Advanced Epidemiological Analysis

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2021-04-05

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Overview

This is a the coursebook for the Colorado State University course ERHS 732, Advanced Epidemiological Analysis. This course provides the opportunity to implement theoretical expertise through designing and conducting advanced epidemiologic research analyses and to gain in-depth experience analyzing datasets from the environmental epidemiology literature.

1.1 License

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Course information

This is a the coursebook for the Colorado State University course ERHS 732, Advanced Epidemiological Analysis. This course provides the opportunity to implement theoretical expertise through designing and conducting advanced epidemiologic research analyses and to gain in-depth experience analyzing datasets from the environmental epidemiology literature. This course will complement the student's training in advanced epidemiological methods, leveraging regression approaches and statistical programming, providing the opportunity to implement their theoretical expertise through designing and conducting advanced epidemiologic research analyses. During the course, students will gain in-depth experience analyzing two datasets from the environmental epidemiology literature—(1) time series data with daily measures of weather, air pollution, and cardiorespiratory outcomes in London, England and (2) a dataset with measures from the Framingham Heart Study. Additional datasets and studies will be discussed and explored as a supplement.

This class will utilize a variety of instructional formats, including short lectures, readings, topic specific examples from the substantive literature, discussion and directed group work on in-course coding exercises putting lecture and discussion content into practice. A variety of teaching modalities will be used, including group discussions, student directed discussions, and in-class group exercises. It is expected that before coming to class, students will read the required papers for the week, as well as any associated code included in the papers' supplemental materials. Students should come to class prepared to do statistical programming (i.e., bring a laptop with statistical software, download any datasets needed for the week etc). Participation is based on in-class coding exercises based on each week's topic. If a student misses a class, they will be expected to complete the in-course exercise outside of class to receive credit for participation in that exercise. Students will be required to do mid-term and final projects which will be presented in class and submitted as a written write-up describing the project.

Prerequisites for this course are:

- ERHS 534 or ERHS 535 and
- ERHS 640 and
- STAR 511 or STAT 511A or STAT 511B

2.1 Course learning objectives

The learning objectives for this proposed course complement core epidemiology and statistics courses required by the program and provide the opportunity for students to implement theoretical skills and knowledge gained in those courses in a more applied setting.

Upon successful completion of this course students will be able to:

- 1. List several possible statistical approaches to answering an epidemiological research questions. (Knowledge)
- 2. Choose among analytical approaches learned in previous courses to identify one that is reasonable for an epidemiological research question. (Application)
- 3. Design a plan for cleaning and analyzing data to answer an epidemiological research question, drawing on techniques learned in previous and concurrent courses. (Synthesis)
- 4. Justify the methods and code used to answer an epidemiological research question. (*Evaluation*)
- 5. Explain the advantages and limitations of a chosen methodological approach for evaluating epidemiological data. (*Evaluation*)
- 6. Apply advanced epidemiological methods to analyze example data, using a regression modeling framework. (Application)
- 7. Apply statistical programming techniques learned in previous courses to prepare epidemiological data for statistical analysis and to conduct the analysis. (Application)
- 8. Interpret the output from statistical analyses of data for an epidemiological research question. (*Evaluation*)
- 9. Defend conclusions from their analysis. (Comprehension)
- 10. Write a report describing the methods, results, and conclusions from an epidemiological analysis. (Application)
- 11. Construct a reproducible document with embedded code to clean and analyze data to answer an epidemiological research question. (Application)

2.2 Meeting time and place

[To be determined]

2.3 Class Structure and Expectations

• Homework/preparation: Every two weeks we will focus on a different topic. It is expected that *before* coming to class, students will read the required papers for the week, as well as any associated code included in the papers' supplemental materials. Students should come to class prepared to prepared to do statistical programming (i.e., bring in a laptop with statistical software, download any datasets needed for the week).

• In-class schedule:

- Topic overview: Each class will start with a vocabulary quiz on a select number of the words from the chapter's vocabulary list.
- Discussion of analysis and coding points: Students and faculty will be divided into small groups to discuss the chapter and think more deeply about the content. This is a time to bring up questions and relate the chapter concepts to other datasets and/or analysis methods you are familiar with.
- Group work: In small groups, students will work on designing an epidemiological analysis for the week's topic and developing code to implement that analysis. Students will use the GitHub platform to work collaboratively during and between class meetings.
- Wrap-up: We will reconvene as one group at the end to discuss topics that came up in small group work and to outline expectations for students before the next meeting.

