

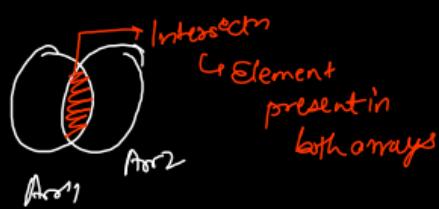
# Intersection of 2 Arrays

# Constraint

Each array contains  
distinct elements

(N) Arr1: { 30, 10, 45, 20, 65, 15, 70 }

(M) Arr2: { 40, 45, 10, 17, 23, 33, 65, 20 }



{ 10, 45, 20, 65 }  
↓  
⇒ Answer order does not matter

# Brute force  $\Rightarrow$  2 Nested loops

↳ outer loop:  $\rightarrow$  first array  $\rightarrow \textcircled{N}$

inner loop:  $\rightarrow$  Second array  $\rightarrow \textcircled{M}$

if ( $\text{arr1}[i] == \text{arr2}[j]$ )  
↑                       ↑  
intersection found

Comparisons  $\rightarrow O(N * M)$

# Optimized Approach → {doubling + Two Pointers}

<  $O(N^2)$  &  $O(N \log N)$   
MergeSort, QuickSort

Arr1: { 10, 15, 20, 30, 45, 65, 70 }  
Arr2: { 10, 17, 20, 23, 33, 40, 45, 65 }

faster will  
be faster  
than the  
brute force

10, 20, 45, 65

ptr1 < arr1.length  
ptr2 < arr2.length  
while

# Comparisons  
10-10 45-33  
15-17 45-40  
20-17 45-45  
20-20 65-65  
30-23  
30-33  
 $O(N+M)$

Activat  
Go to Set

#  
arr1 and arr2  
are already sorted  
An array

# Merging 2 Sorted Arrays

$O(N+M)$

#  
merged array  
should  
also  
be sorted

arr1: { 10, 30, 50, 60, 70, 100, 110, 120, 130 }  
arr2: { 20, 40, 80, 90, 110, 130, 140, 150 }

res: { 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 130, 140, 150 }

{ 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 130, 140, 150 } } output

## Array Rotation of Left

$R=0, 6, 12, 18, 24 \leftarrow [6*m+0]$   
 $\{10, 20, 30, 40, 50, 60\}$

$R=1, 7, 13 \leftarrow [6*m+1]$   
 $\{20, 30, 40, 50, 60, 10\}$

$R=2, 8, 14 \leftarrow [6*m+2]$   
 $\{30, 40, 50, 60, 10, 20\}$

$R=3, 9, 15 \leftarrow [6*m+3]$   
 $\{40, 50, 60, 10, 20, 30\}$

$R=4, 10, 16 \leftarrow [6*m+4]$   
 $\{50, 60, 10, 20, 30, 40\}$

$R=5, 11, 17 \leftarrow [6*m+5]$   
 $\{60, 10, 20, 30, 40, 50\}$

# Smallest Rotation for any R  
 will be  $R/\text{size}$

```
int ptr1 = 0, ptr2 = 0, ptr3 = 0;
int[] res = new int[arr1.length + arr2.length];

while(ptr1 < arr1.length && ptr2 < arr2.length){
    if(arr1[ptr1] < arr2[ptr2]){
        res[ptr3] = arr1[ptr1];
        ptr1++; ptr3++;
    }
    else {
        res[ptr3] = arr2[ptr2];
        ptr2++; ptr3++;
    }
}
```

③ arr1: { 2, 3, 5 }  
 $\begin{matrix} p_1 \\ \downarrow \\ 2 \\ \downarrow \\ 3 \\ \downarrow \\ 5 \end{matrix}$

④ arr2: { 1, 4, 5, 8 }  
 $\begin{matrix} p_2 \\ \downarrow \\ 1 \\ \downarrow \\ 4 \\ \downarrow \\ 5 \\ \downarrow \\ 8 \\ \uparrow \\ p_2 \end{matrix}$

res: { 1 2 3 4 5 5 8 }  
 $\begin{matrix} p_3 \\ \uparrow \\ 1 \\ \uparrow \\ 2 \\ \uparrow \\ 3 \\ \uparrow \\ p_3 \end{matrix}$

g: 10

```
while(ptr1 < arr1.length){
    res[ptr3] = arr1[ptr1];
    ptr1++; ptr3++;
}

while(ptr2 < arr2.length){
    res[ptr3] = arr2[ptr2];
    ptr2++; ptr3++;
}
```

## Rotate Array {Left rotation}

- arr = { 10, 20, 30, 40, 50, 60, 70 }  
k = 0, 7, 14, 21, 28  
After 1st rotation → All multiples of 7 + 1  
{ 10, 20, 30, 40, 50, 60, 70 }  
After 2nd rotation → All multiples of 7 + 2  
{ 20, 30, 40, 50, 60, 70, 10 }  
After 3rd rotation → A ---- + 3  
{ 30, 40, 50, 60, 70, 10, 20 }  
After 4th rotation → All multiples of 7 + 4  
{ 40, 50, 60, 70, 10, 20, 30 }
- arr = { 10, 20, 30, 40, 50, 60, 70 }  
k = 4, 11, 18  
After 4th rotation → { 50, 60, 30, 10, 20, 30, 40 }  
After 5th rotation → { 60, 70, 10, 20, 30, 40, 50 }  
After 6th rotation → { 20, 10, 20, 30, 40, 50, 60 }

~~Eg~~ 83<sup>rd</sup>  $n=7$

Any variable  
 $k \in [0, \infty)$  (not rotating)

$$R=0, 7, 14, 21, 28, \dots = 7 \cdot k \Rightarrow 0$$

$$k=1, 8, 15, 22, 29 = 7 \cdot k + 1 \Rightarrow 1$$

$$k=2, 9, 16, 23, 30 = 7 \cdot k + 2 \Rightarrow 2$$

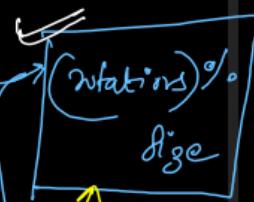
$$k=3, 10, 17, 24, 31 = 7 \cdot k + 3 \Rightarrow 3$$

$$k=4, 11, 18, 25, 32 = 7 \cdot k + 4 \Rightarrow 4$$

$$k=5, 12, 19, 26, 33 = 7 \cdot k + 5 \Rightarrow 5$$

$$k=6, 13, 20, 27, 34, = 7 \cdot k + 6 \Rightarrow 6$$

minimum rotation



### Array Rotation of Left

$$R=0, 6, 12, 18, 24 \leftarrow \boxed{6 \cdot m + 0}$$
$$\{10, 20, 30, 40, 50, 60\}$$

$$R=1, 7, 13 \leftarrow \boxed{6 \cdot m + 1}$$
$$\{20, 30, 40, 50, 60, 10\}$$

$$R=2, 8, 14 \leftarrow \boxed{6 \cdot m + 2}$$
$$\{30, 40, 50, 60, 10, 20\}$$

$$R=3, 9, 15 \leftarrow \boxed{6 \cdot m + 3}$$
$$\{40, 50, 60, 10, 20, 30\}$$

$$R=4, 10, 16 \leftarrow \boxed{6 \cdot m + 4}$$
$$\{50, 60, 10, 20, 30, 40\}$$

$$R=5, 11, 17 \leftarrow \boxed{6 \cdot m + 5}$$
$$\{60, 10, 20, 30, 40, 50\}$$

# Smallest Rotation for any R  
will be  $\boxed{R \% \text{size}}$

① Brute force  $\rightarrow$  By taking another array of same size  
Taking another array  $\uparrow$  {

- Reduce the value of K by  $K/size$
- First skipping the starting K elements
- Store the remaining elements
- Store the starting K elements

② Rotating 1 one by one

## ② Reversal algorithm

- (1)
- (2)
- (3)
- (4)

```
k = k % n; // Reduce the value of k to fit in array

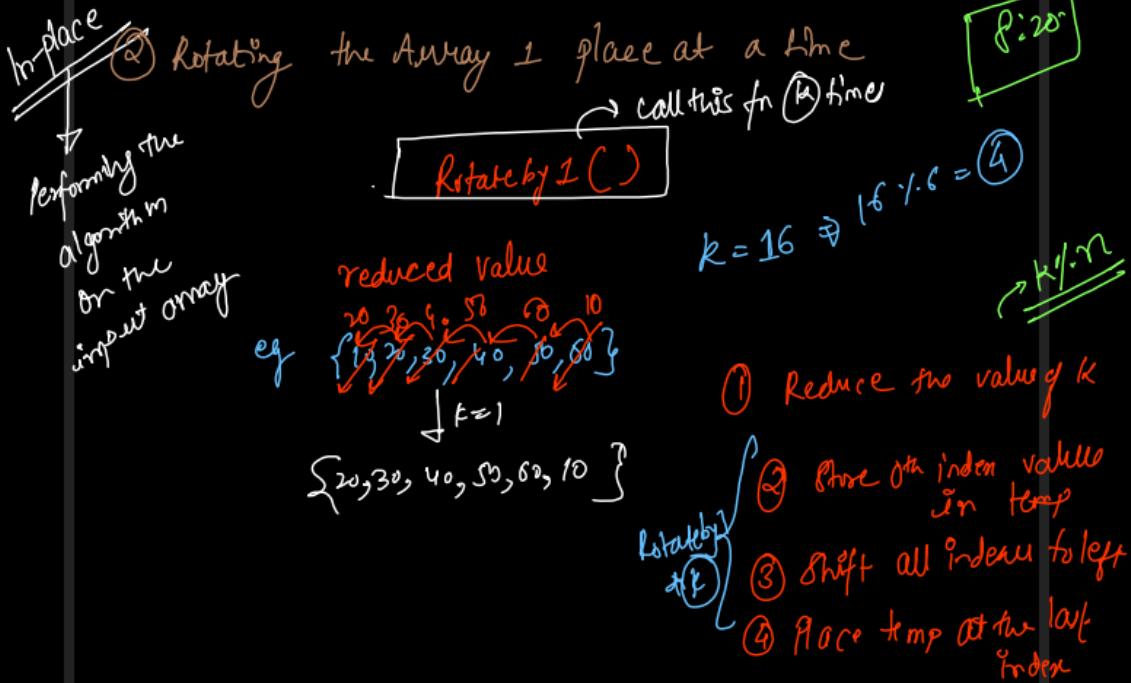
int[] output = new int[n];
int j = 0;

for(int i=k; i<n; i++){
    output[j] = input[i];
    j++;
}

for(int i=0; i<k; i++){
    output[j] = input[i];
    j++;
}
```

13

० १ २ ३ ४ ५ ६ ७  
१०, २०, ३०, ४०, ५०, ६०, ७०  
८० ९० १० २० ३० ४० ५०  

```

public static void rotateby1(int[] arr){
    int temp = arr[0];
    int n = arr.length;

    for(int i=1; i<n; i++){
        arr[i - 1] = arr[i];
    }
    arr[n - 1] = temp;
}
    
```

$k = k \% n;$

```

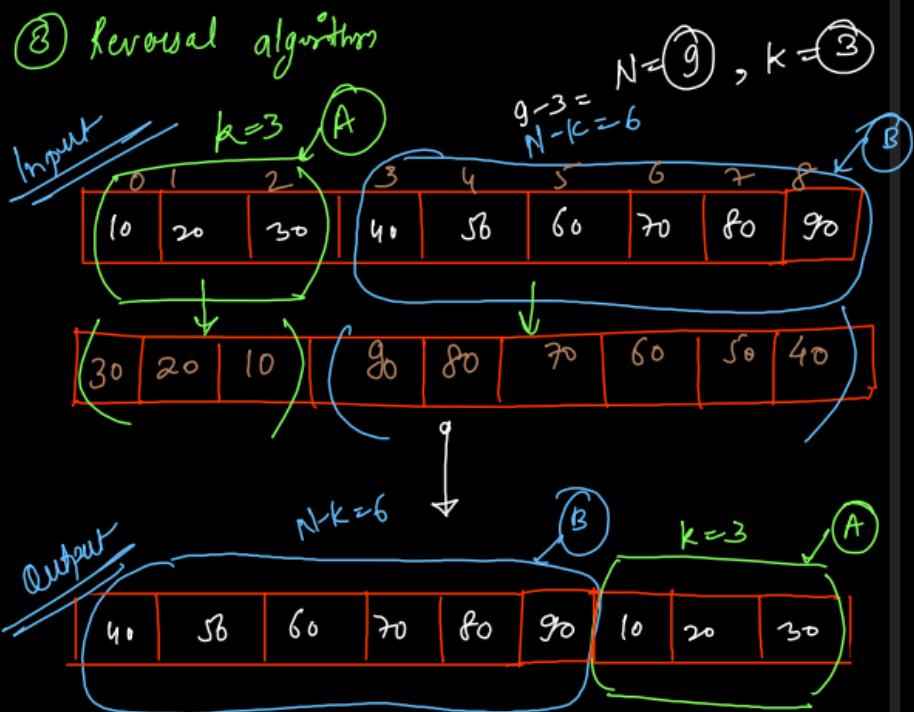
for(int i=0; i<k; i++){
    rotateby1(input);
}

for(int i=0; i<n; i++){
    System.out.print(input[i] + " ");
}
    
```

{ 10, 20, 30, 40, 50 }  
 ↓ rotateby1()  
 { 20, 30, 40, 50, 10 }

{ 30, 40, 50, 10, 20 }  
 ↓ rotateby1()

{ 40, 50, 10, 20, 30 }



#WHAT

① Reverse starting  $k$  elements → single loop +  $n-k$  elements

② Reverse last  $n-k$  elements → single loop +  $k$  elements

③ Reverse the entire array → single loop

Better in terms of time complexity

```

public static void reverse(int[] arr, int start, int end){
    while(start < end){
        int temp = arr[start];
        arr[start] = arr[end];
        arr[end] = temp;
        start++; end--;
    }
}

```

```

// 1. Reverse the starting k elements
reverse(input, 0, k - 1);
// 2. Reverse the ending n - k elements
reverse(input, k, n - 1);
// 3. Reverse the entire array
reverse(input, 0, n - 1);

for(int i=0; i<n; i++){
    System.out.print(input[i] + " ");
}

```



$$(A^T + B^T)^T = (B^T)^T + (A^T)^T = B + A$$

①  $(x+y)^T = y^T + x^T$

②  $(x^T)^T = x$

Activ

$$\text{target} = 16$$

Two sum  $\rightarrow$  sum of pair = Target

$$\{ 10, 17, 12, 9, 4, 7, 20, 1 \}$$

~~Brute force~~ Nested loops  $\rightarrow$  Outer loop  $\rightarrow$  1<sup>st</sup> & Inner loop  $\rightarrow$  2<sup>nd</sup> ele of pair

$$(10, 17) = 27$$

$$(10, 4) = 14$$

$$(17+12) \neq 16 \quad (12+9)$$

$$(10, 12) = 22$$

$$(10, 9) = 17$$

$$(17+9) \neq 16$$

$$(10, 8) = 19$$

$$(10, 20) = 30$$

$$(17+20) \neq 16$$

$$(10, 1) = 11$$

$$(17+1) \neq 16$$

Activ

$\{ 10, 17, 12, 9, 3, 7, 20, 1 \}$

target = 16

$\{ 1, 3, 7, 9, 10, 12, 17, 20 \}$

↑  
start    ↑  
start    end    ↑  
end    end    ↑  
end

$$(1+20) = \begin{cases} 21 > 16 \\ \downarrow \end{cases}$$

start ++ / end --  
↓  
sum ↑      ↓  
sum ↓

$$(1+17) = \begin{cases} 18 > 16 \\ \downarrow \end{cases}$$

$$\begin{aligned} (1+12) &= \begin{cases} 13 < 16 \\ \uparrow \end{cases} \\ (3+12) &= \begin{cases} 15 < 16 \\ \uparrow \end{cases} \end{aligned}$$

$$\begin{aligned} (7+12) &= \begin{cases} 19 > 16 \\ \downarrow \end{cases} \\ (7+10) &= \begin{cases} 17 > 16 \\ \downarrow \end{cases} \\ (7+9) &= 16 = 16 \end{aligned}$$

Activate

$\{ 10, 17, 12, 9, 3, 7, 20, 1 \}$

target = 16

$\{ 1, 3, 7, 9, 10, 12, 17, 20 \}$

↑  
start    ↑  
start    end    ↑  
end    end    ↑  
end

$$(1+20) = \begin{cases} 21 > 16 \\ \downarrow \end{cases}$$

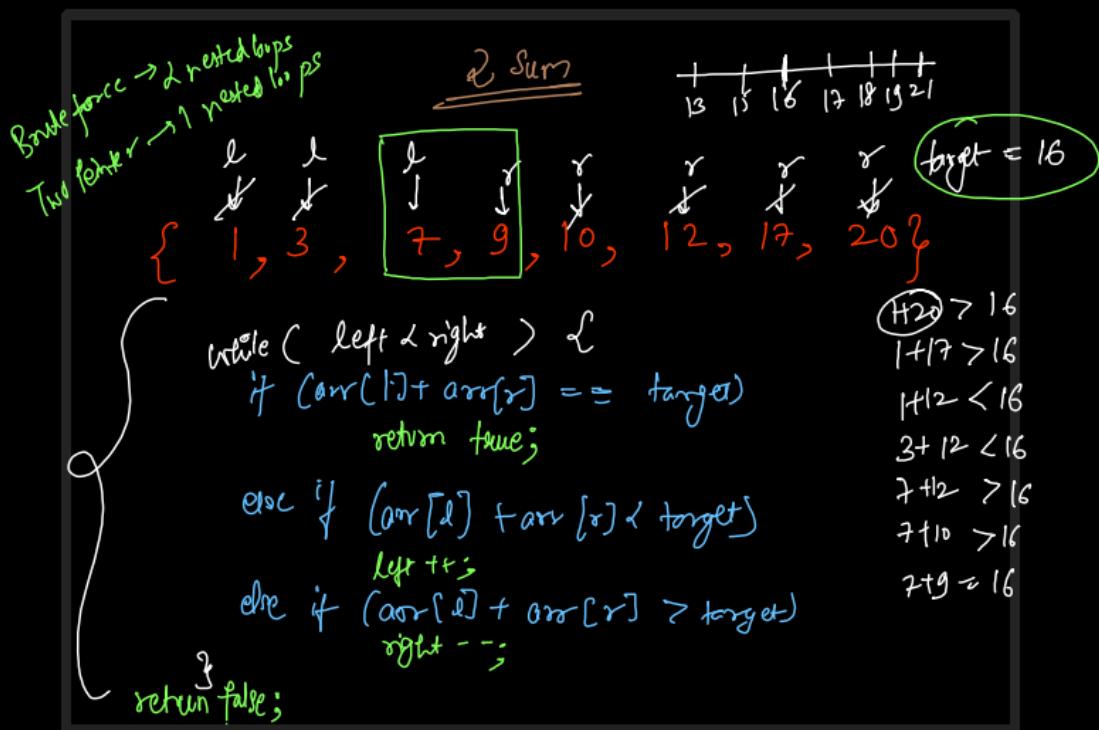
start ++ / end --  
↓  
sum ↑      ↓  
sum ↓

$$(1+17) = \begin{cases} 18 > 16 \\ \downarrow \end{cases}$$

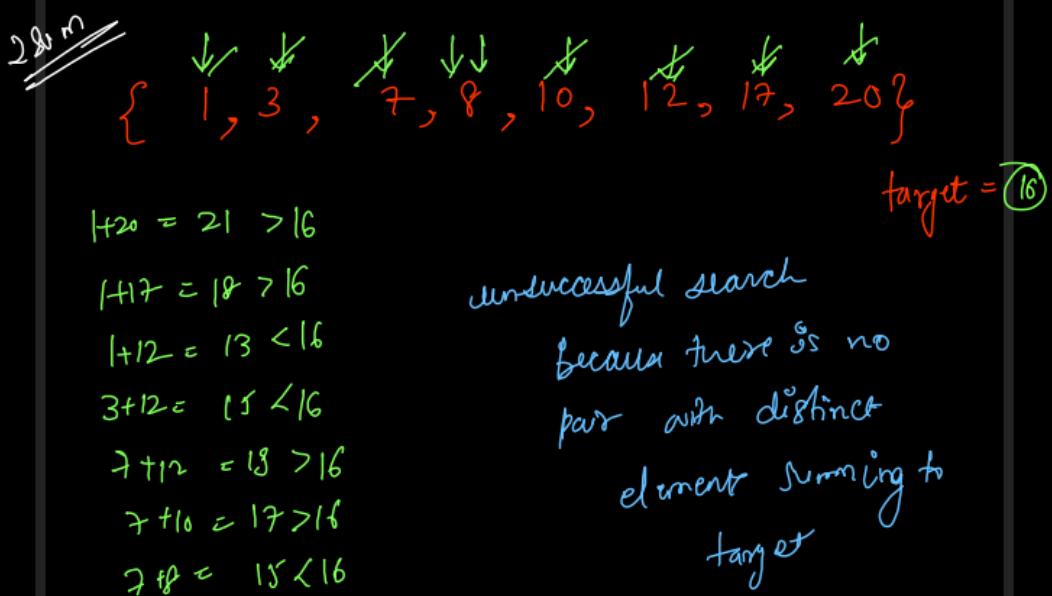
$$\begin{aligned} (1+12) &= \begin{cases} 13 < 16 \\ \uparrow \end{cases} \\ (3+12) &= \begin{cases} 15 < 16 \\ \uparrow \end{cases} \end{aligned}$$

$$\begin{aligned} (7+12) &= \begin{cases} 19 > 16 \\ \downarrow \end{cases} \\ (7+10) &= \begin{cases} 17 > 16 \\ \downarrow \end{cases} \\ (7+9) &= 16 = 16 \end{aligned}$$

Activate



Acti



$1+15=16$   
 $1+15=16$   
 $2+15=16$   
 $2+14=16$   
 $4+14=16$   
 $4+12=16$   
 $5+12=16$   
 $5+12=16$   
 $8+9=16$

2 sum → All the pairs equal to the target

$\{1, 2, 4, 5, 7, 8, 9, 12, 14, 15, 16\}$

while (left < right) {
 if ( $\text{arr}[l] + \text{arr}[r] == \text{target}$ )
  $\text{System.out.println}(\text{arr}[l] + " " + \text{arr}[r]);$ 
 left++;
 else if ( $\text{arr}[l] + \text{arr}[r] < \text{target}$ )
 left++;
 else if ( $\text{arr}[l] + \text{arr}[r] > \text{target}$ )
 right--;
 }

target =  $\boxed{16}$

$\cancel{(1, 15)}$     $\cancel{(4, 12)}$   
 $\cancel{(2, 14)}$     $\cancel{(7, 9)}$

Act

Triplet with target = 30

$\boxed{3 \text{ sum}} \rightarrow$  point true or false

$\{1, 3, 4, 7, 8, 10, 12, 14, 17, 18, 19\}$

first no + pair with target =  $\boxed{2^3}$

first no + pair with target =  $\boxed{2^3}$

$\boxed{3}$     $\text{arr}[i] + \text{arr}[j] + \text{arr}[k] = 30$

$\text{arr}[i] + \text{arr}[j] + \text{arr}[k] == \text{target}$

Brute force?  $\rightarrow$  3 nested loops (most basic approach)

Two pointer Technique  $\rightarrow$  2 nested loops (more optimized)

2 sum  $\rightarrow$  1 loop

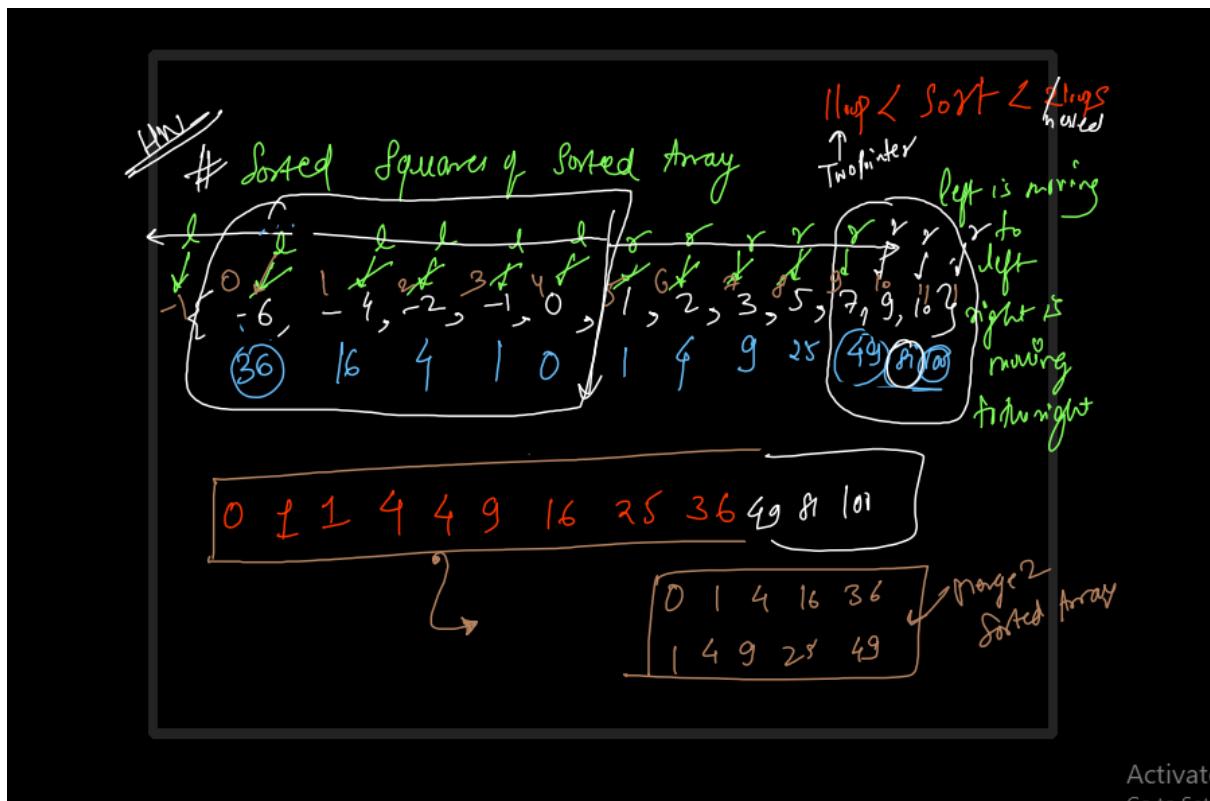
3 sum  $\rightarrow$  2 loops

4 sum  $\rightarrow$  3 loops

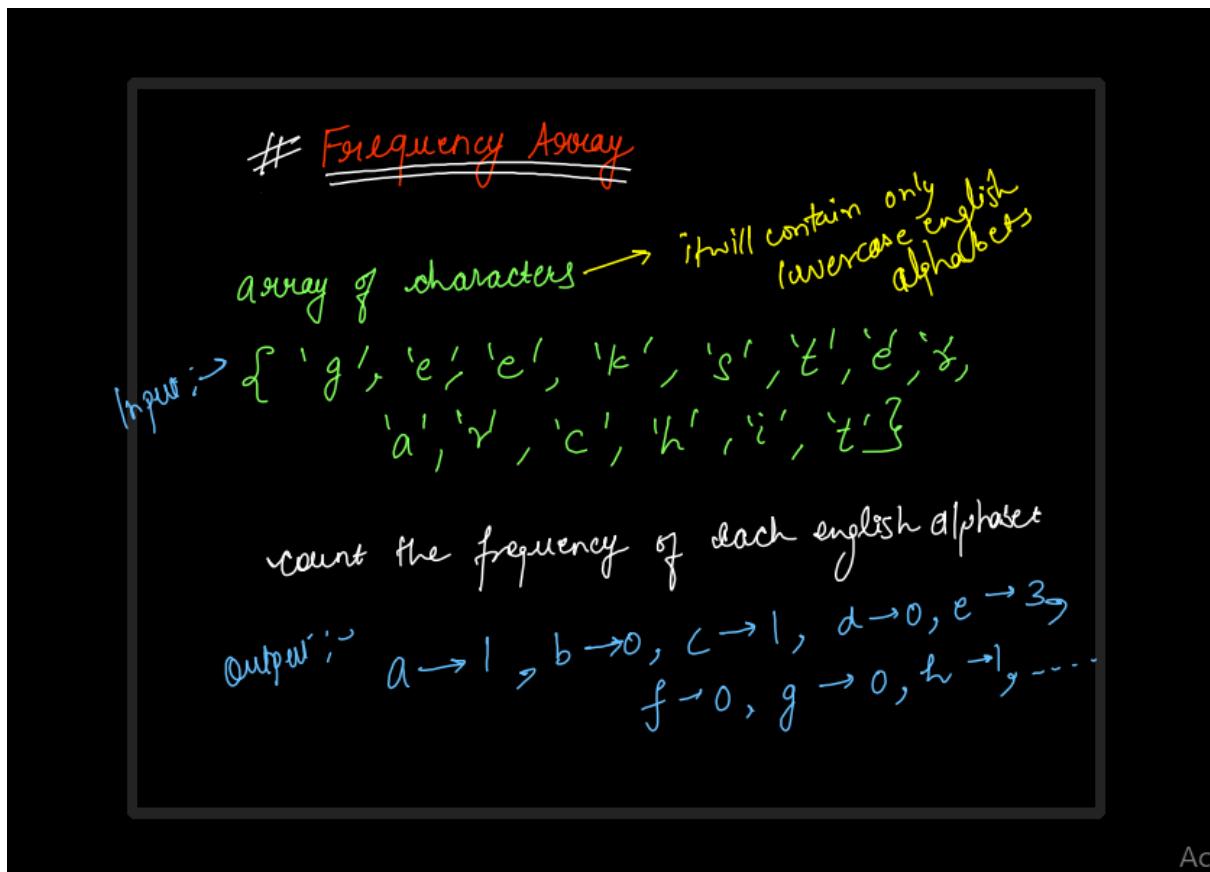
triplet( $i, j, k$ )    $i \neq j \neq k$

$\text{if } i \rightarrow (10, 19)$   
 $\text{if } j \rightarrow (12, 17)$   
 $\text{if } k \rightarrow (8, 15)$   
 $\text{if } i \rightarrow (10, 17)$

Act



Activate  
Go to Set



Ac

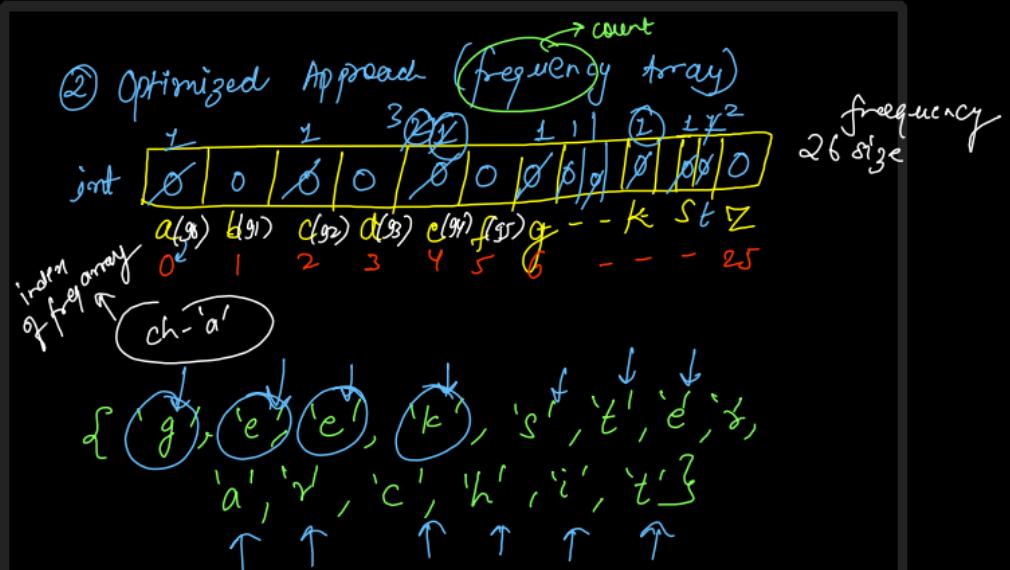
```

// Brute Force
// Outer Loop: Character
for(char i='a'; i<='z'; i++){
    // Inner Loop: Array
    int count = 0;
    for(int j=0; j<n; j++){
        if(arr[j] == i){
            count++;
        }
    }
    System.out.println(i + " -> " + count);
}

```

Amit

$26$   
 $n$   
 $\rightarrow$  Comparisons or  
 $\rightarrow$  operations  
 $\rightarrow$  Tc  
 $\rightarrow$  or



```

// Optimized Approach
int[] freq = new int[26];
// Char 'a' frequency will be stored in 0th index
// Char 'b' frequency will be stored in 1st index
// Char 'c' frequency will be stored in 2nd index
// Char 'z' frequency will be stored in 25th index

// Loop will run for N iterations
for(int i=0; i<n; i++){
    int index = arr[i] - 'a';
    freq[index]++;
}

// Loop will run for 26 iterations
for(int i=0; i<26; i++){
    System.out.print(freq[i] + " ");
}

```

$\sum O(N)$

$\sum O(26)$

$O(N + 26)$

# These are not nested loops

Q2 There are  $N$  students. Each student have got marks from 0 to 100.

You have to count how many students got

$0$	$A+$	$A$	$B+$	$B$	$C+$	$C$	$D+$	$D$	$F$
$\geq 90$	$\geq 80$	$\geq 70$	$\geq 60$	$\geq 50$	$\geq 40$	$\geq 30$	$\geq 20$	$\geq 10$	
$< 90$	$< 80$	$< 70$	$< 60$	$< 50$	$< 40$	$< 30$	$< 20$	$< 10$	

{ 10, 20, 40, 5, 92, 96, 33, 44, 55, 60, 88 }

count of 0 = 2, count of A+ = 1, count of A = 0, --

Activ

```

// Brute Force
// Outer Loop: Pick a Grade
for(int grade=90; grade>=0; grade = grade-10){
    // Count Students in that Grade
    int count = 0;
    for(int i=0; i<n; i++){
        if(marks[i] >= grade && marks[i] < grade + 10){
            count++;
        }
    }
    System.out.println(" >= " + grade + " -> " + count);
}

```

$O(10)$   
 $\times$   
 $O(n)$

$O(10 * n)$   
 nested  
 generally

```

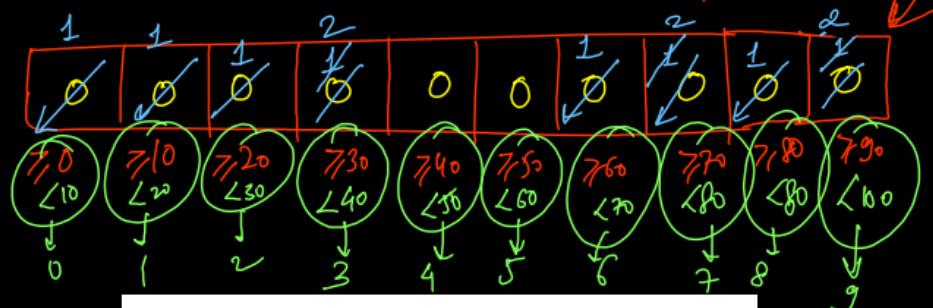
Finished in 125 ms.
>= 90 -> 2
>= 80 -> 1
>= 70 -> 2
>= 60 -> 1
>= 50 -> 0
>= 40 -> 0
>= 30 -> 2
>= 20 -> 1
>= 10 -> 1
>= 0 -> 1

stdin [ ]
12
64 20 34 92 97 88 73 75 0 33 10 100

```

# Approach 2: Frequency Array

types of  
grades



11

64 20 34 92 97 88 73 75 0 33 10 ~~100~~

64/10  
 20/10  
 34/10  
 92/10  
 97/10  
 88/10  
 73/10  
 75/10  
 0/10  
 33/10  
 10/10

=6    =2    =3    =9    =9

```

int[] freq = new int[10];

// Optimized Approach
for(int i=0; i<n; i++){
    int index = marks[i] / 10;
    freq[index]++;
}

for(int i=0; i<10; i++){
    System.out.print(freq[i] + " ");
}

```

1	0	0	8
1	0	2	9
1	0	2	
2	0	3	
0	4		
0	5		
1	6		
2	7		

12 ↓ 64 20 34 92 97 88 73 75 0 33 10 100



Array
sum of all ranges
Subarray  
 $\{l \leq r\}$

Array:  $\{ 10, 12, 8, 16, 2 \}$

$[0,0] = 10 \checkmark$	$[1,1] = 12 \checkmark$	$[3,3] = 16$
$[0,1] = 10 + 12 = 22 \checkmark$	$[1,2] = 12 + 8 = 20$	$[3,4] = 16 + 2 = 18$
$[0,2] = 10 + 12 + 8 = 30$	$[1,3] = 12 + 8 + 16 = 36 \checkmark$	$[4,4] = 2$
$[0,3] = 10 + 12 + 8 + 16 = 46$	$[1,4] = 12 + 8 + 16 + 2 = 38 \checkmark$	$[2,2] = 8$
$[0,4] = 10 + 12 + 8 + 16 + 2 = 48$	$[2,3] = 8 + 16 = 24$	$[3,4] = 8 + 16 + 2 = 26$

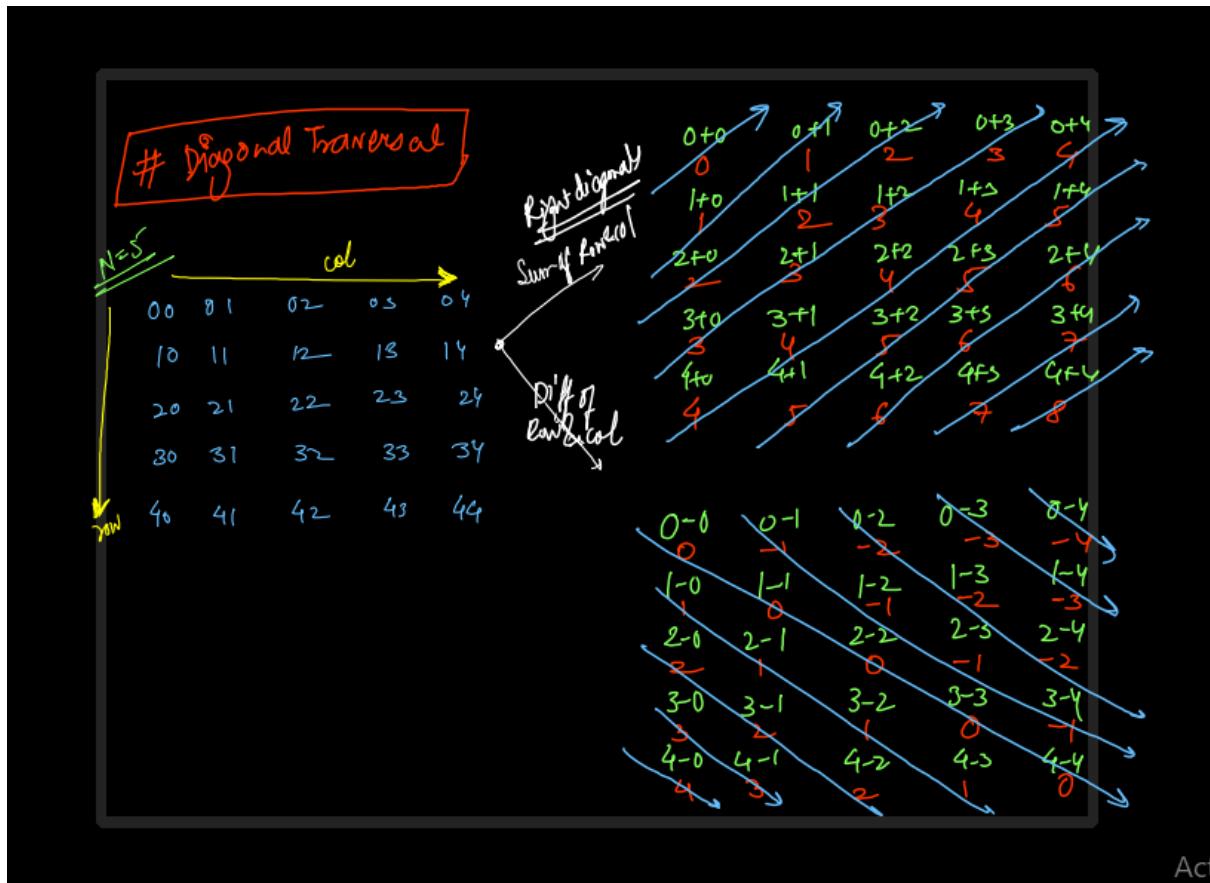
Active

Soft 01

```
// Concept: Prefix Sum Array
int n = scn.nextInt();
int[] arr = new int[n];
for(int i=0; i<n; i++){
    arr[i] = scn.nextInt();
}

for(int l=0; l<n; l++){
    int sum = 0;
    for(int r=l; r<n; r++){
        sum += arr[r];
        System.out.println("[" + l + ", " + r + "] = " + sum);
    }
}
```

elbowe func  
↓  
sum of all  
the ranges

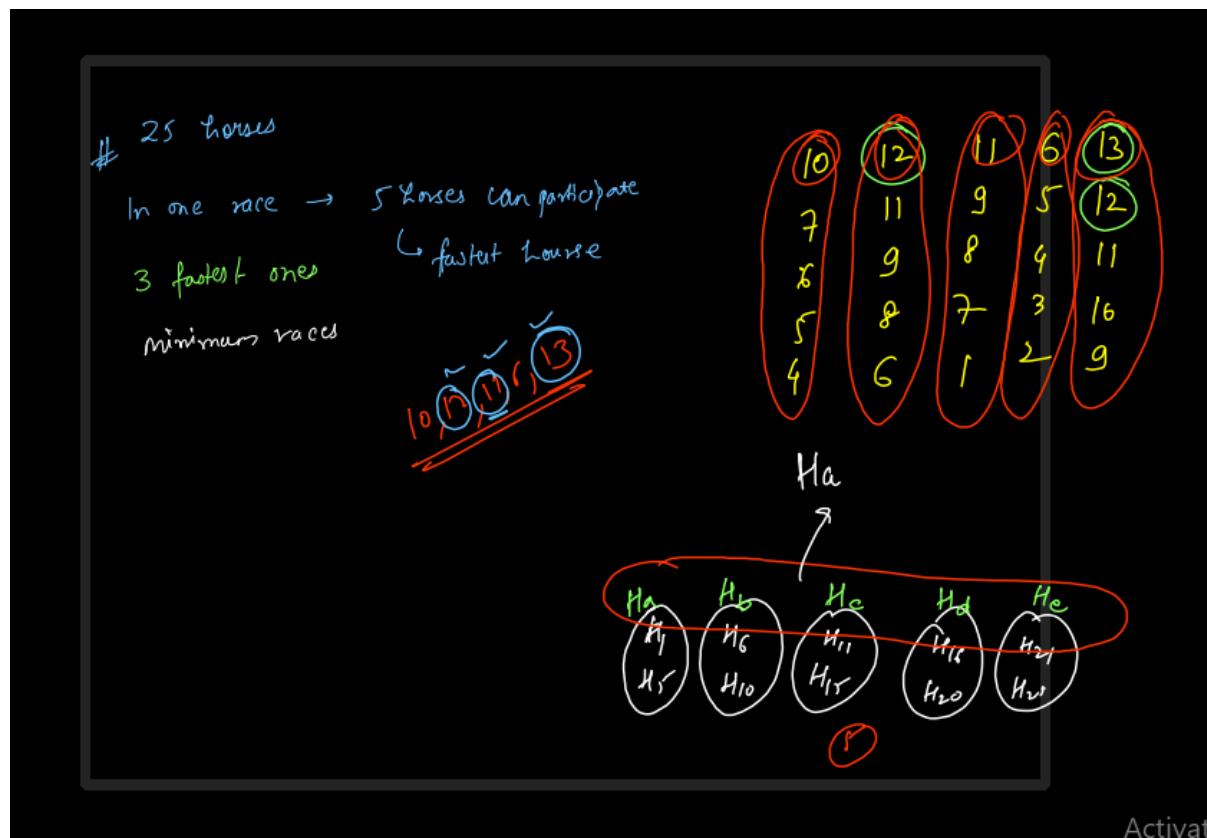
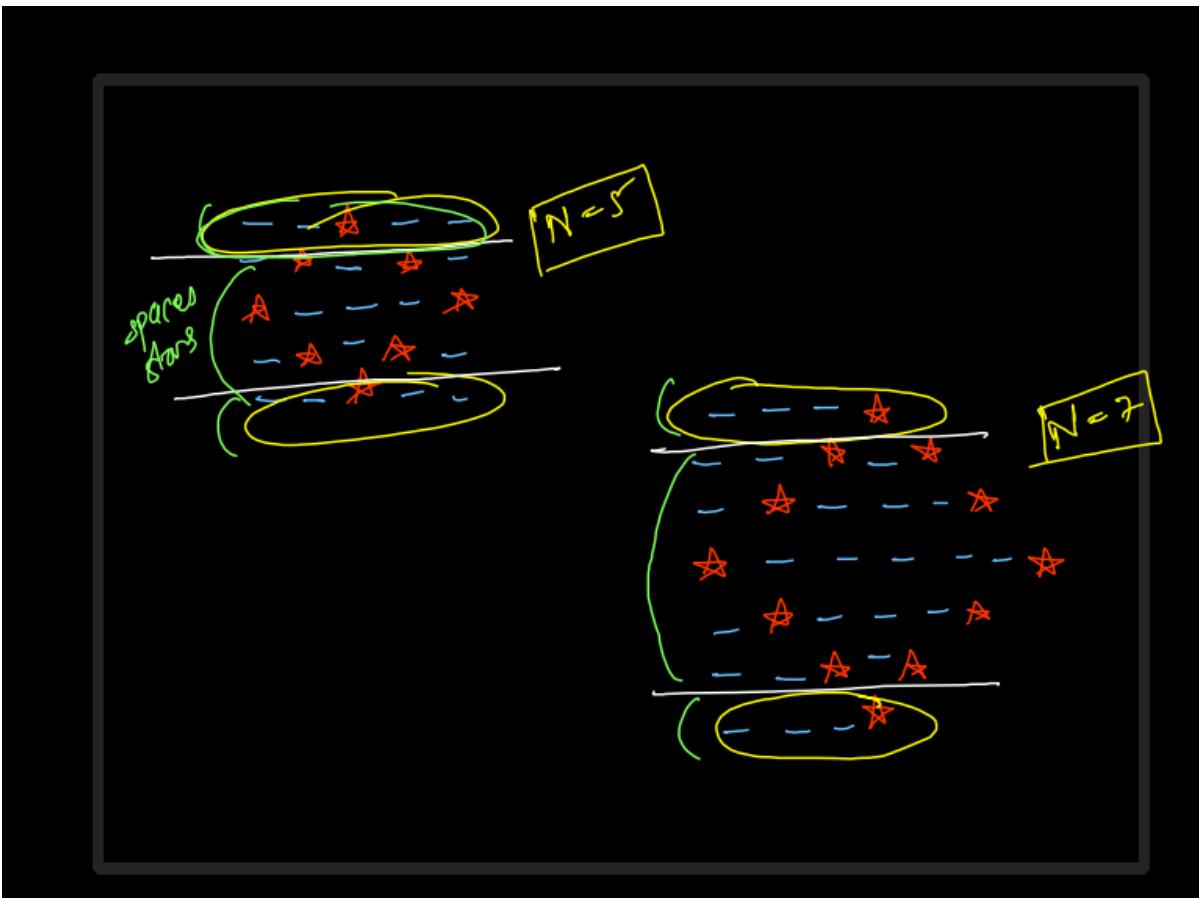


Act

```
// Sum of Row & Col Will Give Equal Elements on Right Diagonals
for(int row=0; row<n; row++){
    for(int col=0; col<n; col++){
        System.out.print(row + col + " ");
    }
    System.out.println();
}

System.out.println();

// Difference of Row & Col Will Give Equal Elements on Left Diagonals
for(int row=0; row<n; row++){
    for(int col=0; col<n; col++){
        System.out.print((row - col) + " ");
    }
    System.out.println();
}
```



Target sum pair (2Sum) → Closest Target

closest  $\Rightarrow$  ~~50~~ ~~52~~ ~~55~~ ~~53~~  
target  $\Rightarrow$  ~~54~~

10, 22, 25, 28, 30, 40  
~~↑~~ ~~↑~~ ↑ ↑ ↑ ↑ ↑ ↑

$$\begin{aligned} |5| &= 5 \\ |-3| &= 3 \\ |+\infty| &= \infty \\ |-\infty| &= -\infty \end{aligned}$$

integer

$$\uparrow 10+40 < 54$$

$$22+40 > 54$$

$$22+30 = 52 < 54$$

$$\downarrow 25+30 = 55 > 54$$

$$25+28 = 53 < 54$$

## Prefix Sum Approach

# sum of All the Subarrays(Ranges)

```
// Concept: Prefix Sum Array
int n = scn.nextInt();
int[] arr = new int[n];
for(int i=0; i<n; i++){
    arr[i] = scn.nextInt();
}

for(int l=0; l<n; l++){
    int sum = 0;
    for(int r=l; r<n; r++){
        sum += arr[r];
        System.out.println("[" + l + "," + r + "] = " + sum);
    }
}
```

N=9

Ex { 10, 8, 12, 15, 5, 7, 13, 20, 3 }

Ques  $\sum_{L \leq R} [L, R] = arr[L] + arr[L+1] + arr[L+2] + \dots + arr[R]$

Ex  $[0, 8] = arr[0] + arr[1] + arr[2] + \dots + arr[8]$   
 $= 10 + 8 + 12 + 15 + \dots + 3 = -$

Ex  $[0, 5] = arr[0] + arr[1] + arr[2] + arr[3] + arr[4] + arr[5]$   
 $= 10 + 8 + 12 + 15 + 5 + 7 = -$

Ex  $[6, 8] = arr[6] + arr[7] + arr[8] + 13 + 20 + 3 = 36$

Ex  $[2, 6] = arr[2] + arr[3] + arr[4] + arr[5] + arr[6]$   
 $= 12 + 15 + 5 + 7 + 13 = -$

Ex  $[5, 3] = 0$     Ex  $[5, 5] = arr[5] = 7$

```

public static void main(String[] args) {
    // Prefix Sum

    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for(int i=0; i<n; i++){
        arr[i] = scn.nextInt();
    }

    int l = scn.nextInt();
    int r = scn.nextInt();

    // Printing the Sum of Range [L, R] where both L, R are included, L <= R
    int sum = 0;
    for(int i=l; i<=r; i++){
        sum = sum + arr[i];
    }

    System.out.println(sum);
}

```

loop is working  
for  
 $O(R-L+1)$

$\approx O(N)$

single query

## MULTIPLE RANGE SUM QUERY

```

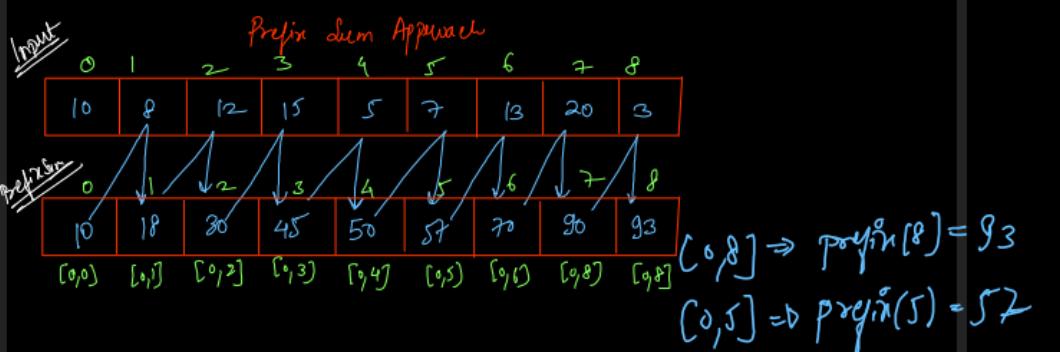
int queuem = ssm.nextInt();
// Multiple Range Sum Queries
for(int i=1; i<queuem; i++){
    int L = ssm.nextInt();
    int R = ssm.nextInt();
    // Printing the sum of range [L, R] where both L, R are included, L <= R
    int sum = 0;
    for(int i=L; i<=R; i++){
        sum = sum + arr[i];
    }
    System.out.println(sum);
}

```

$\leftarrow O(n \times m)$

$\leftarrow O(R-L+1)$

Total time  
 $O(Q \times n \times (R-L+1))$



$$\text{pref}[i] = \text{pref}[i-1] + \text{arr}[i]$$

```

int[] prefix = new int[n];
prefix[0] = arr[0];
for(int i=1; i<n; i++){
    // Sum of elements from 0th index to ith index
    // is sum of elements upto the previous index + current element
    prefix[i] = prefix[i - 1] + arr[i];
}

```

case ① Range  $[i:j] \Rightarrow 0$   
 $i > j$

eg  $[5,3] [8,6] [$   
 $\{0,8\} \Rightarrow \text{prefix}[8]$   
 $\{0,5\} \Rightarrow \text{prefix}[5]$

case ② Range  $[0:j] \Rightarrow \text{prefix}[j]$  eg  $\begin{cases} [0,8] \\ [0,5] \end{cases} \Rightarrow \text{prefix}[8]$   
 $\Rightarrow \text{prefix}[5]$

case ③ Range  $[i:j] \Rightarrow \text{prefix}[j] - \text{prefix}[i-1]$   
 $i > 0 \& i \leq j$

$\begin{cases} [2,5] = [0,5] - [0,1] \\ [3,8] = [0,8] - [0,2] \\ [1,4] = [0,4] - [0,0] \end{cases}$

```

int[] prefix = new int[n];
prefix[0] = arr[0];
for(int i=1; i<n; i++){
    // Sum of elements from 0th index to ith index
    // is sum of elements upto the previous index + current element
    prefix[i] = prefix[i - 1] + arr[i];
}
    
```

$\underbrace{\quad}_{\text{Precomputation}} \quad \underbrace{\text{for } O(N) \text{ queries}}_{\text{multiple queries}}$

```

int queries = scn.nextInt();
// Multiple Range Sum Queries

for(int t=1; t<=queries; t++){
    int l = scn.nextInt();
    int r = scn.nextInt();

    if(l > r){
        System.out.println(0);
    } else if(l == 0){
        System.out.println(prefix[r]);
    } else {
        System.out.println(prefix[r] - prefix[l - 1]);
    }
}
    
```

$\underbrace{\quad}_{\text{if } l > r \text{ eg } [5,3]}$   
 $\underbrace{\quad}_{\text{if } l == 0 \text{ eg } [0,5]}$   
 $\underbrace{\quad}_{\text{if } l < r \text{ eg } [2,5]}$

$\underbrace{\quad}_{O(\text{queries})}$

Altitude  
17:32

# Find the highest altitude [8:55]

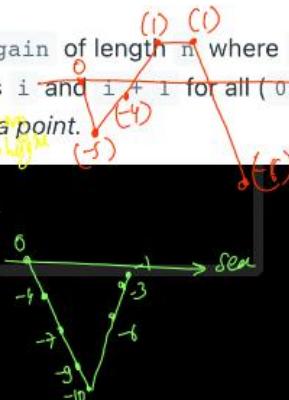
There is a biker going on a road trip. The road trip consists of  $n + 1$  points at different altitudes. The biker starts his trip on point 0 with altitude equal to 0.

