



Chulalongkorn University

Vaporised

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template from KACTL

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```

        if(x<1||r<x) return;
        if(l==r) return void(t[i]=Monoid::op(t[i],v));
        int m=(l+r)/2;
        update(l,m,i*2,x,v);
        update(m+1,r,i*2+1,x,v);
        pull(i);
    }
    template<class U>
    void update(int x,const U &v){
        update(0,n-1,l,x,v);
    }
    T query(int l,int r,int i,int x,int y){
        if(y<1||r<x) return Monoid::unit();
        if(x<=l&&r<=y) return t[i];
        int m=(l+r)/2;
        return Monoid::op(query(l,m,i*2,x,y),query(m+1,r,i*2+1,x,y));
    }
    T query(int x,int y){
        return query(0,n-1,l,x,y);
    }
    template<class F>
    int findfirst(int l,int r,int i,int x,int y,const F &f){
        if(y<1||r<x||!f(t[i])) return n;
        if(l==r) return l;
        int m=(l+r)/2;
        int res=findfirst(l,m,i*2,x,y,f);
        if(res==n) res=findfirst(m+1,r,i*2+1,x,y,f);
        return res;
    }
    template<class F>
    int findfirst(int x,int y,const F &f){
        return findfirst(0,n-1,l,x,y,f);
    }
    template<class F>
    int findlast(int l,int r,int i,int x,int y,const F &f){
        if(y<1||r<x||!f(t[i])) return -1;
        if(l==r) return l;
        int m=(l+r)/2;
        int res=findlast(m+1,r,i*2+1,x,y,f);
        if(res==-1) res=findlast(l,m,i*2,x,y,f);
        return res;
    }
    template<class F>
    int findlast(int x,int y,const F &f){
        return findlast(0,n-1,l,x,y,f);
    }
};

```

LazySegmentTree.hpp

Description: Segment Tree with Lazy Propagation

91ab0c, 103 lines

```

template<class MonoidAction>
struct LazySegmentTree{
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    int n;
    vector<Info> t;
    vector<Tag> lz;
    LazySegmentTree(){}
    LazySegmentTree(int n,function<Info(int)> create){init(n,create);}
    LazySegmentTree(int n,Info v=InfoMonoid::unit()){init(n,[&](int){return v;});}
    template<class T>
    LazySegmentTree(const vector<T> &a){init((int)a.size(),[&](int i){return Info(a[i]);});}
};

```

```

void init(int _n,function<Info(int)> create){
    n=_n;
    int m=4<<(31-__builtin_clz(n));
    t.assign(m,InfoMonoid::unit());
    lz.assign(m,TagMonoid::unit());
    function<void(int,int,int)> build=[&](int l,int r,int i){
        if(l==r) return void(t[i]=create(l));
        int m=(l+r)/2;
        build(l,m,i*2);
        build(m+1,r,i*2+1);
        pull(i);
    };
    build(0,n-1,1);
}
void pull(int i){
    t[i]=InfoMonoid::op(t[i*2],t[i*2+1]);
}
void apply(int i,const Tag &v){
    t[i]=MonoidAction::op(t[i],v);
    lz[i]=TagMonoid::op(lz[i],v);
}
void push(int i){
    apply(i*2,lz[i]);
    apply(i*2+1,lz[i]);
    lz[i]=TagMonoid::unit();
}
void modify(int l,int r,int i,int x,const Info &v){
    if(x<1||r<x) return;
    if(l==r) return void(t[i]=v);
    int m=(l+r)/2;
    push(i);
    modify(l,m,i*2,x,v);
    modify(m+1,r,i*2+1,x,v);
    pull(i);
}
void modify(int x,const Info &v){
    modify(0,n-1,l,x,v);
}
void update(int l,int r,int i,int x,int y,const Tag &v){
    if(y<1||r<x) return;
    if(x<=l&&r<=y) return apply(i,v);
    int m=(l+r)/2;
    push(i);
    update(l,m,i*2,x,y,v);
    update(m+1,r,i*2+1,x,y,v);
    pull(i);
}
void update(int x,int y,const Tag &v){
    update(0,n-1,l,x,y,v);
}
Info query(int l,int r,int i,int x,int y){
    if(y<1||r<x) return InfoMonoid::unit();
    if(x<=l&&r<=y) return t[i];
    int m=(l+r)/2;
    push(i);
    return InfoMonoid::op(query(l,m,i*2,x,y),query(m+1,r,i*2+1,x,y));
}
Info query(int x,int y){
    return query(0,n-1,l,x,y);
}
template<class F>
int findfirst(int l,int r,int i,int x,int y,const F &f){
    if(y<1||r<x||!f(t[i])) return n;
    if(l==r) return l;
    int m=(l+r)/2;
    push(i);
    int res=findfirst(l,m,i*2,x,y,f);
    int res=findfirst(m+1,r,i*2+1,x,y,f);
    return res;
}

```

```

        if(res==n) res=findfirst(m+1,r,i*2+1,x,y,f);
        return res;
    }
    template<class F>
    int findfirst(int x,int y,const F &f){
        return findfirst(0,n-1,l,x,y,f);
    }
    template<class F>
    int findlast(int l,int r,int i,int x,int y,const F &f){
        if(y<1||r<x||!f(t[i])) return -1;
        if(l==r) return l;
        int m=(l+r)/2;
        push(i);
        int res=findlast(m+1,r,i*2+1,x,y,f);
        if(res==-1) res=findlast(l,m,i*2,x,y,f);
        return res;
    }
    template<class F>
    int findlast(int x,int y,const F &f){
        return findlast(0,n-1,l,x,y,f);
    }
};

```

DynamicSegmentTree.hpp

Description: Dynamic Segment Tree

e84eeb, 106 lines

```

template<class MonoidAction>
struct DynamicSegmentTree{
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    struct Node;
    using Ptr = Node*;
    struct Node{
        Info val;
        Tag lz;
        Ptr l,r;
        Node(Info v):val(v),lz(TagMonoid::unit()),l(nullptr),r(nullptr){}
        Node(Info v,Tag t):val(v),lz(t),l(nullptr),r(nullptr){}
    };
    ll lb,ub;
    Ptr rt;
    function<Info(ll,ll)> create;
    DynamicSegmentTree() {init(0,0);}
    DynamicSegmentTree(ll n) {init(0,n-1);}
    DynamicSegmentTree(ll lb,ll ub) {init(lb,ub);}
    DynamicSegmentTree(ll lb,ll ub,function<Info(ll,ll)> create) {init(lb,ub,create);}
    void init(ll _lb,ll _ub,function<Info(ll,ll)> _create=[&](ll l,ll r){return InfoMonoid::unit();}){
        lb=_lb,ub=_ub;
        create=_create;
        rt=new Node(create(lb,ub));
    }
    Info val(Ptr t){
        return t?t->val:InfoMonoid::unit();
    }
    void pull(Ptr &t){
        t->val=InfoMonoid::op(val(t->l),val(t->r));
    }
    void apply(Ptr &t,const Tag &v,ll l,ll r){
        if(!t)t=new Node(create(l,r));
        t->val=MonoidAction::op(t->val,v);
        t->lz=TagMonoid::op(t->lz,v);
    }
    void push(Ptr &t,ll l,ll m,ll r){
        apply(t->l,t->lz,l,m);
    }
};

```

