

# Sorting Algorithms

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Song Name	Time	Track #▲	Artist	Album
✓ Letters from the Wasteland	4:29	1 of 10	The Wallflowers	Breach
✓ When You're On Top	3:54	1 of 13	The Wallflowers	Red Letter Days
✓ Hand Me Down	3:35	2 of 10	The Wallflowers	Breach
✓ How Good It Can Get	4:11	2 of 13	The Wallflowers	Red Letter Days
✓ Sleepwalker	3:31	3 of 10	The Wallflowers	Breach
✓ Closer To You	3:17	3 of 13	The Wallflowers	Red Letter Days
✓ I've Been Delivered	5:01	4 of 10	The Wallflowers	Breach
✓ Everybody Out Of The Water	3:42	4 of 13	The Wallflowers	Red Letter Days
✓ Witness	3:34	5 of 10	The Wallflowers	Breach
✓ Three Ways	4:19	5 of 13	The Wallflowers	Red Letter Days
✓ Some Flowers Bloom Dead	4:43	6 of 10	The Wallflowers	Breach
✓ Too Late to Quit	3:54	6 of 13	The Wallflowers	Red Letter Days
✓ Mourning Train	4:04	7 of 10	The Wallflowers	Breach
✓ If You Never Got Sick	3:44	7 of 13	The Wallflowers	Red Letter Days
✓ Up from Under	3:38	8 of 10	The Wallflowers	Breach
✓ Health and Happiness	4:03	8 of 13	The Wallflowers	Red Letter Days
✓ Murder 101	2:31	9 of 10	The Wallflowers	Breach
✓ See You When I Get There	3:09	9 of 13	The Wallflowers	Red Letter Days
✓ Birdcage	7:42	10 of 10	The Wallflowers	Breach
✓ Feels Like Summer Again	3:48	10 of 13	The Wallflowers	Red Letter Days
✓ Everything I Need	3:37	11 of 13	The Wallflowers	Red Letter Days
✓ Here in Pleasantville	3:40	12 of 13	The Wallflowers	Red Letter Days
✓ Empire in My Mind (Bonus Track)	3:31	13 of 13	The Wallflowers	Red Letter Days



# Bubble Sort

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# Bubble Sort

**Function : BUBBLE\_SORT (K,N)**

1. [Initialize]  
     $LAST \leftarrow N$  (entire list assumed unsorted at this point)
2. [Loop on pass index]  
    Repeat thru step 5 for  $PASS = 1, 2, \dots, N - 1$
3. [Initialize exchanges counter for this pass]  
     $EXCHS \leftarrow 0$
4. [Perform pairwise comparisons on unsorted elements]  
    Repeat for  $I = 1, 2, \dots, LAST - 1$   
    If  $K[I] > K[I + 1]$   
    then  $K[I] \longleftrightarrow K[I + 1]$   
         $EXCHS \leftarrow EXCHS + 1$
5. [Were any exchanges made on this pass ?]  
    If  $EXCHS = 0$   
    then Return (mission accomplished; return early)  
    else  $LAST \leftarrow LAST - 1$  (reduce size of unsorted list)
6. [Finished]  
    Return (maximum number of passes required)

# Bubble Sort

**Function : BUBBLESORT (A)**

**BUBBLESORT(*A*)**

```
1  for  $i = 1$  to  $A.length - 1$ 
2      for  $j = A.length$  downto  $i + 1$ 
3          if  $A[j] < A[j - 1]$ 
4              exchange  $A[j]$  with  $A[j - 1]$ 
```

# Bubble Sort

Function : BUBBLESORT (A)

<i>Unsorted</i>		<i>Pass Number (i)</i>					<i>Sorted</i>
<i>j</i>	<i>K<sub>j</sub></i>	1	2	3	4	5	6
1	42	23	23	11	11	11	11
2	23	42	11	23	23	23	23
3	74	11	42	42	42	36	36
4	11	65	58	58	36	42	<u>42</u>
5	65	58	65	36	58	<u>58</u>	58
6	58	74	36	65	<u>65</u>	65	65
7	94	36	74	<u>74</u>	74	74	74
8	36	94	<u>87</u>	87	87	87	87
9	99	<u>87</u>	94	94	94	94	94
10	87	99	99	99	99	99	99

**FIGURE** Trace of a bubble sort.

# Insertion Sort

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# Insertion Sort

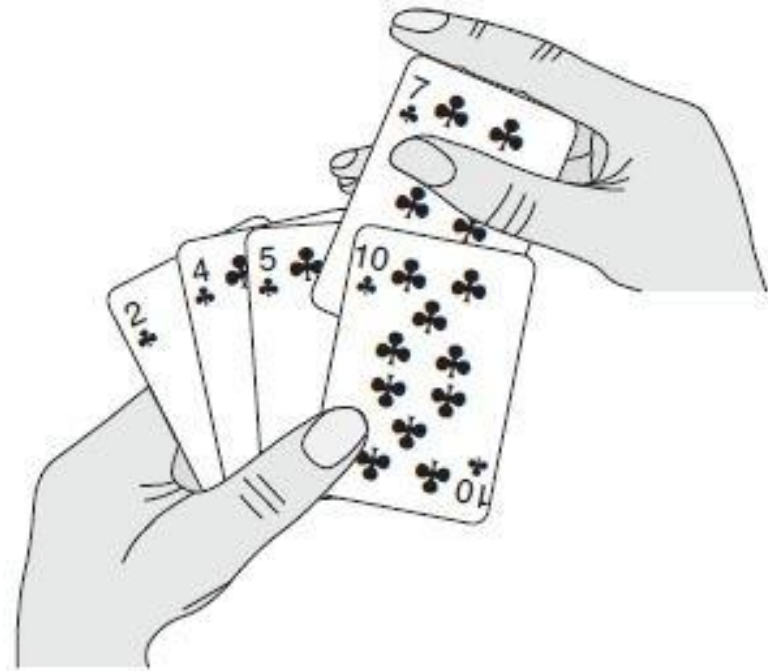


Figure Sorting a hand of cards using insertion sort.



# Insertion Sort

**Function : INSERTION-SORT (*A*)**

INSERTION-SORT(*A*)

```
1  for  $j = 2$  to  $A.length$ 
2       $key = A[j]$ 
3      // Insert  $A[j]$  into the sorted sequence  $A[1 .. j - 1]$ .
4       $i = j - 1$ 
5      while  $i > 0$  and  $A[i] > key$ 
6           $A[i + 1] = A[i]$ 
7           $i = i - 1$ 
8       $A[i + 1] = key$ 
```

# Selection Sort

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# Selection Sort

- Consider sorting  $n$  numbers stored in array  $A$  by first finding the smallest element of  $A$  and exchanging it with the element in  $A[1]$ . Then find the second smallest element of  $A$ , and exchange it with  $A[2]$ . Continue in this manner for the first  $n-1$  elements of  $A$ . Write pseudo-code for this algorithm, which is known as selection sort.

# Merge Sort

---

# Merge Sort

```
MergeSort(low,high)
{
    if(low<high)
    {
        mid=(low+high)/2
        MergeSort(low,mid)
        MergeSort(mid+1,high)
        Merge(low,mid,high)
    }
}
```

# Merge Sort

```
Merge(low,mid,high) {  
    h=low; i=low; j=mid+1;  
    while ( (h<=mid) and (j<=high) )  
    {  
        if(a[h]<=a[j])  
        {  
            b[i]=a[h]  
            h=h+1  
        }  
        else  
        {  
            b[i]=a[j]  
            j=j+1  
        }  
        i=i+1  
    } //End of while
```

```
    If(h>mid)  
    {  
        for k=j to high  
        {  
            b[i]=a[k]  
            i=i+1  
        }  
    }  
    else  
    {  
        for k=h to mid  
        {  
            b[i]=a[k]  
            i=i+1  
        }  
    }  
    for k=low to high  
        a[k]=b[k]  
} //End of Merge
```

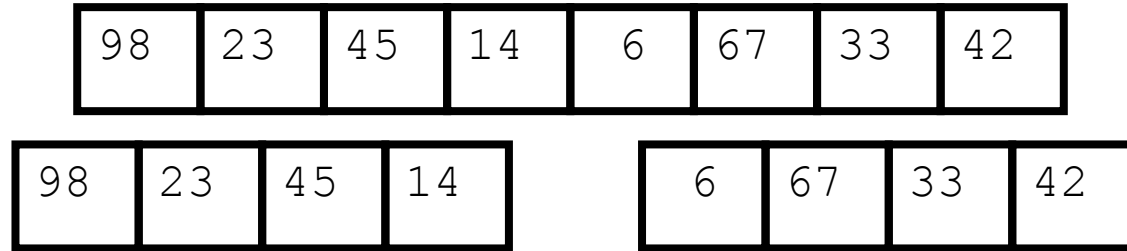
# Merge Sort (Example)

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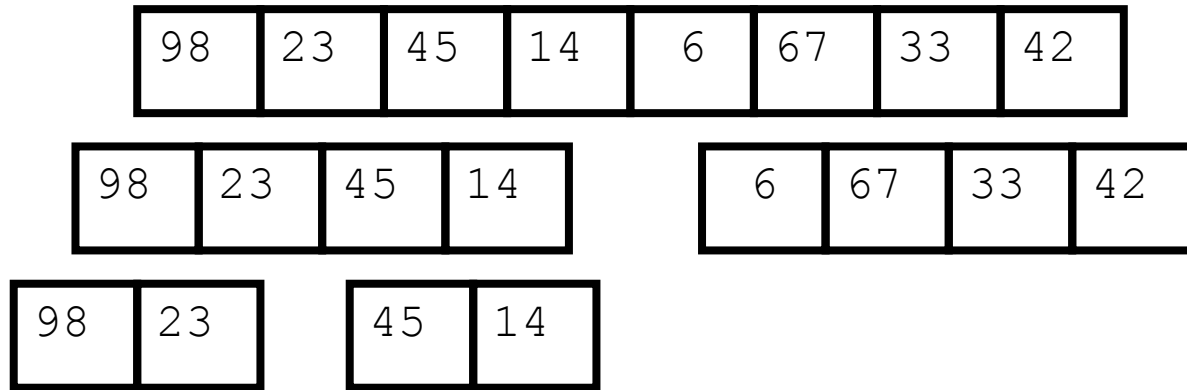
98	23	45	14	6	67	33	42
----	----	----	----	---	----	----	----



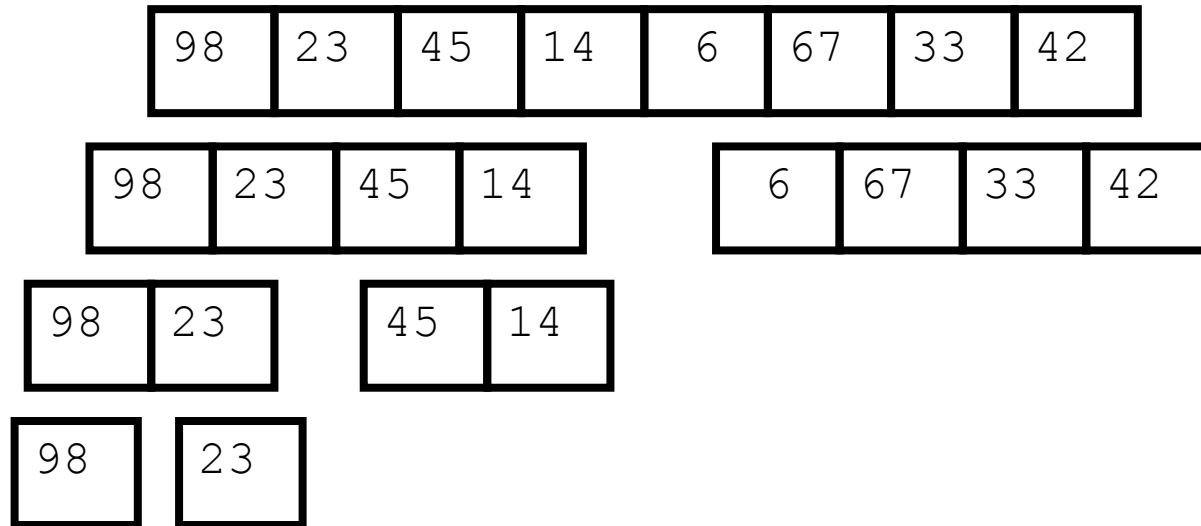
# Merge Sort (Example)



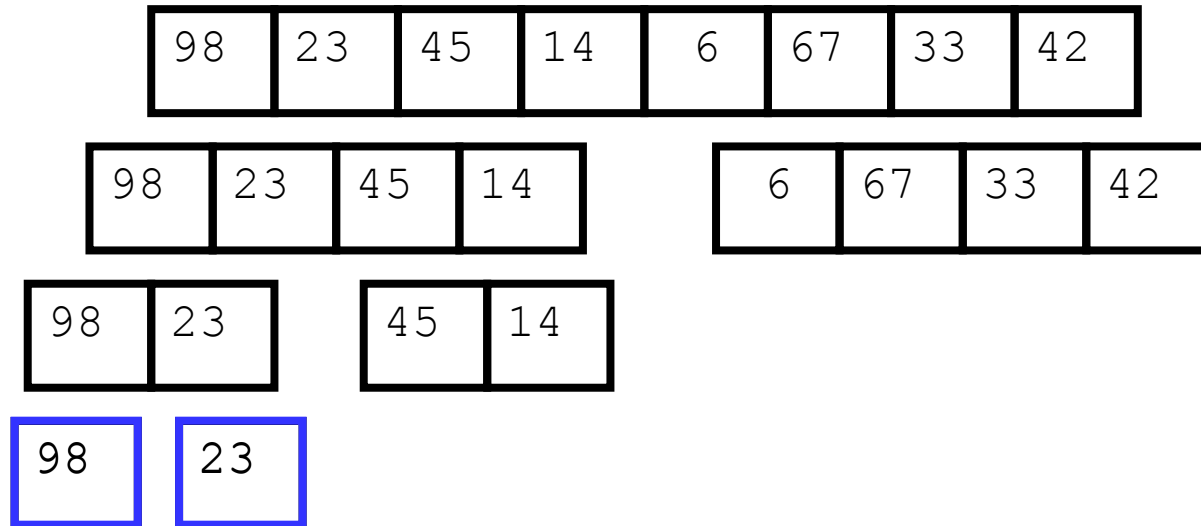
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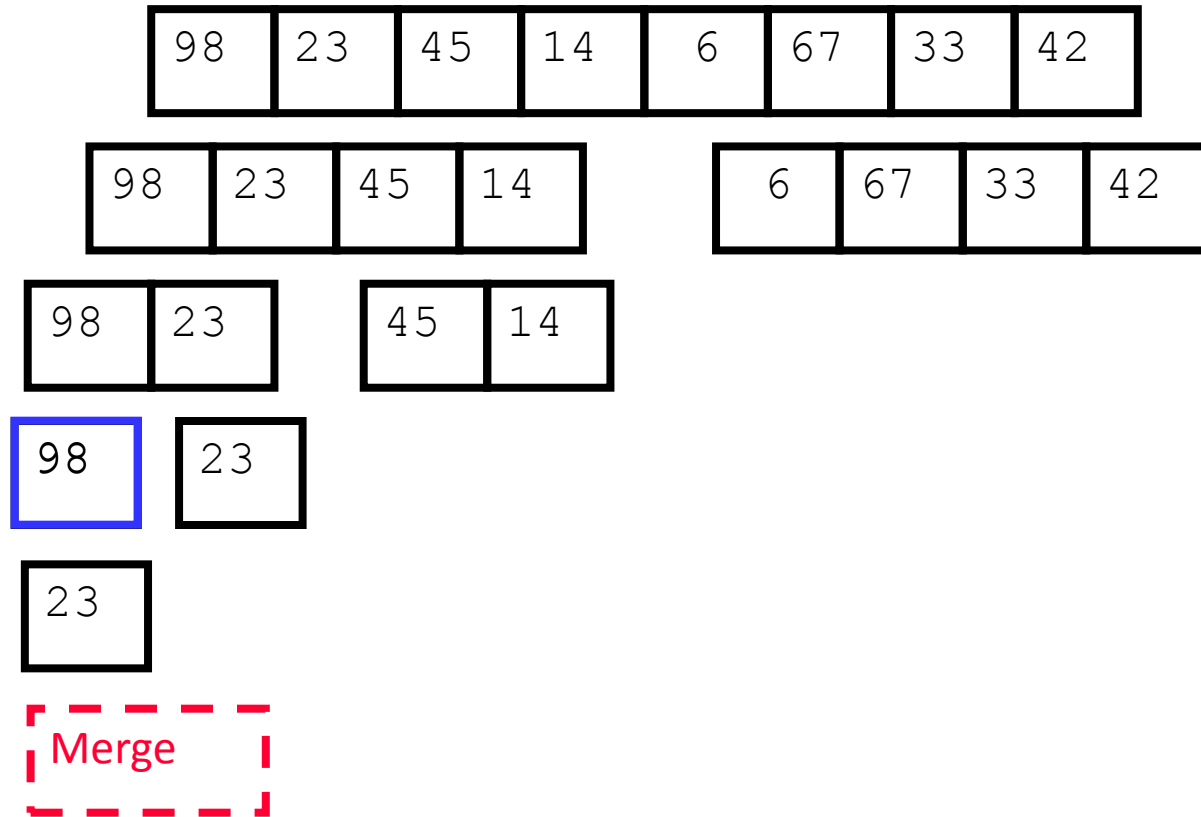