You are given an integer array gain of length  $n$  where gain[i] is the net gain in altitude between points  $i$  and  $i + 1$  for all  $(0 \leq i < n)$ .

Return the highest altitude of a point.

height[i] = preHeight + gain[i].  
will be max height

[ -4, -3, -2, -1, 4, 3, 2 ]



Activate Win

```
class Solution {
    public int largestAltitude(int[] gain) {
        int height = 0;
        int maxHeight = 0; // It is Starting at altitude 0

        for(int i=0; i<gain.length; i++){
            height = height + gain[i];

            if(height > maxHeight) {
                maxHeight = height;
            }
        }

        return maxHeight;
    }
}
```

**724. Find Pivot Index**

Easy 3154 371 Add to List Share

Given an array of integers `nums`, calculate the **pivot index** of this array.

The **pivot index** is the index where the sum of all the numbers **strictly** to the left of the index is equal to the sum of all the numbers **strictly** to the index's right.

If the index is on the left edge of the array, then the left sum is `0` because there are no elements to the left. This also applies to the right edge of the array.

Return the **leftmost pivot index**. If no such index exists, return `-1`.

**Example 1:**

```
Input: nums = [1,7,3,6,5,6]
Output: 3
Explanation:
The pivot index is 3.
Left sum = nums[0] + nums[1] + nums[2] = 1 + 7 + 3 = 11
Right sum = nums[4] + nums[5] = 5 + 6 = 11
```

**Example 2:**

```
Input: nums = [1,2,3]
Output: -1
Explanation:
There is no index that satisfies the conditions in the problem statement.
```

```
class Solution {
    public int pivotIndex(int[] nums) {
        int[] pref = new int[nums.length];
        pref[0] = nums[0];
        for(int i=1; i<nums.length; i++){
            pref[i] = pref[i-1] + nums[i];
        }

        for(int i=0; i<nums.length; i++){
            int leftSum = (i == 0) ? 0 : pref[i-1];
            int rightSum = (i == nums.length - 1) ? 0 : (pref[nums.length - 1] - pref[i]);
            if(leftSum == rightSum) return i;
        }
        return -1;
    }
}
```

```

Scanner scn = new Scanner(System.in);
int row = scn.nextInt();
int col = scn.nextInt();
int[][] mat = new int[row][col];
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        mat[i][j] = scn.nextInt();
    }
}

```

*Outer loop*

*Inner loop*

$\text{rows} = 3, \text{cols} = 5$

0	1	2	3	4
0	10	20	30	40
1	60	70	80	90
2	110	120	130	140
				150

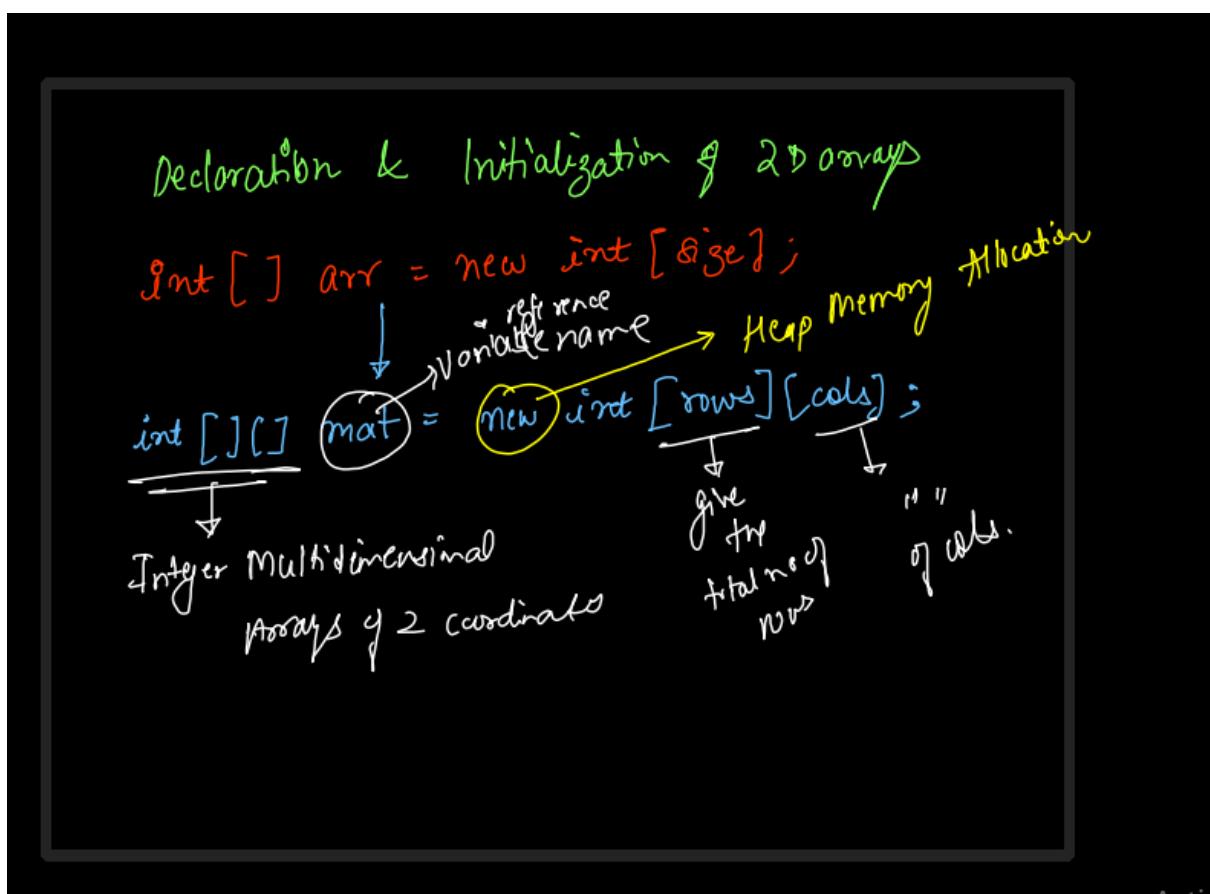
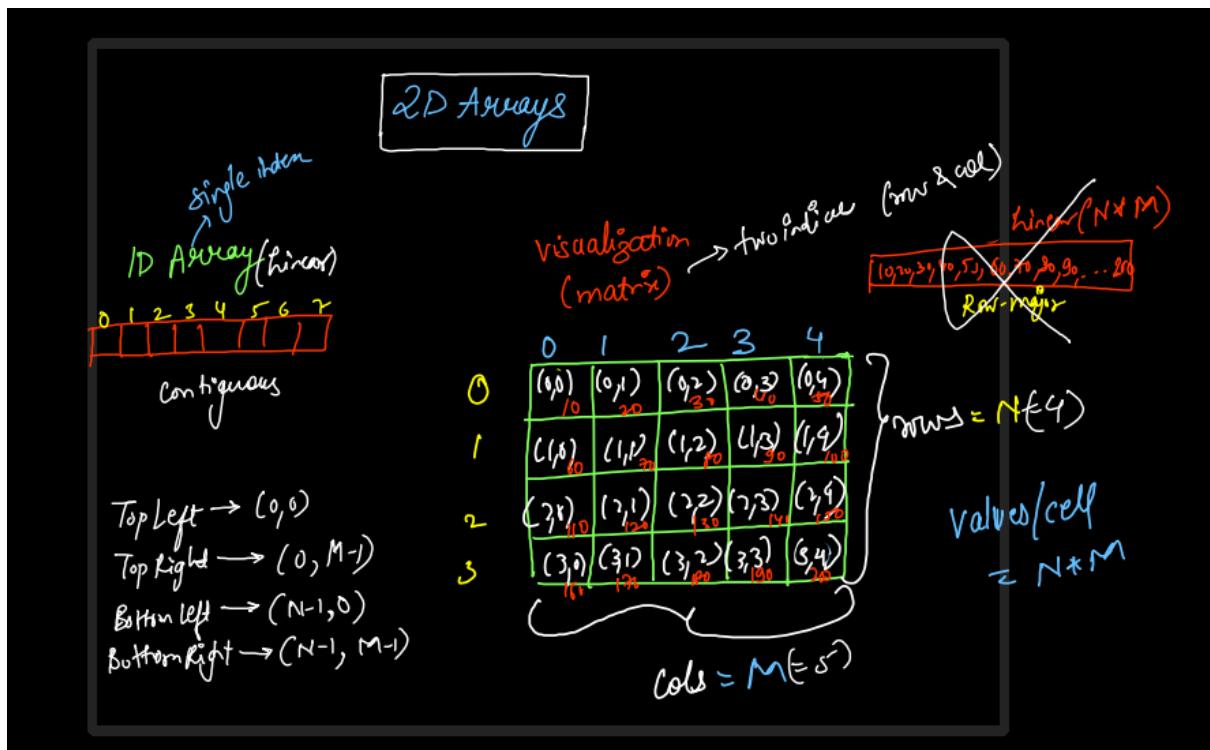
$\text{rows} = 3$

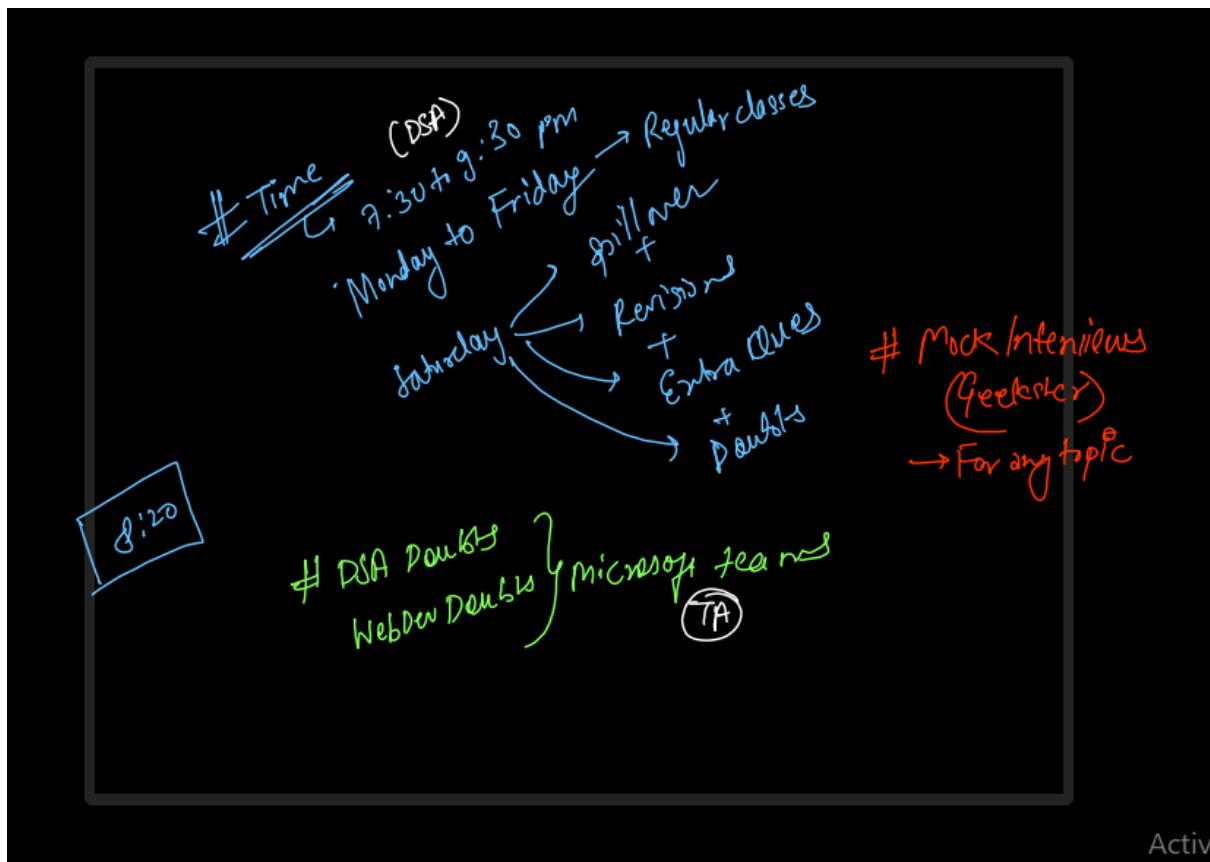
$\text{cols} = 5$

You have to input the elements of a matrix row by row

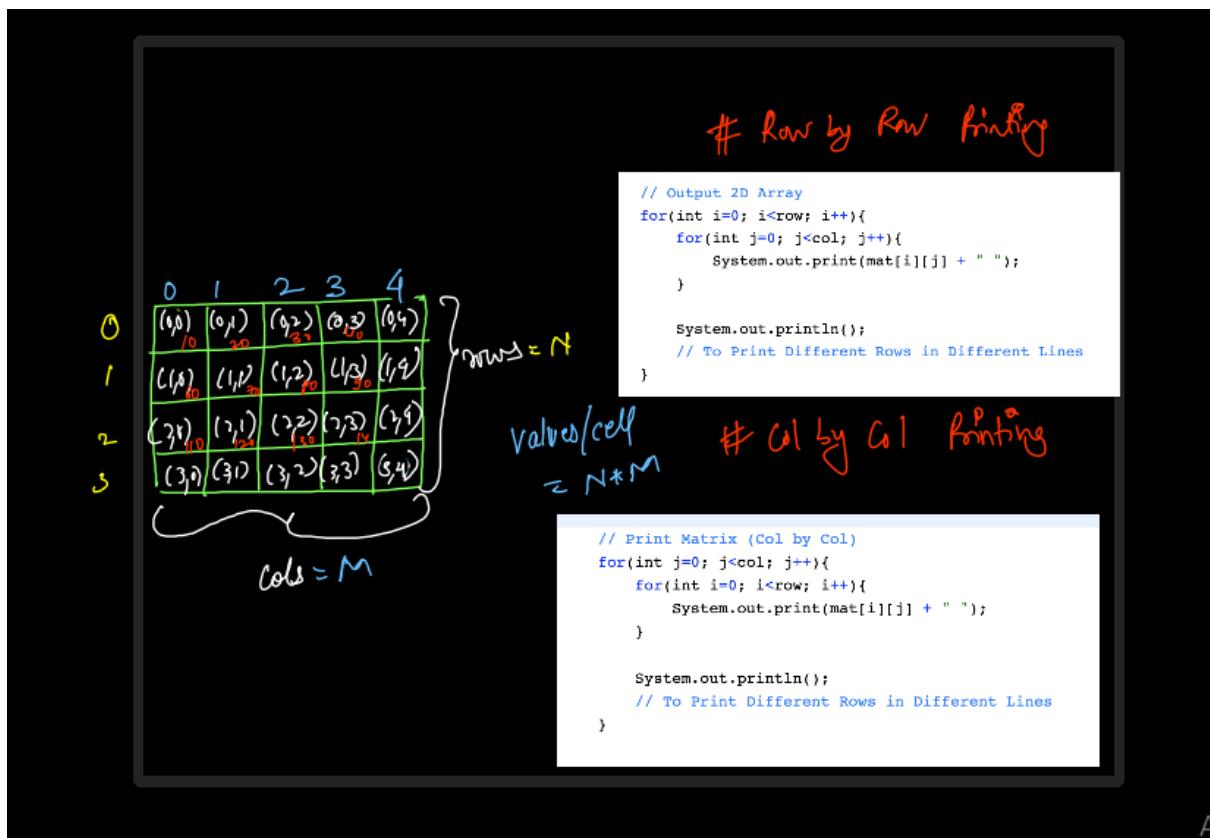
### # Applications (Real-life)

- ① String maps
- ② Image Processing (R, G, B)
  - ↳ pixels of images forms matrix
- ③ Video Processing
- ④ Board Games
  - ↳ Sudoku
  - ↳ Tic Tac Toe
  - ↳ Snakes & Ladders
- ⑤ Vectors





Activ



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Task 1: Print all elements sum

```
// Task 1: Sum of All Elements of Matrix
int sum = 0;
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        sum = sum + mat[i][j];
    }
}
```

```
System.out.println("Sum of All Elements : " + sum);
```

Task 2 : Print All Rows Sum

```
// Task 2: Sum of All Rows of Matrix
for(int i=0; i<row; i++){
    int rowSum = 0;
    for(int j=0; j<col; j++){
        rowSum = rowSum + mat[i][j];
    }

    // Inside the (Row) outer loop, outside the (Col) inner loop
    System.out.println("Sum of " + i + " th Row : " + rowSum);
}
```

Task 3: Print all Columns sum

4 rows 5 columns  
4x5

	0	1	2	3	4
0	(0,0) 10	(0,1) 20	(0,2) 30	(0,3) 40	(0,4) 50
1	(1,0) 10	(1,1) 20	(1,2) 30	(1,3) 40	(1,4) 50
2	(2,0) 10	(2,1) 20	(2,2) 30	(2,3) 40	(2,4) 50
3	(3,0) 10	(3,1) 20	(3,2) 30	(3,3) 40	(3,4) 50

Columns sum

① Row by matrix

Row by row

4x5

0	1	2	3	4	
0	(0,0) 10	(0,1) 20	(0,2) 30	(0,3) 40	(0,4) 50
1	(1,0) 10	(1,1) 20	(1,2) 30	(1,3) 40	(1,4) 50
2	(2,0) 10	(2,1) 20	(2,2) 30	(2,3) 40	(2,4) 50
3	(3,0) 10	(3,1) 20	(3,2) 30	(3,3) 40	(3,4) 50

② Write the col by col

4x5

0	1	2	3	4	
0	(0,0) 10	(0,1) 20	(0,2) 30	(0,3) 40	(0,4) 50
1	(1,0) 10	(1,1) 20	(1,2) 30	(1,3) 40	(1,4) 50
2	(2,0) 10	(2,1) 20	(2,2) 30	(2,3) 40	(2,4) 50
3	(3,0) 10	(3,1) 20	(3,2) 30	(3,3) 40	(3,4) 50

Activity

```

// Col by Col Reversal
for(int j=0; j<col; j++){
    // Reversing the ith Row
    int left = 0, right = row - 1;
    while(left < right){
        int temp = mat[left][j];
        mat[left][j] = mat[right][j];
        mat[right][j] = temp;
        left++; right--;
    }
}

```

```

160 170 180 190 200
110 120 130 140 150
60 70 80 90 100
10 20 30 40 50
stdin @
4 5
10 20 30 40 50
60 70 80 90 100
110 120 130 140 150
160 170 180 190 200

```

4  
Output N=4  
M=5



```

// Row by Row Reversal
for(int i=0; i<row; i++){
    // Reversing the ith Row
    int left = 0, right = col - 1;
    while(left < right){
        int temp = mat[i][left];
        mat[i][left] = mat[i][right];
        mat[i][right] = temp;
        left++; right--;
    }
}

```

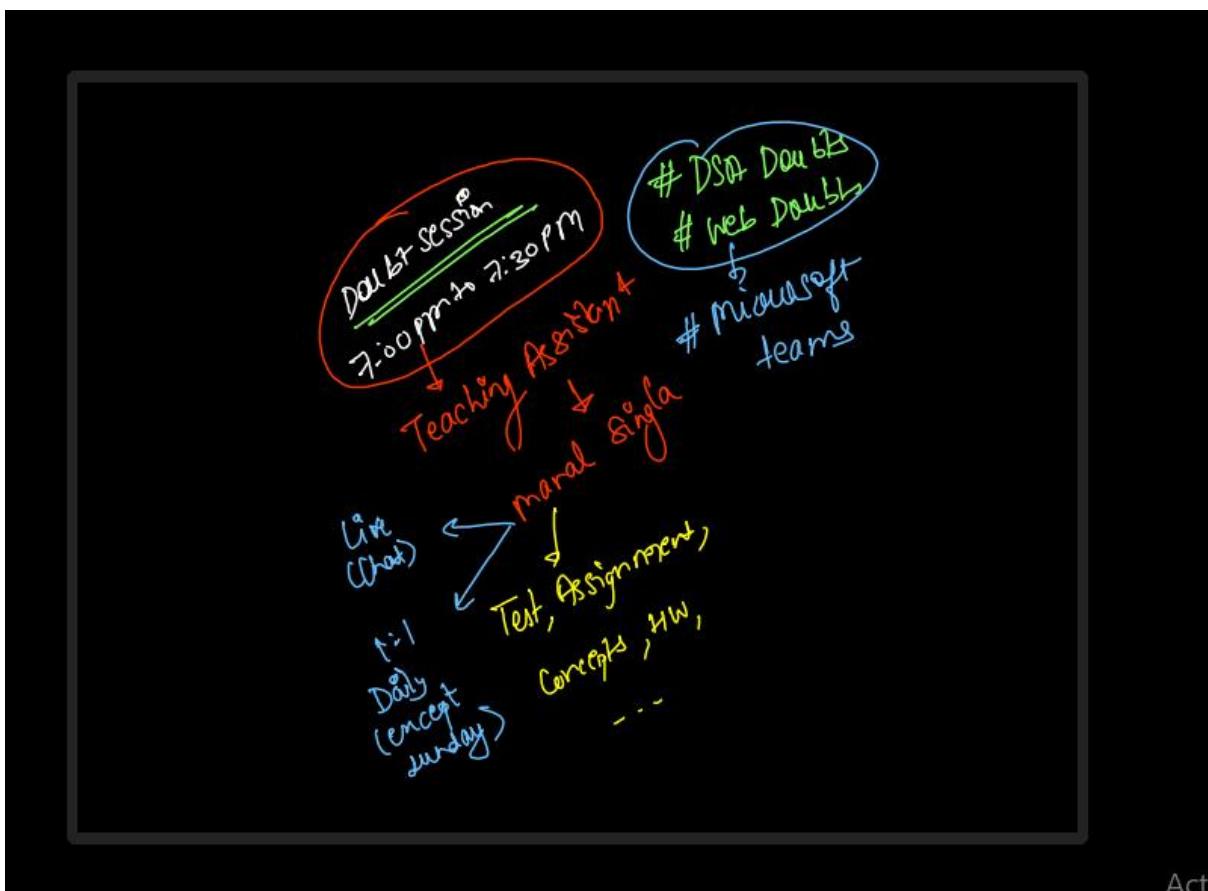
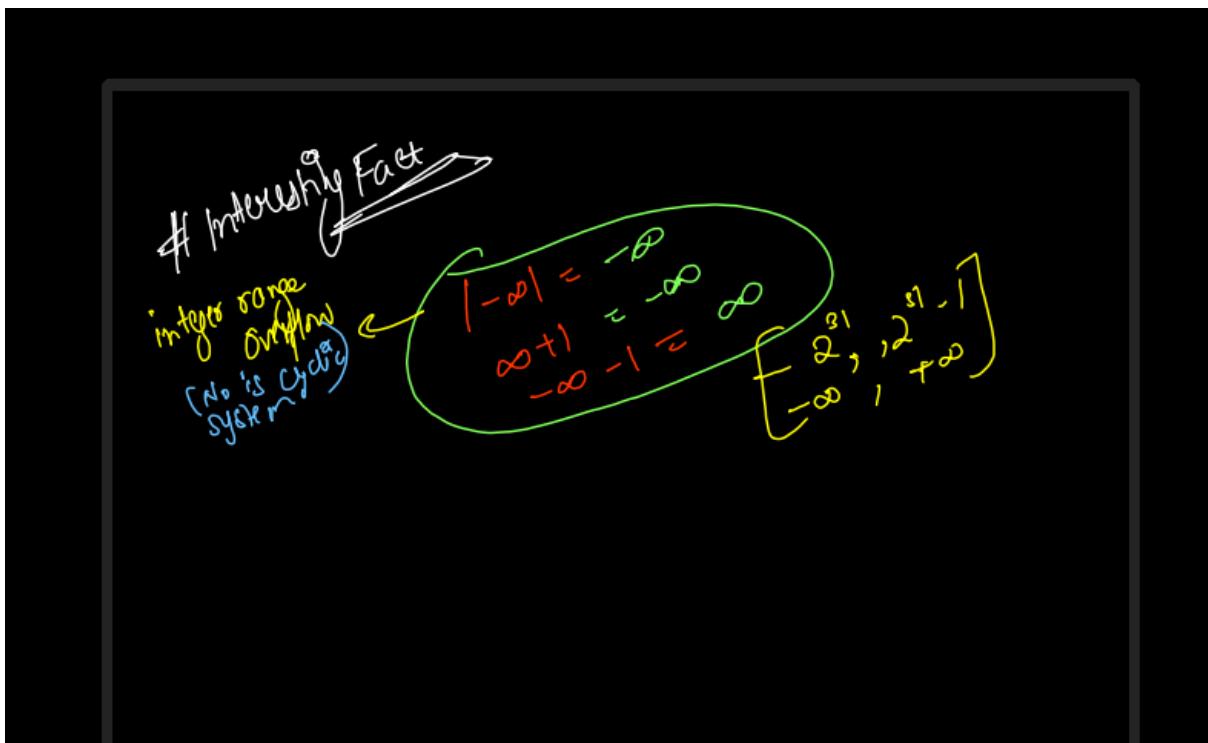
Finished in 1<sup>N=4</sup> ms

```

10 20 30 40 50
60 70 80 90 100
110 120 130 140 150
160 170 180 190 200

50 40 30 20 10
100 90 80 70 60
150 140 130 120 110
200 190 180 170 160

```



Act

2D Array ( Rotate Image by  $180^\circ$ )  
Reverse both by row & cols

$\left[ \begin{matrix} C \\ R \end{matrix} \right]$

	0	1	2	3	4
0	(0,0)	(0,1)	(0,2)	(0,3)	(0,4)
1	(1,0)	(1,1)	(1,2)	(1,3)	(1,4)
2	(2,0)	(2,1)	(2,2)	(2,3)	(2,4)
3	(3,0)	(3,1)	(3,2)	(3,3)	(3,4)

row by Row

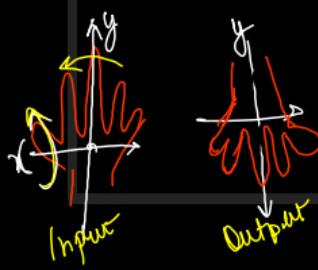
①

	0	1	2	3	4
0	(0,0)	(0,1)	(0,2)	(0,3)	(0,4)
1	(1,0)	(1,1)	(1,2)	(1,3)	(1,4)
2	(2,0)	(2,1)	(2,2)	(2,3)	(2,4)
3	(3,0)	(3,1)	(3,2)	(3,3)	(3,4)

$\left[ \begin{matrix} C \\ R \end{matrix} \right]$   
Horizontally flipped

	0	1	2	3	4
0	(0,0)	(0,1)	(0,2)	(0,3)	(0,4)
1	(1,0)	(1,1)	(1,2)	(1,3)	(1,4)
2	(2,0)	(2,1)	(2,2)	(2,3)	(2,4)
3	(3,0)	(3,1)	(3,2)	(3,3)	(3,4)

$\left[ \begin{matrix} C \\ R \end{matrix} \right]$   
Vertical Flipped



Activity  
Go to

This syntax can be used if matrix is not empty

```

int row = mat.length, col = mat[0].length;
    
```

**(HR)**

```

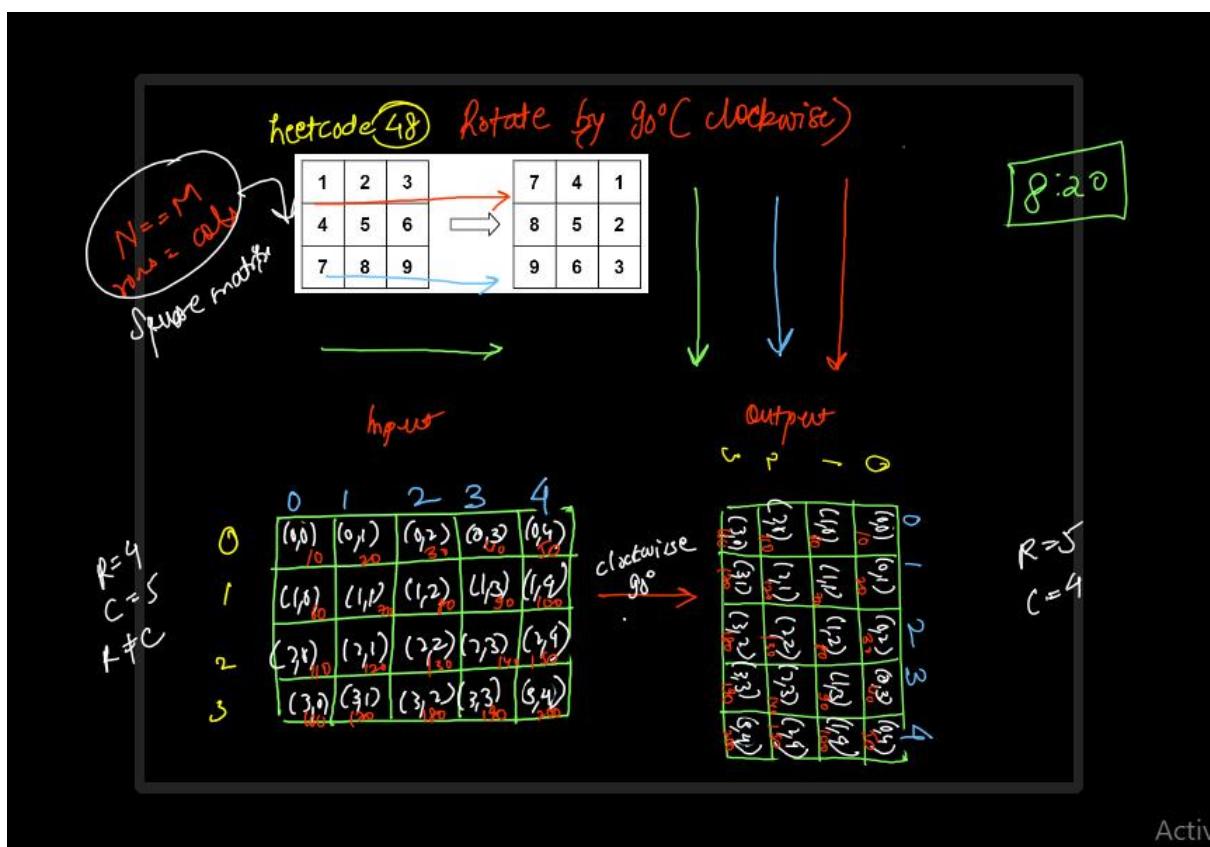
// Step 1: Row by Row Reversal
for(int i=0; i<row; i++){
    int left = 0, right = col - 1;
    while(left < right){
        int temp = mat[i][left];
        mat[i][left] = mat[i][right];
        mat[i][right] = temp;
        left++; right--;
    }
}
    
```

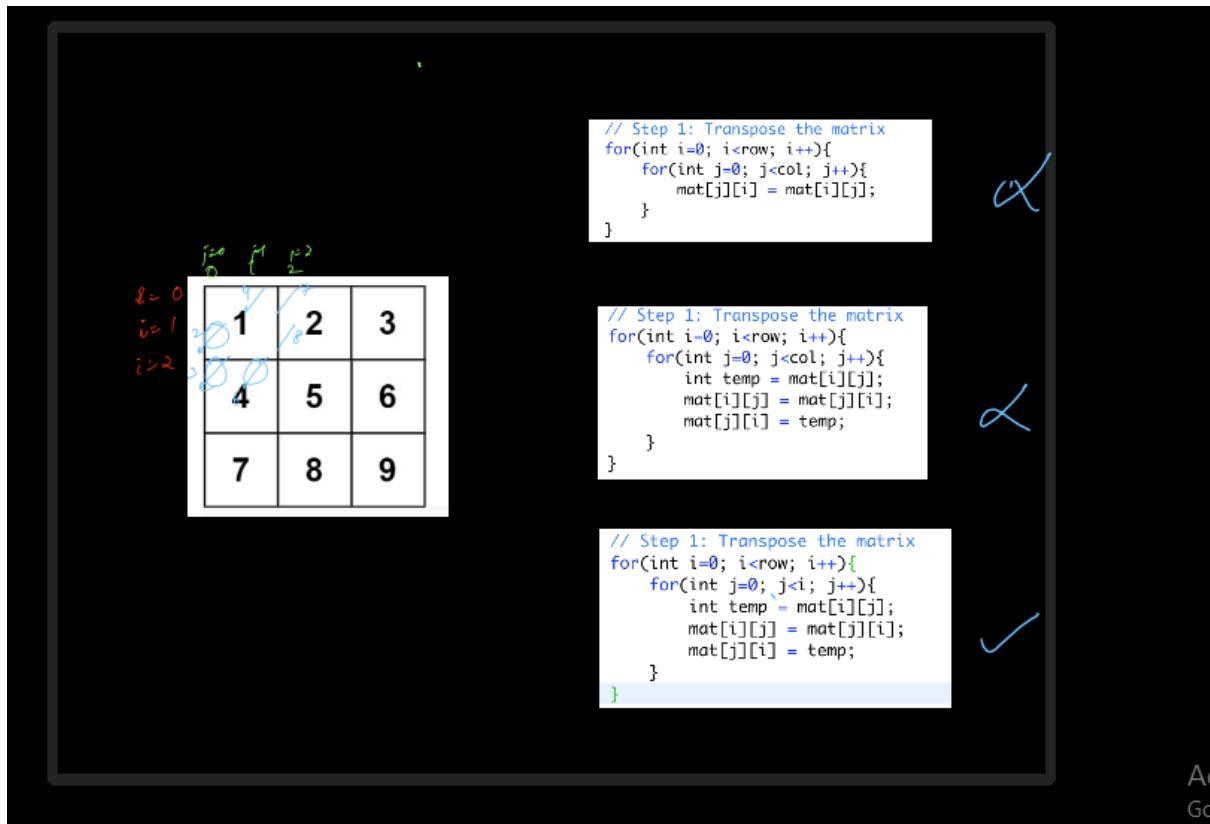
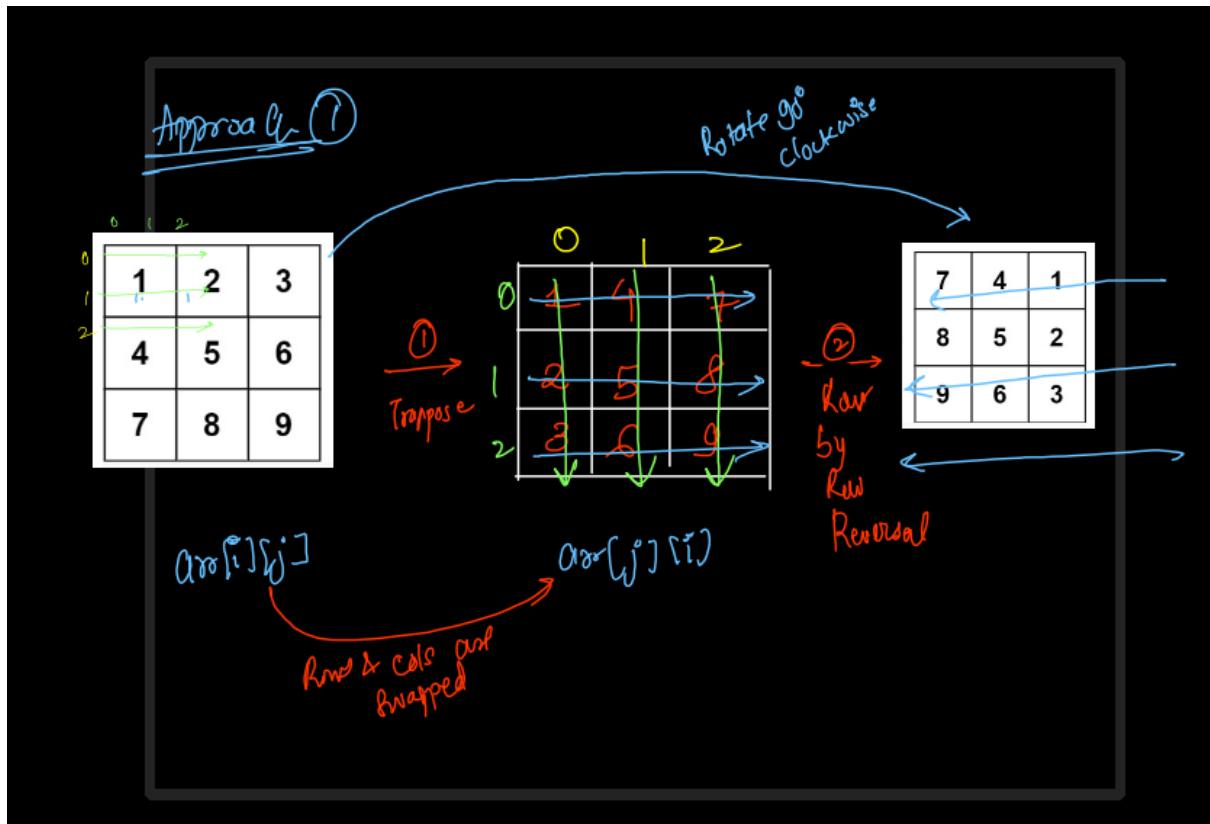
**(VR)**

```

// Step 2: Column by Column Reversal
for(int j=0; j<col; j++){
    int left = 0, right = row - 1;
    while(left < right){
        int temp = mat[left][j];
        mat[left][j] = mat[right][j];
        mat[right][j] = temp;
        left++; right--;
    }
}
    
```

= **90°** Rotation

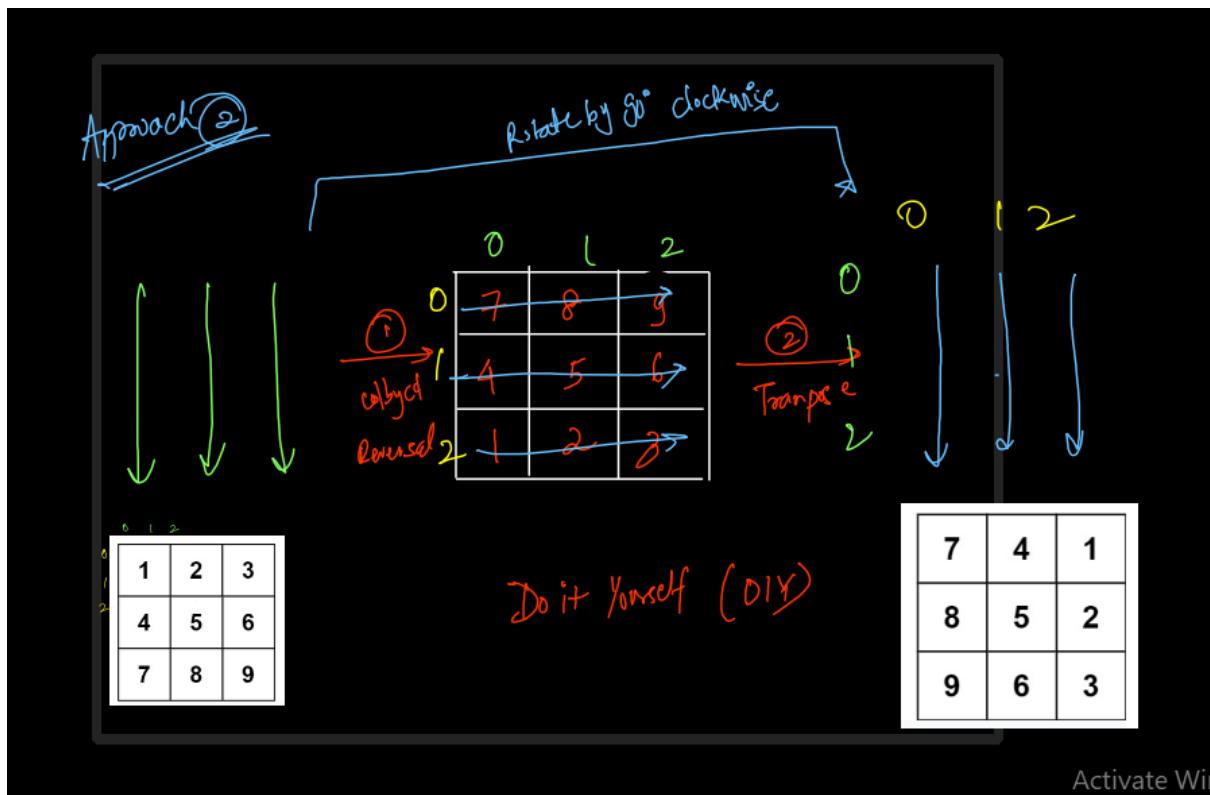




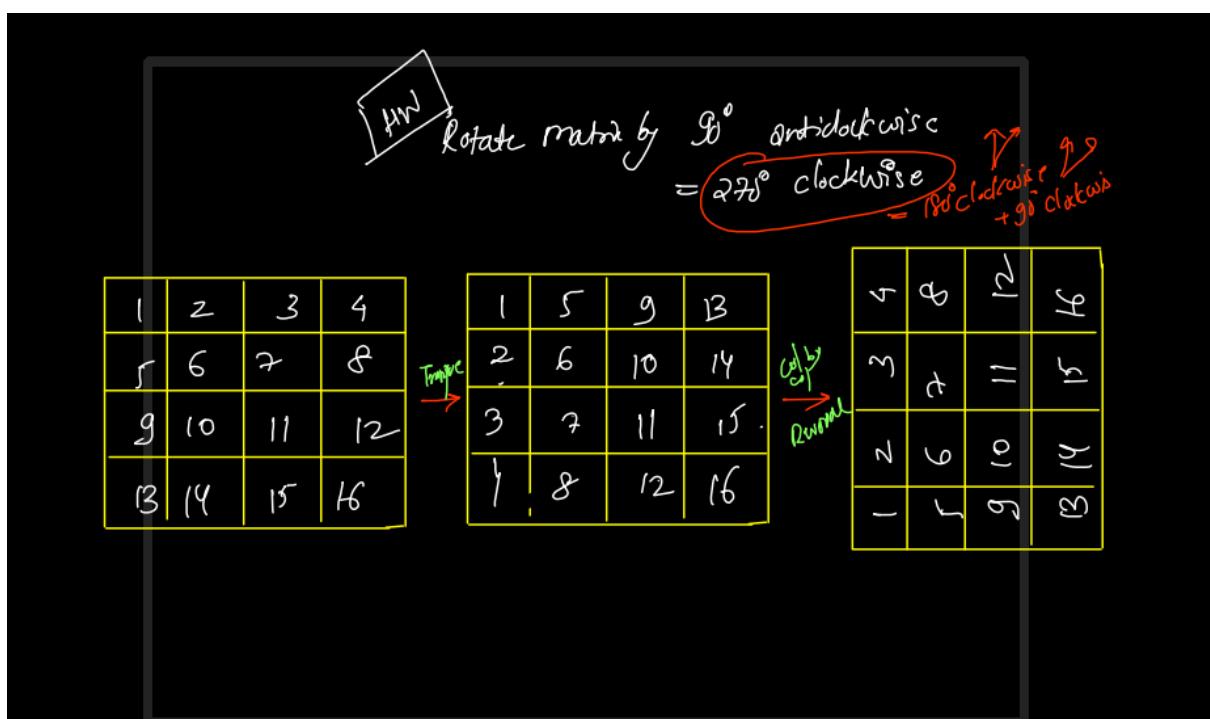
```
class Solution {
    public void rotate(int[][] mat) {
        int row = mat.length, col = mat[0].length;
        // Step 1: Transpose the matrix
        for(int i=0; i<row; i++){
            for(int j=0; j<i; j++){
                int temp = mat[i][j];
                mat[i][j] = mat[j][i];
                mat[j][i] = temp;
            }
        }

        // Step 2: Row by Row Reversal
        for(int i=0; i<row; i++){
            int left = 0, right = col - 1;
            while(left < right){
                int temp = mat[i][left];
                mat[i][left] = mat[i][right];
                mat[i][right] = temp;

                left++; right--;
            }
        }
    }
}
```



Activate Wi-Fi



```

// Check if sum of each row is same
int firstRowSum = 0;

for(int i=0; i<row; i++){
    int rowSum = 0;
    for(int j=0; j<col; j++){
        rowSum = rowSum + mat[i][j];
    }

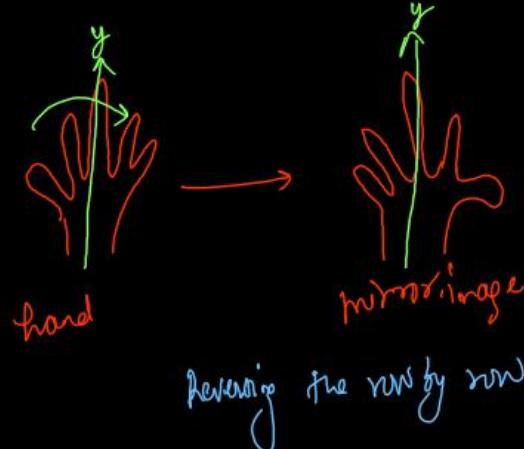
    if(i == 0){
        firstRowSum = rowSum;
    } else {
        if(rowSum != firstRowSum)
            return false;
    }
}

```

return true;

firstRowSum = 10

i:0	1	2	3	4	$\Rightarrow$	rowSum 10
i:1	4	3	2	1	$\Rightarrow$	rowSum 10
i:2	1	1	2	3	$\Rightarrow$	rowSum 7
i:3	3	4	1	2	$\Rightarrow$	rowSum 10

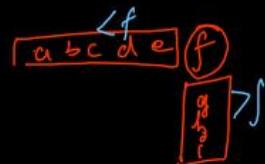
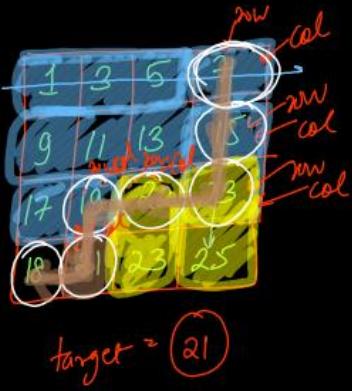


# Mirror the matrix  
↓

Row by Row  
Reversal

1 2 3 4	$\rightarrow$	4 3 2 1
5 6 7 8	$\rightarrow$	8 7 6 5
9 10 11 12	$\rightarrow$	12 11 10 9

search in Matrix  $\rightarrow$  sorted Rows & sorted cols



① linear search

$\rightarrow O(\text{Rows} \times \text{Cols})$  Time

② Two Pointers to point a single cell

{row, col}

Staircase Search

(Divide & Conquer)  
Binary Search  
Merge Sort

$17 \times 19 < 21$

```
int row = 0, col = matrix[0].length - 1; // Top Right Corner
while(row < matrix.length && col >= 0){
    if(matrix[row][col] == target)
        return true;
    else if(matrix[row][col] < target){
        // Discard the current row
        row++;
    }
    else {
        // Discard the current col
        col--;
    }
}
return false;
```

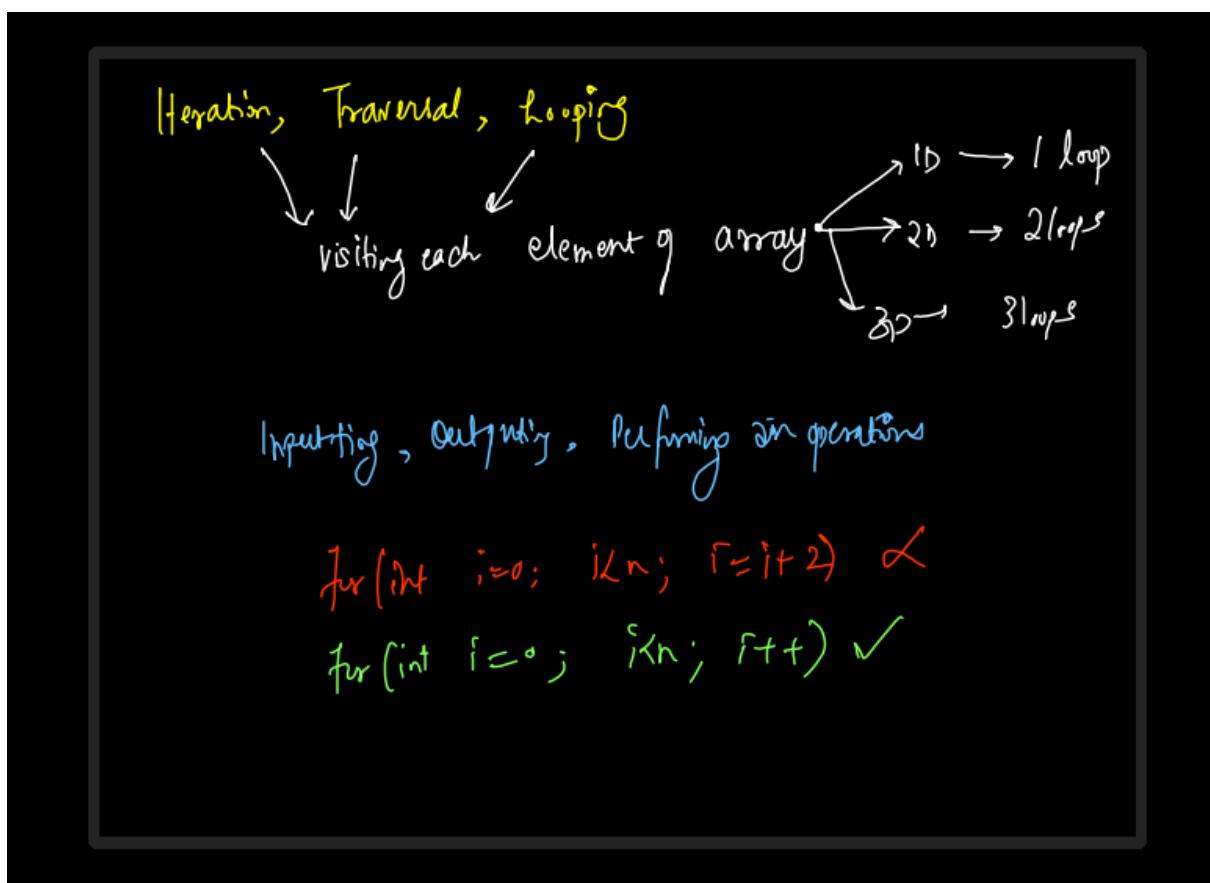
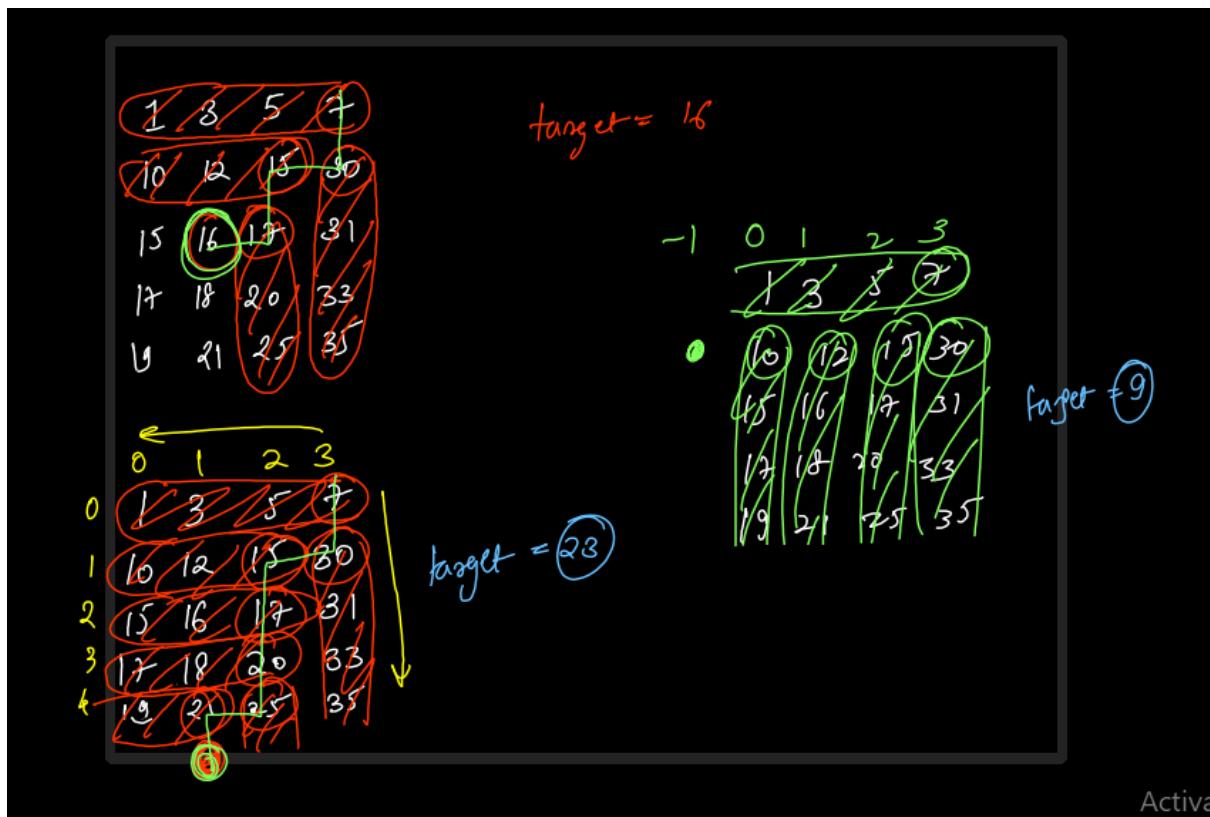
Row is sorted, Col is sorted  
 $\Rightarrow \text{row} = 0, \text{col} = 3$

