

Chulalongkorn University

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template from KACTL

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Τ	$\overline{\text{Cemplate}}$ (1)	
template.cpp		27 lines
#p:	ragma once	
#de	<pre>nclude <bits stdc++.h=""> efine sz(x) (int)(x).size() efine all(x) (x).begin(), (x).end()</bits></pre>	
us	ing namespace std;	
us: us: us: us: us: coi // coi coi coi	<pre>ing ll = long long; ing db = long double; ing vi = vector<int>; ing vl = vector<1l>; ing vd = vector<db>; ing pii = pair<int, int="">; ing pll = pair<1l, ll>; ing pdd = pair<db, db="">; nst int INF = 0x3fffffff; const int MOD=1000000007; nst int MOD = 0x1ffffffffffffffff; nst db DINF = numeric_limits<db>::infinity(); nst db EPS = le-9; nst db PI = acos(db(-1));</db></db,></int,></db></int></pre>	
	<pre>t main() { cin.tie(nullptr)->sync_with_stdio(false);</pre>	
c.s		2 lines
./	+ -std=gnu++2a -Wall \$1 -o a.out a.out Aathematics (2)	

2.1 Goldbatch's Conjecture

• Even number can be written in sum of two primes (Up to 1e12

• Range of N^{th} prime and $N+1^{th}$ prime will be less than or equal to 300 (Up to 1e12)

2.2 Divisibility

Number of divisors of N is given by $\prod_{i=1}^{k} (a_i + 1)$ where $N = \prod_{i=1}^k p_i^{a_i}$ and p_i are prime factors of N.

Numerical (3)

3.1 Newton's Method

```
if F(Q) = 0, then Q_{2n} \equiv Q_n - \frac{F(Q_n)}{F'(Q_n)} \pmod{x^{2n}}
                Q = P^{-1} : Q_{2n} \equiv Q_n \cdot (2 - P \cdot Q_n^2) \pmod{x^{2n}}
                                  Q = \ln P = \int \frac{P'}{P} \mathrm{d}x
                Q = e^p : Q_{2n} \equiv Q_n (1 + P - \ln Q_n) \pmod{x^{2n}}
                Q = \sqrt{P} : Q_{2n} \equiv \frac{1}{2} (Q_n + P \cdot Q_n^{-1}) \pmod{x^{2n}}
               Q = P^k = \alpha^k x^{kt} e^{k \ln T}; P = \alpha \cdot x^t \cdot T, T(0) = 1
```

Data Structures (4)

```
OrderedSet.hpp
Description: Ordered Set
"../template/Header.hpp", <bits/extc++.h>
                                                        1a7f5f, 14 lines
using namespace __gnu_pbds;
template <class T>
using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
     tree_order_statistics_node_update>;
// can be change to less_equal
void usage() {
 ordered_set<int> st, st_2;
 st.insert(2);
 st.insert(1);
 cout << st.order_of_key(2);</pre>
 cout << *st.find_by_order(1);</pre>
 st.join(st_2); // merge
FenwickTree.hpp
Description: Fenwick / Binary Indexed Tree
```

```
43767a, 41 lines
template < class T>
struct Fenwick{
    int n, logn;
    vector<T> t;
    Fenwick(){}
    Fenwick(int _n) {init(vector<T>(_n,T{}));}
    template < class U>
    Fenwick(const vector<U> &a) {init(a);}
    template < class U>
    void init(const vector<U> &a){
        n=(int)a.size();
        logn=31-__builtin_clz(n);
        t.assign(n+1,T{});
```

```
for (int i=1; i<=n; i++) {</pre>
             t[i]=t[i]+a[i-1];
             int j=i+(i&-i);
             if(j<=n)t[j]=t[j]+t[i];</pre>
    void update(int x,const T &v) {
         for (int i=x+1; i<=n; i+=i&-i) t[i] =t[i]+v;</pre>
    void update(int l,int r,const T &v) {
         update (1, v), update (r+1, -v);
    T query(int x) {
        T res{};
         for(int i=x+1;i>0;i-=i&-i)res=res+t[i];
         return res;
    T query(int 1,int r) {
         return query (r) -query (1-1);
    int find(const T &k) {
         int x=0;
        T cur{};
         for(int i=1<<logn;i>0;i>>=1)
             if (x+i \le n\&\& cur + t [x+i] \le k) x+=i, cur = cur + t [x];
         return x;
};
```

Segment Tree.hpp

Description: Segment Tree

```
c51dec. 85 lines
```

```
template < class Monoid>
struct SegmentTree{
    using T = typename Monoid::value_type;
    int n;
    vector<T> t;
    SegmentTree(){}
    SegmentTree(int n, function<T(int)> create) {init(n, create);}
    SegmentTree(int n,T v=Monoid::unit()) {init(n,[&](int){
         return v; });}
    template<class U>
    SegmentTree(const vector<U> &a) {init((int)a.size(),[&](int
         i) {return T(a[i]);});}
    void init(int _n,function<T(int)> create) {
        t.assign(4<<(31-__builtin_clz(n)),Monoid::unit());
        function<void(int,int,int)> build=[&](int l,int r,int i
            if(l==r)return void(t[i]=create(l));
            int m = (1+r)/2;
            build(1, m, i * 2);
            build(m+1, r, i*2+1);
            pull(i);
        };
        build(0, n-1, 1);
    void pull(int i) {
        t[i]=Monoid::op(t[i*2],t[i*2+1]);
    void modify(int 1, int r, int i, int x, const T &v) {
        if (x<1 | | r<x) return;</pre>
        if(l==r)return void(t[i]=v);
        int m = (1+r)/2;
        modify(1, m, i*2, x, v);
        modify (m+1,r,i*2+1,x,v);
        pull(i);
    void modify(int x,const T &v) {
```

```
modify (0, n-1, 1, x, v);
    template<class U>
    void update(int 1, int r, int i, int x, const U &v) {
        if (x<1 | | r<x) return;
        if(l==r)return void(t[i]=Monoid::op(t[i],v));
        int m = (1+r)/2;
        update(1, m, i*2, x, v);
        update (m+1,r,i*2+1,x,v);
        pull(i);
    template<class U>
    void update(int x,const U &v) {
        update (0, n-1, 1, x, v);
    T query(int 1, int r, int i, int x, int y) {
        if (y<1||r<x) return Monoid::unit();</pre>
        if (x<=1&&r<=y) return t[i];</pre>
        int m = (1+r)/2;
        return Monoid::op(query(1, m, i*2, x, y), query(m+1, r, i*2+1,
             x,y));
    T query(int x,int y){
        return query (0, n-1, 1, x, y);
    template<class F>
    int findfirst(int 1, int r, int i, int x, int y, const F &f) {
        if(y<1||r<x||!f(t[i]))return n;
        if (l==r) return 1;
        int m = (1+r)/2;
        int res=findfirst(1, m, i*2, x, y, f);
        if (res==n) res=findfirst (m+1, r, i*2+1, x, y, f);
        return res;
    template<class F>
    int findfirst(int x,int y,const F &f) {
        return findfirst(0,n-1,1,x,y,f);
    template < class F>
    int findlast(int 1, int r, int i, int x, int y, const F &f) {
        if(y<1||r<x||!f(t[i]))return -1;
        if(l==r)return 1;
        int m = (1+r)/2;
        int res=findlast(m+1,r,i*2+1,x,v,f);
        if (res==-1) res=findlast (1, m, i*2, x, y, f);
        return res;
    template < class F>
    int findlast(int x,int y,const F &f) {
         return findlast(0, n-1, 1, x, y, f);
};
LazySegment Tree.hpp
Description: Segment Tree with Lazy Propagation
                                                       91ab0c, 103 lines
template < class MonoidAction>
struct LazySegmentTree{
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    int n;
    vector<Info> t;
    vector<Tag> lz;
    LazySegmentTree() {}
```