2.4 Course grading

| Assessment Components | Percentage of Grade | | |
|--------------------------------------|---------------------|--|--|
| Midterm written report | 30 | | |
| Midterm presentation | 15 | | |
| Final written report | 30 | | |
| Final presentation | 15 | | |
| Participation in in-course exercises | 10 | | |

2.5 Textbooks and Course Materials

Readings for this course will focus on peer-reviewed literature that will be posted for the students in the class. Additional references that will be useful to students throughout the semester include:

- Garrett Grolemund and Hadley Wickham, *R for Data Science*, O'Reilly, 2017. (Available for free online at https://r4ds.had.co.nz/ and in print through most large book sellers.)
- Miguel A. Hernan and James M. Robins, Causal Inference: What If, Boca Raton: Chapman & Hall/CRC, 2020. (Available for free online at https://cdn1.sph.harvard.edu/wp-content/uploads/sites/1268/2021/01/ciwha

- tif_hernanrobins_31jan21.pdf with a print version anticipated in 2021.)
- Francesca Dominici and Roger D. Peng, Statistical Methods for Environmental Epidemiology with R, Springer, 2008. (Available online through the CSU library or in print through Springer.)

Time series / case-crossover study designs

3.1 Reading

The readings for this week are:

- Vicedo-Cabrera et al. (2019), with supplemental material available to download by clicking http://links.lww.com/EDE/B504
- Armstrong et al. (2014), with supplemental material available at https://bmcmedresmethodol.biomedcentral.com/articles/10.1186/1471-2288-14-122#Sec13

3.2 Time series data

[Exploring time series data with daily measurements of health outcomes and environmental exposures]

Andreas section

Brooke's section

Example datasets are available as part of the supplemental material for both of the articles in this chapter's readings. For Vicedo-Cabrera et al. (2019), the example data are available as the file "lndn_obs.csv". These data are saved in a csv format, and so they can be read into R using the read_csv function from the readr package (part of the tidyverse). For example, you can use the following code to read in these data, assuming you have saved them in a "data" subdirectory of your current working directory:

```
library(tidyverse) # Loads all the tidyverse packages, including readr
obs <- read_csv("data/lndn_obs.csv")
obs</pre>
```

```
## # A tibble: 8,279 x 14
##
                                                       all all_0_64 all_65_74 all_75_84
      date
                    vear month
                                   day
                                          doy dow
##
      <date>
                   <dbl> <dbl>
                                <dbl>
                                       <dbl> <chr>
                                                     <dbl>
                                                               <dbl>
                                                                          <dbl>
                                                                                      <dbl>
##
    1 1990-01-01
                    1990
                                            1 Mon
                                                       220
                                                                  38
                                                                              38
                                                                                         82
                              1
                                     1
    2 1990-01-02
                    1990
                                     2
                                                       257
                                                                  50
                                                                              67
                                                                                         87
##
                              1
                                            2 Tue
##
    3 1990-01-03
                    1990
                              1
                                     3
                                            3 Wed
                                                       245
                                                                  39
                                                                              59
                                                                                         86
                                     4
##
    4 1990-01-04
                    1990
                              1
                                            4 Thu
                                                       226
                                                                  41
                                                                              45
                                                                                         77
                                     5
##
    5 1990-01-05
                    1990
                              1
                                            5 Fri
                                                       236
                                                                  45
                                                                              54
                                                                                         85
    6 1990-01-06
                                     6
##
                    1990
                              1
                                            6 Sat
                                                       235
                                                                  48
                                                                              48
                                                                                         84
##
    7 1990-01-07
                    1990
                              1
                                     7
                                            7 Sun
                                                       231
                                                                  38
                                                                              49
                                                                                         96
##
    8 1990-01-08
                    1990
                              1
                                     8
                                            8 Mon
                                                       235
                                                                  46
                                                                              57
                                                                                         76
##
    9 1990-01-09
                    1990
                              1
                                     9
                                            9 Tue
                                                       250
                                                                  48
                                                                              54
                                                                                         96
   10 1990-01-10
##
                    1990
                              1
                                    10
                                           10 Wed
                                                       214
                                                                  44
                                                                              46
                                                                                         62
##
     ... with 8,269 more rows, and 4 more variables: all_85plus <dbl>,
       tmean <dbl>, tmin <dbl>, tmax <dbl>
```