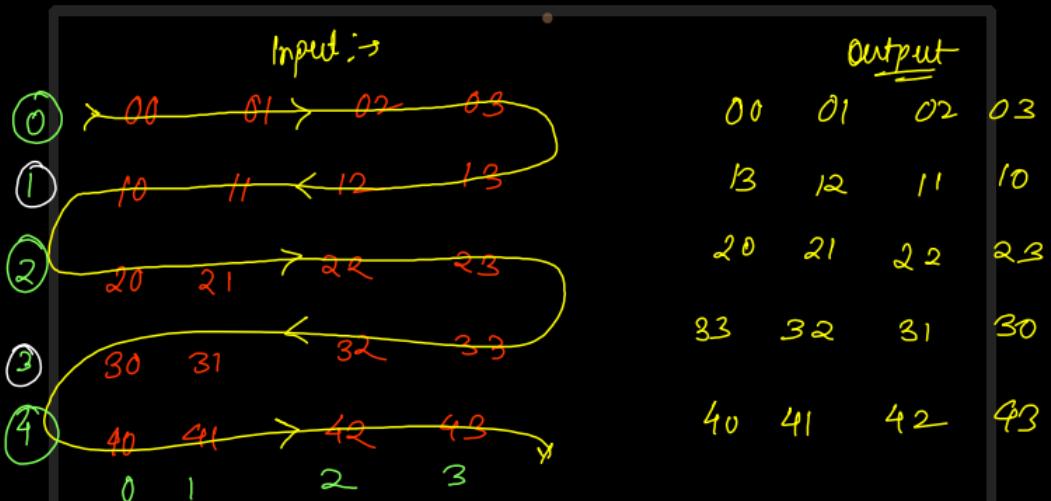


$1, 3, 5 < 7 < 19$   
 $19 < 30 < 31, 33, 35$   
 $10 > 2 < 15 < 19$

$15, 16 < 17 < 19$   
 $19 < 20 < 25$

target = 19  
 $17 < 18 < 19$   
 $19 < 21$





Wave Traversal

↳ Row by Row Zig-Zag Traversal

Index of the row

→ even : → Left to Right

→ odd : → Right to Left

```
// Wave Traversal (Row by Row Zig-Zag Traversal)
```

```
for(int i=0; i<row; i++){
    if(i % 2 == 0){
        // Print Left to Right
        for(int j=0; j<col; j++){
            System.out.print(arr[i][j] + " ");
        }
    } else {
        // Print Right to Left
        for(int j=col-1; j>=0; j--){
            System.out.print(arr[i][j] + " ");
        }
    }
    System.out.println();
}
```

## Row with Max Ones

Binary Search

0 1 2 3 (4)

—

0	1	1	1
0	0	1	1
1	1	1	1
0	0	0	0

$4-1 = 3$   
cols - col index of 1st 1 in each row

$4-2 = 2$

$4-0 = 4$

$4-4 = 0$

```
public static int maxOnes (int arr[][], int N, int M)
{
    int maxZeros = 0, row = 0;
    for(int i=0; i<N; i++){
        // Count the Number of Ones
        int count = 0;
        for(int j=0; j<M; j++){
            if(arr[i][j] == 1) count++;
        }
        if(count > maxZeros){
            maxZeros = count;
            row = i;
        }
    }
    return row;
}
```

~~row~~  $\leftarrow$  to store the row index with max ones

(2)  $\text{row} = 0$ ,  $\text{max} = \emptyset / 4$

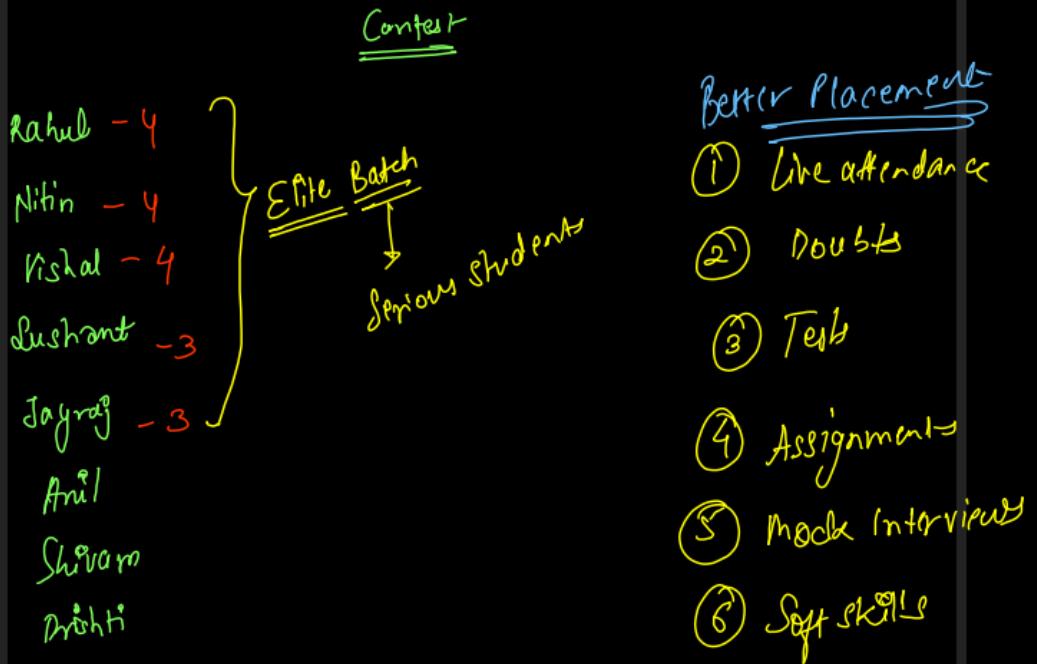
0	0	1	1	1
1	0	0	1	1
2	1	1	1	1
3	0	0	0	0

Count =  $\emptyset / f_3$

Count =  $\emptyset / f_2$

Count =  $\emptyset / f_4$

Count =  $\emptyset$



Activat

Multiplication of 3 Nos as maximum

eg 1  $0, 0, 1, 2, 3, 5, 6, 7, 9$  → if all are positive  
 $5, 0, 2, 6, 0, 7, 9, 1, 3$  → false 3 max<sup>m</sup> nos

Max Product =  $9 \times 7 \times 6$

eg 2  $-11 \quad -10 \quad 0 \quad 5 \quad 6 \quad 7 \quad 0$

Max<sup>m</sup> product =  $-11 \times -10 \times 7$

$\begin{array}{ccccccc} 9 & 3 \\ -11 & -10 & -9 & -8 & -7 & -6 & -5 \\ \times & & & & & & \end{array}$

Max<sup>m</sup> → 3 max<sup>m</sup>  
 ② → 1 max<sup>m</sup>, 2 min<sup>m</sup>

```

        Arrays.sort(arr); // Inbuilt sorting

        int max1 = arr[n - 1], max2 = arr[n - 2], max3 = arr[n - 3];
        int prod1 = max1 * max2 * max3;

        int min1 = arr[0], min2 = arr[1];
        int prod2 = min1 * min2 * max1;

        System.out.println(Math.max(prod1, prod2));
    }
}

```

Max<sup>m</sup> of 3 nos

~~Sort n<sup>2</sup>~~ → O(N log N)  
O(N<sup>2</sup>)

Q1

0, 0, 1, 1, 2, 2, 2, 3, 4, 5, 6, 7, 8, 9  
7 × 8 × 9

Q2

-7, -6, -5, -5, -4, -3, -2, -1  
-1 × -2 × -3 = -6

Q3

(-8, -7), -5, 0, 4, 6, 10  
-8 × -7 × 10 < 560

Q4

-5, -4, 0, 3, 6, 7  
2 × 7 = 140  
3 × 6 × 4 = 144

Activate

```

int max1 = Integer.MIN_VALUE, max2 = Integer.MIN_VALUE, max3 = Integer.MIN_VALUE;
int min1 = Integer.MAX_VALUE, min2 = Integer.MAX_VALUE;

for(int i=0; i<n; i++){
    if(arr[i] >= max1){
        max3 = max2;
        max2 = max1;
        max1 = arr[i];
    }
    else if(arr[i] >= max2){
        max3 = max2;
        max2 = arr[i];
    }
    else if(arr[i] >= max3){
        max3 = arr[i];
    }

    if(arr[i] <= min1){
        min1 = min2;
        min2 = arr[i];
    }
    else if(arr[i] <= min2){
        min2 = arr[i];
    }
}

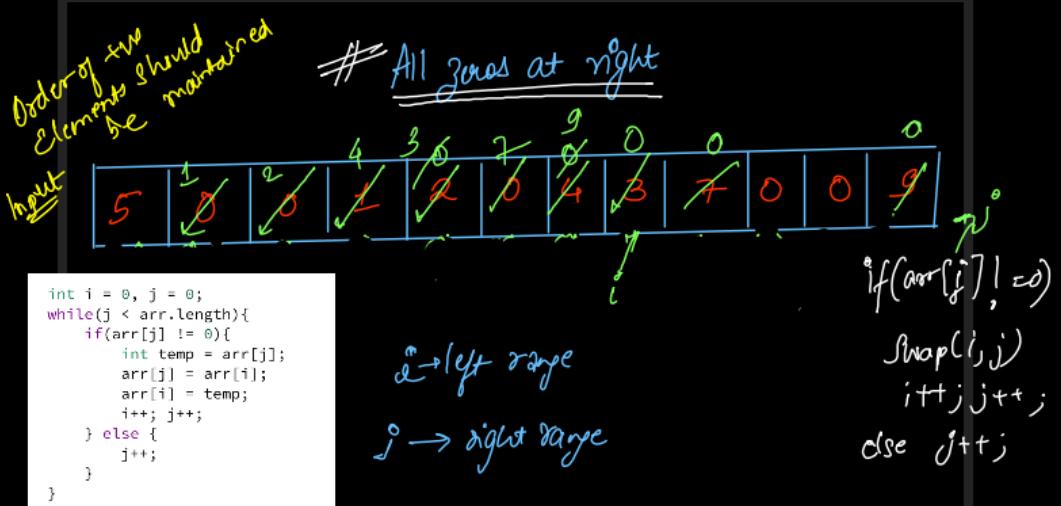
System.out.println(Math.max(max1 * max2 * max3, min1 * min2 * max1));

```

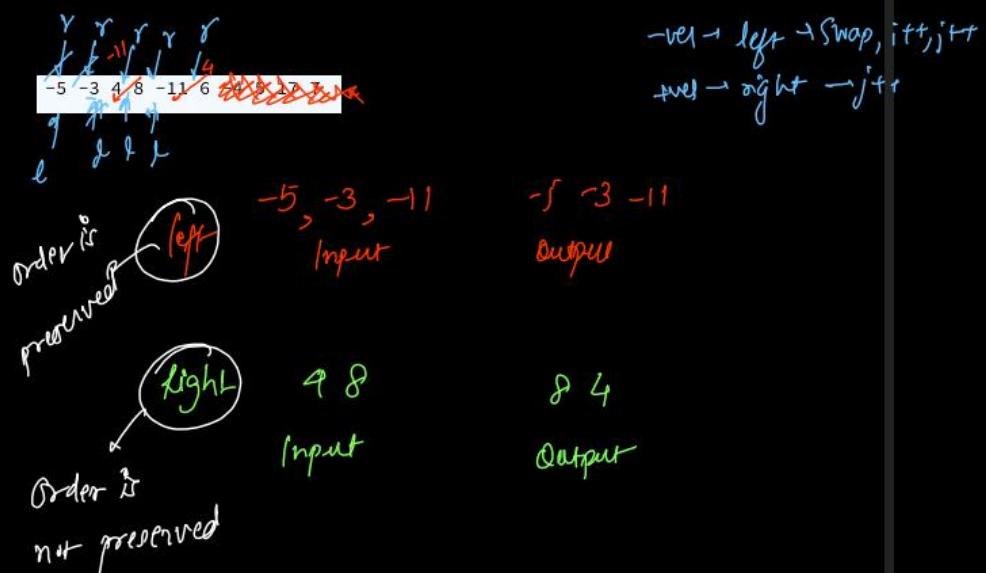
4

7 -2 -9 8 5 1 -10

8, 7, 5, 1, -2, -9, -10  
max1 = 7, max2 = 5, max3 = 1  
min1 = -2, min2 = -9, min3 = -10



Activa



$i$	$j$	$i+j$
0	0	0
1	1	1
2	2	2
3	3	3
4	4	4

$$(1+7+13+19+25) + (21+17+13+9+5) - 13$$

$i$	$j$	$i+j$
0	0	0
1	1	1
2	2	2
3	3	3
4	4	4

$$1+7+13+19 + 16+12+8+4$$

A

$i$	$j$	$i+j$
0	0	0
1	1	1
2	2	2
3	3	3
4	4	4

$$(1+7+13+19+25) + (21+17+13+9+5) - 13$$

$i$	$j$	$i+j$
0	0	0
1	1	1
2	2	2
3	3	3
4	4	4

$$1+7+13+19 + 16+12+8+4$$

A

```

int sum = 0;

// TOP LEFT TO BOTTOM RIGHT
for(int i=0; i<n; i++){
    sum = sum + mat[i][i];
}

// TOP RIGHT TO BOTTOM LEFT
for(int i=0; i<n; i++){
    sum = sum + mat[i][n - 1 - i];
}

if(n % 2 == 1) sum = sum - mat[n/2][n/2];

System.out.println(sum);

```

Doubt Session  
 7:00 PM to 7:30 PM  
 (Monday to Friday)  
 Teams group → Web Party  
 DSA-Java doubts

	0	1	2	3	4	
0	0+0=0	0+1=1	0+2=2	0+3=3	0+4=4	
1	1+0=1	1+1=2	1+2=3	1+3=4	1+4=5	
2	2+0=2	2+1=3	2+2=4	2+3=5	2+4=6	
3	3+0=3	3+1=4	3+2=5	3+3=6	3+4=7	

Indexes  
 sum of (row, col)  
 Diagonals from bottom -  
 left to top-right

Difference of Row, Col

Diagonals from top left to right diagonals

0	0-0	0-1	0-2	0-3	0-4	0-5
1	1-0	1-1	1-2	1-3	1-4	1-5
2	2-0	2-1	2-2	2-3	2-4	2-5
3	3-0	3-1	3-2	3-3	3-4	3-5
4	4-0	4-1	4-2	4-3	4-4	4-5

```

int row = scn.nextInt(), col = scn.nextInt();
// Sum of Row, Col Index
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        System.out.print(i + j + " ");
    }
    System.out.println();
}

System.out.println();

// Difference of Row, Col Index
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        System.out.print(i - j + " ");
    }
    System.out.println();
}

```

Type ① BL to TR

Type ② TL to BR

Symmetric matrix 

	0	1	2	3
0	10	20	30	40
1	20	50	80	100
2	30	80	60	90
3	40	100	90	70

Lower Left Triangle  
= = Upper Right Triangle

$\Rightarrow$  Matrix = Transpose of Matrix

$$\forall i, j \quad a[i][j] = a[j][i]$$

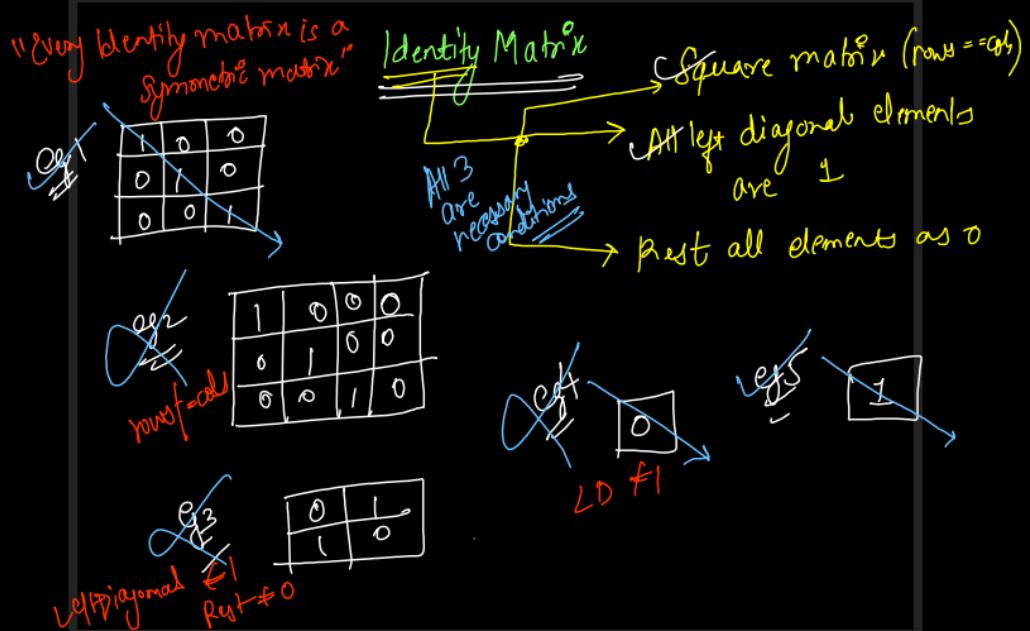
Square matrix  $\rightarrow$  rows = cols

①  $\times$  Square,  $\times$  Symmetric

②  $\checkmark$  Square,  $\times$  Symmetric

③  $\checkmark$  Square,  $\checkmark$  Symmetric

$\times$  Square,  $\checkmark$  Symmetric } This is not possible.



Activate Win

```

if(row != col){
    // Non-Square Matrix can never be Identity Matrix
    System.out.println("false");
    return;
}

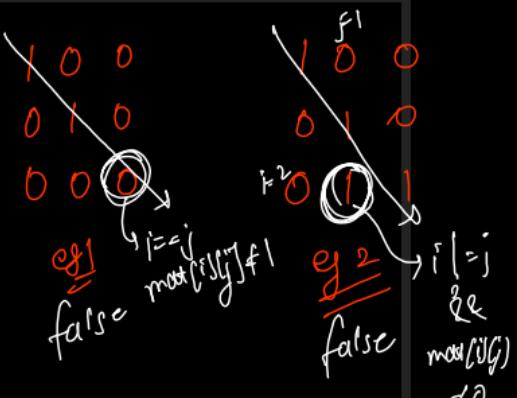
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){

        // Diagonal Elements should be 1
        if(i == j && mat[i][j] != 1){
            System.out.println("false");
            return;
        }

        // Non-Diagonal Elements should be 0
        if(i != j && mat[i][j] != 0){
            System.out.println("false");
            return;
        }
    }
}

```

```
System.out.println("true");
```

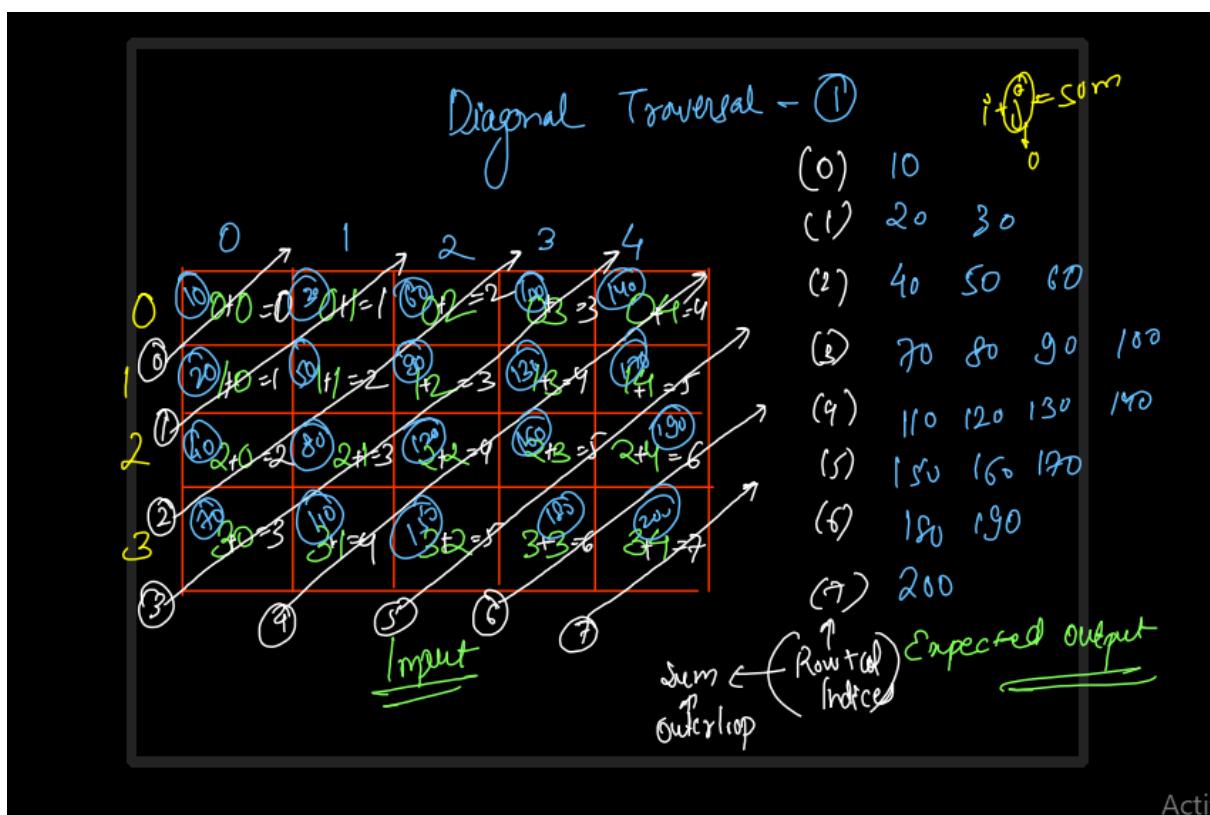
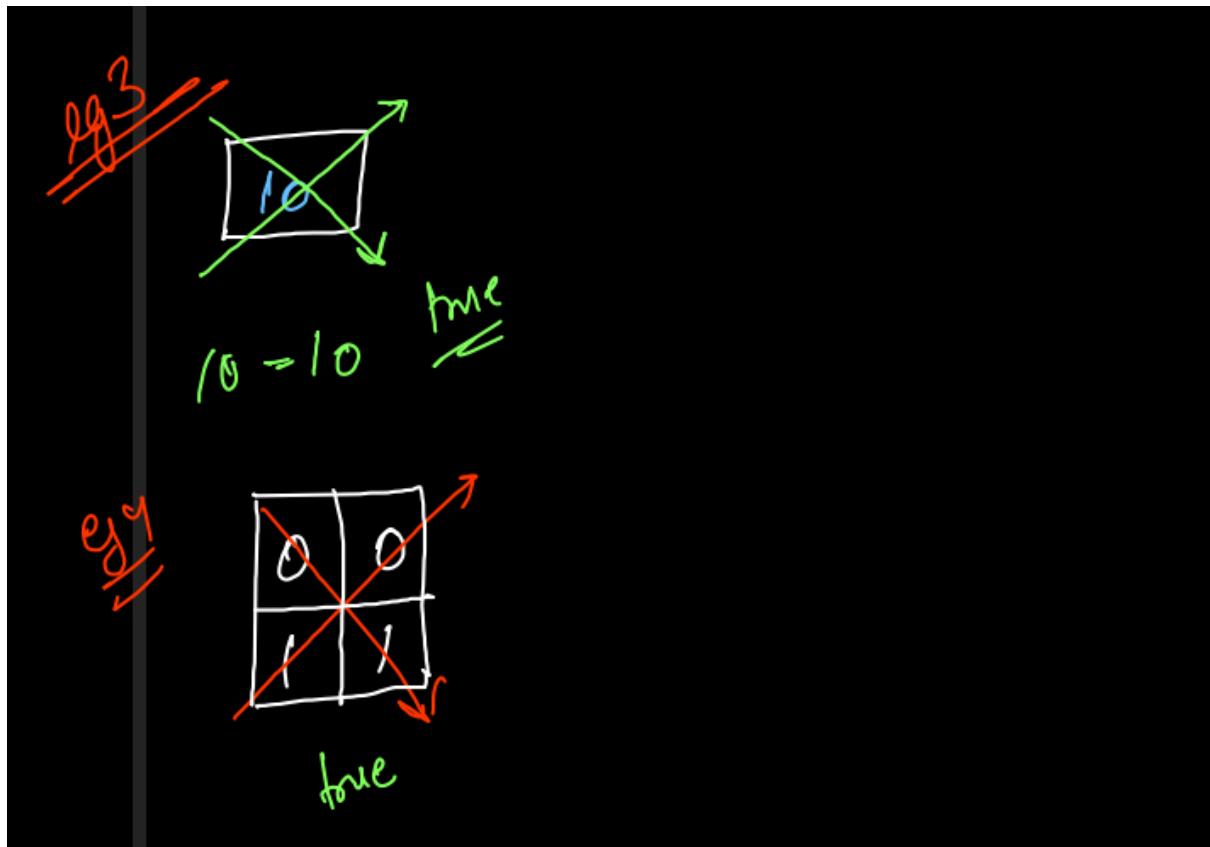


Diagonals sums same or Not				
<del>8:30</del>			row=col, even rows	
<del>row=col, odd rows</del>			row=col, odd rows	
$10 + 20 + 30 + 40 = 150$ $15 + 25 + 35 + 20 = 150$			$10 + 20 + 30 + 40 + 50 = 150$ $30 + 10 + 30 + 30 + 20 = 150$	
<input type="checkbox"/> True			<input checked="" type="checkbox"/> False	

```
// Check Diagonals Sum are equal or not (for Square Matrix)
int leftSum = 0;
for(int i=0; i<row; i++){
    leftSum = leftSum + mat[i][i];
}

int rightSum = 0;
for(int i=0; i<row; i++){
    rightSum = rightSum + mat[i][row - 1 - i];
}

if(leftSum == rightSum) System.out.println("true");
else System.out.println("false");
```



Acti

## Medium - Hand

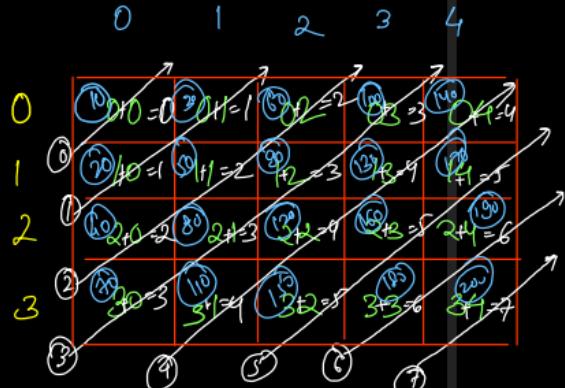
```
// Outer Loop -> Sum of Row + Col -> Picking Diagonals
for(int sum = 0; sum <= (row - 1 + col - 1); sum++){

    // If the Diagonal Starts from the left Wall
    int i = sum, j = 0;

    // If the Diagonal Starts from Bottom Wall
    if(sum >= row){
        i = row - 1;
        j = sum - i;
    }

    while(i >= 0 && j <= col-1){
        System.out.print(mat[i][j] + " ");
        i--;
        j++;
    }

    System.out.println();
}
```



## Diagonal Traversal

## Medium - Hand

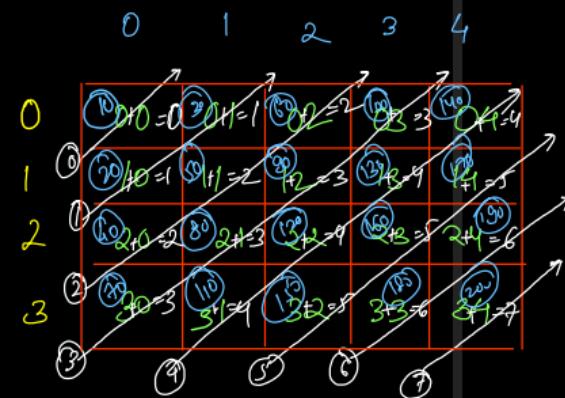
```
// Outer Loop -> Sum of Row + Col -> Picking Diagonals
for(int sum = 0; sum <= (row - 1 + col - 1); sum++){

    // If the Diagonal Starts from the left Wall
    int i = sum, j = 0;

    // If the Diagonal Starts from Bottom Wall
    if(sum >= row){
        i = row - 1;
        j = sum - i;
    }

    while(i >= 0 && j <= col-1){
        System.out.print(mat[i][j] + " ");
        i--;
        j++;
    }

    System.out.println();
}
```



## Diagonal Traversal

2:50

*Addition of 2 matrices*

$$res[i][j] = A[i][j] + B[i][j]$$

$N_1 = N_2 = N_3$	$M_1 = M_2 = M_3$	$\xrightarrow{\text{Constraint}}$
-------------------	-------------------	-----------------------------------

10	20	30	40
50	60	70	80
90	100	110	120

+

15	25	35	45
55	65	75	85
95	105	115	125

=

10+15 =25	20+25 =45	30+35 =65	40+45 =85
50+55 =105	60+65 =125	70+75 =145	80+85 =165
90+95 =185	100+105 =205	110+115 =225	120+125 =245

*A*

*B*

*Res*

$N_1$  rows  
 $M_1$  cols

$N_2$  rows  
 $M_2$  cols

$N_3$  rows  
 $M_3$  cols

```
// Add 2 Matrix
Scanner scn = new Scanner(System.in);
int row = scn.nextInt();
int col = scn.nextInt();

int[][] a = new int[row][col];
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        a[i][j] = scn.nextInt();
    }
}

int[][] b = new int[row][col];
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        b[i][j] = scn.nextInt();
    }
}
```

Finished in 117 ms

25	45	65	85
105	125	145	165
185	205	225	245

stdin

3	4		
10	20	30	40
50	60	70	80
90	100	110	120
15	25	35	45
55	65	75	85
95	105	115	125

```
int[][] res = new int[row][col];
for(int i=0; i<row; i++){
    for(int j=0; j<col; j++){
        res[i][j] = a[i][j] + b[i][j];
        System.out.print(res[i][j] + " ");
    }
}
System.out.println();
```

Time  $\rightarrow O(R \times C)$

## Subtract 2 Matrices

10	20	30	40
50	60	70	80
90	100	110	120

15	25	35	45
55	65	75	85
95	105	115	125

-

10-15	20-25	30-35	40-45
= -5	= -5	= -5	= -5
50-55	60-65	70-75	80-85

$$N_1 = N_2 = N_3$$

$$M_1 = M_2 = M_3$$

### Division of 2 Matrices

→ Not Even Possible

→ Why? → Type mismatch

$$res[i][j] = \sum_{k=0}^{M_1} a[i][k] * b[k][j]$$

### Multiplication of 2 Matrices

Constraint

$$N_1 = N_2$$

cols in i = rows in j

$$I = J$$

Row  $\rightarrow J$

$$Col \rightarrow I$$

$B^{4x3}$  is not possible

0	1	2	3	4
1	2	3	4	5
2	3	4	5	6
3	4	5	6	7
4	5	6	7	8

0	10	20	30
1	40	50	60
2	70	80	90
3	100	110	120

$$A [4 \times 5]$$

$$N_1 \times M_1$$

$$B [5 \times 3]$$

$$N_2 \times M_2$$

$$Res: [4 \times 3]$$

$$N_1 \times M_2$$

$$= 6 \times 20$$

$$2 \times 60$$

$$7 \times 80$$

$$18 \times 120$$

$$3 \times 10$$

$$2 \times 90$$

$$5 \times 120$$

$$4 \times 10$$

$$3 \times 90$$

$$1 \times 120$$

$$5 \times 180$$

$$F$$

$$= 6 \times 20$$

$$2 \times 60$$

$$7 \times 80$$

$$18 \times 120$$

$$3 \times 10$$

$$2 \times 90$$

$$5 \times 120$$

$$4 \times 10$$

$$3 \times 90$$

$$1 \times 120$$

$$5 \times 180$$

$$F$$

Activate

$$\begin{aligned}
 & a[i][0] * b[0][j] \\
 & + \\
 & a[i][1] * b[1][j] \\
 & + \\
 & a[i][2] * b[2][j] \\
 & + \\
 & \vdots \\
 & a[i][4] * b[4][j]
 \end{aligned}$$

*Handout*

$$\begin{array}{c}
 \text{Nested loops} \rightarrow ? \\
 \begin{array}{c}
 \text{Matrix } A[2][2] \\
 \text{Matrix } B[2][3] \\
 \text{Result } C[2][3]
 \end{array}
 \end{array}$$

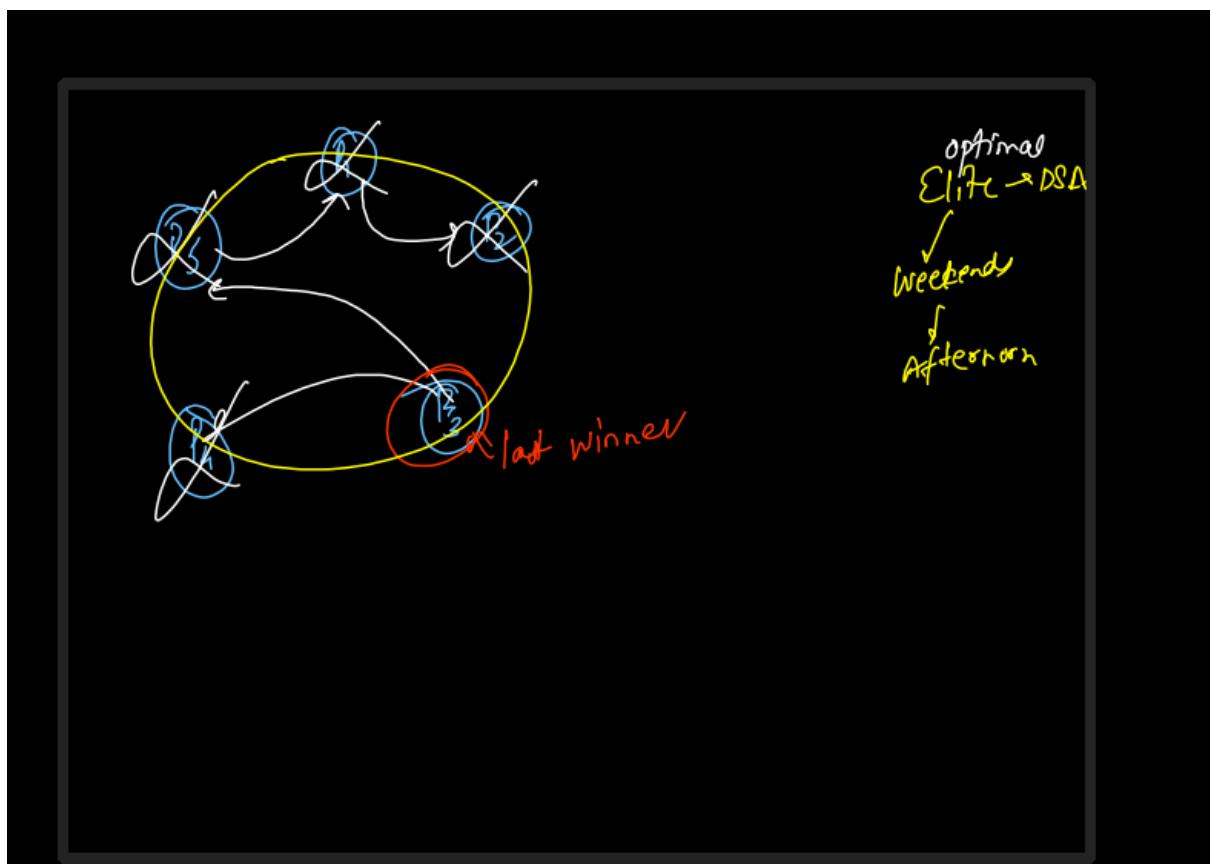
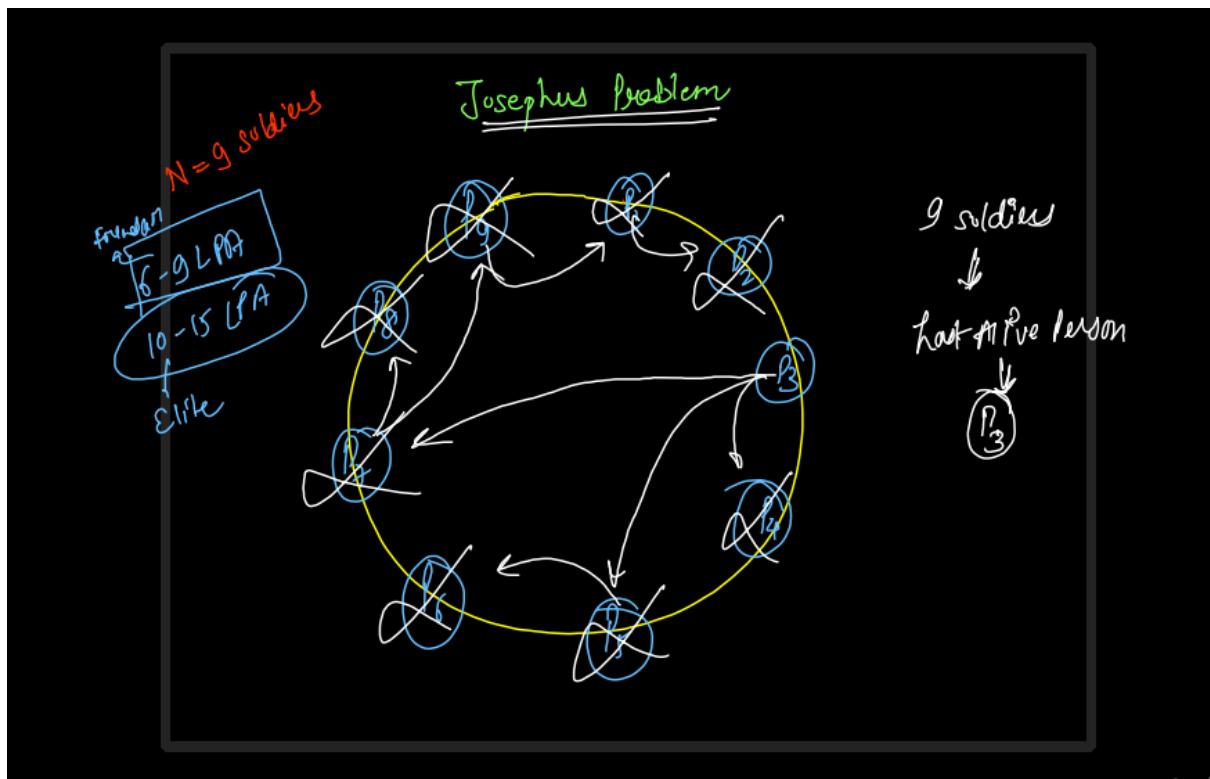
$$\text{row}[1][2] = a[1][0] * b[0][2] + a[1][1] * b[1][2]$$

$$O(R^1 * C^2) = O(N^3)$$

*Multiplication property of matrices is not commutative*

```

for (int i = 0; i < N1; i++) {
    for (int j = 0; j < N2; j++) {
        result[i][j] = 0;
        for (int k = 0; k < N1; k++) {
            result[i][j] += A[i][k] * B[k][j];
        }
    }
}
  
```



Strings

$\text{int marks} = \{10, 20, 30, 40, 50\}$        $(\text{Int} \rightarrow 4 \text{ bytes}) * 5 = 20 \text{ bytes}$

$\text{char initials} = \{ 'A', 'B', 'C', 'D', 'E' \}$        $(\text{char} \rightarrow 2 \text{ bytes}) * 5 = 10 \text{ bytes}$

① ~~String~~  $\text{Char}[ ] [ ]$

$\{ 'A', 'R', 'C', 'H', 'I' \}$        $(\text{char} \rightarrow 2 \text{ bytes}) * 5 = 10 \text{ bytes}$

$\{ \text{Archit}, \text{Bhawani}, \text{Chirag}, \text{Deepak}, \text{Esha} \}$

group of characters  $\{ 'B', 'H', 'A', 'W', 'A', 'N', 'I' \}$

Activ

② Name  $\rightarrow$  String  $\rightarrow$  Archit / Chirag / Deepak / Sushant / Anikumar

College  $\rightarrow$

Enrollment ID

Reg ID

Archit  $\rightarrow$  A R C H I

size is required during initialization

Memory efficient

Many functionalities through substring

concatenation

Reverse

double quotes

single quotes for characters

Lot of memory wastage

Memory is getting wasted

for traversal

Archit  $\rightarrow$  very long string

Char[] = new char[30];

Activat

String → Array of characters

String name = "Archit";  
↓  
class

String name2 = "Chirag";

String of String  
indenting for declaration  
not required

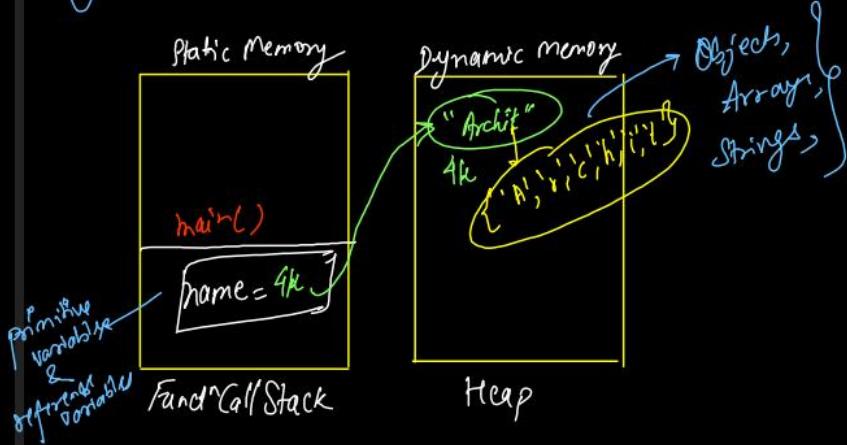
String[] names = { "Archit", "Bhanu", "Chirag",  
"Deepak", "Esha" };

Activate

### Memory Mapping

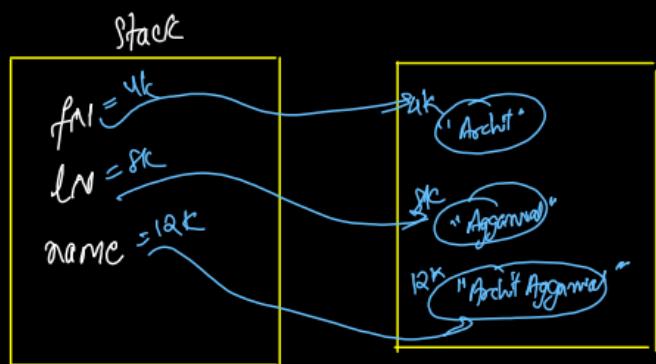
String name = "Archit";

String str; ← Declaration  
String str = "ABC"; ← Initialization



Activate W

f<sub>N</sub> + l<sub>N</sub>  
 "Archit" + "Aggarwal"  
 N<sub>1</sub> N<sub>2</sub>  
 time  
 $O(N_1 + N_2)$   
 = "Archit Aggarwal"  
 oes



```
String name = "";
for(char ch = 'A'; ch <= 'Z'; ch++){
    name = name + ch;
    System.out.println(name);
}
```

name = ~~4K 6K 8K 10K 12K~~  
ch = ~~'A' 'B' 'C' 'D' 'E'~~  
Space

" " + 'A' → ① op

" A" + 'B' → ② operations

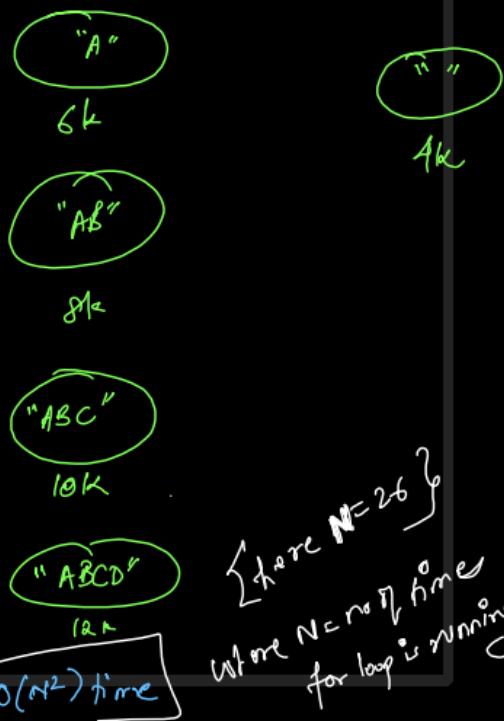
" AB' + 'C' → ③ operator

" ABC" + 'P' → ④ operations

+ 'E' → ⑤

ABCD... " Y" + 'Z'  
→ ⑥ operations

1 + 2 + 3 + 4 + ... 26  
= 26 \* (6^6 + 1)



~~int[]~~  
 int  
 idx  
 String name = "Archit";  
 Array of characters  $\Rightarrow \{ 'A', 'r', 'c', 'h', 'i', 't' \}$   
 Char [] arr =  
 for(int i=0; i<arr.length; i++)  
     System.out.print(arr[i]);  
 String  
 ↓  
 character  
 String []  
 ↗ string

## Iterating / Traversing

```

// Traversal on Character Array
char[] arr = {'A', 'r', 'c', 'h', 'i', 't'};
for(int i=0; i<arr.length; i++){
    // In Array, Length is a Property
    System.out.println(arr[i]);
}

System.out.println();

// Traversal on String
String str = "Archit";
for(int i=0; i<str.length(); i++){
    // In String, Length is a Function
    // Instead of [] bracket, you have to use charAt()
    System.out.println(str.charAt(i));
}
  
```

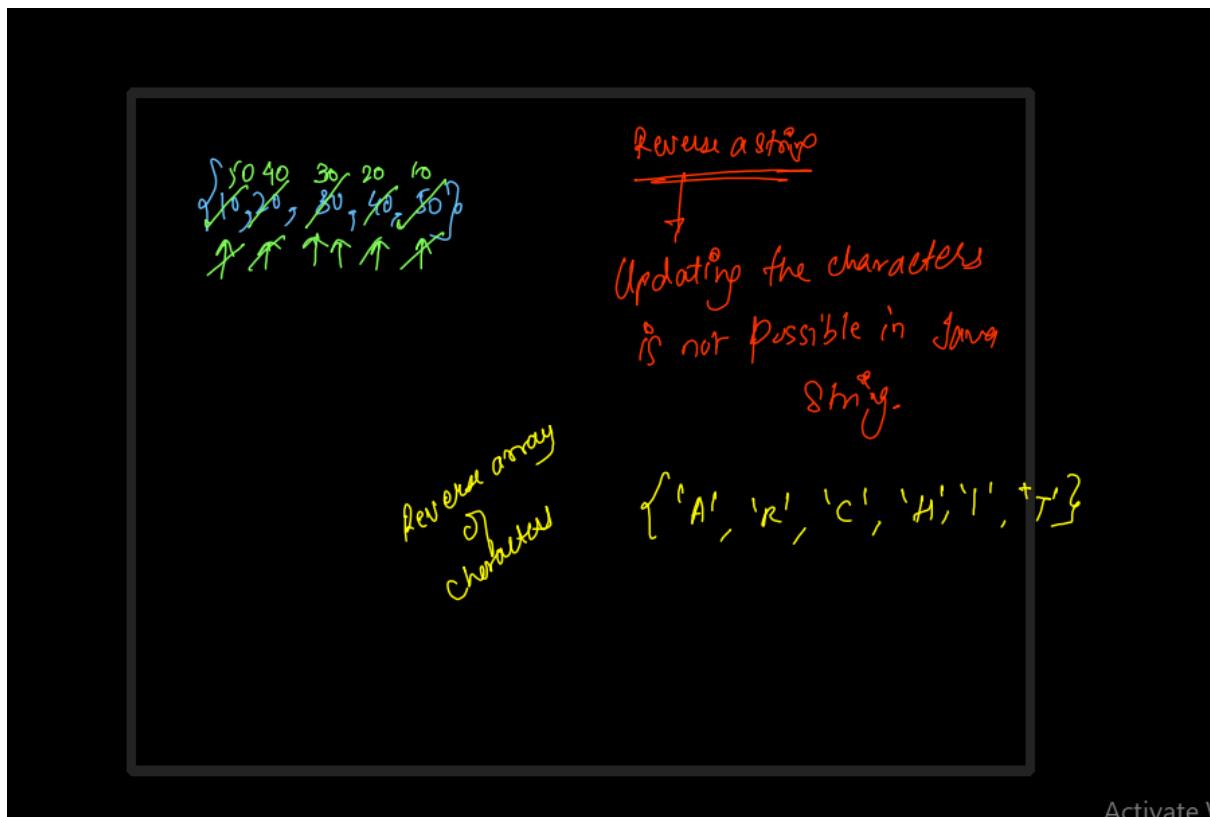
Count of vowels

" Archit - Aggarwal" Count of vowels = 

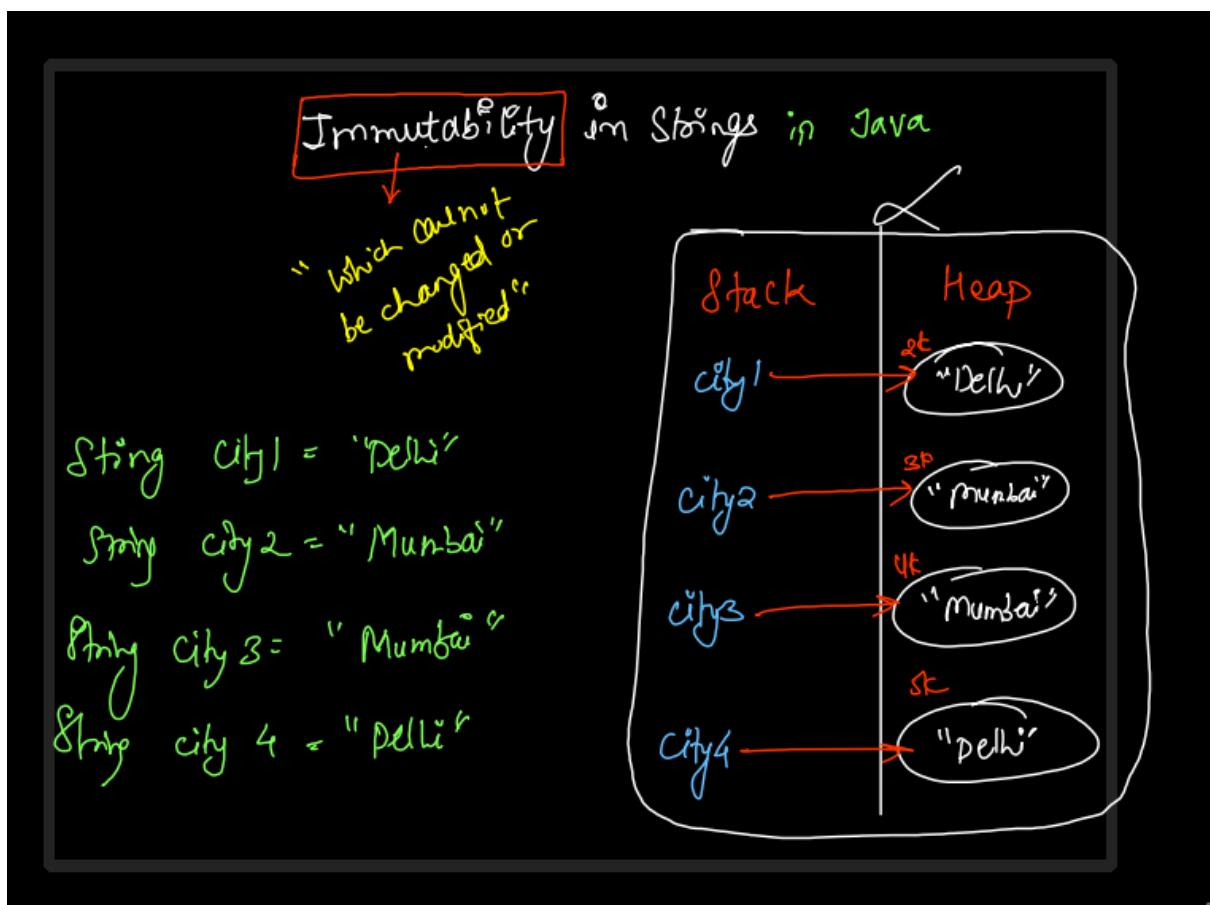
if (str.charAt(i) == 'A' || str.charAt(i) == 'E' || str.charAt(i) == 'I'  
|| str.charAt(i) == 'O' || str.charAt(i) == 'U' || str.charAt(i) == 'a'  
|| str.charAt(i) == 'e' || str.charAt(i) == 'i' || str.charAt(i) == 'o'  
|| str.charAt(i) == 'u')

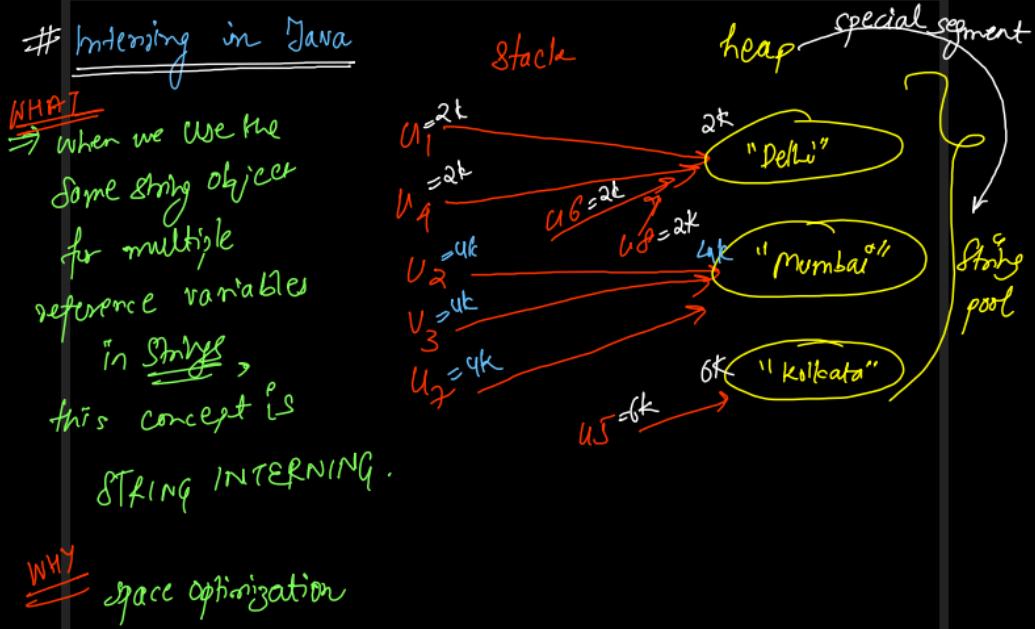
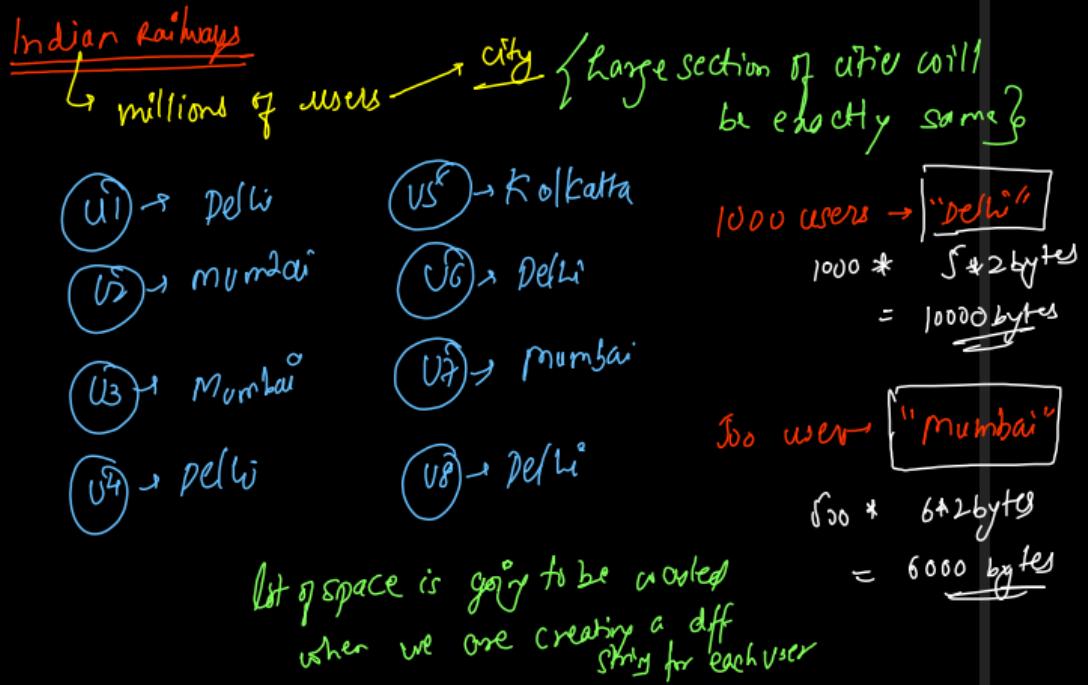
Count ++

```
// - WAP to count vowels in a string.  
Scanner scn = new Scanner(System.in);  
String str = scn.nextLine();  
int vowel = 0;  
for(int i=0; i<str.length(); i++){  
    char ch = str.charAt(i);  
    if(ch == 'A' || ch == 'E' || ch == 'I'  
    || ch == 'O' || ch == 'U'  
    || ch == 'a' || ch == 'e' || ch == 'i'  
    || ch == 'o' || ch == 'u') {  
        vowel++;  
    }  
}  
System.out.println(vowel);
```

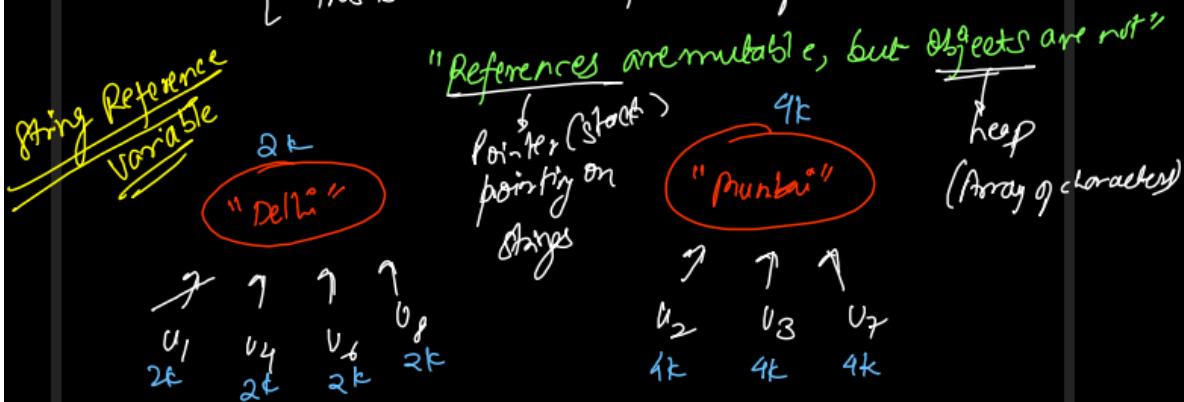


Activate!