LazySegmentTree(int n, function<Info(int)> create) {init(n,

create);}

```
LazySegmentTree(int n, Info v=InfoMonoid::unit()) {init(n
     , [&] (int) {return v;});}
template<class T>
LazySegmentTree(const vector<T> &a) {init((int)a.size(),[&](
     int i) {return Info(a[i]);});}
void init(int _n,function<Info(int)> create){
    int m=4<<(31-__builtin_clz(n));</pre>
    t.assign(m,InfoMonoid::unit());
    lz.assign(m, TagMonoid::unit());
    function<void(int,int,int)> build=[&](int l,int r,int i
        if(l==r)return void(t[i]=create(l));
        int m = (1+r)/2;
        build(l, m, i*2);
        build(m+1, r, i*2+1);
        pull(i);
    build(0, n-1, 1);
void pull(int i) {
    t[i]=InfoMonoid::op(t[i*2],t[i*2+1]);
void apply(int i,const Tag &v){
    t[i]=MonoidAction::op(t[i],v);
    lz[i]=TagMonoid::op(lz[i],v);
void push(int i){
    apply(i*2,lz[i]);
    apply(i*2+1,1z[i]);
    lz[i]=TagMonoid::unit();
void modify(int 1, int r, int i, int x, const Info &v){
    if (x<1 | | r<x) return;</pre>
    if(l==r)return void(t[i]=v);
    int m = (1+r)/2;
    push(i);
    modify (1, m, i*2, x, v);
    modifv(m+1,r,i*2+1,x,v);
    pull(i);
void modify(int x,const Info &v) {
    modify (0, n-1, 1, x, v);
void update(int 1,int r,int i,int x,int y,const Tag &v) {
    if (y<1 | |r<x) return;
    if (x<=1&&r<=y) return apply(i,v);</pre>
    int m = (1+r)/2;
    push(i);
    update(1, m, i*2, x, y, v);
    update (m+1,r,i*2+1,x,y,v);
    pull(i);
void update(int x,int y,const Tag &v) {
    update (0, n-1, 1, x, y, v);
Info query(int 1,int r,int i,int x,int y){
    if(v<1||r<x)return InfoMonoid::unit();</pre>
    if (x<=1&&r<=y) return t[i];</pre>
    int m = (1+r)/2;
    return InfoMonoid::op(query(1,m,i*2,x,y),query(m+1,r,i
         *2+1, x, y));
Info query(int x,int y){
    return query (0, n-1, 1, x, y);
template < class F>
int findfirst(int 1,int r,int i,int x,int y,const F &f) {
```

```
if(y<1||r<x||!f(t[i]))return n;
         if (l==r) return 1;
         int m = (1+r)/2;
        push(i);
         int res=findfirst(1, m, i*2, x, y, f);
        if (res==n) res=findfirst (m+1, r, i \times 2+1, x, y, f);
         return res;
    template<class F>
    int findfirst(int x,int y,const F &f) {
         return findfirst(0, n-1, 1, x, y, f);
    template < class F>
    int findlast(int 1, int r, int i, int x, int y, const F &f) {
         if (y<1 | | r<x | | ! f (t[i])) return -1;</pre>
        if (l==r) return 1;
        int m = (1+r)/2;
        push(i);
         int res=findlast(m+1,r,i*2+1,x,y,f);
        if (res==-1) res=findlast (1, m, i*2, x, y, f);
        return res;
    template<class F>
    int findlast(int x,int y,const F &f){
         return findlast(0, n-1, 1, x, y, f);
};
DynamicSegmentTree.hpp
Description: Dynamic Segment Tree
                                                         e84eeb, 106 lines
template < class MonoidAction >
struct DvnamicSegmentTree{
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    struct Node:
    using Ptr = Node*;
    struct Node {
        Info val:
        Tag lz;
        Ptr l,r;
        Node (Info v): val(v), lz(TagMonoid::unit()), l(nullptr), r(
              nullptr) {}
        \label{eq:node_solution} Node\left(\texttt{Info v,Tag t}\right): \texttt{val(v),lz(t),l(nullptr),r(nullptr)} \left. \right\}
    11 lb, ub;
    Ptr rt:
    function<Info(11,11)> create;
    DynamicSegmentTree(){init(0,0);}
    DynamicSegmentTree(ll n) {init(0, n-1);}
    DynamicSegmentTree(ll lb, ll ub) {init(lb, ub);}
    DynamicSegmentTree(ll lb, ll ub, function<Info(ll, ll)> create
          ) {init(lb,ub,create);}
    void init(ll _lb,ll _ub,function<Info(ll,ll)> _create=[](ll
          1,11 r) {return InfoMonoid::unit();}) {
         lb=_lb,ub=_ub;
        create= create;
        rt=new Node(create(lb,ub));
    Info val(Ptr t){
         return t?t->val:InfoMonoid::unit();
    void pull(Ptr &t) {
        t->val=InfoMonoid::op(val(t->1), val(t->r));
    void apply(Ptr &t,const Tag &v,ll 1,ll r){
         if(!t)t=new Node(create(1,r));
```

