

Chulalongkorn University

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template from KACTL

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	$\frac{Complate}{Complate}$ (1)	
template.cpp #pragma once		27 line
#d	<pre>nclude <bits stdc++.h=""> efine sz(x) (int)(x).size() efine all(x) (x).begin(), (x).end()</bits></pre>	
us	ing namespace std;	
us us us us us co // co co co co	<pre>ing ll = long long; ing db = long double; ing vi = vector<int>; ing vl = vector<1l>; ing vd = vector<db>; ing pii = pair<int, int="">; ing pll = pair<1l, ll>; ing pdd = pair<db, db="">; nst int INF = 0x3fffffff; 'const int MOD=10000000007; nst int MOD = 998244353; nst ll LINF = 0x1ffffffffffffff; nst db DINF = numeric_limits<db>::infinity(); nst db EPS = le-9; nst db PI = acos(db(-1)); t main(){</db></db,></int,></db></int></pre>	
	<pre>t main(){ cin.tie(nullptr)->sync_with_stdio(false);</pre>	
c.:	sh	2 line
./	+ -std=gnu++2a -Wall \$1 -o a.out a.out	

<u>Mathematics</u> (2)

2.1 Goldbatch's Conjecture

• Even number can be written in sum of two primes (Up to 1e12

• Range of N^{th} prime and $N+1^{th}$ prime will be less than or equal to 300 (Up to 1e12)

2.2 Divisibility

Number of divisors of N is given by $\prod_{i=1}^k (a_i + 1)$ where $N = \prod_{i=1}^k p_i^{a_i}$ and p_i are prime factors of N.

Numerical (3)

3.1 Newton's Method

```
if F(Q) = 0, then Q_{2n} \equiv Q_n - \frac{F(Q_n)}{F'(Q_n)} \pmod{x^{2n}}
                Q = P^{-1} : Q_{2n} \equiv Q_n \cdot (2 - P \cdot Q_n^2) \pmod{x^{2n}}
                                  Q = \ln P = \int \frac{P'}{P} \mathrm{d}x
                Q = e^p : Q_{2n} \equiv Q_n (1 + P - \ln Q_n) \pmod{x^{2n}}
                Q = \sqrt{P} : Q_{2n} \equiv \frac{1}{2} (Q_n + P \cdot Q_n^{-1}) \pmod{x^{2n}}
               Q = P^k = \alpha^k x^{kt} e^{k \ln T}; P = \alpha \cdot x^t \cdot T, T(0) = 1
```

Data Structures (4)

```
OrderedSet.hpp
```

Description: Ordered Set

"../template/Header.hpp", <bits/extc++.h> 1a7f5f, 14 lines using namespace __gnu_pbds;

template <class T> using ordered_set = tree<T, null_type, less<T>, rb_tree_tag, tree_order_statistics_node_update>; // can be change to less_equal void usage() { ordered_set<int> st, st_2; st.insert(2); st.insert(1); cout << st.order_of_key(2);</pre> cout << *st.find_by_order(1);</pre> st.join(st_2); // merge

FenwickTree.hpp

Description: Fenwick / Binary Indexed Tree

43767a, 41 lines

```
template<class T>
struct Fenwick{
    int n, logn;
    vector<T> t;
    Fenwick(){}
    Fenwick(int _n) {init(vector<T>(_n,T{}));}
    template<class U>
    Fenwick(const vector<U> &a) {init(a);}
    template<class U>
    void init(const vector<U> &a){
        n=(int)a.size();
        logn=31-__builtin_clz(n);
        t.assign(n+1,T{});
```

```
for(int i=1;i<=n;i++){
             t[i]=t[i]+a[i-1];
             int j=i+(i&-i);
             if (j<=n)t[j]=t[j]+t[i];</pre>
    void update(int x,const T &v) {
        for (int i=x+1; i<=n; i+=i&-i)t[i]=t[i]+v;</pre>
    void update(int l, int r, const T &v) {
        update (1, v), update (r+1, -v);
    T query(int x) {
        T res{};
        for(int i=x+1;i>0;i-=i&-i)res=res+t[i];
        return res;
    T query(int l,int r){
        return query (r) -query (1-1);
    int find(const T &k) {
        int x=0;
        T cur{};
        for (int i=1<<logn; i>0; i>>=1)
             if(x+i \le n\&\&cur+t[x+i] \le k)x+=i,cur=cur+t[x];
        return x:
};
```

Segment Tree.hpp Description: Segment Tree

c51dec. 85 lines

```
template<class Monoid>
struct SegmentTree{
    using T = typename Monoid::value_type;
    int n;
    vector<T> t;
    SegmentTree(){}
    SegmentTree(int n, function<T(int)> create) {init(n, create);}
    SegmentTree(int n,T v=Monoid::unit()){init(n,[&](int){
         return v; });}
    template<class U>
    SegmentTree(const vector<U> &a) {init((int)a.size(),[&](int
         i) {return T(a[i]);});}
    void init(int _n,function<T(int)> create) {
        t.assign(4<<(31-__builtin_clz(n)), Monoid::unit());
        function<void(int,int,int)> build=[&](int 1,int r,int i
            if(l==r)return void(t[i]=create(l));
            int m = (1+r)/2;
            build(1, m, i * 2);
            build(m+1, r, i*2+1);
            pull(i);
        };
        build(0, n-1, 1);
    void pull(int i){
        t[i]=Monoid::op(t[i*2],t[i*2+1]);
    void modify(int 1, int r, int i, int x, const T &v){
        if (x<1 | | r<x) return;</pre>
        if(l==r)return void(t[i]=v);
        int m = (1+r)/2;
        modify(1, m, i*2, x, v);
        modify (m+1,r,i*2+1,x,v);
        pull(i);
    void modify(int x,const T &v){
```

```
modifv(0, n-1, 1, x, v);
template<class U>
void update(int 1,int r,int i,int x,const U &v) {
    if (x<1||r<x) return;</pre>
    if(l==r)return void(t[i]=Monoid::op(t[i],v));
    int m = (1+r)/2;
    update(1, m, i*2, x, v);
    update(m+1,r,i*2+1,x,v);
    pull(i);
template<class U>
void update(int x,const U &v){
    update (0, n-1, 1, x, v);
T query(int 1, int r, int i, int x, int y) {
    if(y<1||r<x)return Monoid::unit();</pre>
    if (x<=1&&r<=y) return t[i];</pre>
    int m = (1+r)/2;
    return Monoid::op(query(1, m, i*2, x, y), query(m+1, r, i*2+1,
         x,y));
T query(int x, int y) {
    return query (0, n-1, 1, x, y);
template<class F>
int findfirst(int 1, int r, int i, int x, int y, const F &f) {
    if(y<1||r<x||!f(t[i]))return n;</pre>
    if (l==r) return 1;
    int m = (1+r)/2;
    int res=findfirst(1, m, i*2, x, y, f);
    if (res==n) res=findfirst (m+1, r, i*2+1, x, y, f);
    return res;
template<class F>
int findfirst(int x, int y, const F &f) {
    return findfirst (0, n-1, 1, x, y, f);
template<class F>
int findlast(int 1, int r, int i, int x, int y, const F &f) {
    if(y<1||r<x||!f(t[i]))return -1;
    if(l==r)return 1;
    int m = (1+r)/2;
    int res=findlast(m+1,r,i*2+1,x,v,f);
    if (res==-1) res=findlast (1, m, i*2, x, y, f);
    return res;
template<class F>
int findlast(int x, int y, const F &f) {
    return findlast(0, n-1, 1, x, y, f);
```

LazySegment Tree.hpp

};