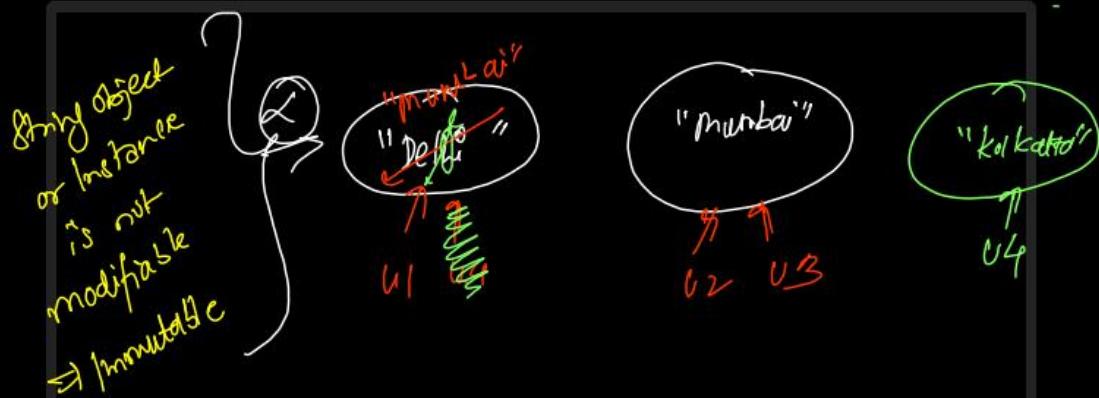


# Immutability for Java strings  
↳ This is a direct consequence of Interning }



If  $u_1$  wants to shift from Delhi to Mumbai,  
⇒ just update reference variable

Activity



① Why is Java Strings Immutable?

→ If you will change the object itself by any one reference variable, due to interning concept, other reference variables will also see the same changes

"Archit" Aggannal  
Aci - gannal

#Word → Ideal word      First letter as capital (Uppercase)  
                                  Rest all the letters as small (lowercase)

eg "Archit"      eg "archit"      or "ARCHIT"      or "A"  
      true                  false                  false                  true

Act

```
String str = scn.next();
boolean isIdeal = true;
for(int i=0; i<str.length(); i++){
    char ch = str.charAt(i);

    if(i == 0){
        // First Letter
        // Should be Uppercase
        if(ch < 'A' || ch > 'Z'){
            isIdeal = false;
            break;
        }
    } else {
        // Remaining Letter
        // Should be Lowercase
        if(ch < 'a' || ch > 'z'){
            isIdeal = false;
            break;
        }
    }
}
```

'A' → 65      'a' → 97  
'B' → 66      'b' → 98  
'C' → 67      'c' → 99  
|  
|  
|  
'Z' → 90      'z' → 122  
91      97  
92      98  
93  
94

Follow up Sentence "Archit Aggarwal - GeeksforGeeks - Mentor"

String → ideal  
 all words are ideal

true

9:20

"Archit Aggarwal"  
 single word → not a ideal word

false

"Archit aggarwal"  
 (not ideal)

false

Ad  
Go

Fundamentals → career  
 Fundamentals + Elite Batch

# M1 → 4-8 LPA  
 ↗ DP / Graph  
 ↗ 13 LPA  
 ↗ TCS interview  
 ↗ Infosys

# M1 → 8-15 LPA  
 ↗ DP / Graph ✓

```
Arrays.sort(arr);

int i = 0;
int expected = 1;
while(i < n){
    int actual = arr[i];
    if(actual <= expected){
        // If the number found is what was expected
        i++;
        if(actual == expected)
            expected++;
    }
    else break;
}

System.out.println(expected);
```

四

Jana/Monique  
Diana

- #Binary Search
- #GOPS

H & H  
H  
S  
V  
K

Smallest Missing Positive

$$-7 \quad -5 \quad -3 \quad 0 \quad 1 \quad 2 \quad 3 \quad 3 \quad 4 \quad 5 \quad 5 \quad 7$$

$$\text{expected} = 1 \neq 4/6$$

first missing  
positive  
site, Batch

Ellie  
Trout  
SP  
(new)  
Bills

## Activation

## Frequency Array

~~a b c d e f g h i j k l m n u p q r s t u v w x y z~~

$\rightarrow \text{Ch}^{-\alpha}$

三

AyB c D E F G M I J k L M N O P Q R S T U V W X Y Z

0 1 2 3 4 5 6 7 8 9

$\rightarrow \text{CH}_3\text{O}$

‘1-2’  
‘1-2’  
‘1-3’

$$\text{shiny} = \text{N}$$

1.  "babbbbcdddccceeff"  
 Expected output -  
 "bbbbccccdddaaaffc"

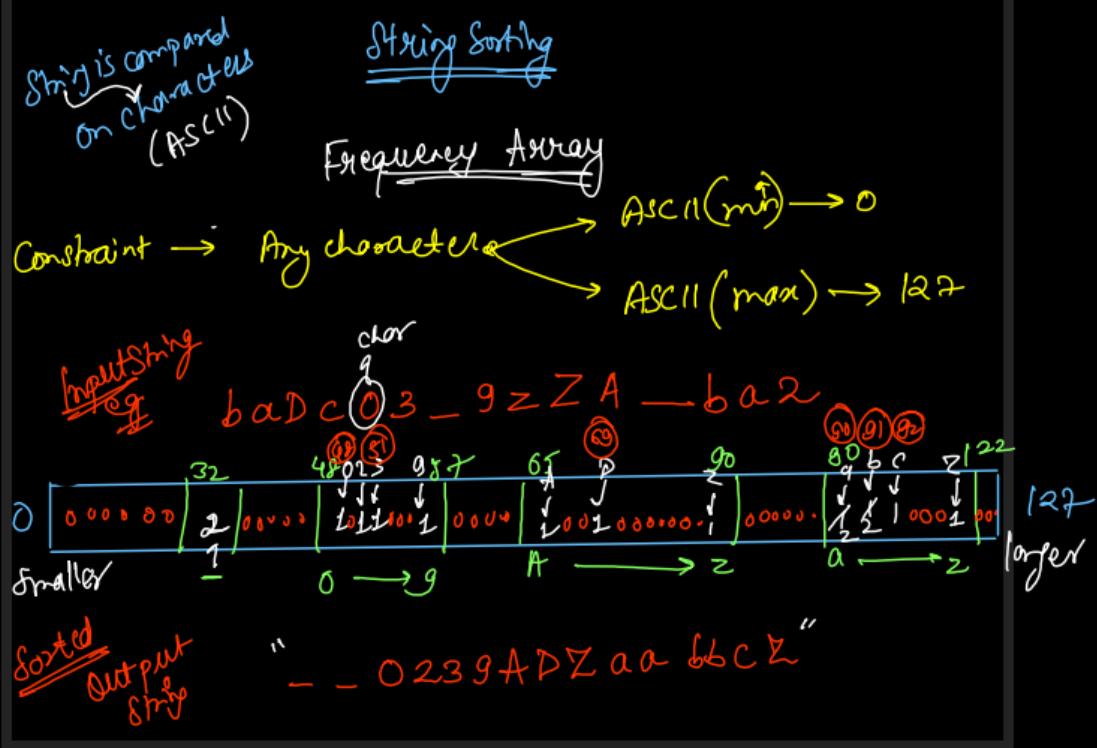
```

public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);

    int min = Integer.MAX_VALUE;
    int max = Integer.MIN_VALUE;
    while(scn.hasNextInt()){
        int val = scn.nextInt();
        min = Math.min(min, val);
        max = Math.max(max, val);
    }

    System.out.print(min + " " + max);
}

```



```

String str = scn.nextLine();
int[] freq = new int[128];

for(int i=0; i<str.length(); i++){
    char ch = str.charAt(i);
    freq[ch]++;
}

String sorted = "";
for(int i=0; i<128; i++){
    // For Each ASCII
    char ch = (char)i;
    for(int j=0; j<freq[i]; j++)
        sorted = sorted + ch;
}
System.out.println(sorted);

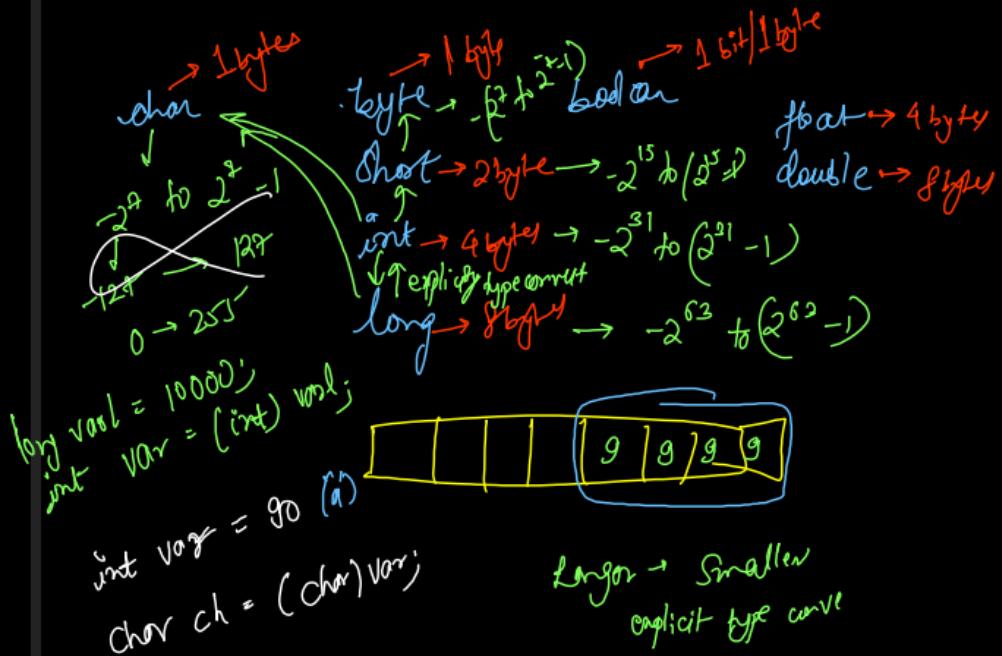
```

eg "bbadaaccdbcfefaa"

97(a)	98(b)	99(c)	100(d)	101(e)	102(f)	
✓	✓	✓	✓	✓	✓	
a	b	c	d	e	f	
1	2	2	2	2	2	
4	3					

$$\begin{aligned}
 & "1 + 'a' + 'a' + 'a' + 'a' \\
 & = "aaaa" + 'b' + 'b' + 'b' \\
 & = "aaaaabb" + 'c' + 'c' \\
 & = "aaaaabbbcc" + 'd' + 'd' \\
 & = "aaaaabbbccdd"
 \end{aligned}$$

Activate



Activ  
Go to S

19:05

## Palindromic String ( $L \rightarrow R = R \rightarrow L$ )

"A" "MADAM" "MOM" "RACECAR"

Palindrome of odd length

"SOS" "ABCDDCBA" "AA" "ABBA"

Palindrome of even length

"PAPA" "ACD" "ABCBBA"

Activate

```
// String is having Alphanumeric Characters
public boolean isPalindrome(String s) {
    int left = 0, right = s.length() - 1;
    while(left <= right){
        char chl = s.charAt(left);
        char chr = s.charAt(right);

        if(chl != chr){
            return false;
        }

        left++; right--;
    }

    return true;
}
```

Time  $\rightarrow$   
 $O(N)$  Linear

Reverse String

~~Iterating  
Immutabile~~

"abcdef" → "fedcba"

String       $\frac{N}{2}$        $\frac{N}{2}$        $O(1)$        $O(N^2)$

$"f" + "c" = "fc" O(2)$

$"fc" + "b" = "fc'b" O(3)$

$"fc'b" + "d" = "fc'b'd" O(4)$

$"fc'b'd" + "e" = "fc'b'd'e" O(5)$

$"fc'b'd'e" + "f" = "fc'b'd'e'f" O(6)$

$$\frac{1+2+3+\dots+N}{2} = \frac{N(N+1)}{2}$$

```
// Reverse String (Word)
String input = scn.next();
String output = "";
for(int i=input.length()-1; i>=0; i--){
    output = output + input.charAt(i);
}
System.out.println(output);
```

Reverse sentence of each word at a time?

Input: Achit - Aggarwal - is - Geekster - Educator

tihcrA      lawraggA      si      retskeeg      rotacude

Output: tihcrA - lawraggA - si - retskeeg - rotacude

①  $i = j+1$   
 $j = j+1$   
 while ( $j < n$  &  $s[i] \neq ' '$ )  $i++$

② Inserting the string  
 $(j-1 \rightarrow i)$   
 { reverse order }

③ Insert the space character

## 557 Leetcode

```

String output = "";
int start = 0, end = 0;

// Exploring Each Word
while(start < input.length()){

    // Taking the End Pointer to the next Space or End of String
    while(end < input.length() && input.charAt(end) != ' '){
        end++;
    }

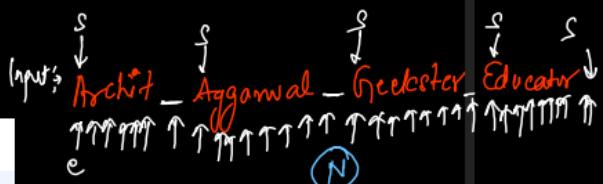
    // Inserting the word in reverse order [end - 1, start]
    for(int i=end-1; i>=start; i--){
        output = output + input.charAt(i);
    }

    // Adding Space after every word but not for the last word
    if(end < input.length()){
        output = output + ' ';
    }

    // Going to the next word
    end++;
    start = end;
}

return output;
}

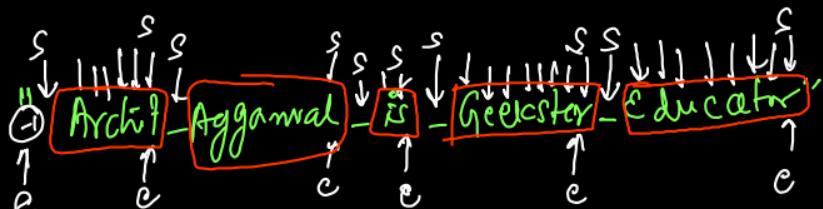
```



output: → thiCrA-lanragga-  
refskee9-rotaclude

$O(N * N * N)$  appending a string  
outer loop  
building in  
reversed order

## Leetcode [151]



"Educator-Geekster-is-Aggarwal-Archit"

"Educator Geekster is Aggarwal Archit"

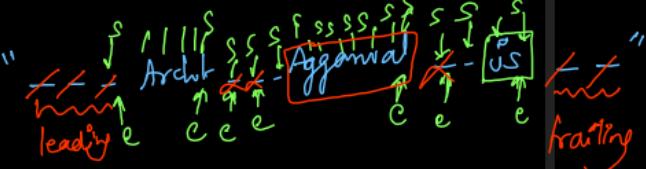
✓ logic  
8:33

✓ Code  
8:47

```

String output = "";
s = trim();
int start = s.length() - 1, end = s.length() - 1;
// Iterate on Each Word
while(cons == 0){
    // Finding the next space from right to left
    while(start >= 0 && s.charAt(start) != ' '){
        start--;
    }
    // Insert the word from [start + 1, end]
    for(int i=start+1; i<end; i++){
        output = output + s.charAt(i);
    }
}

```



Output :> "is - Aggarwal - Archit"

```

// Insert Space for every word except the first word
// Do not Add Space if there are multiple spaces
if(start >= 0 && start < end){
    output = output + ' ';
}
// First Word is Achieved when start == -1
start--;
end = start;
}

return output;

```

## Permutations / Anagrams of String

angel = glean	arc = car	brag = grab
bored = robed	car = act	cider = cried
dusty = study	below = below	inch = chin
right = thing	peach = cheap	players = parsley
wedder = dreads	saw = vase	state = taste

Q1 "a<sub>1</sub>z<sub>2</sub>, b<sub>1</sub>z<sub>2</sub>, c<sub>1</sub>z<sub>2</sub>, d<sub>1</sub>z<sub>2</sub>", "a<sub>1</sub>b<sub>2</sub>c<sub>2</sub>d<sub>2</sub>" True

Q2 "a<sub>1</sub>z<sub>2</sub>, b<sub>1</sub>z<sub>2</sub>, c<sub>1</sub>z<sub>2</sub>, d<sub>1</sub>z<sub>2</sub>", "a<sub>1</sub>b<sub>2</sub>c<sub>1</sub>d<sub>2</sub>" False

Q3 "aaaa@bbbb", "bbbb@aaaa" False String length array equal

Q4 "aaaabbbcccDDA" (B) length "DDDaaaaaccbbb" (A) length False Not anagram

① Sort Both the Strings  $\rightarrow O(N \log N)$

If sorted strings are equal  $\rightarrow$  Anagram ✓  
else ✗

② Frequency Array  $\rightarrow O(N)$

Create Frey Array  
for both strings  
 $\rightarrow$  If Frey array is same  $\rightarrow$  Anagram  
else ✗

Activate

```

public boolean isAnagram(String s1, String s2) {
    if(s1.length() != s2.length()) return false;

    int[] freq1 = new int[26];
    int[] freq2 = new int[26];

    for(int i=0; i<s1.length(); i++){
        int idx = s1.charAt(i) - 'a';
        freq1[idx]++;
    }

    for(int i=0; i<s2.length(); i++){
        int idx = s2.charAt(i) - 'a';
        freq2[idx]++;
    }

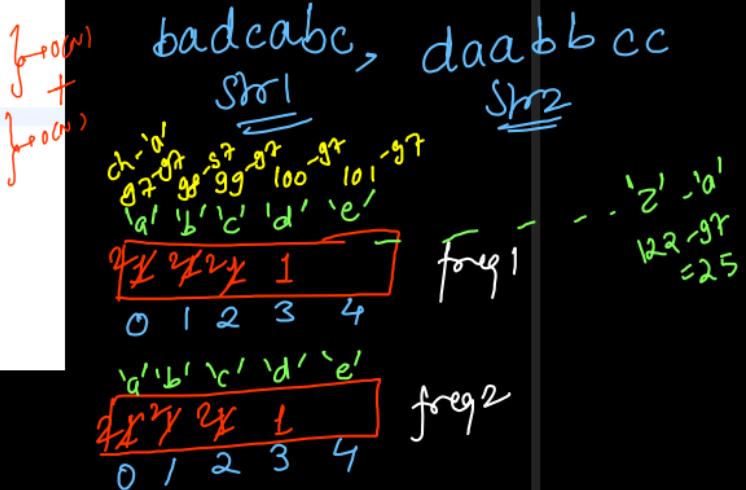
    for(int i=0; i<26; i++){
        if(freq1[i] != freq2[i]){
            return false;
        }
    }

    return true;
}

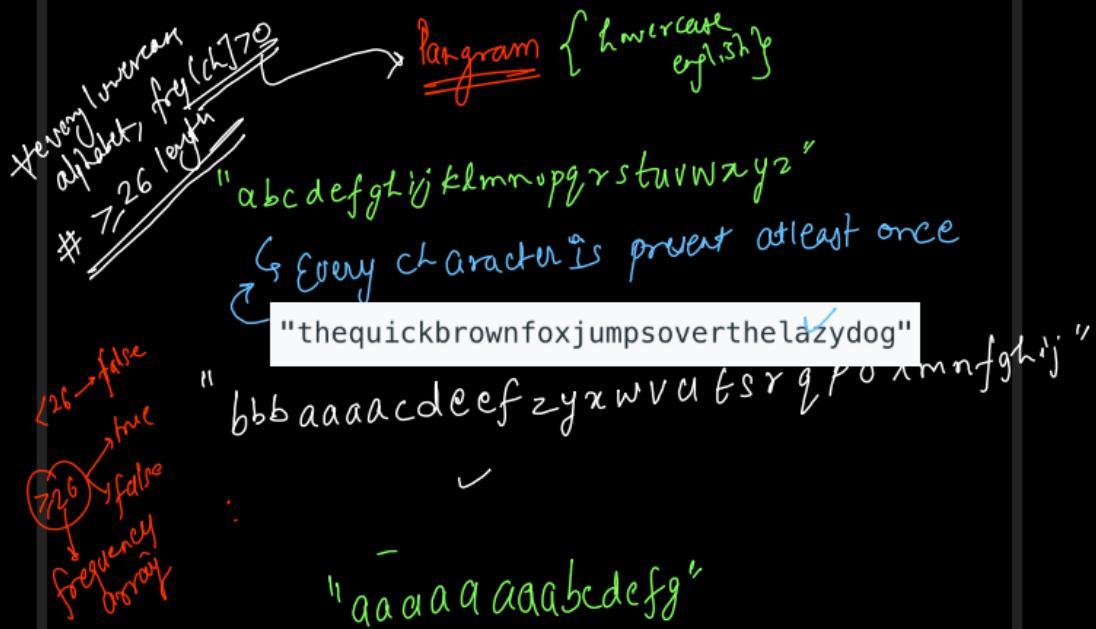
```

lowercase  
English

$\leftarrow \text{if } s1 \neq s2 \text{ (length) } \rightarrow \times \text{ anagram}$



Activate Window



Acti

```

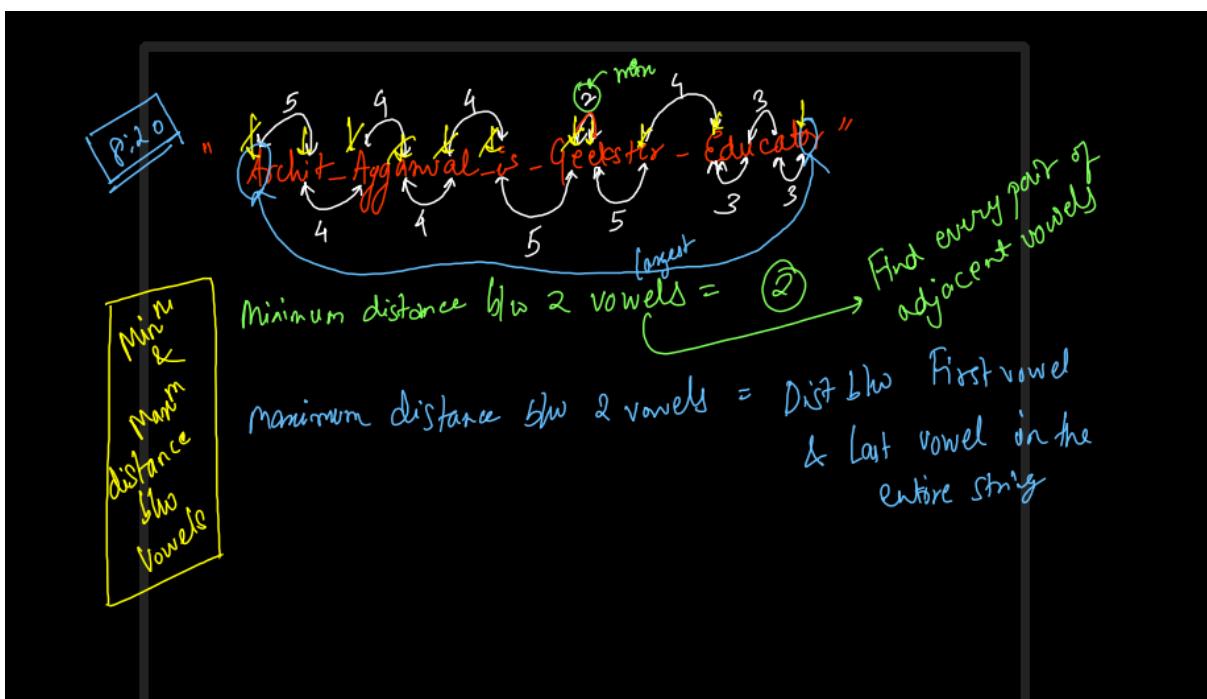
public boolean checkIfPangram(String str) {
    if(str.length() < 26) return false;

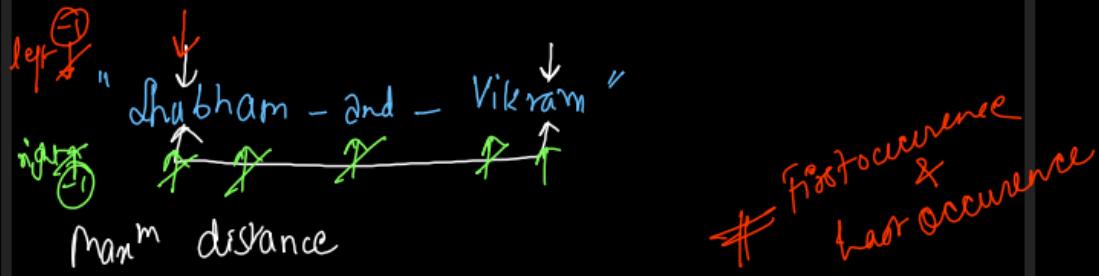
    int[] freq = new int[26];
    for(int i=0; i<str.length(); i++){
        int idx = str.charAt(i) - 'a';
        freq[idx]++;
    }

    for(int i=0; i<26; i++){
        if(freq[i] == 0){
            return false;
        }
    }

    return true;
}

```

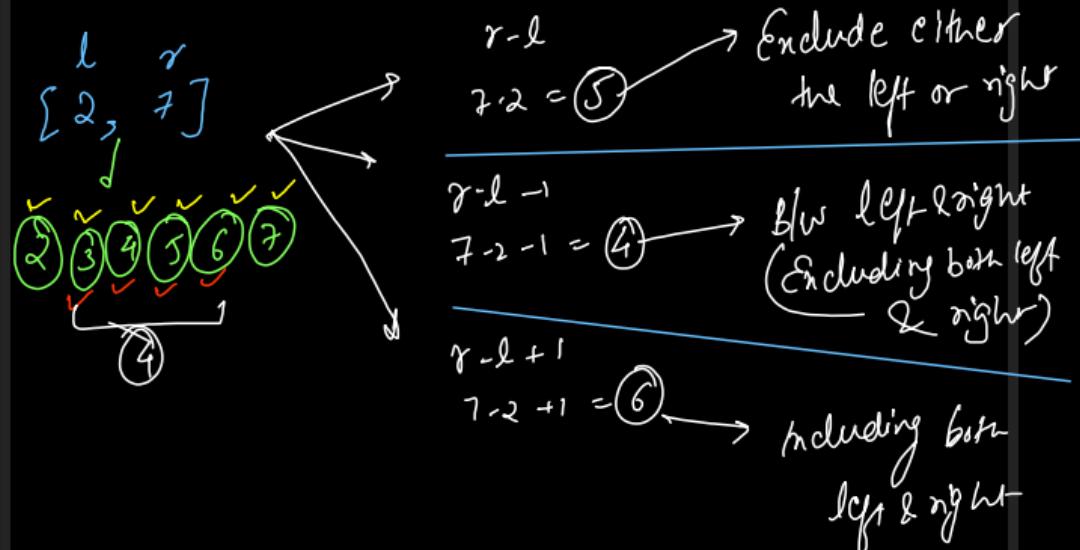


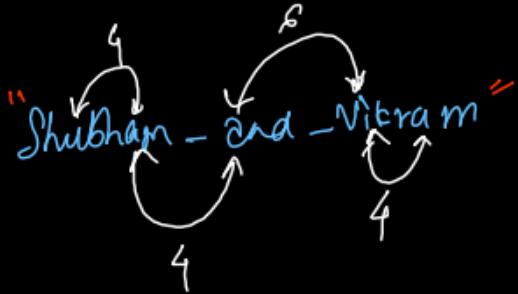


```
// Maximum Distance
int left = -1, right = -1;
for(int i=0; i<str.length(); i++){
    char ch = str.charAt(i);

    if(ch == 'A' || ch == 'E' || ch == 'I' || ch == 'O' || ch == 'U' ||
       ch == 'a' || ch == 'e' || ch == 'i' || ch == 'o' || ch == 'u'){
        right = i;
        if(left == -1)
            left = i;
    }
}

System.out.println(right - left);
```



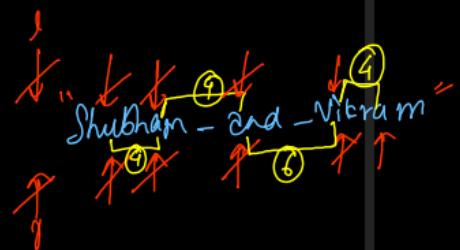


```
// Minimum Distance
int left = -1, right = -1;
int min = Integer.MAX_VALUE;
for(int i=0; i<str.length(); i++){
    char ch = str.charAt(i);

    if(ch == 'A' || ch == 'B' || ch == 'I' || ch == 'O' || ch == 'U' ||
       ch == 'a' || ch == 'e' || ch == 'i' || ch == 'o' || ch == 'u'){
        left = right;
        right = i;

        if(left != -1){
            min = Math.min(min, right - left + 1);
        }
    }
}

System.out.println(min);
```



$$\min = \underline{\underline{+6}}$$

4

Convert String to Integer

String → Integer

"25052022" → 25022022

"99999999" → 99999999

"10000" → 10000

"0001" → 1

"00000" → 0

① inbuilt method

int var = Integer.parseInt(str);

② Parsing each digit (character) & convert it into a integer

$$\begin{array}{l} \text{↓↓} \\ "2505\ 2022" \end{array}$$
$$\begin{array}{l} '3' - '0' = 51 - 48 = 3 \\ '2' - '0' = 50 - 48 = 2 \\ '1' - '0' = 49 - 48 = 1 \\ '0' - '0' = 48 - 48 = 0 \end{array}$$

$$\text{res} = 0 + 2 = 2$$

$'\text{digit}' - '0' = \text{digit}$   
↓  
char      integer

$$\begin{array}{r} 215946 \\ \hline 3 \times 10^5 + 1 \times 10^4 + 5 \times 10^3 \\ + 9 \times 10^2 + 4 \times 10^1 + 6 \times 10^0 \end{array}$$

$$7 \times 10^5 + 1 \times 10^4 + 5 \times 10^3$$

$$+ 9 \times 10^2 + 4 \times 10^1 + 6 \times 10^0$$

Number = Sum of digits + Place values

from  
digit

$$= 6 \times 10^0 + 4 \times 10^1 + 9 \times 10^2 + 5 \times 10^3$$

$$+ 1 \times 10^4 + 7 \times 10^5$$

$$= 6 \times 10^0 + 10 \left( 4 \times 10^0 + 9 \times 10^1 + 5 \times 10^2 \right) + 1 \times 10^3 + 7 \times 10^5$$

$$= 6 \times 10^0 + 10 \left\{ 4 \times 10^0 + 10 \left\{ 9 \times 10^0 + 5 \times 10^1 + 1 \times 10^2 \right\} \right\} + 1 \times 10^3 + 7 \times 10^5$$

$$= 6 \times 10^0 + 10 \left\{ 4 \times 10^0 + 10 \left\{ 9 \times 10^0 + 10 \left\{ 5 \times 10^0 + 10 \left\{ 1 \times 10^0 + 7 \times 10^1 \right\} \right\} \right\} \right\}$$

$$7 \times 10 + 5 = 75$$

$$7 \times 10 + 9 = 79$$

$$7159 \times 10 + 4 = 71594$$

$$71594 + 10 + 6 = 715946$$

Ans  
Java String

```
// Converting Character Digits to Integer Digits
int res = 0;
for(int i=0; i<str.length(); i++){
    int digit = str.charAt(i) - '0';
    res = (res * 10) + digit;
}

System.out.println(str + " " + res);
```

"25314"  
 $\uparrow\uparrow\uparrow\uparrow$

$$2' - '0' = 2$$

$$5' - '0' = 5$$

$$3' - '0' = 3$$

$$1' - '0' = 1$$

$$4' - '0' = 4$$

$$\text{res} = (0 \times 10) + 2 = 2$$

$$= (2 \times 10) + 5 = 25$$

$$= (25 \times 10) + 3 = 253$$

$$= (253 \times 10) + 1 = 2531$$

$$= (2531) \times 10 + 4 = 25314$$

~~leading zeros~~ "00001"

~~all digits as zeros~~  
"00000"

$$\text{res} = 0 \times 10 + 0 = 0$$

$$= 0 \times 10 + 0 = 0$$

$$= 0 \times 10 + 0 = 0$$

$$= 0 \times 10 + 1 = 1$$

$$((0 \times 10 + 0) \times 10 + 0) \times 10 + 0 = 0$$

## Strings - ASCII sum

$$\text{sum} \leftarrow 9 + 98 + 99 + 100 + 101 = 495$$

"abcde"

$$101 + 99 + 100 + 98 + 98 = 495$$

↑ ↑ ↑ ↑ " "

" ec dab " "

$$99 + 99 + 99 + 99 = 495$$

$\uparrow \uparrow \uparrow \uparrow$   
 $C C C C$

250

$$\begin{array}{r}
 11 \\
 b d \quad d b c \quad 11 \\
 \downarrow \quad \downarrow \quad \downarrow \quad \nearrow \\
 98 + 110 + 100 + 98 + 99 \\
 = 495
 \end{array}$$

eeaac"  $\xrightarrow{(s_1+1)_0 + g_2 + s_7 - g_3 = (y)}$

$$\begin{array}{ccc} "D\perp" & \longleftrightarrow & "a" \\ \uparrow & & \uparrow \\ 48 \times u_9 & & g_7 \\ = 0.7 & & \end{array}$$

```
// Ascii sum is the sum of ascii codes of all characters in the string.
Scanner scn = new Scanner(System.in);
String s1 = scn.next();
String s2 = scn.next();

int sum1 = 0, sum2 = 0;
for(int i=0; i<s1.length(); i++){
    sum1 = sum1 + s1.charAt(i);
}

for(int i=0; i<s2.length(); i++){
    sum2 = sum2 + s2.charAt(i);
}

if(sum1 == sum2) System.out.println(true);
else System.out.println(false);
```

### 387 First Unique/ Non Repeating Character *leftmost character in string first*

Given a string  $s$ , find the first non-repeating character in it and return its index. If it does not exist, return -1.

eg " Sachin Tendulkar vs Saurav Ganguly vs Chirag"  $i=3$

3  $\leftarrow$   $i=3$   
idx = 25

$a \rightarrow 1$   $e \rightarrow 1$   $t \rightarrow 1$   
 $b \rightarrow 0$   $f \rightarrow 0$   $s \rightarrow 2$   
 $c \rightarrow 1$   $g \rightarrow 1$   $h \rightarrow 1$   
 $d \rightarrow 0$   $i \rightarrow 1$   
 $n \rightarrow 1$

" Amazon vs microsoft "

$a \rightarrow 1$   $b \rightarrow 2$   $c \rightarrow 2$   
" abcdefghijklmnoprqrsuvwxyz  
the quick brown fox jumps over the lazy dog" (-1)  
No unique character

Activate

#### Algorithm

① Create frequency Array & fill it by looping on string

② Again, loop on string, and find the leftmost character's index having  $\text{freq}[i] = 1$  return that index( $i$ )

③ If there is no such index, return -1;

```

int[] freq = new int[26];

for(int i=0; i<s.length(); i++){
    int idx = s.charAt(i) - 'a';
    freq[idx]++;
}

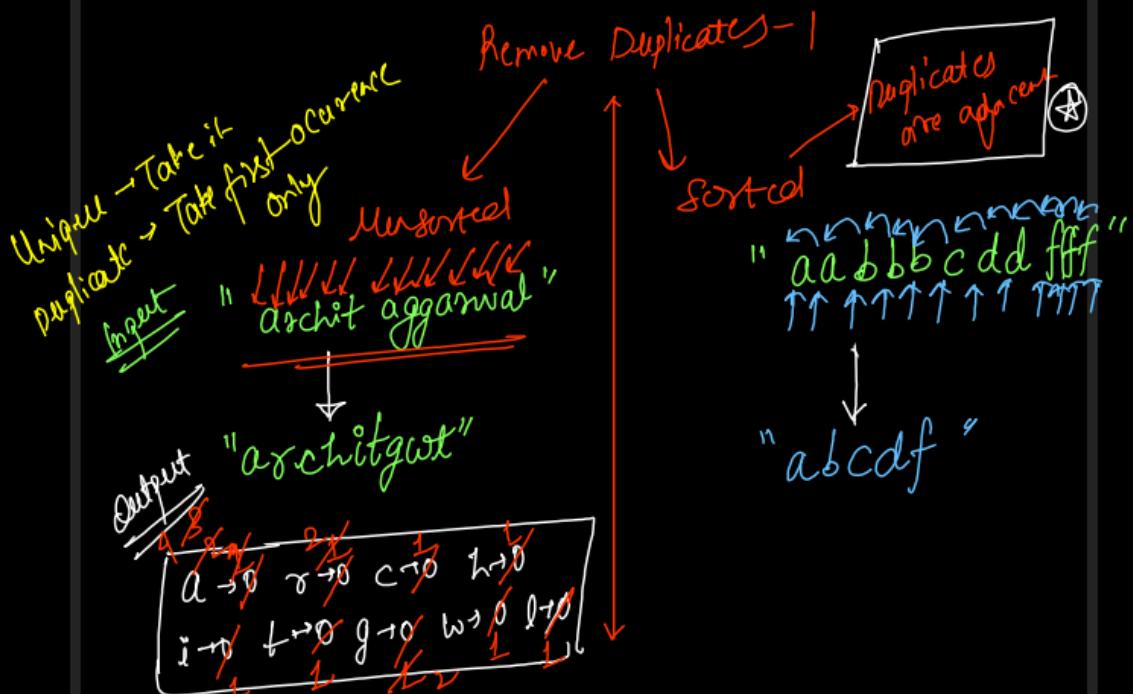
for(int i=0; i<s.length(); i++){
    int idx = s.charAt(i) - 'a';
    if(freq[idx] == 1) return i;
}

return -1;

```

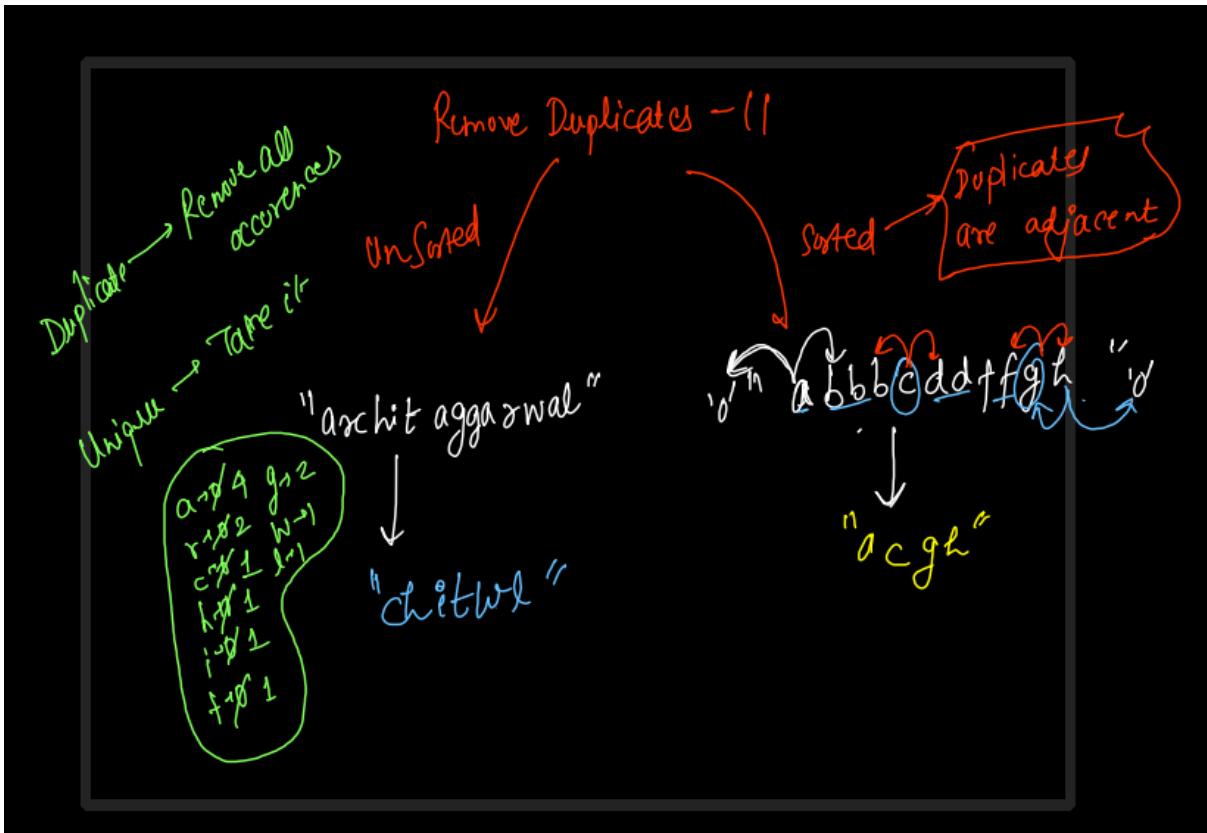
} Filling The freq Array

} Ask If freq[ch] == 1  
return index  
in String



```
// Version - 1 : Unsorted
int[] freq = new int[26];
String output = "";
for(int i=0; i<str.length(); i++){
    int idx = str.charAt(i) - 'a';
    if(freq[idx] == 0){
        output = output + str.charAt(i);
    }
    freq[idx]++;
}
System.out.println(output);
```

```
// Version - 1: Sorted
String output = "";
for(int i=0; i<str.length(); i++){
    // Adding the First Occurrence of each character
    if(i == 0 || str.charAt(i - 1) != str.charAt(i)){
        output = output + str.charAt(i);
    }
}
System.out.println(output);
```



```

// Version - 2: Unsorted
int[] freq = new int[26];
for(int i=0; i<str.length(); i++){
    int idx = str.charAt(i) - 'a';
    freq[idx]++;
}

String output = "";
for(int i=0; i<str.length(); i++){
    int idx = str.charAt(i) - 'a';
    if(freq[idx] == 1){
        output = output + str.charAt(i);
    }
}
System.out.println(output);

```

$N$   
 $+ N$   
 $= 2N$

↓↓↓↓↓↓↓↓↓  
Orchitogganral

$a \rightarrow 4$   $r \rightarrow 2$   $c \rightarrow 1$   
 $f \rightarrow 1$   $i \rightarrow 1$   $t \rightarrow 1$   
 $g \rightarrow 2$   $w \rightarrow 1$   $l \rightarrow 1$

"Chiftwl"

```

// Version - 2: Unsorted
String output = "";

for(int i=0; i<str.length(); i++){
    // Adding the first occurrence of each character
    char left = str.charAt(i);
    int freq = 1;
    for(int j=i+1; j<str.length(); j++){
        if(str.charAt(j) == left){
            freq++;
        } else {
            break;
        }
    }

    output += left;
}

System.out.println(output);

```

Ternary Operator  
 $(cond)? trueStat : falseStat;$

$(-)$  "a b b b c c d e e f g g g g h " r n  
 $\downarrow$   
"adfh"

if ( $i-1 > 0$ )  
 $left = s[i-1];$   
else  
 $left = '0';$

Substrings of a String

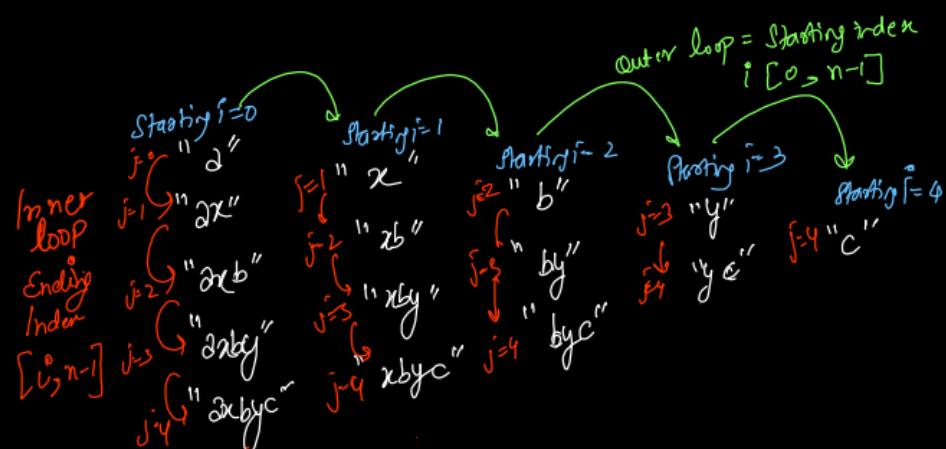
↳ contiguous part of a string

Input  $\vdash$  "abcdef"

- |          |            |          |         |         |
|----------|------------|----------|---------|---------|
| ① "a"    | ⑤ "abcde"  | ⑨ "bcd"  | ⑫ "cd"  | ⑯ "def" |
| ② "ab"   | ⑥ "abcdef" | ⑩ "cde"  | ⑭ "de"  | ⑰ "e"   |
| ③ "abc"  | ⑦ "b"      | ⑪ "bcdg" | ⑮ "cdg" | ⑱ "d"   |
| ④ "abcd" | ⑧ "bc"     | ⑫ "c"    | ⑯ "e"   | ⑲ "f"   |

Ans.

Input  $\vdash$  "axbyc" <sup>0 1 2 3 4</sup>



Ans.