This example dataset shows many characteristics that are common for datasets for time series studies in environmental epidemiology. General characteristics of time series data for environmental epidemiology studies are:

- Observations are given at an aggregated level. For example, instead of individual observations for each person in London, the obs data give counts of deaths throughout London. The level of aggregation is often determined by geopolitical boundaries, for example counties of ZIP codes in the US.
- Observations are given at regularly spaced time steps over a period. In the obs dataset, the time step is day. Typically, values will be provided continuously over that time period, with observations for each time step. Occasionally, however, the time series data may only be available for particular seasons (e.g., only warm season dates for an ozone study), or there may be some missing data on either the exposure or health outcome over the course of the study period.
- Daily observations are given for the health outcome, for the environmental exposure of interest, and for potential time-varying confounders. In the obs dataset, the health outcome is mortality (from all causes; sometimes, the health outcome will focus on a specific cause of mortality or other health outcome). Counts are given for everyone in the city for each day (all column), as well as for specific age categories (all_0_64 for all deaths among those up to 64 years old, and so on). The exposure of interest in the obs dataset is temperature, and three metrics of this are included (tmean, tmin, and tmax). Day of the week is one time-varying factor that could be a confounder, or at least help explain variation in the outcome (mortality). This is included through the dow variable in the obs data.

Sometimes, you will also see a marker for holidays included as a potential time-varying confounder, or other exposure variables (temperature is a potential confounder, for example, when investigating the relationship between air pollution and mortality risk).

 Multiple metrics of an exposure and / or multiple health outcome counts may be included for each time step. In the obs example, three metrics of temperature are included (minimum daily temperature, maximum daily temperature, and mean daily temperature). Several counts of mortality are included, providing information for specific age categories in the population.

When working with time series data, it is helpful to start with some exploratory data analysis. The following applied exercise will take you through some of the questions you might want to answer through this type of exploratory analysis. In general, the lubridate package is an excellent tool for working with date data in R (although, in the example code above, we mostly used tools from base R). You may find it worthwhile to explore this package some more. There is a helpful chapter in Wickham and Grolemund (2016), https://r4ds.had.co.nz/dates-and-times.html, as well as a cheatsheet at https://evoldyn.gitlab.io/evomics-2018/ref-sheets/R_lubridate.pdf. For visualizations, if you are still learning techniques in R, two books you may find useful are Healy (2018) (available online at https://www.cookbook-r.com/Graphs/).

Applied: Exploring time series data

Read the example time series data in R and explore it to answer the following questions:

- 1. What is the study period for the example obs dataset? (i.e., what dates / years are covered by the time series data?)
- 2. Are there any missing dates within this time period?
- 3. Are there seasonal trends in the exposure? In the outcome?
- 4. Are there long-term trends in the exposure? In the outcome?
- 5. Is the outcome associated with day of week? Is the exposure associated with day of week?

Based on your exploratory analysis in this section, talk about the potential for confounding when these data are analyzed to estimate the association between daily temperature and city-wide mortality. Is confounding by seasonal trends a concern? How about confounding by long-term trends in exposure and mortality? How about confounding by day of week?

Applied exercise: Example code

1. What is the study period for the example obs dataset? (i.e., what dates / years are covered by the time series data?)

In the obs dataset, the date of each observation is included in a column called date. The data type of this column is "Date"—you can check this by using the

class function from base R:

```
class(obs$date)
```

[1] "Date"

Since this column has a "Date" data type, you can run some mathematical function calls on it. For example, you can use the min function from base R to get the earliest date in the dataset and the max function to get the latest.

min(obs\$date)

```
## [1] "1990-01-01"
```

max(obs\$date)

```
## [1] "2012-08-31"
```

You can also run the range function to get both the earliest and latest dates with a single call:

```
range(obs$date)
```

```
## [1] "1990-01-01" "2012-08-31"
```