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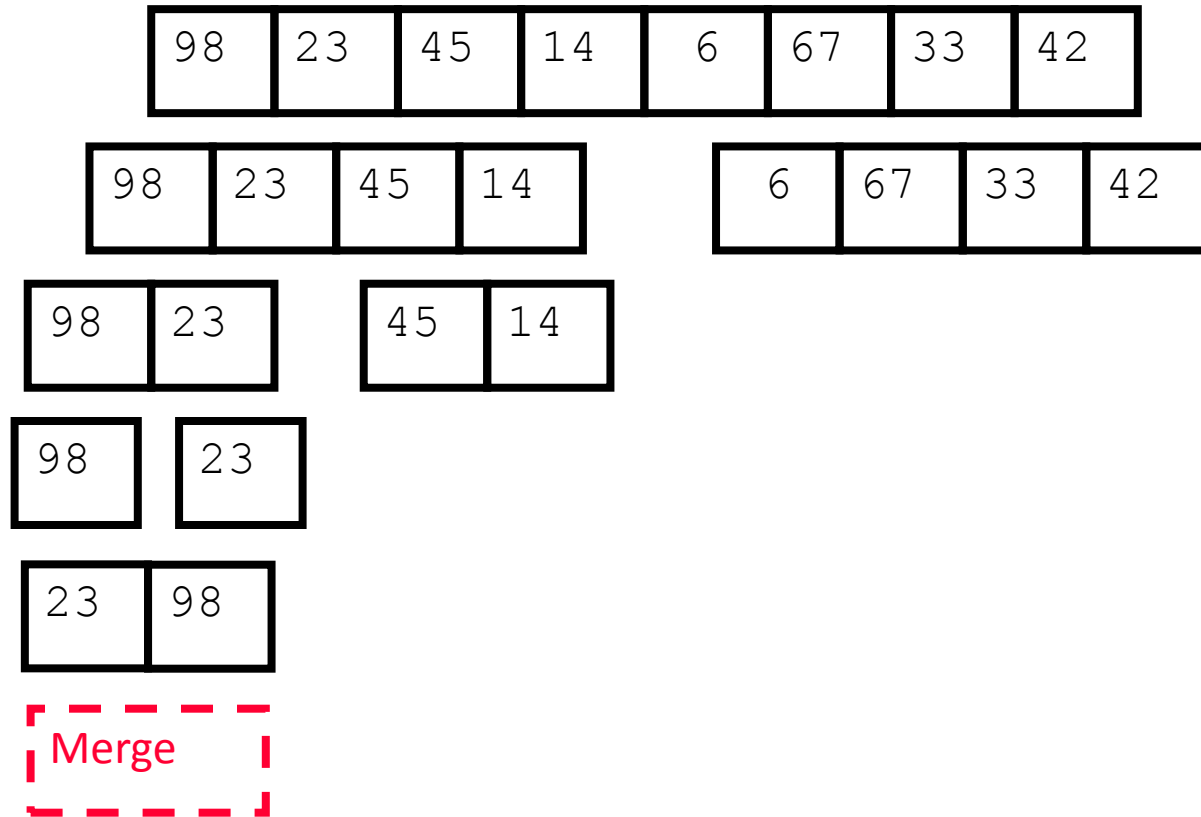


Merge

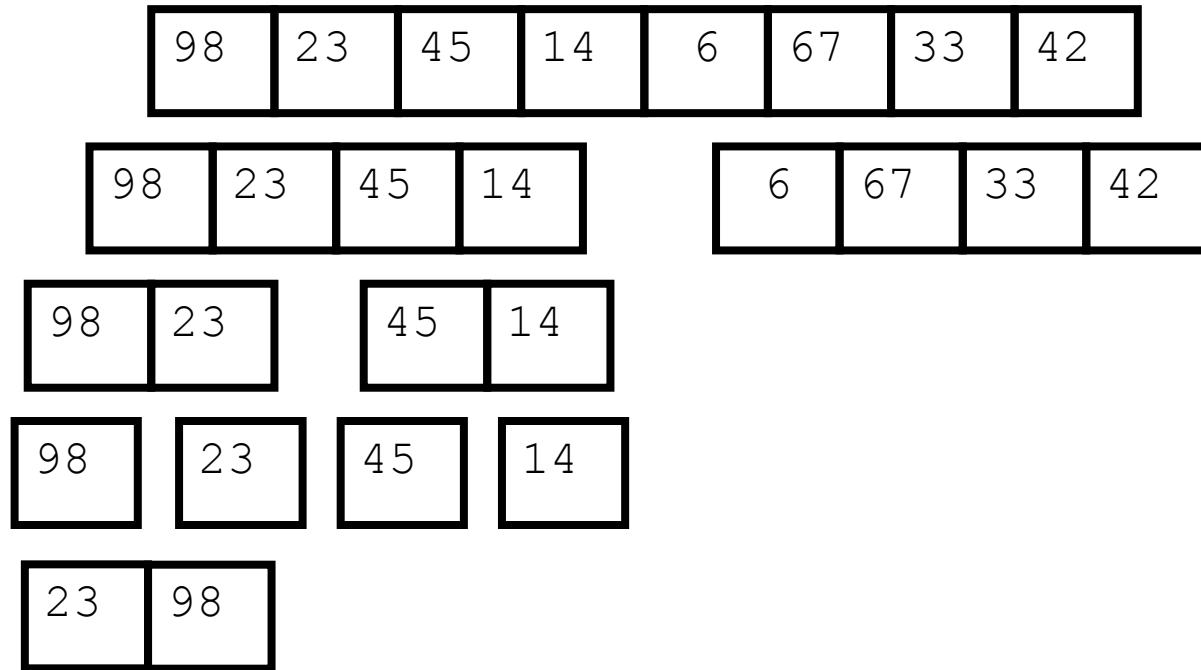
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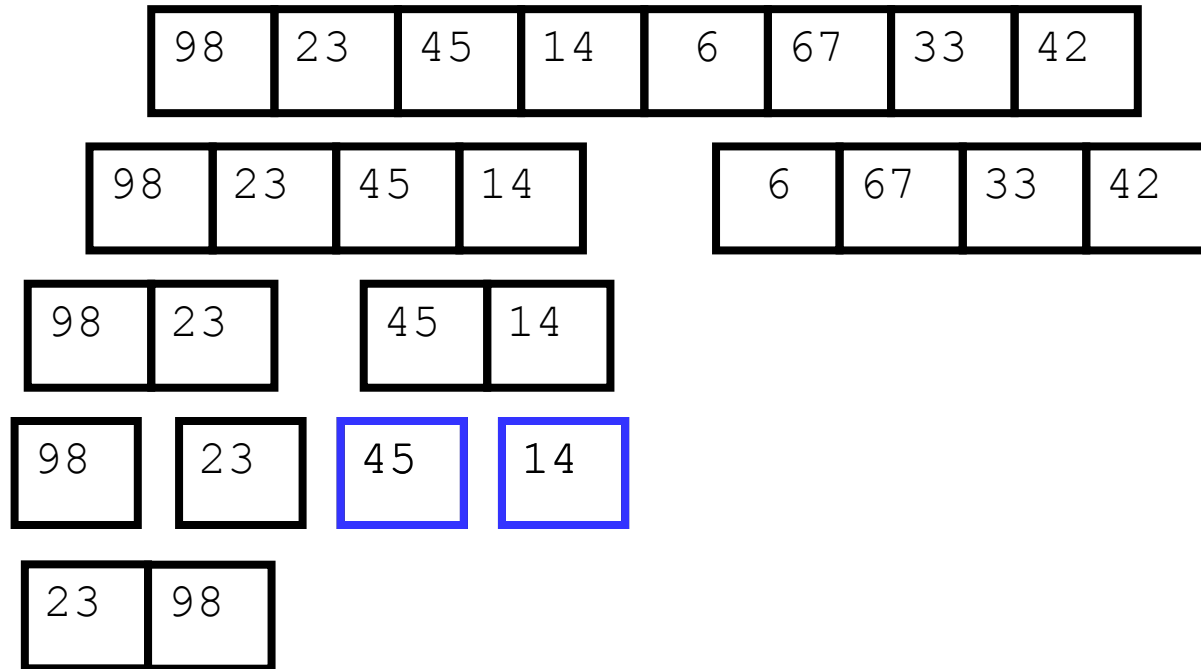


# Merge Sort (Example)



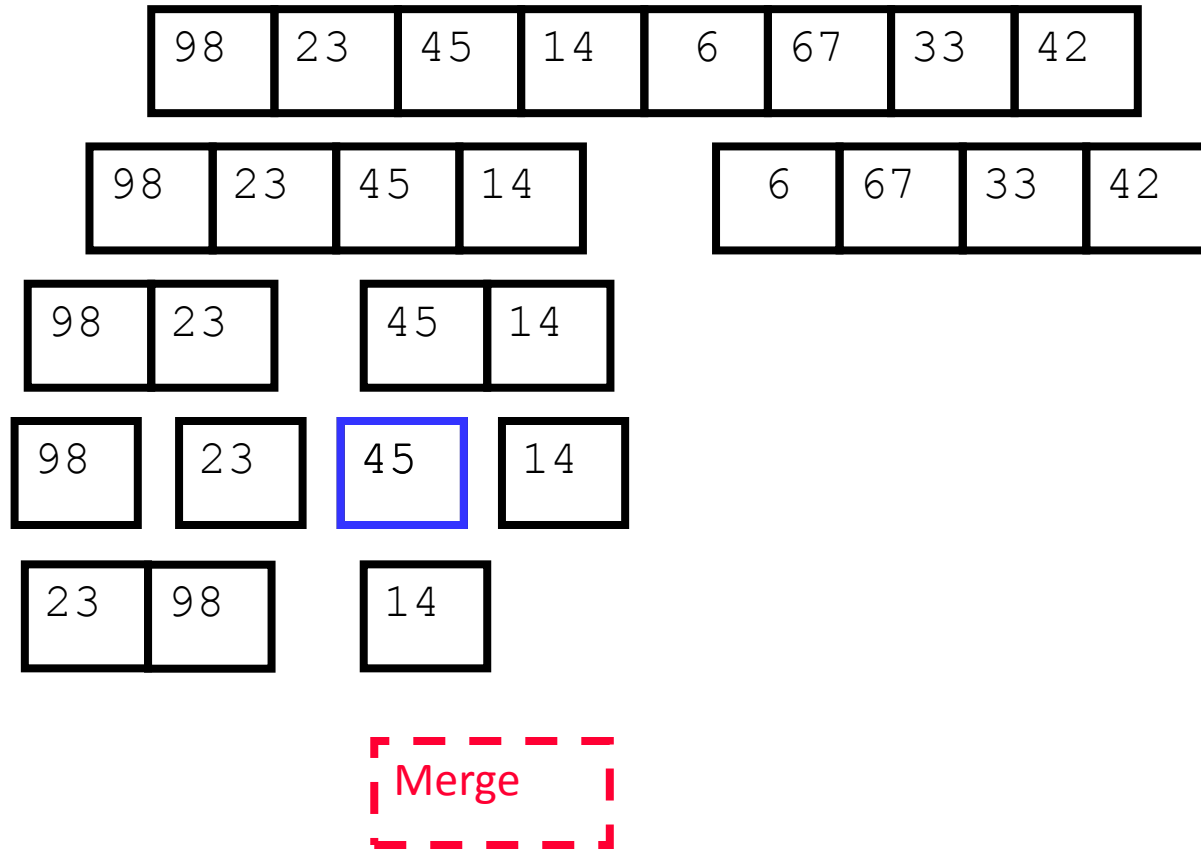


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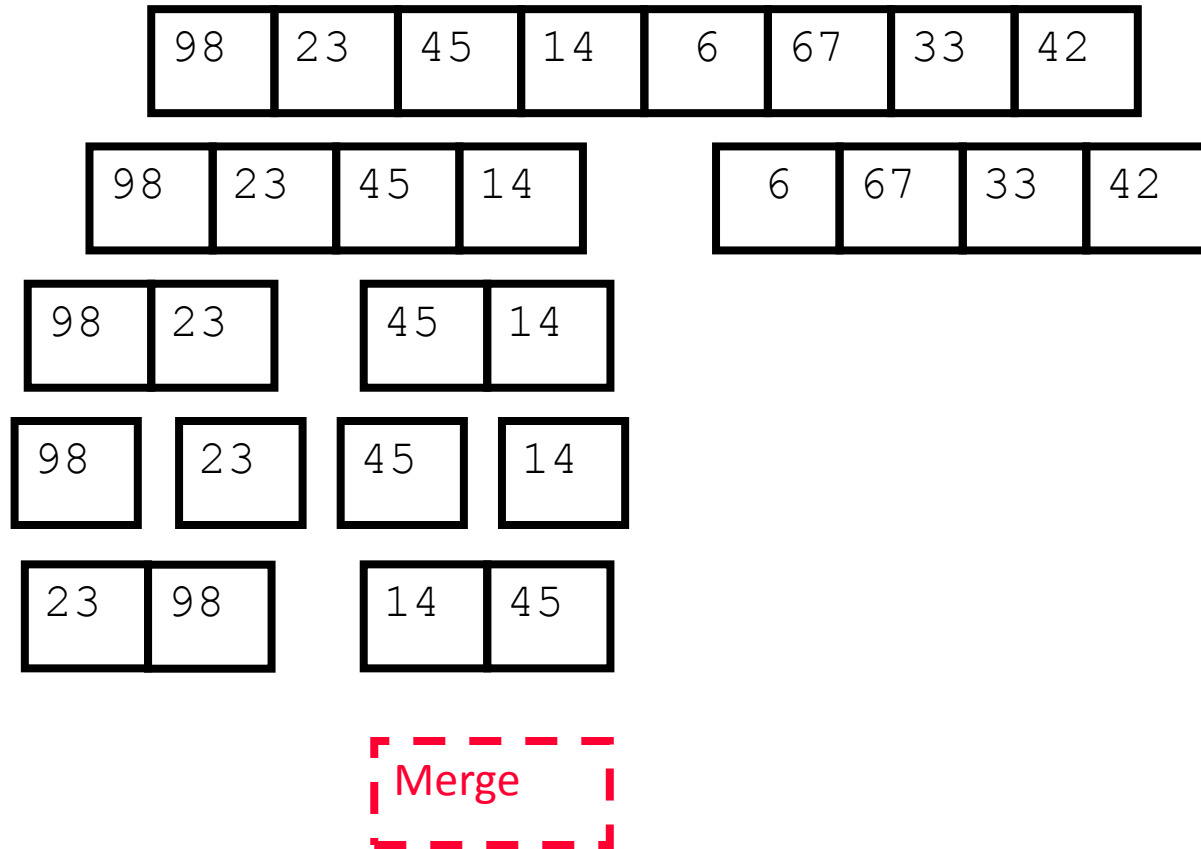


