
That means
   (cons
     (cons
       (cons (toppings (quote mozzarella))
         (quote ()))
       (quote ()))
     (quote ()))
would be ((((mozzarella))))
```

The Twentieth Commandment

When thinking about a value created with (letcc ...), write down the function that is equivalent but does not forget. Then, when you use it, remember to forget.

```
What would be the value of ((((cake))), no? (cons (toppings (quote cake)) (toppings (quote cake)))
```

```
And what is the value of
                                                  (((((((pizza)))))).
  (deep\&co\ 6\ (lambda\ (x)\ x))
(deep\&co\ 2\ (lambda\ (x)\ x))
                                                  ((pizza)), of course.
And how do we get there?
                                                  We ask (zero? 2), which isn't true, and then
                                                  determine the value of
                                                     (deep&co 1
                                                       (lambda (x))
                                                          (k (cons x
                                                               (quote ())))))
                                                  where
                                                    k is (lambda (x) x).
How do we do that?
                                                  We check whether the first argument is 0
                                                  again, and since it still isn't, we recur with
                                                     (deep&co 0
                                                        (lambda (x)
                                                          (k (cons x
                                                               (quote ())))))
                                                  where
                                                     k is (lambda (x)
                                                            (k2 (cons x)
                                                                  (quote ()))))
                                                  and
                                                     k2 is (lambda (x) x).
Is there a better way to describe the
                                                  Yes, it is equivalent to two-layers.
collector?
                                                    (define two-layers
                                                      (lambda (p)
                                                        (cons
                                                           (cons \ p \ (quote \ ()))
                                                           (quote ()))))
```

Why? We can replace k2 with (lambda (x) x), which shows that k is the same as (lambda (x)) $(cons \ x \ (quote \ ()))).$ And then we can replace k with this new function. Are we done now? Yes, we just use two-layers on pizza because the first argument is 0, and doing so gives ((pizza)). What is the last collector when we determine When the first argument for deep&co finally the value of $(deep\&co\ 6\ (lambda\ (x)\ x))$ reaches 0, the collector is the same function as six-layers. And what is the last collector when we four-layers. determine the value of (deep & co 4 (lambda (x) x))

And now take a close look at the function deep&coB

This function remembers the collector in *toppings*.

```
 \begin{array}{c} (\textbf{define} \ deep\&coB \\ (\textbf{lambda} \ (m \ k) \\ (\textbf{cond} \\ \quad & ((\textit{zero?} \ m) \\ \quad & (\textbf{let} \ () \\ \quad & (\textbf{set!} \ toppings \ k) \\ \quad & (k \ (\textbf{quote} \ pizza)))) \\ (\textbf{else} \\ \quad & (\textit{deep\&coB} \ (\textit{sub1} \ m) \\ \quad & (\textbf{lambda} \ (x) \\ \quad & (k \ (\textit{cons} \ x \ (\textbf{quote} \ ()))))))))) \end{array}
```

```
It is
What is toppings after we determine the
value of (deep\&coB \ 2 \ (lambda \ (x) \ x))
                                                      (lambda (x)
                                                        (k (cons x)
                                                             (quote ()))))
                                                   where
                                                      k is (lambda (x))
                                                             (k2 (cons x)
                                                                   (quote ()))))
                                                   and
                                                     k2 is (lambda (x) x).
So what is it?
                                                   It is two-layers.
And what is toppings after we determine the
                                                   It is equivalent to six-layers.
value of (deep\&coB \ 6 \ (lambda \ (x) \ x))
What is the value of
                                                   ((((pizza)))).
  (deep\&coB 4 (lambda (x) x))
                                                   It is just like four-layers.
What is toppings
Does this mean that the final collector is
                                                   Yes, it is a shadow of the value that
                                                   (letcc ...) creates.
related to the function that is equivalent to
the one created with (letcc...) in deepB
What would be the value of
                                                   (((((cake)))) (((cake)))), not (((cake)))).
   (cons (toppings (quote cake))
     (toppings (quote cake)))
Yes, this version of toppings would not forget
                                                   (((((cake)))) ((((mozzarella)))) ((((pizza))))).
everything. What would be the value of
   (cons (toppings (quote cake))
     (cons (toppings (quote mozzarella))
       (cons (toppings (quote pizza))
          (quote ()))))
```

Beware of shadows!

That's correct: shadows are close to the real thing, but we should not forget the difference between them and the real thing.

Do you remember the function two-in-a-row? Sure, we defined it in chapter 11.

What is the value of (two-in-a-row? lat) #f.

where

lat is (mozzarella cake mozzarella)

#f.

What is the value of (two-in-a-row? lat) #f.

Here is our original definition of two-in-a-row?

lat is (mozzarella mozzarella pizza)

Sure, and here is the better version from chapter 12:

Explain what two-in-a-row? does.

Easy,

it determines whether any atom occurs twice in a row in a list of atoms.

Are we going to think about "stars"?
#f.
#t.
#f.
#t.
Here are our words: "The function two-in-a-row*? processes a list of S-expressions and checks whether any atom occurs twice in a row, regardless of parentheses."
We haven't seen walk yet.

Here is the definition of walk