```

        apply(t->r,t->lz,m+1,r);
        t->lz=TagMonoid::unit();
    }
    void modify(ll l,ll r,Ptr &t,ll x,const Info &v){
        if(x<l||r<x)return;
        if(l==r)return void(t->val=v);
        ll m=l+(r-l)/2;
        push(t,l,m,r);
        modify(l,m,t->l,x,v);
        modify(m+1,r,t->r,x,v);
        pull(t);
    }
    void modify(ll x,const Info &v){
        modify(lb,ub,rt,x,v);
    }
    void update(ll l,ll r,Ptr &t,ll x,ll y,const Tag &v){
        if(y<l||r<x)return;
        if(x<=l&&r<=y)return apply(t,v,l,r);
        ll m=l+(r-l)/2;
        push(t,l,m,r);
        update(l,m,t->l,x,y,v);
        update(m+1,r,t->r,x,y,v);
        pull(t);
    }
    void update(ll x,ll y,const Tag &v){
        update(lb,ub,rt,x,y,v);
    }
    Info query(ll l,ll r,Ptr &t,ll x,ll y){
        if(y<l||r<x)return InfoMonoid::unit();
        if(x<=l&&r<=y)return t->val;
        ll m=l+(r-l)/2;
        push(t,l,m,r);
        return InfoMonoid::op(query(l,m,t->l,x,y),query(m+1,r,t->r,x,y));
    }
    Info query(ll x,ll y){
        return query(lb,ub,rt,x,y);
    }
    template<class F>
    ll findfirst(ll l,ll r,Ptr t,ll x,ll y,const F &f){
        if(y<l||r<x||!f(t->val))return -1;
        if(l==r)return l;
        ll m=l+(r-l)/2;
        push(t,l,m,r);
        ll res=findfirst(l,m,t->l,x,y,f);
        if(res==-1)res=findfirst(m+1,r,t->r,x,y,f);
        return res;
    }
    template<class F>
    ll findfirst(ll x,ll y,const F &f){
        return findfirst(lb,ub,rt,x,y,f);
    }
    template<class F>
    ll findlast(ll l,ll r,Ptr t,ll x,ll y,const F &f){
        if(y<l||r<x||!f(t->val))return -1;
        if(l==r)return l;
        ll m=l+(r-l)/2;
        push(t,l,m,r);
        ll res=findlast(m+1,r,t->r,x,y,f);
        if(res==-1)res=findlast(l,m,t->l,x,y,f);
        return res;
    }
    template<class F>
    ll findlast(ll x,ll y,const F &f){
        return findlast(lb,ub,rt,x,y,f);
    }
};

```

DSU.hpp

Description: Disjoint Set Union.

0b3cb8, 26 lines

```

struct DSU{
    vector<int> p,sz;
    DSU(){}
    DSU(int n){init(n);}
    void init(int n){
        p.resize(n);
        iota(p.begin(),p.end(),0);
        sz.assign(n,1);
    }
    int find(int u){
        return p[u]==u?p[u]=find(p[u]);
    }
    bool same(int u,int v){
        return find(u)==find(v);
    }
    bool merge(int u,int v){
        u=find(u),v=find(v);
        if(u==v)return false;
        sz[u]+=sz[v];
        p[v]=u;
        return true;
    }
    int size(int u){
        return sz[find(u)];
    }
};

```

BinaryTrie.hpp

Description: Binary Trie

ae5b7a, 66 lines

```

template<int BIT,class T = uint32_t,class S = int>
struct BinaryTrie{
    struct Node{
        array<int,2> ch;
        S cnt;
        Node():ch{-1,-1},cnt(0){}
    };
    vector<Node> t;
    BinaryTrie():t{(Node())}{}
    int new_node(){
        t.emplace_back(Node());
        return t.size()-1;
    }
    S size(){
        return t[0].cnt;
    }
    bool empty(){
        return size()==0;
    }
    S get_cnt(int i){
        return i!=-1?t[i].cnt:S(0);
    }
    void insert(T x,S k=1){
        int u=0;
        t[u].cnt+=k;
        for(int i=BIT-1;i>=0;i--){
            int v=x>>i&1;
            if(t[u].ch[v]==-1)t[u].ch[v]=new_node();
            u=t[u].ch[v];
            t[u].cnt+=k;
        }
    }
    void erase(T x,S k=1){
        int u=0;
        assert(t[u].cnt>=k);
        t[u].cnt-=k;
        for(int i=BIT-1;i>=0;i--){

```

```

            int v=x>>i&1;
            u=t[u].ch[v];
            assert(u!=-1&&t[u].cnt>=k);
            t[u].cnt-=k;
        }
    }
    T kth(S k,T x=0){
        assert(k<size());
        int u=0;
        T res=0;
        for(int i=BIT-1;i>=0;i--){
            int v=x>>i&1;
            if(k<get_cnt(t[u].ch[v])){
                u=t[u].ch[v];
            }else{
                res|=T(1)<<i;
                k-=get_cnt(t[u].ch[v]);
                u=t[u].ch[v^1];
            }
        }
        return res;
    }
    T min(T x){
        return kth(0,x);
    }
    T max(T x){
        return kth(size()-1,x);
    }
};

```

LiChaoTree.hpp

Description: Li-Chao Tree (minimize).

4ab713, 52 lines

```

template<class T>
struct LiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line{
        T m,c;
        Line(T _m,T _c):m(_m),c(_c){}
        inline T eval(T x)const{return m*x+c;}
    };
    vector<T> xs;
    vector<Line> t;
    LiChaoTree(){}
    LiChaoTree(const vector<T> &xs):xs(x){init(x);}
    LiChaoTree(int n):xs(n){
        vector<T> x(n);
        iota(x.begin(),x.end(),0);
        init(x);
    }
    void init(const vector<T> &x){
        xs=x;
        sort(xs.begin(),xs.end());
        xs.erase(unique(xs.begin(),xs.end()),xs.end());
        t.assign(4<<(31-__builtin_clz(xs.size())),Line(0,INF));
    }
    void insert(int l,int r,int i,Line v){
        int m=(l+r)/2;
        if(v.eval(xs[m])<t[i].eval(xs[m]))swap(t[i],v);
        if(v.eval(xs[l])<t[i].eval(xs[l]))insert(l,m,i*2,v);
        if(v.eval(xs[r])<t[i].eval(xs[r]))insert(m+1,r,i*2+1,v);
    }
    inline void insert(T m,T c){
        insert(0,(int)xs.size()-1,l,Line(m,c));
    }
    void insert_range(int l,int r,int i,T x,T y,Line v){
        if(y<xs[l]||xs[r]<x)return;
        if(x<=xs[l]&&xs[r]<=y)return insert(l,r,i,v);
    }
};

```