Merge

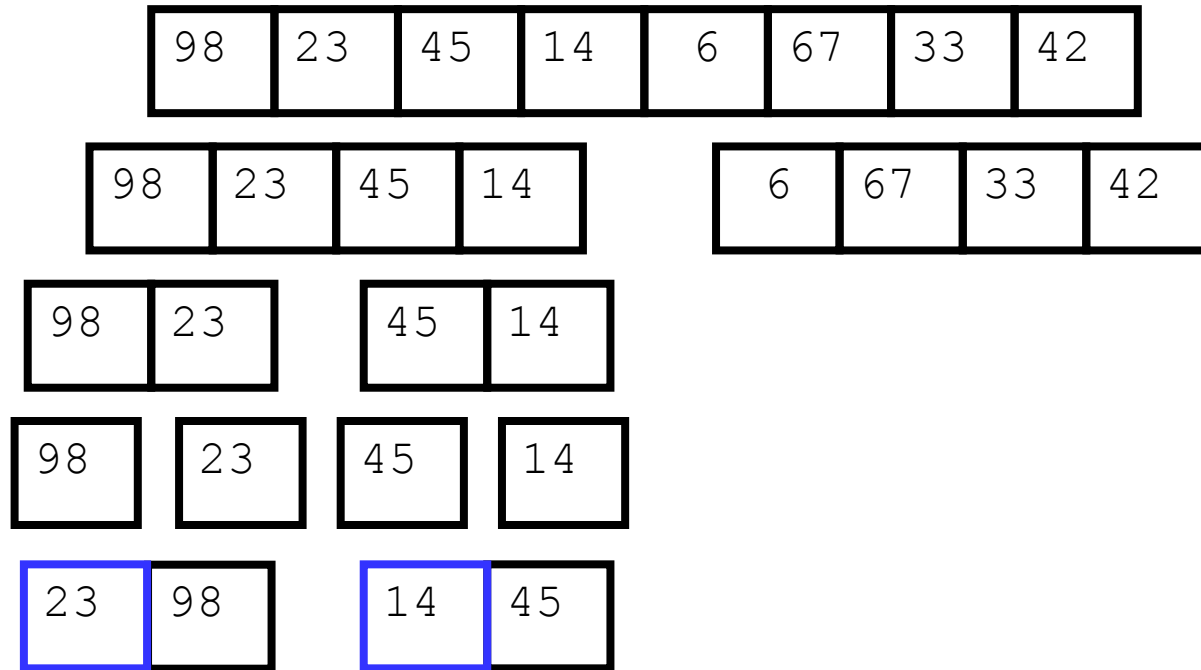
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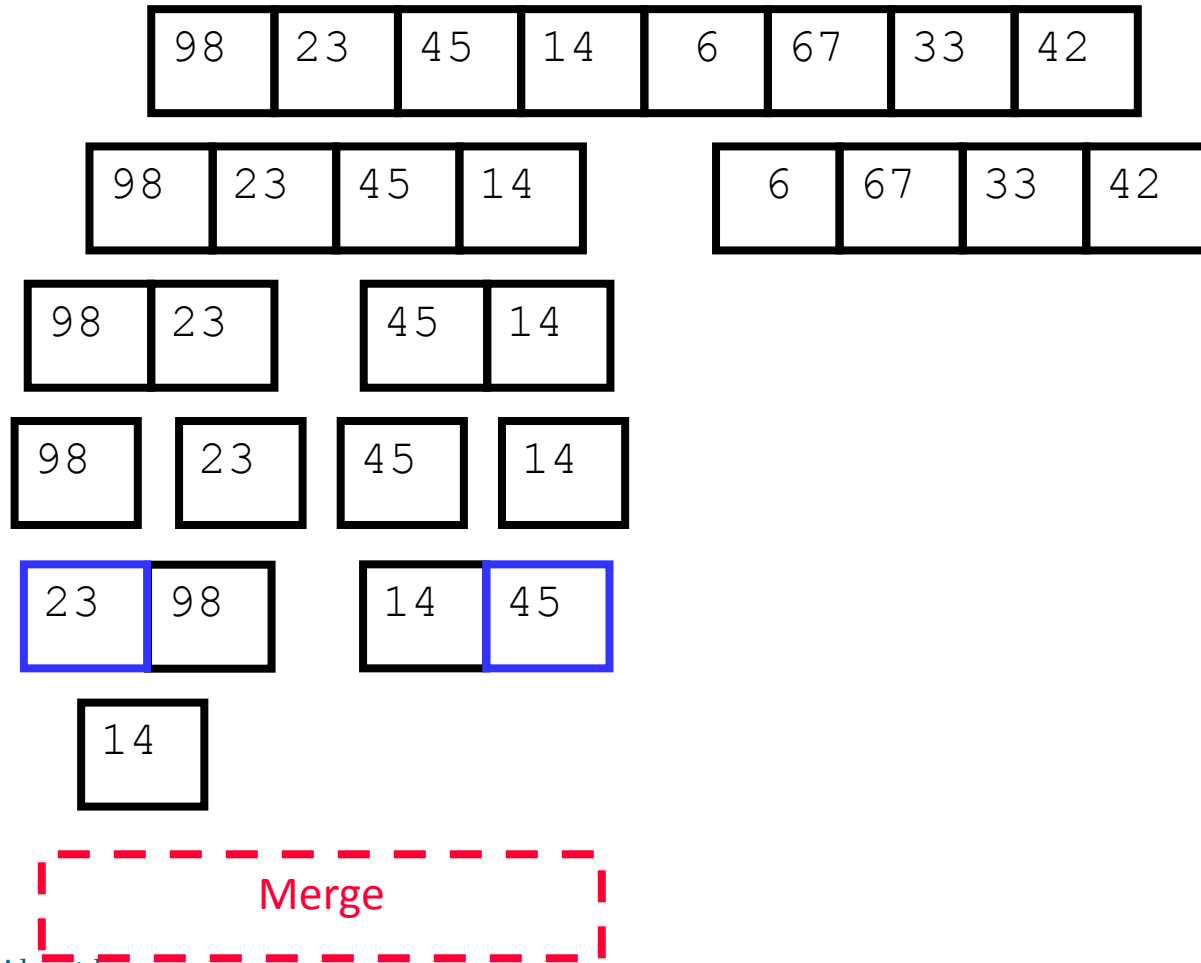
# Merge Sort (Example)



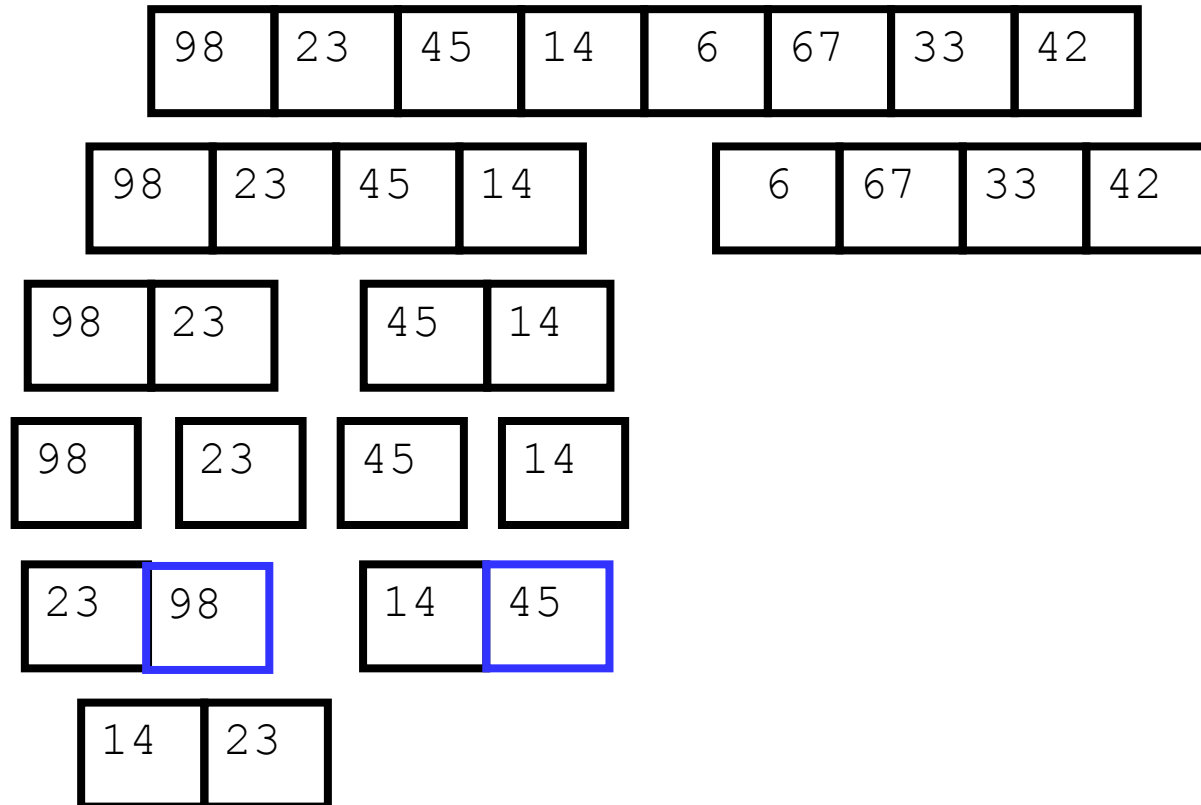
# Merge Sort (Example)



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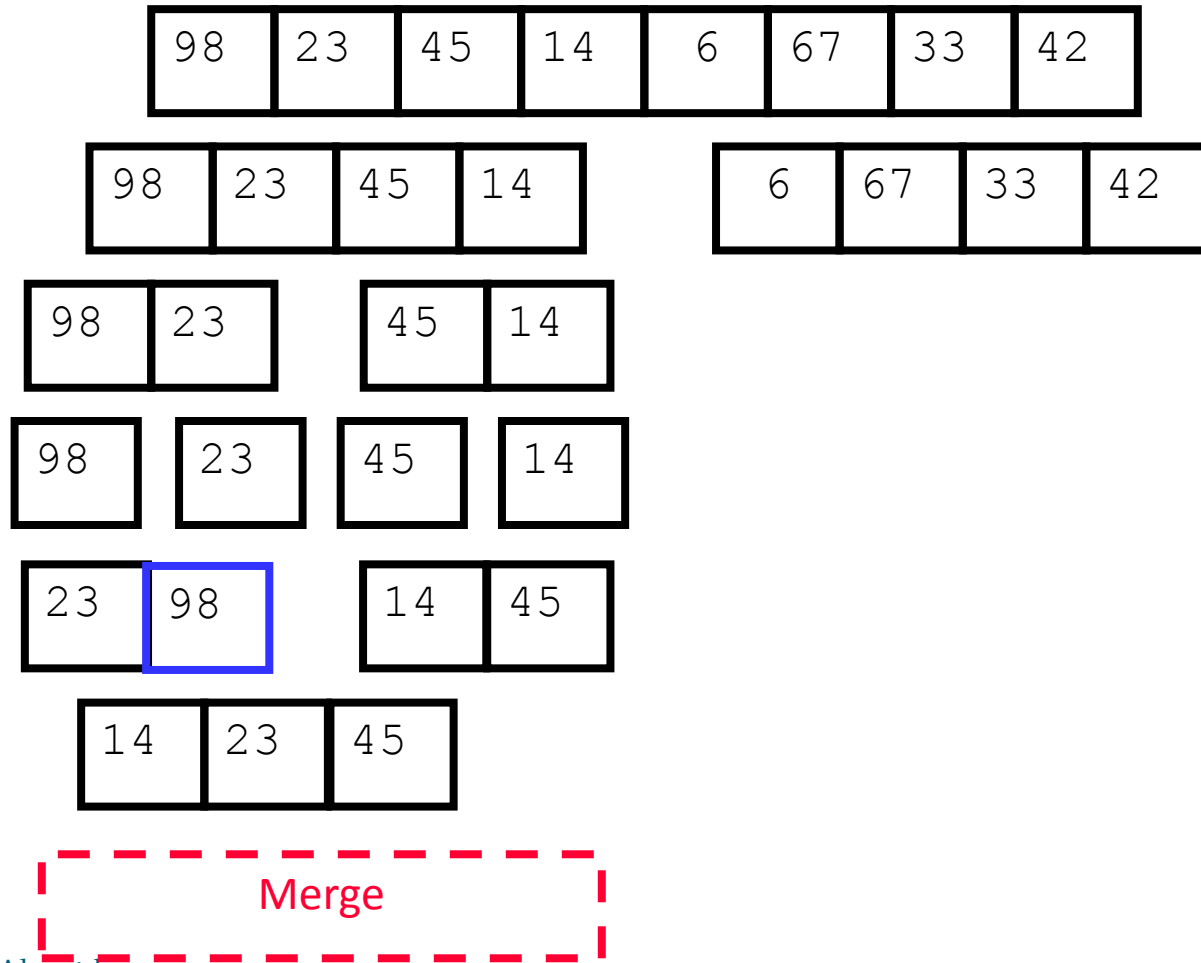


# Merge Sort (Example)



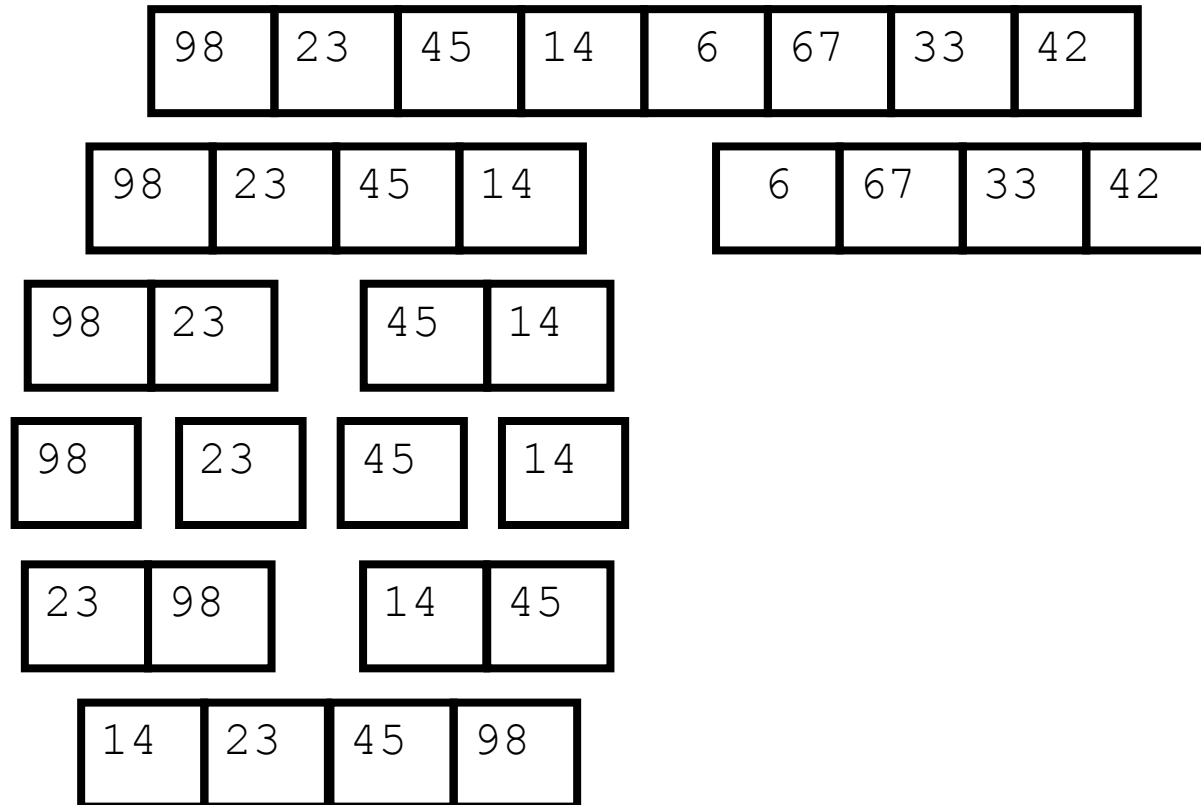
Merge

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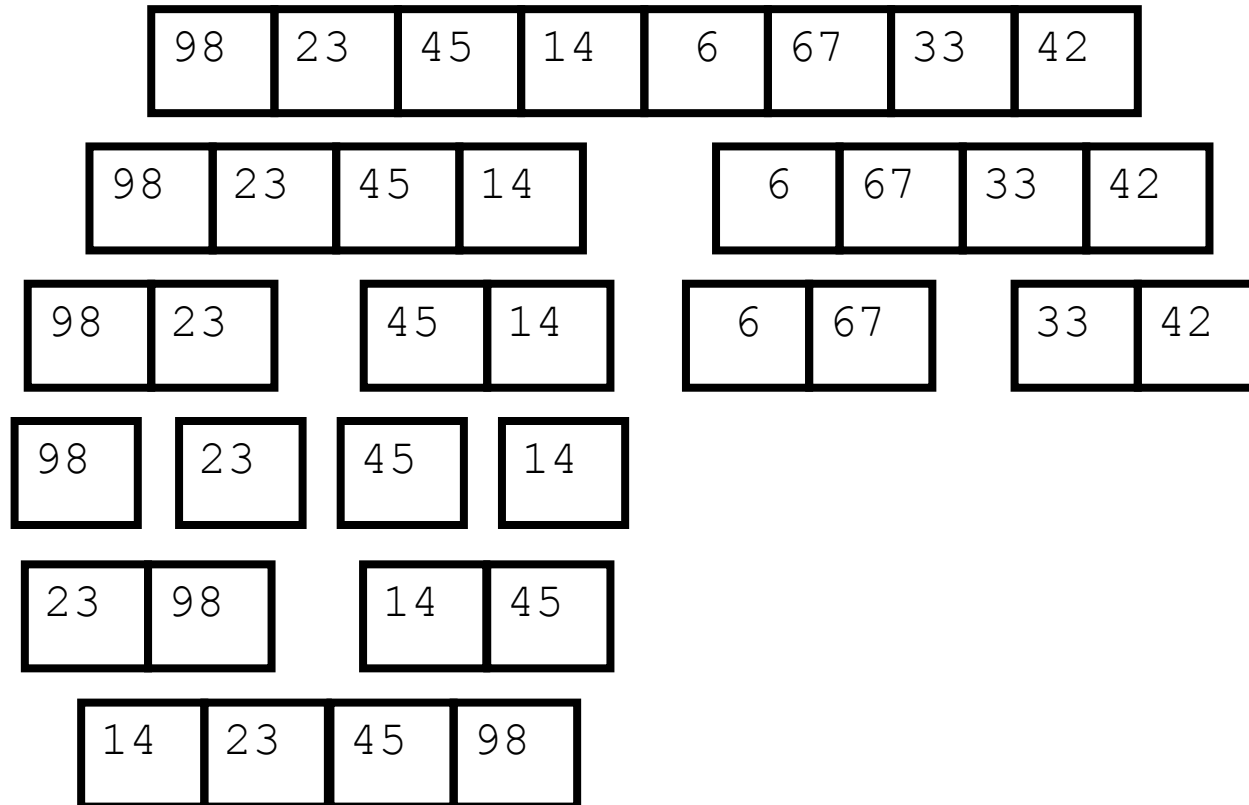


