

# Queues

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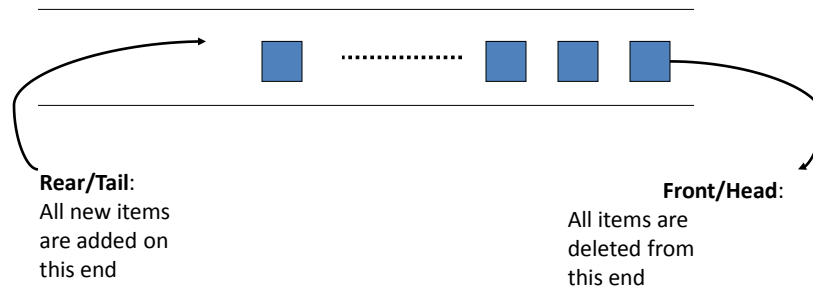
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## Queue: Introduction

- Another subclass of lists that permits deletions to be performed at one end of the list and insertions at the other.
- Information is processed in the same order as it was received
  - i.e. First In First Out (FIFO) or First Come First Serve(FCFS)
- Examples: a checkout line at supermarket cash register, timesharing computer system, line of cars waiting to proceed in some fixed direction at an intersection of streets....

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## A Graphical Model of a Queue



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## Operations on Queues

- **Insert(item):** (also called enqueue)
  - It adds a new item to the tail of the queue
- **Delete( ):** (also called dequeue)
  - It deletes the head item of the queue, and returns to the caller. If the queue is already empty, this operation returns NULL
- **getHead( ):**
  - Returns the value in the head element of the queue
- **getTail( ):**
  - Returns the value in the tail element of the queue
- **isEmpty( )**
  - Returns **true** if the queue has no items
- **size( )**
  - Returns the number of items in the queue

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## Insertion in Queue: Algorithm

**Algorithm** QINSERT(Q,Head, Tail,N, Y)

**Input:** Given Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements, and an element Y, this procedure inserts Y at the Tail of the queue. Prior to first invocation of the procedure, Head and Tail are set to -1.

**Output:** **true** if and only if Y is successfully inserted in Q else **false**

*[Overflow?]*

**if** Tail  $\geq$  N-1 **then**

**return false** {Overflow}

*[Increment Tail pointer]*

Tail  $\leftarrow$  Tail+1

*[Insert element]*

Q[Tail]  $\leftarrow$  Y

*[Is Head properly set?]*

**if** Head = -1 **then**

    Head  $\leftarrow$  0

**return true**

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## Deletion from Queue: Algorithm

**Algorithm** QDELETE(Q,Head, Tail,N)

**Input:** Given Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements, this procedure deletes an element from the Head of the queue.

**Output:** **last element** if deletion is successful else **false**

*[Underflow?]*

**if** Head = -1 **then**

**return false** {Underflow}

*[Delete element]*

Y  $\leftarrow$  Q[Head]

*[Increment Head]*

**if** Head = Tail **then**

    Head  $\leftarrow$  Tail  $\leftarrow$  -1

**else**

    Head  $\leftarrow$  Head+1

*[Return element]*

**return Y**

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## Get Head element of Queue: Algorithm

**Algorithm** GET\_HEAD(Q,Head,Tail,N)

**Input:** Given Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements, this procedure returns an element from the Head of the queue.

**Output:** **Head element** if successful else **false**

*[Underflow?]*

**if** Head = -1 **then**

**return false** {Underflow}

*[Get the element]*

Y ← Q[Head]

*[Return element]*

**return** Y

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## Get Tail element of Queue: Algorithm

**Algorithm** GET\_TAIL(Q,Head,Tail,N)

**Input:** Given Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements, this procedure returns an element from the Tail of the queue.

**Output:** **Tail element** if successful else **false**

*[Underflow?]*

**if** Tail = -1 **then**

**return false** {Underflow}

*[Get the element]*

Y ← Q[Tail]

