



Technische Universität München Department of Mathematics

The tumthesis Class

A Tutorial for Theses

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I hereby confirm that this is my own work, and that I used only the cited sources and materials.
München, January 13, 2021
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Abstract

Here we give a short summary of the project or thesis of length at most a quarter of a page. This could be e.g. as follows:

This document is an introduction to the use of the LATEX-package tumthesis.cls, with which theses can be written in the TUM style. The basic structure of the example files is explained and some optional components are mentioned briefly. There are also some tips for LATEX beginners (and also for more advanced users who want to learn some more) as well as suggested reading for individual study.

Zusammenfassung

Hier schreibt man eine kurze Zusammenfassung der Arbeit im Umfang von maximal einer Viertelseite. Das kann z. B. so aussehen:

Die Arbeit führt in die Verwendung des LATEX-Pakets tumthesis.cls ein, mit dem Abschlussarbeiten im TUM-Stil gesetzt werden können. Die grundlegende Gliederung der Beispieldateien wird erklärt und auf optionale Bestandteile wird kurz eingangen. Außerdem enthält der Text ein paar Tipps für LATEX-Anfänger (und auch für Fortgeschrittene, die noch etwas dazulernen wollen) sowie Literaturhinweise zum Selbststudium.

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Chapter 1

Introduction

This chapter provides a short example of the use of the tumthesis class.

1.1 Files

Table 1.1 shows all the files associated with this example, each with a short description.

File name	Description
tumthesis.cls	class file, defines basic commands and incorporates important packages
tumcolors.sty	IATEX package in which the official TUM colours and logos are defined; used by tumthesis.cls.
thesis.tex	Main file of this example and starting point for own project. All other .tex files are included using this file.
thesis.pdf	PDF version of thesis.tex
preamble.tex	Preamble loading custom packages of user
abstract.tex	Abstract text in English and German
introduction.tex	Text for this chapter
conclusion.tex	Text for the following chapter
appendix.tex	Text for the appendix
thesis.bib	BibTeX file for the bibliography
TopMath-Bildmotiv.jpg	TopMath Logo for the title page

Table 1.1: Files for this example

The following commands should be used to to compile the final pdf from these source files:

```
pdflatex thesis
biber thesis
makeindex -s myindex.ist
pdflatex thesis
```

pdflatex thesis

The first run-through of pdflatex creates various auxiliary files and a (mostly complete) pdf output – some graphics may appear in the wrong place and the references and citations do not yet work correctly. With the biber command, the system works through the thesis.bib file and creates the bibliography (c.f. Section 1.7.2), while the makeindex command creates the index (c.f. Section 1.8.1). The subsequent two pdflatex commands set references and place graphics correctly.

Advanced users can also automise the process by using the command

```
latexmk --pdf thesis
```

The latexmk tool then ensures each command in the BibTEX runthrough is called the correct number of times.

1.2 Configuration and Options

Custom packages of the user or overwritten settings can be loaded in file preamble.tex. The code contained in this file will be included and executed right at the end of the class (just before loading the last packages hyperref and cleveref).

The tumthesis class accepts some options, that help to adjust the titlepage and some behaviour:

• topmath: This option places the "TopMath-Bildmotiv" on the titlepage:

\documentclass[topmath]{tumthesis}

Alternatively, you can place your own logo on the titlepage:

- titlepicture: Filename of your logo
- titlepictureX: Horizontal distance (including unit) between lower right corner of the titlepage and lower right corner of the logo
- titlepictureY: Vertical distance (including unit) between lower right corner of the titlepage and lower right corner of the logo

```
\documentclass[titlepicture=MA_CMYK.pdf,titlepictureX=25mm,titlepictureY=40mm]{tumthesis}
```

would include the math logo once again in the lower right corner of the titlepage.

Furthermore, you can adjust the behaviour of theorems' titles:

• theoremtitle: Whether the content of a theorem is typeset next to its name (nobreak) or not (break, standard option)

\documentclass[theoremtitle=nobreak]{tumthesis}

A further option allows the user to specify the BibLaTeX backend to be used:

• biblatexBackend: The default is set to biber, every valid option for parameter "backend" of the biblatex package is an alternative:

\documentclass[biblatexBackend=bibtex] {tumthesis}

1.3 Basic Settings

At the very beginning, the thesis.tex file fixes some basic settings. The code is as follows:

```
% -----
 % PDF-Information
 \hypersetup{
  pdfauthor={Wolfgang Ferdinand Riedl, Michael Ritter},
5 pdftitle={The tumthesis Class},
  pdfsubject={A Tutorial for Theses},
  pdfkeywords={Master's Thesis, Bachelor's Thesis},
  colorlinks=true, %coloured links (for the PDF version)
 % colorlinks=false, % no coloured links (for the print version)
10 }
 % -----
 % Basisdaten
 \author{Wolfgang F. Riedl, Michael Ritter}
 \title{The \texttt{tumthesis} Class}
 \subtitle{A Tutorial for Theses}
 \faculty{Fakultät für Mathematik}
20 \institute{Lehrstuhl für Angewandte Geometrie und Diskrete ←
    \hookrightarrow Mathematik}
 %\subject{master}
 %\subject{bachelor}
 %\subject{diploma}
 %\subject{project}
25 %\subject{seminar}
 %\subject{idp}
 \subject{Short Overview}
```

```
\professor{Prof. Dr. Peter Gritzmann} %Themensteller \advisor{Dr. René Brandenberg} %Betreuer 30 \date{26.12.2012} %Submission Date \place{München} %Place where document is signed
```

The inputs in the hypersetup command do not appear in the document itself, but are embedded into the pdf file as metadata and can be viewed in Acrobat Reader (and many other pdf-viewers). The remaining commands should be largely self-explanatory. The subject{} command accepts any desired text as input (such as "Short Overview" in this example), or you may use one of the pre-defined key words, which automatically create a title of "Master's Thesis", "Bachelor's Thesis" or other suitable output. To do this, simply remove the commentary marks from the appropriate line and comment out the currently active subject command. Be careful, of course, to match the selected language (see Section 1.4). (The \subject{} can also be omitted entirely, in which case there will be no designation on the title page and only the author name will appear.)

1.4 Language selection und Character set

The class supports English and German as language options. The language is set using the command

```
\selectlanguage{english}
```

at the start of thesis.tex. The language can be changed at any point in the document using this command or respectively \selectlanguage{ngerman}. This also means that some settings are automatically changed to match, e.g. the commands \eg and \ie result in the appropriate text (these commands should be used in any case, since they ensure that the spacing is typographically correct) and the headings change, but there are also some more subtle changes such as the rules for automatic hyphenation. An example of such a language switch can be found in the abstract.