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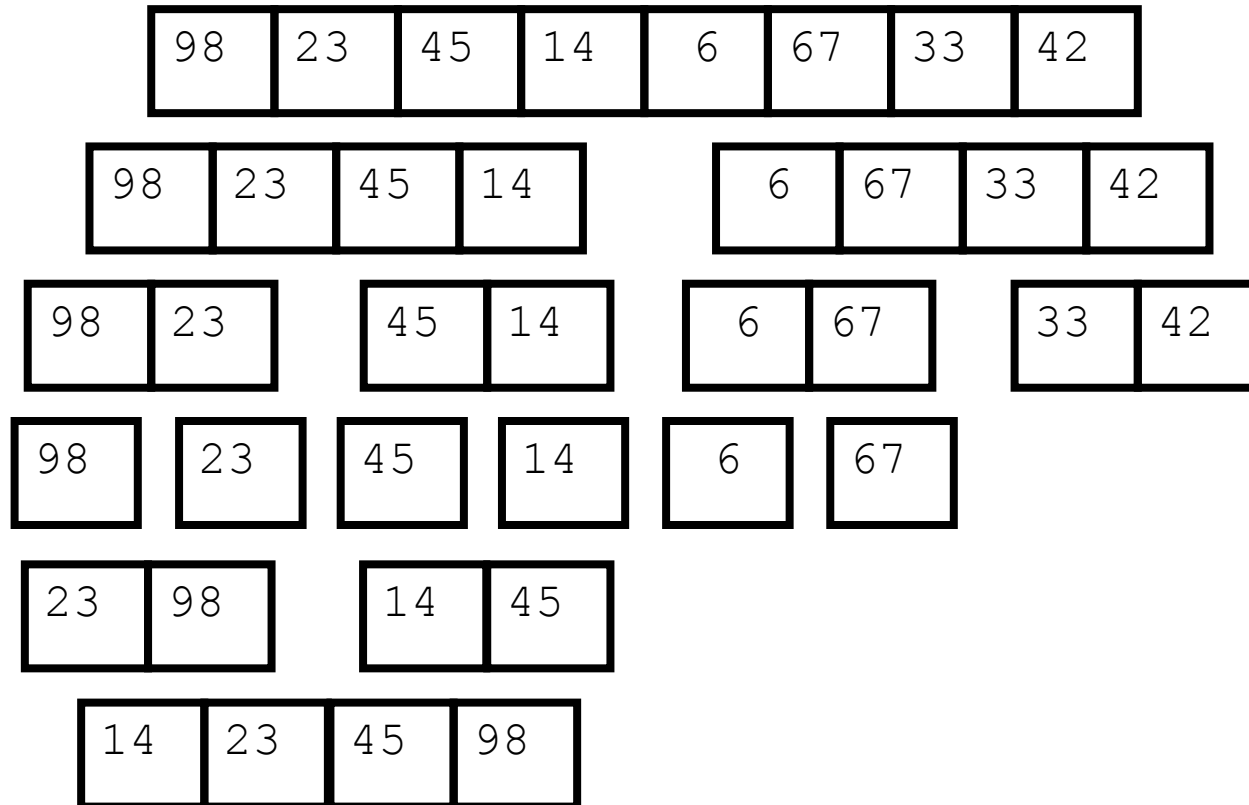


Merge

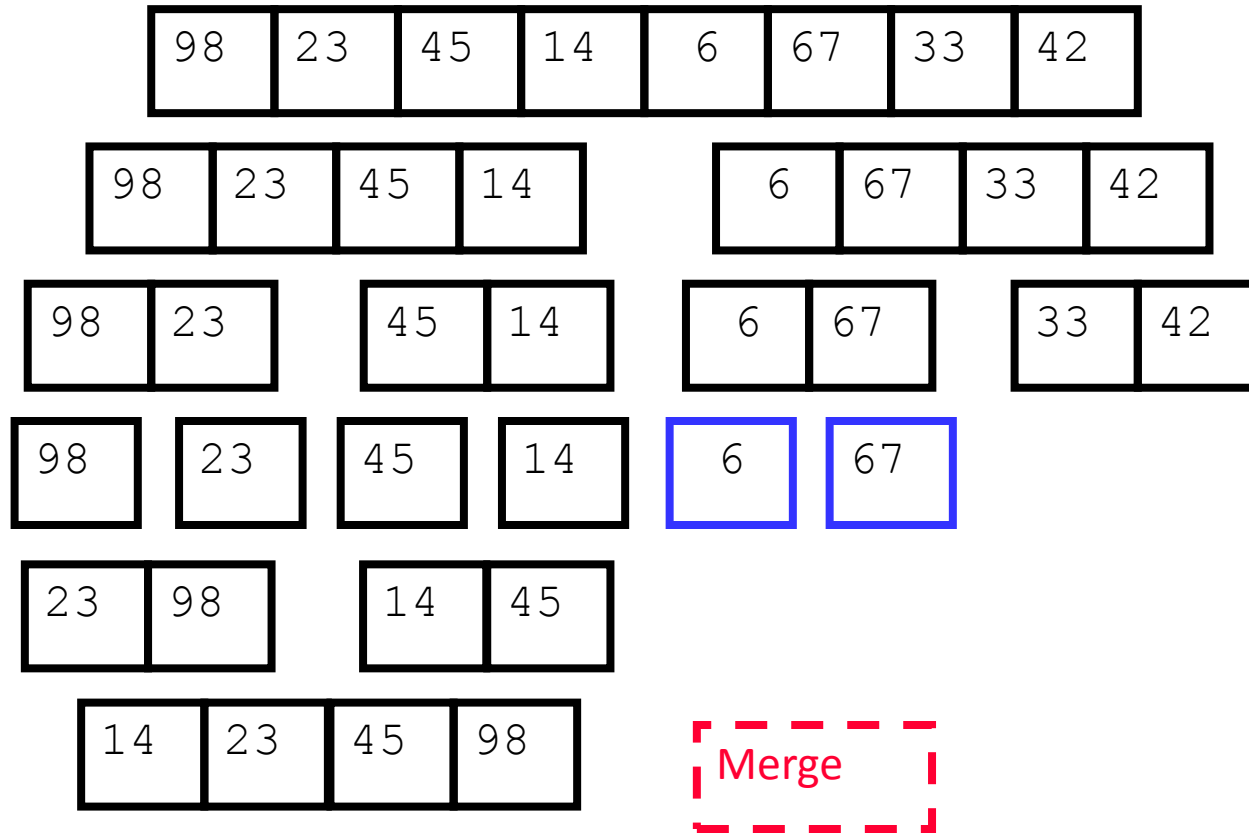
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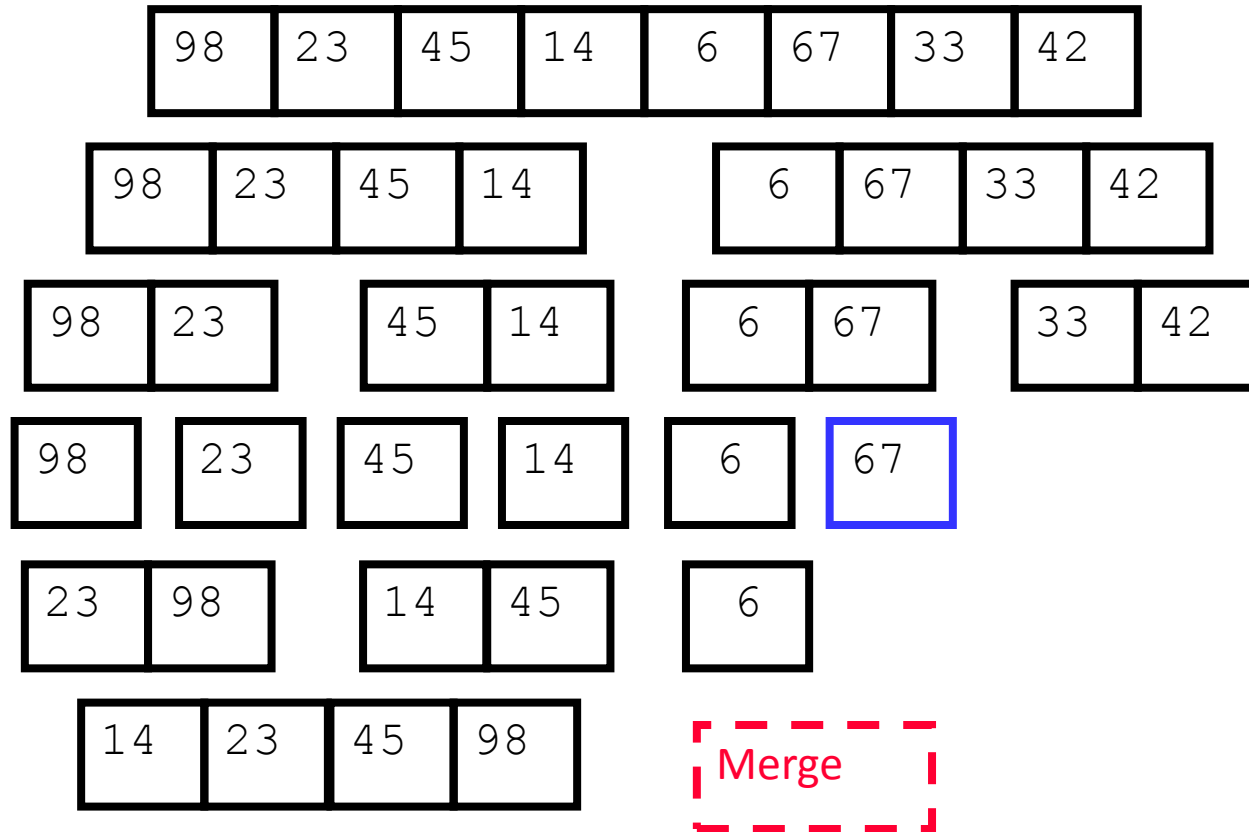
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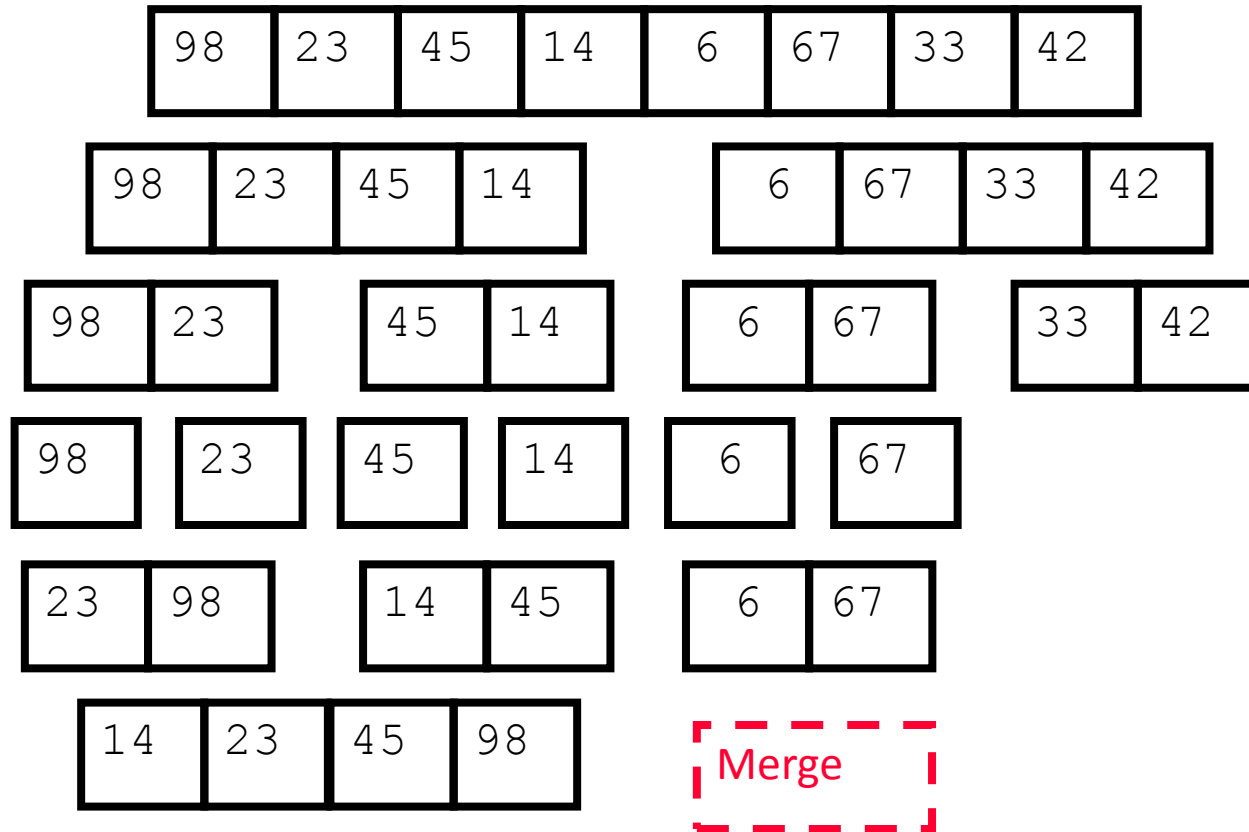
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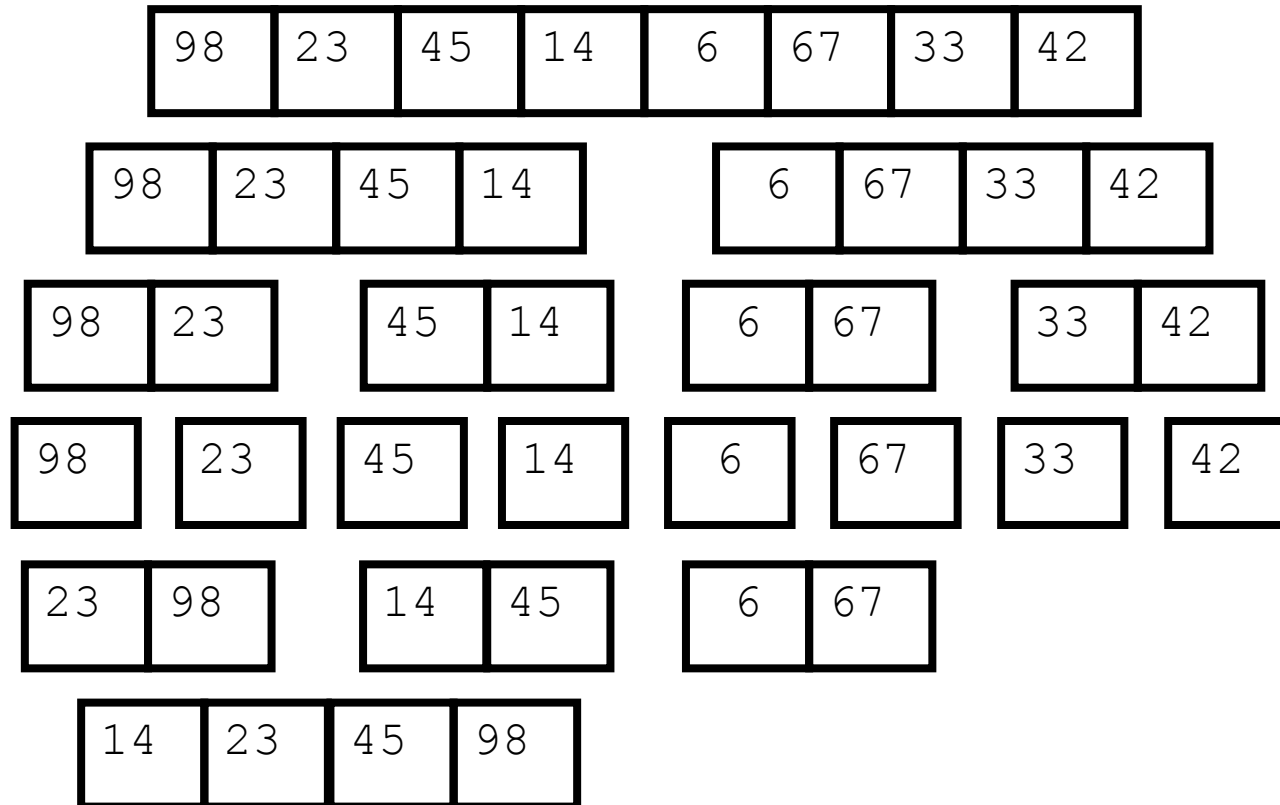
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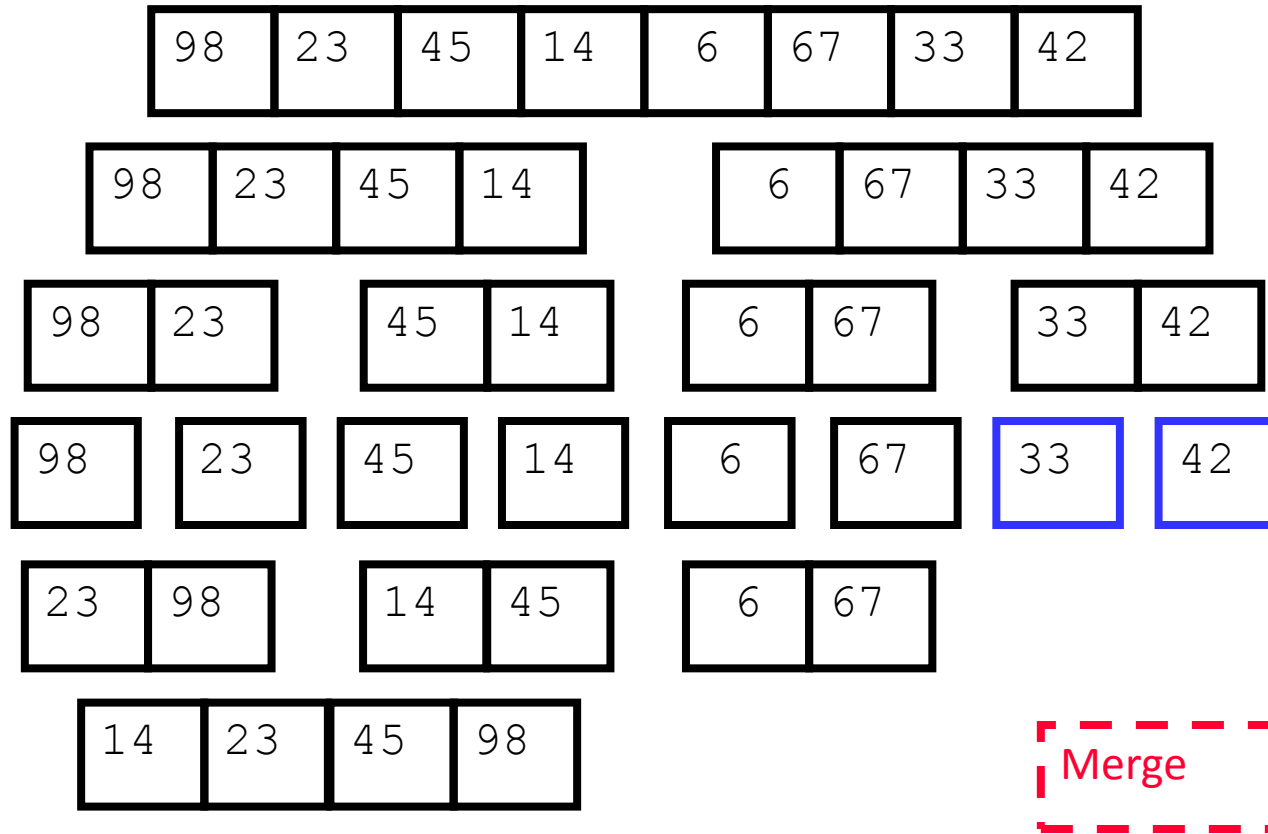