```
        int m=(l+r)/2;
        insert_range(l,m,i*2,x,y,v);
        insert_range(m+1,r,i*2+1,x,y,v);
    }
    inline void insert_range(T m,T c,T x,T y){
        insert_range(0,(int)xs.size()-1,l,x,y,Line(m,c));
    }
    T query(int l,int r,int i,T x){
        if(l==r)return t[i].eval(x);
        int m=(l+r)/2;
        if(x<=xs[m])return min(t[i].eval(x),query(l,m,i*2,x));
        return min(t[i].eval(x),query(m+1,r,i*2+1,x));
    }
    inline T query(T x){
        return query(0,(int)xs.size()-1,l,x);
    }
};
```

DynamicLiChaoTree.hpp

Description: Dynamic Li-Chao Tree (minimize).

b8af36, 50 lines

```
template<class T>
struct DynamicLiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line{
        T m,c;
        Line(T _m,T _c):m(_m),c(_c){}
        inline T eval(T x){const{return m*x+c;}}
    };
    struct Node;
    using Ptr = Node*;
    struct Node{
        Line v;
        Ptr l,r;
        Node():v(0,INF),l(nullptr),r(nullptr){}
        Node(Line _v):v(_v),l(nullptr),r(nullptr){}
    };
    ll lb,ub;
    Ptr root;
    DynamicLiChaoTree(ll _lb,ll _ub):lb(_lb),ub(_ub),root(nullptr){}
    void insert(T l,T r,Ptr &t,Line v){
        if(!t)return void(t=new Node(v));
        T m=l+(r-l)/2;
        if(v.eval(m)<t->v.eval(m))swap(t->v,v);
        if(v.eval(l)<t->v.eval(l))insert(l,m,t->l,v);
        if(v.eval(r)<t->v.eval(r))insert(m+1,r,t->r,v);
    }
    inline void insert(T m,T c){
        insert(lb,ub,root,Line(m,c));
    }
    void insert_range(T l,T r,Ptr &t,T x,T y,Line v){
        if(y<l||r<x)return;
        if(!t)t=new Node();
        if(x<=l&&r<=y)return insert(l,r,t,v);
        T m=l+(r-l)/2;
        insert_range(l,m,t->l,x,y,v);
        insert_range(m+1,r,t->r,x,y,v);
    }
    inline void insert_range(T m,T c,T x,T y){
        insert_range(lb,ub,root,x,y,Line(m,c));
    }
    T query(T l,T r,Ptr t,T x){
        if(!t)return INF;
        T m=l+(r-l)/2;
        if(x<=m)return min(t->v.eval(x),query(l,m,t->l,x));
        return min(t->v.eval(x),query(m+1,r,t->r,x));
    }
    inline T query(T x){
```

```
        return query(lb,ub,root,x);
    }
};

SplayTreeBase.hpp
Description: Splay Tree. splay(u) will make node u be the root of the tree
in amortized O(log n) time.
cc90a9, 113 lines

template<class Node>
struct SplayTreeBase{
    using Ptr = Node*;
    bool is_root(Ptr t){
        return !(t->p)|| (t->p->l!=t&&t->p->r!=t);
    } // The parent of the root stores the path parant in link
        cut tree.
    int size(Ptr t){
        return t?t->size:0;
    }
    virtual void push(Ptr t){};
    virtual void pull(Ptr t){};
    int pos(Ptr t){
        if(t->p){
            if(t->p->l==t)return -1;
            if(t->p->r==t)return 1;
        }
        return 0;
    }
    void rotate(Ptr t){
        Ptr x=t->p,y=x->p;
        if(pos(t)==-1){
            if((x->l==t->r))t->r->p=x;
            t->r=x,x->p=t;
        }else{
            if((x->r==t->l))t->l->p=x;
            t->l=x,x->p=t;
        }
        pull(x),pull(t);
        if((t->p==y)){
            if(y->l==x)y->l=t;
            if(y->r==x)y->r=t;
        }
    }
    void splay(Ptr t){
        if(!t)return;
        push(t);
        while(!is_root(t)){
            Ptr x=t->p;
            if(is_root(x)){
                push(x),push(t);
                rotate(t);
            }else{
                Ptr y=x->p;
                push(y),push(x),push(t);
                if(pos(x)==pos(t))rotate(x),rotate(t);
                else rotate(t),rotate(t);
            }
        }
    }
    Ptr get_first(Ptr t){
        while(t->l)push(t),t=t->l;
        splay(t);
        return t;
    }
    Ptr get_last(Ptr t){
        while(t->r)push(t),t=t->r;
        splay(t);
        return t;
    }
    Ptr merge(Ptr l,Ptr r){
```

```
        splay(l),splay(r);
        if(!l)return r;
        if(!r)return l;
        l=get_last(l);
        l->r=r;
        r->p=l;
        pull(l);
        return l;
    }
    pair<Ptr,Ptr> split(Ptr t,int k){
        if(!t)return {nullptr,nullptr};
        if(k==0)return {nullptr,t};
        if(k==size(t))return {t,nullptr};
        push(t);
        if(k<=size(t->l)){
            auto x=split(t->l,k);
            t->l=x.second;
            t->p=nullptr;
            if(x.second)x.second->p=t;
            pull(t);
            return {x.first,t};
        }else{
            auto x=split(t->r,k-size(t->l)-1);
            t->r=x.first;
            t->p=nullptr;
            if(x.first)x.first->p=t;
            pull(t);
            return {t,x.second};
        }
    }
    void insert(Ptr &t,int k,Ptr v){
        splay(t);
        auto x=split(t,k);
        t=merge(merge(x.first,v),x.second);
    }
    void erase(Ptr &t,int k){
        splay(t);
        auto x=split(t,k);
        auto y=split(x.second,1);
        // delete y.first;
        t=merge(x.first,y.second);
    }
    template<class T>
    Ptr build(const vector<T> &v){
        if(v.empty())return nullptr;
        function<Ptr(int,int)> build=[&](int l,int r){
            if(l==r)return new Node(v[l]);
            int m=(l+r)/2;
            return merge(build(l,m),build(m+1,r));
        };
        return build(0,v.size()-1);
    }
};
```

LazyReversibleBBST.hpp

Description: Lazy Reversible BBST Base.

904708, 81 lines

```
template<class Tree,class Node,class MonoidAction>
struct LazyReversibleBBST:Tree{
    using Tree::merge;
    using Tree::split;
    using typename Tree::Ptr;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;