Description: Segment Tree with Lazy Propagation

91ab0c, 103 lines

```
template < class MonoidAction>
struct LazySegmentTree{
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
   using Tag = typename MonoidAction::Tag;
    int n;
    vector<Info> t;
    vector<Tag> lz;
    LazySegmentTree() {}
    LazySegmentTree(int n, function<Info(int)> create) {init(n,
         create);}
```

```
LazySegmentTree(int n, Info v=InfoMonoid::unit()) {init(n
     ,[&](int){return v;});}
template<class T>
LazySegmentTree(const vector<T> &a){init((int)a.size(),[&](
     int i) {return Info(a[i]);});}
void init(int _n,function<Info(int)> create){
    int m=4<<(31-__builtin_clz(n));</pre>
    t.assign(m, InfoMonoid::unit());
    lz.assign(m, TagMonoid::unit());
    function<void(int,int,int)> build=[&](int l,int r,int i
        if(l==r)return void(t[i]=create(l));
        int m = (1+r)/2;
        build(1, m, i*2);
        build(m+1, r, i \times 2+1);
        pull(i);
    };
    build(0, n-1, 1);
void pull(int i){
    t[i]=InfoMonoid::op(t[i*2],t[i*2+1]);
void apply(int i,const Tag &v){
    t[i]=MonoidAction::op(t[i],v);
    lz[i]=TagMonoid::op(lz[i],v);
void push(int i){
    apply(i*2,lz[i]);
    apply(i*2+1,1z[i]);
    lz[i]=TagMonoid::unit();
void modify(int 1, int r, int i, int x, const Info &v){
    if (x<1||r<x) return;</pre>
    if(l==r)return void(t[i]=v);
    int m = (1+r)/2;
    push(i);
    modify(1, m, i*2, x, v);
    modifv(m+1,r,i*2+1,x,v);
    pull(i);
void modify(int x,const Info &v){
    modify (0, n-1, 1, x, v);
void update(int l, int r, int i, int x, int y, const Tag &v) {
    if (y<1||r<x) return;</pre>
    if (x<=1&&r<=y) return apply(i,v);</pre>
    int m = (1+r)/2;
    push(i);
    update(1, m, i*2, x, y, v);
    update (m+1,r,i*2+1,x,y,v);
    pull(i);
void update(int x,int y,const Tag &v) {
    update (0, n-1, 1, x, y, v);
Info query(int 1,int r,int i,int x,int y){
    if(v<1||r<x)return InfoMonoid::unit();</pre>
    if (x<=1&&r<=y) return t[i];</pre>
    int m = (1+r)/2;
    return InfoMonoid::op(query(1,m,i*2,x,y),query(m+1,r,i
         *2+1, x, y));
Info query(int x,int y){
    return query (0, n-1, 1, x, y);
template<class F>
int findfirst(int 1,int r,int i,int x,int y,const F &f){
```

```
if(y<1||r<x||!f(t[i]))return n;</pre>
         if(l==r)return 1:
        int m = (1+r)/2;
        push(i);
         int res=findfirst(1, m, i*2, x, y, f);
        if (res==n) res=findfirst (m+1, r, i \times 2+1, x, y, f);
         return res;
    template<class F>
    int findfirst(int x, int y, const F &f) {
         return findfirst (0, n-1, 1, x, y, f);
    template<class F>
    int findlast(int 1, int r, int i, int x, int y, const F &f) {
        if(y<1||r<x||!f(t[i]))return -1;
        if(l==r)return 1;
        int m = (1+r)/2;
        push(i);
        int res=findlast (m+1, r, i*2+1, x, y, f);
        if (res==-1) res=findlast (1, m, i*2, x, y, f);
         return res;
    template<class F>
    int findlast(int x,int y,const F &f){
         return findlast(0,n-1,1,x,y,f);
};
```

DynamicSegmentTree.hpp

Description: Dynamic Segment Tree

```
e84eeb, 106 lines
template < class MonoidAction>
struct DynamicSegmentTree{
     using InfoMonoid = typename MonoidAction::InfoMonoid;
     using TagMonoid = typename MonoidAction::TagMonoid;
     using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
     struct Node:
    using Ptr = Node*;
     struct Node{
         Info val:
         Tag lz;
         Ptr l.r:
         Node(Info v):val(v),lz(TagMonoid::unit()),l(nullptr),r(
               nullptr) {}
         \label{eq:node_solution} Node\left(\texttt{Info} \ \ \mathsf{v,Tag} \ \ \mathsf{t}\right) : \texttt{val}\left(\mathsf{v}\right), \texttt{lz}\left(\mathsf{t}\right), \texttt{l}\left(\texttt{nullptr}\right), \texttt{r}\left(\texttt{nullptr}\right)\left\{\right\}
    11 lb,ub;
     Ptr rt:
     function<Info(l1,l1)> create;
    DynamicSegmentTree() {init(0,0);}
     DynamicSegmentTree(ll n) {init(0, n-1);}
     DynamicSegmentTree(ll lb, ll ub) {init(lb, ub);}
     DynamicSegmentTree(ll lb, ll ub, function<Info(ll, ll)> create
           ) {init(lb,ub,create);}
     void init(ll _lb,ll _ub,function<Info(ll,ll)> _create=[](ll
           1,11 r) {return InfoMonoid::unit();}) {
         lb=_lb, ub=_ub;
         create= create;
         rt=new Node(create(lb,ub));
     Info val(Ptr t){
         return t?t->val:InfoMonoid::unit();
     void pull(Ptr &t) {
         t->val=InfoMonoid::op(val(t->1),val(t->r));
     void apply(Ptr &t,const Tag &v,ll 1,ll r){
         if(!t)t=new Node(create(l,r));
```

```
t->val=MonoidAction::op(t->val,v);
    t->1z=TagMonoid::op(t->1z,v);
void push(Ptr &t, ll l, ll m, ll r) {
    apply(t->1,t->1z,1,m);
    apply (t->r,t->lz,m+1,r);
    t->1z=TagMonoid::unit();
void modify(ll 1,ll r,Ptr &t,ll x,const Info &v){
    if (x<1||r<x) return;
    if(l==r)return void(t->val=v);
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    modify(1, m, t->1, x, v);
    modify (m+1, r, t->r, x, v);
    pull(t);
void modify(ll x,const Info &v){
    modify(lb,ub,rt,x,v);
void update(ll 1,ll r,Ptr &t,ll x,ll y,const Tag &v) {
    if (y<1 | | r<x) return;</pre>
    if (x<=1&&r<=y) return apply(t,v,l,r);</pre>
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    update (1, m, t->1, x, y, v);
    update (m+1, r, t->r, x, y, v);
    pull(t);
void update(ll x,ll y,const Tag &v){
    update(lb,ub,rt,x,y,v);
Info query(11 1,11 r,Ptr &t,11 x,11 y){
    if (y<1||r<x) return InfoMonoid::unit();</pre>
    if (x<=1&&r<=y) return t->val;
    11 m=1+(r-1)/2;
    push(t,1,m,r);
    return InfoMonoid::op(query(1, m, t->1, x, y), query(m+1, r, t
         ->r,x,y));
Info query(ll x,ll y){
    return query(lb,ub,rt,x,y);
template<class F>
11 findfirst(ll 1, ll r, Ptr t, ll x, ll y, const F &f) {
    if (y<1||r<x||!f(t->val))return -1;
    if(l==r)return 1;
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    ll res=findfirst(1, m, t \rightarrow 1, x, y, f);
    if (res==-1) res=findfirst (m+1, r, t->r, x, y, f);
    return res;
template<class F>
11 findfirst(ll x,ll y,const F &f){
    return findfirst(lb, ub, rt, x, y, f);
template<class F>
11 findlast(ll 1,ll r,Ptr t,ll x,ll y,const F &f){
    if (y<1||r<x||!t||!f(t->val))return -1;
    if(l==r)return 1;
    11 m=1+(r-1)/2;
    push(t,l,m,r);
    11 res=findlast(m+1, r, t->r, x, y, f);
    if(res==-1)res=findlast(1, m, t->1, x, y, f);
    return res;
template < class F>
11 findlast(ll x,ll y,const F &f) {
```

```
return findlast(lb,ub,rt,x,y,f);
};
DSU.hpp
Description: Disjoint Set Union
                                                       0b3cb8, 26 lines
struct DSU{
    vector<int> p,sz;
    DSU() { }
    DSU(int n) {init(n);}
    void init(int n){
        p.resize(n);
        iota(p.begin(),p.end(),0);
        sz.assign(n,1);
    int find(int u){
        return p[u] == u?u:p[u] = find(p[u]);
    bool same(int u, int v) {
        return find(u) == find(v);
    bool merge(int u,int v){
        u=find(u), v=find(v);
        if (u==v) return false;
        sz[u]+=sz[v];
        p[v]=u;
        return true;
    int size(int u) {
        return sz[find(u)];
};
```