*[Return element]*

**return** Y

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## IsEmpty(): Algorithm

**Algorithm** ISEMPY(Q,Head,Tail,N)

**Input:** Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements.

**Output:** **true** if Q is empty else **false**

*[check if Q is empty or not]*

**if** Head = Tail = -1 **then**

**return true**

**else**

**return false**

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## Size(): Algorithm

**Algorithm** SIZE(Q,Head,Tail,N)

**Input:** Head and Tail, pointers to the head and tail elements of a queue Q consisting of N elements.

**Output:** **number of elements** in Q

*[check if Q is empty or not]*

**if** Head = Tail = -1 **then**

**return 0**

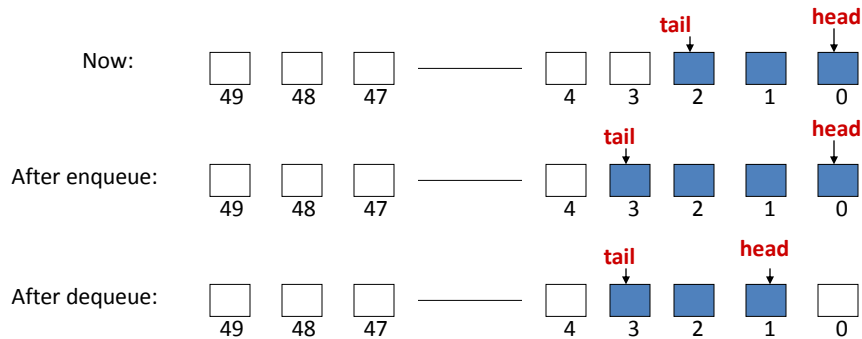
**else**

**return (Tail – Head +1)**

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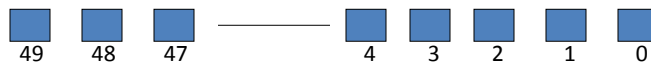
## How **head** and **tail** Change

- **Tail** increases by 1 after each Insert( )
- **Head** increases by 1 after each Delete( )



## False-Overflow

- Suppose 50 calls to Insert( ) have been made, so now the queue array is full



- Assume 4 calls to Delete( ) are made

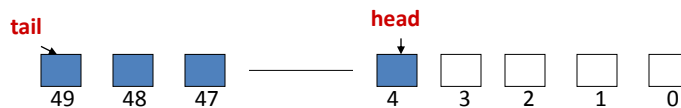


- Assume a call to Insert( ) is made now. The tail part seems to have no space, but the front has 4 unused spaces; if never used, they are wasted.

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## Solution: A Circular Queue

- Allow the head (and the tail) to be moving targets
- When the tail end fills up and front part of the array has empty slots, new insertions should go into the front end

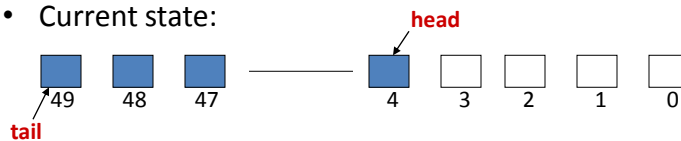


- Next insertion goes into slot 0, and tail tracks it. The insertion after that goes into a lot 1, etc.

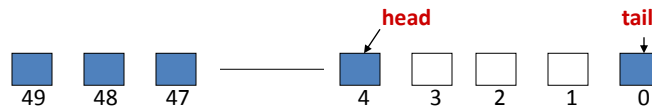
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## Illustration of Circular Queue

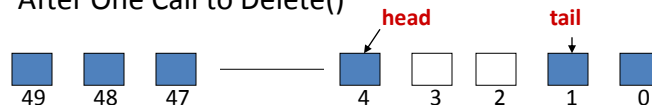
- Current state:



- After One Call to Insert()



- After One Call to Delete()



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## Numerics for Circular Queues

- **head** increases by (1 modulo capacity) after each Delete( ):

$$\text{head} = (\text{head} + 1) \% \text{capacity};$$

- **tail** increases by (1 modulo capacity) after each Insert( ):

$$\text{tail} = (\text{tail} + 1) \% \text{capacity};$$

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## Operations on Circular Queues

- **Insert(item):**
  - It adds a new item to the tail of the circular queue
- **Delete( ):**
  - It deletes the head item of the circular queue, and returns to the caller. If the queue is already empty, this operation returns false.
- **isEmpty( )**
  - Returns **true** if the queue has no items

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## Insertion in Queue: Algorithm

**Algorithm** CQINSERT(Q,Head, Tail,N, Y)

**Input:** Given Head and Tail, pointers to the head and tail elements of a circular queue Q consisting of N elements, and an element Y, this procedure inserts Y at the Tail of the queue. Prior to first invocation of the procedure, Head and Tail are set to -1.

