

# Combinatorial Inference against Label Noise

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## Background and Motivation

### Inevitable label noise in training data

Data collection from crowdsourcing or Internet search engine



Figure 1: Example images of 259-pomeranian class in WebVision [4]. In addition to clean samples, dataset contains closed- and open-set noises where closed-set noises belong to known classes (correct classes marked at corner) and open-set noises are not associated with any known classes.

### Existing mainstream approaches

Focus on noise-resistant training algorithms given level of noise

### Our contribution

- Reducing amount of label noise by constructing meta-classes
- Proposing a novel combinatorial classification framework
- Demonstrate noise-robustness of the proposed method

## Combinatorial Classification

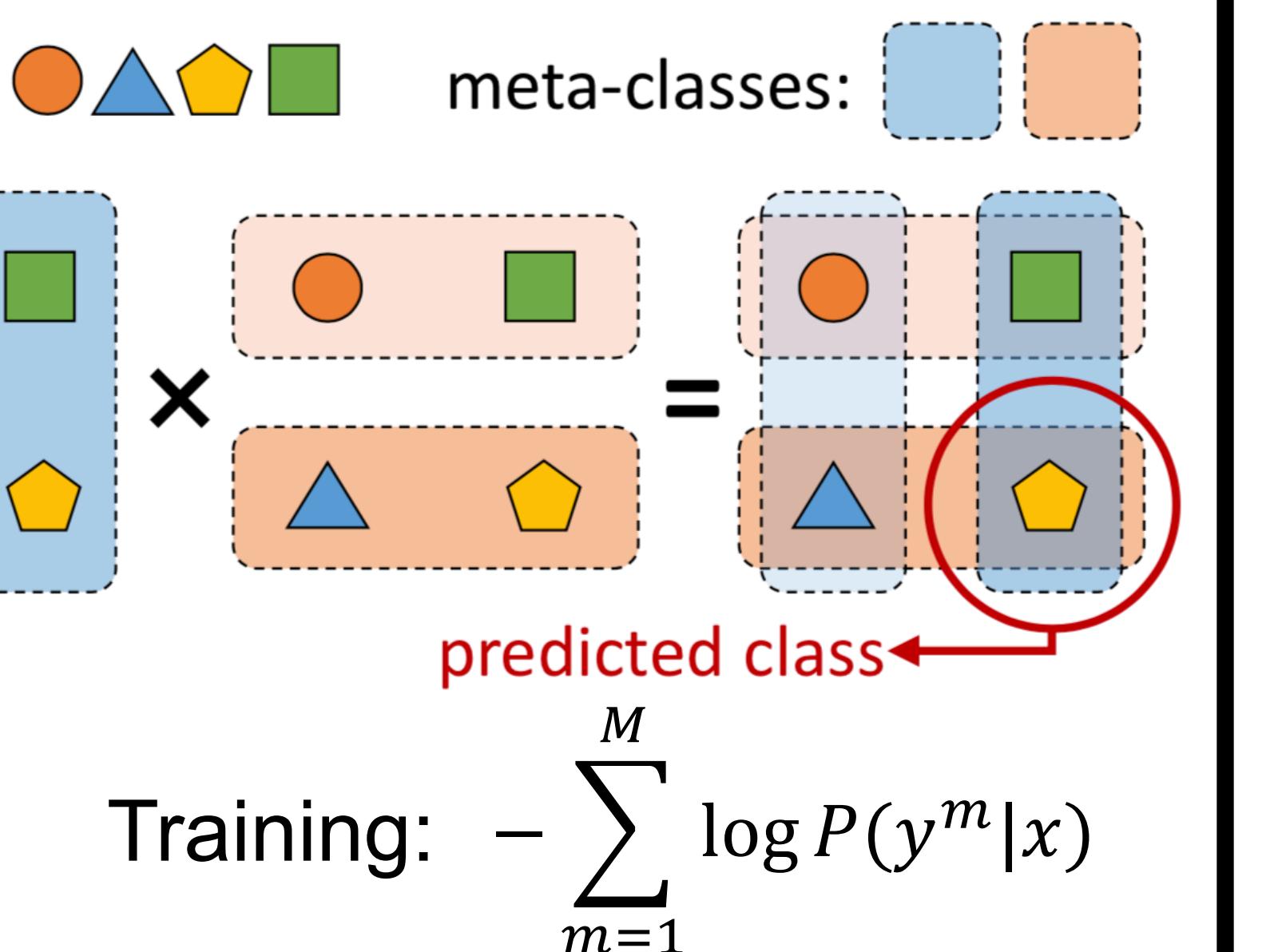
### Definitions

- $K$  original classes  
 $\mathcal{C} = \{c_1, \dots, c_K\}$

- $M$  meta-class sets  
 $\mathcal{C}^m = \{c_1^m, \dots, c_{K_m}^m\} (K \gg K_m)$

### Inference and training

$$\text{Inference: } \frac{\prod_{m=1}^M P(\text{meta}(c_k; m) | x)}{\sum_{j=1}^K \prod_{m=1}^M P(\text{meta}(c_j; m) | x)}$$



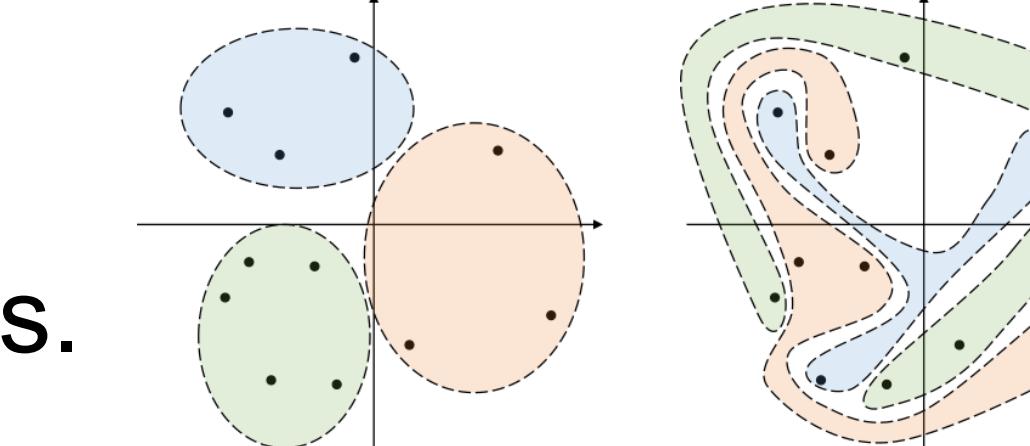
### Deep combinatorial classifier

Single shared feature extractor +  $M$  classification layers

## Meta-class Sets Configurations

### Clustering based meta-class sets configurations

- Use class features from weights from classification layer of pretrained network.
- Select  $Q$  sub-dimensions of class features.
- Perform  $k$ -means clustering.