For your own files it is important to select the correct "encoding". Here the default is Unicode (UTF-8). This allows you to type in umlauts and other special characters directly, but may require the correct settings in the editing programme. Some editors, especially in Windows systems, are set to Latin-1 rather than Unicode – this can lead to interesting errors!

1.5 Printing

When printing, be sure to print the thesis double-sided. The side margins, headers and footers are set out for double-sided printing and binding. If you want to change the space left for binding simply adjust the line

```
BCOR =5 mm % Binding correction , ensures sufficient space \hookrightarrow for binding
```

in file tumthesis.cls.

1.6 Titlepage

Per default, the titlepage is set to a standard titlepage following the TUM-Styleguide as close as possible. By replacing line

\maketitlepage%

in the file thesis.tex with

\maketitlepageDissertation%

a titlepage suitable for a dissertation is created.

1.7 Important notes

1.7.1 Math Environments

As this class loads the package ntheorem, math environments of the following form lead to errors: \[... \]. Replace them by \begin{equation*} ... \end{equation*} instead.

1.7.2 Biblatex

he package currently uses the biber backend which can handle UTF-8 encoded bibliography files. This default option can be changed by the parameter biblatexBackend as described above.

You can find manuals for the setup of your LATEXeditor with biber for most editors by searching the web.

1.8 Some Packages

The tumthesis.cls class includes a range of useful packages, which are listed below.

1.8.1 Index

The tumthesis style file loads the package imakeidx, which allows quick and easy generation of an *index*. To include a word or definition the index, simply append \index{keyword}. For example, the keyword "index" is added to the index of this document in the following way:

```
... easy generation of an \emph{index}\index{index}. To ...
```

Adding symbols is just as easy: The symbol ζ is included in the index by the line

```
... the symbol \z eta \in {\xi} index {\xi} is included ...
```

To change the position of the symbols (or any other elements) in your index, you can specify an additional keyword (which may also be a formula):

To include the symbol π in the index such that it appears in the place where the word "pi" would appear and also in the place where the symbol " p_i " would appear, you can use the code

```
... symbol \pi \simeq {pi@\$\pi} \in {pi@\$\pi}  is \cap included ...
```

Subcategories can also easily be realized, by using \index{keyword!subkeyword}: For example, the definition of a metric space

Definition 1.1 (Metric)

Let X be a set and $d: X \times X \longrightarrow \mathbb{R}$. The function d is a metric on X if the following three properties hold for all $x, y, z \in X$

```
1. d(x,x) \ge 0 and d(x,y) = 0 \iff x = y (non-negativity)
```

```
2. d(x,y) = d(y,x) (symmetry)
```

```
3. d(x,z) \le d(x,y) + d(y,z) (triangle inequality).
```

can be properly referenced in the index by the following code:

```
\begin{definition}[Metric]
  \index{metric}
  Let XX be a set and A: X \times X \to X
     \hookrightarrow \mathbb{R}\$. The function \$d\$ is a metric on \$X\$ if \curvearrowright
     \hookrightarrow the following three properties hold for all $x,y,z \in \curvearrowright
     \hookrightarrow X$
  \begin{enumerate}
    \item d(x,x) \neq 0 and d(x,y) = 0 \in x = y
       \forall x \in  d(x,y) = d(y,x)  (symmetry) \forall x \in  d(x,y) = d(y,x) 
    \item d(x,z) \leq d(x,y) + d(y,z) (triangle \curvearrowright
       \hookrightarrow inequality)\index{metric!triangle inequality}.
  \end{enumerate}
\end{definition}
 To create the index, the line
  \makeindex[title=Index,options=-s myindex]
```

has to be added to the file thesis.tex before the \begin{document} command! The option title=Index specifies the heading of the index, in this case "Index"; the second option sets a custom style file (does not work in any environment, see compiler options below if it does not work).

The index can then be added to the document by the command

```
%Add the index to the table of contents
\addcontentsline{toc}{chapter}{Index}
%print the index
\printindex
```

The index has to be compiled by the command makeindex (which most editors will apply automatically). The layout of the index can be modified by specifing a style file via the option -s stylefile.ist (or sometimes the option given to the \makeindex command above). This document was compiled using the file myindex.ist, which is included in the package.

1.8.2 scrbook

The tumthesis.cls class builds entirely on scrbook.cls. In particular, this means that all of the options and commands in scrbook are available here. More information can be found in the documentation [KohmMorawski2012] or in the printed version KohmMorawski2012b.

1.8.3 csquotes

Among other things, this package makes the \enquote{} command available, which automatically ensures that quotation marks are correct. The package takes account of the currently active language: in English text "English quotation marks" appear, wobei deutsche Texte "entsprechende Anführungszeichen" bekommen.

1.8.4 cleveref

In LATEX we normally make references using \ref{}. This package defines the new commands \cref and \Cref, which ensure that as well as the correct number, the correct descriptive text also appears (in the currently selected language). The latter command also ensures capitalisation and should therefore be used at the beginning of a sentence (although in German this often makes no difference, since labels are usually nouns, which are capitalised in any case). An example can be found above and also here: The references to Table 1.1 are made using cleveref, the word "Table" is included automatically.

1.8.5 ntheorem

This package prepares a range of standard environments for definitions, theorems, proofs etc. The labels are determined by the language. For example:

Definition 1.2

Every element of a vector space is called a *vector*.

Theorem 1.3 (Fundamental theorem of vector space terminology) For every vector v there is a vector space V with $v \in V$.

Proof. The proof is trivial and is left as an exercise for the reader. It is really not hard, just try it. \Box

Wir zeigen jetzt eine deutsche Version dieses Beweises:

Beweis. Der Beweis von Theorem 1.3 ist höchst trivial und nur ein Vollidiot würde es nicht selber können. Wenn Sie sich überhaupt die Mühe gemacht haben, diesen Beweis zu lesen, überlegen sie sich vielleicht, ob Sie nicht lieber ein anderes Fach studieren sollten.

We formulate another theorem in order to demonstrate another feature of $\tt cref$ with which one may group several references together. To this end, we reference Theorems 1.3 and 1.4

Theorem 1.4 LATEX is great!

The environment can of course be extended and customised. For more information, see the examples in tumthesis.cls or the documentation for the ntheorem package [ntheorem]. All of the pre-defined environments are listed in Table 1.2.

1.8.6 booktabs

This package allows for nicer tables, such as Table 1.1. There are many tips on setting out tables in the extensive documentation for this package.

1.8.7 tabularx

A tabular modifying the width of certain columns in order to achieve a custom width can be constructed using package tabularx.