    LazyReversibleBBST()=default;
```

```

Info sum(Ptr t){
    return t?->sum:InfoMonoid::unit();
}
void pull(Ptr t){
    if (!t) return;
    push(t);
    t->size=1;
    t->sum=t->val;
    t->revsum=t->val;
    if (t->l){
        t->size+=t->l->size;
        t->sum=InfoMonoid::op(t->l->sum,t->sum);
        t->revsum=InfoMonoid::op(t->revsum,t->l->revsum);
    }
    if (t->r){
        t->size+=t->r->size;
        t->sum=InfoMonoid::op(t->sum,t->r->sum);
        t->revsum=InfoMonoid::op(t->r->revsum,t->revsum);
    }
}
void push(Ptr t){
    if (!t) return;
    if (t->rev){
        toggle(t->l);
        toggle(t->r);
        t->rev=false;
    }
    if (t->lz!=TagMonoid::unit()){
        propagate(t->l,t->lz);
        propagate(t->r,t->lz);
        t->lz=TagMonoid::unit();
    }
}
void toggle(Ptr t){
    if (!t) return;
    swap(t->l,t->r);
    swap(t->sum,t->revsum);
    t->rev^=true;
}
void propagate(Ptr t,const Tag &v){
    if (!t) return;
    t->val=MonoidAction::op(t->val,v);
    t->sum=MonoidAction::op(t->sum,v);
    t->revsum=MonoidAction::op(t->revsum,v);
    t->lz=TagMonoid::op(t->lz,v);
}
void apply(Ptr &t,int l,int r,const Tag &v){
    if (l>r) return;
    auto x=split(t,l);
    auto y=split(x.second,r-l+1);
    propagate(y.first,v);
    t=merge(x.first,merge(y.first,y.second));
}
Info query(Ptr &t,int l,int r){
    if (l>r) return InfoMonoid::unit();
    auto x=split(t,l);
    auto y=split(x.second,r-l+1);
    Info res=sum(y.first);
    t=merge(x.first,merge(y.first,y.second));
    return res;
}
void reverse(Ptr &t,int l,int r){
    if (l>r) return;
    auto x=split(t,l);
    auto y=split(x.second,r-l+1);
    toggle(y.first);
    t=merge(x.first,merge(y.first,y.second));
}
};

```

LazyReversibleSplayTree.hpp

Description: Lazy Reversible Splay Tree.

"SplayTreeBase.hpp", "LazyReversibleBBST.hpp" b8455b, 23 lines

```

template<class MonoidAction>
struct LazyReversibleSplayTreeNode{
    using Ptr = LazyReversibleSplayTreeNode*;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    using value_type = Info;
    Ptr l,r,p;
    Info val,sum,revsum;
    Tag lz;
    int size;
    bool rev;
    LazyReversibleSplayTreeNode(const Info &_val=InfoMonoid::
        unit(),const Tag &_lz=TagMonoid::unit())
        :l(),r(),p(),val(_val),sum(_val),revsum(_val),lz(_lz),
        size(1),rev(false){}
};

template<class MonoidAction>
struct LazyReversibleSplayTree
    : LazyReversibleBBST<SplayTreeBase<
        LazyReversibleSplayTreeNode<MonoidAction>>,
        LazyReversibleSplayTreeNode<MonoidAction>,MonoidAction>{
    using Node = LazyReversibleSplayTreeNode<MonoidAction>;
};

```

LinkCutTreeBase.hpp

Description: Link Cut Tree Base.

Usage: evert(u): make u be the root of the tree.

link(u,v): attach u to v.

cut(u,v): remove edge between u and v.

get_root(u): get the root of the tree containing u.

lca(u,v): get the lowest common ancestor of u and v.

fold(u,v): get the value of the path from u to v.

b432c3, 59 lines

```

template<class Splay>
struct LinkCutTreeBase:Splay{
    using Node = typename Splay::Node;
    using Ptr = Node*;
    using T = typename Node::value_type;
    Ptr expose(Ptr t){
        Ptr pc=nullptr; // preferred child
        for (Ptr cur=t;cur;cur=cur->p){
            this->splay(cur);
            cur->r=pc;
            this->pull(cur);
            pc=cur;
        }
        this->splay(t);
        return pc;
    }
    void evert(Ptr t){ // make t be the root of the tree
        expose(t);
        this->toggle(t);
        this->push(t);
    }
    void link(Ptr u,Ptr v){ // attach u to v
        evert(u);
        expose(v);
        u->p=v;
    }
    void cut(Ptr u,Ptr v){ // cut edge between u and v
        evert(u);
        expose(v);
        assert (u->p==v);
    }
};

```

```

v->l=u->p=nullptr;
this->pull(v);
}
Ptr get_root(Ptr t){
    expose(t);
    while (t->l) this->push(t),t=t->l;
    this->splay(t);
    return t;
}
Ptr lca(Ptr u,Ptr v){
    if (get_root(u)!=get_root(v)) return nullptr;
    expose(u);
    return expose(v);
}
void set_val(Ptr t,const T &val){
    this->evert(t);
    t->val=val;
    this->pull(t);
}
T get_val(Ptr t){
    this->evert(t);
    return t->val;
}
T fold(Ptr u,Ptr v){
    evert(u);
    expose(v);
    return v->sum;
}
};

```

LazyLinkCutTree.hpp

Description: Lazy Link Cut Tree.

Usage: using Lct = LazyLinkCutTree<Action>;

using Ptr = Lct::Ptr;

using Node = Lct::Node;

vector<Ptr> ptr(n);

for(int i=0;i<n;i++)ptr[i]=new Node(val[i]);

auto link=[](int u,int v){

Lct::link(ptr[u],ptr[v]);

};

auto cut=[](int u,int v){

Lct::cut(ptr[u],ptr[v]);

};

auto update=[](int u,int v,Action::Tag val){

Lct::apply(ptr[u],ptr[v],val);

};

auto query=[](int u,int v){

return Lct::fold(ptr[u],ptr[v]);

};

"LazyReversibleSplayTree.hpp", "LinkCutTreeBase.hpp" ead3da, 12 lines

```

template<class MonoidAction>
struct LazyLinkCutTree:LinkCutTreeBase<LazyReversibleSplayTree<
    MonoidAction>>{
    using base = LinkCutTreeBase<LazyReversibleSplayTree<
        MonoidAction>>;
    using Ptr = typename base::Ptr;
    using Tag = typename MonoidAction::Tag;

    void apply(Ptr u,Ptr v,const Tag &val){
        this->evert(u);
        this->expose(v);
        this->propagate(v,val);
    }
};

```

Number Theory (5)

ExtendedEuclid.hpp

Description: Extended Euclid algorithm for solving diophantine equation ($ax + by = \gcd(a, b)$).

Time: $\mathcal{O}(\log \max\{a, b\})$

```

"../template/Header.hpp"
229e7c, 13 lines

pair<ll,ll> euclid(ll a,ll b){
    ll x=1,y=0,x1=0,y1=1;
    while(b!=0){
        ll q=a/b;
        x-=q*x1;
        y-=q*y1;
        a-=q*b;
        swap(x,x1);
        swap(y,y1);
        swap(a,b);
    }
    return {x,y};
}
```

5.1 Prime Numbers

LinearSieve.hpp

Description: Prime Number Generator in Linear Time

Time: $\mathcal{O}(N)$