```
(define leave)
```

Have we seen something like this before?

Yes, walk is the minor function lm in leftmost.

And what does lm do?

It searches a list of S-expressions from left to right for the first atom and then gives this atom to a value created by (letcc...).

So, what would be the value of $(walk \ l)$ where

l is ((potato) (chips (chips (with))) fish)

If *leave* is a magnetic needle like *skip*, *walk* uses it on the leftmost atom.

Does this mean walk is like leftmost if we put the right kind of value into leave

Yes!

What would be the value of $(start-it \ l)$ where

l is ((potato) (chips (chips (with))) fish)
and the definition for start-it is

```
(define start-it
(lambda (l)
(letcc here
(set! leave here)
(walk l))))
```

Okay, now leave would be a needle!

Why?	Because <i>start-it</i> first sets up a North Pole and then remembers it in <i>leave</i> . When we finally get to (<i>leave</i> (<i>car l</i>)), <i>leave</i> is a needle that is attracted to the North Pole in <i>start-it</i> .
What would be the value of leave	It would be a function that does whatever is left to do after the value of (start-it l) is determined.
And what would be the value of (start-it l)	It would be potato.
Can you explain how to determine the value of $(start-it\ l)$	Your words could be: "The function start-it sets up a North Pole in here, remembers it in leave, and then determines the value of (walk l). The function walk crawls over l from left to right until it finds an atom and then uses leave to return that atom as the value of (start-it l)."
Write the function waddle which is like walk except for two small things.	What things?
First, if $(leave\ (car\ l))$ ever has a value, waddle should look at the elements in $(cdr\ l)$	That's easy: we just add (waddle (cdr l)) after (leave (car l)), ordering the two steps using (let ()): (let () (leave (car l)) (waddle (cdr l))) But why would we want to do this? We know that leave always forgets.
Because of our second change.	And that is?

Second, before determining the value of (leave (car l)) the function waddle should remember in fill what is left to do.

This is similar to what we did with deepB.

(define fill)

Is it now possible that $(leave\ (car\ l))$ yields a value?

No, not really! But something similar may occur: if *fill* is ever used, it will restart waddle.

donuts, of course.