Environment	Text	
	English	German
definition	Definition	Definition
theorem	Theorem	Satz
satz	Theorem	Satz
lemma	Lemma	Lemma
proposition	Proposition	Proposition
corollary	Corollary	Korollar
korollar	Corollary	Korollar
remark	Remark	Bemerkung
bemerkung	Remark	Bemerkung
example	Example	Beispiel
beispiel	Example	Beispiel
proof	Proof	Beweis
beweis	Proof	Beweis
conjecture	Vermutung	Conjecture
vermutung	Vermutung	Conjecture
problem	Problem	problem

Table 1.2: predefined ntheorem environments

1.8.8 TikZ

TikZ may not be a graphics program, but you can still create some excellent graphics with it. The documentation [Tantau2007] is extensive. Online under http://www.texample.net are a number of examples which demonstrate what you can do with this package. Lest the list of figures remain empty, we include a TikZ graphic in Fig. 1.1a. Fear not, you do not have to understand the code straight away. There are some simpler and well-described examples in the TikZ manual.

1.8.9 subcaption

To create multiple subfigures within a figure, you can use the package **subcaption** and its environment **\begin{subfigure}** ... **\end{subfigure}**. It gives the opportunity to create subfigures and subtables using the same syntax as used for figures and tables.

1.8.10 fixme

This package allows you to make notes in your document which mark points where more work is needed. A "List of Corrections" then appears at the very end of the document, in which all the notes are listed. To demonstrate, this paragraph contains two such

FiXme Note!

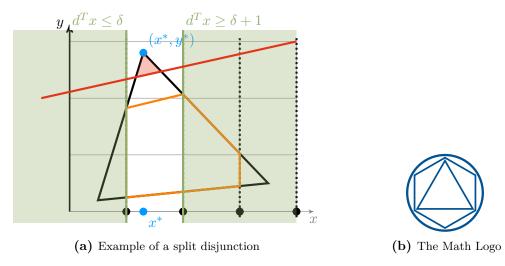


Figure 1.1: Two graphics

FiXme Note!

FixMe notes—these appear as notes at the side, but also in the aforementioned "List of Corrections" at the very end of the document. Here also there are many possible settings and the *documentation* is recommended reading. We mention here one setting which should appear at the beginning of the thesis.tex file:

```
%FixMe-Status: final (no FixMe notes) or draft (notes visible)
\fxsetup{draft}
%\fxsetup{final}
```

Replacing the "draft" line with the "final" line will result in two things: All \fxfatal{} commands will become LaTeXerrors which break off the TeXcompilation of the document (useful for highlighting really bad mistakes which should definitely not be overlooked). All other fixme commands (i.e. \fxnote{}, \fxwarning{}, \fxerror{}) will simply become invisible, the notes in the text and the "List of Corrections" at the end of the document disappear. More information on the available commands and the many possible settings can be found in the documentation [fixme].

1.8.11 hyperref

The hyperref package fixes a number of pdf settings (see Section 1.3). Furthermore, the package ensures that all references, citations and the table of contents become clickable links which allow the reader to jump back and forth in the document. By default these links appear in black and are therefore not immediately visible. Alternatively with the colorlinks=true setting in the \hypersetup{} command at the beginning of the document, these links become dark blue. This is convenient for the on-screen version; however for the print version you should revert to black, i. e. use the option

colorlinks=false (after all, you can't click on links in the printed document).

```
hypersetup{
  pdfauthor={Wolfgang Ferdinand Riedl, Michael Ritter},
  pdftitle={The tumthesis Class},
  pdfsubject={A Tutorial for Theses},
  pdfkeywords={Master's Thesis, Bachelor's Thesis},
  colorlinks=true, %coloured links (for the PDF version)
% colorlinks=false, % no coloured links (for the print version)
}
```

1.8.12 listings

The listings package allows you to produce nicely formatted source code listings. In this example it is used to produce LATEX source code. The standard settings take care of line numbering, line breaks and various other details. Of course many settings can be customised; for details see the documentation [listings]. One small warning: The package is set up to deal with umlauts and "ß" in the source texts, but other special characters may cause problems (even in comments). It is best to avoid special characters altogether in source texts—if this is not possible, take a look at tumthesis.cls to see how to modify the settings to deal with other special characters.

1.8.13 algorithm2e

algorithm2e provides the possibility to create floating algorithm environments. In contrast to listings it does not produce source code formatted according to a certain programming language, instead you write formatted pseudo-code with a predefined syntax.

1.8.14 tumcolors2

The package tumcolors2 provides a number of colors according to the TUM styleguide. It also contains commands that draw the TUM logo and the math faculty logo.

\mathlogo{width=2cm}
\mathlogo{height=2cm}
\tumlogo{width=2cm}
\tumlogo{height=2cm}





example	name	alternatives
	tumblue1 tumblue2	tumblau1, tumblue, tumblau tumblau2
	tumblue3	tumblau3
	tumblue4	tumblau4
	dark tumblue1	dunkles tumblau1, dark tumblue, dunkles tumblau
	dark tumblue2	dunkles tumblau2
	dark tumblue3	dunkles tumblau3
	dark tumblue4	dunkles tumblau4
	dark gray	dunkelgrau
	medium gray	mittelgrau
	light gray	hellgrau
	accentuating light blue	Akzent-Hellblau
	accentuating dark blue	Akzent-Dunkelblau
	accentuating ivory	Akzent-Elfenbein
	accentuating orange	Akzent-Orange
	accentuating green	Akzent-Gruen

Table 1.3: TUM colors

Chapter 2

Single bidder and single item

Single-parameter agents, i.e., agent i's valuation for receiving service is v_i and their valuation for no service is normalized to zero.

It is impossible to collect the information about the true prior of bidders valuation. In addition, it may impact on bidders' incentive and pefermance of the auction mechanism. Therefore, it is interesting to design a mechanism with less assumption on the proir distribution/with limited information of this prior. Normally we start to consider the worst case analysis.