```

"../template/Header.hpp"
194fb1, 15 lines

vi linear_sieve(int n) {
    vi prime, composite(n + 1);
    for(int i=2; i<=n; ++i) {
        if(!composite[i]) {
            prime.emplace_back(i);

            for(int j=0; j<(int) prime.size() && i*prime[j]<=n; ++j) {
                composite[i * prime[j]] = true;
                if(i % prime[j] == 0) {
                    break;
                }
            }
        }
    }
    return prime;
}
```

FastEratosthenes.hpp

Description: Prime sieve for generating all primes smaller than LIM.

Time: LIM=1e9 ≈ 1.5s

```

"../template/Header.hpp"
295b58, 33 lines

const int LIM = 1e6;
bitset<LIM> isPrime;
vi eratosthenes() {
    const int S = (int) round(sqrt(LIM)), R = LIM / 2;
    vi pr = {2}, sieve(S + 1);
    pr.reserve((int)(LIM/log(LIM) * 1.1));
    vector<pii> cp;
    for(int i=3; i<=S; i+=2) {
        if(!sieve[i]) {
            cp.emplace_back(i, i * i / 2);
            for(int j=i*i; j<=S; j+=2*i) {
                sieve[j] = 1;
            }
        }
    }
    for(int L=1; L<=R; L+=S) {
        array<bool, S> block{};
        for(auto &[p, idx]: cp) {
            for(int i=idx; i<S+L; idx=(i+p)) {
                block[i - L] = 1;
            }
        }
        for(int i=0; i<min(S, R-L); ++i) {
```

```

        if(!block[i]) {
            pr.emplace_back((L + i) * 2 + 1);
        }
    }
}

for(int i: pr) {
    isPrime[i] = 1;
}

return pr;
}
```

GolbatchConjecture.hpp

Description: Find two prime numbers which sum equals s

Time: $\mathcal{O}(N \log N)$

```

"FastEratosthenes.hpp"
88fb23, 18 lines

pair<int, int> goldbatchConjecture(int s, vi pr = {}){
    if (s <= 2 || s % 2 != 0) {
        return make_pair(-1, -1);
    }
    if (pr.size() == 0) {
        pr = eratosthenes();
    }
    for (auto x : pr) {
        if (x > s / 2) {
            break;
        }
        int d = s - x;
        if (binary_search(pr.begin(), pr.end(), d)) {
            return make_pair(min(x, d), max(x, d));
        }
    }
    return make_pair(-1, -1);
}
```

Graph (6)

6.1 Matching

HopcroftKarp.hpp

Description: Fast bipartite matching algorithm.

Time: $\mathcal{O}(E\sqrt{V})$

```

"../template/Header.hpp"
0bd56f, 52 lines

struct HopcroftKarp{
    int n,m;
    vi l,r,lv,ptr;
    vector<vi> adj;
    HopcroftKarp(){}
    HopcroftKarp(int _n,int _m){init(_n,_m);}
    void init(int _n,int _m){
        n=_n,m=_m;
        adj.assign(n+m,vi{});
    }
    void addEdge(int u,int v){
        adj[u].emplace_back(v+n);
    }
    void bfs(){
        lv=vi(n,-1);
        queue<int> q;
        for(int i=0;i<n;i++)if(l[i]==-1){
            lv[i]=0;
            q.emplace(i);
        }
        while(!q.empty()){
            int u=q.front();
            q.pop();
            for(int v:adj[u])if(r[v]!=-1&&lv[r[v]]==-1){
                lv[r[v]]=lv[u]+1;
```

```

                q.emplace(r[v]);
            }
        }
    }
    bool dfs(int u){
        for(int &i=ptr[u];i<sz(adj[u]);i++){
            int v=adj[u][i];
            if(r[v]==-1||(lv[r[v]]==lv[u]+1&&dfs(r[v]))){
                l[u]=v,r[v]=u;
                return true;
            }
        }
        return false;
    }
    int maxMatching(){
        int match=0,cnt=0;
        l=r=vi(n+m,-1);
        do{
            ptr=vi(n);
            bfs();
            cnt=0;
            for(int i=0;i<n;i++)if(l[i]==-1&&dfs(i))cnt++;
            match+=cnt;
        }while(cnt);
        return match;
    }
};
```

Kuhn.hpp

Description: Kuhn Algorithm to find maximum bipartite matching or find augmenting path in bipartite graph.

Time: $\mathcal{O}(VE)$

```

"../template/Header.hpp"
fc7d17, 15 lines

vi adj[1010], match(1010, -1);
bitset<1010> visited;
bool kuhn(int u) {
    if(visited[u]) {
        return false;
    }
    visited[u] = true;
    for(auto x: adj[u]) {
        if(match[x] == -1 || kuhn(match[x])) {
            match[x] = u;
            return true;
        }
    }
    return false;
}
```

6.2 Network Flow

Dinic.hpp

Description: Fast max-flow algorithm.

Time: $\mathcal{O}(VE \log U)$ where $U = \max |cap|$

```

"../template/Header.hpp"
7409c7, 68 lines

template<class T>
struct Dinic{
    struct Edge{
        int to;
        ll flow,cap;
        Edge(int _to,ll _cap):to(_to),flow(0),cap(_cap){}
        ll getcap(){
            return cap-flow;
        }
    };
    int n;
    ll U;
    vector<Edge> e;
    vector<vi> adj;
```

```
vi ptr,lv1;
Dinic(){}
Dinic(int _n){
    init(_n);
}
void init(int _n){
    n=_n,U=0;
    e.clear();
    adj.assign(n,{});
}
void addEdge(int u,int v,ll cap){
    U=max(U,cap);
    adj[u].emplace_back(sz(e));
    e.emplace_back(v,cap);
    adj[v].emplace_back(sz(e));
    e.emplace_back(u,0); // change 0 to cap for undirected flow
}
bool bfs(int s,int t,ll scale){
    lv1.assign(n,0);
    vi q(s);
    lv1[s]=1;
    for(int i=0;i<sz(q);i++){
        int u=q[i];
        for(auto j:adj[u])if(!lv1[e[j].to]&&e[j].getcap()>=scale){
            q.emplace_back(e[j].to);
            lv1[e[j].to]=lv1[u]+1;
        }
    }
    return lv1[t];
}
ll dfs(int u,int t,ll f){
    if(u==t||!f)return f;
    for(int &i=ptr[u];i<sz(adj[u]);i++){
        int j=adj[u][i];
        if(lv1[e[j].to]==lv1[u]+1){
            if(ll p=dfs(e[j].to,t,min(f,e[j].getcap()))){
                e[j].flow+=p;
                e[j^1].flow-=p;
                return p;
            }
        }
    }
    return 0;
}
ll flow(int s,int t){
    ll flow=0;
    for(ll L=1ll<<(63-__builtin_clzll(U));L>0;L>=1) // L = 1 may be faster but it's O(V^2 E)
        while(bfs(s,t,L)){
            ptr.assign(n,0);
            while(ll p=dfs(s,t,LINF))flow+=p;
        };
    return flow;
}
};
```

MinCostFlow.hpp

Description: minimum-cost flow algorithm.
Time: $\mathcal{O}(FE \log V)$ where F is max flow.

Seaid2, 83 lines