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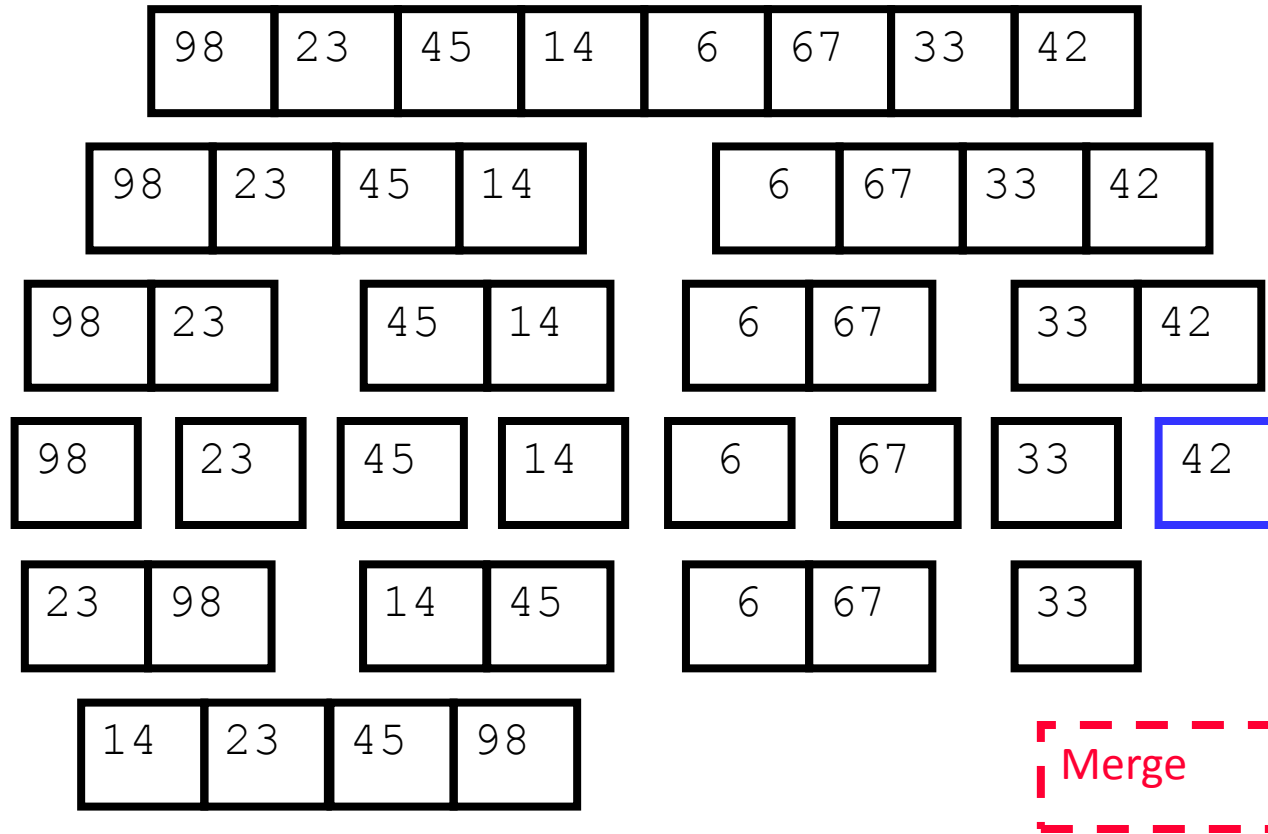




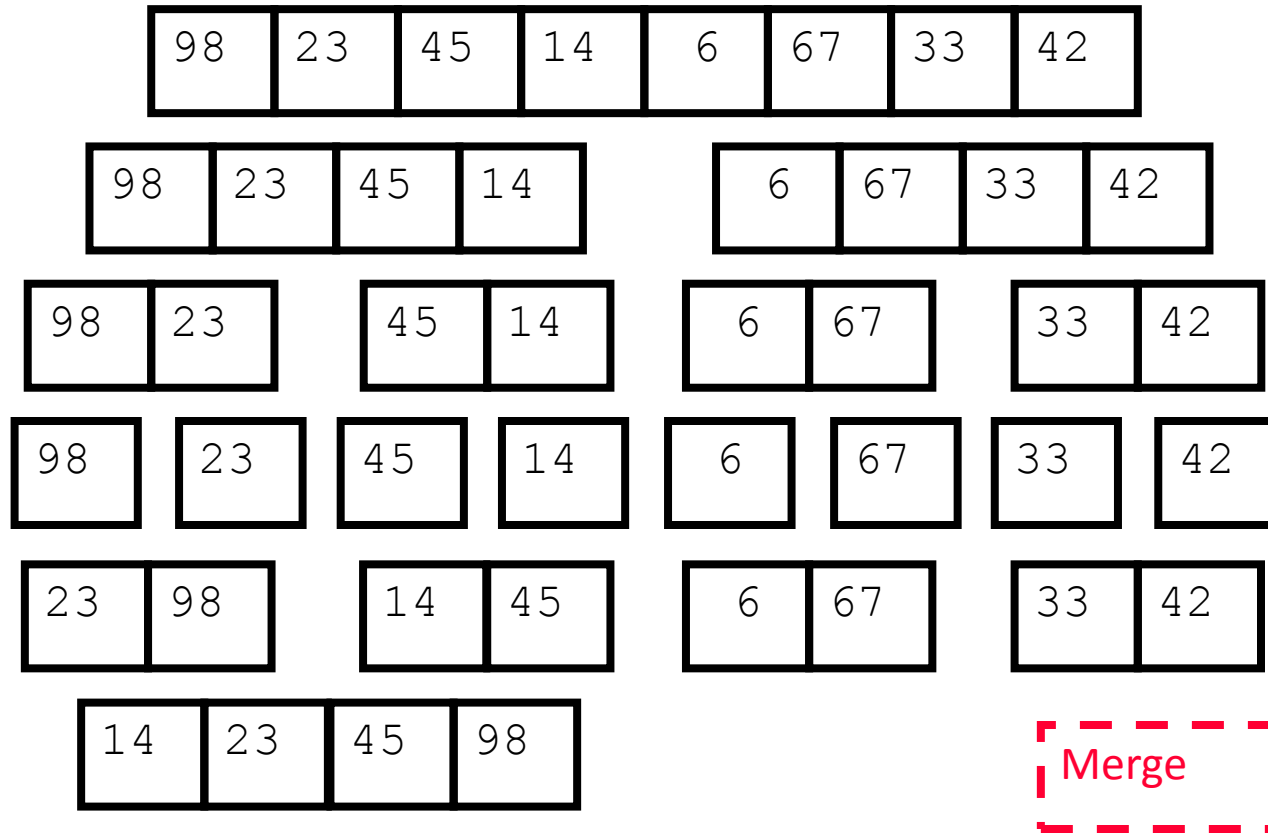
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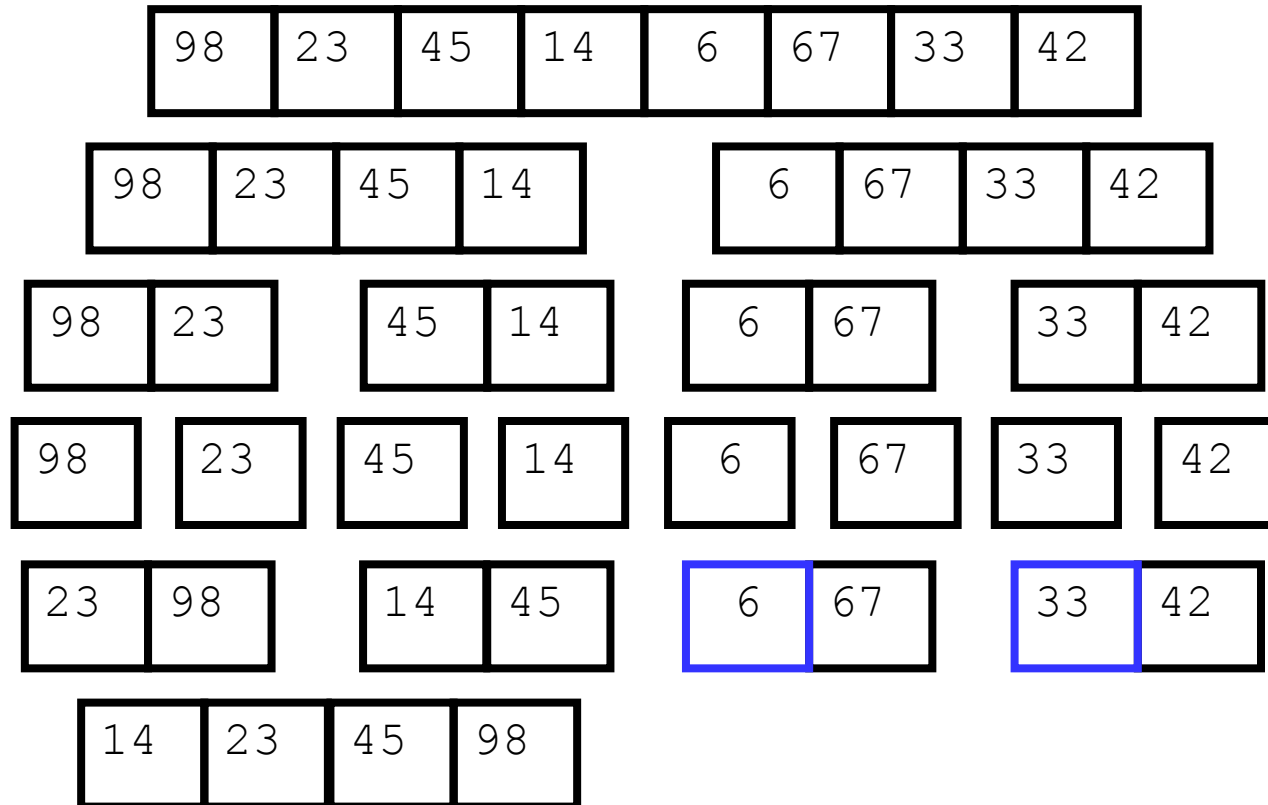
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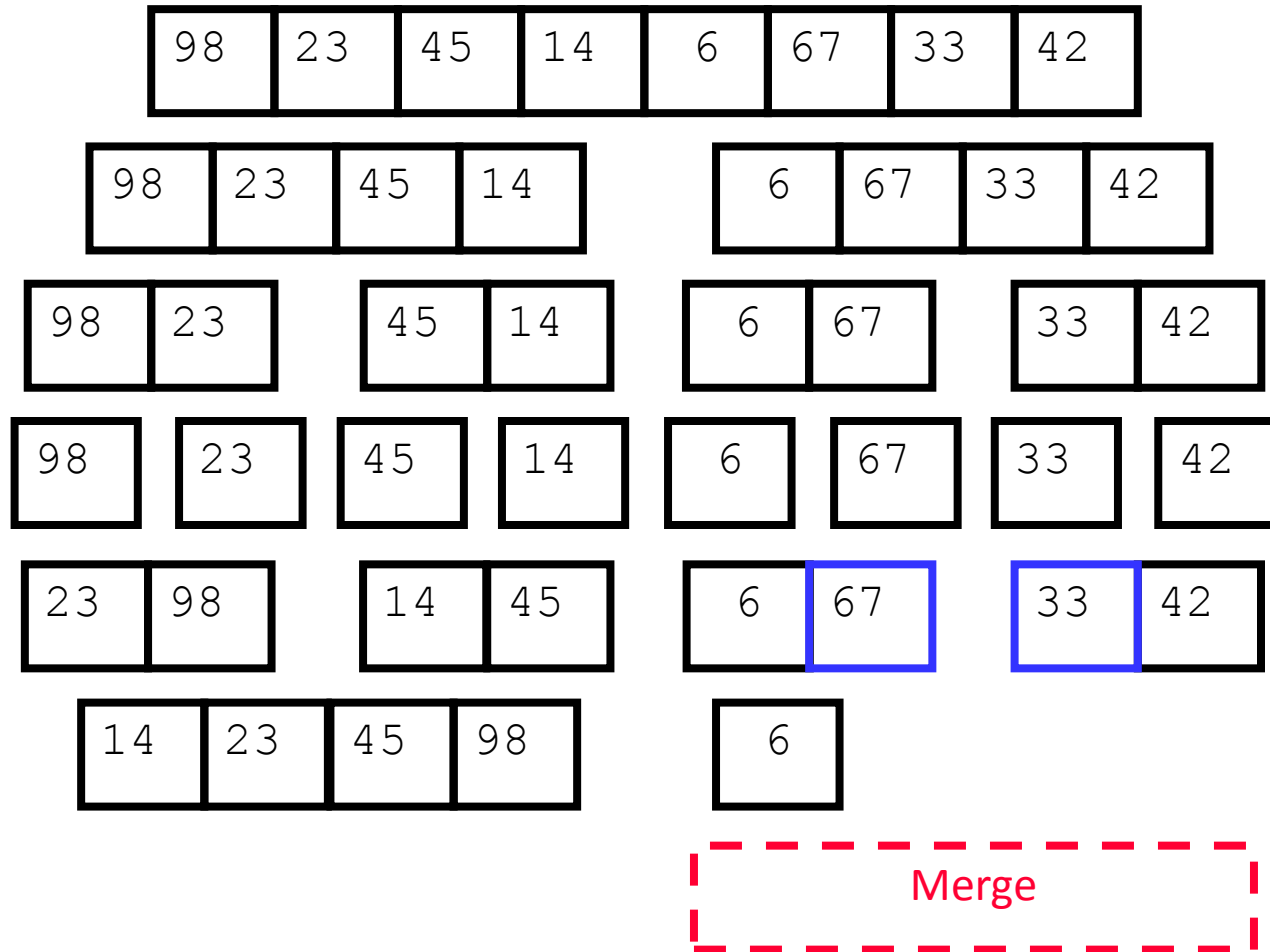