## # Substring of a string

```

for(int st=0; st<n; st++){
    String substr = "";
    for(int end=st; end<n; end++){
        substr = substr + str.charAt(end);
        System.out.println(substr);
    }
}

```

$O(N \times N \times N)$   
 $\uparrow$   $\uparrow$   $\uparrow$   
 $st$   $end$   $+ concat$

$st = 'a'$ $(0)$ $end = 0$ $"a"$ $\overset{0 \rightarrow 0}{}$ $end = 1$	$st = 'bcde'$ $(1)$ $end = "b"$ $"bc"$ $\overset{0 \rightarrow 1}{}$ $end = 2$	$st = 'c'$ $(2)$ $end = 2$ $"bc"$ $\overset{0 \rightarrow 2}{}$ $end = 3$
$st = 'ab'$ $(3)$ $end = 2$	$st = 'cd'$ $(4)$ $end = 3$	$st = 'd'$ $end = 4$
$st = 'abc'$ $(5)$ $end = 3$	$st = 'de'$ $(6)$ $end = 4$	$st = 'e'$ $end = 5$
$st = 'abcd'$ $(7)$ $end = 4$	$st = "de"$ $(8)$ $end = 5$	$st = "bcde"$ $(9)$ $end = 6$

# Inbuilt substring method in Java  
 $\rightarrow$  it is included  $\rightarrow$  it is excluded

str.substring ( starting index, ending index )

$"abcde"$ $\overset{0 \ 1 \ 2 \ 3 \ 4}{}$ $str$	$"be"$ $\rightarrow$ $str.substring(1, 3)$	$"abcdef"$ $\overset{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6}{}$ $str$	$"cdef"$ $\rightarrow$ $str.substring(2, 6)$	$"abcdefg"$ $\overset{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6}{}$ $str$	$"bcdef"$ $\rightarrow$ $str.substring(0, 6)$	$"abcde"$ $\rightarrow$ $str.substring(1, 5)$
$"abcdefg"$ $\overset{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6}{}$ $str$	$"d"$ $\rightarrow$ $str.substring(3, 4)$	$"bcdefg"$ $\rightarrow$ $str.substring(1, 7)$	$"bcde"$ $\rightarrow$ $str.substring(0, 5)$	$"bcde"$ $\rightarrow$ $str.substring(1, 5)$	$"bcde"$ $\rightarrow$ $str.substring(0, 5)$	$"bcde"$ $\rightarrow$ $str.substring(1, 5)$

```

for(int st=0; st<n; st++){
    for(int end=st; end<n; end++){
        System.out.println(str.substring(st, end - 1));
    }
}

```

Activate

$$n \rightarrow 1+2+3+\dots+n = \frac{n*(n+1)}{2}$$

"architagg"

Printing Substrings having  
[No] vowels

$$\text{rch} \rightarrow ③ \rightarrow \frac{3+4}{2} = 6$$

$$"t" \rightarrow ① \rightarrow \frac{1+2}{2} = 1$$

$$"g" \rightarrow ② \rightarrow \frac{2+3}{2} = 3$$

✓ "g" ✓ "k"  
 ✓ "gc" ✓ "t"  
 ✓ "rch" ✓ "j"  
 ✓ "c" ✓ "gg"  
 ✓ "ch" ✓ "g"

10 substrings  
that are having  
no vowels in  
them!

Q:25

"architagganwal"

Archita

Architagg

architagganwo

Print substring  
starting & ending at 'a'.

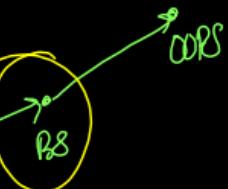
agga

anwa

aggawo

String  
 $(2^{n+1})$

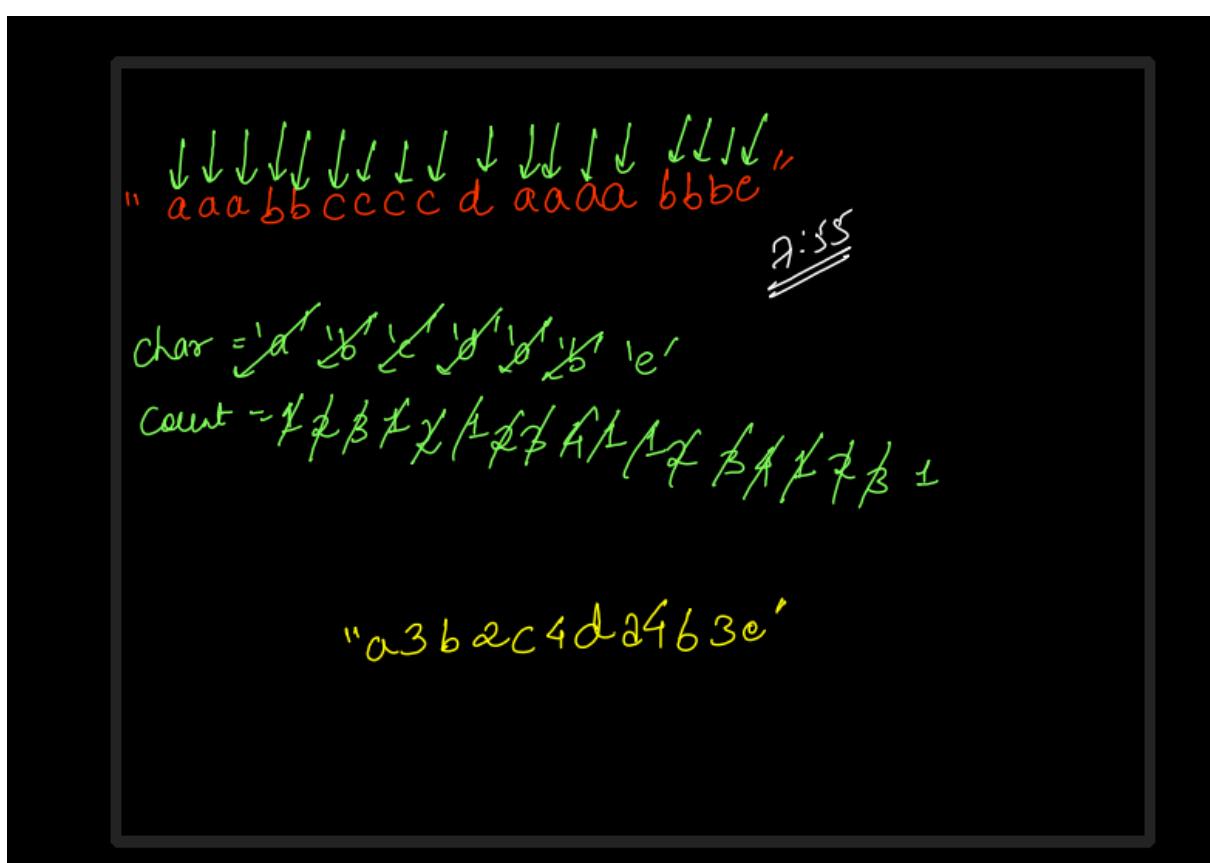
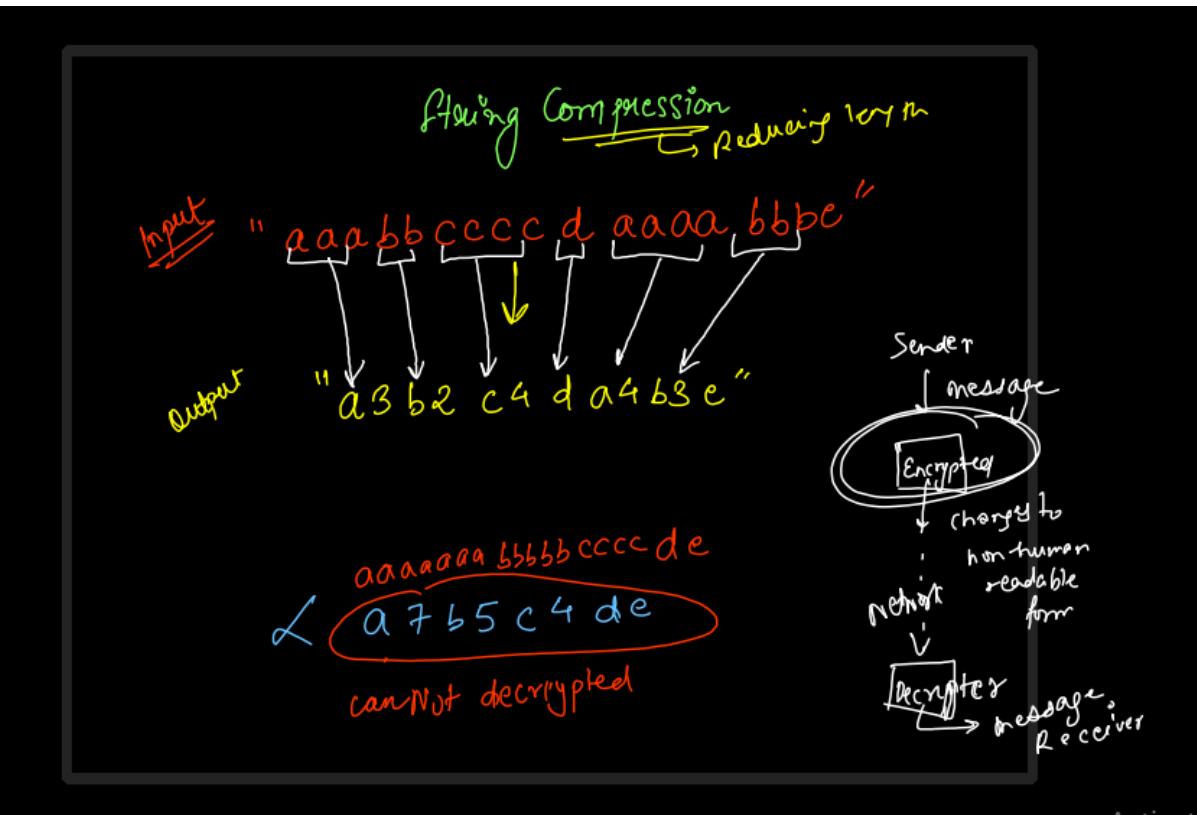
maths



8

B

8



```

String encode(String str)
{
    if(str.length() == 0) return "";

    char ch = str.charAt(0);
    int freq = 1;
    String output = "";

    for(int i=1; i<str.length(); i++){
        if(str.charAt(i - 1) != str.charAt(i)){
            output = output + ch + freq;
            ch = str.charAt(i);
            freq = 1;
        } else {
            freq++;
        }
    }

    output = output + ch + freq;
    return output;
}

```

## String Compression

"aaaabbbbccccdd"

output = "a3b4c2d3"

ch = a b c d

freq = 3 4 2 3

## Power of a string

abbccqdddeeeeeeffggghheecccc

Power set / Subsequence / Subset

They need to be contiguous

Substrings

$$\frac{4 \times (4+1)}{2} = \frac{4 \times 5}{2} = 10$$

a      b      c      d  
 ab    bc    cd  
 abc    bcd  
 abcd

"abcd"  
 2↑2↑2↑2

Subsequence

They can't be contiguous

$$2^n = 2^4 = 16$$

Diagram illustrating the 16 subsequences of "abcd":

```

graph TD
    Root[""] -- a --> A["a"]
    Root -- b --> B["b"]
    Root -- c --> C["c"]
    Root -- d --> D["d"]
    A -- b --> AB["ab"]
    A -- c --> AC["ac"]
    A -- d --> AD["ad"]
    B -- c --> B_C["bc"]
    B -- d --> BD["bd"]
    C -- d --> CD["cd"]
    A -- b --> ABC["abc"]
    A -- c --> AC_C["acc"]
    A -- d --> A_CD["acd"]
    B -- c --> B_CD["bcd"]
    B -- d --> B_D["bd"]
    C -- d --> C_D["cd"]
    A -- b --> ABCD["abcd"]
    A -- c --> A_CD_C["acdc"]
    A -- d --> A_CD_D["acd"]
    B -- c --> B_CD_C["bcda"]
    B -- d --> B_CD_D["bcdb"]
    C -- d --> C_CD_C["ccda"]
    C -- d --> C_CD_D["ccdb"]
    D --> D_C["dc"]
    D --> D_B["bd"]
    D --> D_CD["cd"]
    D --> D_CD_C["cdca"]
    D --> D_CD_D["cdcb"]
    D --> D_CD_CD["cdcd"]
  
```

Activity

Is Subsequence

eg) Input:  $s = "abc"$ ,  $t = "ahbgdc"$

eg) Input:  $s = "abc"$ ,  $t = "axyczb"$  false

eg) Input:  $s = "axb"$ ,  $t = "apqrab"$  false

eg)  $s = "abc"$  isSubset  $t = "ahbgdc"$  true

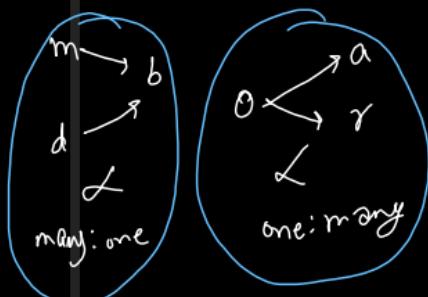
eg)  $s = "acb"$  isSubset  $t = "ahbgdc"$  false

eg)  $s = "axc"$  isSubset  $t = "ahbgdc"$  false

Given two strings  $s$  and  $t$ , determine if they are isomorphic.

Two strings  $s$  and  $t$  are isomorphic if the characters in  $s$  can be replaced to get  $t$ .

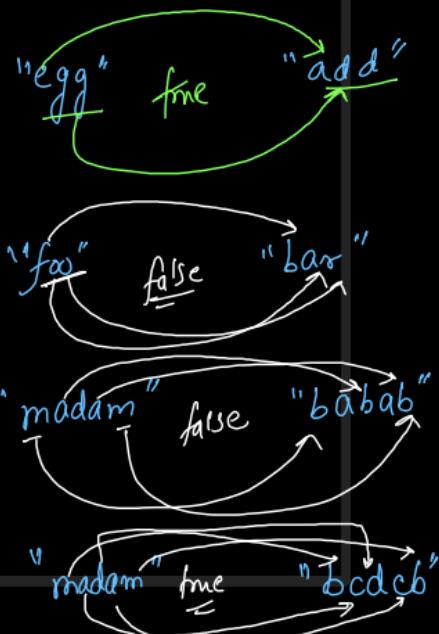
All occurrences of a character must be replaced with another character while preserving the order of characters. No two characters may map to the same character, but a character may map to itself.



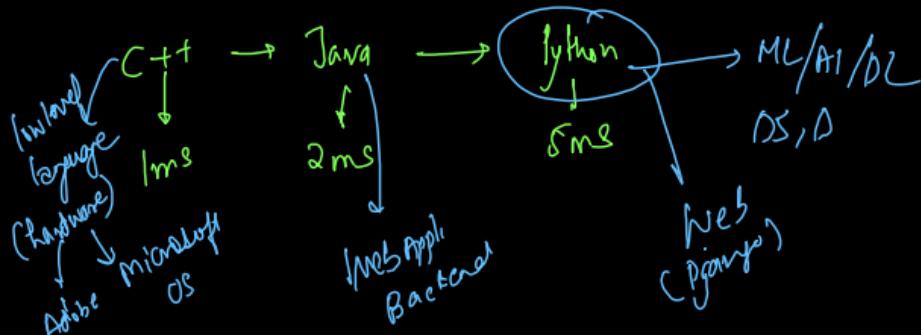
**Input:**  $s = \text{"paper"}$ ,  $t = \text{"title"}$   
**Output:** true

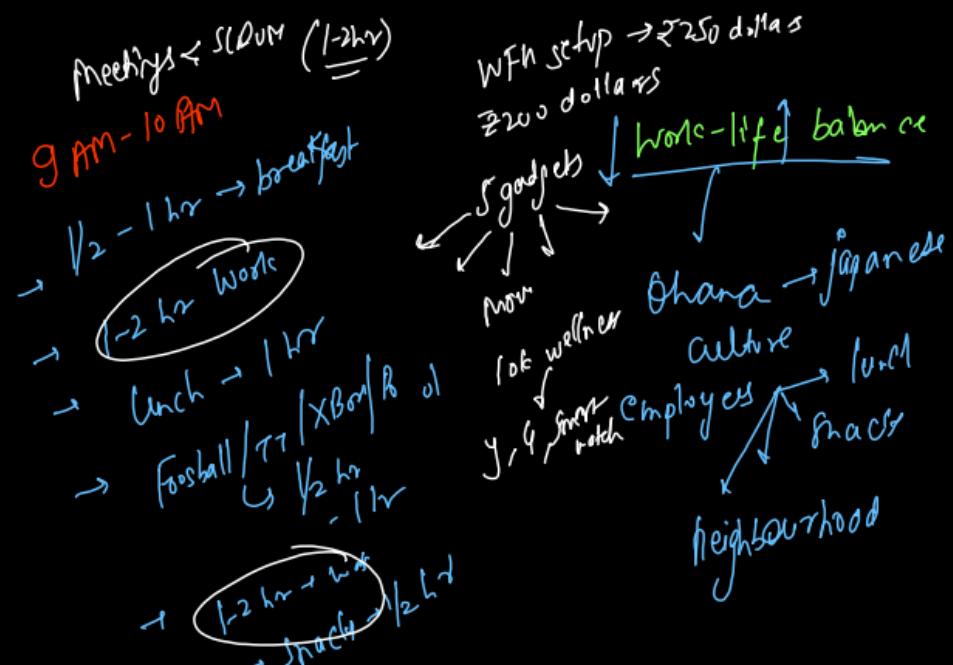
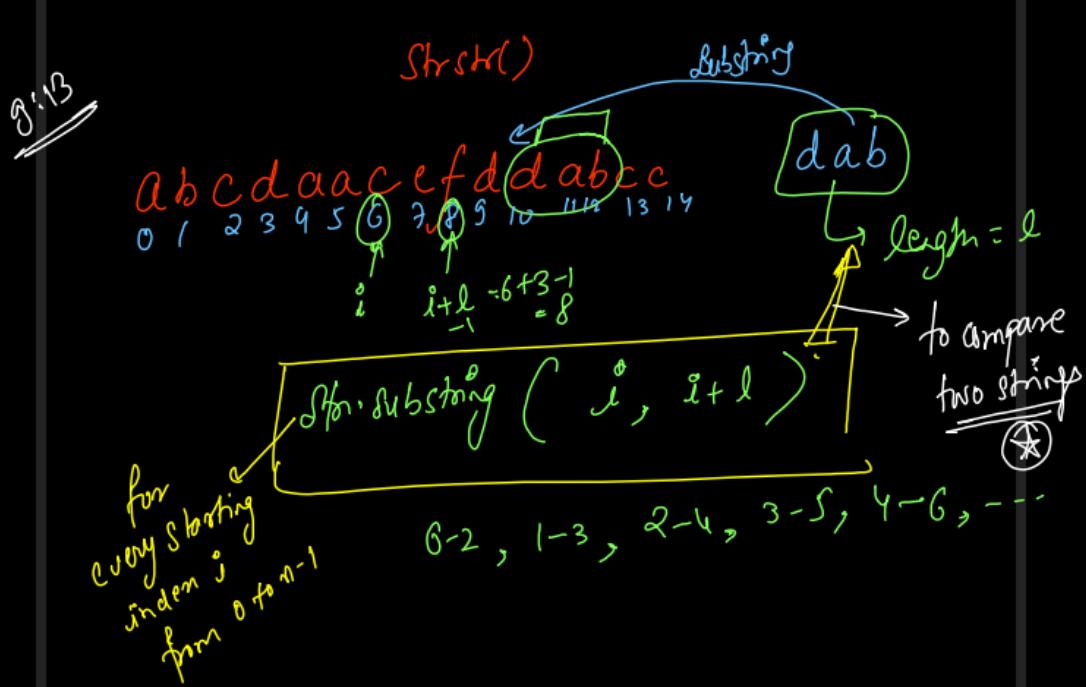
$p \rightarrow t$   
 $a \rightarrow i$   
 $e \rightarrow l$   
 $r \rightarrow c$

### Isomorphic Strings



Ans

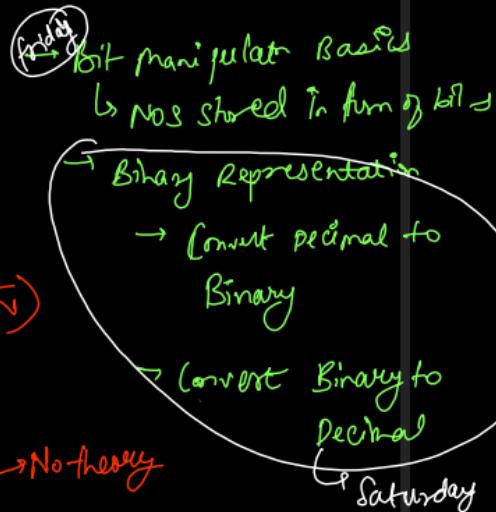




→ Brute force  $\rightarrow O(N \cdot M)$

```
for(int i=0; i<= actual.length()-required.length(); i++){
    if(actual.substring(i, i + required.length()).equals(required) == true){
        return i;
    }
}
return -1;
```

- ✓ Modular Arithmetic
- ✓ Prime Factorization
- ✓ Check No is prime or not
  - ↓
  - $O(N)$
  - $O(\frac{N}{2})$
  - $O(\sqrt{N})$
- ✓ GCD & LCM



## Modulo Operator

$(a/b) \rightarrow$  It gives remainder when a is divided by b.

If  $a < b \Rightarrow a \% b = a$

$$1 \% 100 = 1$$

1% Integer max-value = 1

$$2 \% 100 = 2$$

$$2 \% 100 = 2$$

$$3 \% 100 = 3$$

$$3 \% 100 = 3$$

$$4 \% 100 = 4$$

$$4 \% 100 = 4$$

⋮

$$99 \% 100 = 99$$

⋮

$$(2^{31}-1) = 2^{31} - 2 \% 2^{31}-1 = 2^{31}-2$$

Remainder  
order  
of  
numbers

$$\leftarrow \text{division by composite no}$$
  
 $11 \% 10 = 1$

Division by prime no

$$12 \% 10 = 2$$

$$14 \% 13 = 1$$

$$13 \% 10 = 3$$

$$24 \% 13 = 2$$

$$14 \% 10 = 4$$

$$16 \% 13 = 3$$

$$15 \% 10 = 5$$

$$28 \% 13 = 4$$

$$16 \% 12 = 8$$

$$1 \% 13 = 1$$

$$17 \% 10 = 7$$

$$1 \% 13 = 2$$

$$18 \% 10 = 8$$

$$25 \% 13 = 12$$

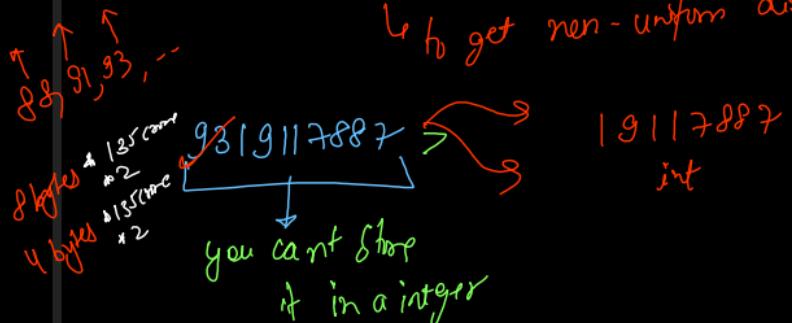
$$19 \% 10 = 9$$

$$28 \% 13 = 0$$

$$20 \% 10 = 0$$

$$39 \% 13 = 0$$

→ Modular operation should be performed using  
a "large" and "prime" no  
↳ to get non-uniform distribution.



Activator

### Properties of modular Arithmetic

$$\textcircled{1} \quad (a+b) \% m = (\underline{a \% m} + \underline{b \% m}) \% m$$

ex ①  $(7+12) \% 10 \rightarrow 19 \% 10 = 9$   
 $\underline{(7 \% 10 + 12 \% 10)} \% 10 = \underline{(7+2 \% 10)} \% 10 = 9 \% 10 = 9$

②  $(100+129) \% 3 \rightarrow 229 \% 3 = 2$   
 $\rightarrow \underline{(100 \% 3 + 129 \% 3)} \% 3 = \underline{(1+1 \% 3)} \% 3 = 2$

$$\textcircled{2} \quad (a \times b)^{\frac{1}{m}} = \underbrace{(a^{\frac{1}{m}} \times b^{\frac{1}{m}})}_{\substack{a \\ b \\ \underbrace{\phantom{a} \times \phantom{b}}_{(10 \times 12)}}}^{\frac{1}{m}}$$

$$\textcircled{2} \quad (10 \times 12)^{\frac{1}{7}} \xrightarrow{120^{\frac{1}{7}} = 1} \underbrace{(10^{\frac{1}{7}} \times 12^{\frac{1}{7}})^{\frac{1}{7}}}_{= (3 \times 5)^{\frac{1}{7}}} = 15^{\frac{1}{7}}$$

$$\textcircled{2} \quad (13 \times 17)^{\frac{1}{5}} \xrightarrow[=1]{221^{\frac{1}{5}}} \underbrace{(13^{\frac{1}{5}} \times 17^{\frac{1}{5}})^{\frac{1}{5}}}_{= (3 \times 2)^{\frac{1}{5}}} = 1$$

$$\textcircled{3} \quad (a - b)^{\frac{1}{m}} = \underbrace{(a^{\frac{1}{m}} - b^{\frac{1}{m}})}_{+m}^{\frac{1}{m}}$$

to avoid negative  
vs getting  
modulo

$$\textcircled{2} \quad (3^9 - 11)^{\frac{1}{4}} = 28^{\frac{1}{4}} = 0$$

$$(3^9 - 11^4 + 4)^{\frac{1}{4}} = (3 - 3 + 4)^{\frac{1}{4}} = 4^{\frac{1}{4}} = 0$$

$$\textcircled{2} \quad (12 - 39)^{\frac{1}{4}} \xrightarrow{-27^{\frac{1}{4}} = 1}$$

$$(12^{\frac{1}{4}} - 39^{\frac{1}{4}} + 4)^{\frac{1}{4}} = (0 - 3 + 4)^{\frac{1}{4}} = 1^{\frac{1}{4}} = 1$$

$$13 = 4 \cdot 3 + 1$$

$$\begin{array}{r} 4 \sqrt{13} \\ \underline{-12} \\ \hline 1 \end{array}$$

$$d = m+n + \textcircled{2} \quad d \nmid m$$

$$15 = 4 \cdot 3 + 3$$

$$\begin{array}{r} 4 \sqrt{15} \\ \underline{-12} \\ \hline 3 \end{array}$$

$$\begin{array}{r} 4 \sqrt{20} \\ \underline{-16} \\ \hline 4 \end{array} \quad 2 \nmid 4 - 2$$

$$2 = 4 \cdot 0 + 2$$

↓ ↓ ↑ ↓  
divisor quotient remainder

$\text{Theorem } 5$  is not applicable

$$(a/b)^{1/m} \neq ((a^{1/m}) / (b^{1/m}))^{1/m}$$

$$\frac{3^9}{17}^{1/4} = (2^{20})^{1/4} = \textcircled{2}$$

$$((3^9/17) / (17^{1/4}))^{1/4} = (3/1)^{1/4} = \textcircled{3}$$

$$(a/b)^{1/m} = ((a^{1/m}) * (b^{-1/m}))^{1/m}$$

Multiplicative inverse of b

They are individually fit in integer

$$\left( \frac{2000000000}{Var1} + \frac{2000000000}{Var2} \right) \% 17$$

$D+1 = -P$

$$(a+b) \% m$$

$$\left( \frac{4000000000}{17} \right) \% 17$$

*(This is not in integer range)*

$$= (-16) \% 17$$

$$= garbage$$

$$(a \% m + b \% m) \% m$$

$$\left( \left( \frac{2^{31}-1}{17} \right) \% 17 + \left( \frac{2^{31}-1}{17} \right) \% 17 \right) \% 17$$

$$= (14 + 14) \% 17$$

$$= 28 \% 17$$

$$= 11$$

$$\left( 2^{31} - 1 \approx 2^{31} \right) \% 17$$

$2^{31} - 1 \approx 2^{31}$

$10 digits$

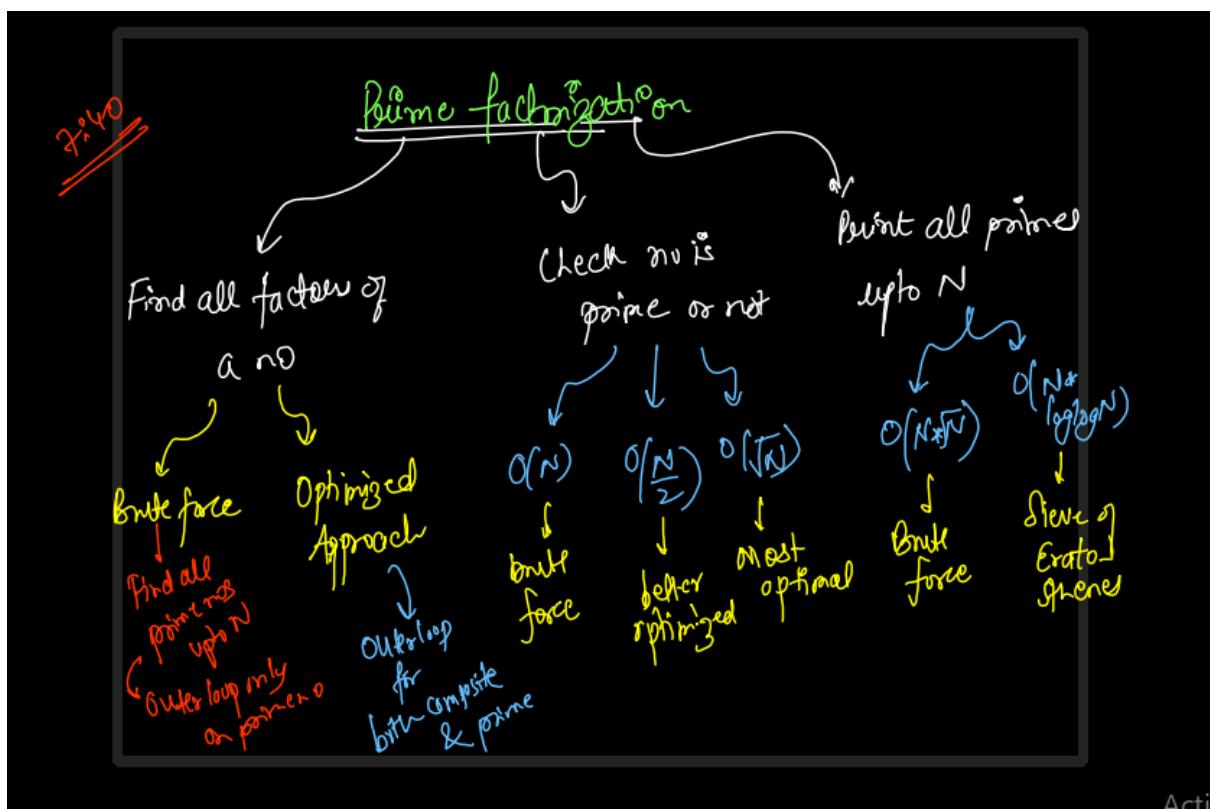
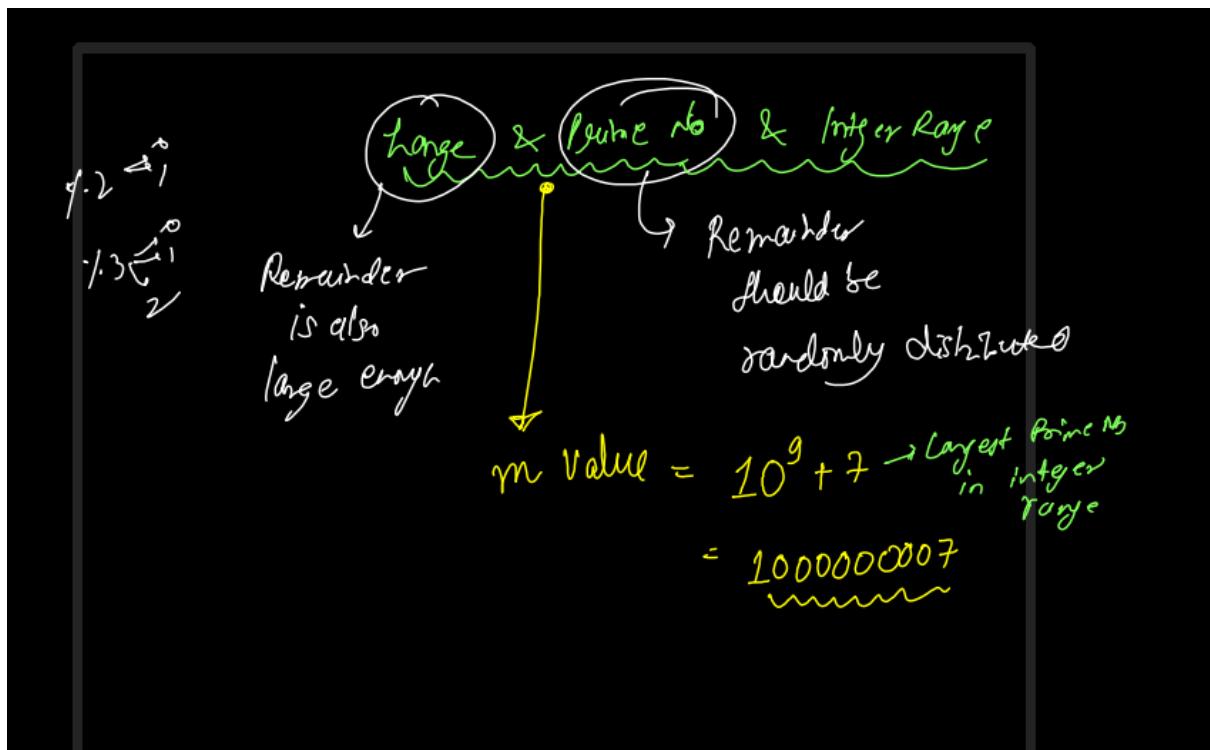
$$= (2^{31}) \% 17$$

$$= (overflow) \% 17 = garbage$$

$$\left( (2^{31}) \% 17 + (2^{31}) \% 17 \right) \% 17$$

$$= (14 + 14) \% 17 = 19 \% 17 = 9$$

Acti



Acti

### Prime Factorization

2	120
2	60
2	30
3	15
5	5
	1

$$120 = 2 \times 2 \times 3 \times 5$$

2	1386
3	693
3	231
7	77
11	11
	1

$$1386 = 2 \times 3 \times 3 \times 7 \times 11$$

~~2, 3, 5, 7, 9, 11, 13, 17~~  
Store all prime  
no's in array

$O(N^2)$  worst case  
Try to divide N  
by each prime factor

```
// Prime Factorization
int n = sc.nextInt();

for(int fact=2; fact<=N; fact++){
    // fact is a prime factor of N
    while(N % fact == 0){
        N = N / fact;
        System.out.print(fact + " ");
    }
}
```

Divide N by fact  
as long as it is  
divisible

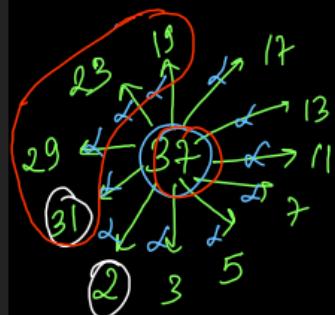
fact = 2	5940 / n
2	2970
fact = 3	1485
3	495
3	165
fact = 5	55
5	11
	1

2, 3, 4, 5, 6, 7,  
8, 9, 10, 11

② Check whether a no is

prime or not

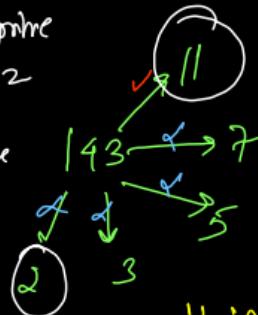
only 2 factors  $\leftarrow$  No itself



It is a prime

Start  $\rightarrow$  smallest prime  
no  $\rightarrow 2$

end  $\rightarrow$  largest prime  
no  $\rightarrow N$



If is not prime  
or it is  
Composite

$O(N)$

```
if(N <= 1) return 0;    Q - - - - (N-1)
```

```
for(int fact=2; fact<N; fact++){
    if(N % fact == 0){
        // Fact is a factor of N
        // True  $\rightarrow$  Prime
        // N is Composite (not prime)
        return 0;
    }
}

return 1;
```

Activate

```

static int isPrime(int N){
    if(N <= 1) return 0;

    for(int fact=2; fact<=N/2; fact++){
        if(N % fact == 0){
            // Fact is a factor of N
            // N is Composite (not prime)
            return 0;
        }
    }

    return 1;
}

```

# Optimization

if  $\text{fact} > \frac{N}{2} \Rightarrow$

$2 * \text{fact} > N$

and also

$\text{fact} \neq N$

$\text{factors} > N/2$

should not  
be checked

$\Leftarrow N \text{ is not divisible}$   
by fact

$O(N^2)$

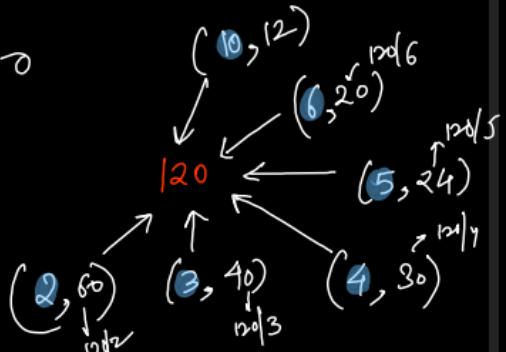
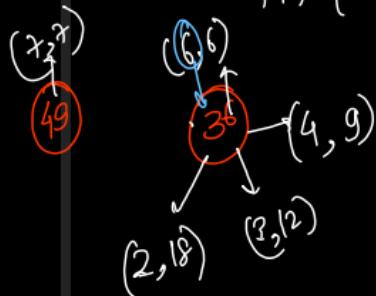
Activation

# most  
optimised  
approach

~~Property~~ Factors always occur in pairs

$$N \% a == 0 \Rightarrow N = a * b$$

$$N \% (N/a) == 0$$



```

 $\Theta(\sqrt{N})$ 
static int isPrime(int N){
    if(N <= 1) return 0;

    int sq = (int)Math.sqrt(N);

    for(int fact=2; fact<=sq; fact++){
        if(N % fact == 0){
            // Fact is a factor of N  $\Theta(3)$ 
            // N is Composite (not prime)
            return 0;
        }
    }

    return 1;
}

```

$\textcircled{1}$   $2 - (N-1)$  factors comparable greater than  $N$  if  $N$  is prime  
 $\textcircled{2}$   $2 - \frac{N}{2}$  ↑ if  $\text{fact} > \sqrt{N}/2$   
 $\textcircled{3}$   $2 - \sqrt{N}$  ↓ if  $\text{fact} \leq \sqrt{N}$   
 Since factors occur in pairs, smaller factor will be  $\leq \sqrt{N}$

$N = 101$   
 $\textcircled{99}$  iterations

$\textcircled{50}$  iterations

$\textcircled{10}$  iterations

Count primes till  $N$

$$N = 30$$

2, 3, 5, 7, 11, 13, 17, 19, 23, 29  $\Rightarrow \textcircled{10}$

```

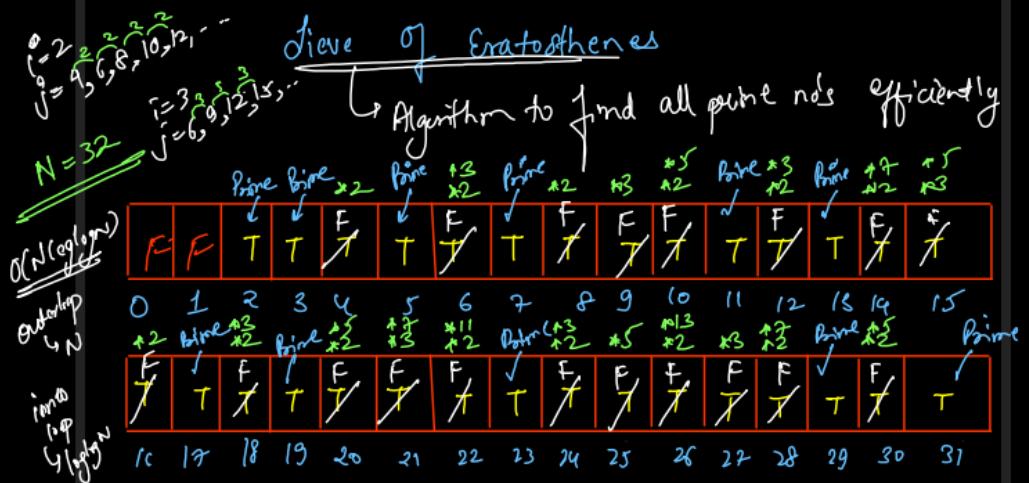
public boolean isPrime(int n){
    for(int fact=2; fact<=(int)Math.sqrt(n); fact++){
        if(n % fact == 0) return false;
    }
    return true;
}

public int countPrimes(int n) {
    int count = 0;

    // Check Each No, If it is prime, then increase the count
    for(int i=2; i<n; i++){
        if(isPrime(i) == true){
            count++;
        }
    }
    return count;
}

```

$\Theta(N * \sqrt{N})$   
 brute force



If no is prime → true  
else (composite) → false

Inner loop { Multiples of prime as composite  
↳ ran for only prime nos

```
public int countPrimes(int n) {
    // Sieve of Eratosthenes
    boolean[] prime = new boolean[n + 1];
    for(int i=2; i<n; i++) prime[i] = true;

    int count = 0;
    for(int i=2; i<n; i++){
        if(prime[i] == false) continue;

        count++;
        for(int j=2*i; j<n; j = j + i)
            prime[j] = false;
    }

    return count;
}
```

$\Theta(N \log \log N)$   
Most optimized approach

Assume all no's are prime ↳ for i = 4, 6, 8, 9  
 ↳ if no is not prime (composite)  
 ↳ all of its multiples are already false  
 ↳ do not run the inner loop  
 ↳ if no is prime  
 ↳ increase count  
 ↳ make all its multiples as false

```

public int countPrimes(int n) {
    // Sieve of Eratosthenes
    boolean[] prime = new boolean[n - 1];
    for (int i=2; i<n; i++) prime[i] = true;

    int count = 0;
    for (int i=2; i<n; i++){
        if(prime[i] == false) continue;

        count++;
        for (int j=2*i; j<n; j+=i)
            prime[j] = false;
    }

    return count;
}

```

} composite  
} prime

$i=2$   
 $j = 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30$

$i=3$   
 $j = 6, 9, 12, 15, 18, 21, 24, 27, 30$

$i=4$   $\otimes$   $i=5$   $j = 10, 15, 20, 25, 30$

	prime														
0															
1															
2	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
3	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
4	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
5	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
6	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
7	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
8	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
9	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
10	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
11	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
12	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
13	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
14	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
15	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
16	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
17	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
18	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
19	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
20	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
21	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
22	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
23	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
24	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
25	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
26	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
27	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
28	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
29	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T
30	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
31	T	F	T	F	T	F	T	F	T	F	T	F	T	F	T

$\underline{\underline{N=32}}$

GCD or HCF  
↳ Greatest Common Divisor

$$\begin{array}{r}
 \textcircled{2} \Big| 80 = 12 \times 5 = 12 \times 4 \\
 \textcircled{2} \Big| 30, 24 \\
 \textcircled{3} \Big| 15, 12 \\
 \hline
 5, 4
 \end{array}$$

~~Prime factorization of both numbers together~~  
 $2 \times 2 \times 3 = \textcircled{12}$

Highest Common Factor

$$\begin{array}{r}
 48 \overline{) 60} \quad 1 \\
 -48 \\
 \hline
 12 \overline{) 48} \quad 4 \\
 -48 \\
 \hline
 0
 \end{array}$$

ans

long Division Method

Actin

$$(2+2+3+3+5) = 180$$

$$2+3+3+3+5*7 = 1890$$

$$2+3*3+5 = 10*9 = 90$$

$$2+3+5*7 = 210$$

$$5*11 = 55$$

$$\frac{d}{n} \quad \begin{array}{r} 1890 \\ -180 \\ \hline 90 \end{array}$$

$$\frac{d}{n} \quad \begin{array}{r} 210 \\ -165 \\ \hline 45 \end{array}$$

$$\frac{d}{n} \quad \begin{array}{r} 55 \\ -45 \\ \hline 10 \end{array}$$

$$\frac{d}{n} \quad \begin{array}{r} 45 \\ -40 \\ \hline 5 \end{array}$$

$$\frac{d}{n} \quad \begin{array}{r} 10 \\ -10 \\ \hline 0 \end{array}$$

$\boxed{\gcd(n, d) = \gcd(d, n \% d)}$

```

public int gcd(int n, int d)
{
    if(n % d == 0) return d;
    return gcd(d, n % d);
}

```

$\text{num} = 210, \text{den} = 55$   
 $\downarrow$   
 $\frac{210}{55} = \frac{55 \times 3 + 45}{55}$   
 $\text{num} \quad \text{den}$

$\text{num} = 55, \text{den} = 45$   
 $\downarrow$   
 $\frac{55}{45} = \frac{45 + 10}{45}$   
 $N \quad D \quad R$

$N = 45, D = 10$   
 $\downarrow$   
 $\frac{45}{10} = \frac{10 \times 4 + 5}{10}$   
 $N \quad D \quad R$

$N = 10, D = 5$   
 $10 \times 1 = 10 \Rightarrow 5 \text{ is gcd}$

$$\text{num} = 4, \text{ den} = 16$$

$$4 = 16 \times 0 + 4$$

$$\text{num} = 16, \text{ den} = 4$$

$$\begin{array}{r} 16 \sqrt{4} \\ -0 \\ \hline 4 \end{array}$$
  
$$\begin{array}{r} 4 \sqrt{16} \\ -16 \\ \hline 0 \end{array}$$

$$\text{num} = 48, \text{ den} = 60$$

$$\begin{array}{r} 60 \sqrt{48} \\ -48 \\ \hline 0 \end{array}$$
  
$$\begin{array}{r} 48 \sqrt{60} \\ -48 \\ \hline 0 \end{array}$$
  
$$\begin{array}{r} 12 \sqrt{48} \\ -48 \\ \hline 0 \end{array}$$

Activation

$$\cancel{\text{HCF}} \text{LCM}(48, 60) = \frac{48 * 60}{\cancel{12}_{\text{HCF}}} = 240$$

$$\begin{array}{l} 48 = \cancel{12} \cancel{4} \\ 60 = \cancel{12} \cancel{5} \end{array}$$

$$\text{LCM} = 12 * 4 * 5 = 240$$

$$= \frac{(12 * 4) * (12 * 5)}{12} = \frac{48 * 60}{12}$$

$$\cancel{\text{HCF}} \text{LCM} = \frac{a * b}{\text{HCF}}$$

$$a * b = \text{LCM}(a, b) * \text{HCF}(a, b)$$

## Binary Exponentiation

$2^p \Rightarrow 2 * 2 * 2 * \dots$  p times  $\rightarrow \underline{\underline{O(p) \text{ time}}}$

$$2^0 \Rightarrow 1$$

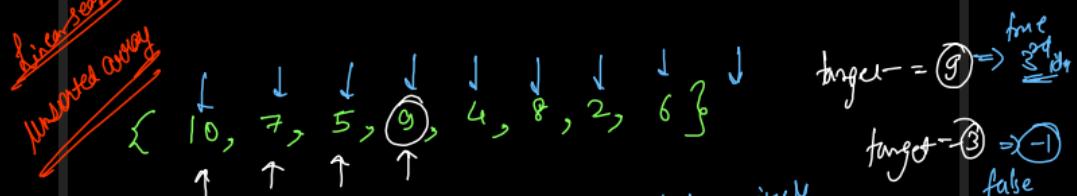
$$2^1 \Rightarrow 1 * 2 = 2$$

$$2^2 \Rightarrow 1 * 2 * 2 = 4$$

$$2^3 \Rightarrow 1 * 2 * 2 * 2 = 8$$

Linear search  
Unsorted array

## Binary Search Algorithm



best case  $\rightarrow O(1)$  in the 0th index itself

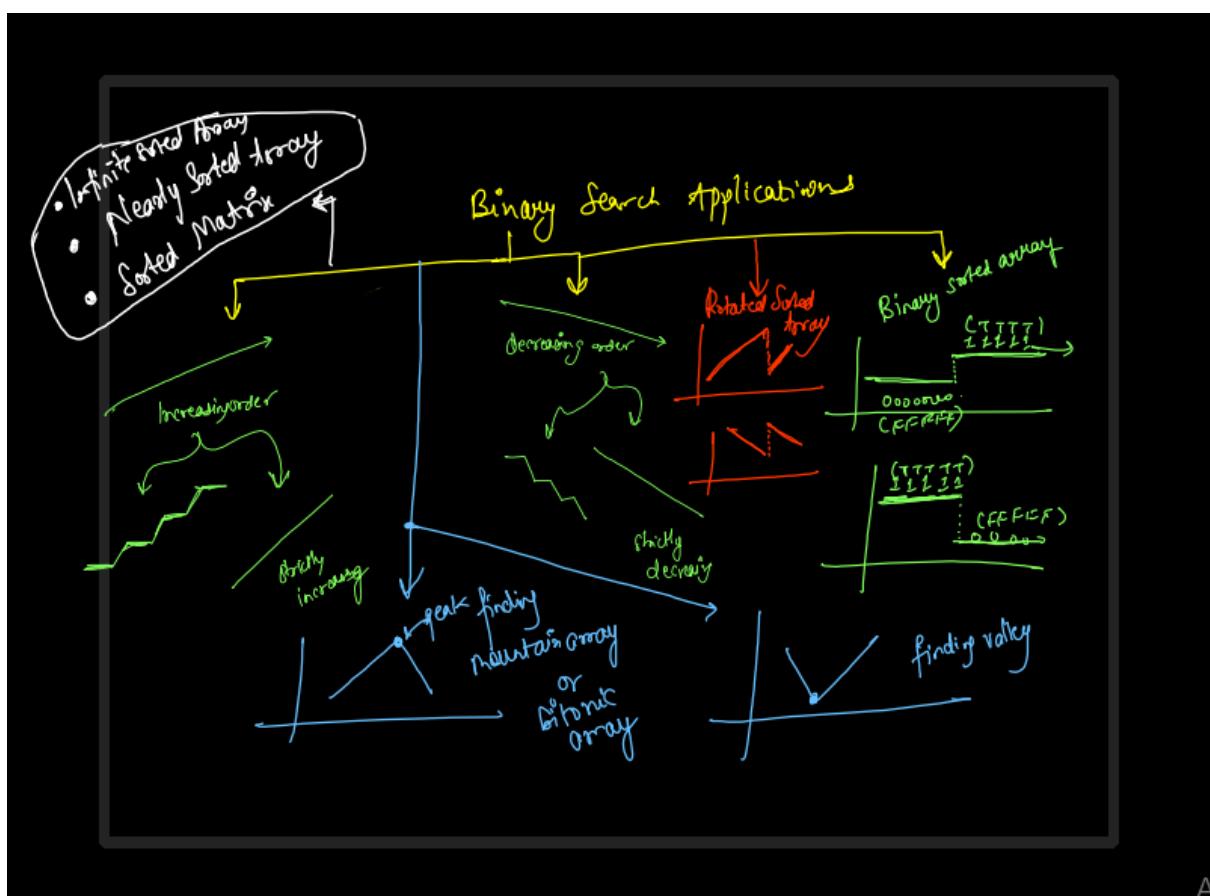
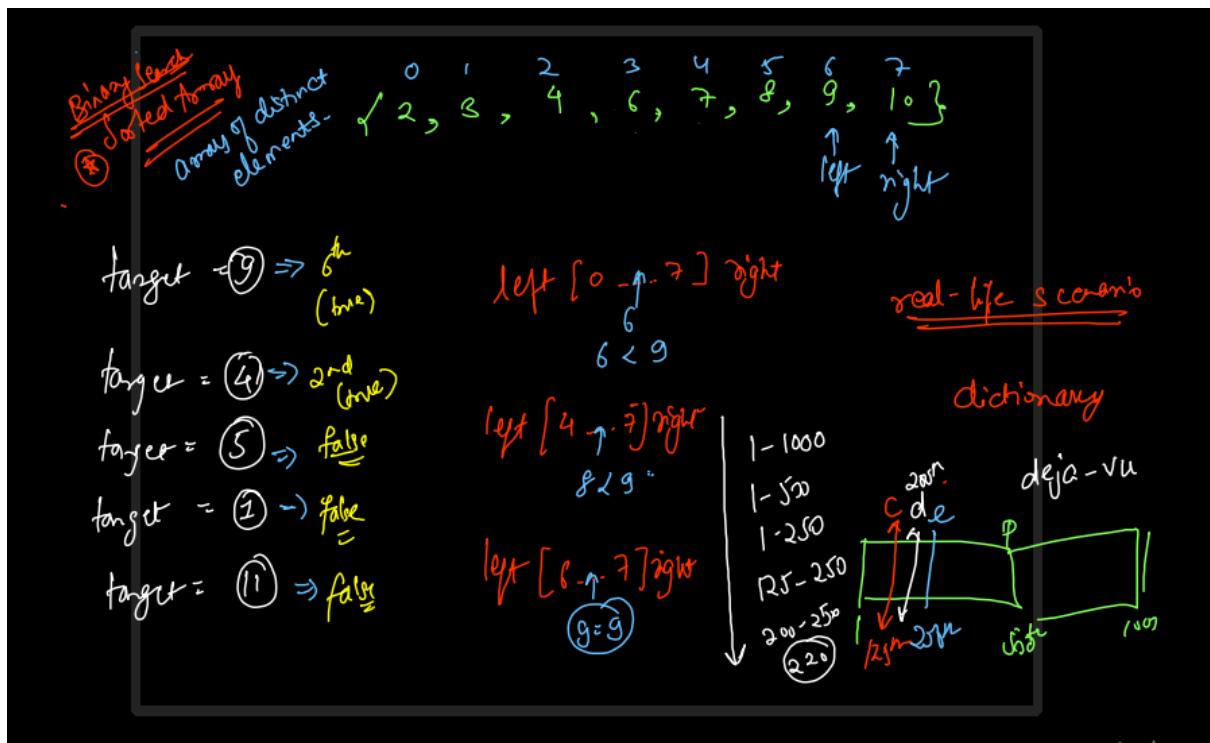
worst case  $\rightarrow O(n)$  unsuccessful search