2. Are there any missing dates within this time period?

There are a few things you should check to answer this question. First (and easiest), you can check to see if there are any NA values within any of the observations in the dataset. The summary function will provide a summary of the values in each column of the dataset, including the count of missing values (NAs) if there are any:

summary(obs)

```
##
          date
                                year
                                                month
                                                                    day
##
            :1990-01-01
                                                   : 1.000
    Min.
                           Min.
                                   :1990
                                           Min.
                                                              Min.
                                                                     : 1.00
##
    1st Qu.:1995-09-01
                           1st Qu.:1995
                                           1st Qu.: 3.000
                                                              1st Qu.: 8.00
    Median :2001-05-02
                           Median:2001
                                           Median : 6.000
                                                              Median :16.00
##
            :2001-05-02
##
    Mean
                           Mean
                                   :2001
                                           Mean
                                                   : 6.464
                                                              Mean
                                                                      :15.73
    3rd Qu.:2006-12-31
                           3rd Qu.:2006
                                           3rd Qu.: 9.000
                                                              3rd Qu.:23.00
##
##
            :2012-08-31
                           Max.
                                   :2012
                                           Max.
                                                   :12.000
                                                              Max.
                                                                      :31.00
##
         doy
                          dow
                                                all
                                                               all_0_64
##
    Min.
                     Length:8279
                                          Min.
                                                  : 81.0
                                                            Min.
                                                                    : 9.0
               1.0
    1st Qu.: 90.5
                     Class : character
                                          1st Qu.:138.0
                                                            1st Qu.:27.0
##
##
    Median :180.0
                     Mode : character
                                          Median :157.0
                                                            Median:32.0
##
    Mean
            :181.3
                                          Mean
                                                  :160.2
                                                            Mean
                                                                    :32.4
##
    3rd Qu.:272.0
                                          3rd Qu.:178.0
                                                            3rd Qu.:37.0
##
    Max.
            :366.0
                                          Max.
                                                  :363.0
                                                            Max.
                                                                    :64.0
      all_65 74
                                          all 85plus
                                                               tmean
##
                        all 75 84
    Min.
            : 6.00
                             : 17.00
                                                : 17.00
                                                                  :-5.503
                     Min.
                                        Min.
                                                           Min.
                     1st Qu.: 41.00
                                        1st Qu.: 39.00
    1st Qu.:23.00
                                                           1st Qu.: 7.470
```

```
##
    Median :29.00
                     Median : 49.00
                                       Median : 45.00
                                                         Median :11.465
##
    Mean
           :30.45
                     Mean
                            : 50.65
                                       Mean
                                              : 46.68
                                                         Mean
                                                                :11.614
    3rd Qu.:37.00
                                       3rd Qu.: 53.00
                                                         3rd Qu.:15.931
                     3rd Qu.: 58.00
##
    Max.
           :70.00
                            :138.00
                                       Max.
                                              :128.00
                                                         Max.
                                                                :29.143
                     Max.
##
         tmin
                           tmax
##
    Min.
           :-8.940
                     Min.
                             :-3.785
##
    1st Qu.: 3.674
                      1st Qu.:10.300
##
    Median : 7.638
                      Median :14.782
##
    Mean
           : 7.468
                      Mean
                             :15.058
##
    3rd Qu.:11.438
                      3rd Qu.:19.830
   Max.
           :20.438
                      Max.
                             :37.087
```

Based on this analysis, all observations are complete for all dates included in the dataset.

However, this does not guarantee that every date between the start date and end date of the study period are included in the recorded data. Sometimes, some dates might not get recorded at all in the dataset, and the summary function won't help you determine when this is the case.

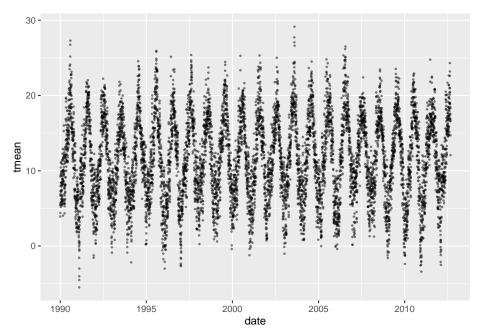
There are a few alternative explorations you can do. First, you can check the number of days between the start and end date of the study period, and then see if the number of observations in the dataset is the same:

3. Are there seasonal trends in the exposure? In the outcome?

You can use a simple plot to visualize patterns over time in both the exposure and the outcome. For example, the following code plots a dot for each daily temperature observation over the study period. The points are set to a smaller size (size = 0.5) and plotted with some transparency (alpha = 0.5) since there are so many observations.

```
ggplot(obs, aes(x = date, y = tmean)) +
geom_point(alpha = 0.5, size = 0.5)
```

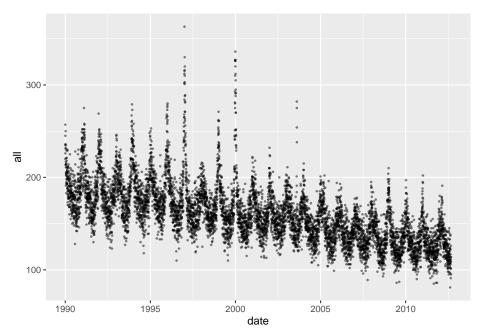
16 CHAPTER 3. TIME SERIES / CASE-CROSSOVER STUDY DESIGNS



There is clear evidence here of a strong seasonal trend in mean temperature, with values typically lowest in the winter and highest in the summer.

You can plot the outcome variable in the same way:

```
ggplot(obs, aes(x = date, y = all)) +
geom_point(alpha = 0.5, size = 0.5)
```

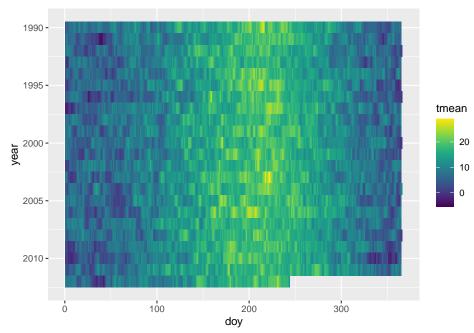


Again, there are seasonal trends, although in this case they are inversed. Mortality tends to be highest in the winter and lowest in the summer. Further, the seasonal pattern is not equally strong in all years—some years it has a much higher winter peak, probably in conjunction with severe influenza seasons.

Another way to look for seasonal trends is with a heatmap-style visualization, with day of year along the x-axis and year along the y-axis. This allows you to see patterns that repeat around the same time of the year each year (and also unusual deviations from normal seaonsal patterns).

For example, here's a plot showing temperature in each year, where the observations are aligned on the x-axis by time in year. We've reversed the y-axis so that the earliest years in the study period start at the top of the visual, then later study years come later—this is a personal style, and it would be no problem to leave the y-axis as-is. We've used the viridis color scale for the fill, since that has a number of features that make it preferable to the default R color scale, including that it is perceptible for most types of color blindness and be printed out in grayscale and still be correctly interpreted.

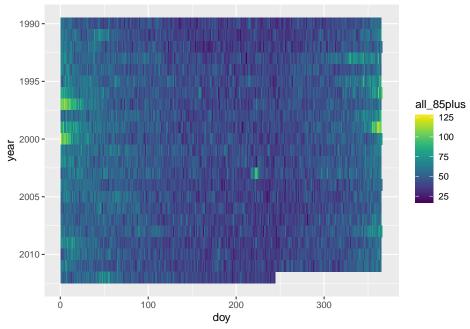
```
library(viridis)
ggplot(obs, aes(x = doy, y = year, fill = tmean)) +
  geom_tile() +
  scale_y_reverse() +
  scale_fill_viridis()
```



From this visualization, you can see that temperatures tend to be higher in the summer months and lower in the winter months. "Spells" of extreme heat or cold are visible—where extreme temperatures tend to persist over a period, rather than randomly fluctuating within a season. You can also see unusual events, like the extreme heat wave in the summer of 2003, indicated with the brightest yellow in the plot.