Binary Trie. hpp

```
Description: Binary Trie
                                                       ae5b7a, 66 lines
template<int BIT, class T = uint32_t, class S = int>
struct BinaryTrie{
    struct Node{
        array<int,2> ch;
        S cnt:
        Node():ch\{-1,-1\}, cnt(0){}
    vector<Node> t;
    BinaryTrie():t{Node()}{}
    int new_node(){
        t.emplace_back(Node());
        return t.size()-1;
   S size(){
        return t[0].cnt;
   bool empty(){
        return size() == 0;
    S get_cnt(int i) {
        return i!=-1?t[i].cnt:S(0);
    void insert(T x,S k=1){
        int u=0;
        t[u].cnt+=k;
        for (int i=BIT-1; i>=0; i--) {
            int v=x>>i&1;
            if(t[u].ch[v] == -1)t[u].ch[v] = new_node();
            u=t[u].ch[v];
            t[u].cnt+=k;
```

```
void erase(T x,S k=1){
        int u=0:
        assert(t[u].cnt>=k);
        t[u].cnt-=k;
        for (int i=BIT-1; i>=0; i--) {
            int v=x>>i&1;
            u=t[u].ch[v];
            assert (u!=-1\&\&t[u].cnt>=k);
            t[u].cnt-=k;
    T kth(S k, T x=0) {
        assert(k<size());
        int u=0;
        T res=0;
        for (int i=BIT-1; i>=0; i--) {
            int v=x>>i&1;
            if (k < get_cnt (t[u].ch[v])) {
                 u=t[u].ch[v];
            }else{
                 res | =T(1) << i;
                 k-=get\_cnt(t[u].ch[v]);
                 u=t[u].ch[v^1];
        return res;
    T min(T x) {
        return kth(0,x);
    T max(T x){
        return kth(size()-1,x);
};
```

LiChaoTree.hpp

```
Description: Li-Chao Tree (minimize)
                                                       4ab713, 52 lines
template<class T>
struct LiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line{
        T m.c:
        Line(T _m,T _c):m(_m),c(_c){}
        inline T eval(T x)const{return m*x+c;}
    vector<T> xs;
    vector<Line> t;
    LiChaoTree(){}
    LiChaoTree(const vector<T> &x):xs(x){init(x);}
    LiChaoTree(int n):xs(n){
        vector<T> x(n);
        iota(x.begin(), x.end(), 0);
        init(x);
    void init(const vector<T> &x) {
        sort(xs.begin(),xs.end());
        xs.erase(unique(xs.begin(), xs.end()), xs.end());
        t.assign(4 << (31-\_builtin\_clz(xs.size())), Line(0, INF));
    void insert(int l, int r, int i, Line v) {
        int m = (1+r)/2;
        if(v.eval(xs[m]) <t[i].eval(xs[m])) swap(t[i],v);</pre>
        if(v.eval(xs[1]) < t[i].eval(xs[1]))insert(1, m, i * 2, v);
        if(v.eval(xs[r]) < t[i].eval(xs[r]))insert(m+1,r,i*2+1,v)
    inline void insert (T m, T c) {
```

```
insert(0,(int)xs.size()-1,1,Line(m,c));
    void insert_range(int l, int r, int i, T x, T y, Line v) {
        if (y<xs[1] | |xs[r]<x) return;</pre>
        if (x<=xs[1] & &xs[r] <=y) return insert(1,r,i,v);
        int m = (1+r)/2;
        insert_range(1, m, i * 2, x, y, v);
        insert_range(m+1,r,i*2+1,x,y,v);
    inline void insert_range(T m,T c,T x,T y){
        insert_range(0, (int) xs.size()-1, 1, x, y, Line(m, c));
    T query(int l,int r,int i,T x){
        if (l==r) return t[i].eval(x);
        int m = (1+r)/2;
        if (x \le xs[m]) return min (t[i].eval(x), query(1, m, i*2, x));
        return min(t[i].eval(x), query(m+1, r, i*2+1, x));
    inline T query(T x){
        return query(0,(int)xs.size()-1,1,x);
};
```

DynamicLiChaoTree.hpp

Description: Dynamic Li-Chao Tree (minimize).

```
b8af36, 50 lines
template<class T>
struct DynamicLiChaoTree{
    static const T INF=numeric_limits<T>::max()/2;
    struct Line{
        T m,c;
        Line (T _m, T _c) : m(_m), c(_c) {}
        inline T eval(T x)const{return m*x+c;}
    struct Node:
    using Ptr = Node*:
    struct Node{
        Line v:
        Ptr l,r;
        Node():v(0,INF),l(nullptr),r(nullptr){}
        Node(Line _v):v(_v),l(nullptr),r(nullptr){}
    11 lb, ub;
    Ptr root:
    DynamicLiChaoTree(ll _lb,ll _ub):lb(_lb),ub(_ub),root(
         nullptr) {}
    void insert(T 1, T r, Ptr &t, Line v) {
        if(!t)return void(t=new Node(v));
        T m=1+(r-1)/2;
        if (v.eval(m) < t->v.eval(m)) swap (t->v,v);
        if (v.eval(1) <t->v.eval(1)) insert(1, m, t->1, v);
        if (v.eval(r) <t->v.eval(r)) insert(m+1, r, t->r, v);
    inline void insert(T m, T c) {
        insert(lb, ub, root, Line(m, c));
    void insert_range(T 1, T r, Ptr &t, T x, T y, Line v) {
        if (y<1||r<x) return;</pre>
        if(!t)t=new Node();
        if (x<=1&&r<=y) return insert(1, r, t, v);</pre>
        T m=1+(r-1)/2;
        insert_range(1, m, t \rightarrow 1, x, y, v);
        insert_range (m+1, r, t->r, x, y, v);
    inline void insert_range(T m, T c, T x, T y) {
        insert_range(lb, ub, root, x, y, Line(m, c));
    T query(T 1,T r,Ptr t,T x) {
        if(!t)return INF;
```

```
T m=1+(r-1)/2;
        if (x \le m) return min (t \ge v.eval(x), query(1, m, t \ge 1, x));
        return min(t->v.eval(x), query(m+1, r, t->r, x));
    inline T query(T x){
        return query(lb,ub,root,x);
};
SplayTreeBase.hpp
Description: Splay Tree. splay(u) will make node u be the root of the tree
in amortized O(log n) time.
template<class Node>
struct SplayTreeBase{
    using Ptr = Node*;
    bool is_root(Ptr t){
        return ! (t->p) | | (t->p->1!=t&&t->p->r!=t);
    } // The parent of the root stores the path parant in link
    int size(Ptr t){
        return t?t->size:0;
    virtual void push(Ptr t){};
    virtual void pull(Ptr t){};
    int pos(Ptr t){
        if(t->p){
            if(t->p->l==t)return -1;
            if (t->p->r==t) return 1;
        return 0;
    void rotate(Ptr t){
        Ptr x=t->p, y=x->p;
        if(pos(t) == -1){
            if((x->l=t->r))t->r->p=x;
            t->r=x, x->p=t;
        }else{
            if((x->r=t->1))t->1->p=x;
            t->1=x, x->p=t;
        pull(x),pull(t);
        if((t->p=y)){
            if(y->1==x)y->1=t;
            if(y->r==x)y->r=t;
    void splay(Ptr t) {
        if(!t)return;
        push(t);
        while(!is_root(t)){
            Ptr x=t->p;
            if(is_root(x)){
                push(x), push(t);
                rotate(t);
            }else{
                Ptr y=x->p;
                push(y), push(x), push(t);
                if(pos(x) == pos(t)) rotate(x), rotate(t);
                else rotate(t), rotate(t);
    Ptr get_first(Ptr t){
        while (t->1) push (t), t=t->1;
        splay(t);
        return t;
```