DSU BinaryTrie LiChaoTree

```
t->val=MonoidAction::op(t->val,v);
    t->1z=TagMonoid::op(t->1z,v);
void push(Ptr &t, ll l, ll m, ll r) {
    apply (t->1, t->1z, 1, m);
    apply (t->r,t->lz,m+1,r);
    t->1z=TagMonoid::unit();
void modify(ll 1,ll r,Ptr &t,ll x,const Info &v){
    if (x<1||r<x) return;</pre>
    if (l==r) return void(t->val=v);
    11 m=1+(r-1)/2;
    push(t,1,m,r);
   modify(1, m, t->1, x, v);
    modify (m+1, r, t->r, x, v);
    pull(t);
void modify(ll x,const Info &v) {
    modify(lb,ub,rt,x,v);
void update(ll 1,ll r,Ptr &t,ll x,ll y,const Tag &v) {
    if (y<1 | | r<x) return;</pre>
    if(x<=l&&r<=y) return apply(t,v,l,r);</pre>
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    update (1, m, t->1, x, y, v);
    update (m+1,r,t->r,x,y,v);
    pull(t);
void update(ll x,ll y,const Tag &v){
    update(lb,ub,rt,x,y,v);
Info query(11 1,11 r,Ptr &t,11 x,11 y){
    if (y<1||r<x) return InfoMonoid::unit();</pre>
    if (x<=1&&r<=v) return t->val;
   11 m=1+(r-1)/2;
    push(t,1,m,r);
    return InfoMonoid::op(query(1, m, t->1, x, y), query(m+1, r, t
         ->r,x,v));
Info query(ll x,ll y){
    return query(lb,ub,rt,x,y);
template<class F>
11 findfirst(ll 1, ll r, Ptr t, ll x, ll y, const F &f) {
    if (y<1 | | r<x | | ! f (t->val) ) return -1;
    if(l==r)return 1;
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    ll res=findfirst(l, m, t \rightarrow l, x, y, f);
    if (res==-1) res=findfirst (m+1, r, t->r, x, y, f);
    return res;
template<class F>
ll findfirst(ll x, ll y, const F &f) {
    return findfirst(lb, ub, rt, x, y, f);
template<class F>
11 findlast(ll 1, ll r, Ptr t, ll x, ll y, const F &f) {
    if (y<1||r<x||!t||!f(t->val)) return -1;
    if(l==r)return 1;
   11 m=1+(r-1)/2;
    push(t,l,m,r);
    ll res=findlast(m+1, r, t->r, x, y, f);
    if (res==-1) res=findlast(1, m, t->1, x, y, f);
    return res;
template<class F>
11 findlast(ll x,ll y,const F &f) {
```

```
return findlast(lb,ub,rt,x,y,f);
};
DSU.hpp
Description: Disjoint Set Union.
                                                       0b3cb8, 26 lines
struct DSU{
    vector<int> p,sz;
    DSU() { }
    DSU(int n) {init(n);}
    void init(int n){
        p.resize(n);
        iota(p.begin(), p.end(), 0);
        sz.assign(n,1);
    int find(int u){
         return p[u] == u?u:p[u] = find(p[u]);
    bool same(int u,int v) {
        return find(u) == find(v);
    bool merge(int u,int v) {
        u=find(u), v=find(v);
        if (u==v) return false;
        sz[u]+=sz[v];
        p[v]=u;
        return true;
    int size(int u) {
        return sz[find(u)];
};
Binary Trie. hpp
Description: Binary Trie
                                                       ae5b7a, 66 lines
template<int BIT, class T = uint32_t, class S = int>
struct BinaryTrie{
    struct Node {
        array<int,2> ch;
        S cnt:
        Node():ch\{-1,-1\}, cnt(0){}
    vector<Node> t;
    BinaryTrie():t{Node()}{}
    int new node(){
        t.emplace_back(Node());
        return t.size()-1;
    S size(){
        return t[0].cnt;
    bool empty() {
        return size() ==0;
    S get_cnt(int i) {
        return i!=-1?t[i].cnt:S(0);
    void insert(T x,S k=1){
        int u=0;
        t[u].cnt+=k;
        for(int i=BIT-1; i>=0; i--) {
             int v=x>>i&1;
            if(t[u].ch[v]==-1)t[u].ch[v]=new_node();
            u=t[u].ch[v];
            t[u].cnt+=k;
```

```
t[u].cnt-=k;
        for(int i=BIT-1; i>=0; i--) {
            int v=x>>i&1;
            u=t[u].ch[v];
            assert (u!=-1&&t[u].cnt>=k);
            t[u].cnt-=k;
    T kth(S k, T x=0) {
        assert(k<size());
        int u=0;
        T res=0;
        for(int i=BIT-1; i>=0; i--) {
            int v=x>>i&1;
            if(k<get_cnt(t[u].ch[v])){
                u=t[u].ch[v];
            }else{
                res|=T(1)<<i;
                k=get_cnt(t[u].ch[v]);
                u=t[u].ch[v^1];
        return res;
    T min(T x) {
        return kth(0,x);
    T max(T x){
        return kth(size()-1,x);
};
LiChaoTree.hpp
Description: Li-Chao Tree (minimize)
                                                       4ab713, 52 lines
template<class T>
struct LiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line{
        T m.c:
        Line(T _m, T _c):m(_m), c(_c){}
        inline T eval(T x)const{return m*x+c;}
    };
    vector<T> xs;
    vector<Line> t;
    LiChaoTree(){}
    LiChaoTree(const vector<T> &x):xs(x){init(x);}
    LiChaoTree(int n):xs(n){
        vector<T> x(n);
        iota(x.begin(), x.end(), 0);
        init(x);
    void init(const vector<T> &x) {
        sort(xs.begin(),xs.end());
        xs.erase(unique(xs.begin(), xs.end()), xs.end());
        t.assign(4<<(31-__builtin_clz(xs.size())),Line(0,INF));
    void insert(int l, int r, int i, Line v) {
        int m = (1+r)/2;
        if(v.eval(xs[m]) <t[i].eval(xs[m])) swap(t[i],v);</pre>
        if (v.eval(xs[1]) <t[i].eval(xs[1])) insert(1, m, i*2, v);</pre>
        if(v.eval(xs[r]) < t[i].eval(xs[r]))insert(m+1, r, i*2+1, v)
    inline void insert(T m,T c){
```

void erase(T x,S k=1){

assert(t[u].cnt>=k);

int u=0:

```
if(y<xs[1]||xs[r]<x)return;
        if (x<=xs[1]&&xs[r]<=y) return insert(1,r,i,v);</pre>
        int m = (1+r)/2:
        insert_range(1, m, i * 2, x, y, v);
        insert_range (m+1, r, i*2+1, x, y, v);
    inline void insert_range(T m,T c,T x,T y) {
        insert_range(0,(int)xs.size()-1,1,x,y,Line(m,c));
    T query(int 1,int r,int i,T x) {
        if(l==r)return t[i].eval(x);
        int m = (1+r)/2;
        if (x \le xs[m]) return min (t[i].eval(x), query(1, m, i*2, x));
        return min(t[i].eval(x), query(m+1, r, i*2+1, x));
    inline T query(T x){
        return query(0,(int)xs.size()-1,1,x);
};
DynamicLiChaoTree.hpp
Description: Dynamic Li-Chao Tree (minimize).
                                                        b8af36, 50 lines
template < class T>
struct DynamicLiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line(
        T m,c;
        Line (T _m, T _c) : m(_m), c(_c) {}
        inline T eval(T x)const{return m*x+c;}
    struct Node:
    using Ptr = Node*;
    struct Node {
        Line v:
        Ptr l,r;
        Node():v(0,INF),l(nullptr),r(nullptr){}
        Node(Line _v):v(_v),l(nullptr),r(nullptr){}
    11 lb, ub;
    Ptr root:
    DynamicLiChaoTree(ll _lb,ll _ub):lb(_lb),ub(_ub),root(
    void insert(T 1, T r, Ptr &t, Line v) {
        if(!t)return void(t=new Node(v));
        T m=1+(r-1)/2;
        if(v.eval(m) <t->v.eval(m)) swap(t->v,v);
        if(v.eval(1)<t->v.eval(1))insert(1,m,t->1,v);
        if (v.eval(r) <t->v.eval(r)) insert(m+1, r, t->r, v);
    inline void insert(T m,T c){
        insert(lb, ub, root, Line(m, c));
    void insert_range(T 1, T r, Ptr &t, T x, T y, Line v) {
        if (y<1 | | r<x) return;
        if(!t)t=new Node();
        if (x<=1&&r<=y) return insert(l,r,t,v);</pre>
        T m=1+(r-1)/2;
        insert_range(l, m, t->l, x, y, v);
        insert_range(m+1,r,t->r,x,y,v);
    inline void insert_range(T m, T c, T x, T y) {
        insert_range(lb, ub, root, x, y, Line(m, c));
    T query(T 1,T r,Ptr t,T x) {
        if(!t)return INF;
```

insert (0, (int) xs.size()-1,1,Line(m,c));