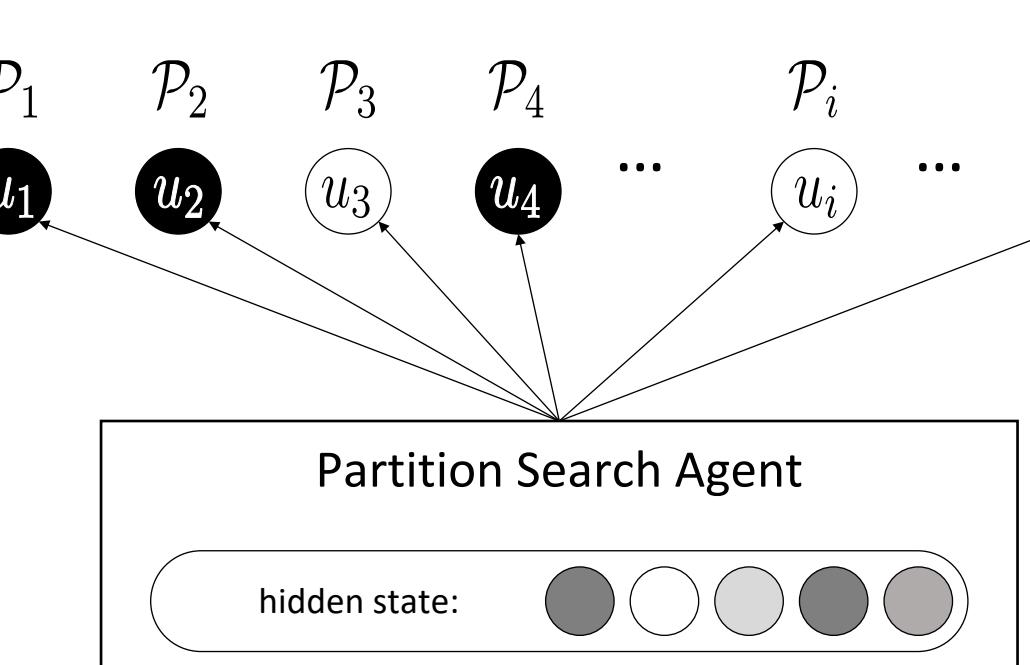
### Reinforced meta-class sets search

Train search agent that selects optimal set of meta-class sets using policy gradients:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{S} \sum_{s=1}^S \sum_{i=1}^N \nabla_{\theta} \log P(u_i^{(s)} | h; \theta) (\mathcal{R}^{(s)} - B)$$

$$\text{where reward } \mathcal{R} = \mathcal{R}_{\text{acc}} - \alpha \sum_{i=1}^N u_i$$

In-batch sample accuracy Number of selected meta-class sets



## Noise-robustness

### Label noise reduction

Meta-class representation directly reduces noise level:

$$\eta(\hat{D}) = \mathbb{E}_{\hat{D}}[\mathbf{1}(y \neq \hat{y})] = \frac{1}{N} \sum_i^N \mathbf{1}(y \neq \hat{y})$$

( $y$ : clean label,  $\hat{y}$ : corrupted label)

