HPSC - FINAL ASSIGNMENT

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Problem

Solve the Laplace equation using multigrid.

$$\frac{\partial^2 p}{\partial x^2} + \frac{\partial^2 p}{\partial y^2} = 0,$$

in a x = [0, 2], y = [0, 1] domains with boundary conditions:

$$p=0\ at\ x=0,$$

$$p = y \ at \ x = 2$$
,

$$\partial p/\partial y=0$$
 at $y=0,1.$

Modify the code in demo.py so that it runs with the sparse matrix from step1.py.

The source code and jupyter notebook for this assignment can be found at:

 $\verb|https://github.com/gear/HPSC/tree/master/hw| File name: assign2_worksheet.ipynb|$

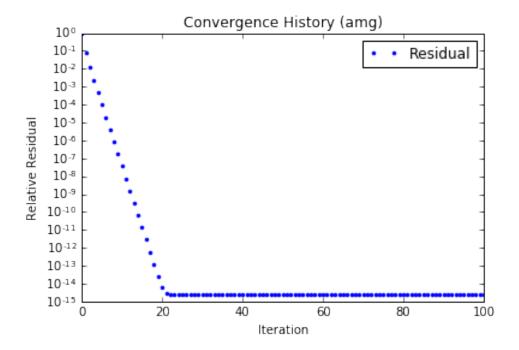
Answer

Using the given code in step1.py, I have the matrix A, vector b. This procedure is rewritten in $assign2_worksheet.ipynb$ as $laplace_eq$.

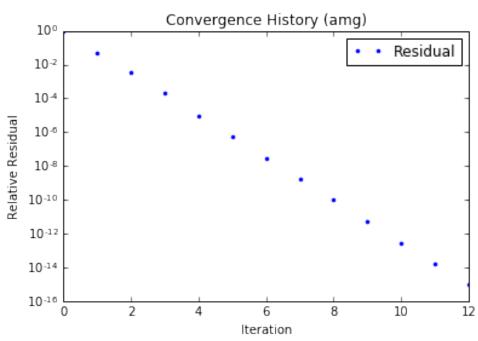
Listing 1: Solving Laplace equation using pyamg

```
1
       # Extracted from assign2\_worksheet.ipynb
2
       def amg_solver(A, b, cg=False, name='amg', tol=1e-10):
         mls = rootnode_solver(A)
3
         print mls
4
          # Solve Ax = b
5
6
         residuals = []
7
         if cg:
              x = mls.solve(b, tol=tol, accel='cg', residuals=
8
                 residuals)
9
          else :
10
              x = mls.solve(b, tol=tol, accel=None, residuals=
                 residuals)
          # Compute relative residuals
11
          residuals = numpy.array(residuals)/residuals[0]
12
13
          # Plot convergence history
          import pylab
14
15
         pylab.figure()
16
         pylab.title('Convergence History (%s)' % name)
         pylab.xlabel('Iteration')
17
18
         pylab.ylabel('Relative_Residual')
         pylab.semilogy(residuals, label='Residual', linestyle='
19
            None', marker='.')
20
         pylab.legend()
21
         pylab.show()
```

The result plots:



(a) Convergence of AMG without CG method.



(b) Convergence of AMG with CG method.

Figure 1: Convergence of AMG.