We created the same style of plot for the health outcome. In this case, we focused on mortality among the oldest age group, as temperature sensitivity tends to increase with age, so this might be where the strongest patterns are evident.

```
ggplot(obs, aes(x = doy, y = year, fill = all_85plus)) +
geom_tile() +
scale_y_reverse() +
scale_fill_viridis()
```

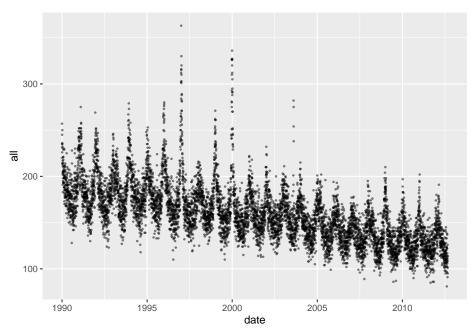


For mortality, there tends to be in increase in the winter compared to the summer. Some winters have stretches with particularly high mortality—these are likely a result of seasons with strong influenza outbreaks. You can also see on this plot the impact of the 2003 heat wave on mortality among this oldest age group.

4. Are there long-term trends in the exposure? In the outcome?

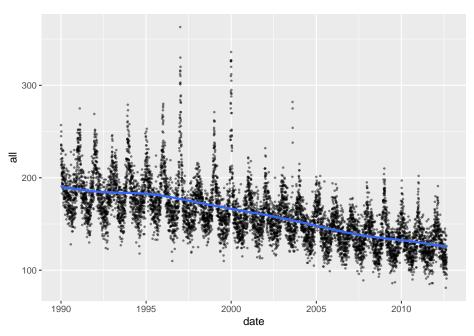
Some of the plots we created in the last section help in exploring this question. For example, the following plot shows a clear pattern of decreasing daily mortality counts, on average, over the course of the study period:

```
ggplot(obs, aes(x = date, y = all)) +
geom_point(alpha = 0.5, size = 0.5)
```



It can be helpful to add a smooth line to help detect these longer-term patterns, which you can do with <code>geom_smooth</code>:

```
ggplot(obs, aes(x = date, y = all)) +
geom_point(alpha = 0.5, size = 0.5) +
geom_smooth()
```



You could also take the median mortality count across each year in the study period, although you should take out any years without a full year's worth of data before you do this, since there are seasonal trends in the outcome:

```
obs %>%
  group_by(year) %>%
  filter(year != 2012) %>% # Take out the last year
  summarize(median_mort = median(all)) %>%
  ggplot(aes(x = year, y = median_mort)) +
  geom_line()
```



5. Is the outcome associated with day of week? Is the exposure associated with day of week?

The data already has day of week as a column in the data (dow). However, this is in a character data type, so it doesn't have the order of weekdays encoded (e.g., Monday comes before Tuesday). This makes it hard to look for patterns related to things like weekend / weekday.

class(obs\$dow)

[1] "character"

We could convert this to a factor and encode the weekday order when we do it, but it's even easier to just recreate the column from the date column. We used the wday function from the lubridate package to do this—it extracts weekday as a factor, with the order of weekdays encoded (using a special "ordered" factor type):

```
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
obs <- obs %>%
  mutate(dow = wday(date, label = TRUE))
class(obs$dow)
## [1] "ordered" "factor"
levels(obs$dow)
## [1] "Sun" "Mon" "Tue" "Wed" "Thu" "Fri" "Sat"
We looked at the mean, median, and 25th and 75th quantiles of the mortality
counts by day of week:
obs %>%
  group_by(dow) %>%
  summarize(mean(all),
            median(all),
            quantile(all, 0.25),
            quantile(all, 0.75))
## # A tibble: 7 x 5
            `mean(all)` `median(all)` `quantile(all, 0.25)` `quantile(all, 0.75)`
     dow
## * <ord>
                                 <dbl>
                  <dbl>
                                                        <dbl>
                                                                                <dbl>
## 1 Sun
                   156.
                                   154
                                                         136
                                                                                  173
## 2 Mon
                   161.
                                   159
                                                         138
                                                                                  179
## 3 Tue
                   161.
                                   158
                                                         139
                                                                                  179
## 4 Wed
                   160.
                                   157
                                                         138.
                                                                                  179
## 5 Thu
                   161.
                                   158
                                                         139
                                                                                  179
## 6 Fri
                   162.
                                   159
                                                         141
                                                                                  179
## 7 Sat
                   159.
                                   156
                                                         137
                                                                                  178
```

Mortality tends to be a bit higher on weekdays than weekends, but it's not a dramatic difference.

