

1.4.9.d

EE24BTECH11025 - GEEDI HARSHA

Question: Given that $\mathbf{P}(3, 2, -4)$, $\mathbf{Q}(5, 4, -6)$ and $\mathbf{R}(9, 8, -10)$ are collinear. Find the ratio in which Q divides PR .

Variable	Description
k	ratio in which point divides a line segment
$\mathbf{P}(3, 2, -4)$	coordinates of point P
$\mathbf{Q}(5, 4, -6)$	coordinates of point Q
$\mathbf{R}(9, 8, -10)$	coordinates of point R
k	ratio in which Q divides \mathbf{PR}

TABLE 0: Input Parameters

Solution: As Q lies between P and R , P can be represented as

$$Q = \frac{kR + P}{k + 1} \quad (0.1)$$

where k is the ratio,

$$Q = \frac{k \begin{pmatrix} 9 \\ 8 \\ -10 \end{pmatrix} + \begin{pmatrix} 3 \\ 2 \\ -4 \end{pmatrix}}{k + 1} \quad (0.2)$$

$$Q = \frac{\begin{pmatrix} 9k + 3 \\ 8k + 2 \\ -10k - 4 \end{pmatrix}}{k + 1} \quad (0.3)$$

$$Q = \begin{pmatrix} 5 \\ 4 \\ -6 \end{pmatrix} \quad (0.4)$$

on equating both sides

$$k = \frac{1}{2} \quad (0.5)$$

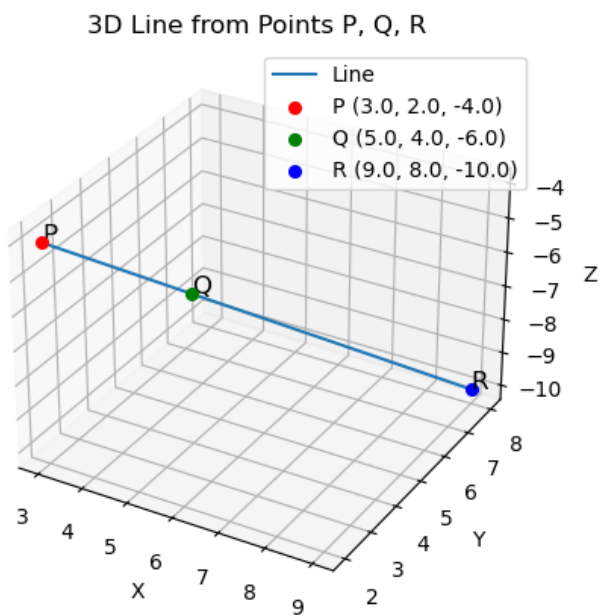


Fig. 0.1: The Plot of the given points