EE24BTECH11025 - GEEDI HARSHA

Question: A die is thrown. Describe the following event:

(a) F: a number not less than 3.

Solution:

A fair six-sided die has outcomes in the sample space:

$$S = \{1, 2, 3, 4, 5, 6\}. \tag{0.1}$$

The event F represents getting a number not less than 3, which means:

$$F = \{3, 4, 5, 6\}. \tag{0.2}$$

Since the die is fair, each face has an equal probability of occurring. The probability mass function (PMF) describes the probability of each outcome:

$$P(X = x) = \frac{1}{6}, \quad x \in \{1, 2, 3, 4, 5, 6\}. \tag{0.3}$$

The cumulative distribution function (CDF) gives the probability of rolling a number less than or equal to x:

$$P(X \le x) = \sum_{k=1}^{x} P(X = k) = \frac{x}{6}, \quad x \in \{1, 2, 3, 4, 5, 6\}.$$
 (0.4)

The probability of event F occurring is calculated as follows:

$$P(F) = \frac{\text{Number of favorable outcomes}}{\text{Total number of outcomes}}.$$
 (0.5)

$$=\frac{4}{6}=\frac{2}{3}.\tag{0.6}$$

Thus, the probability of rolling a number not less than 3 is $\frac{2}{3}$.

This means that in a large number of trials, about 66.67% of the rolls will yield a number between 3 and 6.

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