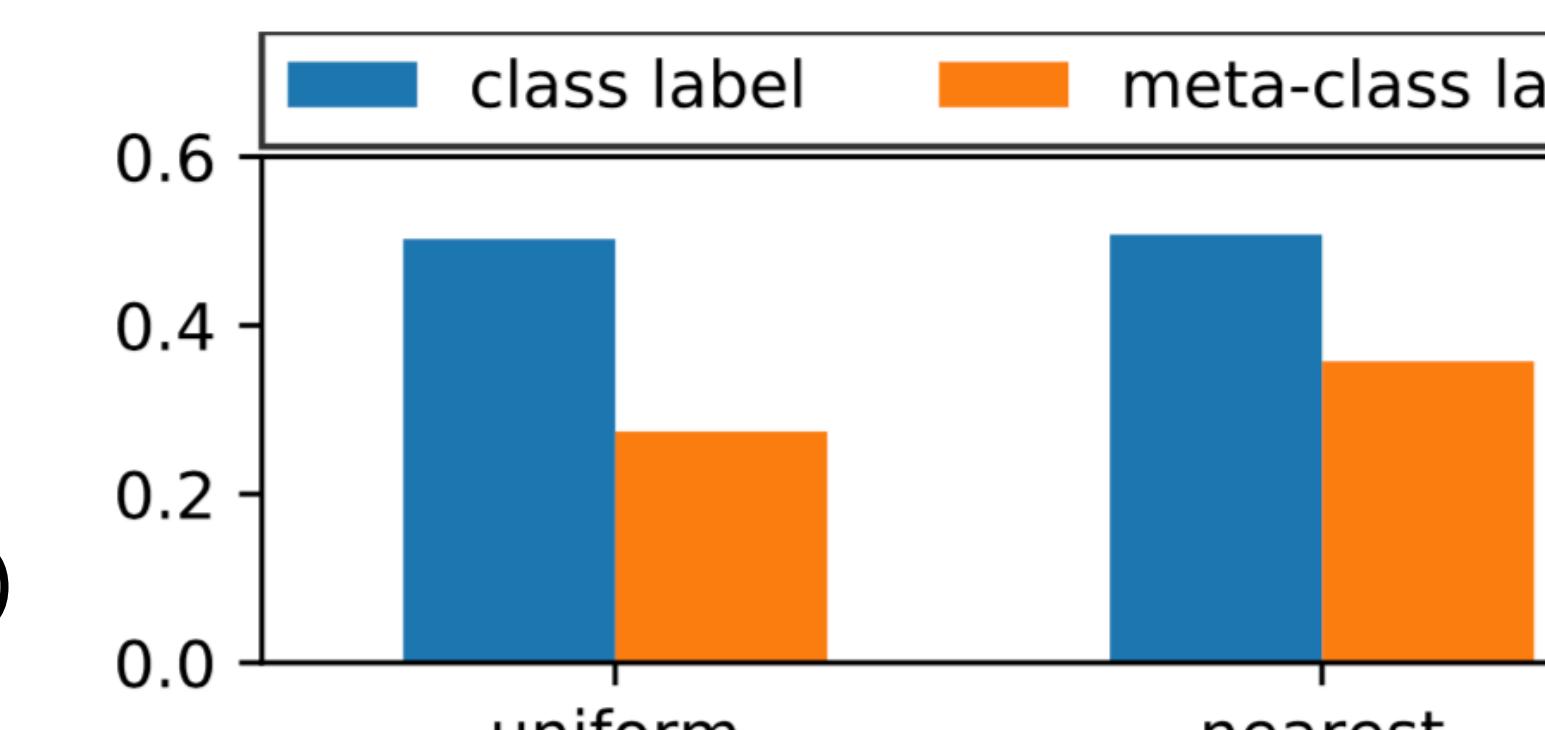


Figure 2:

### Experiments on toy example

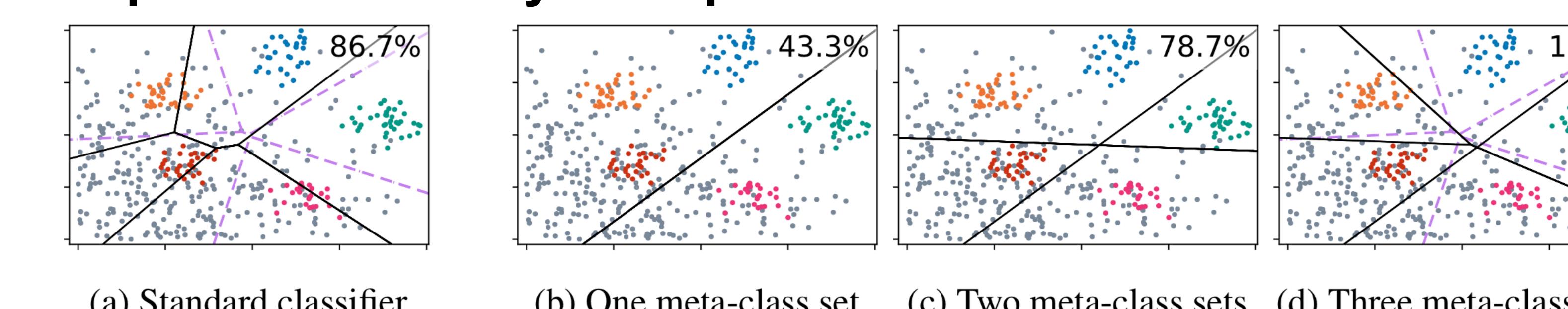


Figure 3: Visualizations of decision boundaries of (a) standard classifier and (b-d) combinatorial classifiers on two-dimensional Gaussian mixture model with five components. Accuracies are at the top-right corner for each classifier. For combinatorial classifiers, we gradually add classifiers one-by-one from (b) to (d). Gray dots show noisy samples with random labels while black solid and purple dashed lines represent decision boundaries drawn by clean and noisy datasets, respectively.