2.1 Uniform distribution

from Myerson** for single-item settings the optimum revenue can be achieved by a deterministic mechanis by setting a price p and it becomes a single take-it-or-leave-it auction with price p, and therefore the optimal revenue is:

$$OPT(F) = \sup_{p \geqslant 0} REV(p; F) = \sup_{p \geqslant 0} p \times (1 - F(p-))$$
(2.1)

where F(p-) = Pr[x < p], we will use this calculation for optimal revenue in the following different experiments. $OPT(\cdot)$ denote Myerson optimal operator

For an uniform distribution $U[a, b], 0 \le a \le b$, we know:

- mean $\mu = \frac{b+a}{2}$ and $\sigma^2 = \frac{(b-a)^2}{12}$
- $\operatorname{cdf} F(x) = \frac{x-a}{b-a}$
- pdf $f(x) = \frac{1}{b-a}$

Using Myerson optimal operator, we can write:

$$OPT(F) = \sup_{p \ge 0} REV(p; F) = \sup_{p \ge 0} p \times \left(1 - \frac{p - a}{b - a}\right)$$

We can find the optimal revenue by maximizing expected revenue $p \times (1 - \frac{p-a}{b-a})$, take first derivative and set it to 0, we compute that when $p_{opt} = max\{a, \frac{b}{2}\}$, it reaches maximum value, and we have $\mathrm{OPT}(F) = p_{opt} \times (1 - \frac{p_{opt} - a}{b-a})$

From paper Robust**, we can compute the deterministic robust approximation ratio ρ_D by solving following equation:

$$\frac{(\rho_D - 1)^3}{(2\rho_D - 1)^2} = r^2 \tag{2.2}$$

where $r = \frac{\sigma}{u}$ is called *coefficient of variation (CV)*. If we look at the right hand side expression $\frac{(\rho_D - 1)^3}{(2\rho_D - 1)^2}$ is increasing and goes from 0 at $\rho_D = 1$ to ∞ at $\rho_d \to \infty$, so that for any nonegative r there is a unique solution $\rho_D \in [1, \infty)$ to the above equation. Using this ratio, we can determine the *take-it-or-leave-it price of* $p = \frac{\rho_D(r)}{2\rho_D(r) - 1} \cdot \mu$.

For a given uniform distribution, i.e. a and b are known, therefore r^2 is also known: $r^2 = (\frac{\sigma}{u})^2 = \frac{(b-a)^2}{3(b+a)^2}$, then we can solve equation (2.2) and compute reserve price proposed by Robust paper, we denote this price as p_r . As we can see, the expected revenue when set price p_r is equal to REV = $p_r \times (1 - \frac{p_r - a}{b - a})$ we can indeed find the DAPX explicitly

2.1.1 Design of experiment

Find DAPX tentatively

We first pick up an arbitrary uniform distribution, for example a=2 and b=10 and then (detailed code can be found in appendix ... or link github)

- we can compute ρ_D numerically using scientific package in python fsolve**(explain what method this function used to solve nonlinear functions) function from scipy. Then substitude it into above equation to compute reserve price p_r .
- Run an auction n times (n can be a large number, i.e.10000000), for each auction, generate a random number x (bid) from U[a,b], compare it against p_r . If the bid bits price p_r , then the bidder wins this auction and the revenue of this auction is p_r
- We sum up the revenue for all the winning auctions and then take average $(expected_revenue = \frac{total_revenue}{n})$

Although we know the exact optimal revenue for this auction, to be fair, we should run the above experiment with the optimal reserve price $\frac{b}{2}$. In this case, we can find our experiment result DAPX = $\frac{\text{OPT}}{\text{REV}} = \frac{\text{REV}(p = max\{a, \frac{b}{2}\})}{\text{REV}(p = \frac{\rho_D(r)}{2\rho_D(r) - 1} \cdot \mu)}$ for uniform distribution.

Example:show one Experiment

Experiment on r

Now we want to see when r changes how DAPX differs. One idea is that we can fix mean mu and gradually increase b-a, because mu if middle point between a and b, at each iteration i, a_i and b_i take a same "step" away this mu, therefore sigma increases

meanwhile r increases. Within each step, we have a new uniform distribution, we repeat above experiment for this distribution and dertermine the experiment DAPX. We save the results of DAPX and also ρ_d for each step and plot them in the same graph for comparison. As you can see Figure 0.0 below (we start $a_0 = \text{and } b_0 =$, so we have $mu = \text{and } sigma = \text{, and step size is } 0.1, \text{ and we take } 50 \text{ iterations, then } a_n = \text{and } b_n = \text{,)}$

Interesting findings

From various experimenting, we notice that no matter how we change mu and sigma, the coefficience variance r for uniform distribution is way smaller than 1. Which is expected, as uniform distribution is well defined distribution and actually indeed we can write r in terms of a and b explicitly:

$$r = \frac{b-a}{\sqrt{3}(a+b)} = \frac{a+b-2a}{\sqrt{3}(a+b)} = \frac{1}{\sqrt{3}}(1-\frac{2}{1+\frac{b}{a}})$$

when a=0. then $r=\frac{1}{\sqrt{3}}$, otherwise, when $b\to\infty$ and $a\leqslant b$, we can have:

$$\sup r = \lim_{\frac{b}{a} \to \infty} (\frac{1}{\sqrt{3}} (1 - \frac{2}{1 + \frac{b}{a}})) = \frac{1}{\sqrt{3}}$$

as we can see the CV of uniform distribution is at most $\frac{1}{\sqrt{3}}$. From equation 2.2 ρ_d is monotonically increasing with r, then $\sup \rho_d$ is achieved when $r = \frac{1}{\sqrt{3}}$, let's denote this maximum value as $\hat{\rho_d}$ (using numerical solver we can find this value is equal to 3.05937594), we know the equation of computing the reserve price, $p = \frac{\rho_D}{2\rho_D - 1} \cdot \left(\frac{a+b}{2}\right) = \frac{1}{2-\frac{1}{\rho_D}} \cdot \left(\frac{a+b}{2}\right)$ now lets write DAPX explicitly when $\frac{b}{2} \geqslant a$ so $p_{opt} = \frac{b}{2}$:

$$DAPX = \frac{OPT}{REV} = \frac{\frac{b^2}{4(b-a)}}{\frac{\rho_D}{2\rho_D - 1} \cdot \mu \cdot \left(1 - \frac{\frac{\rho_D}{2\rho_D - 1} \cdot \mu - a}{b-a}\right)}$$

simplified we get

$$DAPX = \frac{b^2}{\frac{2\rho_D}{2\rho_D - 1} \cdot 2\mu \cdot (b - \frac{\rho_D}{2\rho_D - 1} \cdot \mu)}$$

substitute $b = \sqrt{3}\sigma + \mu$

$$\begin{aligned} \text{DAPX} &= \frac{(\sqrt{3}\sigma + \mu)^2}{\frac{2\rho_D}{2\rho_D - 1} \cdot 2\mu \cdot (\sqrt{3}\sigma + \mu - \frac{\rho_D}{2\rho_D - 1} \cdot \mu)} \\ &= \frac{\mu^2 \cdot (\sqrt{3}r + 1)^2}{\frac{2\rho_D}{2\rho_D - 1} \cdot 2\mu^2 \cdot (\sqrt{3}r + 1 - \frac{\rho_D}{2\rho_D - 1})} \\ &= \frac{(\sqrt{3}r + 1)^2}{4 \cdot \frac{\rho_D}{2\rho_D - 1} \cdot (\sqrt{3}r + 1 - \frac{\rho_D}{2\rho_D - 1})} \end{aligned}$$