void insert range(int l,int r,int i,T x,T v,Line v) {

```
T m=1+(r-1)/2;
        if (x<=m) return min (t->v.eval(x), query(1, m, t->1, x));
        return min(t->v.eval(x), query(m+1, r, t->r, x));
    inline T query(T x){
        return query(lb,ub,root,x);
};
SplayTreeBase.hpp
Description: Splay Tree. splay (u) will make node u be the root of the tree
in amortized O(log n) time.
template < class Node >
struct SplayTreeBase{
    using Ptr = Node*;
    bool is_root(Ptr t){
        return ! (t->p) | | (t->p->l!=t&&t->p->r!=t);
    } // The parent of the root stores the path parant in link
    int size(Ptr t){
        return t?t->size:0;
    virtual void push(Ptr t){};
    virtual void pull(Ptr t){};
    int pos(Ptr t){
        if(t->p){
            if(t->p->1==t)return -1;
            if(t->p->r==t)return 1;
        return 0;
    void rotate(Ptr t){
        Ptr x=t->p, y=x->p;
        if (pos(t) == -1) {
            if ((x->l=t->r))t->r->p=x;
            t->r=x, x->p=t;
        }else{
            if((x->r=t->1))t->1->p=x;
            t->1=x, x->p=t;
        pull(x),pull(t);
        if((t->p=y)){
            if(y->l==x)y->l=t;
            if (y->r==x) y->r=t;
    void splay(Ptr t) {
        if(!t)return;
        push(t);
        while(!is_root(t)){
            Ptr x=t->p;
            if(is_root(x)){
                push(x), push(t);
                rotate(t);
             }else{
                Ptr y=x->p;
                push(y), push(x), push(t);
                if(pos(x) == pos(t)) rotate(x), rotate(t);
                else rotate(t), rotate(t);
    Ptr get_first(Ptr t){
        while (t->1) push (t), t=t->1;
        splay(t);
        return t;
    Ptr get_last(Ptr t){
```

```
while (t->r) push (t), t=t->r;
        splay(t);
        return t;
    Ptr merge(Ptr 1,Ptr r) {
        splay(1),splay(r);
        if(!1)return r;
        if(!r)return 1;
        l=get_last(1);
        1->r=r:
        r->p=1;
        pull(1);
        return 1;
    pair<Ptr,Ptr> split(Ptr t,int k) {
        if(!t)return {nullptr,nullptr};
        if (k==0) return {nullptr,t};
        if(k==size(t))return {t,nullptr};
        push(t);
        if(k<=size(t->1)){
            auto x=split(t->1,k);
            t->1=x.second;
            t->p=nullptr;
            if(x.second) x.second->p=t;
            pull(t);
            return {x.first,t};
        }else{
            auto x=split(t->r,k-size(t->l)-1);
            t->r=x.first;
            t->p=nullptr;
            if(x.first)x.first->p=t;
            pull(t);
            return {t,x.second};
    void insert(Ptr &t,int k,Ptr v) {
        splay(t);
        auto x=split(t,k);
        t=merge(merge(x.first,v),x.second);
    void erase(Ptr &t,int k) {
        splav(t);
        auto x=split(t,k);
        auto v=split(x.second,1);
        // delete y.first;
        t=merge(x.first,y.second);
    template<class T>
    Ptr build(const vector<T> &v) {
        if(v.emptv())return nullptr;
        function<Ptr(int,int)> build=[&](int 1,int r){
            if(l==r)return new Node(v[1]);
            int m = (1+r)/2;
            return merge(build(1,m),build(m+1,r));
        return build(0, v.size()-1);
};
LazyReversibleBBST.hpp
Description: Lazy Reversible BBST Base.
template < class Tree, class Node, class MonoidAction >
struct LazyReversibleBBST:Tree{
    using Tree::merge;
    using Tree::split;
    using typename Tree::Ptr;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
```

```
using Info = typename MonoidAction::Info;
using Tag = typename MonoidAction::Tag;
LazyReversibleBBST() = default;
Info sum(Ptr t){
    return t?t->sum:InfoMonoid::unit();
void pull(Ptr t){
    if(!t)return;
    push(t);
    t->size=1;
    t->sum=t->val;
    t->revsum=t->val;
    if(t->1) {
        t->size+=t->l->size;
        t->sum=InfoMonoid::op(t->l->sum,t->sum);
        t->revsum=InfoMonoid::op(t->revsum,t->l->revsum);
    if(t->r) {
        t->size+=t->r->size;
        t->sum=InfoMonoid::op(t->sum,t->r->sum);
        t->revsum=InfoMonoid::op(t->r->revsum,t->revsum);
void push (Ptr t) {
   if(!t)return;
    if (t->rev) {
        toggle (t->1);
        toggle(t->r);
        t->rev=false;
    if(t->lz!=TagMonoid::unit()){
        propagate (t->1,t->1z);
        propagate(t->r,t->lz);
        t->1z=TagMonoid::unit();
void toggle (Ptr t) {
    if(!t)return;
    swap(t->1,t->r);
    swap(t->sum,t->revsum);
    t->rev^=true;
void propagate (Ptr t, const Tag &v) {
    if(!t)return;
    t->val=MonoidAction::op(t->val,v);
    t->sum=MonoidAction::op(t->sum, v);
    t->revsum=MonoidAction::op(t->revsum,v);
    t->1z=TagMonoid::op(t->1z,v);
void apply(Ptr &t,int 1,int r,const Tag &v) {
    if(1>r)return;
    auto x=split(t,1);
    auto y=split(x.second, r-l+1);
    propagate(y.first,v);
    t=merge(x.first, merge(y.first, y.second));
Info query(Ptr &t,int 1,int r){
    if(l>r)return InfoMonoid::unit();
    auto x=split(t,1);
    auto y=split(x.second, r-1+1);
    Info res=sum(y.first);
    t=merge(x.first, merge(y.first, y.second));
    return res:
void reverse(Ptr &t,int 1,int r) {
    if (1>r) return;
    auto x=split(t,1);
```

```
auto y=split(x.second, r-1+1);
        toggle(y.first);
        t=merge(x.first, merge(y.first, y.second));
};
LazyReversibleSplayTree.hpp
Description: Lazy Reversible Splay Tree.
"SplayTreeBase.hpp", "LazyReversibleBBST.hpp"
                                                     b8455b, 23 lines
template < class MonoidAction>
struct LazyReversibleSplayTreeNode{
    using Ptr = LazyReversibleSplayTreeNode*;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    using value_type = Info;
   Ptr 1, r, p;
    Info val, sum, revsum;
    Tag lz;
    int size;
    LazyReversibleSplayTreeNode(const Info &_val=InfoMonoid::
        unit(),const Tag &_lz=TagMonoid::unit())
        :1(),r(),p(),val(_val),sum(_val),revsum(_val),lz(_lz),
             size(1), rev(false){}
template < class MonoidAction>
struct LazyReversibleSplayTree
    : LazyReversibleBBST<SplayTreeBase<
         LazyReversibleSplayTreeNode<MonoidAction>>,
      LazyReversibleSplayTreeNode<MonoidAction>, MonoidAction>{
    using Node = LazyReversibleSplayTreeNode<MonoidAction>;
LinkCutTreeBase.hpp
Description: Link Cut Tree Base.
Usage: evert(u): make u be the root of the tree.
link(u,v): attach u to v.
cut(u,v): remove edge between u and v.
get_root(u): get the root of the tree containing u.
lca(u,v): get the lowest common ancestor of u and v.
fold(u,v): get the value of the path from u to v. _{b432c3, 59 \; lines}
template<class Splay>
struct LinkCutTreeBase:Splay{
    using Node = typename Splay::Node;
    using Ptr = Node*;
    using T = typename Node::value_type;
   Ptr expose (Ptr t) {
        Ptr pc=nullptr; // preferred child
        for(Ptr cur=t;cur;cur=cur->p) {
            this->splay(cur);
            cur->r=pc;
            this->pull(cur);
            pc=cur;
        this->splay(t);
        return pc;
    void evert(Ptr t) { // make t be the root of the tree
        expose(t);
        this->toggle(t);
        this->push(t);
    void link(Ptr u,Ptr v) { // attach u to v
        evert(u);
        expose(v);
```

```
u->p=v;
    void cut(Ptr u,Ptr v){ // cut edge between u and v
        evert(u);
        expose (v);
        assert (u->p==v);
        v->1=u->p=nullptr;
        this->pull(v);
    Ptr get_root(Ptr t){
        expose(t);
        while (t->1) this->push (t), t=t->1;
        this->splay(t);
        return t;
    Ptr lca(Ptr u,Ptr v) {
        if (get_root(u)!=get_root(v)) return nullptr;
        expose(u);
        return expose(v);
    void set_val(Ptr t,const T &val) {
        this->evert(t);
        t->val=val;
        this->pull(t);
    T get_val(Ptr t){
        this->evert(t);
        return t->val;
    T fold (Ptr u, Ptr v) {
        evert(u);
        expose (v);
        return v->sum;
LazyLinkCutTree.hpp
Description: Lazy Link Cut Tree.
Usage: using Lct = LazyLinkCutTree<Action>;
using Ptr = Lct::Ptr;
using Node = Lct:: Node;
vector<Ptr> ptr(n);
for(int i=0;i<n;i++)ptr[i]=new Node(val[i]);</pre>
auto link=[](int u,int v){
Lct::link(ptr[u],ptr[v]);
auto cut=[](int u,int v){
Lct::cut(ptr[u],ptr[v]);
auto update=[](int u,int v,Action::Tag val){
Lct: : apply(ptr[u],ptr[v],val);
auto query=[](int u,int v){
return Lct::fold(ptr[u],ptr[v]);
"LazyReversibleSplayTree.hpp", "LinkCutTreeBase.hpp"
                                                       ead3da, 12 lines
template < class MonoidAction >
struct LazyLinkCutTree:LinkCutTreeBase<LazyReversibleSplayTree<</pre>
     MonoidAction>>{
    using base = LinkCutTreeBase<LazyReversibleSplayTree<</pre>
         MonoidAction>>;
    using Ptr = typename base::Ptr;
    using Tag = typename MonoidAction::Tag;
    void apply (Ptr u, Ptr v, const Tag &val) {
        this->evert(u);
        this->expose(v);
        this->propagate(v, val);
```