Ptr get_last(Ptr t){

```
while (t->r) push (t), t=t->r;
        splay(t);
        return t;
    Ptr merge(Ptr 1,Ptr r) {
        splay(1), splay(r);
        if(!1)return r;
        if(!r)return 1;
        l=get_last(1);
        1->r=r;
        r->p=1;
        pull(1);
        return 1;
    pair<Ptr,Ptr> split(Ptr t,int k) {
        if(!t)return {nullptr,nullptr};
        if (k==0) return {nullptr,t};
        if (k==size(t)) return {t, nullptr};
        push(t);
        if(k<=size(t->1)){
            auto x=split(t->1,k);
            t->1=x.second;
            t->p=nullptr;
            if (x.second) x.second->p=t;
            pull(t);
            return {x.first,t};
        }else{
            auto x=split(t->r,k-size(t->1)-1);
            t->r=x.first;
            t->p=nullptr;
            if (x.first) x.first->p=t;
            pull(t);
            return {t,x.second};
    void insert(Ptr &t,int k,Ptr v) {
        splay(t);
        auto x=split(t,k);
        t=merge(merge(x.first,v),x.second);
    void erase(Ptr &t,int k) {
        splav(t);
        auto x=split(t,k);
        auto v=split(x.second,1);
        // delete y.first;
        t=merge(x.first,y.second);
    template<class T>
    Ptr build(const vector<T> &v) {
        if(v.empty())return nullptr;
        function<Ptr(int,int)> build=[&](int 1,int r){
            if(l==r)return new Node(v[1]);
            int m = (1+r)/2;
            return merge(build(1,m),build(m+1,r));
        };
        return build(0, v.size()-1);
};
```

LazyReversibleBBST.hpp

Description: Lazy Reversible BBST Base.

```
template < class Tree, class Node, class MonoidAction >
struct LazyReversibleBBST:Tree{
    using Tree::merge;
    using Tree::split;
    using typename Tree::Ptr;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
```

```
using Info = typename MonoidAction::Info;
using Tag = typename MonoidAction::Tag;
LazyReversibleBBST()=default;
Info sum(Ptr t){
    return t?t->sum:InfoMonoid::unit();
void pull(Ptr t){
   if(!t)return;
   push(t);
    t->size=1;
    t->sum=t->val;
   t->revsum=t->val:
   if(t->1){
        t->size+=t->l->size;
        t->sum=InfoMonoid::op(t->l->sum,t->sum);
        t->revsum=InfoMonoid::op(t->revsum,t->l->revsum);
    if(t->r){
        t->size+=t->r->size;
        t->sum=InfoMonoid::op(t->sum,t->r->sum);
        t->revsum=InfoMonoid::op(t->r->revsum,t->revsum);
void push(Ptr t) {
   if(!t)return;
   if(t->rev){
        toggle (t->1);
        toggle(t->r);
        t->rev=false;
    if (t->lz!=TagMonoid::unit()) {
        propagate (t->1,t->1z);
        propagate(t->r,t->lz);
        t->1z=TagMonoid::unit();
void toggle(Ptr t){
   if(!t)return;
    swap(t->1,t->r);
    swap(t->sum,t->revsum);
    t->rev^=true;
void propagate (Ptr t, const Tag &v) {
    if(!t)return;
    t->val=MonoidAction::op(t->val,v);
    t->sum=MonoidAction::op(t->sum,v);
    t->revsum=MonoidAction::op(t->revsum,v);
    t->1z=TagMonoid::op(t->1z,v);
void apply (Ptr &t, int 1, int r, const Tag &v) {
   if(l>r)return;
    auto x=split(t,1);
    auto y=split(x.second,r-l+1);
   propagate(y.first,v);
    t=merge(x.first, merge(y.first, y.second));
Info query(Ptr &t,int 1,int r){
   if(l>r)return InfoMonoid::unit();
    auto x=split(t,1);
   auto y=split(x.second,r-1+1);
   Info res=sum(y.first);
    t=merge(x.first, merge(y.first, y.second));
    return res;
void reverse(Ptr &t,int l,int r) {
   if(l>r)return;
    auto x=split(t,1);
```

```
auto y=split(x.second, r-1+1);
        toggle(y.first);
        t=merge(x.first, merge(y.first, y.second));
};
LazyReversibleSplayTree.hpp
Description: Lazy Reversible Splay Tree.
"SplayTreeBase.hpp", "LazyReversibleBBST.hpp"
                                                     b8455b, 23 lines
template < class MonoidAction>
struct LazyReversibleSplayTreeNode{
    using Ptr = LazyReversibleSplayTreeNode*;
    using InfoMonoid = typename MonoidAction::InfoMonoid;
    using TagMonoid = typename MonoidAction::TagMonoid;
    using Info = typename MonoidAction::Info;
    using Tag = typename MonoidAction::Tag;
    using value_type = Info;
   Ptr 1, r, p;
    Info val, sum, revsum;
    Tag lz;
    int size;
    LazyReversibleSplayTreeNode(const Info &_val=InfoMonoid::
        unit(),const Tag &_lz=TagMonoid::unit())
        :1(),r(),p(),val(_val),sum(_val),revsum(_val),lz(_lz),
             size(1), rev(false){}
template < class MonoidAction >
struct LazyReversibleSplayTree
    : LazyReversibleBBST<SplayTreeBase<
         LazyReversibleSplayTreeNode<MonoidAction>>,
      LazyReversibleSplayTreeNode<MonoidAction>, MonoidAction>{
    using Node = LazyReversibleSplayTreeNode<MonoidAction>;
LinkCutTreeBase.hpp
Description: Link Cut Tree Base.
Usage: evert(u): make u be the root of the tree.
link(u,v): attach u to v.
cut(u,v): remove edge between u and v.
get_root(u): get the root of the tree containing u.
lca(u,v): get the lowest common ancestor of u and v.
fold(u,v): get the value of the path from u to v.
                                                     b432c3, 59 lines
template<class Splay>
struct LinkCutTreeBase:Splay{
    using Node = typename Splay::Node;
   using Ptr = Node*;
   using T = typename Node::value_type;
   Ptr expose(Ptr t) {
        Ptr pc=nullptr; // preferred child
        for (Ptr cur=t; cur; cur=cur->p) {
            this->splay(cur);
            cur->r=pc;
            this->pull(cur);
            pc=cur;
       this->splay(t);
        return pc;
    void evert(Ptr t) { // make t be the root of the tree
        expose(t);
        this->toggle(t);
        this->push(t);
    void link(Ptr u,Ptr v){ // attach u to v
        evert(u);
       expose(v);
```

```
void cut(Ptr u,Ptr v){ // cut edge between u and v
        evert(u);
        expose(v);
        assert (u->p==v);
        v->1=u->p=nullptr;
        this->pull(v);
    Ptr get_root(Ptr t){
        expose(t);
        while (t->1) this->push (t), t=t->1;
        this->splay(t);
        return t;
    Ptr lca(Ptr u,Ptr v) {
        if (get_root(u)!=get_root(v)) return nullptr;
        expose(u);
        return expose(v);
    void set_val(Ptr t,const T &val){
        this->evert(t);
        t->val=val;
        this->pull(t);
    T get_val(Ptr t){
        this->evert(t);
        return t->val;
    T fold(Ptr u,Ptr v) {
        evert(u);
        expose(v);
        return v->sum;
LazyLinkCutTree.hpp
Description: Lazy Link Cut Tree.
Usage: using Lct = LazyLinkCutTree<Action>;
using Ptr = Lct::Ptr;
using Node = Lct:: Node;
vector<Ptr> ptr(n);
for(int i=0;i<n;i++)ptr[i]=new Node(val[i]);</pre>
auto link=[](int u,int v){
Lct::link(ptr[u],ptr[v]);
auto cut=[](int u,int v){
Lct: : cut(ptr[u],ptr[v]);
auto update=[](int u,int v,Action:: Tag val){
Lct: : apply(ptr[u],ptr[v],val);
auto query=[](int u,int v){
return Lct::fold(ptr[u],ptr[v]);
"LazyReversibleSplayTree.hpp", "LinkCutTreeBase.hpp"
                                                      ead3da, 12 lines
template < class MonoidAction>
struct LazyLinkCutTree:LinkCutTreeBase<LazyReversibleSplayTree<</pre>
     MonoidAction>>{
    using base = LinkCutTreeBase<LazyReversibleSplayTree<</pre>
         MonoidAction>>;
    using Ptr = typename base::Ptr;
    using Tag = typename MonoidAction::Tag;
    void apply(Ptr u,Ptr v,const Tag &val){
        this->evert(u);
        this->expose(v);
        this->propagate(v,val);
```