when $\frac{b}{2} \leqslant a$ so $p_{opt} = a$

$$\mathrm{DAPX} = \frac{\mathrm{OPT}}{\mathrm{REV}} = \frac{a}{\frac{\rho_D}{2\rho_D - 1} \cdot \mu \cdot \left(1 - \frac{\frac{\rho_D}{2\rho_D - 1} \cdot \mu - a}{b - a}\right)}$$

simplified we get

$$DAPX = \frac{a(b-a)}{\frac{\rho_D}{2\rho_D - 1} \cdot \mu \cdot (b - \frac{\rho_D}{2\rho_D - 1} \cdot \mu)}$$

substitute $b = \mu + \sqrt{3}\sigma$ and $a = \mu - \sqrt{3}\sigma$

$$\begin{aligned} \text{DAPX} &= \frac{2\sqrt{3}\sigma(\mu - \sqrt{3}\sigma)}{\frac{\rho_{D}}{2\rho_{D} - 1} \cdot \mu \cdot (\sqrt{3}\sigma + \mu - \frac{\rho_{D}}{2\rho_{D} - 1} \cdot \mu)} \\ &= \frac{\mu^{2} \cdot r(1 - \sqrt{3}r)}{\mu^{2} \cdot \frac{\rho_{D}}{2\rho_{D} - 1} \cdot (\sqrt{3}r + 1 - \frac{\rho_{D}}{2\rho_{D} - 1})} \\ &= \frac{r(1 - \sqrt{3}r)}{\frac{\rho_{D}}{2\rho_{D} - 1} \cdot (\sqrt{3}r + 1 - \frac{\rho_{D}}{2\rho_{D} - 1})} \end{aligned}$$

Below we show the plot comparing uniform distributed DAPX against ρ_D from the the paper.(show example, set a =1, change r value, since for each r there is a corresponding value of b, which is a valid uniform distribution, then we can get following plot

 $\frac{\rho_D}{2\rho_D-1} = \frac{1}{2-\frac{1}{\rho_D}}$ as $\rho_D \geqslant 1$ because optimal revenue is always greater than the expected revenue, then $\frac{\rho_D}{2\rho_D-1} \leqslant 1$. ρ_d is also a function of r, it seems that DAPX is a quadratic equation in terms of r?????? not too sure, since I cannot derive the pd using r

note: another interesting things when a uniform ditribution has $\frac{b}{a} = 2.44224957$, then DAPX = 1, by setting $p = p_{opt}$ which is equavlent to $\frac{\rho_D}{2\rho_D - 1} \cdot (\frac{a+b}{2}) = \frac{b}{2}$ then solving equation 2.2.

2.2 Exponential and Poisson distribution

This two distributions have very special property that the mean and the standard deviation are the same, which results in constant CV, for exponential distribution $r = \frac{\sigma}{\mu} = \frac{1}{\lambda} = 1$ and for poisson distribution $r = \frac{\sigma}{\mu} = \frac{\lambda}{\lambda} = 1$, therefore ρ_d is also constant by solving equation 2.2. Thus from these two distribution we cannot find a useful relation between DAPX and r.

We can still perform some insight of this type distribution, and let us look at exponential distribution for example. For any exponential distribution, we denote as $exp(\lambda)$, its mean and standard deviation are $\frac{1}{\lambda}$, then using myerson optimal operator,

we can determine the optimal reserve price is $\frac{1}{\lambda}$ and the optimal revenue is $\frac{1}{\lambda \cdot e}$. Let's denote $\hat{\rho_D}$ as the the value of ρ_D when r=1, and our expected revenue we can write as $\frac{\hat{\rho_D}}{\lambda(2\hat{\rho_D}-1)}e^{-\frac{\hat{\rho_D}}{(2\hat{\rho_D}-1)}}$, then:

$$\begin{split} \mathrm{DAPX} &= \frac{\mathrm{OPT}}{\mathrm{REV}} \\ &= \frac{\frac{1}{\lambda \cdot e}}{\frac{\rho_{\hat{D}}}{\lambda(2\rho_{\hat{D}} - 1)}} e^{-\frac{\rho_{\hat{D}}}{(2\rho_{\hat{D}}^2 - 1)}} \\ &= \frac{1}{\frac{\rho_{\hat{D}}}{(2\rho_{\hat{D}}^2 - 1)}} e^{1 - \frac{\rho_{\hat{D}}}{(2\rho_{\hat{D}}^2 - 1)}} \end{split}$$

From above result we can see DAPX is indepedent of λ , and it is a constant as well. we will not explore any futher on these two distributions.

2.3 Truncated Normal distribution

A normal distribution is defined by two parameters μ and σ . For an normal distribution $N(\mu, \sigma^2)$, it is unbounded, however normally we assume a bidder's valuation is nonnegative, therefore we need to consider a truncated normal distribution. Let's denote $f_t(x)$ and $F_t(x)$ as pdf and cdf for the truncated normal distribution $N_t(\mu, \sigma^2)$,

We can write truncated normal into following form. First we introduce following notation:

$$\xi = \frac{x-u}{\sigma}, \qquad \alpha = \frac{a-u}{\sigma}, \qquad \beta = \frac{b-u}{\sigma}, \qquad Z = \Phi(\beta) - \Phi(\alpha)$$

where $\Phi(\cdot)$ is the cumulative distribution function for standard normal distribution. a,b stands for the lower bound and upper bound for the truncated normal distribution, in our case, a=0 and $b=\infty$, thus, $\alpha=\frac{-u}{\sigma}, \beta=\infty, Z=1-\Phi(\alpha)$. Then the pdf and cdf of truncated normal distribution is:

$$f_t(x) = \frac{\phi(\xi)}{\sigma Z}$$
 and $F_t(x) = \frac{\Phi(\xi) - \Phi(\alpha)}{Z}$

where $\phi(\cdot)$ is density distribution function of standard normal distribution. To find optimal reserve price based on Myerson optimal acution, before we use Myerson optimal operator, this time we consider virtual valuation which is defined

Definition 2.3 The *virtual valuation* of bidder i with valuation v_i is

$$\phi_i(v_i) = v_i - \frac{1 - F_i(v_i)}{f_i(v_i)}$$

The optimal reserve price is set this *virtual valuation* to 0 and find the value of v. Therefore for normal distribution, the optimal reserve price $p_{opt} = \phi^{-1}(0)$, in our case, we only have one bidder, so just use v instead of v_i , then we assume v is nonnegative, thus we can write $\phi(v) = v - \frac{1 - F_t(v)}{f_t(v)}$, in the implementation we use numerical solver to solve this equation $\phi(v) = 0$ to get p_{opt} .