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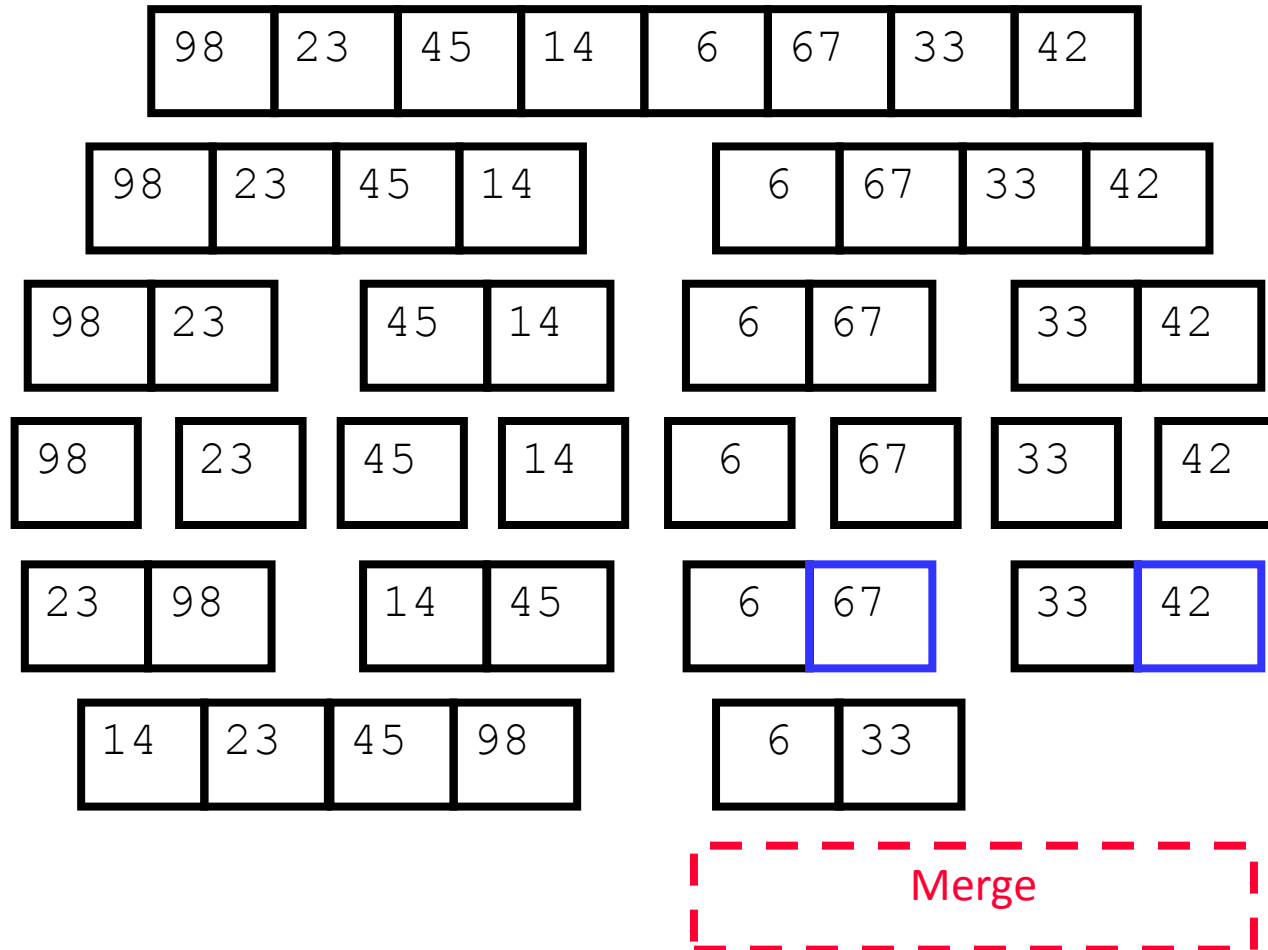


Merge

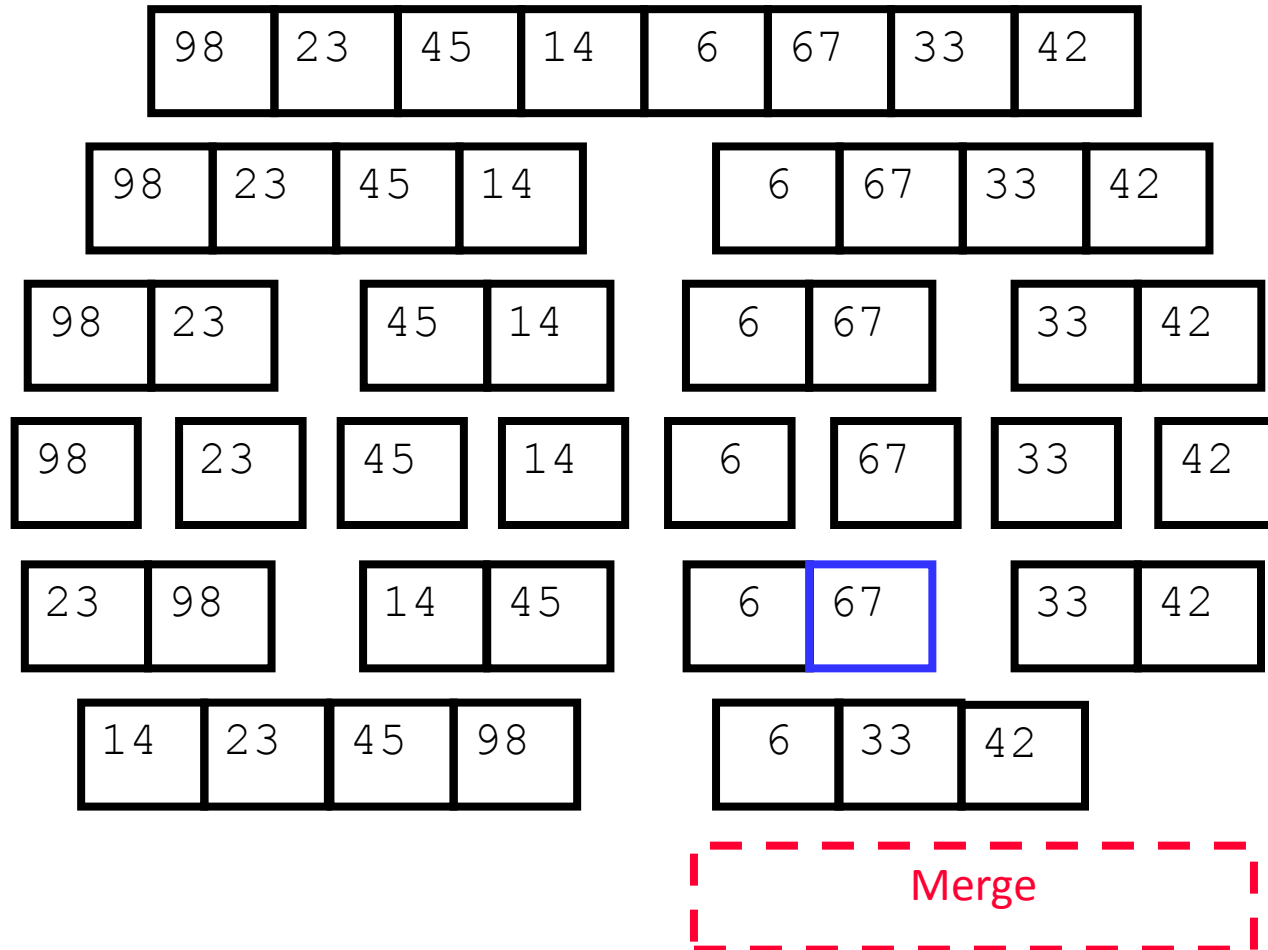
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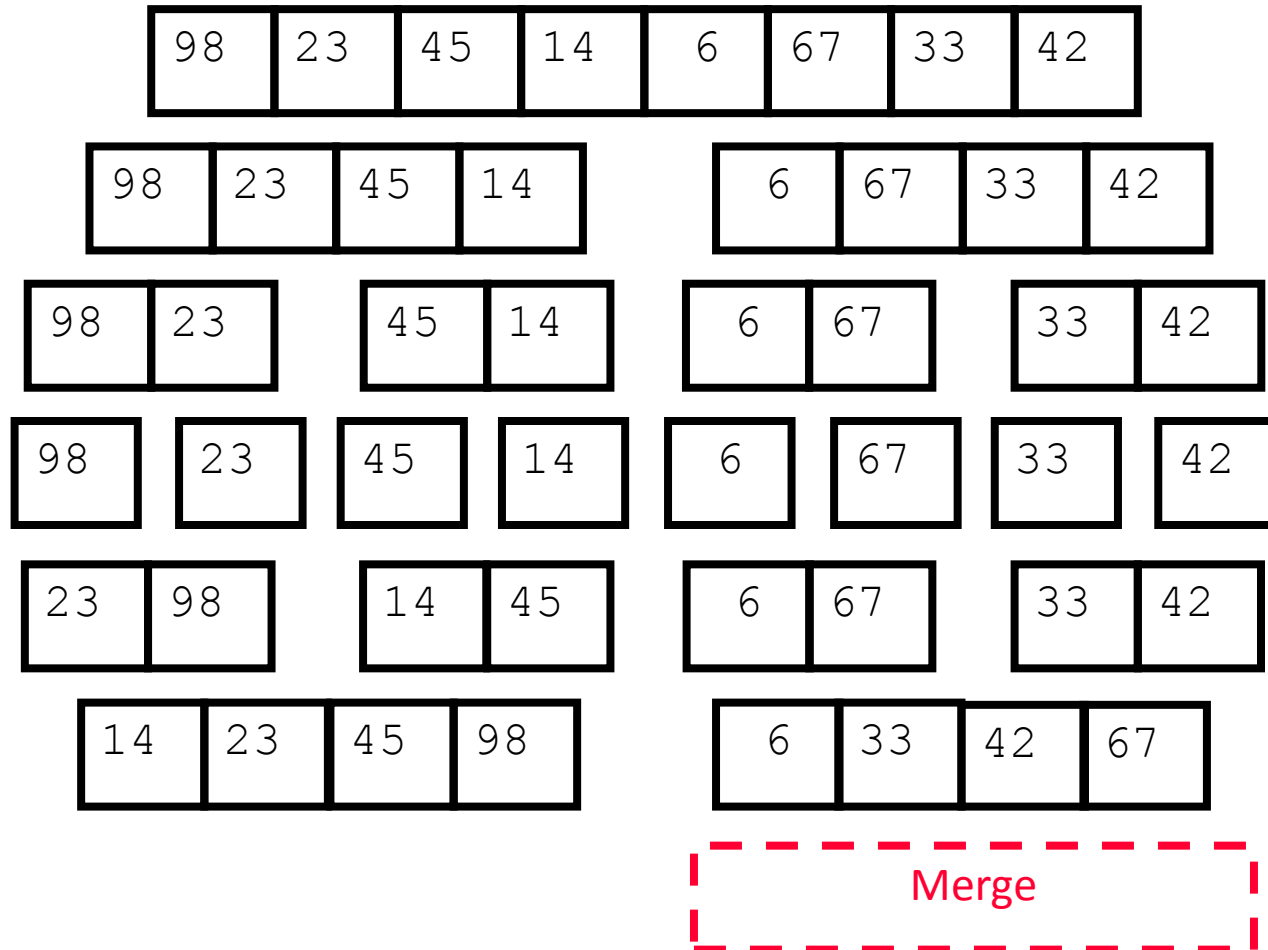
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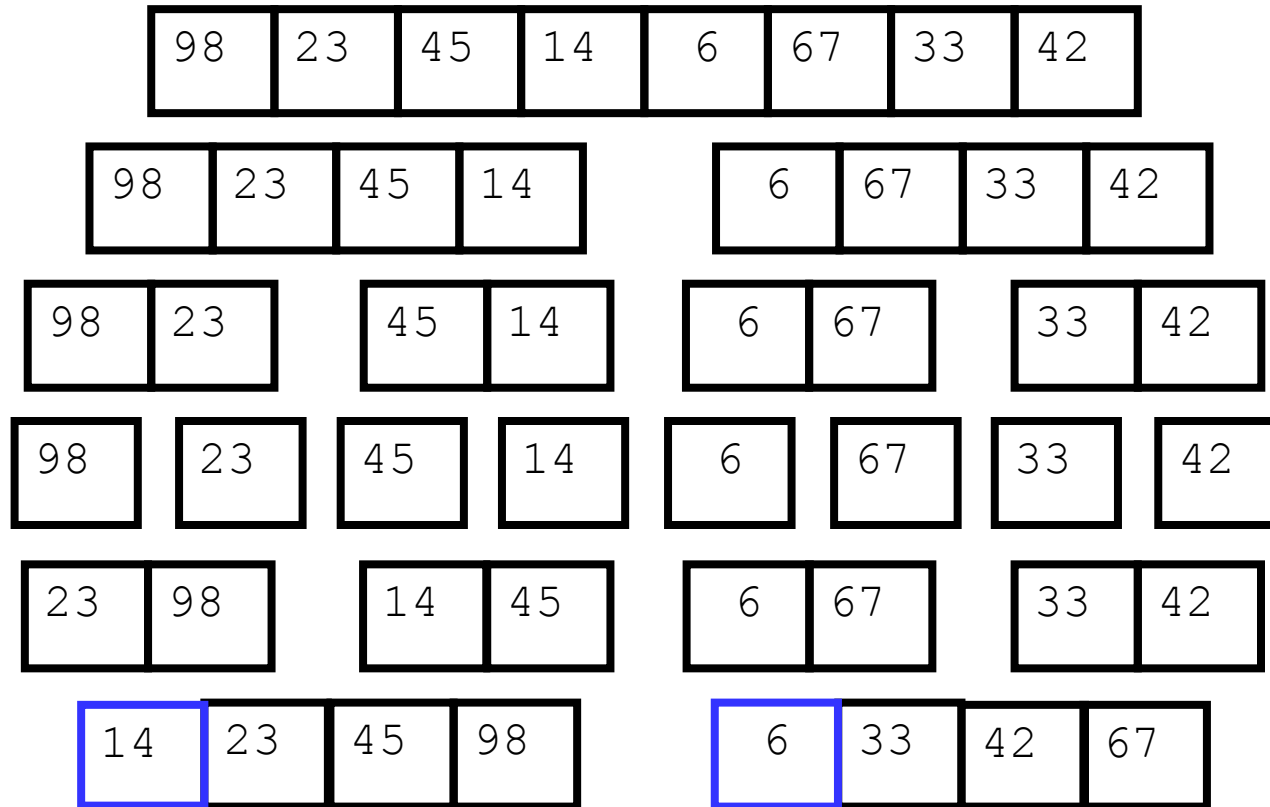