u->p=v;

Number Theory (5)

```
Extended Euclid. hpp
```

Description: Extended Euclid algorithm for solving diophantine equation (ax + by = gcd(a, b)).

Time: $\mathcal{O}(\log \max\{a,b\})$

"../template/Header.hpp" 229e7c, 13 lines
pair<11,11> euclid(11 a,11 b) {
 11 x=1, y=0, x1=0, y1=1;
 while (b!=0) {
 11 q=a/b;
 x-=q*x1;
 y-=q*y1;
 a-=q*b;
 swap (x, x1);
 swap (y, y1);
 swap (a, b);
 }
 return {x,y};

5.1 Prime Numbers

LinearSieve.hpp

Description: Prime Number Generator in Linear Time

Time: $\mathcal{O}(N)$

```
"../template/Header.hpp" 194fb1, 15 lines
vi linear_sieve(int n) {
  vi prime, composite(n + 1);
  for(int i=2; i<=n; ++i) {
    if(!composite[i]) {
      prime.emplace_back(i);
    }
    for(int j=0; j<(int) prime.size() && i*prime[j]<=n; ++j) {
      composite[i * prime[j]] = true;
      if(i % prime[j] == 0) {
         break;
    }
    }
  }
  return prime;
}</pre>
```

FastEratosthenes.hpp

Description: Prime sieve for generating all primes smaller than LIM. **Time:** LIM= $1e9 \approx 1.5s$

```
"../template/Header.hpp"
                                                      295b58, 33 lines
const int LIM = 1e6;
bitset<LIM> isPrime;
vi eratosthenes() {
  const int S = (int) round(sqrt(LIM)), R = LIM / 2;
  vi pr = \{2\}, sieve(S + 1);
  pr.reserve(int(LIM/log(LIM) * 1.1));
  vector<pii> cp;
  for(int i=3; i<=S; i+=2) {
    if(!sieve[i]) {
      cp.emplace_back(i, i * i / 2);
      for(int j=i*i; j<=S; j+=2*i) {
        sieve[j] = 1;
  for(int L=1; L<=R; L+=S) {
    array<bool, S> block{};
    for(auto &[p, idx]: cp) {
```

```
for(int i=idx; i<S+L; idx=(i+=p)) {</pre>
        block[i - L] = 1;
    for(int i=0; i<min(S, R-L); ++i) {</pre>
      if(!block[i]) {
        pr.emplace_back((L + i) * 2 + 1);
  for(int i: pr) {
    isPrime[i] = 1;
 return pr;
GolbatchConjecture.hpp
Description: Find two prime numbers which sum equals s
Time: \mathcal{O}(N \log N)
"FastEratosthenes.hpp"
                                                       88fb23, 18 lines
pair<int, int> goldbatchConjecture(int s, vi pr = {}) {
 if (s <= 2 || s % 2 != 0) {
    return make_pair(-1, -1);
 if (pr.size() == 0) {
    pr = eratosthenes();
 for (auto x : pr) {
    if (x > s / 2) {
      break;
    int d = s - x;
    if (binary_search(pr.begin(), pr.end(), d)) {
      return make_pair(min(x, d), max(x, d));
  return make_pair(-1, -1);
```

$\underline{\text{Graph}}$ (6)

6.1 Matching

HopcroftKarp.hpp

Description: Fast bipartite matching algorithm.

Time: $\mathcal{O}\left(E\sqrt{V}\right)$

```
"../template/Header.hpp"
                                                        0bd56f, 52 lines
struct HopcroftKarp{
    int n, m;
    vi l,r,lv,ptr;
   vector<vi> adj;
   HopcroftKarp(){}
   HopcroftKarp(int _n,int _m){init(_n,_m);}
   void init(int _n,int _m){
        n=_n, m=_m;
        adj.assign(n+m, vi{});
   void addEdge(int u,int v){
        adj[u].emplace_back(v+n);
   void bfs() {
        lv=vi(n,-1);
        queue<int> q;
        for (int i=0; i< n; i++) if (1[i]==-1) {
            lv[i]=0;
             q.emplace(i);
```

```
while(!q.empty()){
        int u=q.front();
        q.pop();
        for (int v:adj[u]) if (r[v]!=-1&&lv[r[v]]==-1) {
            lv[r[v]]=lv[u]+1;
            q.emplace(r[v]);
bool dfs(int u){
    for(int &i=ptr[u];i<sz(adj[u]);i++){</pre>
        int v=adj[u][i];
        if (r[v] ==-1||(lv[r[v]] ==lv[u]+1&&dfs(r[v]))){
            l[u]=v,r[v]=u;
            return true;
    return false;
int maxMatching() {
    int match=0, cnt=0;
    l=r=vi(n+m,-1);
        ptr=vi(n);
        bfs();
        cnt=0;
        for (int i=0; i<n; i++) if (l[i] ==-1&&dfs(i))cnt++;
    }while(cnt);
    return match;
```

Kuhn.hpp

};

Description: Kuhn Algorithm to find maximum bipartite matching or find augmenting path in bipartite graph.

```
Time: \mathcal{O}\left(VE\right)
```

```
"../template/Header.hpp" fc7d17, 15 lines
vi adj[1010], match(1010, -1);
bitset<1010> visited;
bool kuhn(int u) {
   if(visited[u]) {
      return false;
   }
   visited[u] = true;
   for(auto x: adj[u]) {
      if(match[x] == -1 || kuhn(match[x])) {
       match[x] = u;
      return true;
    }
   }
   return false;
}
```

6.2 Network Flow

Dinic.hpp

Description: Fast max-flow algorithm.