```
(define start-it2
(lambda (l)
(letcc here
(set! leave here)
(waddle l))))
```

But?

In addition, waddle would remember rest in fill.

What is rest	It is a needle, just as $jump$ in $deepB$.
Didn't we say that <i>jump</i> would be like a function?	Yes, it would have been like a function, but when used, it would have also forgotten what to do afterward.
What kind of function does rest correspond to?	If rest is to waddle what jump is to deepB, the function ignores its argument and then it acts like waddle for the rest of the list until it encounters the next atom.
Why does this function ignore its argument?	Because the new North Pole creates a function that remembers the rest of what waddle has to do after (letcc) produces a value. Since the value of the first expression in the body of (let ()) is ignored, the function throws away the value of the argument.
What does the function do afterward?	It looks for the first atom in the rest of the list and then uses <i>leave</i> on it. It also remembers what is left to do.
What is the rest of the list?	Since <i>l</i> is ((donuts)

Can you define the function that corresponds No problem: to rest (define rest1 (lambda (x))(waddle l1))) where l1 is (() (cheerios (cheerios (spaghettios))) donuts). Was this really no problem? Well, x is never used but that's no problem. What would be the value of The value would be cheerios. (get-next (quote go)) where (define get-next (lambda (x)(letcc here-again (set! leave here-again) (fill (quote go))))) Why? Because fill is like rest1, except that it forgets what to do. Since (rest1 (quote go)) would eventually determine the value of (leave (quote cheerios)), and since leave is just the North Pole here-again, the result of (get-next (quote go)) would be just cheerios. And what else would have happened? Well, fill would now remember a new needle. And what would this needle correspond to? It would have corresponded to a function like rest1, except that the rest of the list would have been smaller.

Define this function.	(define rest2 (lambda (x) (waddle l2))) where l2 is (((cheerios (spaghettios))) donuts).
Does get-next deserve its name?	Yes, it sets up a new North Pole for fill to return the next atom to.
What else does it do?	Just before fill determines the next atom in the list of S-expressions that was given to start-it2, it changes itself so that it can resume the search for the next atom when used again.
Does this mean that the value of (get-next (quote go)) would be cheerios again?	Yes, if after determining the first value of (get-next (quote go)) we asked for the value again, we would again receive cheerios, because the original list was ((donuts)
And if we were to determine the value of (get-next ¹ (quote go)) a third time, what would we get?	spaghettios, because the next atom in the list is spaghettios.
¹ This is not a mathematical function.	
Let's imagine we asked (get-next (quote go)) for a fourth time.	donuts.
Last time: (get-next (quote go))	Wow!

and the second s	
Wow, what?	Since donuts is the very last atom in l , waddle finally reaches $(null?\ l)$ where l is ().
And then?	Well, the final value is ().
What is so bad about that?	If we had done all of what we intended to do we would be back where we originally asked what the value of (start-it2 l) would be where l was ((donuts)
And from there on?	Heaven knows what would happen. Perhaps it was a good thing that we always asked "what would be the value of" instead of "what is the value of."
Why would it get back to start-it2	Once the original input list to waddle is completely exhausted, it returns a value without using any needle. In turn, start-it2 returns this value, too.
What should happen instead?	If get-next really deserves its name, it should return (), so that we know that the list is completely exhausted.
But didn't we say that get-next deserved its name?	We did and it does most of the time. Indeed, with the exception of the very last case, when the original input list is exhausted, get-next works exactly as expected.
Does this mean that start-it2 would deserve the name get-first	No, it wouldn't. It does get the first atom, but later it also returns () when everything is over.

Is it also true that waddle doesn't use leave to return ()	Yes, it is.
And is it true that using (leave (quote ())) after the list is exhausted would help things?	Yes, it would: if <i>leave</i> were used, then get-next would return () eventually, and we would know that the list was exhausted.
Does get-first deserve its name:	Yes!
(define get-first (lambda (l) (letcc here (set! leave here) (waddle l) (leave (quote ())))))	
Does $(get\text{-}first\ l)$ return () when l doesn't contain an atom?	Yes!
And does get-next deserve its name?	Yes!
Does (get-next (quote go)) return () when the latest argument of get-first didn't contain an atom?	Yes!
$(get ext{-}first\ l)$ where l is $(donut)$	donut.
(get-next (quote go))	().
What would (get-first l) be where l was (fish (chips))	fish.

Why does two-in-a-row-b*? check whether n is an atom?

Returning (), a non-atom, is get-next's way of saying that there are no more atoms in l.

Didn't we forget The Thirteenth Commandment?

That's easy to fix, and since *get-first* is only used once, we can get rid of it, too:

```
(define two-in-a-row*?
  (letrec
     ((T_{\cdot}^{Q}(\mathbf{lambda}(a)))
             (let ((n (get-next 0)))
               (if (atom? n)
                   (or (eq? n \ a)
                     (T? n)
                   #f))))
      (qet-next
        (\mathbf{lambda}\ (x))
          (letcc here-again
             (set! leave here-again)
             (fill (quote go)))))
      (fill (lambda (x) x))
      (waddle
        (lambda (l)
          (cond
             ((null? l) (quote ()))
             ((atom? (car l))
              (let ()
                (letcc rest
                  (set! fill rest)
                  (leave (car l)))
                (waddle (cdr l))))
             (else (let ()
                     (waddle (car l))
                     (waddle\ (cdr\ l)))))))
      (leave\ (lambda\ (x)\ x)))
    (lambda (l)
      (let ((fst (letcc here
                    (set! leave here)
                    (waddle 1)
                    (leave (quote ())))))
         (if (atom? fst) (T? fst) #f)))))
```