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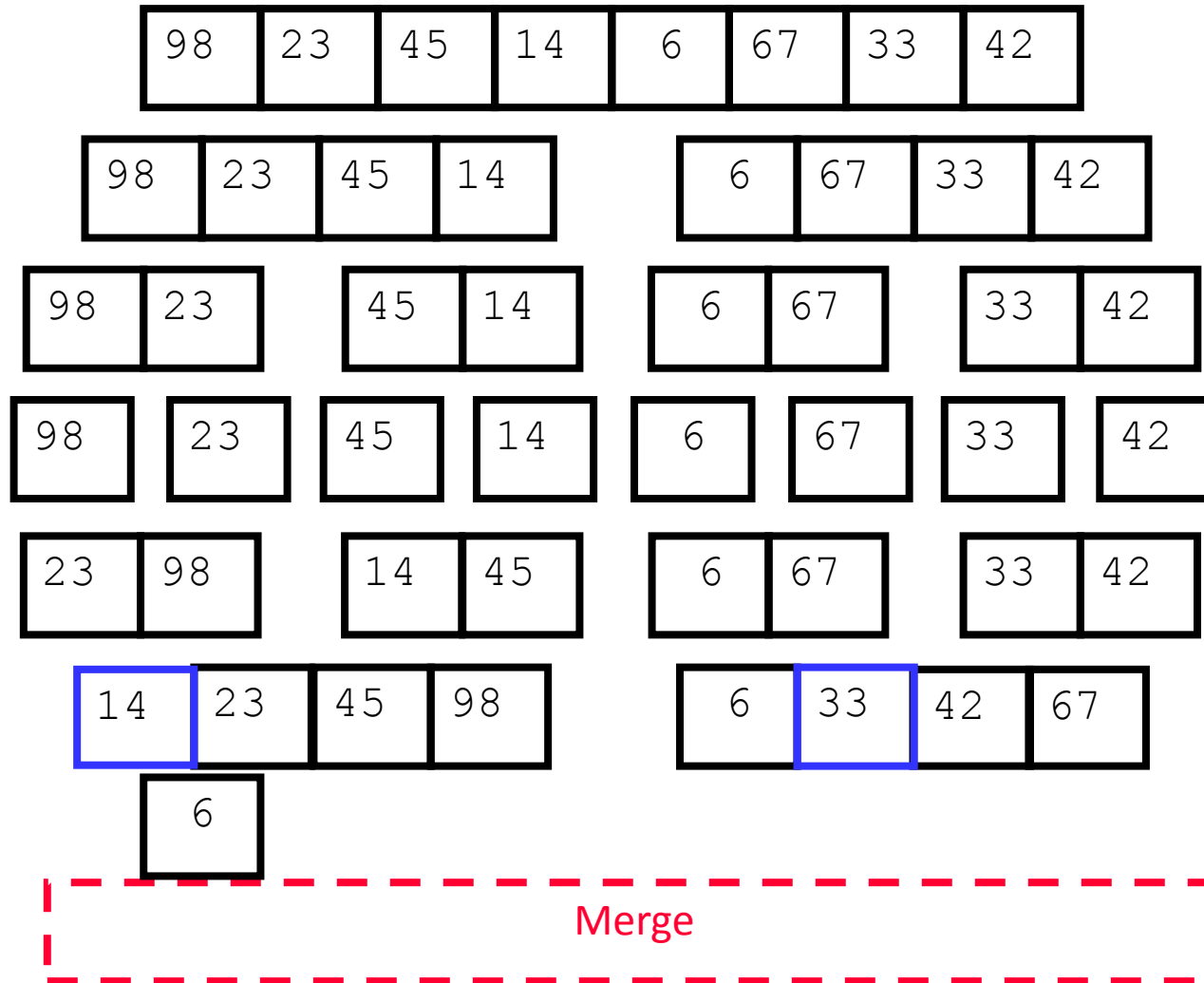