Time: $\mathcal{O}(VE \log U)$ where $U = \max |\operatorname{cap}|$

```
"../template/Header.hpp" 7409c7, 68 lines
template<class T>
struct Dinic{
    struct Edge{
        int to;
        ll flow, cap;
        Edge(int _to,ll _cap):to(_to),flow(0),cap(_cap){}
        ll getcap(){
            return cap-flow;
        }
}
```

```
};
int n:
11 U;
vector<Edge> e;
vector<vi> adj;
vi ptr, lvl;
Dinic(){}
Dinic(int _n) {
    init(_n);
void init(int _n){
    n=_n, U=0;
    e.clear();
    adj.assign(n, {});
void addEdge(int u,int v,ll cap){
    U=max(U,cap);
    adj[u].emplace_back(sz(e));
    e.emplace_back(v,cap);
    adj[v].emplace_back(sz(e));
    e.emplace_back(u,0); // change 0 to cap for undirected
bool bfs(int s,int t,ll scale) {
    lvl.assign(n,0);
    vi q{s};
    lv1[s]=1;
    for (int i=0; i < sz(q); i++) {
        int u=q[i];
        for(auto j:adj[u])if(!lvl[e[j].to]&&e[j].getcap()>=
            q.emplace_back(e[j].to);
            lvl[e[j].to]=lvl[u]+1;
    return lvl[t];
11 dfs(int u,int t,ll f){
    if (u==t||!f) return f;
    for(int &i=ptr[u];i<sz(adj[u]);i++){</pre>
        int j=adj[u][i];
        if (lvl[e[i].to]==lvl[u]+1) {
            if(ll p=dfs(e[j].to,t,min(f,e[j].getcap()))){
                 e[i].flow+=p;
                 e[j^1].flow-=p;
                 return p;
    return 0;
11 flow(int s,int t){
    for(ll L=111<<(63-_builtin_clzl1(U));L>0;L>>=1) //L =
          1 may be faster but it's O(V^2 E)
    while(bfs(s,t,L)){
        ptr.assign(n,0);
        while(ll p=dfs(s,t,LINF))flow+=p;
    };
    return flow;
```

```
MinCostFlow.hpp
```

};

Description: minimum-cost flow algorithm. **Time:** $\mathcal{O}(FE \log V)$ where F is max flow.

"../template/Header.hpp"

template<class F,class C>
struct MinCostFlow{

8ea1d2, 83 lines

```
struct Edge{
    int to:
   F flow, cap;
    Edge(int _to,F _cap,C _cost):to(_to),flow(0),cap(_cap),
         cost(cost){}
    F getcap(){
        return cap-flow;
};
int n;
vector<Edge> e;
vector<vi> adj;
vector<C> pot, dist;
vi pre;
bool neg;
const F FINF=numeric_limits<F>::max()/2;
const C CINF=numeric_limits<C>::max()/2;
MinCostFlow(){}
MinCostFlow(int _n) {
    init(_n);
void init(int n){
    e.clear();
    adj.assign(n,{});
    neg=false;
void addEdge(int u,int v,F cap,C cost){
    adj[u].emplace_back(sz(e));
    e.emplace_back(v,cap,cost);
    adj[v].emplace_back(sz(e));
    e.emplace_back(u,0,-cost);
    if (cost<0) neg=true;</pre>
bool dijkstra(int s, int t) {
    using P = pair<C, int>;
    dist.assign(n,CINF);
    pre.assign(n,-1);
    priority_queue<P, vector<P>, greater<P>> pq;
    dist[s]=0;
    pg.emplace(0,s);
    while(!pq.empty()){
        auto [d,u]=pq.top();
        pq.pop();
        if (dist[u] < d) continue;
        for(int i:adj[u]){
            int v=e[i].to;
            C ndist=d+pot[u]-pot[v]+e[i].cost;
            if(e[i].getcap()>0&&dist[v]>ndist){
                pre[v]=i;
                 dist[v]=ndist;
                pq.emplace(ndist, v);
    return dist[t] < CINF;
pair<F,C> flow(int s,int t) {
   F flow=0;
    C cost=0;
    pot.assign(n,0);
    if (neg) for (int t=0; t< n; t++) for (int i=0; i< sz(e); i++) if (e
         [i].getcap()>0){
        int u=e[i^1].to, v=e[i].to;
        pot[v]=min(pot[v],pot[u]+e[i].cost);
    } // Bellman—Ford
    while(dijkstra(s,t)){
        for(int i=0;i<n;i++)pot[i]+=dist[i];</pre>
```

```
F aug=FINF;
    for(int u=t;u!=s;u=e[pre[u]^1].to){
        aug=min(aug,e[pre[u]].getcap());
} // find bottleneck
    for(int u=t;u!=s;u=e[pre[u]^1].to){
        e[pre[u]].flow+=aug;
        e[pre[u]^1].flow-=aug;
} // push flow
    flow+=aug;
    cost+=aug*pot[t];
}
return {flow,cost};
};
```

Polynomials (7)

FormalPowerSeries.hpp

Description: basic operations of formal power series

```
416433, 136 lines
template<class mint>
struct FormalPowerSeries:vector<mint>{
    using vector<mint>::vector;
    using FPS = FormalPowerSeries;
    FPS & operator += (const FPS & rhs) {
        if(rhs.size()>this->size())this->resize(rhs.size());
        for(int i=0;i<rhs.size();i++)(*this)[i]+=rhs[i];</pre>
        return *this;
    FPS & operator += (const mint &rhs) {
        if(this->empty())this->resize(1);
        (*this)[0]+=rhs;
        return *this;
    FPS & operator -= (const FPS & rhs) {
        if (rhs.size()>this->size())this->resize(rhs.size());
        for(int i=0;i<rhs.size();i++)(*this)[i]-=rhs[i];</pre>
        return *this;
    FPS & operator -= (const mint &rhs) {
        if(this->empty())this->resize(1);
        (*this)[0]-=rhs;
        return *this;
    FPS &operator *= (const FPS &rhs) {
        auto res=NTT<mint>()(*this,rhs);
        return *this=FPS(res.begin(),res.end());
    FPS & operator *= (const mint &rhs) {
        for(auto &a:*this)a*=rhs;
        return *this;
    friend FPS operator+(FPS lhs, const FPS &rhs) {return lhs+=
    friend FPS operator+(FPS lhs,const mint &rhs) {return lhs+=
    friend FPS operator+(const mint &lhs, FPS &rhs) {return rhs+=
    friend FPS operator-(FPS lhs, const FPS &rhs) {return lhs-=
    friend FPS operator-(FPS lhs, const mint &rhs) {return lhs-=
    friend FPS operator-(const mint &lhs, FPS rhs) {return -(rhs-
    friend FPS operator* (FPS lhs, const FPS &rhs) {return lhs*=
```