Avg case  $\rightarrow O(n) = \frac{n}{2}$

$$N \rightarrow N-1 \rightarrow N-2 \rightarrow N-3 \rightarrow N-4$$

$$N-5$$

$$O^{-1}$$



target = 40

✓ 0 1 2 3 4 5 6 7  
✓ 20, 30, 40, 60, 70, 80, 90, 100  
↑  
left = 0      mid =  $\frac{(left+right)}{2}$       right =  $n-1 = 8-1 = 7$

40 < 60       $\leftarrow \begin{pmatrix} 20, 30, 40, 60 \\ 70, 80, 90, 100 \end{pmatrix}$   
target < arr[mid] < arr[right]

→ discard left

✓ 0 1 2 3 4 5 6 7  
✓ 20, 30, 40, 60, 70, 80, 90, 100  
↑  
left      mid      right  
mid =  $(0+2)/2 = 1^{\text{st}} \text{ index}$

discard left

✓ 20 30 40

✓ 0 1 2 3 4 5 6 7  
left      mid      right  
mid =  $\frac{(2+2)}{2} = 2$

40 = 40      True

Activate  
Go to Sett

target = 105

✓ 0 1 2 3 4 5 6 7 8 9  
✓ 20, 40, 50, 60, 100, 110, 120, 130, 150  
↑  
right      left  
right > left  
unsuccessful

~~Sig<sup>e</sup>~~  $N \rightarrow N/2 \rightarrow N/4 \rightarrow N/8 \rightarrow N/16 \dots \rightarrow 0$

```
public int search(int[] nums, int target) {  
    int left = 0, right = nums.length - 1;  
  
    while(left <= right){  
        int mid = (left + right) / 2;  
  
        if(nums[mid] == target) return mid;  
        else if(nums[mid] < target)  
            left = mid + 1; // Discard the Left Range  
        else right = mid - 1; // Discard the Right Range  
    }  
  
    return -1;  
}
```

{  
    Best case  $\rightarrow O(1)$   
    Worst case  $\rightarrow O(\log_2 n)$   
    Avg case  $\rightarrow O(\log_2 n)$

Time Complexity  $\rightarrow O(\log_2 n)$

~~int mid = left + (right - left) / 2;~~

$$\begin{aligned} l + \left( \frac{r-l}{2} \right) &= l + \frac{r}{2} - \frac{l}{2} = \frac{l}{2} + \frac{r}{2} \\ &= \frac{1}{2}(l+r) \end{aligned}$$

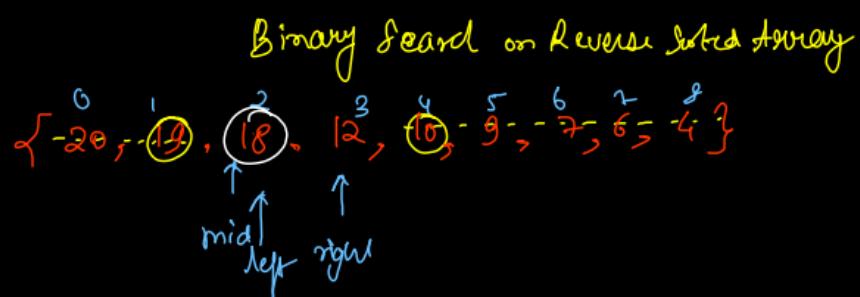
*Integer Overflow*

$$\begin{aligned} l &\approx 10^{10}, r = 2 \cdot 10^{10} \\ l + \frac{(r-l)}{2} &= 2 \cdot 10^{10} + \frac{(2 \cdot 10^{10} - 10^{10})}{2} = 2 \cdot 10^{10} \checkmark \end{aligned}$$

Activate

	Time Complexity Chart Linear Search $\Rightarrow O(n)$	Binary Search $\Rightarrow O(\log_2 n)$ Divide & Conquer
$N = 2^0$	1	1
$N = 2^1$	2	2
$N = 2^2$	4	2
$N = 2^3$	8	3
$N = 2^4$	16	4
$N = 2^5$	32	5
$N = 2^6$	64	6

Activation



target = 18

```
public int searchInDecreasing(int[] nums, int target) {
    int left = 0, right = nums.length - 1;

    while(left <= right){
        int mid = left + (right - left) / 2;

        if(nums[mid] == target) return mid;
        else if(nums[mid] > target)
            left = mid + 1; // Discard the Left Range
        else right = mid - 1; // Discard the Right Range
    }

    return -1;
}
```

Activation

- ✓ First Occurrence → leftmost occurrence
  - ✓ Last Occurrence → rightmost occurrence
  - ✓ Count Occurrences →  $i - j + 1$
  - ✓ Lower Bound → target  $\leq \lceil \text{target} \rceil$
  - ✓ Upper Bound (Just Greater - Ceil) →  $\lceil \text{target} \rceil$
  - ✓ Floor of a No (Just Smaller)
- Binary Sorted Array  
 ✓ Transition Point  
 ✓ First Bad Version? (Google)  
 ✓ Rotated Sorted Array  
 ✓ Mountain Array

- ~~Topic Help~~
- Time & Space Complexity
  - Bit Manipulation
  - Binary Representation  $\xleftarrow{\quad} B \rightarrow D$   $D \rightarrow B$
  - Binary Exponentiation

*First Occurrence* { Increasing → Duplicate Elements }

	0	1	2	3	4	5	6	7	8	9	10
	10	10	10	20	20	30	40	40	40	40	40

$$\text{ans(FI)} = \cancel{1} \cancel{2} \cancel{3}$$

target = 20

$$\text{ans(FI)} = \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} \cancel{6}$$

target = 40

$$\text{ans(FI)} = \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} \cancel{6}$$

target = 10

$$\text{ans(FI)} = \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} \cancel{6}$$

target = 35

$$F_1 = 718$$

$$L_1 = 718$$

Activate

```
int[] ans = new int[2];
ans[0] = ans[1] = -1;

// First Occurrence
int left = 0, right = nums.length - 1;
while(left <= right){
    int mid = left + (right - left) / 2;

    if(nums[mid] == target){
        ans[0] = mid;
        // Store the current occurrence
        right = mid - 1;
        // continue the binary search to the left range
    } else if(nums[mid] < target){
        left = mid + 1;
    } else {
        right = mid - 1;
    }
}
```

```
// Last Occurrence
left = 0; right = nums.length - 1;
while(left <= right){
    int mid = left + (right - left) / 2;

    if(nums[mid] == target){
        ans[1] = mid;
        // Store the current occurrence
        left = mid + 1;
        // continue the binary search to the right range
    } else if(nums[mid] < target){
        left = mid + 1;
    } else {
        right = mid - 1;
    }
}

return ans;
```

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

$L1(40)$

$target = 40$

$ans = \cancel{1} \cancel{8} \cancel{9} \cancel{10}$

$L1(20)$

$target = 20$

$ans = \cancel{1} \cancel{2} \cancel{4}$

```
// Last Occurrence
left = 0; right = nums.length - 1;
while(left <= right){
    int mid = left + (right - left) / 2;

    if(nums[mid] == target){
        ans[1] = mid;
        // Store the current occurrence
        left = mid + 1;
        // continue the binary search to the right range
    } else if(nums[mid] < target){
        left = mid + 1;
    } else {
        right = mid - 1;
    }
}

return ans;
```

Activity

Count Occurrences

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

$$C1(10) = 3 = L1(10) - F1(10) + 1$$

$$C1(20) = 2 = L1(20) - F1(20) + 1$$

$$C1(30) = 1 = L1(30) - F1(30) + 1$$

$$C1(40) = 5 = L1(40) - F1(40) + 1$$

$$C1(35) = 0 \quad \text{circled } L1(35) = -1 \quad \text{circled } F1(35) = -1$$

## Lower Bound & Upper Bound

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

Lower Bound

Search Insert Position

$$LB(10) = 0, LB(20) = 3 ; LB(30) = 5 ; LB(40) = 6$$

$$LB(5) = 0, LB(18) = 3, LB(25) = 5, LB(35) = 6, LB(45) = \cancel{11}$$

array

If the target is found, then first occurrence  
is the lower bound

If target is not found, just greater value  
or ceil value's first occurrence

Activation

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

```
ss Solution {
public int searchInsert(int[] nums, int target) {
    int ans = nums.length;
    int left = 0, right = nums.length - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;

        if(nums[mid] >= target){
            ans = mid;
            // Store the current occurrence
            right = mid - 1;
            // continue the binary search to the left range
        } else if(nums[mid] < target){
            left = mid + 1;
        }
    }

    return ans;
}}
```

$LB(35)$

ans = ~~11~~ ~~6~~

$LB(5)$

ans = ~~11~~ ~~0~~

$LB(45)$

ans = 11

Activation

## Upper Bound

0	1	2	3	4	5	6	7	8	9	10
30	30	10	20	20	30	40	40	40	40	40

Upper bound  $\rightarrow$  just greater's value first occurrence  
irrespective of the target occurrence

(10)  $\Rightarrow$  3<sup>rd</sup>      (20)  $\Rightarrow$  5<sup>th</sup>      (30)  $\Rightarrow$  6<sup>th</sup>      (40)  $\Rightarrow$  11<sup>th</sup>  
(or last)

(5)  $\Rightarrow$  0<sup>th</sup>      (18)  $\Rightarrow$  3<sup>rd</sup>      (25)  $\Rightarrow$  5<sup>th</sup>      (45)  $\Rightarrow$  11<sup>th</sup>  
(or -1<sup>th</sup>)

Activate \

```
// Lower Bound
public int searchInsert(int[] nums, int target) {
    int ans = nums.length;
    int left = 0, right = nums.length - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;

        if(nums[mid] >= target){
            ans = mid;
            // Store the current occurrence
            right = mid - 1;
            // continue the binary search to the left range
        } else {
            left = mid + 1;
        }
    }
    return ans;
}
```

```
// Upper Bound
public static int ceil(int[] nums, int target){
    int ans = nums.length;
    int left = 0, right = nums.length - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;
        if(nums[mid] > target){
            ans = mid;
            // Store the current occurrence
            right = mid - 1;
            // continue the binary search to the left range
        } else {
            left = mid + 1;
        }
    }
    return ans;
}
```

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

```
// Upper Bound
public static int ceil(int[] nums, int target){
    int ans = nums.length;
    int left = 0, right = nums.length - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;
        if(nums[mid] > target){
            ans = mid;
            // Store the current occurrence
            right = mid - 1;
            // continue the binary search to the left range
        } else {
            left = mid + 1;
        }
    }
    return ans;
}
```

UB(30)

ans = ~~11~~ ↴ 6

UB(18)

ans = ~~11~~ ↴ 3

UB(40)

ans = 11 (arr.length)

8.27

Assignment → last occurrence of that  
Floor of a No (Just smaller value)

0	1	2	3	4	5	6	7	8	9	10
10	10	10	20	20	30	40	40	40	40	40

$$\text{floor}(40) = 5^{\text{th}} \{ \text{l1 of } 30 \}$$

$$\text{floor}(45) = 10^{\text{th}} \{ \text{l1 of } 40 \}$$

$$\text{floor}(30) = 4^{\text{th}} \{ \text{l1 of } 20 \}$$

$$\text{floor}(35) = 5^{\text{th}} \{ \text{l1 of } 30 \}$$

$$\text{floor}(20) = 2^{\text{nd}} \{ \text{l1 of } 10 \}$$

$$\text{floor}(25) = 4^{\text{th}} \{ \text{l1 of } 20 \}$$

$$\text{floor}(10) = (-1) \{ \text{no floor value} \}$$

$$\text{floor}(15) = 2^{\text{nd}} \{ \text{l1 of } 10 \}$$

$$\text{floor}(5) = (-1) \{ \text{no floor value} \}$$

~~Time  $\rightarrow O(n)$~~

```
// n is the size of array
static int findFloor(long arr[], int n, long x)
{
    int left = 0, right = n - 1;
    int ans = -1;

    while(left <= right){
        int mid = left + (right - left) / 2;
        if(arr[mid] <= x){
            ans = mid;
            left = mid + 1;
        } else {
            right = mid - 1;
        }
    }

    return ans;
}
```

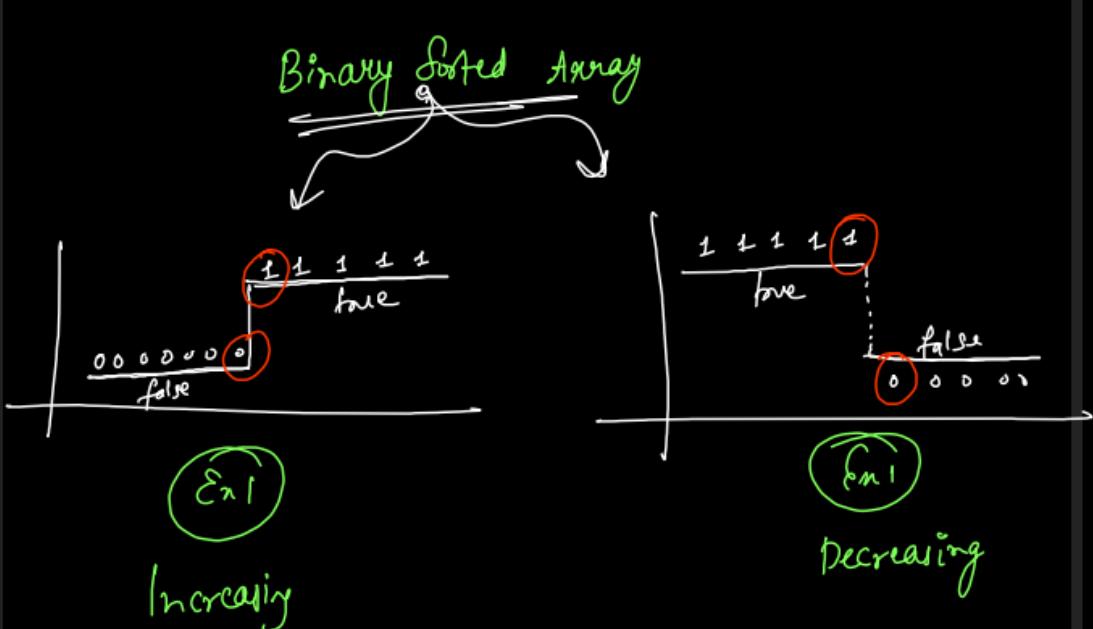
# Note: → It is for

either

Last occurrence  
of target

else

if is just smaller  
value's last  
occurrence



Transition point

$\{ 0, 0, 0, 0, 0, 0, 1, 1, 1, 1 \}$

first occurrence of L

$left = 0, right = 10, ans = -1$

$if(arr[mid] == 0)$

$left = mid + 1$

$else arr[mid] == 1$

$right = mid - 1,$   
 $ans = mid$

Corner Case 1 :  
All elements are 0  
 $\Rightarrow$  no transition point

$\{ 0, 0, 0, 0, 0 \}$        $ans = -1$

Corner Case 2 :  
All elements are 1  
 $\Rightarrow$  0th index is transition pt of first occurrence of 1

$\{ 1, 1, 1, 1, 1 \}$        $ans = 0$

```

int transitionPoint(int arr[], int n) {
    int left = 0, right = n - 1, ans = -1;

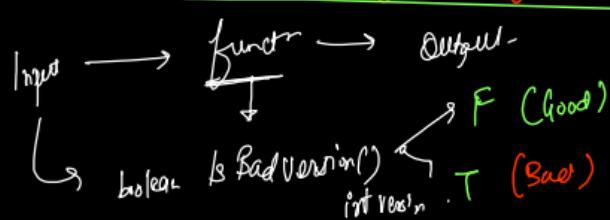
    while(left <= right){
        int mid = left + (right - left) / 2;

        if(arr[mid] == 0){
            left = mid + 1;
        } else {
            right = mid - 1;
            ans = mid;
        }
    }

    return ans;
}

```

API → Application Programming Interface



○	○	○	○	○	○	○	○	○	○	○
G	G	G	G	G	B	B	B	B	B	B
v1	v2	v3	v4	v5	v6	v7	v8	v9	v10	v11

First Bad Version  
== Transition pt

```

public int firstBadVersion(int n) {
    int left = 1, right = n, ans = n;

    while(left <= right){
        int mid = left + (right - left) / 2;

        if(isBadVersion(mid) == false) {
            left = mid + 1;
        } else {
            right = mid - 1;
            ans = mid;
        }
    }

    return ans;
}

```

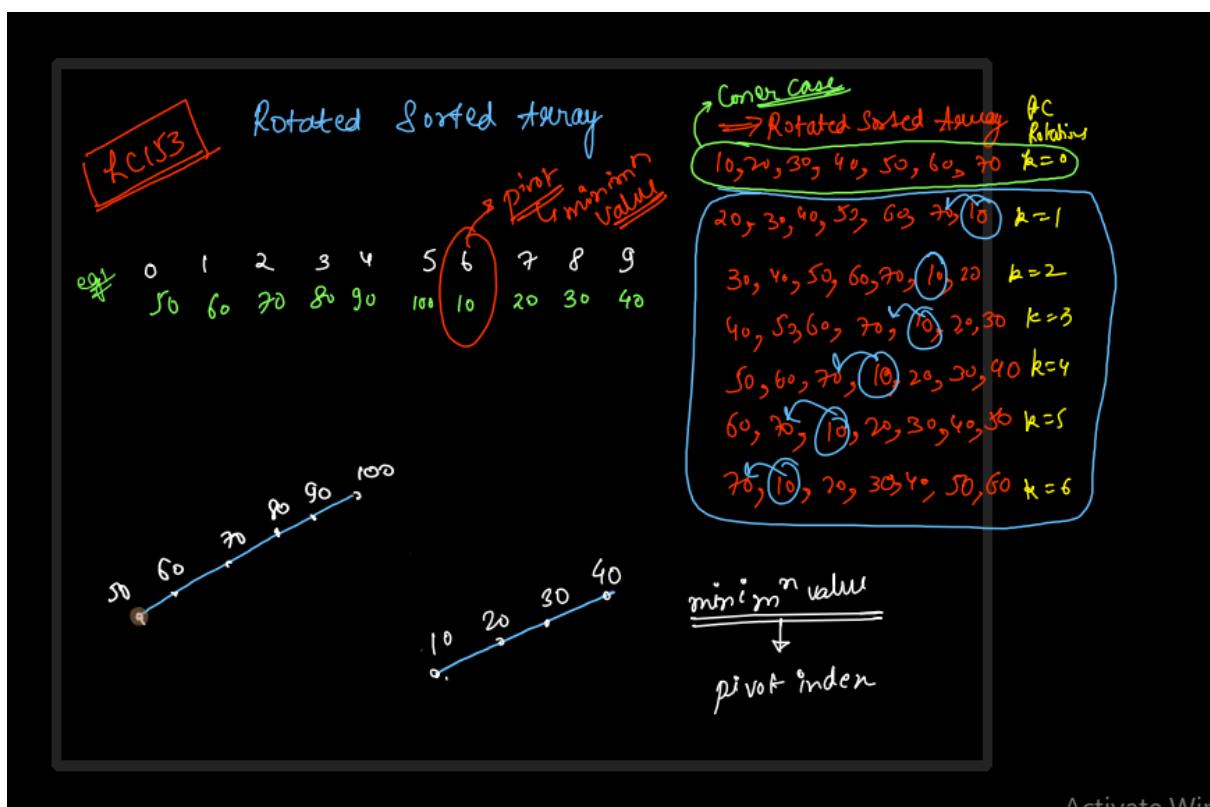


Diagram illustrating a rotated sorted array search:

Corner case (No rotation)

Time  $\rightarrow O(\log n)$

```

public int findMin(int[] nums) {
    int left = 0, right = nums.length - 1;

    while(left <= right){ → mid is min/pivot
        int mid = left + (right - left) / 2;
        → mid lies in two right sides
        if(mid >= 1 && nums[mid - 1] > nums[mid]){
            //Pivot Element is at Mid
            return nums[mid];
        }
        else if(nums[mid] >= nums[0]){
            left = mid + 1;
        } else {
            right = mid - 1;
        }
    }

    // Corner Case: Sorted Array without Rotations
    return nums[0];
}

```

Diagram illustrating a mountain array peak element search:

8:52

Mountain Array  $\rightarrow$  Peak Element

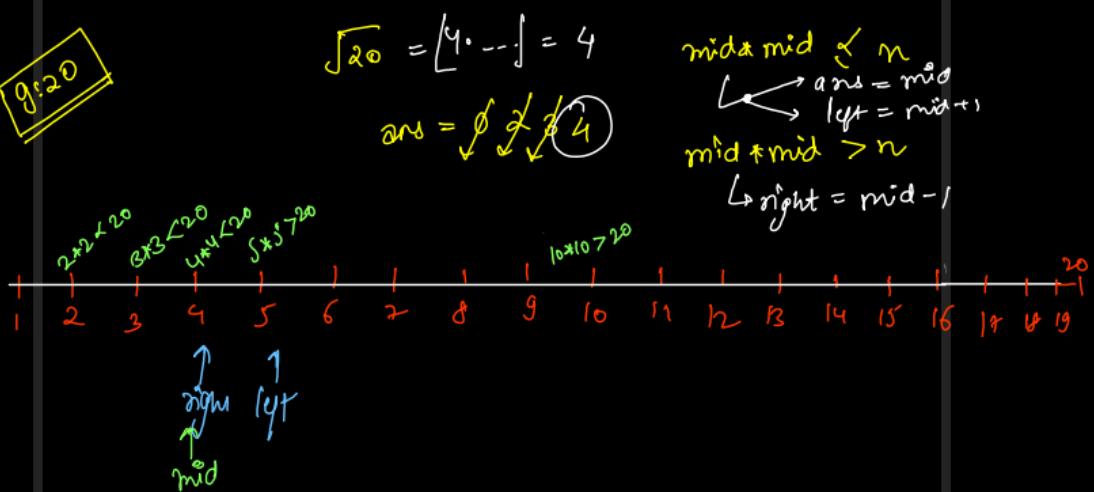
① sorted array  
② Binary Search

Time  $\rightarrow O(\log_2 N)$

```
int left = 1, right = nums.length - 2;
while(left <= right){
    int mid = left + (right - left) / 2;

    if(nums[mid] > nums[mid - 1] && nums[mid] > nums[mid + 1]){
        // Peak Element
        return mid;
    }

    else if(nums[mid] < nums[mid + 1]){
        // Uphill
        left = mid + 1;
    } else {
        // Downhill
        right = mid - 1;
    }
}
```



## Binary No System

Decimal system No  $\rightarrow$  Base 10

0	10	20	30	...	90	100
1	11	/	/		/	
2	12	/	/		/	
3	13	/	/		/	
4	14	/	/		/	
5	15	/	/		/	
6	16	/	/		/	
7	17	/	/		/	
8	18	29	39		89	
9	19					
10	20					
11	21					
12	22					
13	23					
14	24					
15	25					
16	26					
17	27					
18	28					
19	29					
20	30					
21	31					
22	32					
23	33					
24	34					
25	35					
26	36					
27	37					
28	38					
29	39					
30	40					
31	41					
32	42					
33	43					
34	44					
35	45					
36	46					
37	47					
38	48					
39	49					
40	50					
41	51					
42	52					
43	53					
44	54					
45	55					
46	56					
47	57					
48	58					
49	59					
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51	61					
52	62					
53	63					
54	64					
55	65					
56	66					
57	67					
58	68					
59	69					
60	70					
61	71					
62	72					
63	73					
64	74					
65	75					
66	76					
67	77					
68	78					
69	79					
70	80					
71	81					
72	82					
73	83					
74	84					
75	85					
76	86					
77	87					
78	88					
79	89					
80	90					
81	91					
82	92					
83	93					
84	94					
85	95					
86	96					
87	97					
88	98					
89	99					
90	100					

(OFF) 0 (ON)

Binary System  $\rightarrow$  Base 2

$$000 \rightarrow 0 \quad 1000 \rightarrow 8$$

$$001 \rightarrow 1 \quad 1001 \rightarrow 9$$

$$010 \rightarrow 2 \quad 1010 \rightarrow 10$$

$$011 \rightarrow 3 \quad 1011 \rightarrow 11$$

$$100 \rightarrow 4 \quad 1100 \rightarrow 12$$

$$101 \rightarrow 5 \quad 1101 \rightarrow 13$$

$$110 \rightarrow 6 \quad 1110 \rightarrow 14$$

$$111 \rightarrow 7 \quad 1111 \rightarrow 15$$

bit

$$2 \frac{10}{973}$$

$$+ 285$$

$$\hline 1258$$

$$(10)_2 = 1 + 1 + 1 + 1 + 1 + \dots \text{ 1 times}$$

$$(10)_{10} = 1 + 1 + 1 + 1 + \dots \text{ 10 times}$$

$$\begin{array}{r} \cancel{\text{Adding 2 bits}} \\ \begin{array}{r} 0 \\ + 0 \\ \hline 0 \end{array} \end{array}$$

$$\begin{array}{r} 0 \\ + 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ + 0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ + 1 \\ \hline 10 \end{array}$$

$$(10)_2 = 1 \times 2^1 + 0 \times 2^0$$

$$(10)_2 = 1 \times 2^1 + 0 \times 2^0$$

$$= 2 + 0 = (2)_{10}$$

Decimal No

$$\left( \begin{smallmatrix} 1 & 0 & 2 & 1 & 0 & 1 & 0 \\ 9 & 7 & 3 \end{smallmatrix} \right)_{10} = 9 * 10^6 + 7 * 10^5 + 3 * 10^0$$

$$= 9000 + 70 + 3 = 973$$

$$\left( \begin{smallmatrix} 2 & 8 & 5 \end{smallmatrix} \right)_{10} = 2 * 10^2 + 8 * 10^1 + 5 * 10^0$$

$$= 200 + 80 + 5 = 285$$

Binary No

$$\left( \begin{smallmatrix} 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\ 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \end{smallmatrix} \right)_2 = 1 * 2^0 + 0 * 2^1 + 0 * 2^2 + 1 * 2^3 +$$

$$1 * 2^4 + 0 * 2^5 + 1 * 2^6 + 0 * 2^7 + 1 * 2^8$$

$$= (1 + 8 + 16 + 64 + 256)_{10} = (357)_{10}$$

Binary Addition

$\begin{array}{r} 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 & 0 \\ + & 1 & 1 & 0 & 0 & 1 \\ \hline 1 & 0 & 1 & 1 & 1 & 0 \end{array}$	$\begin{array}{r} 1 & 1 & 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 & 0 & 0 \\ + & 1 & 1 & 1 & 1 & 0 \\ \hline 1 & 1 & 0 & 1 & 0 & 1 \end{array}$
--	--

$$(1+1+1) = (3)_{10}$$

$$(11)_2 = 1 * 2^1 + 1 * 2^0$$

$$= 2 + 1 = (3)_{10}$$

Ans

### Decimal Subtraction

$$\begin{array}{r}
 9 \cancel{8} \quad 3 \overset{10}{6} \\
 - 2 \overset{7}{4} \quad 7 \overset{1}{1} \\
 \hline
 7 \overset{3}{3} \quad 5 \overset{5}{5}
 \end{array}$$

$$\begin{array}{r}
 6 \overset{10}{4} \quad 2 \overset{10}{9} \\
 - 6 \overset{5}{5} \quad 9 \overset{2}{2} \\
 \hline
 0 \overset{6}{6} \quad 5 \overset{7}{7}
 \end{array}$$

$$\begin{array}{r}
 9836 = \frac{9}{10^3} + \frac{8}{10^2} + \frac{3}{10^1} + \frac{6}{10^0}
 \end{array}$$

$$\begin{array}{r}
 8 * 10^2 \rightarrow 7 * 10^2 \\
 + \\
 3 * 10^1 \rightarrow 13 * 10^1 \\
 \hline
 830 \qquad \qquad \qquad 700 + 130 = 830
 \end{array}$$

### Binary Subtraction

$$\begin{array}{r}
 00 \\
 101 \cancel{1} \cancel{0} \cancel{1} \overset{0}{0} \\
 - 100110110 \\
 \hline
 000101111
 \end{array}$$

$$\begin{array}{r}
 1 \\
 - 0 \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 0 \\
 - 0 \\
 \hline
 0
 \end{array}
 \quad
 \begin{array}{r}
 1 \\
 - 1 \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 10 \overset{0}{0} \overset{2}{1} \overset{2}{0} \overset{2}{1} \overset{2}{0} \overset{2}{1} \\
 - 100111111 \\
 \hline
 000101010
 \end{array}$$

$$\begin{array}{r}
 (-1) \quad (+2) \\
 0 \\
 - 1 \\
 \hline
 \end{array}$$

$$\begin{aligned}
 & \text{String} \rightarrow \text{Binary No} \\
 & (10010011100)_2 \\
 & = 2^9 + 2^8 + 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 \\
 & = (4 + 8 + 16 + 128 + 1024)_{10} \\
 & = (1180)_{10}
 \end{aligned}$$

```
public int binary_to_decimal(String str) {  
    int place = 1, res = 0;  
  
    for(int i=str.length() - 1; i>=0; i--){  
        if(str.charAt(i) == '1') res += place;  
        place = place * 2;  
    }  
  
    return res;  
}
```

$$\begin{array}{r} \text{Decimal to Binary} \\ 141^2 + 141^0 \\ + 2 \times 10 + 2^0 \times 10^0 \\ \uparrow \\ (11101)_2 = (?)_2 \end{array}$$

$$\begin{cases} \text{even } y_2 = 0 \\ \text{odd } y_2 = 1 \end{cases}$$

2	1172	
2	586	0
2	293	0
2	146	1
2	73	0
2	36	1
2	18	0
2	9	0
2	4	1
2	2	0
2	1	0
	0	1

↑

$1172 = 586 \times 2 + 0$   
 $586 = 293 \times 2 + 0$   
 $293 = 146 \times 2 + 1$   
 $146 = 73 \times 2 + 0$   
 $73 = 36 \times 2 + 1$   
 $36 = 18 \times 2 + 0$   
 $18 = 9 \times 2 + 0$   
 $9 = 4 \times 2 + 1$   
 $4 = 2 \times 2 + 0$   
 $2 = 1 \times 2 + 0$   
 $1 = 0 \times 2 + 1$

$$\underbrace{(10010010100)}_2$$

remainders in reverse order

```
String bin = "";
while(dec > 0){
    int bit = dec % 2;
    bin = bin + bit;
    dec = dec / 2;
}
// Printing Remainders or Bits in Reverse Order
for(int i=bin.length() - 1; i>=0; i--){
    System.out.print(bin.charAt(i));
}
```

$26 = 13 \times 2 + 0 \Rightarrow 26 = 0 \cdot 2^5 + 1 \cdot 2^4 + 0 \cdot 2^3 + 1 \cdot 2^2 + 1 \cdot 2^1 + 0 \cdot 2^0$   $(26)_{10} = (?)_2$   
 $13 = 6 \times 2 + 1 \Rightarrow 13 = 0 \cdot 2^4 + 1 \cdot 2^3 + 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0$   
 $6 = 3 \times 2 + 0 \Rightarrow 6 = 0 \cdot 2^3 + 1 \cdot 2^2 + 1 \cdot 2^1 + 0 \cdot 2^0$   
 $3 = 1 \times 2 + 1 \Rightarrow 3 = 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0$   
 $1 = 0 \cdot 2 + 1$

dec	26		bin
2	13	0	" "
2	6	1	"0"
2	3	0	"01"
2	1	1	"010"
0	1	1	"0101"
			↓
			$\text{rev}(10101)$
			$\text{bin} = (11010)_2$

```

String bin = "";
while(dec > 0){
    int bit = dec % 2;
    bin = bin + bit;
    dec = dec / 2;
}

// Printing Remainders or Bits in Reverse Order
for(int i=bin.length() - 1; i>0; i--){
    System.out.print(bin.charAt(i));
}
}

```

## # Time & Space Complexity

### # TIME COMPLEXITY

- ✓ ① Compile Time vs Run-time/Execution-time
  - ↳ Architecture/machine Dependency
- ✓ ② Asymptotic Analysis
  - ↳ Upper Bound or Big O or Worst case
  - ↳ Tight Bound or Omega (Ω) or Average case
  - ↳ Lower Bound or Theta (Θ) or Best case
- ✓ Ignoring the constants or smaller polynomial terms
- ✓ Ignoring the smaller input vs runtime trend
- Time Complexity Trend ↪ I II For-loops time

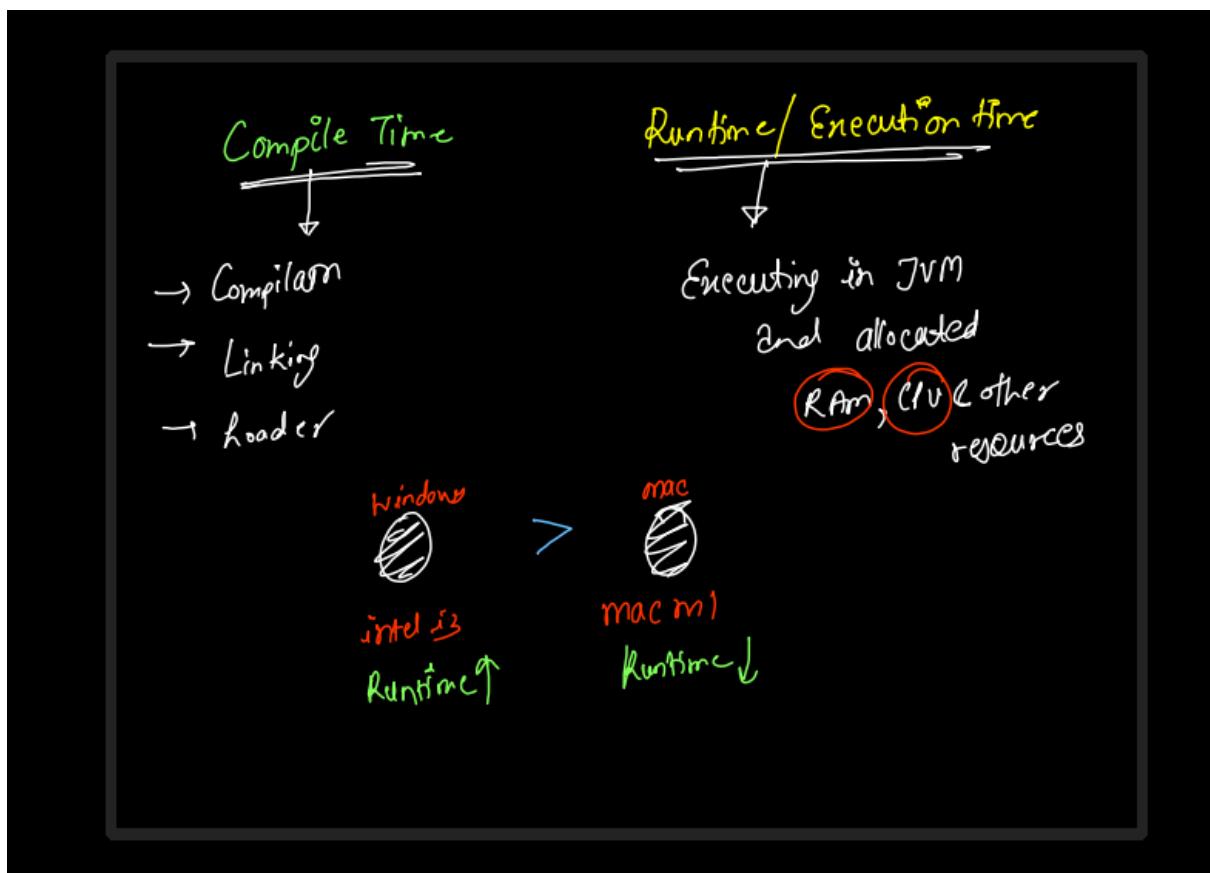
# Errors  
Compile time  
# Process memory  
Diagram

Runtime

# Amortized Time Complexity  
↳ ArrayList (Collection)



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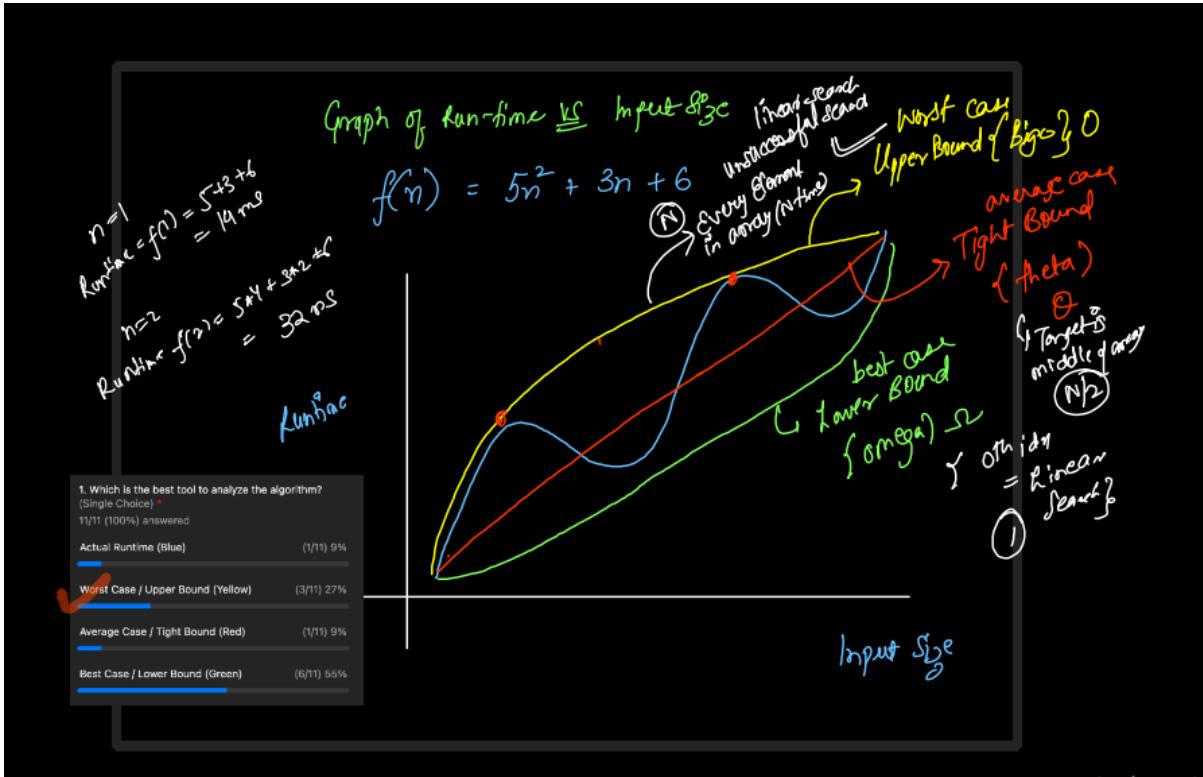
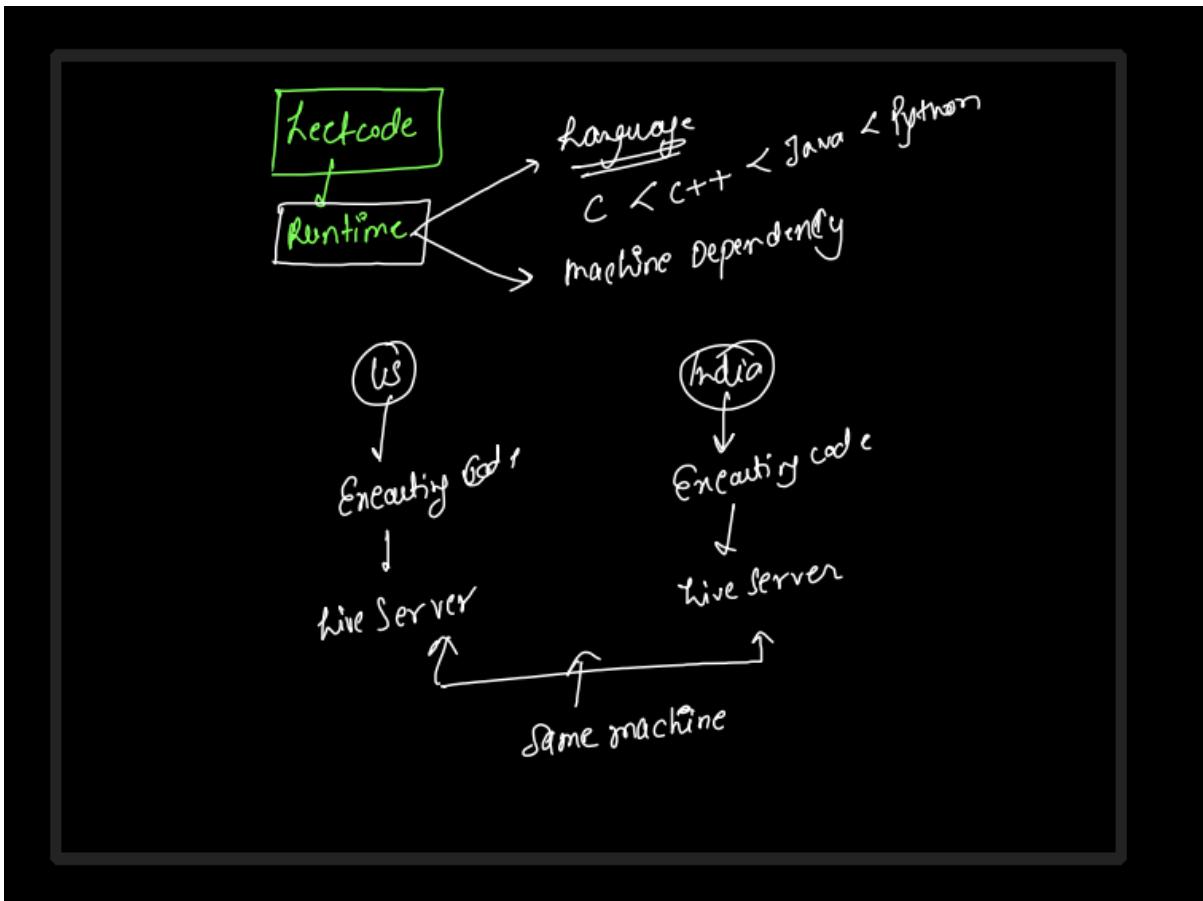
<u>Algorithms</u>	<u>Runtime</u>	<u>Runtime</u>	<u>To compare algorithms based on run-time, you need to have the same machine.</u>
<u>Linear Search</u>	is, 4gb 100 ms $n=10$ $n=100$	is, 16gb 10 ms $\downarrow \times 10$ $\downarrow \times 10$ 100 ms	
<u>Binary Search</u>	20 ms $n=10$ $n=100$	1 ms 40 ms 3 ms	

Asymptotic Analysis

⇒ Analysis of <sup>rate of</sup> growth of runtime with respect to the input size

→ architecture neutrality ( $32\text{bit}/64\text{bit}$ ) ( $8\text{gb ram}/32\text{gb ram}$ )

→ machine independence ( $i_3 = m$ )

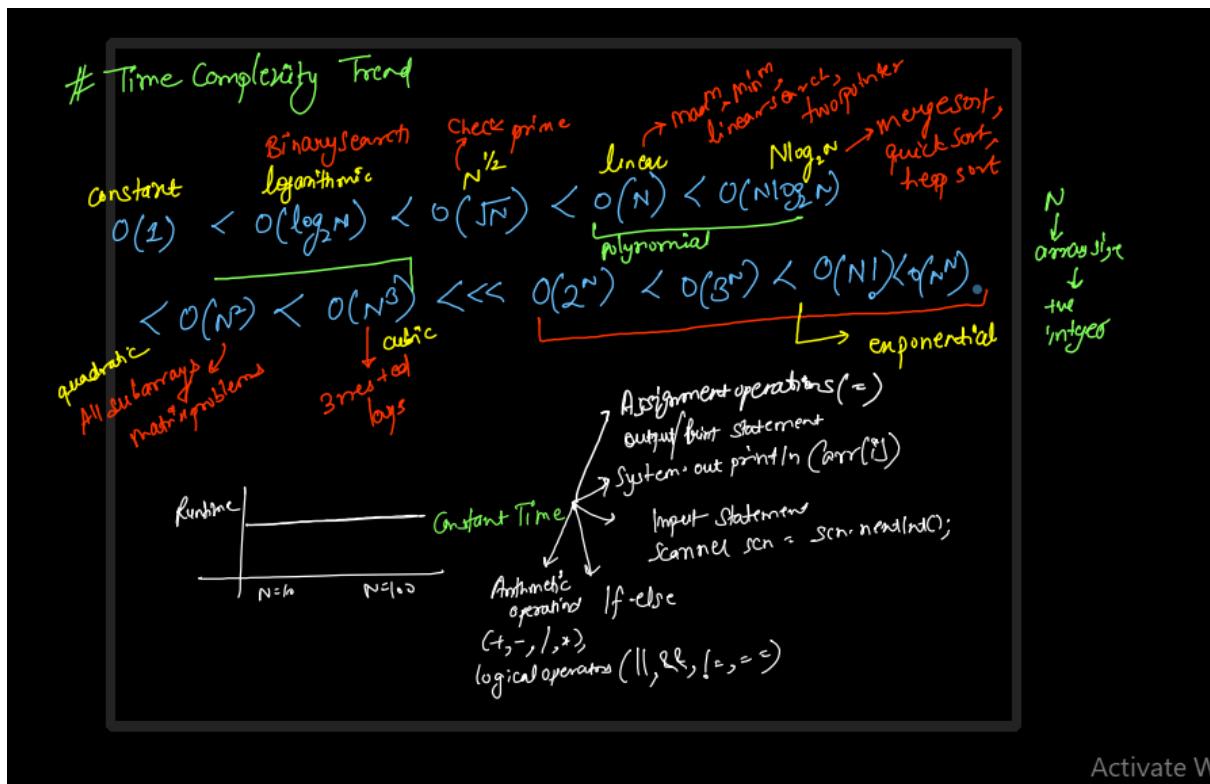


① ignore the smaller terms  
 $f(n) = \sqrt{5n^2 + 3n + 6}$   $\quad n \geq 1$   
 $UB(f(n)) = 14n^4$   
 $14n^3 \geq 5n^2 + 3n + 6$   
 ② ignore constant term  
 $14n^2 \geq 5n^2 + 3n + 6$   
 $14n^2 \geq 5n^2 + 3n + 6$   
 ③ ignoring the smaller term instead  
 $LB(f(n)) = 0$   
 $n \leq 5n^2 + 3n + 6$   
 $n^2 \leq 5n^2 + 3n + 6$   
 $4n^2 \leq 5n^2 + 3n + 6$   
 $TB(f(n)) = \frac{UB + LB}{2} = \frac{4n^2 + 14n^2}{2} = (9n^2) \rightarrow O(n^2)$

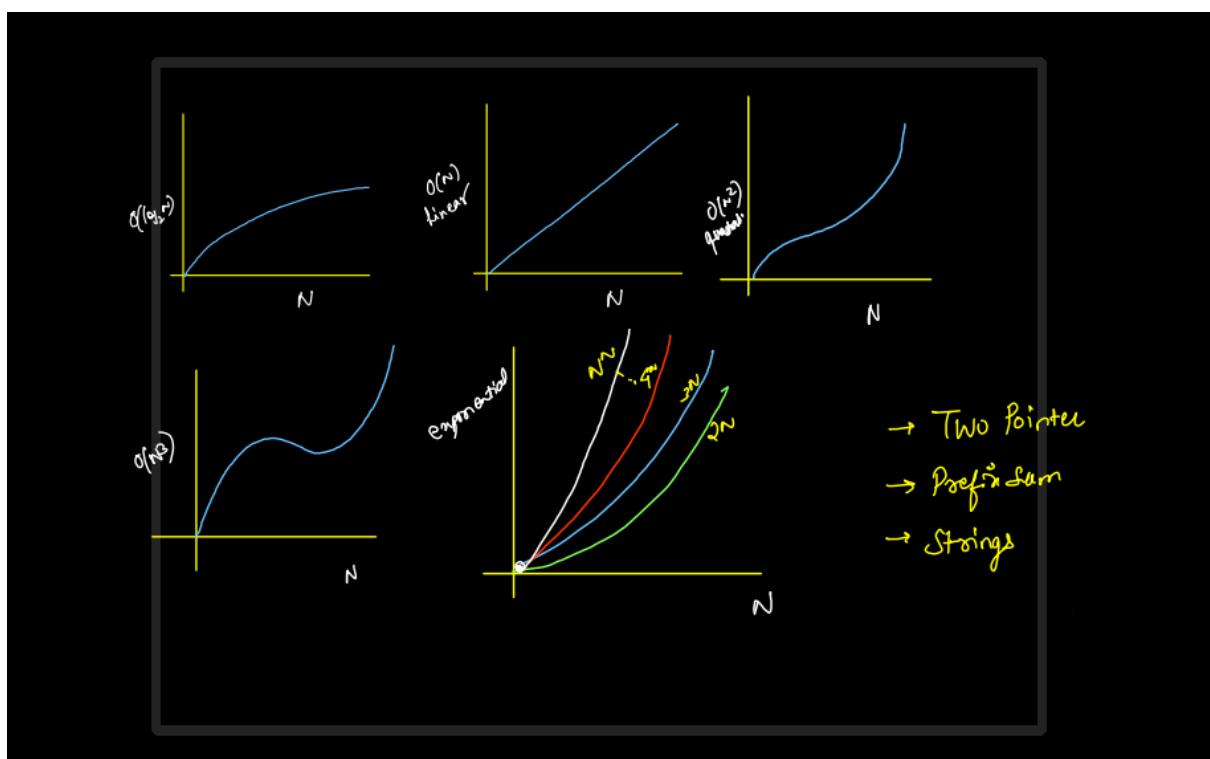
Act

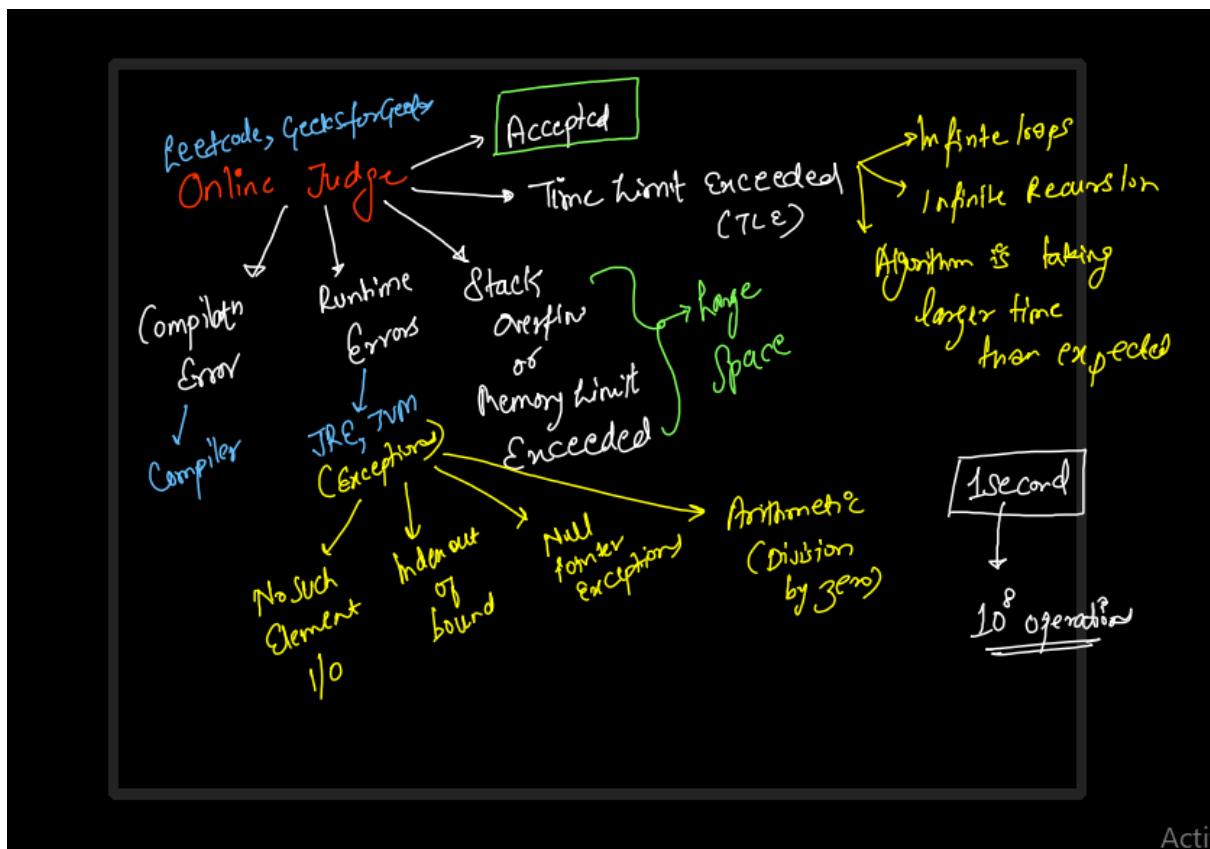
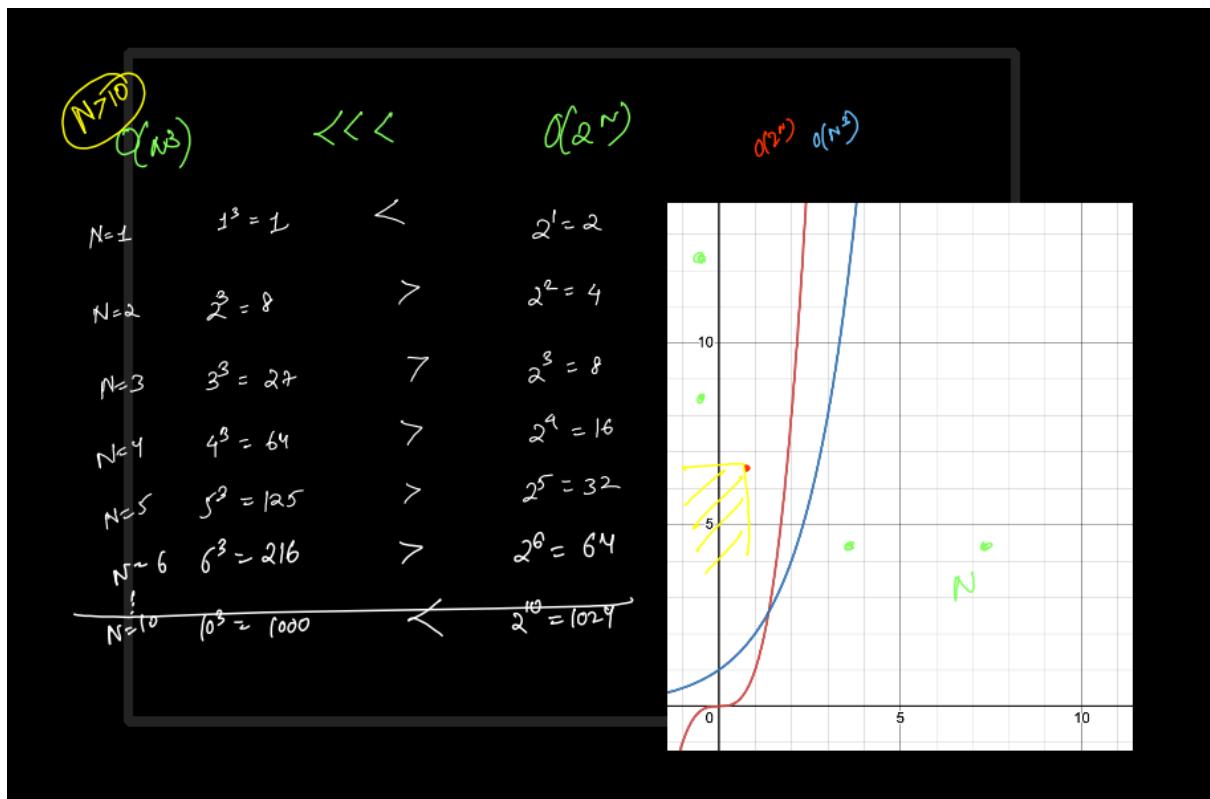
$100n^2 + n^2$   
 $20n^2$   
 $(4n^2)n^2$   
 $14n^2$   
 ignore the constant  
 $\Rightarrow$  it does not affect  
 the rate of growth  
 $\theta(n^2)$