Number Theory (5)

```
Extended Euclid. hpp
Description: Extended Euclid algorithm for solving diophantine equation
(ax + by = gcd(a, b)).
Time: \mathcal{O}(\log \max\{a, b\})
"../template/Header.hpp"
                                                             229e7c, 13 lines
pair<11,11> euclid(11 a,11 b) {
    11 x=1, y=0, x1=0, y1=1;
    while(b!=0){
         11 q=a/b;
         x = q * x1;
         y=q*y1;
         a = q * b;
         swap(x, x1);
         swap(y,y1);
         swap(a,b);
```

5.1 Prime Numbers

```
LinearSieve.hpp
```

return {x,y};

Description: Prime Number Generator in Linear Time Time: $\mathcal{O}(N)$

```
"../template/Header.hpp"
                                                         194fb1, 15 lines
vi linear_sieve(int n) {
 vi prime, composite(n + 1);
  for(int i=2; i<=n; ++i) {</pre>
    if(!composite[i]) {
      prime.emplace_back(i);
    for(int j=0; j<(int) prime.size() && i*prime[j]<=n; ++j) {</pre>
      composite[i * prime[j]] = true;
      if(i % prime[j] == 0) {
        break;
 return prime;
```

FastEratosthenes.hpp

Description: Prime sieve for generating all primes smaller than LIM. Time: LIM=1e9 $\approx 1.5s$

```
"../template/Header.hpp"
                                                         295b58, 33 lines
const int LIM = 1e6;
bitset<LIM> isPrime;
vi eratosthenes() {
  const int S = (int) round(sqrt(LIM)), R = LIM / 2;
  vi pr = \{2\}, sieve(S + 1);
  pr.reserve(int(LIM/log(LIM) * 1.1));
  vector<pii> cp;
  for(int i=3; i<=S; i+=2) {</pre>
    if(!sieve[i]) {
      cp.emplace_back(i, i * i / 2);
      for(int j=i*i; j<=S; j+=2*i) {</pre>
        sieve[j] = 1;
  for(int L=1; L<=R; L+=S) {</pre>
    array<bool, S> block{};
    for(auto &[p, idx]: cp) {
```

```
for(int i=idx; i<S+L; idx=(i+=p)) {</pre>
        block[i - L] = 1;
    for(int i=0; i<min(S, R-L); ++i) {</pre>
      if(!block[i]) {
        pr.emplace_back((L + i) * 2 + 1);
 for(int i: pr) {
   isPrime[i] = 1;
 return pr;
GolbatchConjecture.hpp
Description: Find two prime numbers which sum equals s
Time: \mathcal{O}(N \log N)
"FastEratosthenes.hpp"
                                                       88fb23, 18 lines
pair<int, int> goldbatchConjecture(int s, vi pr = {}) {
 if (s <= 2 || s % 2 != 0) {
    return make_pair(-1, -1);
 if (pr.size() == 0) {
   pr = eratosthenes();
 for (auto x : pr) {
    if (x > s / 2) {
      break;
    int d = s - x;
    if (binary_search(pr.begin(), pr.end(), d)) {
      return make_pair(min(x, d), max(x, d));
 return make_pair(-1, -1);
```

Graph (6)

6.1 Matching

Hopcroft Karp.hpp

Description: Fast bipartite matching algorithm.

```
Time: \mathcal{O}\left(E\sqrt{V}\right)
"../template/Header.hpp"
```

```
0bd56f, 52 lines
struct HopcroftKarp{
    int n, m;
    vi l,r,lv,ptr;
    vector<vi> adj;
   HopcroftKarp(){}
   HopcroftKarp(int _n,int _m){init(_n,_m);}
    void init(int _n,int _m) {
        n=_n, m=_m;
        adj.assign(n+m, vi{});
   void addEdge(int u,int v) {
        adj[u].emplace_back(v+n);
   void bfs() {
        lv=vi(n,-1);
        queue<int> q;
        for (int i=0; i<n; i++) if (1[i]==-1) {</pre>
            lv[i]=0;
             q.emplace(i);
```

```
while(!q.empty()){
             int u=q.front();
             q.pop();
             for(int v:adj[u])if(r[v]!=-1&&lv[r[v]]==-1){
                 lv[r[v]]=lv[u]+1;
                 q.emplace(r[v]);
    bool dfs(int u) {
        for(int &i=ptr[u];i<sz(adj[u]);i++) {</pre>
            int v=adj[u][i];
            if(r[v]==-1||(lv[r[v]]==lv[u]+1&&dfs(r[v]))){
                 l[u]=v,r[v]=u;
                 return true;
        return false:
    int maxMatching() {
        int match=0, cnt=0;
        l=r=vi(n+m,-1);
             ptr=vi(n);
            bfs();
            cnt=0;
            for (int i=0; i<n; i++) if (l[i] ==-1&&dfs(i)) cnt++;</pre>
        }while(cnt);
        return match;
};
```

Kuhn.hpp

Description: Kuhn Algorithm to find maximum bipartite matching or find augmenting path in bipartite graph.

```
Time: \mathcal{O}(VE)
"../template/Header.hpp"
```

```
fc7d17, 15 lines
```

7409c7, 68 lines

```
vi adj[1010], match(1010, -1);
bitset<1010> visited:
bool kuhn(int u)
  if(visited[u])
    return false:
  visited[u] = true;
  for(auto x: adj[u]) {
    if(match[x] == -1 \mid \mid kuhn(match[x]))  {
      match[x] = u;
      return true;
  return false;
```

Network Flow

Dinic.hpp

"../template/Header.hpp"