return (pre(deg).diff()*inv(deg)).pre(deg-1).integral()

```
friend FPS operator* (FPS lhs, const mint &rhs) {return lhs*=
friend FPS operator* (const mint &lhs, FPS rhs) {return rhs*=
     lhs;}
FPS operator-(){return (*this)*-1;}
FPS rev() {
    FPS res(*this);
    reverse(res.beign(),res.end());
    return res;
FPS pre(int sz){
    FPS res(this->begin(),this->begin()+min((int)this->size
         (),sz));
    if(res.size() < sz) res.resize(sz);</pre>
    return res;
FPS shrink(){
    FPS res(*this);
    while(!res.empty() &&res.back() ==mint{}) res.pop_back();
    return res;
FPS operator>>(int sz){
    if(this->size()<=sz)return {};</pre>
    FPS res(*this);
    res.erase(res.begin(),res.begin()+sz);
    return res;
FPS operator << (int sz) {
    FPS res(*this);
    res.insert(res.begin(),sz,mint{});
    return res;
FPS diff(){
    const int n=this->size();
    FPS res(max(0,n-1));
    for (int i=1; i<n; i++) res[i-1] = (*this)[i] *mint(i);
    return res;
FPS integral(){
    const int n=this->size();
    FPS res(n+1);
    res[0]=0;
    if (n>0) res[1]=1;
    11 mod=mint::get_mod();
    for (int i=2; i<=n; i++) res[i]=(-res[mod%i]) * (mod/i);</pre>
    for (int i=0; i<n; i++) res[i+1] *= (*this)[i];
    return res;
mint eval(const mint &x) {
    mint res=0, w=1;
    for(auto &a:*this)res+=a*w,w*=x;
    return res:
FPS inv(int deg=-1) {
    assert(!this->empty()&&(*this)[0]!=mint(0));
    if (deg==-1) deg=this->size();
    FPS res{mint(1)/(*this)[0]};
    for(int i=2;i>>1<deq;i<<=1){</pre>
        res=(res*(mint(2)-res*pre(i))).pre(i);
    return res.pre(deg);
FPS log(int deg=-1){
    assert(!this->empty()&&(*this)[0] ==mint(1));
    if (deg==-1) deg=this->size();
```

```
FPS exp(int deg=-1) {
        assert(this->empty() | | (*this)[0] == mint(0));
        if (deg==-1) deg=this->size();
        FPS res{mint(1)};
        for(int i=2;i>>1<deq;i<<=1){</pre>
             res=(res*(pre(i)-res.log(i)+mint(1))).pre(i);
        return res.pre(deg);
    FPS pow(ll k,int deg=-1){
        const int n=this->size();
         if (deg==-1) deg=n;
        i.f(k==0) {
             FPS res(deg);
             if (deg) res[0] = mint(1);
             return res;
         for(int i=0;i<n;i++){</pre>
             if (__int128_t(i)*k>=deg)return FPS(deg,mint(0));
             if((*this)[i]==mint(0))continue;
             mint rev=mint(1)/(*this)[i];
             FPS res=(((*this*rev)>>i).log(deg)*k).exp(deg);
             res=((res*binpow((*this)[i],k))<<(i*k)).pre(deg);
             return res;
        return FPS(deg,mint(0));
using FPS=FormalPowerSeries<mint>;
FFT.hpp
Description: Fast Fourier transform
Time: \mathcal{O}(N \log N)
"../template/Header.hpp"
                                                         5d476b, 73 lines
template<class T=11,int mod=0>
struct FFT{
 using vt = vector<T>;
 using cd = complex<db>;
 using vc = vector<cd>;
  static const bool INT=true;
  static void fft(vc &a){
    int n=a.size(),L=31-__builtin_clz(n);
    vc rt(n);
    rt[1]=1;
    for (int k=2; k < n; k *=2) {
      cd z=polar(db(1),PI/k);
      for (int i=k; i<2*k; i++) rt[i]=i&1?rt[i/2]*z:rt[i/2];</pre>
    vi rev(n);
    for (int i=1; i<n; i++) rev[i] = (rev[i/2] | (i&1) <<L) /2;</pre>
    for (int i=1; i<n; i++) if (i<rev[i]) swap(a[i], a[rev[i]]);</pre>
    for (int k=1; k < n; k *=2) for (int i=0; i < n; i+2 \times k) for (int j=0; j < k
         ; j++) {
      cd z=rt[j+k]*a[i+j+k];
      a[i+j+k]=a[i+j]-z;
      a[i+j]+=z;
 template<class U>
  static db norm(const U &x) {
    return INT?round(x):x;
 static vt conv(const vt &a,const vt &b) {
    if(a.empty()||b.empty())return {};
```

```
vt res(a.size()+b.size()-1);
    int L=32-__builtin_clz(res.size()), n=1<<L;</pre>
    vc in(n), out(n);
     copy(a.begin(),a.end(),in.begin());
     for (int i=0; i < b.size(); i++) in[i].imag(b[i]);</pre>
     fft(in):
     for(auto &x:in)x*=x;
     for(int i=0;i<n;i++)out[i]=in[-i&(n-1)]-conj(in[i]);</pre>
     fft(out);
     for (int i=0; i < res. size(); i++) res[i] = norm(imag(out[i]) / (4*n)
         );
    return res;
  static vl convMod(const vl &a,const vl &b) {
    assert (mod>0);
    if(a.empty()||b.empty())return {};
    vl res(a.size()+b.size()-1);
    int L=32-__builtin_clz(res.size()), n=1<<L;</pre>
    11 cut=int(sqrt(mod));
    vc in1(n),in2(n),out1(n),out2(n);
     for (int i=0; i<a.size(); i++) in1[i]=cd(l1(a[i])/cut,l1(a[i])%</pre>
          cut); // a1 + i * a2
     for(int i=0;i<b.size();i++)in2[i]=cd(ll(b[i])/cut,ll(b[i])%</pre>
          cut); // b1 + i * b2
     fft(in1), fft(in2);
     for (int i=0; i<n; i++) {</pre>
       int j=-i\&(n-1);
       out1[j] = (in1[i] + conj(in1[j])) * in2[i] / (2.1*n); // f1 * (g1)
             + i * g2) = f1 * g1 + i f1 * g2
       out2[j]=(in1[i]-conj(in1[j]))*in2[i]/cd(0.1,2.1*n); // f2
             * (g1 + i * g2) = f2 * g1 + i f2 * g2
    fft(out1),fft(out2);
     for(int i=0;i<res.size();i++){</pre>
      11 x=round(real(out1[i])),y=round(imag(out1[i]))+round(
            real(out2[i])), z=round(imag(out2[i]));
       res[i] = ((x \mod \times \text{cut} + y) \mod \times \text{cut} + z) \mod ; // a1 * b1 * cut^2
            + (a1 * b2 + a2 * b1) * cut + a2 * b2
    return res:
  vt operator()(const vt &a,const vt &b){
     return mod>0?conv(a,b):convMod(a,b);
};
template<>
struct FFT<db>{
 static const bool INT=false;
};
NTT.hpp
Description: Number theoretic transform
Time: \mathcal{O}(N \log N)
"../template/Header.hpp", "../modular-arithmetic/BinPow.hpp",
"../modular-arithmetic/MontgomeryModInt.hpp"
                                                         2b2392, 39 lines
template < class mint = mint >
struct NTT{
  using vm = vector<mint>;
  static constexpr mint root=mint::get_root();
    static_assert(root!=0);
  static void ntt(vm &a){
    int n=a.size(),L=31-__builtin_clz(n);
    vm rt(n);
    rt[1]=1;
     for (int k=2, s=2; k < n; k *=2, s++) {
      mint z[]=\{1, binpow(root, MOD>>s)\};
      for (int i=k; i<2*k; i++) rt[i]=rt[i/2]*z[i&1];
```

525bf4, 59 lines

DVC SlopeTrick GaussianElimination BinaryTrie

```
vi rev(n);
    for (int i=1; i<n; i++) rev[i] = (rev[i/2] | (i&1) <<L) /2;</pre>
    for (int i=1; i < n; i++) if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
    for (int k=1; k < n; k \times = 2) for (int i=0; i < n; i+=2 \times k) for (int j=0; j < k
         ; j++) {
      mint z=rt[j+k]*a[i+j+k];
      a[i+j+k]=a[i+j]-z;
      a[i+j]+=z;
  static vm conv(const vm &a,const vm &b) {
    if(a.empty()||b.empty())return {};
    int s=a.size()+b.size()-1, n=1<<(32-__builtin_clz(s));</pre>
    mint inv=mint(n).inv();
    vm in1(a),in2(b),out(n);
    in1.resize(n),in2.resize(n);
    ntt(in1),ntt(in2);
    for (int i=0; i<n; i++) out [-i&(n-1)]=in1[i]*in2[i]*inv;</pre>
    return vm(out.begin(),out.begin()+s);
  vm operator()(const vm &a,const vm &b){
    return conv(a,b);
};
```