## Experimental Results

### Datasets

- CUB-200**: controlled experiments with synthetic noise
  - 1) Open- vs. closed-set noise
  - 2) Uniform vs. nearest noise
- WebVision**: large-scale experiments with real-world noise

### Results on CUB-200

Table 1: Accuracies [%] on CUB-200 with different levels and types of label noise.

Methods	Open-set noise				Closed-set noise					
	Clean dataset ( $\eta = 0$ )	Moderate noise level Uniform	Moderate noise level Nearest	Extreme noise level Uniform	Extreme noise level Nearest	Clean dataset ( $\eta = 0$ )	Moderate noise level Uniform	Moderate noise level Nearest	Extreme noise level Uniform	Extreme noise level Nearest
Standard	80.57 ± 0.37	73.37 ± 0.34	77.14 ± 0.27	70.04 ± 0.71	75.45 ± 0.50	79.58 ± 0.18	63.65 ± 0.26	65.21 ± 0.42	42.35 ± 0.50	47.70 ± 0.41
Decoupling [6]	79.32 ± 0.83	71.42 ± 0.70	76.07 ± 0.40	66.79 ± 0.44	74.80 ± 0.46	77.79 ± 0.23	62.52 ± 0.23	66.24 ± 0.53	43.91 ± 0.52	51.92 ± 0.18
F-correction [19]	80.66 ± 0.60	73.55 ± 0.70	77.03 ± 0.29	69.76 ± 0.59	75.52 ± 0.32	80.01 ± 0.42	63.81 ± 0.16	64.69 ± 0.21	42.23 ± 0.54	48.00 ± 0.46
S-model [18]	80.75 ± 0.37	73.52 ± 0.47	77.13 ± 0.97	70.06 ± 0.65	75.59 ± 0.33	79.42 ± 0.27	63.08 ± 0.74	64.90 ± 0.29	42.17 ± 0.70	48.01 ± 0.47
MentorNet [7]	80.39 ± 0.36	73.53 ± 0.56	77.27 ± 0.49	70.34 ± 0.42	75.75 ± 0.62	79.78 ± 0.20	68.03 ± 0.32	65.49 ± 0.14	47.74 ± 1.64	48.25 ± 0.39
$q$ -loss ( $q = 0.3$ ) [10]	81.55 ± 0.52	75.04 ± 0.46	78.09 ± 0.40	71.84 ± 0.95	76.32 ± 0.65	80.41 ± 0.36	68.52 ± 0.51	66.34 ± 0.25	53.18 ± 0.49	49.30 ± 0.35
$q$ -loss ( $q = 0.5$ ) [10]	82.19 ± 0.58	77.51 ± 0.53	78.58 ± 0.40	75.40 ± 0.66	76.47 ± 0.34	80.76 ± 0.38	67.49 ± 0.56	68.20 ± 0.31	50.24 ± 0.32	49.28 ± 0.57
$q$ -loss ( $q = 0.8$ ) [10]	75.15 ± 1.98	71.02 ± 1.68	47.40 ± 1.16	67.16 ± 1.29	32.60 ± 2.38	40.70 ± 2.25	29.31 ± 1.14	24.98 ± 1.61	17.67 ± 1.06	15.95 ± 0.65
Co-teaching [11]	80.90 ± 0.13	75.37 ± 0.54	77.41 ± 0.36	74.02 ± 0.29	75.57 ± 0.22	79.74 ± 0.14	68.21 ± 0.35	66.24 ± 0.30	52.72 ± 0.56	49.81 ± 0.19
CombCls	<b>82.80 ± 0.36</b>	<b>79.38 ± 0.83</b>	<b>79.28 ± 0.52</b>	<b>79.19 ± 0.29</b>	<b>77.95 ± 0.53</b>	<b>81.36 ± 0.23</b>	<b>71.75 ± 0.24</b>	<b>68.35 ± 0.35</b>	<b>51.90 ± 0.35</b>	<b>52.00 ± 0.22</b>
CombCls+Co-teaching	82.86 ± 0.25	79.93 ± 0.44	80.22 ± 0.31	80.50 ± 0.61	78.26 ± 0.43	81.52 ± 0.47	75.30 ± 0.10	70.46 ± 0.31	62.77 ± 0.66	52.49 ± 0.79