**Output:** **true** if and only if Y is successfully inserted in Q else **false**

*[Reset Tail pointer]*

**if** Tail = N-1 **then**

Tail  $\leftarrow$  0

**else**

Tail  $\leftarrow$  Tail + 1

*[Overflow?]*

**if** Head = Tail **then**

**return false** {Overflow}

*[Insert element]*

Q[Tail]  $\leftarrow$  Y

*[Is Head properly set?]*

**if** Head = -1 **then**

Head  $\leftarrow$  0

**return true**

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## Deletion from Circular Queue: Algorithm

**Algorithm** CQDELETE(Q,Head, Tail,N)

**Input:** Given Head and Tail, pointers to the head and tail elements of a circular queue Q consisting of N elements, this procedure deletes an element from the Head of the circular queue.

**Output:** **last element** if deletion is successful else **false**

*[Underflow?]*

**if** Head = -1 **then**

**return false** {Underflow}

*[Delete element]*

Y  $\leftarrow$  Q[Head]

*[Is Q empty?]*

**if** Head = Tail **then**

Head  $\leftarrow$  Tail  $\leftarrow$  -1

*[Increment Head]*

**if** Head = N-1 **then**

Head  $\leftarrow$  0

**else**

Head  $\leftarrow$  Head+1

*[Return element]*

**return Y**

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## IsEmpty(): Algorithm

**Algorithm** CQ\_IS\_EMPTY(Q,Head, Tail,N)

**Input:** Given Head and Tail, pointers to the head and tail elements of a circular queue Q consisting of N elements

**Output:** **true** if Q is empty else **false**

*[Underflow?]*

**if** Head = Tail = -1 **then**

**return true**

**else**

**return false**

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## Tutorial :Size(): Algorithm

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## Double ended queue (Deque)

pronounced deck

- More general than a stack and a queue
- A linear list in which insertions and deletions are made to or from either end of the structure
- Two variations
  - Input-restricted deque
    - allows insertions at only one end
  - Output-restricted deque
    - allows deletions from only one end

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## Double ended queue (Deque)

pronounced deck

- Tutorial :
  1. Formulate an algorithm for performing an insertion into an input-restricted deque
  2. Formulate an algorithm for performing a deletion from an input-restricted deque
  3. Repeat 1 & 2 for output-restricted deque

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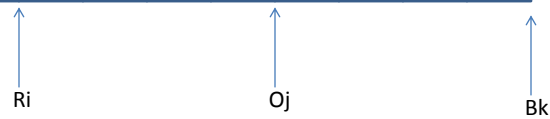
## Priority Queue

- A queue in which we are able to insert or remove items from any position based on some priority

Task identification

R1	R2	...	Ri-1	O1	O2	...	Oj-1	B1	B2	...	Bk-1
1	1	...	1	2	2	...	2	3	3	...	3

Priority



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## Applications of Queue

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## Applications

- Shared resources management (system programming):
  - Access to the processor;
  - Access to the peripherals such as disks and printers.
- Application programs:
  - Simulations

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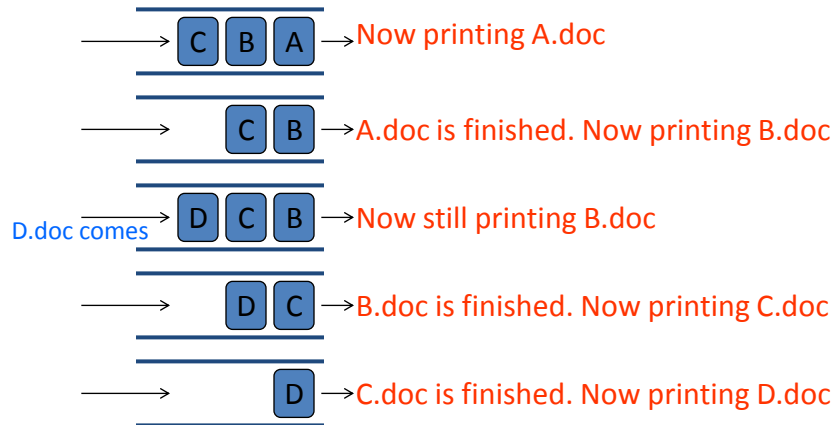
## Printing Job Management

- Many users send their printing jobs to a public printer
- Printer will put them into a queue according to the arrival time and print the jobs one by one
- These printing documents are A.doc, B.doc, C.doc and D.doc

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## Printing Queue

- A.doc B.doc C.doc arrive to printer.