We did the same check for temperature:

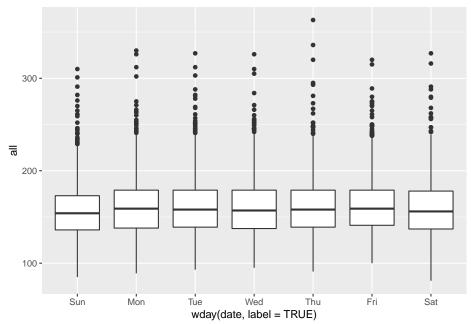
```
quantile(tmean, 0.25),
quantile(tmean, 0.75))
```

```
## # A tibble: 7 x 5
     dow
            `mean(tmean)` `median(tmean)` `quantile(tmean, 0.2~ `quantile(tmean, 0.~
## * <ord>
                    <dbl>
                                     <dbl>
                                                             <dbl>
                                                                                   <dbl>
## 1 Sun
                     11.6
                                      11.3
                                                              7.48
                                                                                    15.9
## 2 Mon
                     11.6
                                      11.4
                                                             7.33
                                                                                    15.8
## 3 Tue
                     11.5
                                      11.4
                                                              7.48
                                                                                    15.9
## 4 Wed
                     11.7
                                      11.7
                                                              7.64
                                                                                    16.0
## 5 Thu
                     11.6
                                      11.5
                                                             7.57
                                                                                    16.0
## 6 Fri
                     11.6
                                      11.6
                                                             7.41
                                                                                    15.8
## 7 Sat
                     11.6
                                      11.5
                                                             7.53
                                                                                    15.9
```

In this case, there does not seem to be much of a pattern by weekday.

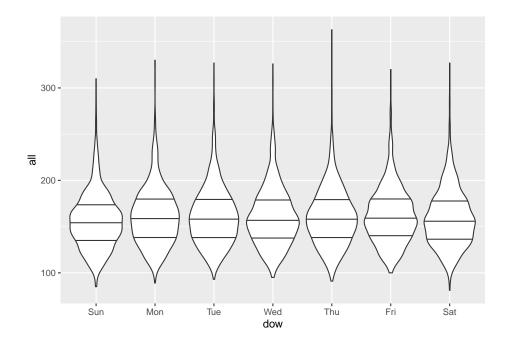
You can also visualize the association using boxplots:

```
ggplot(obs, aes(x = wday(date, label = TRUE), y = all)) +
geom_boxplot()
```



You can also try violin plots—these show the full distribution better than boxplots, which only show quantiles.

```
ggplot(obs, aes(x = dow, y = all)) + geom_violin(draw_quantiles = <math>c(0.25, 0.5, 0.75))
```



3.3 Fitting models

[Fitting models under time series and case-crossover study designs]

 $And reas\ section$

Brooke's section

3.4 Chapter vocabulary

Each class will start with a vocabulary quiz on a select number of the words from the chapter's vocabulary list. The vocabulary words for this chapter are:

- time-series study design
- case-crossover study design
- exposure
- health outcome
- confounder
- study period
- seasonal trends
- long-term trends

Generalized linear models

4.1 Splines in GLMs

[Using splines to model non-linear associations in a GLM]

4.2 Cross-basis functions in GLMs

[Using a cross-basis to model an exposure's association with the outcome in two dimensions (dimensions of time and exposure level)]

Natural experiments

5.1 Interrupted time series

[Interrupted time series assessing effects of policy/intervention in specific point in time] $\,$

5.2 Difference-in-differences

[Difference-in differences application for intervention introduced in one point in time] $\begin{tabular}{ll} \hline \end{tabular}$

Risk assessment

[Predict expected heat-related mortality under a climate change scenario]

Longitudinal cohort study designs

- 7.1 Coding a survival analysis
- 7.2 Handling complexity
- 7.2.1 Multi-level exposure
- 7.2.2 Recurrent outcome
- 7.2.3 Time-varying coeffificents
- $7.2.4 \quad Using \ survey \ results$

[e.g., NHANES]

Some approaches for confounding

- 8.1 Inverse probability weighting
- 8.2 Propensity scores

[Modeling for weights/propensity scores, involves machine learning]

Mixed models

[Using a mixed modeling framework to help analyze repeated measures]

Instrumental variables

Causal inference

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