### Ablation Studies

Dataset used for meta-class set generation	Open-set		Closed-set	
	Open-set	Closed-set	Open-set	Closed-set
Clean	77.82	45.40		
Moderately noisy	77.58	50.22		
Extremely noisy	79.19	51.90		

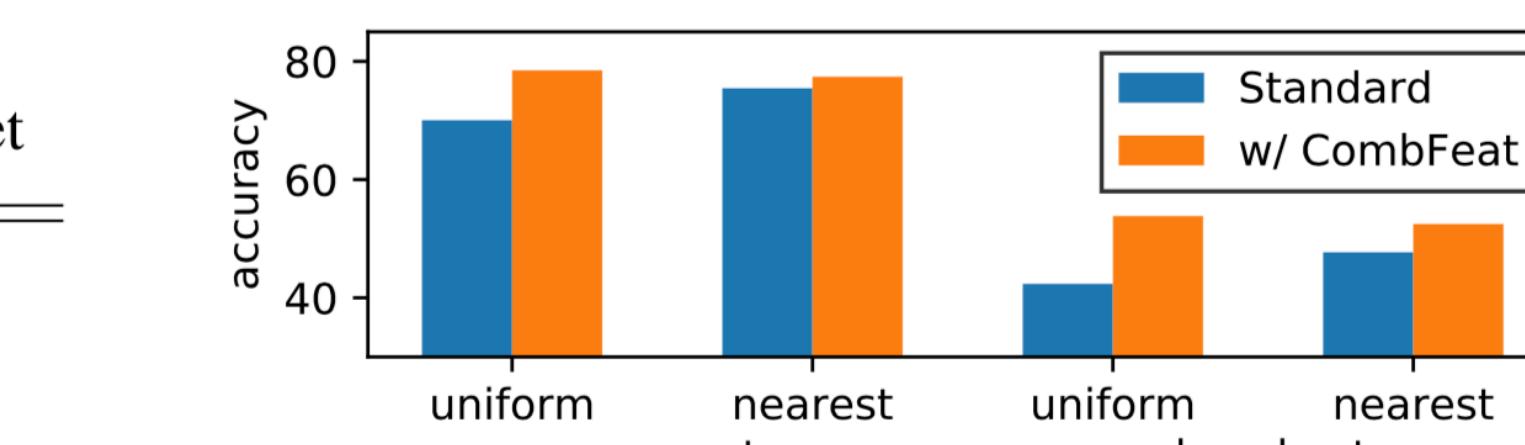
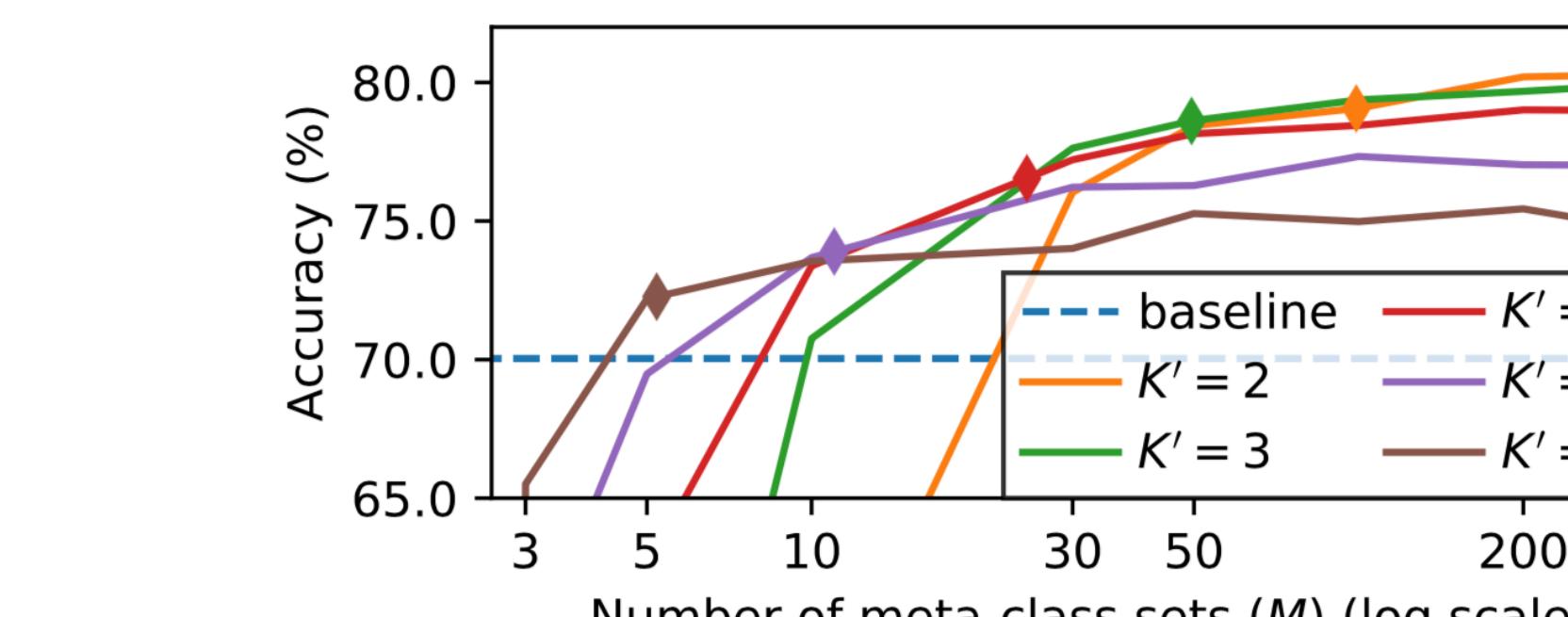


Figure 5: Results of ablation studies. Accuracies [%] of (left) combinatorial classifier trained on extremely noisy datasets with meta-class sets generated from datasets with different levels of uniform noise and (right) Standard with feature extractor of CombCls in various noise configurations.

Table 3: Results of combinatorial classification on extremely noisy datasets with different meta-class set configurations. Acc. means accuracy [%] and Param. represents ratio of model parameter count to that of Standard.

Methods	Meta-class set	Open-set noises		Closed-set noises	
		Acc.	Param.	Acc.	Param.
Standard	N/A	70.04	1.00	75.45	1.00
CombCls	Random	78.66	1.00	76.75	1.00
Clustering		79.19	1.00	77.95	1.00
Clustering+Search		<b>79.98</b>	0.42	<b>78.35</b>	0.44
				<b>54.52</b>	<b>0.41</b>
				<b>52.43</b>	<b>0.29</b>

### Model Analysis and Results on WebVision



Methods	Acc. [%]	
	Baseline	Others
Standard	79.82	79.82
Decoupling [6]	79.38	79.38
F-correction [19]	80.96	80.96
S-model [18]	81.36	81.36
MentorNet [7]	80.46	80.46
$q$ -loss ( $q = 0.3$ ) [10]	82.18	