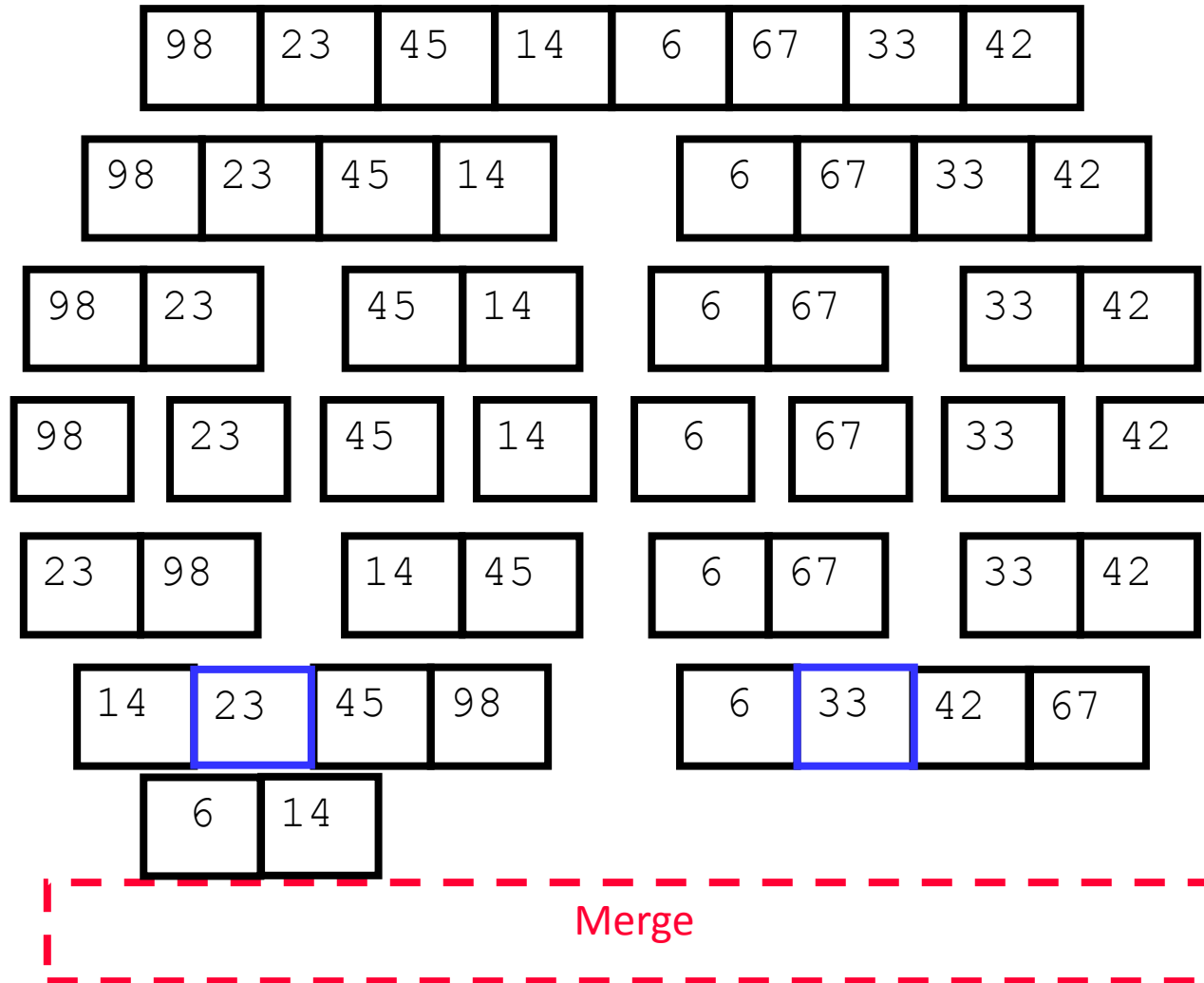
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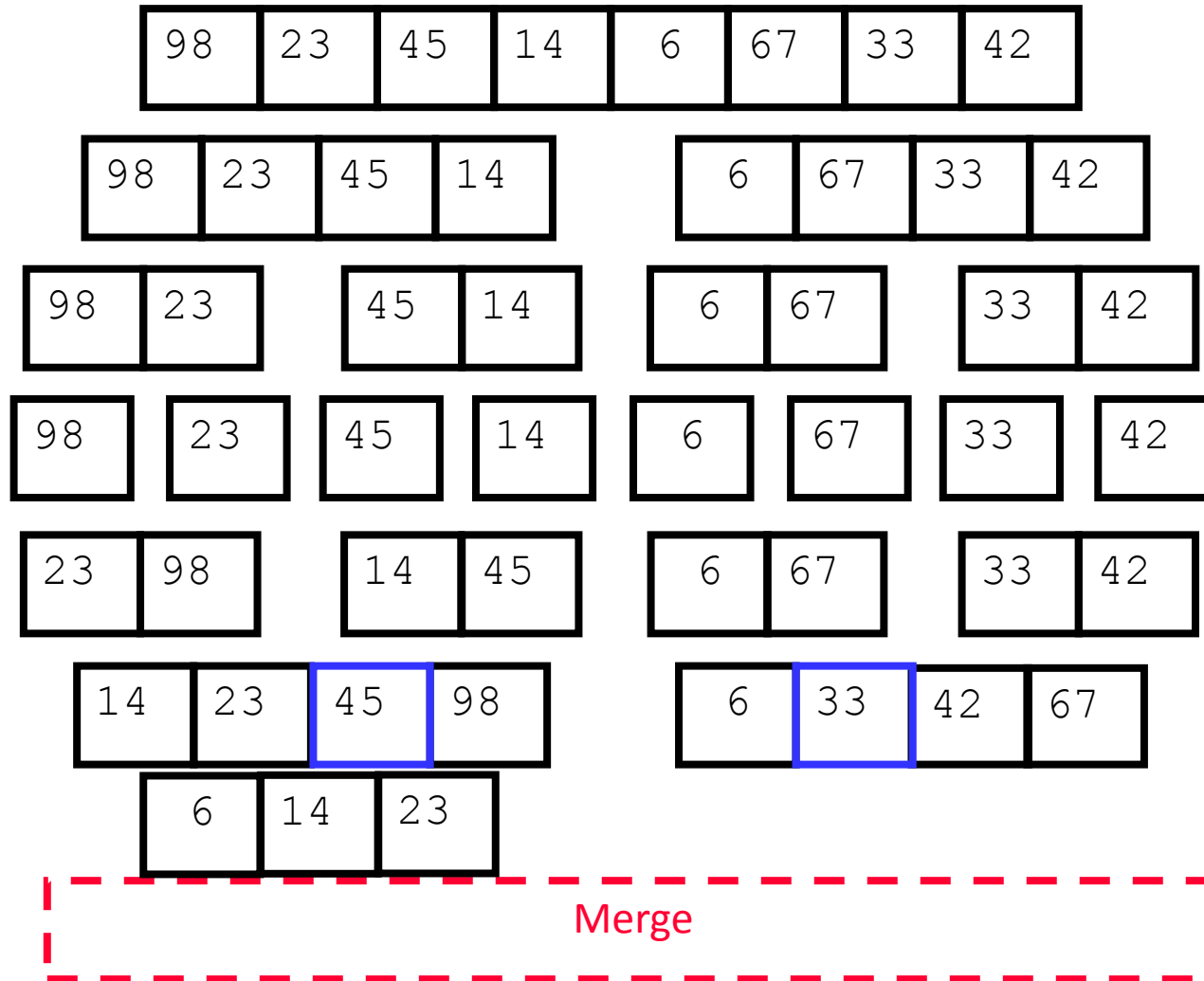
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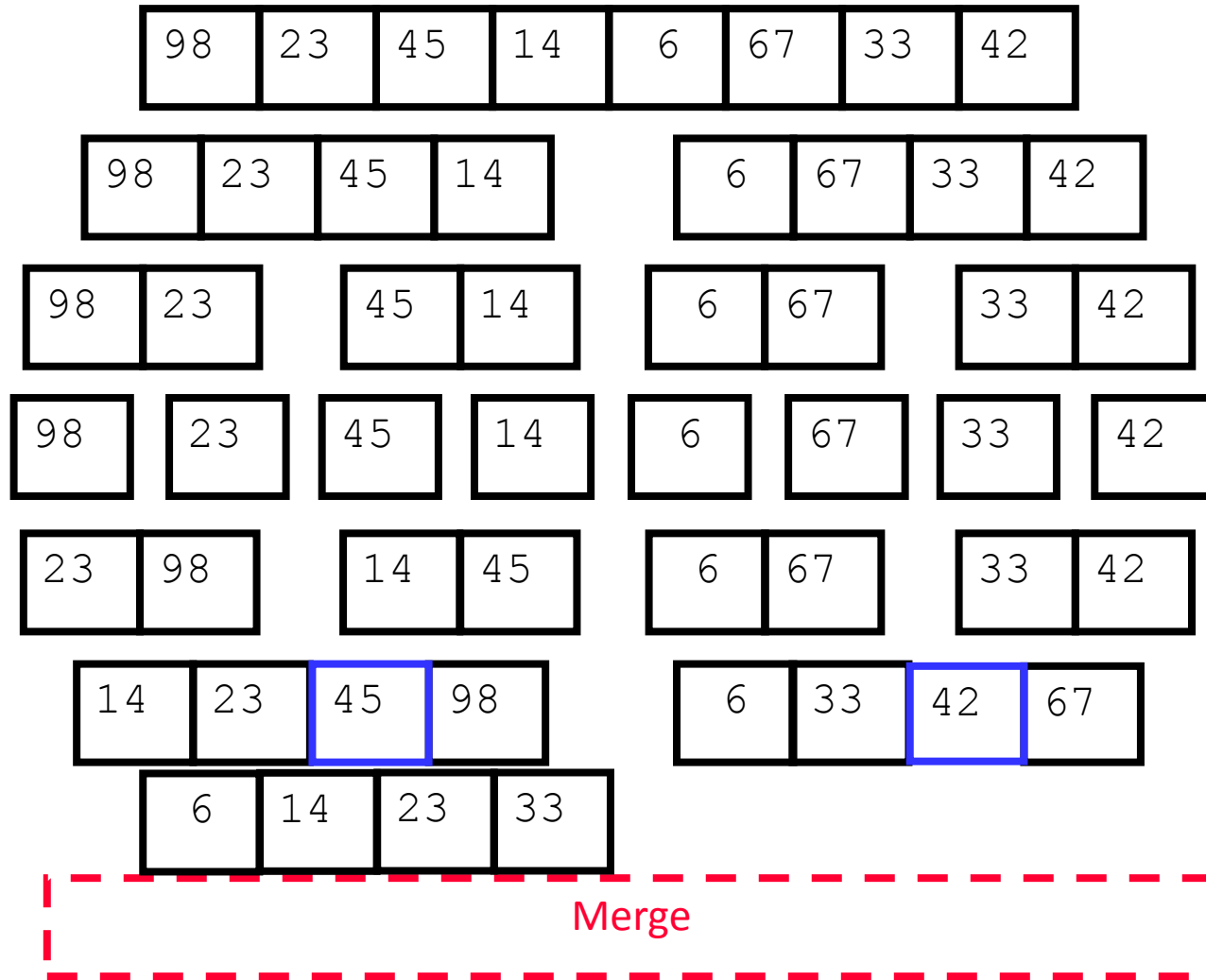
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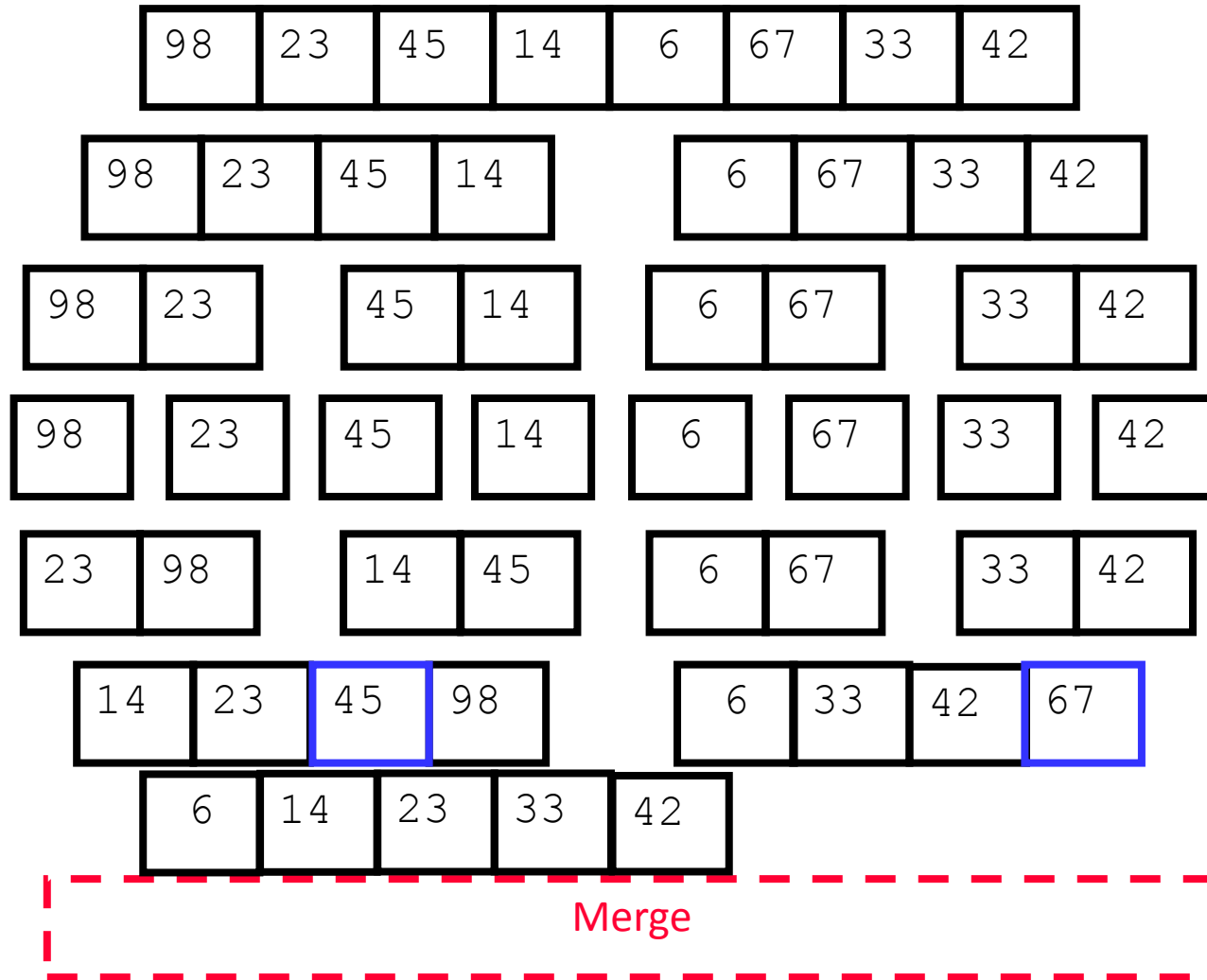
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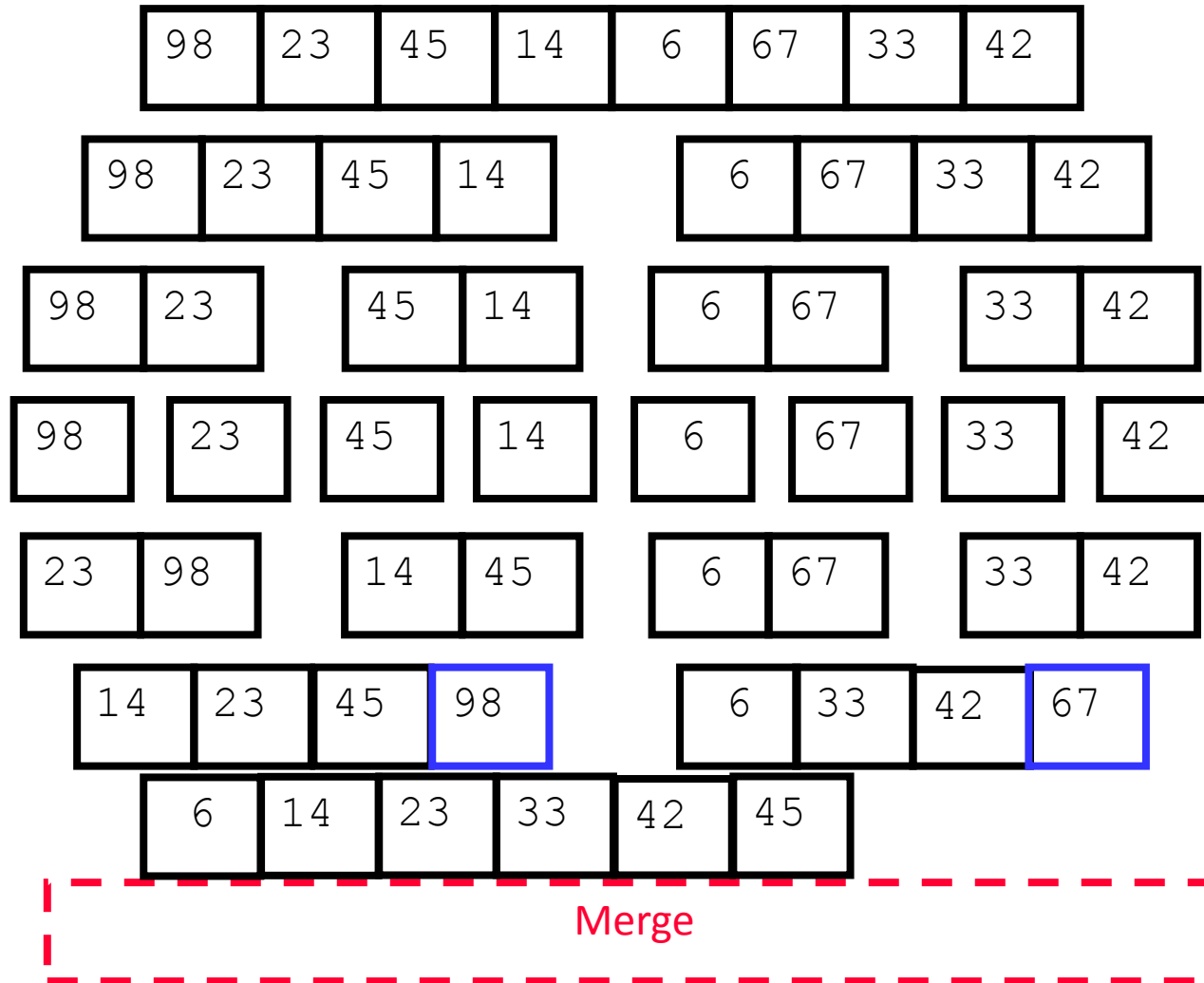
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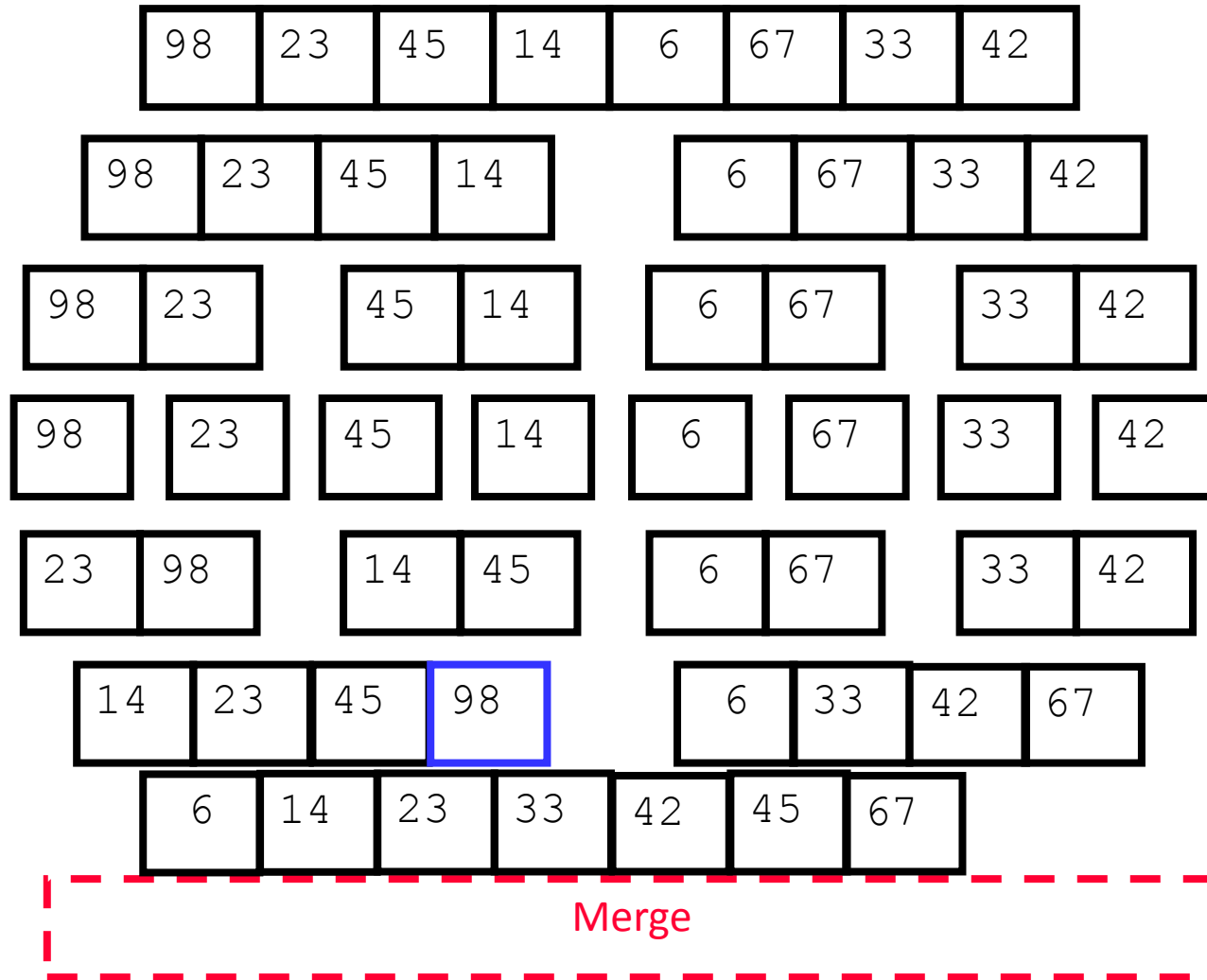
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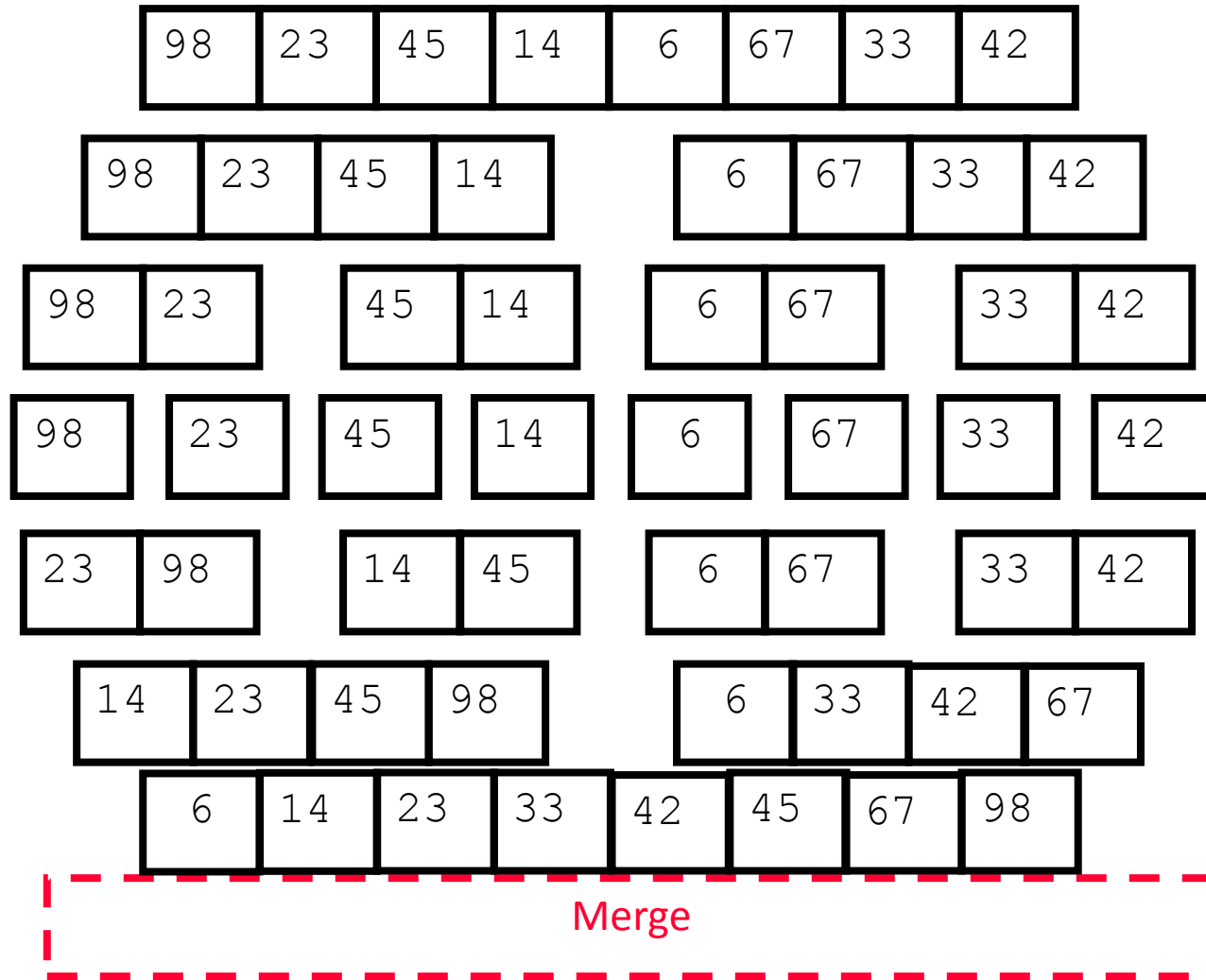


# Merge Sort (Example)





# Merge Sort (Example)



# Quicksort

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# Quicksort

QUICKSORT( $A, p, r$ )

```
1  if  $p < r$ 
2       $q = \text{PARTITION}(A, p, r)$ 
3      QUICKSORT( $A, p, q - 1$ )
4      QUICKSORT( $A, q + 1, r$ )
```

To sort an entire array  $A$ , the initial call is QUICKSORT( $A, 1, A.length$ ).

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PARTITION( $A, p, r$ )

```
1   $x = A[r]$ 
2   $i = p - 1$ 
3  for  $j = p$  to  $r - 1$ 
4      if  $A[j] \leq x$ 
5           $i = i + 1$ 
6          exchange  $A[i]$  with  $A[j]$ 
7  exchange  $A[i + 1]$  with  $A[r]$ 
8  return  $i + 1$ 
```

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