Description: Fast max-flow algorithm. **Time:** $\mathcal{O}(VE \log U)$ where $U = \max |\operatorname{cap}|$

return cap-flow;

```
template<class T>
struct Dinic{
    struct Edge {
        int to;
        11 flow, cap;
        Edge(int _to,ll _cap):to(_to),flow(0),cap(_cap){}
        11 getcap() {
```

struct MinCostFlow{

```
};
    int n:
    11 U;
    vector<Edge> e;
    vector<vi> adj;
   vi ptr, lvl;
   Dinic(){}
   Dinic(int _n) {
       init(_n);
   void init(int _n){
       n=_n, U=0;
        e.clear();
        adj.assign(n,{});
   void addEdge(int u,int v,ll cap){
        U=max(U,cap);
        adj[u].emplace_back(sz(e));
        e.emplace_back(v,cap);
        adj[v].emplace_back(sz(e));
        e.emplace_back(u,0); // change 0 to cap for undirected
   bool bfs(int s,int t,ll scale) {
       lvl.assign(n,0);
       vi q{s};
       lvl[s]=1;
        for(int i=0;i<sz(q);i++){</pre>
            int u=q[i];
            for(auto j:adj[u])if(!lvl[e[j].to]&&e[j].getcap()>=
                q.emplace_back(e[j].to);
                lvl[e[j].to]=lvl[u]+1;
        return lvl[t];
    11 dfs(int u,int t,ll f){
        if (u==t||!f) return f;
        for(int &i=ptr[u];i<sz(adj[u]);i++) {</pre>
            int j=adj[u][i];
            if(lvl[e[i].to]==lvl[u]+1){
                if(ll p=dfs(e[j].to,t,min(f,e[j].getcap()))){
                     e[i].flow+=p;
                     e[j^1].flow-=p;
                     return p;
        return 0;
    11 flow(int s,int t) {
        11 flow=0;
        for (11 L=111<<(63-_builtin_clz11(U)); L>0; L>>=1) //L =
              1 may be faster but it's O(V^2 E)
        while (bfs(s,t,L)) {
            ptr.assign(n,0);
            while(ll p=dfs(s,t,LINF))flow+=p;
        };
        return flow;
MinCostFlow.hpp
Description: minimum-cost flow algorithm.
Time: \mathcal{O}(FE \log V) where F is max flow.
"../template/Header.hpp"
                                                       8ea1d2, 83 lines
template<class F,class C>
```

```
struct Edge{
    int to:
    F flow, cap;
    C cost;
    Edge(int _to,F _cap,C _cost):to(_to),flow(0),cap(_cap),
         cost(cost){}
    F getcap(){
        return cap-flow;
};
int n;
vector<Edge> e;
vector<vi> adj;
vector<C> pot, dist;
vi pre;
bool neg;
const F FINF=numeric_limits<F>::max()/2;
const C CINF=numeric_limits<C>::max()/2;
MinCostFlow(){}
MinCostFlow(int _n) {
    init(_n);
void init(int n){
    n=_n;
    e.clear();
    adj.assign(n,{});
    neg=false;
void addEdge(int u,int v,F cap,C cost){
    adj[u].emplace_back(sz(e));
    e.emplace_back(v,cap,cost);
    adj[v].emplace_back(sz(e));
    e.emplace_back(u,0,-cost);
    if (cost<0) neg=true;</pre>
bool dijkstra(int s, int t) {
    using P = pair<C,int>;
    dist.assign(n,CINF);
    pre.assign(n,-1);
    priority_queue<P, vector<P>, greater<P>> pq;
    dist[s]=0;
    pg.emplace(0,s);
    while(!pq.empty()){
        auto [d,u]=pq.top();
        pq.pop();
        if (dist[u] < d) continue;</pre>
        for(int i:adj[u]){
             int v=e[i].to;
            C ndist=d+pot[u]-pot[v]+e[i].cost;
            if(e[i].getcap()>0&&dist[v]>ndist){
                 pre[v]=i;
                 dist[v]=ndist;
                 pq.emplace(ndist, v);
    return dist[t] < CINF;</pre>
pair<F,C> flow(int s,int t) {
    F flow=0;
    C cost=0;
    pot.assign(n,0);
    if (neg) for (int t=0; t< n; t++) for (int i=0; i< sz(e); i++) if (e
         [i].getcap()>0){
        int u=e[i^1].to, v=e[i].to;
        pot[v]=min(pot[v],pot[u]+e[i].cost);
    } // Bellman-Ford
    while(dijkstra(s,t)){
         for (int i=0; i < n; i++) pot[i] += dist[i];</pre>
```

Polynomials (7)