Dynamic Programming (8)

DVC.hpp

```
Description: Optimize O(N^2K) to O(NK \log N)
```

```
"../template/Header.hpp"
                                                       aa5ddf, 19 lines
vector<vl> cst, dp;
11 cost(int 1, int r) {
 return cst[l][r];
void divide(int 1, int r, int opt_1, int opt_r, int c) {
  if(1 > r) return;
  int mid = (1 + r) / 2;
  pair<11, int> best = make_pair(INF, -1);
  for(int k=opt_l; k<=min(mid, opt_r); ++k) {</pre>
   best = min(best, make_pair(dp[c - 1][k] + cost(k + 1, mid),
          k));
  dp[c][mid] = best.first;
  divide(1, mid - 1, opt_1, best.second, c);
  divide (mid + 1, r, best.second, opt_r, c);
// for (int c=1; c<=K; ++c) divide(1, N, 1, N, c);
```

SlopeTrick.hpp

Description: Absolute Smth

lz_r -= extending_value;

```
extending = true;
    if(ms_1.empty() && ms_r.empty()) {
     ms l.emplace(v);
     ms_r.emplace(v);
   else if(v <= *ms_l.rbegin() + lz_l) {</pre>
     min_y += (*ms_l.rbegin() + lz_l) - v;
     ms r.emplace(*ms_l.rbegin() + lz_l - lz_r);
     ms_l.erase(--ms_l.end());
     ms_l.emplace(v - lz_l);
     ms_l.emplace(v - lz_l);
    else if(v \ge *ms_r.begin() + lz_r) {
     min_y += v - (*ms_r.begin() + lz_r);
     ms_l.emplace(*ms_r.begin() + lz_r - lz_l);
     ms_r.erase(ms_r.begin());
     ms_r.emplace(v - lz_r);
     ms_r.emplace(v - lz_r);
    else {
     ms_1.emplace(v - lz_1);
     ms_r.emplace(v - lz_r);
};
```

8.1 Various

return res;

};

Gaussian Elimination.hpp Description: Gaussian Elimination

```
"../template/Header.hpp"
                                                       e89ecb, 34 lines
struct Gauss {
 int n, sz;
 vector<11> basis;
 Gauss(int n = 0) {
    init(n):
 void init(int _n) {
    n = n, sz = 0;
    basis.assign(n, 0);
 void insert(ll x) {
    for (int i = n - 1; i >= 0; i--)
      if (x >> i & 1) {
        if (!basis[i]) {
          basis[i] = x;
          sz++;
          return;
          ^= basis[i];
 ll \ getmax(ll \ k = 0)  {
    11 \text{ tot} = 111 << sz, res = 0;
    for (int i = n - 1; i >= 0; i--)
      if (basis[i]) {
        tot >>= 1;
        if ((k >= tot && res >> i & 1) || (k < tot && res >> i
             & 1 ^ 1))
          res ^= basis[i];
        if (k >= tot)
          k -= tot;
```

```
BinaryTrie.hpp
Description: Binary Trie
".../template/Header.hpp"
```

```
using node_t = array<int, 2>;
template<size t S>
struct binary trie {
 vector<node_t> t = {node_t()};
  vector<int> cnt = {0};
 int cnt_nodes = 0;
 void insert(int v)
   int cur = 0;
    cnt[0]++;
    for(int i=S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1: 0;
      if(!t[cur][b]) {
       t[cur][b] = ++cnt_nodes;
        t.emplace_back(node_t());
        cnt.emplace_back(0);
      cnt[t[cur][b]]++;
      cur = t[cur][b];
 void remove(int v) {
    int cur = 0;
    cnt[0]--;
    for(int i=S-1; i>=0; --i) {
     int b = (v \& (1 << i)) ? 1: 0;
      cnt[t[cur][b]]--;
      cur = t[cur][b];
  int get_min(int v) {
    int cur = 0, res = 0;
    for(int i=(int) S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1 : 0;
      if(t[cur][b] && cnt[t[cur][b]]) {
        cur = t[cur][b];
      else {
        res |= (1 << i);
        cur = t[cur][!b];
    return res;
  int get max(int v) {
    int cur = 0, res = 0;
    for (int i = (int) S-1; i>=0; --i) {
      int b = (v \& (1 << i)) ? 1 : 0;
      if(t[cur][!b] && cnt[t[cur][!b]]) {
        res |= (1 << i);
        cur = t[cur][!b];
      else {
        cur = t[cur][b];
    return res;
};
```

Competitive Programming Topics



topics.txt

Bitonic cycle

159 lines

Recursion Divide and conquer Finding interesting points in N log N Algorithm analysis Master theorem Amortized time complexity Greedy algorithm Scheduling Max contiguous subvector sum Invariants Huffman encoding Graph theory Dynamic graphs (extra book-keeping) Breadth first search Depth first search * Normal trees / DFS trees Dijkstra's algorithm MST: Prim's algorithm Bellman-Ford Konig's theorem and vertex cover Min-cost max flow Lovasz toggle Matrix tree theorem Maximal matching, general graphs Hopcroft-Karp Hall's marriage theorem Graphical sequences Flovd-Warshall Euler cycles Flow networks * Augmenting paths * Edmonds-Karp Bipartite matching Min. path cover Topological sorting Strongly connected components Cut vertices, cut-edges and biconnected components Edge coloring * Trees Vertex coloring * Bipartite graphs (=> trees) * 3^n (special case of set cover) Diameter and centroid K'th shortest path Shortest cycle Dynamic programming Knapsack Coin change Longest common subsequence Longest increasing subsequence Number of paths in a dag Shortest path in a dag Dynprog over intervals Dynprog over subsets Dynprog over probabilities Dynprog over trees 3^n set cover Divide and conquer Knuth optimization Convex hull optimizations RMQ (sparse table a.k.a 2^k-jumps)

Log partitioning (loop over most restricted) Combinatorics Computation of binomial coefficients Pigeon-hole principle Inclusion/exclusion Catalan number Pick's theorem Number theory Integer parts Divisibility Euclidean algorithm Modular arithmetic * Modular multiplication * Modular inverses * Modular exponentiation by squaring Chinese remainder theorem Fermat's little theorem Euler's theorem Phi function Frobenius number Quadratic reciprocity Pollard-Rho Miller-Rabin Hensel lifting Vieta root jumping Game theory Combinatorial games Game trees Mini-max Nim Games on graphs Games on graphs with loops Grundy numbers Bipartite games without repetition General games without repetition Alpha-beta pruning Probability theory Optimization Binary search Ternary search Unimodality and convex functions Binary search on derivative Numerical methods Numeric integration Newton's method Root-finding with binary/ternary search Golden section search Matrices Gaussian elimination Exponentiation by squaring Sorting Radix sort Geometry Coordinates and vectors * Cross product * Scalar product Convex hull Polygon cut Closest pair Coordinate-compression Quadtrees KD-trees All segment-segment intersection Discretization (convert to events and sweep) Angle sweeping Line sweeping Discrete second derivatives Strings

Longest common substring Palindrome subsequences Knuth-Morris-Pratt Tries Rolling polynomial hashes Suffix array Suffix tree Aho-Corasick Manacher's algorithm Letter position lists Combinatorial search Meet in the middle Brute-force with pruning Best-first (A*) Bidirectional search Iterative deepening DFS / A* Data structures LCA (2^k-jumps in trees in general) Pull/push-technique on trees Heavy-light decomposition Centroid decomposition Lazy propagation Self-balancing trees Convex hull trick (wcipeg.com/wiki/Convex_hull_trick) Monotone queues / monotone stacks / sliding queues Sliding queue using 2 stacks Persistent segment tree

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