

Expectation Argument

Lemma

Let X be a random variable on a discrete space S such that $E(X) = \mu$. Then $\Pr[X \geq \mu] > 0$ and $\Pr[X \leq \mu] > 0$.

Max cut

```
Data: graph  $G = \langle V, E \rangle$   
foreach vertex  $v \in V$  do  
    | Assign  $v$  to A or to B with probability  $1/2$   
return (A, B)
```

Lemma 1 (to prove)

The expected value of the number of edges in the cut (A, B) is at least $m/2$

Lemma 2 (to prove)

The probability that the cut (A, B) has at least $m/2$ edges is $\geq \frac{1}{m/2+1}$

Sample and modifying

Lemma 1 (to prove)

Let $G = \langle V, E \rangle$ be a undirected graph. Then $G = \langle V, E \rangle$ has an independent set with at least $\frac{n^2}{4m}$ vertices.

Hint 1: $d = \frac{2m}{n}$ is the average degree.

Hint 2: the proof is a probabilistic algorithm

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