2.3.1 Prove of regularity

In order to use this *virtual valuation* concept, we needs to prove its regularity. And to prove $\phi(v)$ is regular we can also prove that the truncated normal distribution is a MHR distribution, because MHR implies regularity (this theory is mentioned where first). Hazard rate for truncated normal distribution is $h(v) = \frac{f_t(v)}{1 - F_t(v)}$, to prove this is monotone, we can take first derivative and see if the first derivative is nonnagative or not (here we assume $v \ge 0$):

$$h'(v) = \frac{f_t'(v)}{1 - F_t(v)} + \frac{f_t(v) \cdot F_t'(v)}{(1 - F_t(v))^2}$$
$$= \frac{f_t'(v)}{1 - F_t(v)} + \frac{f_t^2(v)}{(1 - F_t(v))^2}$$
$$= \frac{kf'(v)}{1 - F_t(v)} + \frac{f_t^2(v)}{(1 - F_t(v))^2}$$

where we know $f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}(\frac{x-u}{\sigma})^2}$ then $f'(v) = -\frac{v-u}{\sigma^2}\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}(\frac{v-u}{\sigma})^2} = -\frac{v-u}{\sigma^2}\cdot f(v)$ substitute this result into above equation, we get:

$$h'(v) = \frac{-\frac{v-u}{\sigma^2} \cdot f_t(v)}{1 - F_t(v)} + \frac{f_t^2(v)}{(1 - F_t(v))^2}$$
$$= \frac{-\frac{v-u}{\sigma^2} \cdot f_t(v)(1 - F_t(v)) + f_t^2(v)}{(1 - F_t(v))^2}$$

Now we only need to prove the dominator is non-negative or not, and then we substitute the pdf and cdf funtion, in this case, we set $\xi = \frac{v - \mu}{\sigma}$.

$$-\frac{v-u}{\sigma^2} \cdot f_t(v)(1-F_t(v)) + f_t^2(v) = -\frac{\xi}{\sigma} \frac{\phi(\xi)}{\sigma Z} \left(1 - \frac{\Phi(\xi) - \Phi(\alpha)}{Z}\right) + \frac{\phi(\xi)^2}{\sigma^2 Z^2}$$

$$= -\frac{\xi}{\sigma} \frac{\phi(\xi)}{\sigma Z} \left(\frac{1 - \Phi(\alpha) - \Phi(\xi) + \Phi(\alpha)}{Z}\right) + \frac{\phi(\xi)^2}{\sigma^2 Z^2}$$

$$= -\frac{\xi \phi(\xi)}{\sigma^2 Z^2} (1 - \Phi(\xi)) + \frac{\phi(\xi)^2}{\sigma^2 Z^2}$$

$$= \frac{-\xi \phi(\xi) (1 - \Phi(\xi)) + \phi(\xi)^2}{\sigma^2 Z^2}$$

Again we get nonnegative denominator, so we can just check the sign of nominator. We consider it into two cases:

- Case 1: if $v \leq \mu$ then $-\xi \geq 0$, we know $\phi(\xi), 1 \Phi(\xi)$ is nonnegative, then $-\xi \phi(\xi) (1 \Phi(\xi)) + \phi(\xi)^2$ is nonnegative
- Case 2: if $v > \mu$ then $\xi > 0$, We know that Q-funtion is defined as $Q(\xi) = 1 \Phi(\xi)$, and it has two bounds when $\xi > 0$, $\left(\frac{\xi}{1+\xi^2}\right)\phi(\xi) < Q(\xi) < \frac{\phi(\xi)}{\xi}$, thus $-\xi\phi(\xi)\left(1-\Phi(\xi)\right) = -\xi\phi(\xi)Q(\xi) > -\xi\phi(\xi)\frac{\phi(\xi)}{\xi} = -\phi(\xi)^2$ and then $-\xi\phi(\xi)\left(1-\Phi(\xi)\right) + \phi(\xi)^2 > -\phi(\xi)^2 + \phi(\xi)^2 = 0$

The nominator is again nonnegative. We prove that the first derivative is nonnagtive, thus the hazard rate of truncated normal distribution is monotonly increasing, and truncated normal distribution MHR distribution.

Now let's determine the mean and variance of this one sided truncated normal distribution. One sided truncation with $X \ge 0$, let $\alpha = \frac{-\mu}{\sigma}$, $\beta = \infty$ and $\phi(x)$, $\Phi(x)$ are pdf and cdf of standard normal distribution, thus $\phi(\beta) = 0$, $\Phi(\beta) = 1$ then

$$E(X|X \ge 0) = \mu + \frac{\sigma\phi(\alpha)}{1 - \Phi(\alpha)}$$
$$Var(X|X \ge 0) = \sigma^2 \left[1 + \frac{\alpha\phi(\alpha)}{1 - \Phi(\alpha)} - \left(\frac{\phi(\alpha)}{1 - \Phi(\alpha)}\right)^2\right]$$

where $\phi(x)$, $\Phi(x)$ are pdf and cdf of standard normal distribution and

2.3.2 Result of experiment

Similar design like we created above for uniform distribution. We choose an arbitrary normal distribution, then sample from nonnegative part of this normal distribution, we simply using the rejection sampling. A rejection sampling for a truncated distribution is simply: draws a realization from knowned $N(\mu, \sigma^2)$ and accepts it iff the draw $\in (0, \infty)$. Therefore this can be easily implemented. To compute optimal reserve price and robust reserve price we use numerical solver. The step of solving the robust reserve price is the same as above, we first solve ρ_D from equation 2.2 and then substitute it into reserve price equation proposed by the paper.

change in r We can first fix μ , and change the value of σ , if we gradually increase σ , then r is also linearly increase in terms of σ . wlog, we can choose this μ to 1, because if $x \sim N(5,5)$, then we can find a corresponding normal distribution with $\mu = 1$ that is $\frac{x}{5} \sim N(1,\frac{1}{5})$ they have the same DAPX.

$$DAPX = \frac{OPT}{REV} = \frac{p_{opt}(1 - \int_0^{p_{opt}} kf(x))}{p_D(1 - \int_0^{p_D} kf(x))} = \frac{p_{opt}(1 - k(F(p_{opt}) - F(0)))}{p_D(1 - k(F(p_D) - F(0)))}$$

2.4 Pareto distribution

Here we also want to consider Pareto distribution. This distribution can possible be used in description of auction data when most bids are consetrated at lower values while high bid is hardly to occur.