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## Customer Service In Royal Bank

- Suppose there is only one customer service available in Royal Bank on Saturday morning
- In every 3 minutes, a new customer arrives at the end of waiting line
- Each customer will need 5 minutes for the service
- Print out the information after the first 30 minutes
  - The time of arriving and leaving for each customer
  - How many customers are in the line?
  - Who is the current serving customer?

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## Customer Service Queue

```
public void run( ) {
    // Create a new queue
    QueuePT que = new ArrayQueuePT(100);
    int time = 0;           // in minutes
    int incustomer = 0;     // sequence of
                           customers
    int servicetime = 0;    // service times
}
```

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## Customer In Service

```
// what's going on in 30 minutes
while ( time <= 30 ) {
    // if queue is not empty, one customer service is working
    if( que.size()!=0 ) {
        servicetime = servicetime + 1;
        // customer leaves when finishing the service, the service time
        // is 5 minutes
        if( servicetime == 5 ) {
            String name = (String)que.dequeue();
            System.out.println("<< " + name + " leaves at time = " +
time);
            // start to service time for next customer
            servicetime = 0;
        }
    }
}
```

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## New Customer Comes

```
// every 3 minutes, there is a new customer coming.
if( time%3==0 )
{
    incustomer = incustomer + 1;
    String name = "CUSTOMER " + incustomer;
    que.enqueue( name );
    System.out.println(">> " + name + " arrives at time
= " + time);
}
time = time + 1;
}
```

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## Print Status After 30 Minutes

```
// print the status after 30 minutes
System.out.println("\n=====");
if( que.size()!=0 )
{
    System.out.println("There are " + que.size() + " customers in
the line" );
    System.out.println("The current serving customer is " +
que.peek() );
}
else
{
    System.out.println("There are no customers in the line" );
}
}
```

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## Priority Queue --- Air Travel

- Only one check-in service in Air Canada at airport
- Two waiting lines for passengers
  - one is First class service
  - the other is Economy class service
- Passengers in the first-class waiting line have higher priority to check in than those in the economy-class waiting line.



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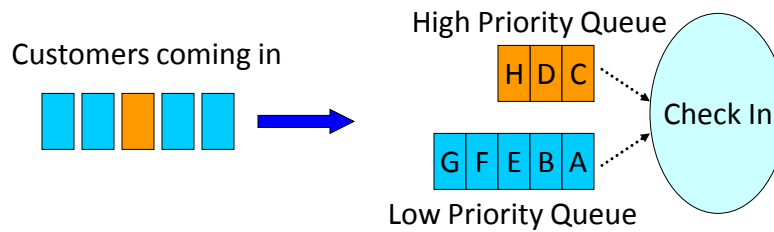
## Priority Queue

- Two queues
  - one is high priority queue
  - the other is low priority queue
- Service rules:
  - First serve the people in high priority queue
  - If no passengers are in high priority queue, serve the passengers in low priority queue

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## Two Queues

- High Priority Queue,  will come in *hpQue*
- Low Priority Queue,  will come in *lpQue*



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## Pseudocode For Arrival

Passengers Arrival:

```

if( new Passenger comes ) {
    if( is First Class)
        hpQue.enqueue( new Passenger );
    else
        lpQue.enqueue( new Passenger );
}

```

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## Pseudocode For Service

Check-In Service:

```

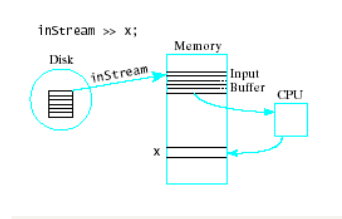
if( hpQue is not empty ) {
    serve the passenger from high priority queue,
    hpQue.dequeue();
}
else {
    serve the passenger from low priority queue,
    lpQue.dequeue();
}

```

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## Application of Queues: Buffers and Scheduling

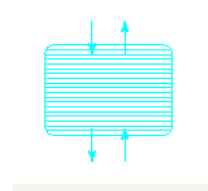
- Important use of queues is I/O scheduling
  - Use buffers in memory to improve program execution
  - Buffer arranged in FIFO structure



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## Application of Queues: Buffers and Scheduling

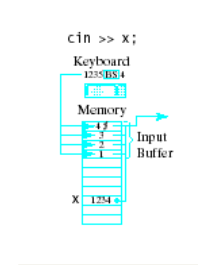
- Also times when insertions, deletions must be made from both ends
  - Consider a scrolling window on the screen
- This requires a double ended queue



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## Application of Queues: Buffers and Scheduling

- Consider a keyboard buffer
  - Acts as a queue
  - But elements may be removed from the back of the queue with backspace key



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