$n = 1 \text{ million}$   
 $100 * (1 \text{ million})^2$   
 $20 * (1 \text{ million})^2$



Activate W





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Competitive Programming Chart		
Input Size	Time Complexity	Examples
$\leq 10$ $\leq 18$ $\leq 22$ $\leq 10^2$ $\leq 4 \times 10^2$ $\leq 2 \times 10^3$ $\leq 10^4$ $\leq 10^5 - 10^6$ $\leq 10^8$ $\leq 10^{10}$	$O(n)$ or $O(2^n)$ $O(2^n \cdot n)$ $O(2^n \cdot n^2)$ $O(n^4)$ $O(n^3)$ $O(n^2 \log n)$ $O(n^2)$ $O(n \log n)$ $O(n)$ $O(\log n)$ or $O(1)$	<p style="text-align: center;">Time Complexity Worst Case</p> <p>Backtracking [e.g. permutations, subsets]</p> <p>Traveling Salesman</p> <p>DP with Bitmasking</p> <p>Quadruplets / 4 Nested loops (4P 2P)</p> <p>3 nested loops, Find max/min, 3D DP</p> <p>Nested loops &amp; Binary Search</p> <p>2 Nested loops (Bubble, Insertion, Selection, etc.)</p> <p>Sorting (QS, MS), BS in answer, Greedy, etc.</p> <p>Arrays &amp; Strings (1D DP)</p> <p>mathematical formula {Bit Manipulation}</p>

Time Complexity	
<pre>① for (int i = 0; i &lt; n; i++) {     System.out.println(i); }</pre>	<p>Time Complexity</p> <p>for (int i = 0; i &lt; n; i++) {     System.out.println(i); } → Constant → <math>O(1)</math> → <math>k</math> ms / 0 ms</p> <p><math>i=0 \Rightarrow k \text{ ms}</math>  <math>i=1 \Rightarrow k \text{ ms}</math>  <math>i=2 \Rightarrow k \text{ ms}</math>  <math>\vdots</math>  <math>i=N-1 \Rightarrow k \text{ ms}</math>  <math>\vdots</math>  <math>i=N \Rightarrow k \text{ ms}</math></p> <p><math>f(i) \cdot 2 = 0</math> if <math>i</math> is even  <math>f(i) \cdot 2 = 1</math> if <math>i</math> is odd</p> <p>Total time = <math>(k + k + k + \dots + k) * n</math> ms  <math>= kn</math> ms  <math>\Rightarrow O(n)</math>  <math>\Rightarrow O(n)</math></p>

(2)

```
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        System.out.println(i + " " + j);
    }
}
```

Nested loops

No5

$i=0$	$j=0, j=1, j=2, j=3, j=4$
$i=1$	$j=0, j=1, j=2, j=3, j=4$
$i=2$	$j=0, j=1, j=2, j=3, j=4$
$i=3$	$j=0, j=1, j=2, j=3, j=4$
$i=4$	$j=0, j=1, j=2, j=3, j=4$

$$\left. \begin{array}{l} k*n \\ + \\ k*n \\ + \\ k*n \\ + \\ k*n \\ + \\ k*n \end{array} \right\} = k*n+n$$

$O(n^2)$

Active

(3)

```
for (int i = 0; i < n; i++) {
    for (int j = n - 1; j >= 0; j--) {
        System.out.println(i + j);
    }
}
```

No5

$i=0$	$j=4, j=3, j=2, j=1, j=0$
$i=1$	$j=3, j=2, j=1, j=0$
$i=2$	$j=2, j=1, j=0$
$i=3$	$j=1, j=0$
$i=4$	$j=0$

$$\left. \begin{array}{l} kn \\ + \\ bn \\ + \\ kn \\ + \\ bn \\ + \\ kn \end{array} \right\} \text{Hilfsm} = O(kn+n) \Rightarrow \underline{\underline{O(n^2)}}$$

Active

④

```

for (int i = 0; i < n; i++) {
    for (int j = 0; j < i; j++) {
        System.out.print(i + " " + j);
    }
}

```

$$k * (1+2+3+4+\dots+n) \text{ ms}$$

$$= k * \left\{ \frac{n * (n+1)}{2} \right\}$$

$N = 5$

$i=0$	$j=0$	$\rightarrow k * 1 \text{ ms}$	$= \frac{k}{2} n^2 + \frac{k}{2} n$
$i=1$	$j=0, j=1$	$\rightarrow k * 2 \text{ ms}$	$\downarrow$
$i=2$	$j=0, j=1, j=2$	$\rightarrow k * 3 \text{ ms}$	$O(n^2)$
$i=3$	$j=0, j=1, j=2, j=3$	$\rightarrow k * 4 \text{ ms}$	
$i=4$	$j=0, j=1, j=2, j=3, j=4$	$\rightarrow k * 5 \text{ ms}$	

Activate V

⑤

```

for (int i = 1; i < n; i *= 2) {
}

```

$N = 16$

$$i=0, j=2^0, j=2^1, j=2^2, j=2^3, j=2^4, j=2^5, i=32 \\ k + k + k + k + k + k = k * \log_2 n$$

$\Rightarrow O(\log_2 n)$

Multiplying or  
Dividing by 2

while ( $N > 1$ )  
 $i$   
 $N = N/2$   
 $j$

$$2^5 \rightarrow 2^4 \rightarrow 2^3 \rightarrow 2^2 \rightarrow 2^1 \Rightarrow 5 \text{ ops}$$

$$2^{10} \rightarrow 2^9 \rightarrow 2^8 \rightarrow \dots \rightarrow 2^1 \Rightarrow 10 \text{ ops}$$

$$N = 2^y \Rightarrow y = \log_2 N \quad \underline{\underline{O(\log_2 n)}}$$

$i \times i$   
 $i = 1, 4, 9, 16, 25, 36, 49, \dots$  (6)

```

    for (int i = 0; i * i < n; i++) {
    }
  
```

$\mathcal{O}(\sqrt{n})$

$N = 2^4$   
 $i=0 \Rightarrow 0 \times 0 < 16$   
 $i=1 \Rightarrow 1 \times 1 < 16$   
 $i=2 \Rightarrow 2 \times 2 < 16$   
 $i=3 \Rightarrow 3 \times 3 < 16$

$N = 3^2$   
 $i=0 \Rightarrow 0 \times 0 < 32$   
 $i=1 \Rightarrow 1 \times 1 < 32$   
 $i=2 \Rightarrow 2 \times 2 < 32$   
 $i=3 \Rightarrow 3 \times 3 < 32$   
 $i=4 \Rightarrow 4 \times 4 < 32$   
 $i=5 \Rightarrow 5 \times 5 < 32$

$N = 2^6$   
 $i=0 \Rightarrow 0 \times 0 < 64$   
 $i=1 \Rightarrow 1 \times 1 < 64$   
 $i=2 \Rightarrow 2 \times 2 < 64$   
 $i=3 \Rightarrow 3 \times 3 < 64$   
 $i=4 \Rightarrow 4 \times 4 < 64$   
 $i=5 \Rightarrow 5 \times 5 < 64$   
 $i=6 \Rightarrow 6 \times 6 < 64$   
 $i=7 \Rightarrow 7 \times 7 < 64$   
 $i=8 \Rightarrow 8 \times 8 = 64$

Activation

$\mathcal{O}(n)$   
 $\mathcal{O}(m)$   
 $\mathcal{O}(n+m)$

```

    for (int i = 0; i < n; i++) {
        System.out.println(i);
    }
    for (int j = 0; j < m; j++) {
        System.out.println(j);
    }
  
```

Example  
 Merge 2 sorted arrays

⑧

```
for (int i = 0; i < n; i++) {  
    for (int j = 0; j < n; j++) {  
        System.out.println(i + " " + j);  
    }  
}
```

$10^4 \text{ ms}$

$10k + 10k + 10k + \dots n \text{ times} = 10nk \text{ ms}$   
 $\Rightarrow O(n)$

⑨

```
for (int i = 0; i < n; i += 2) {  
    Sys...  
}
```

# Monday  
Tuesday  
Wednesday  
Thursday  
Friday  
Time Space  
LS vs RS  
# Tuesday  
RS

$$\sqrt{N} = 4$$
  
$$\log_2(N) = 4$$
  
$$N = 16$$

$$i=0, i=2, i=4, i=6, i=8, i=10, i=12, i=14, i=16$$

$$f(\text{operation}) = \frac{1}{2}n * 10 \text{ ms} \Rightarrow O(n)$$

$$\sqrt{N} = 8$$
  
$$\log_2(N) = 6$$
  
$$N = 64$$

$$0, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, \dots 64$$
  
$$32 \text{ operations}$$

$\sqrt{16} = 4$   
 $(\log_2 16) = 4$   
 $\underline{\underline{N=16}}$   
 $\sqrt{N} \rightarrow 8$   
 $\log_2 N \rightarrow 4$   
 $\underline{\underline{N=64}}$

⑨ `for (int i = 0; i < n; i += 2) { }`

$i=0, i=2, i=4, i=6, i=8, i=10, i=12, i=14, i=16$   
 $\underbrace{ }_{32 \text{ operations}}$

$\text{operations} = \frac{1}{2}n * \log_2 n \Rightarrow O(n)$

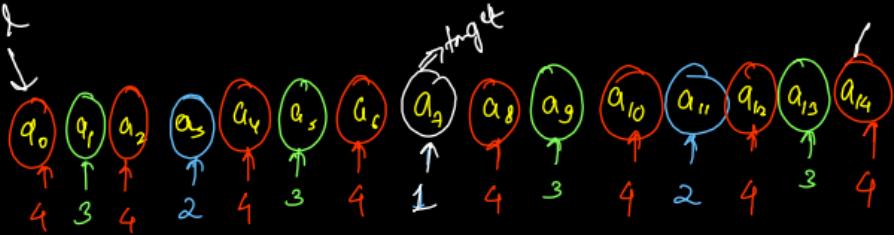
# Monday → Day 4  
 Tuesday → Day 5  
 Wednesday → Day 6  
 Thursday → Day 7  
 Friday → Day 8  
 Saturday → Day 9  
 Sunday → Day 10  
 ↓  
 18 vs 8  
 ↓  
 10 vs 5  
 ↓  
 5 vs 2  
 ↓  
 2 vs 1  
 ↓  
 1 vs 0

Activate W

### Time Complexity

<p>Linear Search</p> <p>6 5 8 3 7 2 9</p> <p>best case <math>\Rightarrow</math> target = arr[0]  <math>\Rightarrow \Theta(1)</math></p> <p>worst case <math>\Rightarrow</math> target = arr[n-1]  <math>\text{or}</math>  <math>\text{target is not found}</math>  <math>\Rightarrow \Omega(n)</math></p> <p>Average case <math>\Rightarrow</math> target is in the middle  <math>\Rightarrow \Theta(n)</math></p>	<p>Binary Search</p> <p>n → n/2 → n/4 → n/8  <math>\vdots</math>      2 3 5 6 7 8 9</p> <p>best case <math>\Rightarrow</math> target = middle of array  <math>\Rightarrow \Theta(1)</math></p> <p>worst case <math>\Rightarrow \Theta(\log n)</math>  <math>\{</math> dividing array in 2 halves <math>\}</math></p> <p>Average case <math>\Rightarrow \Theta(\log n)</math></p>
--	--

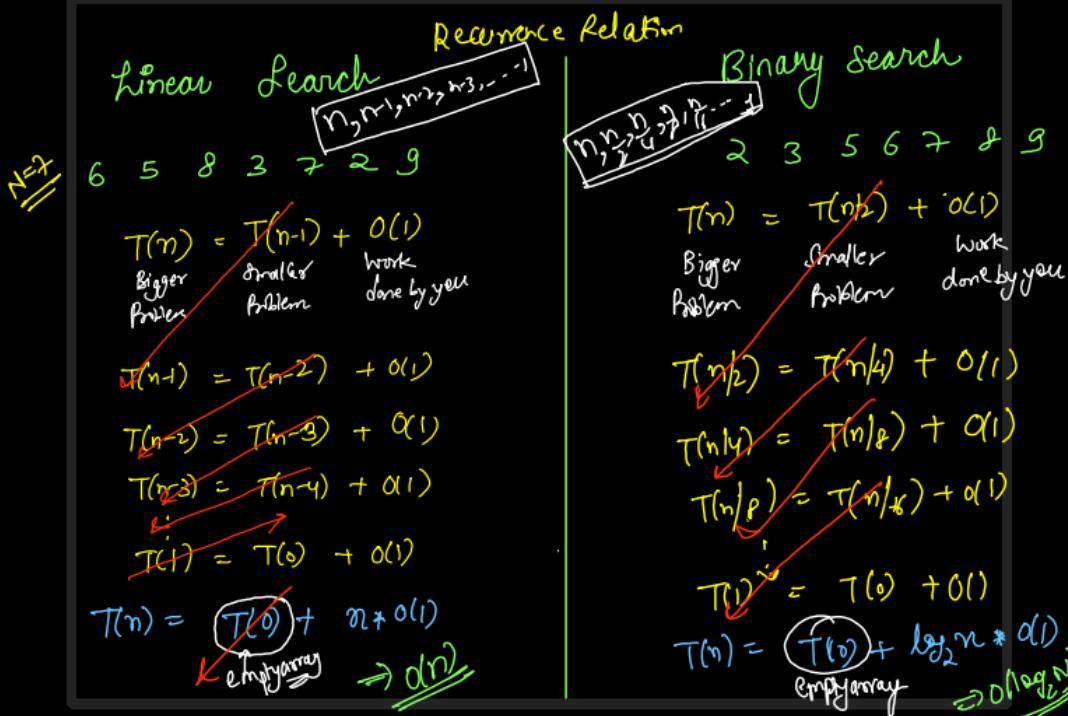
Activate V



Best case  $\rightarrow$  middle  $\rightarrow O(1)$

Worst case  $\rightarrow$  4 iterations  $\rightarrow O(\log_2 n)$

$$\text{Average Case} = \frac{4*7 + 3*4 + 2*2 + 1*1}{15} \rightarrow 3 \text{ iterations} \\ \Rightarrow O(\log_2 n)$$



## # Mock Interviews

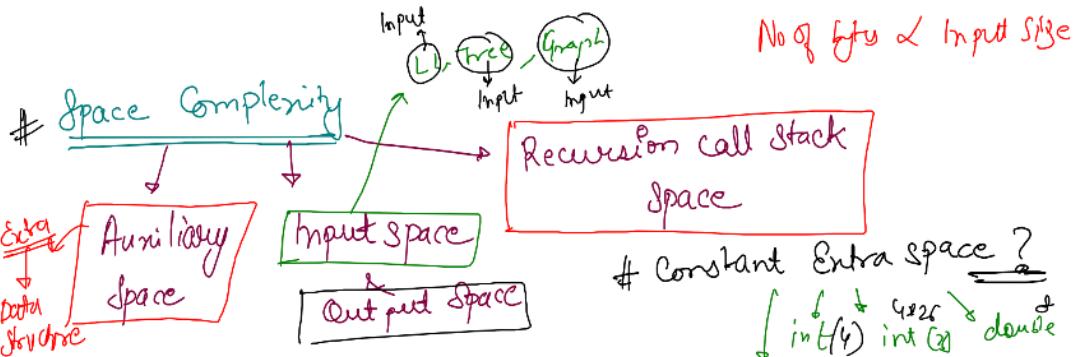
- # Recurrence Relations
- ~~①  $T(n) = T(n-1) + O(1)$  Linear search~~
  - ~~②  $T(n) = T(n-1) + O(n)$  Bubble/Insertion Sort~~
  - ~~③  $T(n) = T(n/2) + O(1)$  Binary Search~~
  - ~~④  $T(n) = T(n/2) + O(n)$  Quick Select~~
  - ~~⑤  $T(n) = 2T(n-1) + O(1)$  Tower of Hanoi subsets~~
  - ~~⑥  $T(n) = 2T(n/2) + O(1)$  Divide & Conquer~~
  - ~~⑦  $T(n) = 2T(n/2) + O(n)$  Merge Sort~~

Activate

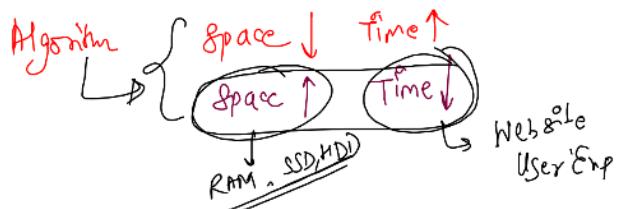
$$\begin{aligned}
 ② \quad T(n) &= T(n-1) + O(n) \\
 T(n-1) &= T(n-2) + O(n) \\
 T(n-2) &= T(n-3) + O(n) \\
 &\vdots \\
 T(1) &= T(0) + O(n) \\
 T(n) &= T(0) + n * O(n) \\
 &\Rightarrow O(n^2)
 \end{aligned}$$

$$\begin{aligned}
 ④ \quad T(n) &= T(n/2) + O(n) \\
 T(n/2) &= T(n/4) + O(n/2) \\
 T(n/4) &= T(n/8) + O(n/4) \\
 T(n/8) &= T(n/16) + O(n/8) \\
 &\vdots \\
 T(1) &= T(0) + O(1) \\
 T(n) &= T(0) + \left\{ \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \dots + 1 \right\} \\
 &= T(0) + n \left\{ \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + 0 \right\} \\
 &= T(0) + 2 * n
 \end{aligned}$$

Activate



# Time vs Space Tradeoff!



~~$$⑤ \underset{2}{T(n)} = 2T(n-1) + O(1)$$~~

~~$$2T(n-1) = 2^2 T(n-2) + 2O(1)$$~~

~~$$2^2 T(n-2) = 2^3 T(n-3) + 2O(1)$$~~

~~$$2^3 T(n-3) = 2^4 T(n-4) + 2O(1)$$~~

~~$$\vdots$$~~
~~$$2^x T(1) = 2^{x+1} T(0) + 2O(1)$$~~

$$\begin{aligned}
 T(n) &= 2^{x+1} T(0) \\
 &\quad + \{1+2+2^2+2^3+\dots+2^x\} \\
 &= 2^n T(0) + \frac{2^n - 1}{2 - 1} \\
 &\Rightarrow O(2^n)
 \end{aligned}$$

$$x = \text{no of terms} = n$$

## # Rotate Array by k positions

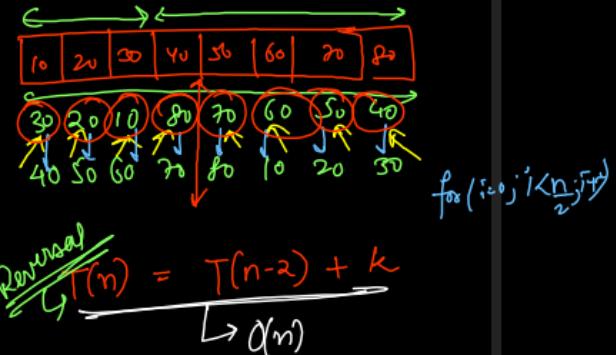
```

void reverse(int[] nums, int start, int end) {
    while(start < end) {
        int temp = nums[start];
        nums[start] = nums[end];
        nums[end] = temp;
        start++; end--;start+=1; end-=1;
    }
}

public void rotate(int[] nums, int k) {
    int n = nums.length;
    k = k % n;

    reverse(nums, 0, n-1);
    reverse(nums, 0, k-1);
    reverse(nums, k, n-1);
}

```



$$\begin{aligned}
\text{Time} &\rightarrow O(n) + O(k) + O(n+k) \\
&= O(n+k) = O(2n) \\
&= O(n)
\end{aligned}$$

Rotate Matrix

```

int row = mat.length, col = mat[0].length;
// Step 1: Transpose the matrix
for(int i=0; i<row; i++){
    for(int j=0; j<i; j++){
        int temp = mat[i][j];
        mat[i][j] = mat[j][i];
        mat[j][i] = temp;
    }
}

```

$$\begin{array}{lll}
i=0 & j=0 & 0+1+2+\dots+(n-1) \\
i=1 & j=0 & = \frac{n \times n - 1}{2} \\
i=2 & j=0, 1 & \Rightarrow O(n^2) \\
\vdots & & \\
i=n & j=0, 1, 2, \dots, n-1 &
\end{array}$$

```

// Step 2: Row-by-Row Reversal
for(int i=0; i<row; i++){
    int left = 0, right = col - 1;
    while(left < right){
        int temp = mat[i][left];
        mat[i][left] = mat[i][right];
        mat[i][right] = temp;

        left++; right--;
    }
}

```

$$\begin{aligned}
&= O(n^2) + O(n^2) \\
&\approx O(n^2)
\end{aligned}$$

# String → Array of character  
↳  $O(\text{no of characters})$

Input: String str = scn.nextLine();  $\rightarrow O(\text{length})$

Output: System.out.println(str);  
 $\downarrow$   
 $O(\text{length})$

for(int i=0; i<str.length(); i++) {  
 System.out.print(str.charAt(i));  
}

### # Check if string is Palindrome

```
public boolean isPalindrome(String s) {  
    int left = 0, right = s.length() - 1;  
    while(left <= right){  
        char chl = s.charAt(left);  
        char chr = s.charAt(right);  
  
        if(chl != chr){  
            return false;  
        }  
  
        left++; right--;  
    }  
  
    return true;  
}
```

length =  $N = 9$   
malayalam

$$T(n) = T(n-2) + O(1)$$
$$\Rightarrow O(n)$$

$n = \text{string's length}$

Reverse String

Result for  
`static String revStr(String str) {  
 String res = "";  
 for(int i=str.length() - 1; i>=0; i--){  
 res = res + str.charAt(i);  
 }  
 return res;  
}`

Input Space  $\rightarrow O(n)$ , Output Space  $\rightarrow O(n)$   
 Extra Space  $\rightarrow O(1)$

$O(n)$   $\Rightarrow O(n \times n) = O(n^2)$   
 $O(n^2)$  Time,  $O(1)$  Space

"Archit"  
 str

Total Time  $= 1+2+3+\dots+n$   
 $= O(n^2)$

- ① " " + 't' = "t" 1 operat
- ② "t" + 'i' = "ti" 2 operat
- ③ "ti" + 'l' = "til" 3 operat
- ④ "til" + 'c' = "tilc" 4 operat
- ⑤ "tilc" + 'r' = "tilcr" 5 operat
- ⑥ "tilcr" + 'o' = "tilcro" 6 operat

Reverse string  
Optimized Approach

```
// O(N) Time
char[] arr = new char[str.length()];
int left = 0, right = str.length() - 1;
while(left < str.length()){
    arr[left] = str.charAt(right);
    left++; right--;
}
String res = new String(arr);
return res;
```

Input  
 abcd  
 $\downarrow$   
 $O(n)$

Output  
 dcba  
 $\downarrow$   
 $O(n)$

Extra Space  $\rightarrow O(n)$

$O(n)$  Time  
 $O(n)$  Space

$O(n)$  time,  $O(n)$  space

## ~~String Compression~~

```

Input space → O(N)
Output space → O(N)

if(str.length() == 0) return "";
char ch = str.charAt(0);
int freq = 1;
String output = "";

for(int i=1; i<str.length(); i++){
    if(str.charAt(i - 1) != str.charAt(i)){
        output = output + ch + freq;
        ch = str.charAt(i);
        freq = 1;
    } else {
        freq++;
    }
}

output = output + ch + freq;
return output;

```

Extra space → O(1)

### Best case

"aaaaaaa"

ch = 'a' , f = 8

res = "

~~unlike str only one~~

" + 'a' + 8

O(n)

### Worst case

"abcdefghijklm"

ch = 'a' , f = 1

res = "

" + 'a' + 1

"a" + 'b' + 1

"ab" + 'c' + 1

"abc" + 'd' + 1

"abcd" + 'e' + 1

"abcde" + 'f' + 1

"abcdef" + 'g' + 1

"abcdefg" + 'h' + 1

"abcdefgh" + 'i' + 1

"abcdefghi" + 'j' + 1

"abcdefgij" + 'k' + 1

"abcdefgijk" + 'l' + 1

"abcdefgijkl" + 'm' + 1

"abcdefgijklm"

$$2+n+f+\dots+2+n = O(n^2)$$

## ~~Merge 2 Sorted Arrays~~

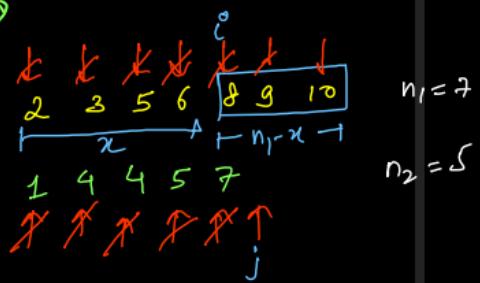
Extra space → O(1)  
Input → O(N) + O(M)  
Output → O(N + M)

```

int i = 0, j = 0, k = 0;
while (i < n1 && j < n2) {
    if (arr1[i] < arr2[j])
        arr3[k++] = arr1[i++];
    else
        arr3[k++] = arr2[j++];
}
while (i < n1)
    arr3[k++] = arr1[i++];
while (j < n2)
    arr3[k++] = arr2[j++];

```

$$\left\{ \begin{array}{l} n_2+x \\ n_1-x \\ 0 \end{array} \right.$$



$$T(n+m) = T(n+m-1) + O(1)$$

$\hookrightarrow O(n+m)$

$$\begin{aligned} (n_2+x) + (n_1-x) + 0 \\ = O(n_1+n_2) \end{aligned}$$

The diagram illustrates the insertion sort algorithm and its time complexity analysis.

**Code:**

```

Start of
int i = 0;
for(int j=0; j<arr.length; j++){
    if(arr[j] == 0){
        int temp = arr[i];
        arr[i] = arr[j];
        arr[j] = temp;
        i++;
    }
}
return arr;

```

**Diagram:**

A 2D array representation of the input array. The columns are labeled  $i$  and  $j$ . The array contains binary values (0 or 1). The first column ( $i$ ) has values 0, 0, 0, 1, 1, 1, 1. The second column ( $j$ ) has values 1, 2, 3, 4, 5, 6, 7. Handwritten annotations show arrows indicating the swap of element 0 at index 3 with element 1 at index 2, and so on.

**Analysis:**

Annotations above the array indicate the movement of element 0:  $0 \rightarrow \text{left}$  and  $1 \rightarrow \text{right}$ .

**Time Complexity:**

The time complexity is analyzed as follows:

- Best case:**  $\Theta(N)$
- Average case:**  $\Theta(N^2)$
- Worst case:**  $\Theta(N^2)$

**Space Complexity:**

Extra space  $\Rightarrow \Theta(1)$

**Output:**

Input  $\rightarrow$  Binary Array  $\sim O(N)$   
 Output  $\rightarrow$  Binary Array  $\sim O(N)$

Equilibrium Point or Pivot Index

```

public int pivotIndex(int[] nums) {
    int[] pref = new int[nums.length];
    pref[0] = nums[0];
    for(int i=1; i<nums.length; i++){
        pref[i] = pref[i - 1] + nums[i];
    }

    for(int i=0; i<nums.length; i++){
        int leftSum = (i == 0) ? 0 : pref[i - 1];
        int rightSum = (i == nums.length - 1) ? 0 : (pref[nums.length - 1] - pref[i]);
        if(leftSum == rightSum) return i;
    }
    return -1;
}

```

} Prefix Array → O(n)

} → O(n)

Input → 1D Array → O(n)  
Output → Pivot Index → O(1)

Extra space → O(n)  
(Prefix Array)

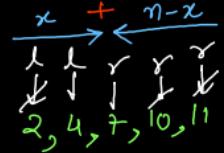


PrefSum → O(n)

# Two Pointers → Two sum

```
int start = 0, end = nums.length - 1;
while(start < end){
    if(nums[start] + nums[end] == target){
        res[0] = start + 1; res[1] = end + 1;
        return res;
    } else if(nums[start] + nums[end] < target){
        start++;
    } else {
        end--;
    }
}
```

Two Pointers  $\Rightarrow$  Dependent  
on each other.

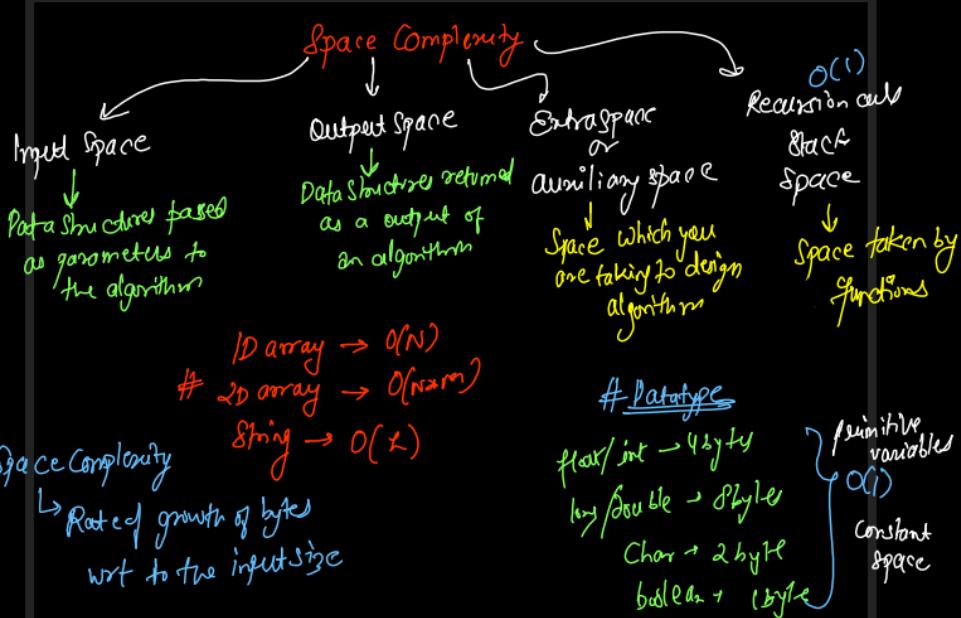


$13 > 11$   
 $12 > 11$   
 $9 < 11$   
 $11 = 11$

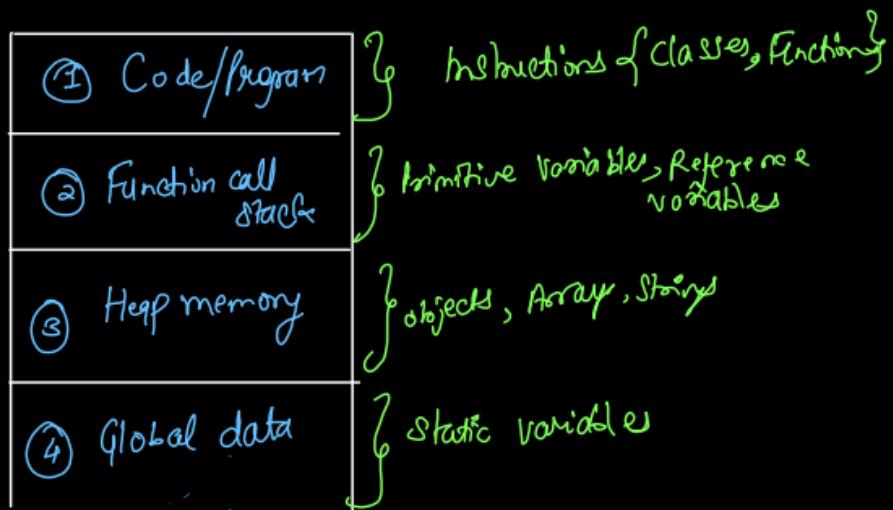
Total time =  $x + n - x$

$\Rightarrow O(N)$

Input Space  $\rightarrow O(N)$   
Output space  $\rightarrow 8 \text{ bytes} \rightarrow \text{Pair} \rightarrow O(1)$   
Extra space  $\rightarrow 8 \text{ bytes} \rightarrow [L, R] \rightarrow O(1)$



## Process Memory Layout

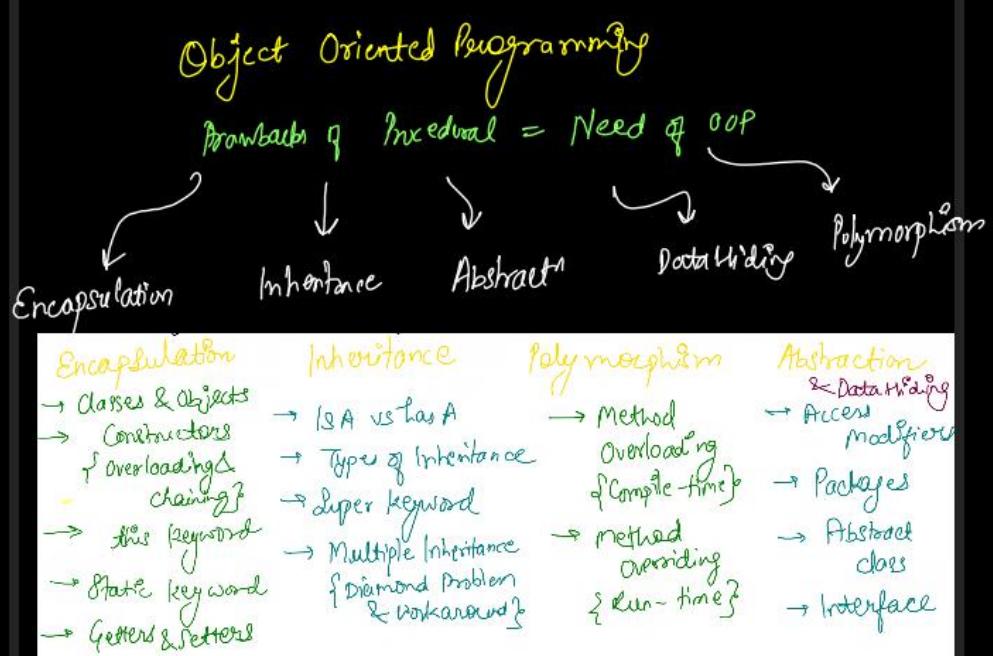
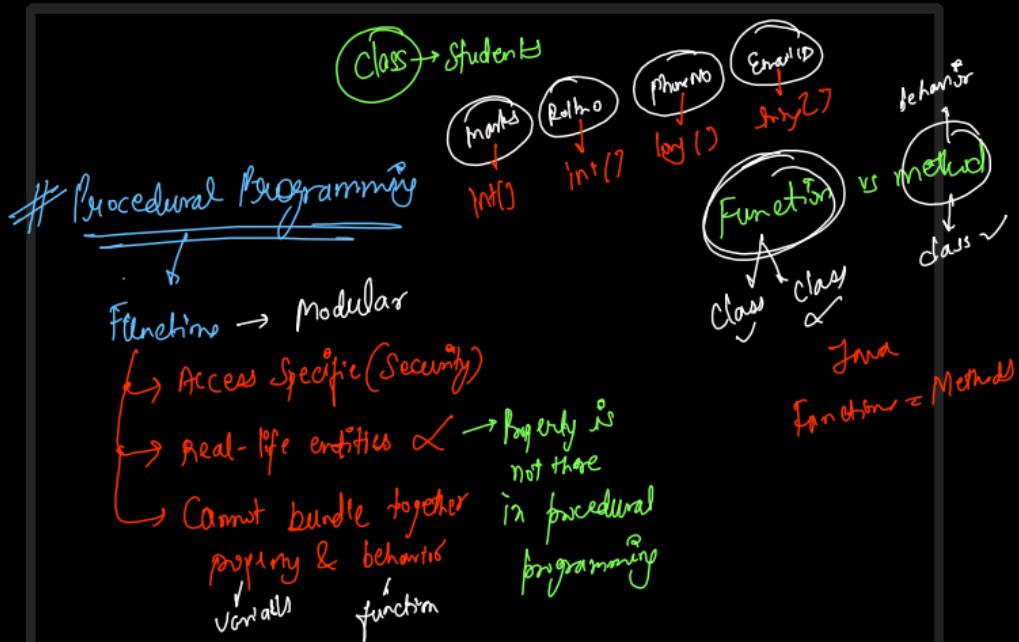


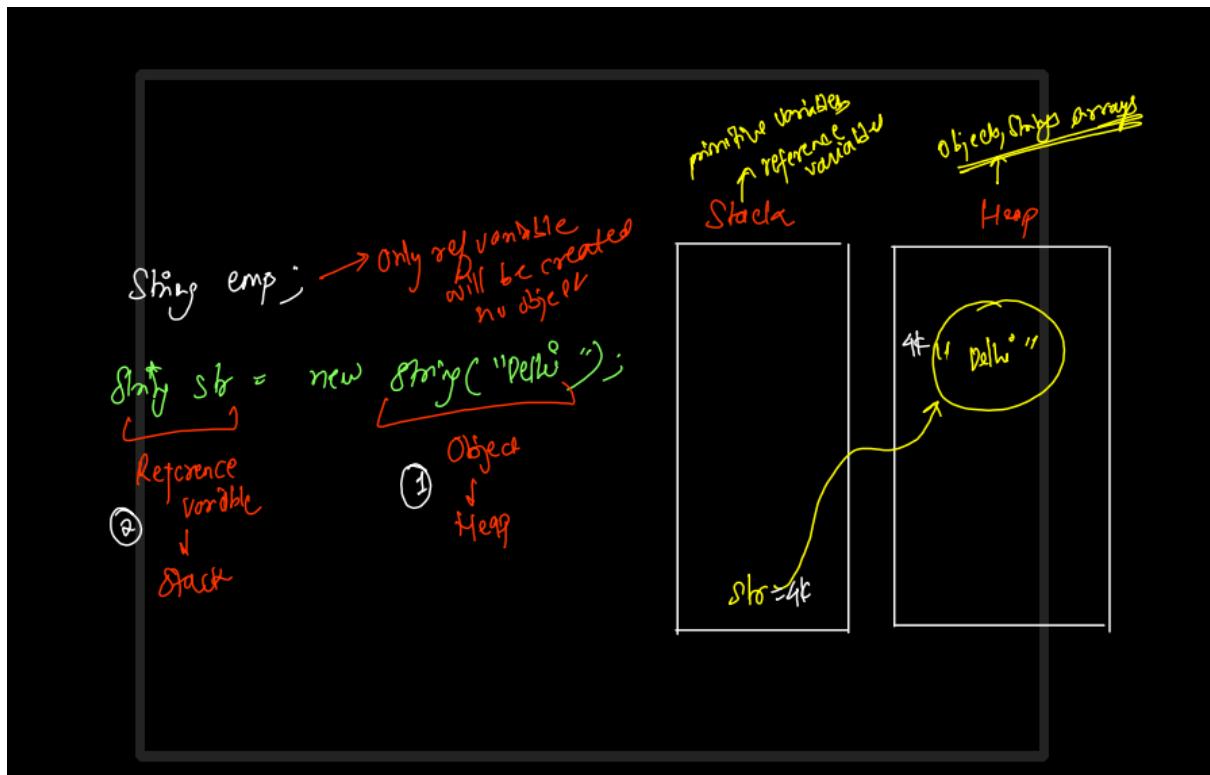
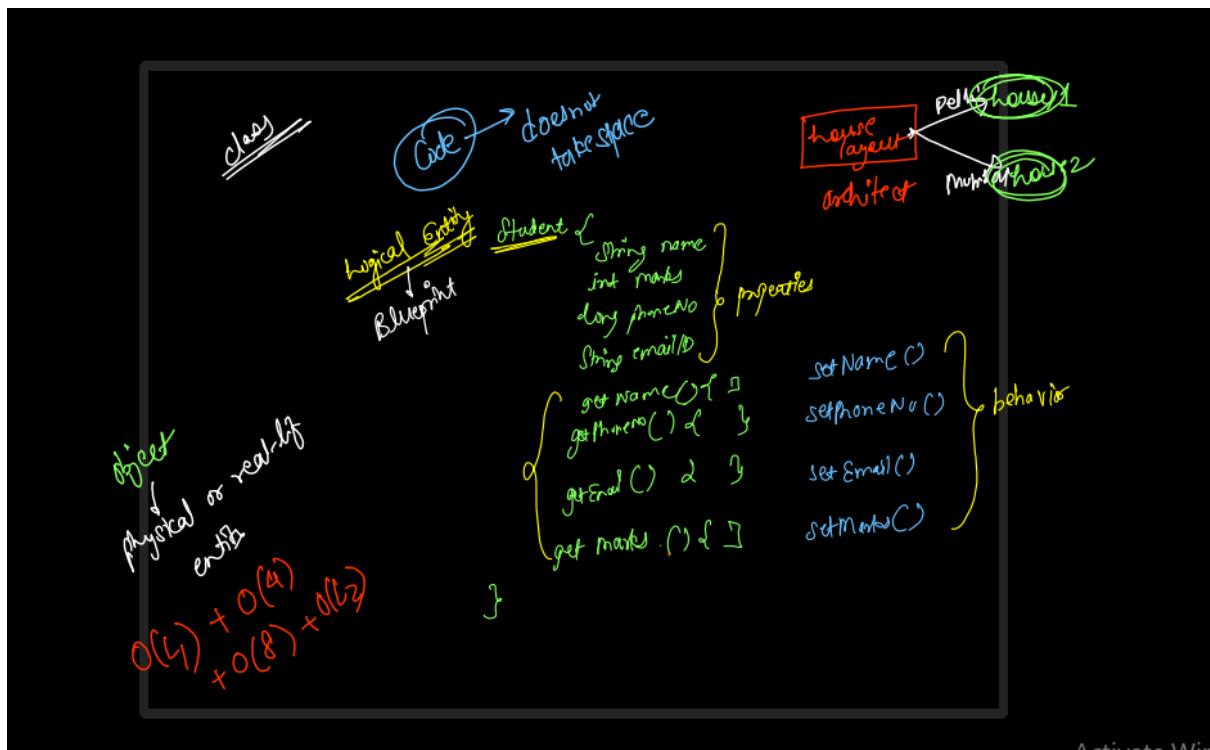
# Runtime vs Extra Space Tradeoff  
Time vs Space Complexity Tradeoff

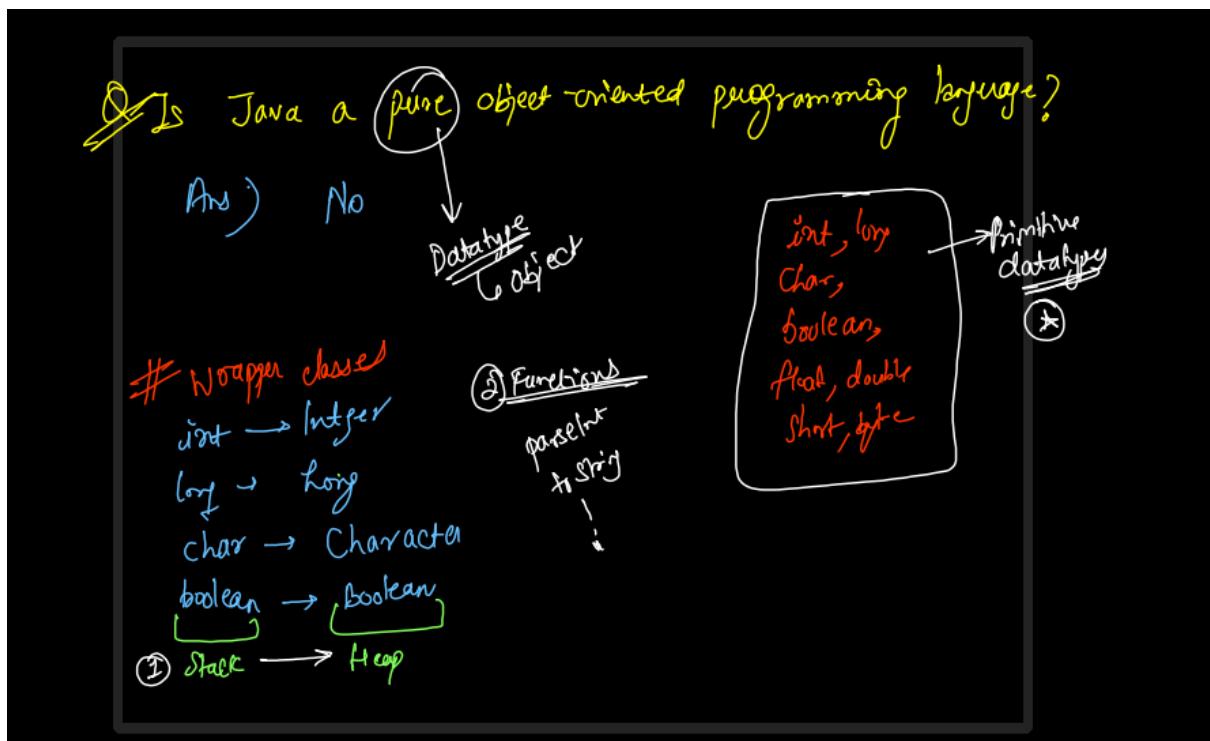
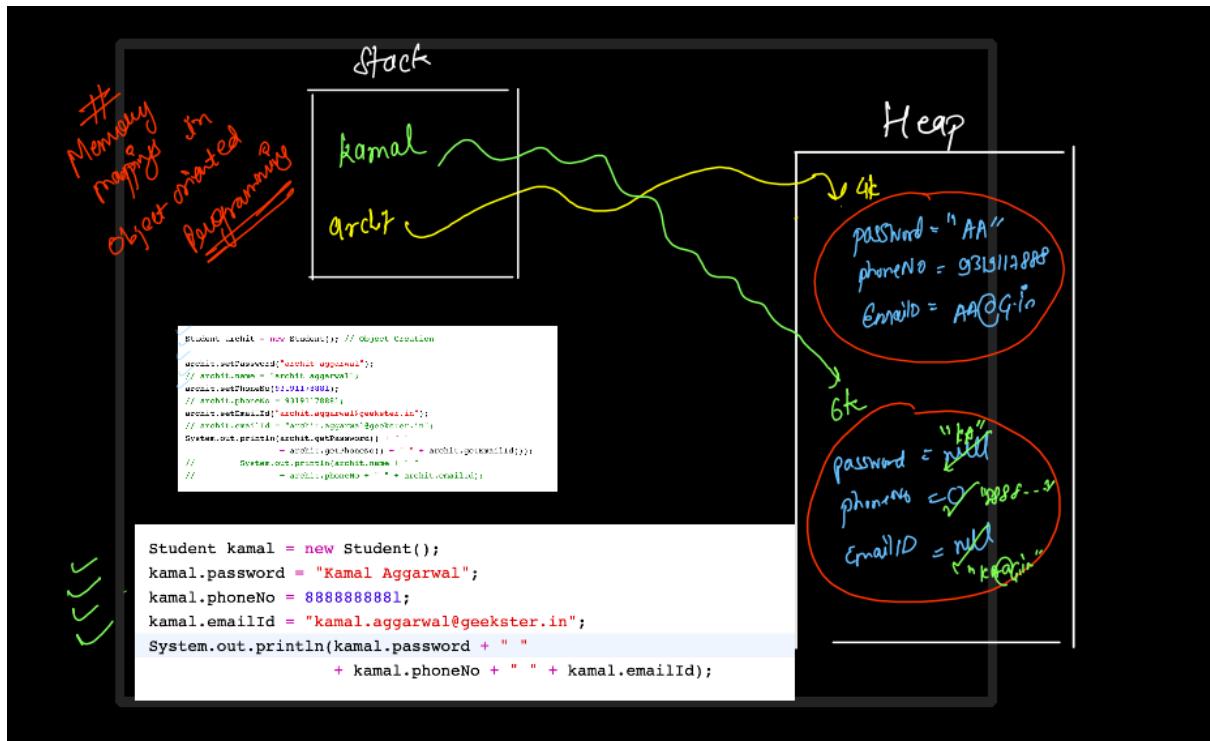
~~Brute force~~ ① Time ↑ Space ↓  
~~Optimized Approach~~ ② Time ↓ Space ↑

# Time → Expensive

# Space → Cheap







Reference variables are getting swapped  
↑  
not the objects

```

public static void swap(Student s1, Student s2){
    Student temp = s1;
    s1 = s2;
    s2 = temp;
}

Student archit = new Student();
archit.password = "archit agarwal";
archit.phoneNo = 93191178881;
archit.emailId = "archit.aggarwal@geekster.in";
System.out.println(archit.password + " "
    + archit.phoneNo + " " + archit.emailId);

Student kamal = new Student();
kamal.password = "Kamal Aggarwal";
kamal.phoneNo = 8888888881;
kamal.emailId = "Kamal.aggarwal@geekster.in";
System.out.println(kamal.password + " "
    + kamal.phoneNo + " " + kamal.emailId);

swap(archit, kamal);

System.out.println(archit.password + " "
    + archit.phoneNo + " " + archit.emailId);

System.out.println(kamal.password + " "
    + kamal.phoneNo + " " + kamal.emailId);

```

① Archit, ② Kamal, ③ Kamal, ④ Archit (copy swap)  
 ⑤ Archit, Kamal, Archit, Archit  
 ⑥ Archit, Kamal, Kamal, Kamal  
 ⑦ Archit, Kamal, Archit, Kamal (Deep)

Reference variables (Stack) are getting updated/copied,  
then you are performing a shallow copy ①

⇒ Objects are intact (They are not getting copied/updated)

Swap 1

```

public static void swap(Student s1, Student s2){
    Student temp = s1;
    s1 = s2;
    s2 = temp;
}

```

```

public static void swap2(Student s1, Student s2){
    Student temp = new Student();
    temp.password = s1.password;
    temp.phoneNo = s1.phoneNo;
    temp.emailId = s1.emailId;

    s1 = s2;
    s2 = temp;
}

```

```

Student archit = new Student();
archit.password = "archit agarwal";
archit.phoneNo = 93191178881;
archit.emailId = "archit.aggarwal@geekster.in";
System.out.println(archit.password + " "
+ archit.phoneNo + " " + archit.emailId);

Student kamal = new Student();
kamal.password = "Kamal Aggarwal";
kamal.phoneNo = 8888888881;
kamal.emailId = "kamal.aggarwal@geekster.in";
System.out.println(kamal.password + " "
+ kamal.phoneNo + " " + kamal.emailId);

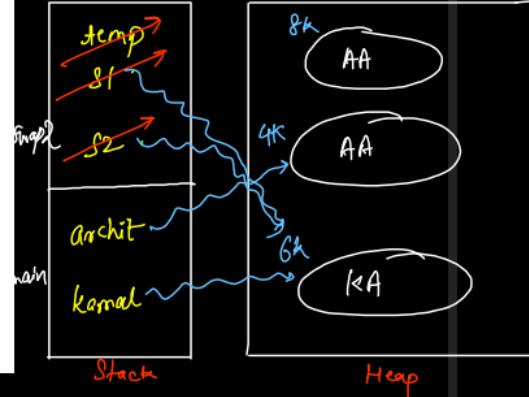
swap(archit, kamal);

System.out.println(archit.password + " "
+ archit.phoneNo + " " + archit.emailId);

System.out.println(kamal.password + " "
+ kamal.phoneNo + " " + kamal.emailId);

```

- A Archit, Kamal, Kamal, Archit  
 B Archit, Kamal, Archit, Archit  
 C Archit, Kamal, Kamal, Kamal  
 D Archit, Kamal, Archit, Kamal



Activate Wi-Fi

```

public static void swap3(Student s1, Student s2){
    Student temp = new Student();
    temp.password = s1.password;
    temp.phoneNo = s1.phoneNo;
    temp.emailId = s1.emailId;

    s1.password = s2.password;
    s1.phoneNo = s2.phoneNo;
    s1.emailId = s2.emailId;

    s2 = temp;
}

Student archit = new Student();
archit.password = "archit agarwal";
archit.phoneNo = 93191178881;
archit.emailId = "archit.aggarwal@geekster.in";
System.out.println(archit.password + " "
+ archit.phoneNo + " " + archit.emailId);

Student kamal = new Student();
kamal.password = "Kamal Aggarwal";
kamal.phoneNo = 8888888881;
kamal.emailId = "kamal.aggarwal@geekster.in";
System.out.println(kamal.password + " "
+ kamal.phoneNo + " " + kamal.emailId);

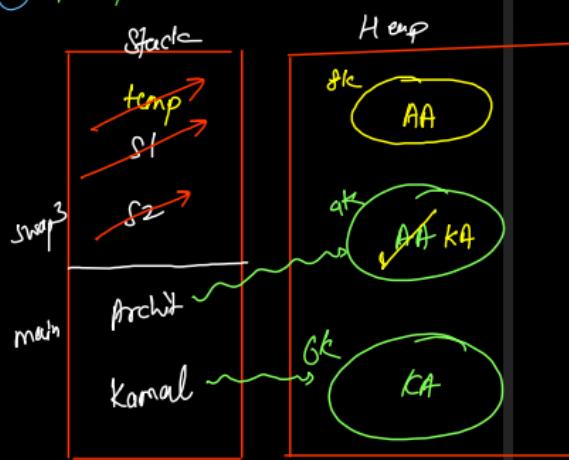
swap(archit, kamal);

System.out.println(archit.password + " "
+ archit.phoneNo + " " + archit.emailId);

System.out.println(kamal.password + " "
+ kamal.phoneNo + " " + kamal.emailId);

```

- A Archit, Kamal, Kamal, Archit  
 B Archit, Kamal, Archit, Archit  
 C Archit, Kamal, Kamal, Kamal  
 D Archit, Kamal, Archit, Kamal



If the actual object is getting copied into a new object (and not just the reference variables), it is known as deep copy ⚡

```
public static void swap4(Student s1, Student s2){  
    Student temp = new Student();  
    temp.password = s1.password;  
    temp.phoneNo = s1.phoneNo;  
    temp.emailId = s1.emailId;  
  
    s1.password = s2.password;  
    s1.phoneNo = s2.phoneNo;  
    s1.emailId = s2.emailId;  
  
    s2.password = temp.password;  
    s2.phoneNo = temp.phoneNo;  
    s2.emailId = temp.emailId;  
}
```

## # Initialization

```
public void initialize(String newPassword, long newPhoneNo, String newEmailId){  
    setPassword(newPassword);  
    setPhoneNo(newPhoneNo);  
    setEmailId(newEmailId);  
}  
  
Student archit = new Student();  
archit.initialize("archit aggarwal", 9319117881, "archit@geekster.in");  
  
System.out.println(archit.password + " "  
                  + archit.phoneNo + " " + archit.emailId);  
  
Student kamal = new Student();  
kamal.initialize("kamal aggarwal", 888888888881, "kamal@geekster.in");  
System.out.println(kamal.password + " "  
                  + kamal.phoneNo + " " + kamal.emailId);
```

## # Dynamic Initialization

```
// Constructor  
public Student(String newPassword, long newPhoneNo, String newEmailId){  
    setPassword(newPassword);  
    setPhoneNo(newPhoneNo);  
    setEmailId(newEmailId);  
}
```

```
Student archit = new Student("archit aggarwal", 93191178881, "archit@geekster.in");  
// archit.initialize("archit aggarwal", 93191178881, "archit@geekster.in");  
  
System.out.println(archit.password + " "  
+ archit.phoneNo + " ." + archit.emailId);  
  
Student kamal = new Student("kamal aggarwal", 888888888881, "kamal@geekster.in");  
// kamal.initialize("kamal aggarwal", 888888888881, "kamal@geekster.in");  
System.out.println(kamal.password + " "  
+ kamal.phoneNo + " ." + kamal.emailId);
```

### Constructors

# Dynamic Initialization → Creation of object + Initialization of properties

Constructor → Function which is called as soon as the object is created

① Constructor name → class name

② no return type

// Default constructor (implicitly)

```
public Student () {}
```

automatically provided by  
Compiler

① No parameters

② No body { default values of all properties }

int, long, short, byte → 0  
char → null character  
boolean → false  
float, double → 0.0  
reference var → null

```
// Constructor  
public Student(String newPassword, long newPhoneNo, String newEmailId){  
    setPassword(newPassword);  
    setPhoneNo(newPhoneNo);  
    setEmailId(newEmailId);  
}
```

But if you write a constructor of your own,  
the default constructor will be gone.