```
template<class F,class C>
struct MinCostFlow{
    struct Edge{
        int to;
        F flow,cap;
        C cost;
```

```
Edge(int _to,F _cap,C _cost):to(_to),flow(0),cap(_cap),
    cost(_cost){}
F getcap(){
    return cap-flow;
}
};
int n;
vector<Edge> e;
vector<vi> adj;
vector<C> pot,dist;
vi pre;
bool neg;
const F FINF=numeric_limits<F>::max()/2;
const C CINF=numeric_limits<C>::max()/2;
MinCostFlow(){}
MinCostFlow(int _n){
    init(_n);
}
void init(int _n){
    n=_n;
    e.clear();
    adj.assign(n,{});
    neg=false;
}
void addEdge(int u,int v,F cap,C cost){
    adj[u].emplace_back(sz(e));
    e.emplace_back(v,cap,cost);
    adj[v].emplace_back(sz(e));
    e.emplace_back(u,0,-cost);
    if(cost<0)neg=true;
}
bool dijkstra(int s,int t){
    using P = pair<C,int>;
    dist.assign(n,CINF);
    pre.assign(n,-1);
    priority_queue<P,vector<P>,greater<P>> pq;
    dist[s]=0;
    pq.emplace(0,s);
    while(!pq.empty()){
        auto [d,u]=pq.top();
        pq.pop();
        if(dist[u]<d)continue;
        for(int i:adj[u]){
            int v=e[i].to;
            C ndist=d+pot[u]-pot[v]+e[i].cost;
            if(e[i].getcap()>0&&dist[v]>ndist){
                pre[v]=i;
                dist[v]=ndist;
                pq.emplace(ndist,v);
            }
        }
    }
    return dist[t]<CINF;
}
pair<F,C> flow(int s,int t){
    F flow=0;
    C cost=0;
    pot.assign(n,0);
    if(neg)for(int t=0;t<n;t++)for(int i=0;i<sz(e);i++)if(e[i].getcap()>0){
        int u=e[i^1].to,v=e[i].to;
        pot[v]=min(pot[v],pot[u]+e[i].cost);
    } // Bellman-Ford
    while(dijkstra(s,t)){
        for(int i=0;i<n;i++)pot[i]+=dist[i];
        F aug=FINF;
        for(int u=t;u!=s;u=e[pre[u]^1].to){
            aug=min(aug,e[pre[u]].getcap());
        } // find bottleneck
```

```
for(int u=t;u!=s;u=e[pre[u]^1].to){
    e[pre[u]].flow+=aug;
    e[pre[u]^1].flow-=aug;
} // push flow
flow+=aug;
cost+=aug*pot[t];
}
return {flow,cost};
}
};
```

Polynomials (7)

FormalPowerSeries.hpp

Description: basic operations of formal power series

NTT.hpp416433, 136 lines

```
template<class mint>
struct FormalPowerSeries:vector<mint>{
    using vector<mint>::vector;
    using FPS = FormalPowerSeries;

FPS &operator+=(const FPS &rhs){
    if(rhs.size()>this->size())this->resize(rhs.size());
    for(int i=0;i<rhs.size();i+)(*this)[i]+=rhs[i];
    return *this;
}
FPS &operator+=(const mint &rhs){
    if(this->empty())this->resize(1);
    (*this)[0]+=rhs;
    return *this;
}
FPS &operator-=(const FPS &rhs){
    if(rhs.size()>this->size())this->resize(rhs.size());
    for(int i=0;i<rhs.size();i+)(*this)[i]-=rhs[i];
    return *this;
}
FPS &operator-=(const mint &rhs){
    if(this->empty())this->resize(1);
    (*this)[0]-=rhs;
    return *this;
}
FPS &operator*=(const FPS &rhs){
    auto res=NTT<mint>()(*this, rhs);
    return *this=FPS(res.begin(),res.end());
}
FPS &operator*=(const mint &rhs){
    for(auto &a:a*rhs)
        return *this;
}
friend FPS operator+(FPS lhs,const FPS &rhs){return lhs+=rhs;}
friend FPS operator+(FPS lhs,const mint &rhs){return lhs+=rhs;}
friend FPS operator+(const mint &lhs,FPS &rhs){return rhs+=lhs;}
friend FPS operator-(FPS lhs,const FPS &rhs){return lhs-=rhs;}
friend FPS operator-(FPS lhs,const mint &rhs){return lhs-=rhs;}
friend FPS operator-(const mint &lhs,FPS rhs){return -(rhs-lhs);}
friend FPS operator*(FPS lhs,const FPS &rhs){return lhs*=rhs;}
friend FPS operator*(FPS lhs,const mint &rhs){return lhs*=rhs;}
friend FPS operator*(FPS lhs,const FPS rhs){return lhs*=rhs;}
friend FPS operator*(const mint &lhs,FPS rhs){return rhs*=lhs;}
```



```

FPS operator-() {return (*this)*-1;}

FPS rev() {
    FPS res(*this);
    reverse(res.begin(), res.end());
    return res;
}

FPS pre(int sz) {
    FPS res(this->begin(), this->begin() + min((int) this->size(), sz));
    if(res.size() < sz) res.resize(sz);
    return res;
}

FPS shrink() {
    FPS res(*this);
    while(!res.empty() && res.back() == mint{}) res.pop_back();
    return res;
}

FPS operator>>(int sz) {
    if(this->size() <= sz) return {};
    FPS res(*this);
    res.erase(res.begin(), res.begin() + sz);
    return res;
}

FPS operator<<(int sz) {
    FPS res(*this);
    res.insert(res.begin(), sz, mint{});
    return res;
}

FPS diff() {
    const int n = this->size();
    FPS res(max(0, n-1));
    for(int i=1; i<n; i++) res[i-1] = (*this)[i] * mint(i);
    return res;
}

FPS integral() {
    const int n = this->size();
    FPS res(n+1);
    res[0] = 0;
    if(n > 0) res[1] = 1;
    ll mod = mint::get_mod();
    for(int i=2; i<=n; i++) res[i] = (-res[mod%i]) * (mod/i);
    for(int i=0; i<n; i++) res[i+1] *= (*this)[i];
    return res;
}

mint eval(const mint &x) {
    mint res=0, w=1;
    for(auto &a: *this) res += a*w, w*=x;
    return res;
}

FPS inv(int deg=-1) {
    assert(!this->empty() && (*this)[0] != mint(0));
    if(deg == -1) deg = this->size();
    FPS res(mint(1) / (*this)[0]);
    for(int i=2; i>>1 < deg; i<=1) {
        res = (res * (mint(2) - res * pre(i))).pre(i);
    }
    return res.pre(deg);
}