Pareto distribution is definde by two parameters x_m , c and $x \in [x_m, \infty]$. To simplify, we choose the scale parameter $x_m = 1$ for now. then we have following PDF and CDF for pareto distribution:

$$f(x) = \frac{c}{x^{c+1}}$$

and

$$F(x) = 1 - \frac{1}{x^c}$$

Another special property of pareto distribution is that when parameter $c \leq 1$, it does not have a mean (the mean is infinite), in addition, when $c \leq 2$ its variance is infinite too. Thus in order to have a valid CV r during the experiment, we want to choose parameter c > 2.

Then let's have a look at the optimal revenue if our bidder valuation is from this pareto distribution. The optimal revenue is archieved by maximizing expected revenue which can be written as:

$$\mathrm{OPT}\left(F\right) = \sup_{p \geqslant 1} \mathrm{REV}(p; F) = \sup_{p \geqslant 1} p \cdot \left(1 - \left(1 - \frac{1}{p^c}\right)\right) = \sup_{p \geqslant 1} \ \frac{1}{p^{c-1}}$$

since c > 2, then $\frac{1}{p^{c-1}}$ is monotone decreasing. When reserve price is p = 1, it reach the maximum expected revenue, thus $\mathrm{OPT}(F) = 1$. However during the experiment, the reserve price proposed by the paper is always smaller than 1, and based on the support of pareto distribution, all the bidders' valuation is not less than 1. It is obiviously not a good option to set the reserve price to below 1. When c increases, the experiment reserve price is closer to 1, thus the resulted DAPX gets closer to 1.

2.4.1 another idea: integrate f(x) to 1

now if we change the previous pareto distribution by shifting the distribution to the left by 1, in another word by extending its support to $x \in [0, \infty]$, we get:

$$f(x) = \frac{c}{(x+1)^{c+1}}$$

and

$$F(x) = 1 - \frac{1}{(x+1)^c}$$

Obviously the mean and variance of this distribution is just: E[X-1]=E[X]-1 and Var[X-1]=Var[X], which can be implemented easily in python. This time $p_{opt}=\arg\max_{p}\ p(1-(1-\frac{1}{(p-1)^c}))=\arg\max_{p}\ \frac{p}{(p-1)^c}$ for me it is unclear which is optimal reserve price,

Chapter 3

Single bidder and single item Randomization

pdf of the given cdf:

$$f_{\mu,\sigma}^{log}(x) = \frac{\pi_2 \frac{1}{x} - 1}{\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1)}$$

between range $[\pi_1, \pi_2]$, $max(f_{\mu,\sigma}^{log}(x)) = f_{\mu,\sigma}^{log}(\pi_1)$, therefore we can use rejection sampling method by propose an envelope density

$$q(x) = \begin{cases} \frac{1}{\pi_2 - \pi_1} & \text{if } x \in [\pi_1, \pi_2] \\ 0 & \text{otherwise} \end{cases}$$

Then a valid envelope constant can be: $A = f_{\mu,\sigma}^{log}(\pi_1) \cdot (\pi_2 - \pi_1)$, since $A \cdot q(x) \ge f_{\mu,\sigma}^{log}(x), \forall x \in [\pi_1, \pi_2]$

The steps this reject sampling

Algorithm 1 rejection sampling algorithm

```
1: procedure Rejection Sampling(for bounded density on bounded support)
 2:
        n \leftarrow 0
        while n \leq N do
                                                                                     \triangleright N is sample size
 3:
             draw x \sim q(x)
 4:
             compute acception probability a := \frac{f_{\mu,\sigma}^{log}(x)}{Aq(x)}
 5:
             draw a random variable u \sim U[0, 1]
 6:
             if u \leqslant a then
 7:
                 accept x, add it to x_{list}
 8:
 9:
                 n \leftarrow n + 1
        return x_{list}
10:
```

3.1 Uniform distribution

Now the robust reserve price $P_{\mu,\sigma}^{log}$ is distributed over the nonnegative interval support $[\pi_1, \pi_2]$ and we assume bidder valuation is follow a uniform distribution U[a, b]. Then using a randomized mechanism, our expected revenue

$$REV(P_{\mu,\sigma}^{log}; U[a, b]) = \underset{p \sim F_{\mu,\sigma}^{log}}{\mathbb{E}} \left[p(1 - F_{uniform}(p)) \right]$$

$$= \int_{\pi_1}^{\pi_2} p(1 - \frac{p - a}{b - a}) f_{\mu,\sigma}^{log}(p) dp$$

$$= \int_{\pi_1}^{\pi_2} p(1 - \frac{p - a}{b - a}) \cdot \frac{\pi_2 \frac{1}{p} - 1}{\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1)} dp$$

$$= \int_{\pi_1}^{\pi_2} \frac{p(b - p)}{b - a} \cdot \frac{\pi_2 - p}{p(\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1))} dp$$

$$= \frac{1}{(b - a)(\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1))} \int_{\pi_1}^{\pi_2} (b - p)(\pi_2 - p) dp$$

$$= \frac{1}{(b - a)(\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1))} \cdot \left(\frac{p^3}{3} - \frac{bp^2}{2} - \frac{\pi_2 p^2}{2} + b\pi_2 p\right|_{\pi_2}^{\pi_1}$$

As we can see, the expected revenue can be determined explicitly, we also know that the optimal revenue for a given uniform distribution will be $OPT(F_{uniform}) = \frac{b^2}{4(b-a)}$.

Then APX =
$$\frac{\text{OPT}(F_{uniform})}{\text{REV}(P_{\mu,\sigma}^{log}; F_{uniform})}$$

3.2 Normal distribution

Similarly the expected revenue of a truncated normal distribution $N_t(\mu, \sigma^2)$

$$\begin{aligned} \text{REV}(P_{\mu,\sigma}^{log}; N_t(\mu, \sigma^2)) &= \underset{p \sim F_{\mu,\sigma}^{log}}{\mathbb{E}} [p(1 - F_{N_t}(p))] \\ &= \int_{\pi_1}^{\pi_2} p(1 - k(F_N(p) - F_N(0))) f_{\mu,\sigma}^{log}(p) dp \\ &= \int_{\pi_1}^{\pi_2} p(1 - k(F_N(p) - F_N(0))) \cdot \frac{\pi_2 - p}{p(\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1))} dp \\ &= \frac{1}{\pi_2 \ln \frac{\pi_2}{\pi_1} - (\pi_2 - \pi_1)} \int_{\pi_1}^{\pi_2} (1 - k(F_N(p) - F_N(0))) (\pi_2 - p) dp \end{aligned}$$

 π_1, π_2 are the (unique) solutions of the system:

$$\begin{cases} \pi_1(1 + \ln\frac{\pi_2}{\pi_1}) = \mu \\ \pi_1(2\pi_2 - \pi_1) = \mu^2 + \sigma^2 \end{cases}$$

however $\exists \mu, \sigma$ that the above system has no solutions. For example we can write:

$$\begin{cases} \pi_2 = \pi_1 e^{\frac{\mu}{\pi_1} - 1} \\ \pi_2 = \frac{\frac{\mu^2 + \sigma^2}{\pi_1} + \pi_1}{2} \end{cases}$$

If there is a solution for π_2 then by ploting above two equations, there should be an intersection, but it seems when r increases, there is no solution for the system.