FormalPowerSeries.hpp

Description: basic operations of formal power series

```
416433, 136 lines
template < class mint >
struct FormalPowerSeries:vector<mint>{
    using vector<mint>::vector;
    using FPS = FormalPowerSeries;
    FPS & operator += (const FPS & rhs) {
        if (rhs.size()>this->size())this->resize(rhs.size());
        for(int i=0;i<rhs.size();i++)(*this)[i]+=rhs[i];</pre>
        return *this;
    FPS & operator += (const mint &rhs) {
        if(this->empty())this->resize(1);
         (*this) [0] += rhs;
        return *this;
    FPS & operator -= (const FPS & rhs) {
        if (rhs.size()>this->size())this->resize(rhs.size());
        for(int i=0;i<rhs.size();i++)(*this)[i]-=rhs[i];</pre>
        return *this;
    FPS & operator -= (const mint &rhs) {
        if(this->empty())this->resize(1);
        (*this) [0]-=rhs;
        return *this;
    FPS & operator *= (const FPS & rhs) {
        auto res=NTT<mint>() (*this, rhs);
        return *this=FPS(res.begin(), res.end());
    FPS & operator *= (const mint &rhs) {
        for(auto &a:*this)a*=rhs;
        return *this;
    friend FPS operator+(FPS lhs, const FPS &rhs) {return lhs+=
    friend FPS operator+(FPS lhs,const mint &rhs) {return lhs+=
    friend FPS operator+ (const mint &lhs, FPS &rhs) {return rhs+=
    friend FPS operator-(FPS lhs, const FPS &rhs) {return lhs-=
    friend FPS operator-(FPS lhs, const mint &rhs) {return lhs-=
    friend FPS operator-(const mint &lhs, FPS rhs) {return -(rhs-
    friend FPS operator* (FPS lhs, const FPS &rhs) {return lhs*=
```

```
friend FPS operator* (FPS lhs, const mint &rhs) {return lhs*=
     rhs: }
friend FPS operator* (const mint &lhs, FPS rhs) {return rhs*=
     lhs; }
FPS operator-(){return (*this)*-1;}
FPS rev(){
    FPS res(*this);
    reverse(res.beign(),res.end());
    return res;
FPS pre(int sz) {
    FPS res(this->begin(),this->begin()+min((int)this->size
         (),sz));
    if(res.size() < sz) res.resize(sz);</pre>
    return res;
FPS shrink(){
    FPS res(*this);
    while(!res.empty() &&res.back() ==mint{}) res.pop_back();
    return res;
FPS operator>>(int sz){
    if (this->size()<=sz) return {};</pre>
    FPS res(*this);
    res.erase(res.begin(),res.begin()+sz);
    return res;
FPS operator<<(int sz) {</pre>
    FPS res(*this);
    res.insert(res.begin(),sz,mint{});
    return res;
FPS diff() {
    const int n=this->size();
    FPS res(max(0,n-1));
    for (int i=1; i<n; i++) res[i-1] = (*this) [i] *mint(i);</pre>
    return res;
FPS integral(){
    const int n=this->size();
    FPS res(n+1);
    res[0]=0;
    if(n>0)res[1]=1;
    11 mod=mint::get_mod();
    for(int i=2;i<=n;i++)res[i]=(-res[mod%i])*(mod/i);</pre>
    for (int i=0; i<n; i++) res[i+1] *= (*this)[i];</pre>
    return res;
mint eval(const mint &x) {
    mint res=0, w=1;
    for(auto &a:*this) res+=a*w, w*=x;
    return res:
FPS inv(int deg=-1) {
    assert(!this->empty()&&(*this)[0]!=mint(0));
    if (deg==-1) deg=this->size();
    FPS res{mint(1)/(*this)[0]};
    for(int i=2;i>>1<deq;i<<=1){</pre>
         res=(res*(mint(2)-res*pre(i))).pre(i);
    return res.pre(deg);
FPS log(int deg=-1){
    assert (!this->empty() && (*this) [0] ==mint(1));
    if (deg==-1) deg=this->size();
```

```
return (pre(deg).diff()*inv(deg)).pre(deg-1).integral()
    FPS exp(int deg=-1) {
         assert (this->empty() | | (*this) [0] ==mint(0));
         if (deg==-1) deg=this->size();
         FPS res{mint(1)};
         for (int i=2;i>>1<deq;i<<=1) {</pre>
             res=(res*(pre(i)-res.log(i)+mint(1))).pre(i);
         return res.pre(deg);
    FPS pow(11 k,int deg=-1){
         const int n=this->size();
         if (deg==-1) deg=n;
        if(k==0){
             FPS res(deg);
             if (deg) res[0]=mint(1);
             return res;
         for (int i=0; i<n; i++) {</pre>
             if (__int128_t(i)*k>=deg) return FPS(deg, mint(0));
             if((*this)[i]==mint(0))continue;
             mint rev=mint(1)/(*this)[i];
             FPS res=(((*this*rev)>>i).log(deg)*k).exp(deg);
             res=((res*binpow((*this)[i],k))<<(i*k)).pre(deg);
             return res;
         return FPS(deg,mint(0));
using FPS=FormalPowerSeries<mint>;
FFT.hpp
Description: Fast Fourier transform
Time: \mathcal{O}(N \log N)
"../template/Header.hpp"
                                                         5d476b, 73 lines
template<class T=11,int mod=0>
struct FFT{
  using vt = vector<T>;
  using cd = complex<db>;
  using vc = vector<cd> ;
  static const bool INT=true;
  static void fft(vc &a){
    int n=a.size(),L=31-__builtin_clz(n);
    vc rt(n);
    rt[1]=1;
    for (int k=2; k<n; k*=2) {</pre>
      cd z=polar(db(1),PI/k);
      for(int i=k;i<2*k;i++)rt[i]=i&1?rt[i/2]*z:rt[i/2];</pre>
    vi rev(n);
    for (int i=1; i<n; i++) rev[i] = (rev[i/2] | (i&1) <<L) /2;</pre>
    for (int i=1; i<n; i++) if (i<rev[i]) swap (a[i], a[rev[i]]);</pre>
    for (int k=1; k < n; k *=2) for (int i=0; i < n; i+2 *k) for (int j=0; j < k
         ; j++) {
      cd z=rt[j+k]*a[i+j+k];
      a[i+j+k]=a[i+j]-z;
      a[i+j]+=z;
  template<class U>
  static db norm(const U &x) {
    return INT?round(x):x;
  static vt conv(const vt &a, const vt &b) {
    if(a.empty()||b.empty())return {};
```

```
vt res(a.size()+b.size()-1);
    int L=32-__builtin_clz(res.size()), n=1<<L;</pre>
    vc in(n), out(n);
    copy(a.begin(),a.end(),in.begin());
    for(int i=0;i<b.size();i++)in[i].imag(b[i]);</pre>
    fft (in):
    for(auto &x:in)x*=x;
    for(int i=0;i<n;i++)out[i]=in[-i&(n-1)]-conj(in[i]);</pre>
    for (int i=0;i<res.size();i++) res[i]=norm(imag(out[i])/(4*n)</pre>
         );
    return res;
  static vl convMod(const vl &a,const vl &b) {
    assert (mod>0);
    if(a.empty()||b.empty())return {};
    vl res(a.size()+b.size()-1);
    int L=32-__builtin_clz(res.size()), n=1<<L;</pre>
    11 cut=int(sqrt(mod));
    vc in1(n),in2(n),out1(n),out2(n);
    for (int i=0; i<a.size(); i++) in1[i]=cd(l1(a[i])/cut,l1(a[i])%</pre>
          cut); // a1 + i * a2
    for(int i=0;i<b.size();i++)in2[i]=cd(ll(b[i])/cut,ll(b[i])%</pre>
          cut); // b1 + i * b2
    fft(in1), fft(in2);
    for(int i=0;i<n;i++) {</pre>
      int j=-i&(n-1);
      out1[j]=(in1[i]+conj(in1[j]))*in2[i]/(2.1*n); // f1 * (g1)
             + i * g2) = f1 * g1 + i f1 * g2
      out2[j]=(in1[i]-conj(in1[j]))*in2[i]/cd(0.1,2.1*n); // f2
             * (g1 + i * g2) = f2 * g1 + i f2 * g2
    fft (out1), fft (out2);
    for(int i=0;i<res.size();i++){</pre>
      11 x=round(real(out1[i])),y=round(imag(out1[i]))+round(
            real(out2[i])), z=round(imag(out2[i]));
      res[i] = ((x \mod \cot + y) \mod \cot + z) \mod; // a1 * b1 * cut^2
            + (a1 * b2 + a2 * b1) * cut + a2 * b2
    return res;
  vt operator()(const vt &a,const vt &b){
    return mod>0?conv(a,b):convMod(a,b);
};
template<>
struct FFT<db>{
  static const bool INT=false;
NTT.hpp
Description: Number theoretic transform
Time: \mathcal{O}(N \log N)
"../template/Header.hpp", "../modular-arithmetic/BinPow.hpp",
"../modular-arithmetic/MontgomeryModInt.hpp"
                                                        2b2392, 39 lines
template < class mint = mint >
struct NTT{
  using vm = vector<mint>;
  static constexpr mint root=mint::get_root();
    static_assert(root!=0);
  static void ntt(vm &a){
    int n=a.size(),L=31-__builtin_clz(n);
    vm rt(n);
    rt[1]=1;
    for (int k=2, s=2; k < n; k * = 2, s++) {
      mint z[]={1,binpow(root,MOD>>s)};
      for (int i=k; i<2*k; i++) rt[i]=rt[i/2]*z[i&1];</pre>
```