FPS log(int deg=-1) {
    assert(!this->empty() && (*this)[0] == mint(1));
    if(deg == -1) deg = this->size();
    return pre(deg).diff() * inv(deg).pre(deg-1).integral();
}

FPS exp(int deg=-1) {
    assert(this->empty() || (*this)[0] == mint(0));

```

```

    if(deg == -1) deg = this->size();
    FPS res(mint(1));
    for(int i=2; i>>1 < deg; i<=1) {
        res = (res * (pre(i) - res.log(i) + mint(1))).pre(i);
    }
    return res.pre(deg);
}

FPS pow(ll k, int deg=-1) {
    const int n = this->size();
    if(deg == -1) deg = n;
    if(k == 0) {
        FPS res(deg);
        if(deg) res[0] = mint(1);
        return res;
    }
    for(int i=0; i<n; i++) {
        if(__int128_t(i) * k >= deg) return FPS(deg, mint(0));
        if((__this)[i] == mint(0)) continue;
        mint rev = mint(1) / (*this)[i];
        FPS res = (((*this * rev) >> i).log(deg) * k).exp(deg);
        res = (res * binpow((*this)[i], k) << (i * k)).pre(deg);
        return res;
    }
    return FPS(deg, mint(0));
}

};
using FPS = FormalPowerSeries<mint>;

```

FFT.hpp

Description: Fast Fourier transform

Time: $\mathcal{O}(N \log N)$

../template/Header.hpp 5d476b, 73 lines

```

template<class T=ll, int mod=0>
struct FFT {
    using vt = vector<T>;
    using cd = complex<db>;
    using vc = vector<cd>;

    static const bool INT=true;

    static void fft(vc &a) {
        int n=a.size(), L=31-__builtin_clz(n);
        vc rt(n);
        rt[1]=1;
        for(int k=2; k<n; k*=2) {
            cd z=polar(db(1), PI/k);
            for(int i=k; i<2*k; i++) rt[i]=i&1?rt[i/2]*z:rt[i/2];
        }
        vi rev(n);
        for(int i=1; i<n; i++) rev[i]=(rev[i/2] | (i&1)<<L)/2;
        for(int i=1; i<n; i++) if(i<rev[i]) swap(a[i], a[rev[i]]);
        for(int k=1; k<n; k*=2) for(int i=0; i<n; i+=2*k) for(int j=0; j<k; j++) {
            cd z=rt[j+k]*a[i+j+k];
            a[i+j+k]=a[i+j]-z;
            a[i+j]+=z;
        }
    }

    template<class U>
    static db norm(const U &x) {
        return INT?round(x):x;
    }

    static vt conv(const vt &a, const vt &b) {
        if(a.empty() || b.empty()) return {};
        vt res(a.size()+b.size()-1);
        int L=32-__builtin_clz(res.size()), n=1<<L;
        vc in(n), out(n);
        copy(a.begin(), a.end(), in.begin());
        for(int i=0; i<b.size(); i++) in[i].imag(b[i]);
    }
}

```

```

    fft(in);
    for(auto &x:in) x*=x;
    for(int i=0; i<n; i++) out[i]=in[-i&(n-1)]-conj(in[i]);
    fft(out);
    for(int i=0; i<res.size(); i++) res[i]=norm(imag(out[i])/(4*n));
    return res;
}

static vl convMod(const vl &a, const vl &b) {
    assert(mod>0);
    if(a.empty() || b.empty()) return {};
    vl res(a.size()+b.size()-1);
    int L=32-__builtin_clz(res.size()), n=1<<L;
    ll cut=int(sqrt(mod));
    vc in1(n), in2(n), out1(n), out2(n);
    for(int i=0; i<a.size(); i++) in1[i]=cd(ll(a[i])/cut, ll(a[i])%cut); // a1 + i * a2
    for(int i=0; i<b.size(); i++) in2[i]=cd(ll(b[i])/cut, ll(b[i])%cut); // b1 + i * b2
    fft(in1), fft(in2);
    for(int i=0; i<n; i++) {
        int j=-i&(n-1);
        out1[j]=(in1[i]+conj(in1[j]))*in2[i]/(2.1*n); // f1 * (g1 + i * g2) = f1 * g1 + i f1 * g2
        out2[j]=(in1[i]-conj(in1[j]))*in2[i]/cd(0.1, 2.1*n); // f2 * (g1 + i * g2) = f2 * g1 + i f2 * g2
    }
    fft(out1), fft(out2);
    for(int i=0; i<res.size(); i++) {
        ll x=round(real(out1[i])), y=round(imag(out1[i]))+round(real(out2[i])), z=round(imag(out2[i]));
        res[i]=((x%mod*cut+y)%mod*cut+z)%mod; // a1 * b1 * cut^2 + (a1 * b2 + a2 * b1) * cut + a2 * b2
    }
    return res;
}

vt operator()(const vt &a, const vt &b) {
    return mod>0?conv(a,b):convMod(a,b);
}

};
template<>
struct FFT<db> {
    static const bool INT=false;
};

```

NTT.hpp

Description: Number theoretic transform

Time: $\mathcal{O}(N \log N)$

../template/Header.hpp, ../modular-arithmetic/BinPow.hpp,

../modular-arithmetic/MontgomeryModInt.hpp 2b2392, 39 lines

```

template<class mint=mint>
struct NTT {
    using vm = vector<mint>;

    static constexpr mint root=mint::get_root();
    static_assert(root!=0);

    static void ntt(vm &a) {
        int n=a.size(), L=31-__builtin_clz(n);
        vm rt(n);
        rt[1]=1;
        for(int k=2, s=2; k<n; k*=2, s++) {
            mint z[]={1, binpow(root, MOD>>s)};
            for(int i=k; i<2*k; i++) rt[i]=rt[i/2]*z[i&1];
        }
        vi rev(n);
        for(int i=1; i<n; i++) rev[i]=(rev[i/2] | (i&1)<<L)/2;
        for(int i=1; i<n; i++) if(i<rev[i]) swap(a[i], a[rev[i]]);
    }
}

```

```
        for(int k=1;k<n;k*=2)for(int i=0;i<n;i+=2*k)for(int j=0;j<k
            ;j++){
            mint z=rt[j+k]*a[i+j+k];
            a[i+j+k]=a[i+j]-z;
            a[i+j]+=z;
        }
    }
    static vm conv(const vm &a,const vm &b){
        if(a.empty()||b.empty())return {};
        int s=a.size()+b.size()-1,n=1<<(32-__builtin_clz(s));
        mint inv=mint(n).inv();
        vm in1(a),in2(b),out(n);
        in1.resize(n),in2.resize(n);
        ntt(in1),ntt(in2);
        for(int i=0;i<n;i++)out[-i&(n-1)]=in1[i]*in2[i]*inv;
        ntt(out);
        return vm(out.begin(),out.begin()+s);
    }
    vm operator()(const vm &a,const vm &b){
        return conv(a,b);
    }
};
```

7.1 Various

GaussianElimination.hpp

Description: Gaussian Elimination

"/template/Header.hpp" e89ecb, 34 lines