Chapter 4

Additional notes

4.1 truncated normal distribution part

$$f_t(x) = \begin{cases} kf(x) & \text{if } x \geqslant 0\\ 0 & \text{otherwise} \end{cases}$$

where k is a normalizing constant. We can determine k by using the knowledge of the sum of the probablity equals to 1. Then we have:

$$1 = \int_{R} f_t(x) dx = \int_0^\infty k f(x) dx = k \cdot \int_0^\infty f(x) dx$$
$$\implies k = \frac{1}{\int_0^\infty f(x) dx} = \frac{1}{1 - F(0)}$$

Here $x \ge 0$, then the coresponding cdf is:

$$F_t(x) = \int_0^x k f(t) dt = k \cdot \int_0^x f(t) dt = k(F(x) - F(0))$$

question to answer:

1.two random variables, X,Y, let Y = c*X where c>0 constant. let F_X , f_X be the cdf, pdf of X what is the relation of F_Y , f_y to F_X , f_X

$$F_Y(y) = P(Y \geqslant y) = P(cX \leqslant y) = P(X \leqslant \frac{y}{c}) = F_X(\frac{y}{c})$$
 we know $f_Y(y) = f_X(g^{-1}(y)) |\frac{dg^{-1}(y)}{dy}|$ thus:

$$f_Y(y) = f_X(\frac{y}{c}) \cdot |\frac{1}{c}| = \frac{1}{c} f_X(\frac{y}{c})$$

2. what is the relation of myerson(Y) and myerson(X)

Myerson(X) optimal revenue can be achieved by a deterministic mechanism, let denot v_x of optimal reverse price for X, then $OPT(X) = v_x(1 - F_X(v_x))$, what if optimal reserve price for Y? we can compute optimla reserve price by setting virtual valuation for Y equal to 0:

$$v - \frac{1 - F_X(\frac{v}{c})}{\frac{1}{c} f_X(\frac{v}{c})} = 0$$
$$\frac{v}{c} - \frac{1 - F_X(\frac{v}{c})}{f_X(\frac{v}{c})} = 0$$

set $v^{'} = \frac{v}{c}$, above equation has solution v_x . Then denote optimal reserve price for Y: $v_y = cv_x$ then $\mathrm{OPT}(Y) = v_y(1 - F_Y(v_y)) = cv_x(1 - F_X(\frac{cv_x}{c})) = cv_x(1 - F_X(v_x))$. Therefore $\mathrm{OPT}(Y) = \mathrm{cOPT}(X)$ 3. what is the relation of $\mathrm{REV}(Y)$ and $\mathrm{REV}(x)$, given v as reserve price

REV(Y) =
$$v(1 - F_Y(v)) = v(1 - F_X(\frac{v}{c}))$$

REV(X) = $v(1 - F_X(v))$

$$v(1 - F_X(\frac{v}{c})) \stackrel{0 < c < 1}{<} v(1 - F_X(v))$$

$$\stackrel{c=1}{=}$$

$$\stackrel{c>1}{>}$$

Experiment Evaluation of Robust Revenue-Maximizing Auctions

n = 1000000

outside for loop Normal distribution APX = [1.12655521] the total runtime: 123.03474499999993 seconds

np.average($opt/exp_norm_revenue_list$) 1.1516288151898313 within the for loop $np.average(APX_norm_list)$ Normal distribution APX = 1.1515851528631347 the total runtime: 2193.8029290000004 seconds sum(opt_norm_list)/sum($exp_norm_revenue_list$) array([1.12662361])

n = 100000 Normal distribution APX = 1.1518479638482406 the total runtime: 220.4375460000001 seconds array([1.12673402])

Chapter 5

One hot encoding

one hot encoding is convert a categorical variable into n*k (n is number of instances, k is number of categories). Dummy variable trap leads to the problem known as multicolinearity.

- The features were preprocessed with dummy coding for the categorical variables
- $\bullet\,$ and min-max-scaling for numerical ones
- use poisson deviation as loss function
- use relu as activation function and one hidden layer
- out put final layer logit identically and feed it into GLM

$$L(\hat{y}, y, i) = \begin{cases} \hat{y} - y ln(\hat{y}) + ln(\Gamma(y)) & \text{if } i = 1\\ \hat{y} + \frac{y}{\hat{y}} - \sqrt{y} & \text{if } i = 2\\ \frac{(\hat{y})^{2-i}}{2-i} - y \frac{(\hat{y})^{1-i}}{1-i} - (\frac{y^{2-i}}{2-i} - y \frac{y^{1-i}}{1-i}) & \text{otherwise} \end{cases}$$

source for possible twee die loss function:https://towardsdatascience.com/twee die-loss-function-for-right-skewed-data-2c5ca470678f source:https://www.analyticsvidhya.com/blog/2020/03/one-hot-encoding-vs-label-encoding-using-scikit-learn/

Chapter 6

Further Reading

In this chapter we collect some suggested literature for LATEX matters, which may be of use for beginners and for more advanced users and may provide some useful tips.

Ishort: "The Not So Short Introduction to LATEX" (see [l2short]) is an up-to-date introduction which can be worked through in a moderate amount of time (the authors give an estimated time of 157 minutes for version 5.01, the most recent at the time of writing.) An up-to-date version can be found at http://tobi.oetiker.ch/lshort/lshort.pdf.

LATEX and Friends: The book [vanDongen2012] is a recommended and up-to-date introduction to LATEX which addresses many current packages. Worth a look for both beginners and advanced users.

l2tabu: There are many tips for older packages and LATEX commands in [l2tabu], which are particularly recommended for advanced LATEX users. Here you can learn why certain commands are best avoided and what the alternatives are. Note: The tumthesis.cls class automatically calls upon the nag package, which immediately rings alarm bells with many of the mistakes listed in l2tabu.

Appendix A

Remarks on Implementation

In the appendix you can include e.g. computer codes or further remarks which would disturb the flow of the main text. If you do not need an appendix, you can simply leave out this file (in which case you should also delete the \include command in thesis.tex).

List of Figures

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All figures in this document were created by the author using TikZ, the excellent T_EX -package by Till Tantau, see [Tantau2007].

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Note:	include in the list of recommended literature	1(