DVC SlopeTrick GaussianElimination BinaryTrie

```
vi rev(n):
    for(int i=1;i<n;i++)rev[i]=(rev[i/2]|(i&1)<<L)/2;</pre>
    for (int i=1; i < n; i++) if (i < rev[i]) swap (a[i], a[rev[i]]);</pre>
    for (int k=1; k < n; k \neq 2) for (int i=0; i < n; i+2 \neq k) for (int j=0; j < k
     mint z=rt[j+k]*a[i+j+k];
     a[i+j+k] = a[i+j]-z;
      a[i+j]+=z;
  static vm conv(const vm &a,const vm &b) {
    if(a.empty()||b.empty())return {};
    int s=a.size()+b.size()-1, n=1<<(32-__builtin_clz(s));</pre>
    mint inv=mint(n).inv();
    vm in1(a),in2(b),out(n);
    in1.resize(n),in2.resize(n);
    ntt(in1),ntt(in2);
    for (int i=0; i < n; i++) out [-i&(n-1)] = in1[i] * in2[i] * inv;</pre>
    nt.t.(out.):
    return vm(out.begin(),out.begin()+s);
  vm operator()(const vm &a,const vm &b){
    return conv(a,b);
};
Dynamic Programming (8)
DVC.hpp
Description: Optimize O(N^2K) to O(NK \log N)
"../template/Header.hpp"
                                                        aa5ddf, 19 lines
vector<vl> cst, dp;
11 cost(int 1, int r) {
 return cst[l][r];
void divide(int 1, int r, int opt_1, int opt_r, int c) {
 if(1 > r) return ;
  int mid = (1 + r) / 2;
  pair<11, int> best = make_pair(INF, -1);
  for(int k=opt_l; k<=min(mid, opt_r); ++k) {</pre>
   best = min(best, make_pair(dp[c - 1][k] + cost(k + 1, mid),
          k));
  dp[c][mid] = best.first;
  divide(1, mid - 1, opt_1, best.second, c);
  divide (mid + 1, r, best.second, opt_r, c);
// for(int c=1; c \le K; ++c) divide(1, N, 1, N, c);
SlopeTrick.hpp
Description: Absolute Smth
"../template/Header.hpp"
                                                        f62f9a, 36 lines
11 extending value;
struct slope_trick {
  multiset<11> ms_1, ms_r;
  11 \min_{y} = 011, 1z_1 = 011, 1z_r = 011;
  bool extending = false;
  void add_line(ll v) {
    if(extending) {
      lz 1 -= extending value;
      lz_r -= extending_value;
```

```
extending = true;
    if(ms_1.empty() && ms_r.empty()) {
     ms l.emplace(v);
     ms_r.emplace(v);
    else if(v <= *ms_l.rbegin() + lz_l) {</pre>
     min_y += (*ms_l.rbegin() + lz_l) - v;
     ms_r.emplace(*ms_l.rbegin() + lz_l - lz_r);
     ms_l.erase(--ms_l.end());
     ms_l.emplace(v - lz_l);
     ms_l.emplace(v - lz_l);
    else if(v >= *ms_r.begin() + lz_r) {
     min_y += v - (*ms_r.begin() + lz_r);
     ms_l.emplace(*ms_r.begin() + lz_r - lz_l);
     ms_r.erase(ms_r.begin());
     ms_r.emplace(v - lz_r);
     ms_r.emplace(v - lz_r);
    else {
     ms_1.emplace(v - lz_1);
     ms_r.emplace(v - lz_r);
};
```

8.1 Various

```
Gaussian Elimination.hpp
Description: Gaussian Elimination
```

```
e89ecb, 34 lines
"../template/Header.hpp"
struct Gauss {
 int n, sz;
 vector<ll> basis;
 Gauss(int n = 0) {
    init(n):
 void init(int _n) {
   n = n, sz = 0;
    basis.assign(n, 0);
 void insert(ll x) {
    for (int i = n - 1; i >= 0; i--)
      if (x >> i & 1) {
        if (!basis[i]) {
          basis[i] = x:
          sz++;
          return;
          ^= basis[i];
 ll \ getmax(ll \ k = 0)  {
    11 \text{ tot} = 111 << sz, res = 0;
    for (int i = n - 1; i >= 0; i--)
      if (basis[i]) {
        tot >>= 1;
        if ((k >= tot && res >> i & 1) || (k < tot && res >> i
             & 1 ^ 1))
          res ^= basis[i];
        if (k >= tot)
          k -= tot;
    return res;
};
```

```
Description: Binary Trie
"../template/Header.hpp"
                                                      525bf4, 59 lines
using node_t = array<int, 2>;
template<size t S>
struct binary trie {
 vector<node_t> t = {node_t()};
  vector<int> cnt = {0};
 int cnt_nodes = 0;
 void insert(int v)
    int cur = 0;
    cnt[0]++;
    for(int i=S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1: 0;
      if(!t[cur][b]) {
       t[cur][b] = ++cnt_nodes;
        t.emplace_back(node_t());
        cnt.emplace_back(0);
      cnt[t[cur][b]]++;
      cur = t[cur][b];
 void remove(int v) {
    int cur = 0;
    cnt[01--;
    for(int i=S-1; i>=0; --i) {
      int b = (v & (1 << i)) ? 1: 0;
      cnt[t[cur][b]]--;
      cur = t[cur][b];
  int get_min(int v) {
    int cur = 0, res = 0;
    for(int i=(int) S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1 : 0;
      if(t[cur][b] && cnt[t[cur][b]]) {
        cur = t[cur][b];
      else {
        res |= (1 << i);
        cur = t[cur][!b];
    return res;
  int get max(int v) {
    int cur = 0, res = 0;
    for(int i=(int) S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1 : 0;
      if(t[cur][!b] && cnt[t[cur][!b]]) {
        res |= (1 << i);
        cur = t[cur][!b];
      else {
        cur = t[cur][b];
    return res;
};
```

BinaryTrie.hpp

Log partitioning (loop over most restricted)

Competitive Programming Topics



topics.txt

159 lines

Recursion Divide and conquer Finding interesting points in N log N Algorithm analysis Master theorem Amortized time complexity Greedy algorithm Scheduling Max contiguous subvector sum Invariants Huffman encoding Graph theory Dynamic graphs (extra book-keeping) Breadth first search Depth first search * Normal trees / DFS trees Dijkstra's algorithm MST: Prim's algorithm Bellman-Ford Konig's theorem and vertex cover Min-cost max flow Lovasz toggle Matrix tree theorem Maximal matching, general graphs Hopcroft-Karp Hall's marriage theorem Graphical sequences Flovd-Warshall Euler cycles Flow networks * Augmenting paths * Edmonds-Karp Bipartite matching Min. path cover Topological sorting Strongly connected components Cut vertices, cut-edges and biconnected components Edge coloring * Trees Vertex coloring * Bipartite graphs (=> trees) * 3^n (special case of set cover) Diameter and centroid K'th shortest path Shortest cycle Dynamic programming Knapsack Coin change Longest common subsequence Longest increasing subsequence Number of paths in a dag Shortest path in a dag Dynprog over intervals Dynprog over subsets Dynprog over probabilities Dynprog over trees 3^n set cover Divide and conquer Knuth optimization Convex hull optimizations

RMQ (sparse table a.k.a 2^k-jumps)

Bitonic cycle

Combinatorics Computation of binomial coefficients Pigeon-hole principle Inclusion/exclusion Catalan number Pick's theorem Number theory Integer parts Divisibility Euclidean algorithm Modular arithmetic * Modular multiplication * Modular inverses * Modular exponentiation by squaring Chinese remainder theorem Fermat's little theorem Euler's theorem Phi function Frobenius number Quadratic reciprocity Pollard-Rho Miller-Rabin Hensel lifting Vieta root jumping Game theory Combinatorial games Game trees Mini-max Nim Games on graphs Games on graphs with loops Grundy numbers Bipartite games without repetition General games without repetition Alpha-beta pruning Probability theory Optimization Binary search Ternary search Unimodality and convex functions Binary search on derivative Numerical methods Numeric integration Newton's method Root-finding with binary/ternary search Golden section search Matrices Gaussian elimination Exponentiation by squaring Sorting Radix sort Geometry Coordinates and vectors * Cross product * Scalar product Convex hull Polygon cut Closest pair Coordinate-compression Quadtrees KD-trees All segment-segment intersection Discretization (convert to events and sweep) Angle sweeping Line sweeping Discrete second derivatives Strings

Longest common substring Palindrome subsequences Knuth-Morris-Pratt Tries Rolling polynomial hashes Suffix array Suffix tree Aho-Corasick Manacher's algorithm Letter position lists Combinatorial search Meet in the middle Brute-force with pruning Best-first (A*) Bidirectional search Iterative deepening DFS / A* Data structures LCA (2^k-jumps in trees in general) Pull/push-technique on trees Heavy-light decomposition Centroid decomposition Lazy propagation Self-balancing trees Convex hull trick (wcipeg.com/wiki/Convex_hull_trick) Monotone queues / monotone stacks / sliding queues Sliding queue using 2 stacks Persistent segment tree

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