```
struct Gauss {
    int n, sz;
    vector<ll> basis;
    Gauss(int n = 0) {
        init(n);
    }
    void init(int _n) {
        n = _n, sz = 0;
        basis.assign(n, 0);
    }
    void insert(ll x) {
        for (int i = n - 1; i >= 0; i--)
            if (x >> i & 1) {
                if (!basis[i]) {
                    basis[i] = x;
                    sz++;
                    return;
                }
                x ^= basis[i];
            }
    }
    ll getmax(ll k = 0) {
        ll tot = 1ll << sz, res = 0;
        for (int i = n - 1; i >= 0; i--)
            if (basis[i]) {
                tot >>= 1;
                if ((k >= tot && res >> i & 1) || (k < tot && res >> i
                    & 1 ^ 1))
                    res ^= basis[i];
                if (k >= tot)
                    k -= tot;
            }
        return res;
    }
};
```

BinaryTrie.hpp

Description: Binary Trie

"/template/Header.hpp" 525bf4, 59 lines

```
using node_t = array<int, 2>;
template<size_t S>
```

```
struct binary_trie {
    vector<node_t> t = {node_t{}};
    vector<int> cnt = {0};
    int cnt_nodes = 0;
    void insert(int v) {
        int cur = 0;
        cnt[0]++;
        for(int i=S-1; i>=0; --i) {
            int b = (v & (1 << i)) ? 1: 0;
            if(!t[cur][b]) {
                t[cur][b] = ++cnt_nodes;
                t.emplace_back(node_t{});
                cnt.emplace_back(0);
            }
            cnt[t[cur][b]]++;
            cur = t[cur][b];
        }
    }
    void remove(int v) {
        int cur = 0;
        cnt[0]--;
        for(int i=S-1; i>=0; --i) {
            int b = (v & (1 << i)) ? 1: 0;
            cnt[t[cur][b]]--;
            cur = t[cur][b];
        }
    }
    int get_min(int v) {
        int cur = 0, res = 0;
        for(int i=(int) S-1; i>=0; --i) {
            int b = (v & (1 << i)) ? 1 : 0;
            if(t[cur][b] && cnt[t[cur][b]]) {
                cur = t[cur][b];
            }
            else {
                res |= (1 << i);
                cur = t[cur][!b];
            }
        }
        return res;
    }
    int get_max(int v) {
        int cur = 0, res = 0;
        for(int i=(int) S-1; i>=0; --i) {
            int b = (v & (1 << i)) ? 1 : 0;
            if(t[cur][!b] && cnt[t[cur][!b]]) {
                res |= (1 << i);
                cur = t[cur][!b];
            }
            else {
                cur = t[cur][b];
            }
        }
        return res;
    }
};
```

Competitive Programming Topics

(A)

topics.txt

159 lines

Recursion
Divide and conquer
 Finding interesting points in $N \log N$
Algorithm analysis
 Master theorem
 Amortized time complexity
Greedy algorithm
 Scheduling
 Max contiguous subvector sum
 Invariants
 Huffman encoding
Graph theory
 Dynamic graphs (extra book-keeping)
 Breadth first search
 Depth first search
 * Normal trees / DFS trees
 Dijkstra's algorithm
 MST: Prim's algorithm
 Bellman-Ford
 Konig's theorem and vertex cover
 Min-cost max flow
 Lovasz toggle
 Matrix tree theorem
 Maximal matching, general graphs
 Hopcroft-Karp
 Hall's marriage theorem
 Graphical sequences
 Floyd-Warshall
 Euler cycles
 Flow networks
 * Augmenting paths
 * Edmonds-Karp
 Bipartite matching
 Min. path cover
 Topological sorting
 Strongly connected components
 2-SAT
 Cut vertices, cut-edges and biconnected components
 Edge coloring
 * Trees
 Vertex coloring
 * Bipartite graphs (\Rightarrow trees)
 * 3^n (special case of set cover)
 Diameter and centroid
 K'th shortest path
 Shortest cycle
Dynamic programming
 Knapsack
 Coin change
 Longest common subsequence
 Longest increasing subsequence
 Number of paths in a dag
 Shortest path in a dag
 Dynprog over intervals
 Dynprog over subsets
 Dynprog over probabilities
 Dynprog over trees
 3^n set cover
 Divide and conquer
 Knuth optimization
 Convex hull optimizations
 RMQ (sparse table a.k.a 2^k -jumps)
 Bitonic cycle

 Log partitioning (loop over most restricted)
Combinatorics
 Computation of binomial coefficients
 Pigeon-hole principle
 Inclusion/exclusion
 Catalan number
 Pick's theorem
Number theory
 Integer parts
 Divisibility
 Euclidean algorithm
 Modular arithmetic
 * Modular multiplication
 * Modular inverses
 * Modular exponentiation by squaring
 Chinese remainder theorem
 Fermat's little theorem
 Euler's theorem
 Phi function
 Frobenius number
 Quadratic reciprocity
 Pollard-Rho
 Miller-Rabin
 Hensel lifting
 Vieta root jumping
Game theory
 Combinatorial games
 Game trees
 Mini-max
 Nim
 Games on graphs
 Games on graphs with loops
 Grundy numbers
 Bipartite games without repetition
 General games without repetition
 Alpha-beta pruning
Probability theory
Optimization
 Binary search
 Ternary search
 Unimodality and convex functions
 Binary search on derivative
Numerical methods
 Numeric integration
 Newton's method
 Root-finding with binary/ternary search
 Golden section search
Matrices
 Gaussian elimination
 Exponentiation by squaring
Sorting
 Radix sort
Geometry
 Coordinates and vectors
 * Cross product
 * Scalar product
 Convex hull
 Polygon cut
 Closest pair
 Coordinate-compression
 Quadtrees
 KD-trees
 All segment-segment intersection
Sweeping
 Discretization (convert to events and sweep)
 Angle sweeping
 Line sweeping
 Discrete second derivatives
Strings

 Longest common substring
 Palindrome subsequences
 Knuth-Morris-Pratt
 Tries
 Rolling polynomial hashes
 Suffix array
 Suffix tree
 Aho-Corasick
 Manacher's algorithm
 Letter position lists
Combinatorial search
 Meet in the middle
 Brute-force with pruning
 Best-first (A*)
 Bidirectional search
 Iterative deepening DFS / A*
Data structures
 LCA (2^k -jumps in trees in general)
 Pull/push-technique on trees
 Heavy-light decomposition
 Centroid decomposition
 Lazy propagation
 Self-balancing trees
 Convex hull trick (wcipeg.com/wiki/Convex_hull_trick)
 Monotone queues / monotone stacks / sliding queues
 Sliding queue using 2 stacks
 Persistent segment tree