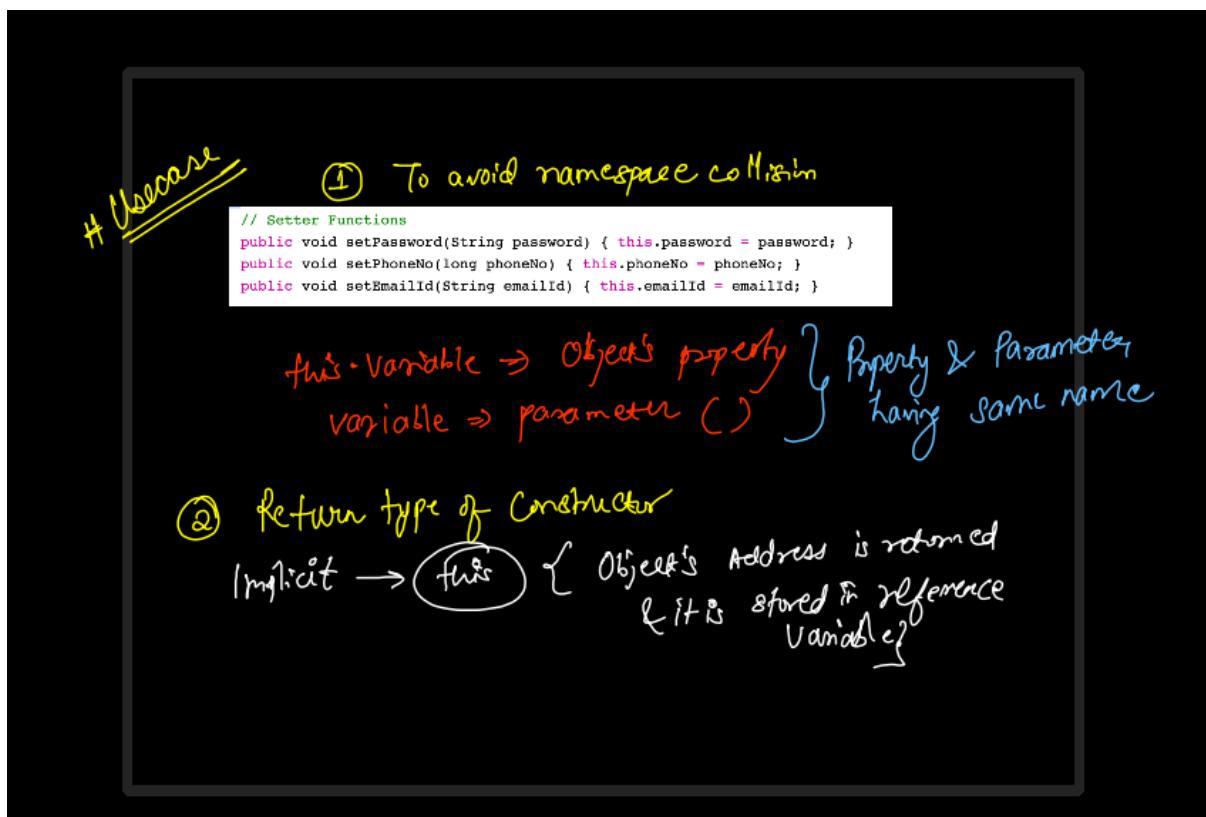
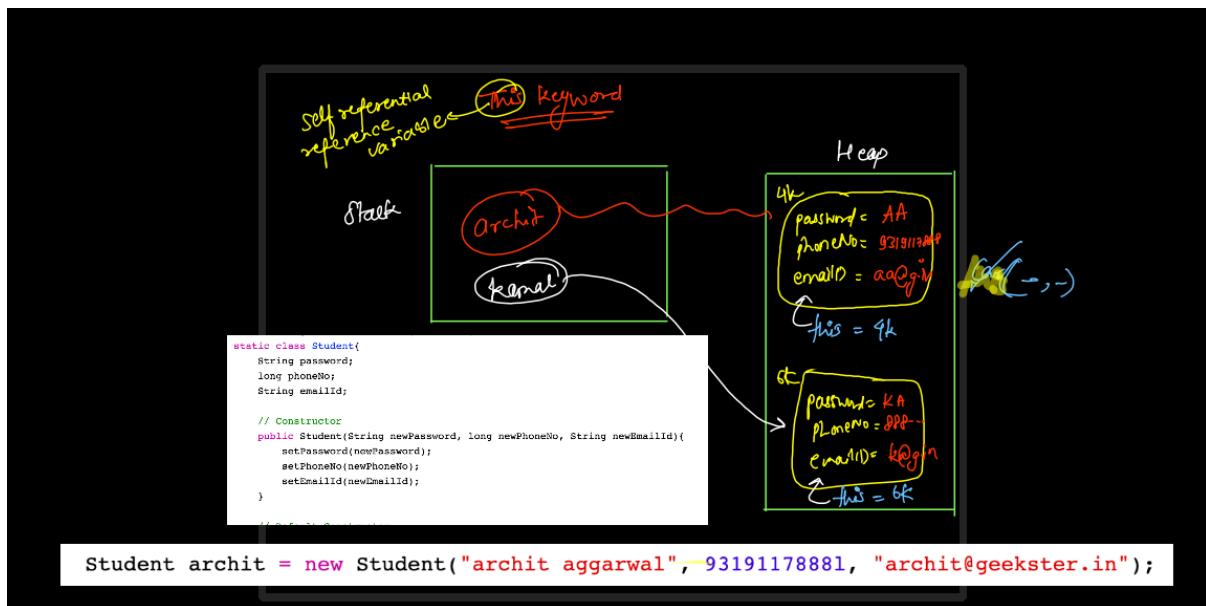
Explicit  
public Student () {}

2 functions with  
some name  
but different  
parameters

Function overloading

① Polymorphism  
↓  
Static/Compile  
Time  
Polymorphism

Activate Win



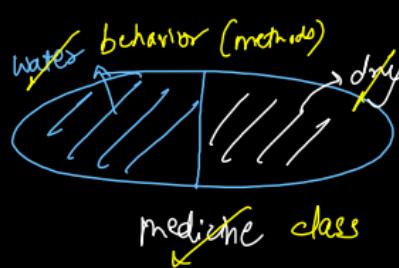
### ③ Constructor chaining

→ One constructor calls another constructor

```
static class Student{  
    String password;  
    long phoneNo;  
    String emailId;  
  
    // Constructor  
    public Student(String newPassword, long newPhoneNo, String newEmailId){  
        setPassword(newPassword);  
        setPhoneNo(newPhoneNo);  
        setEmailId(newEmailId);  
    }  
  
    // Default Constructor  
    public Student(){  
        this("admin", 8888888881, "admin@gmail.com");  
    }  
}
```

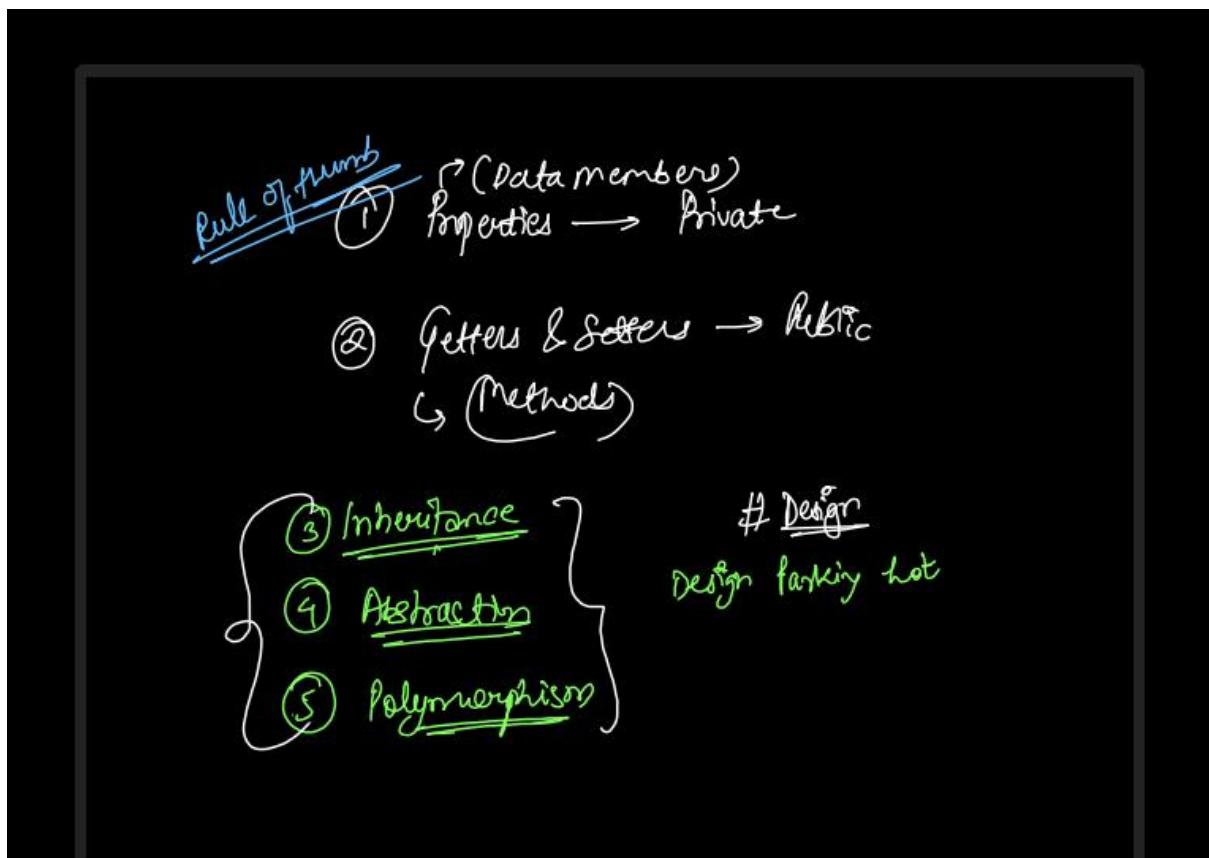
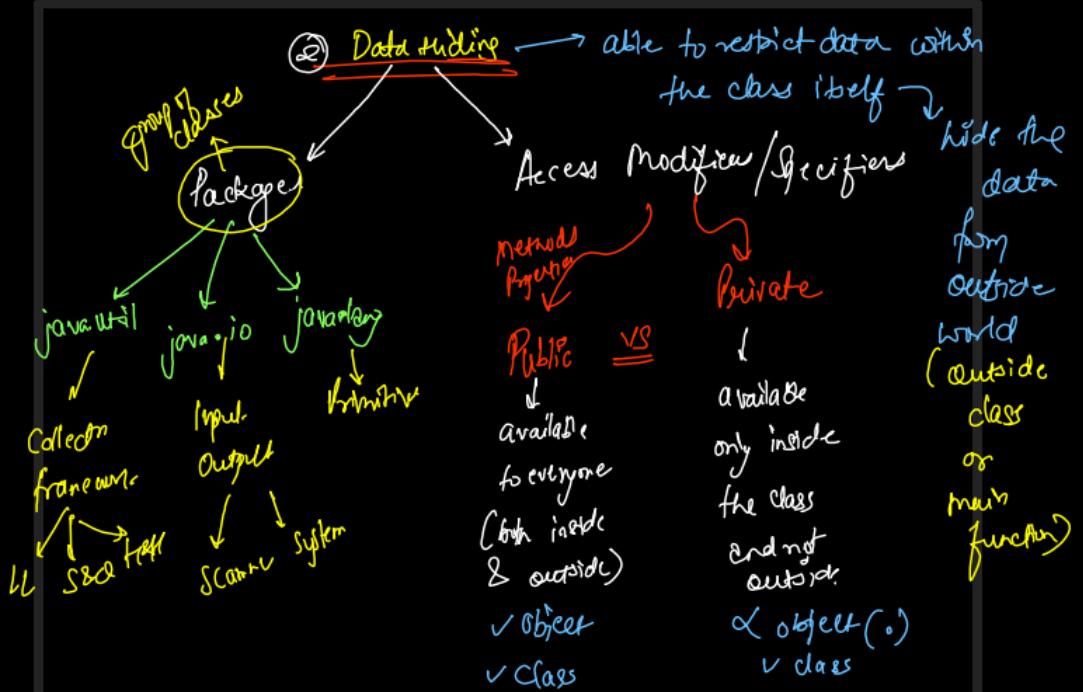
### ① Encapsulation

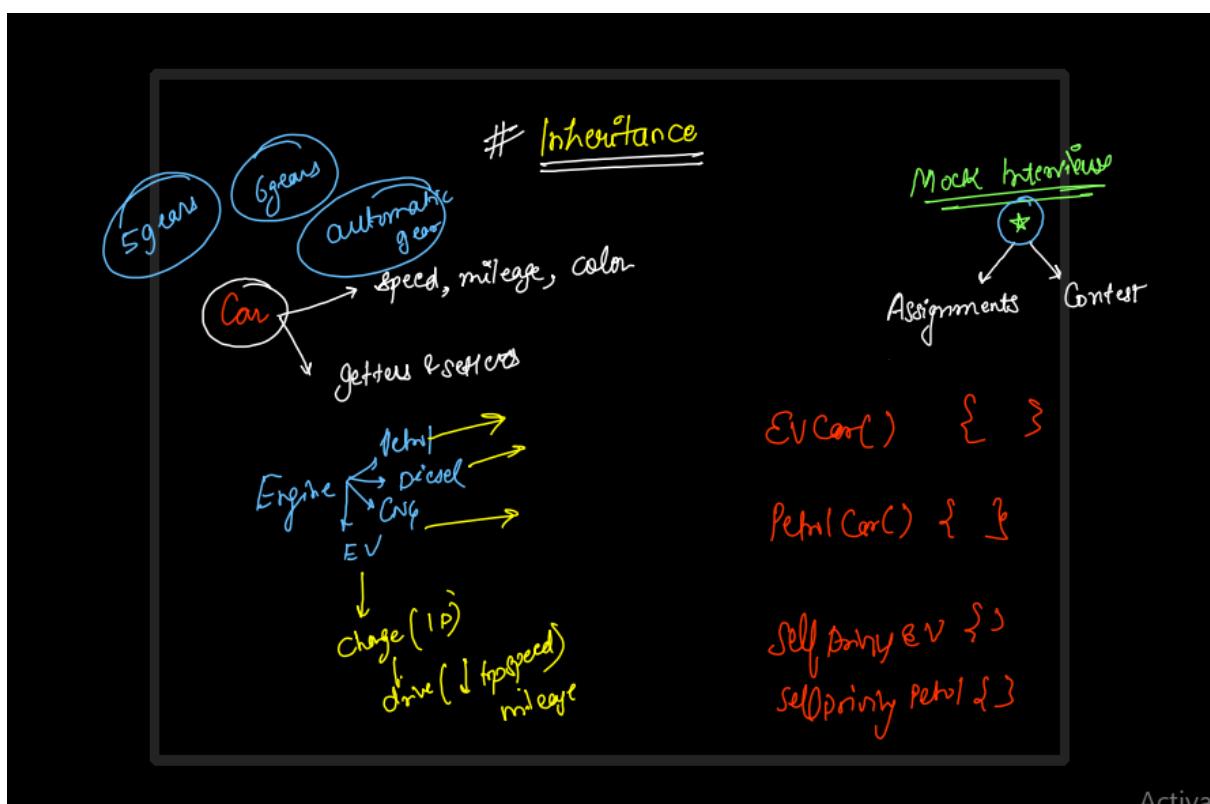
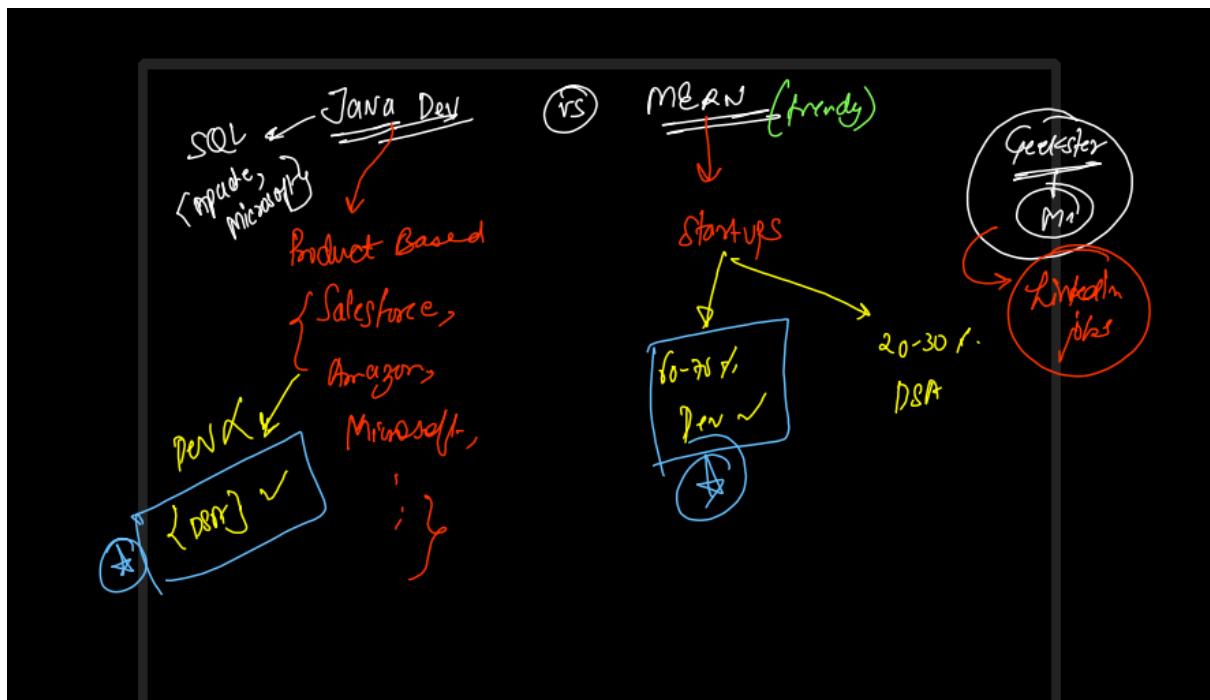
"Wrapping up data members (properties) with the behaviors (methods) into a single entity (class), this is known as encapsulation."



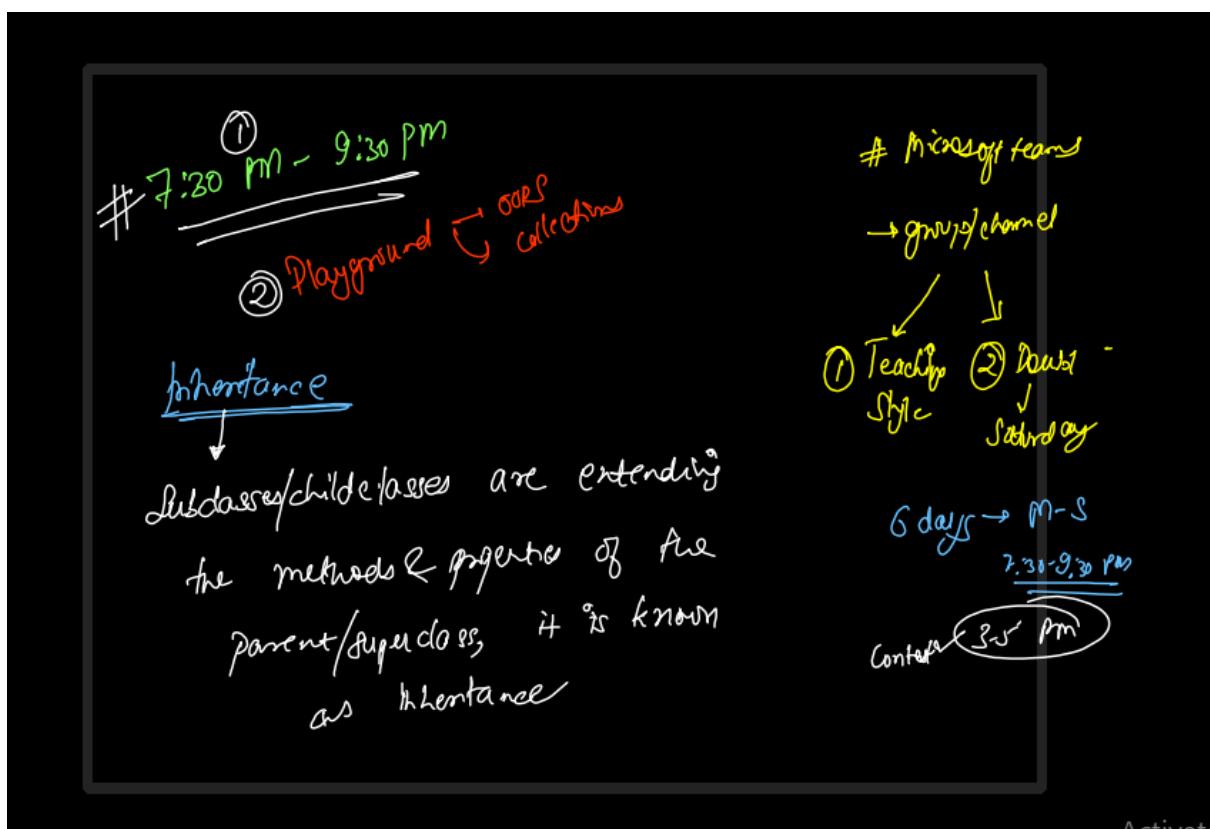
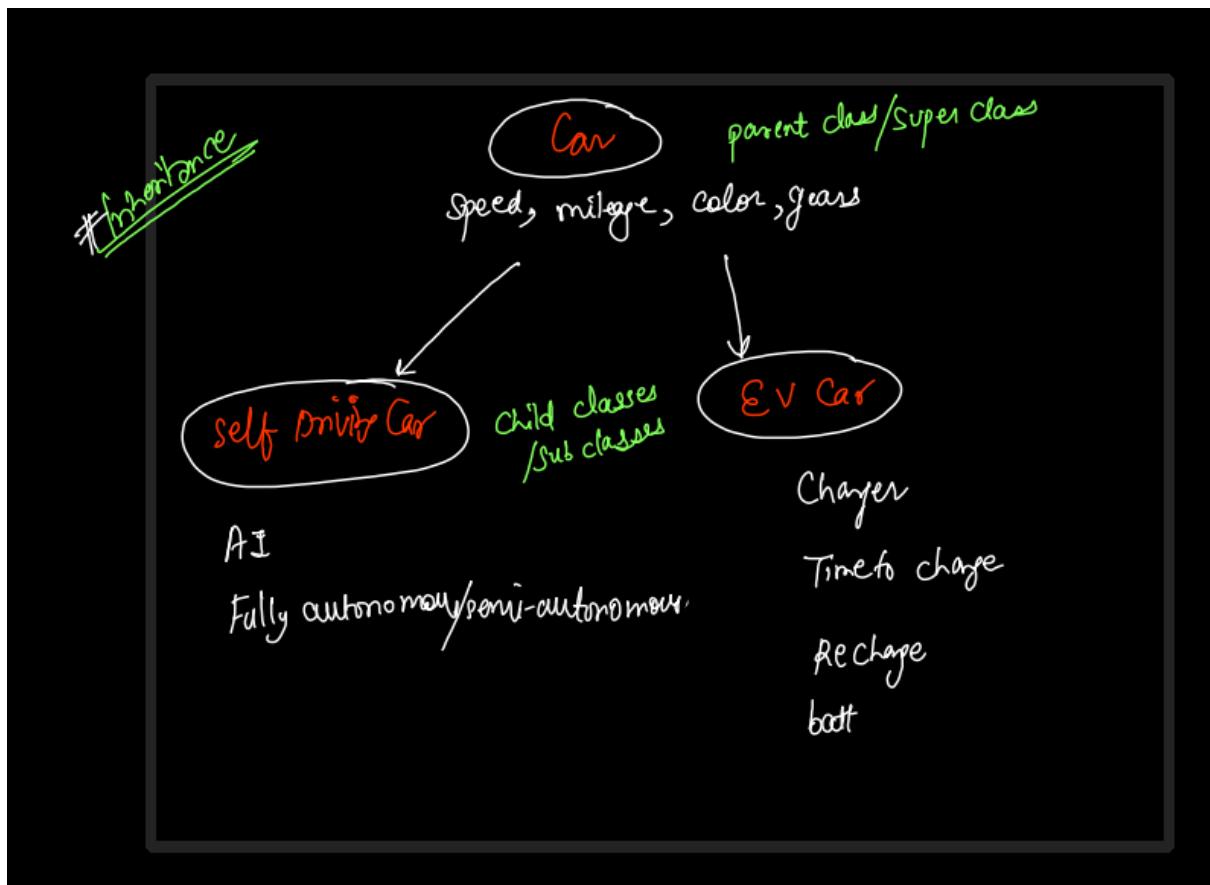
Implementation of  
Encapsulation

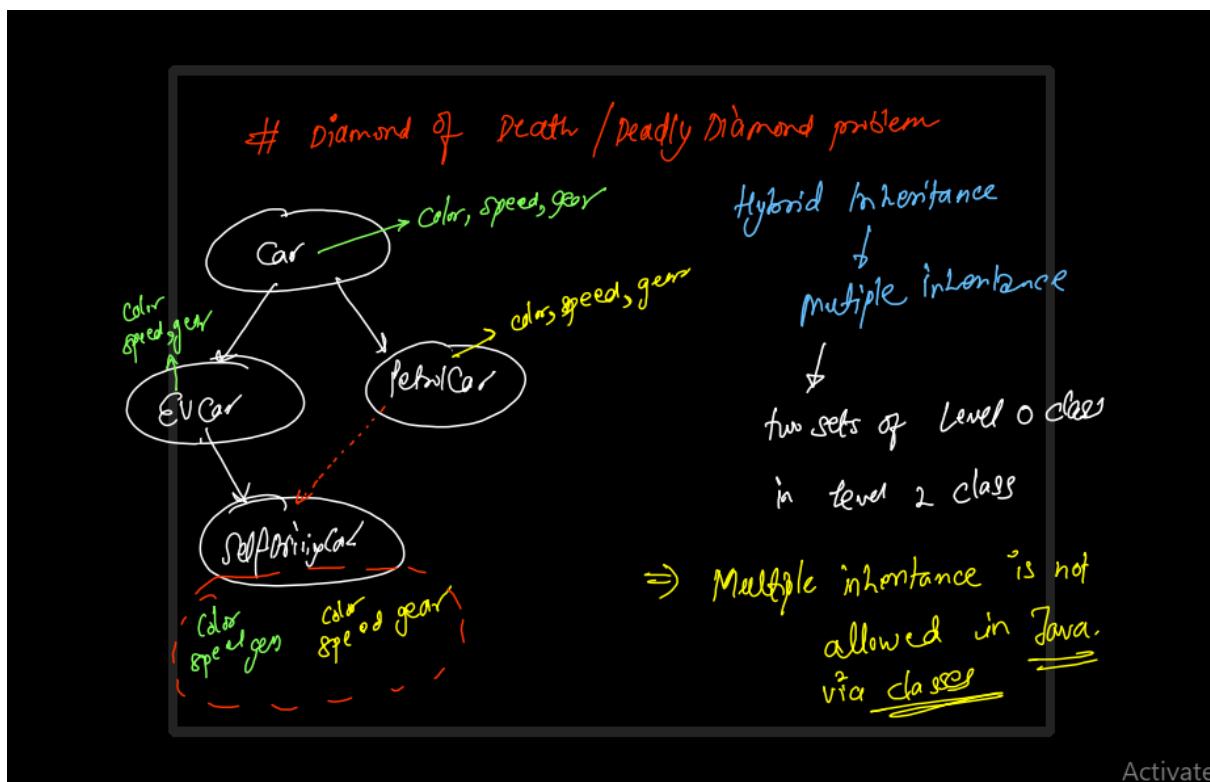
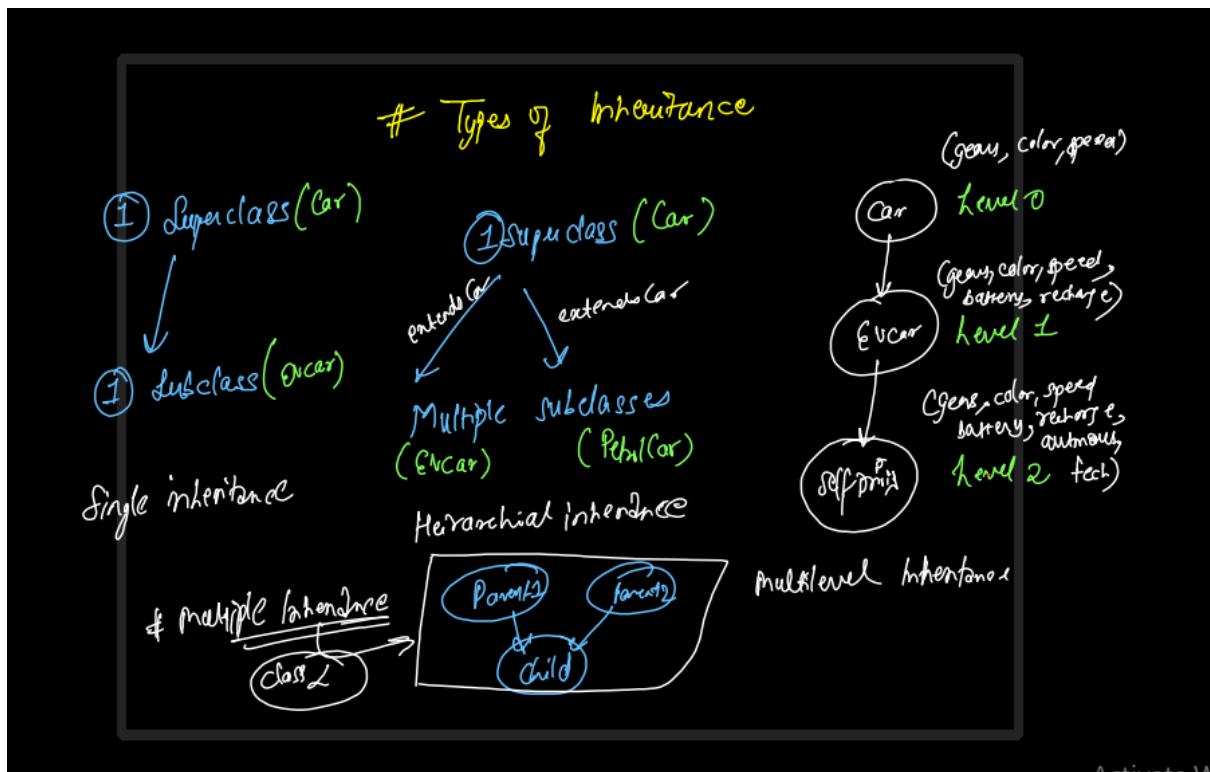
↓  
Writing a class  
& creating its object.





Activite





## ~~#~~ Super Keyword



Self referential variable → This

Reference pointing to parent class object → Super

Usecase ①

To avoid namespace collision

b/w 2 properties/ methods

b/w child class object

& parent class object

# speed ← Car's speed (Super)  
                  Motor's speed (This)

Usecase ②

```
public EVCar(int maxCapacity, int rechargeTime, String color, int gears, int speed){  
    super(gears, speed, color);  
    this.setMaxCapacity(maxCapacity);  
    this.setRechargeTime(rechargeTime);  
}
```

You can call parent's constructor

(parameters), Super can  
be used

```

class Car{
    private int speed; // Car's Speed
    private int gears;
    private String color;

    public Car(){ this(4, 5, "White"); }

    public Car(int speed, int gears, String color){
        setSpeed(speed);
        setGears(gears);
        setColor(color);
    }
}

class EVCar extends Car{
    private int maxCapacity;
    private int rechargeTime;
    private int speed; // Motor's Speed

    public EVCar(){
        this(100, 24);
        this.speed = 30;
    }

    public EVCar(int maxCapacity, int rechargeTime){
        this.setCapacity(maxCapacity);
        this.setRechargeTime(rechargeTime);
    }
}

```

`EVCar obj = new EVCar();`

Constructors In Inheritance

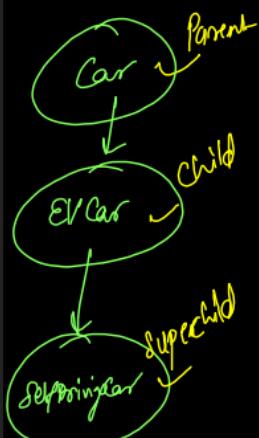
Order of Execution  
of Constructors

Parent  
① Car()  
Child  
② EVCar()  
↓

Order of calling  
of Constructors

① EVCar()  
② Car()  
↓

capacity, recharge  
speed, gears, color

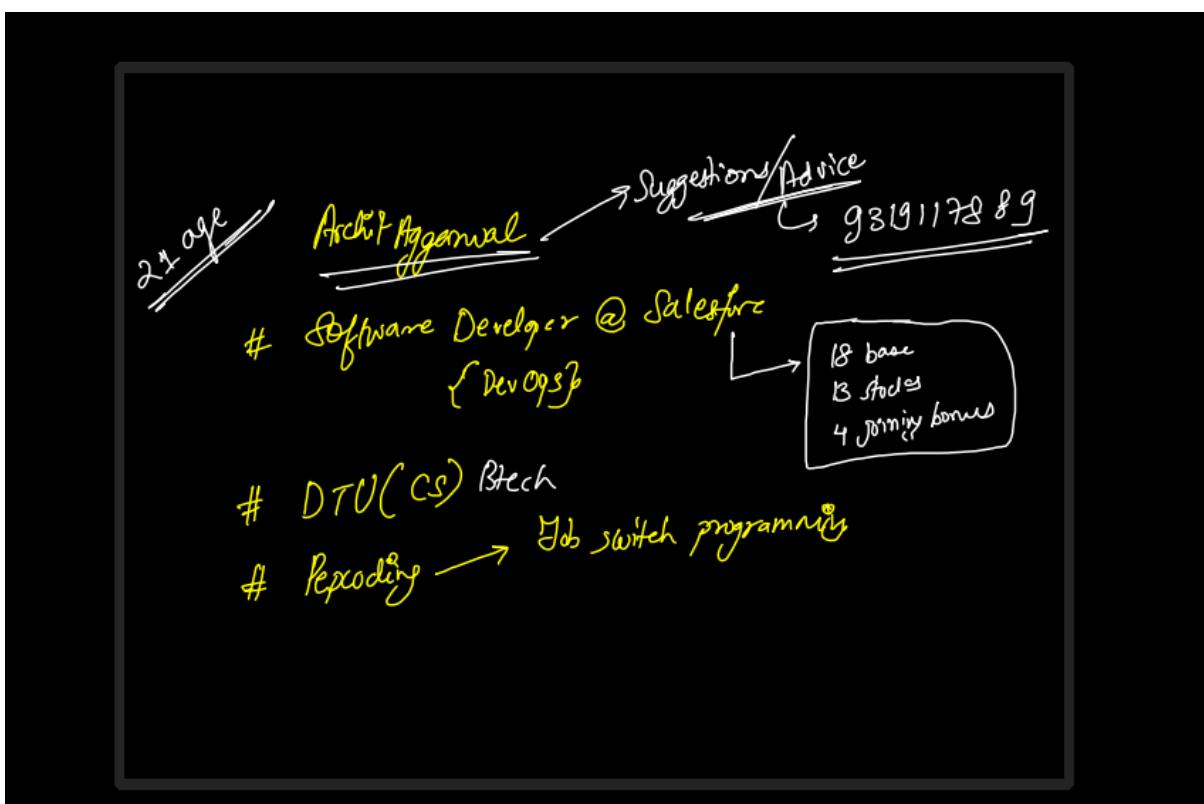
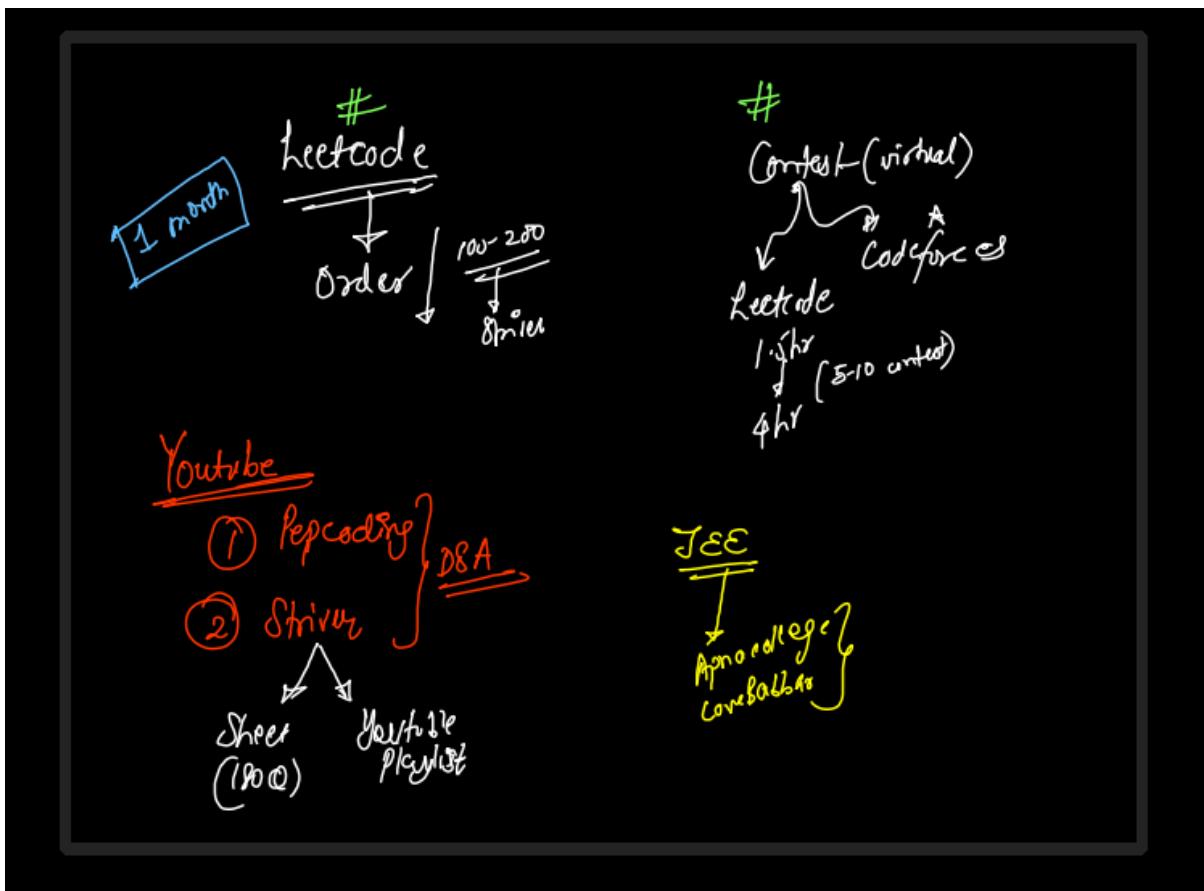


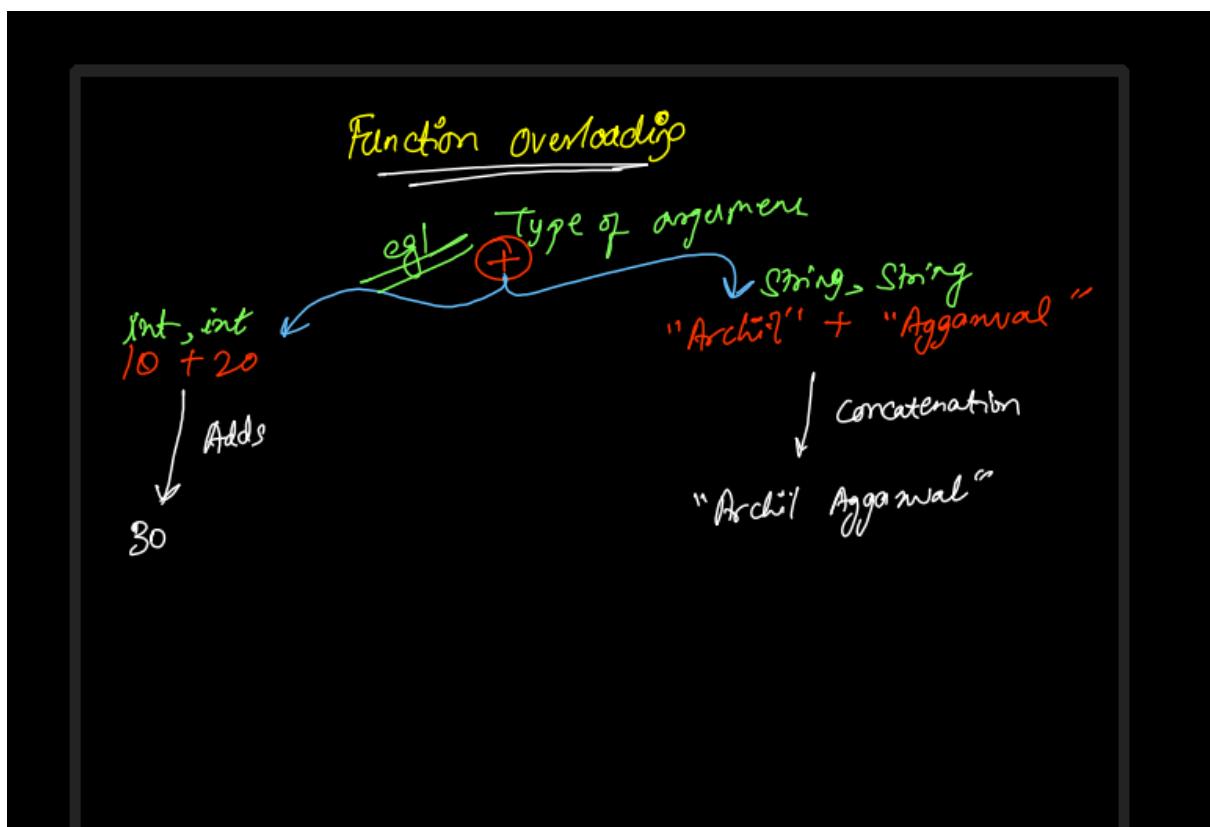
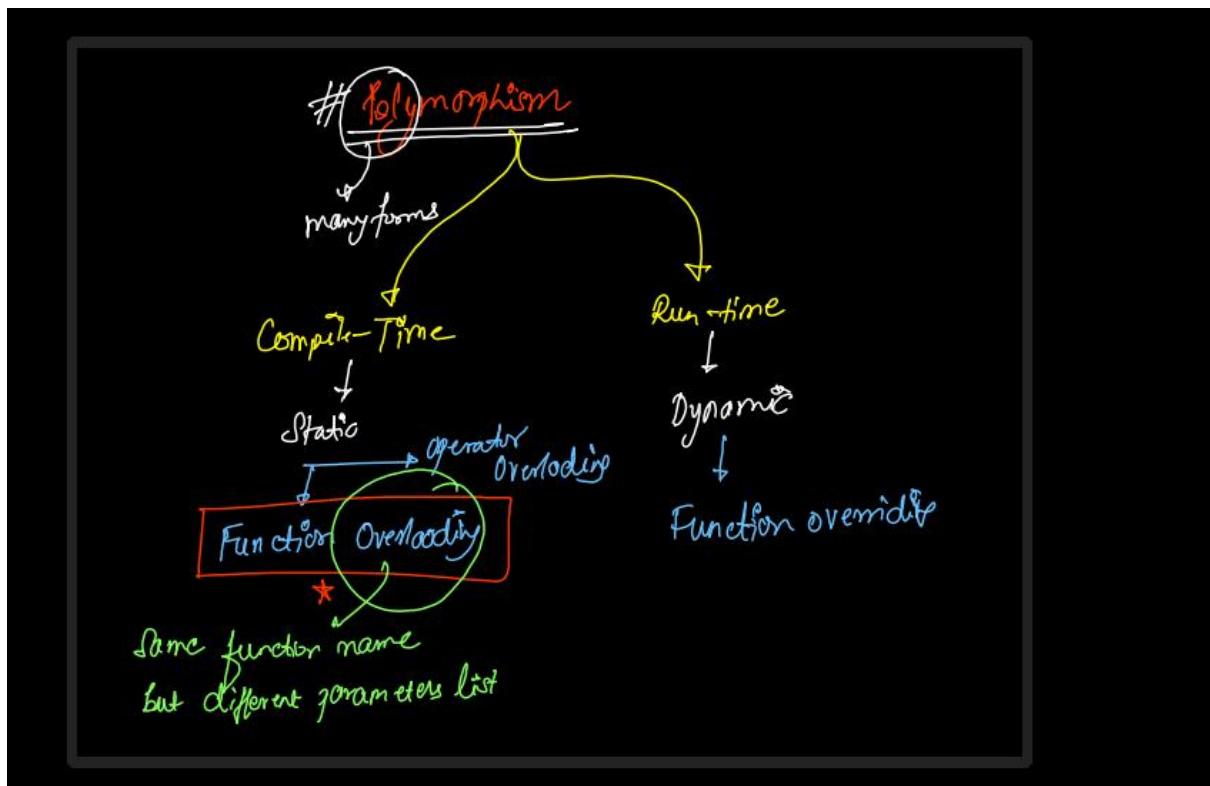
goal  
Order of calls  
① SelfDrivingCar()  
normal  
② EVCar()  
newer  
③ Car()

Order of Execution  
① Car() w,s,40  
② EVCar() 100% 24 L  
③ SelfDrivingCar()  
Fully Autonomous  
A7

`SelfDrivingCar obj = new SelfDrivingCar();`

8:35





~~Q2~~

Number of parameters

Function overloading

of function name should be same

① Number of arguments

② Type of arguments

③ Order of arguments

④ Changing the return type

Access modifier public, private

```

sum(int a, int b) {
    return a+b;
}

sum(int a, int b, int c) {
    return a+b+c;
}

```

```
// Type 1: DataType of arguments
public static int sum(int a, int b){
    return a + b;
}

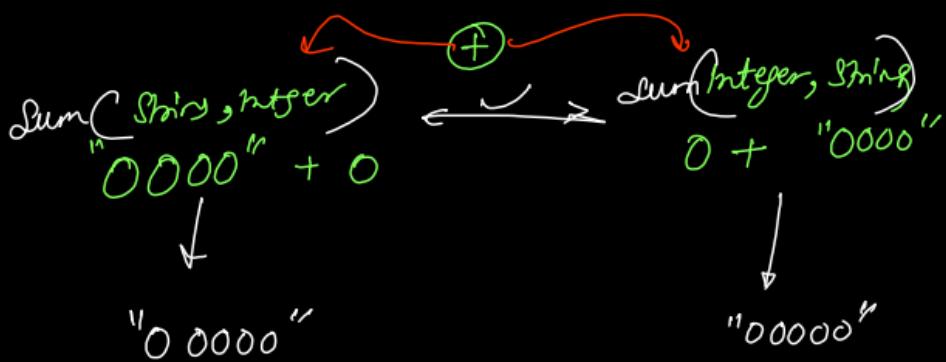
public static String sum(String a, String b){
    return a + b;
}

// Type 2: Number of arguments
public static int sum(int a, int b, int c){
    return a + b + c;
}

// Type 3: Order of Arguments
public static String sum(int a, String b){
    return a + b;
}

public static String sum(String a, int b){
    return a + b;
}
```

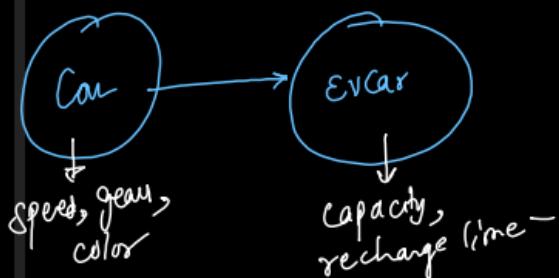
```
public static void functionOverloadingDemo(){
    System.out.println(sum(10, 20));
    System.out.println(sum("Archit", "Aggarwal"));
    System.out.println(sum(10, 20, 30));
    System.out.println(sum("Archit", 10));
    System.out.println(sum(10, "Archit"));
```



$\text{int fun(int, int)}$      $\leftrightarrow \text{void sum(int, int)}$

They cannot  
be overloaded  
 $\Rightarrow$  Return type ( $\lambda$ )

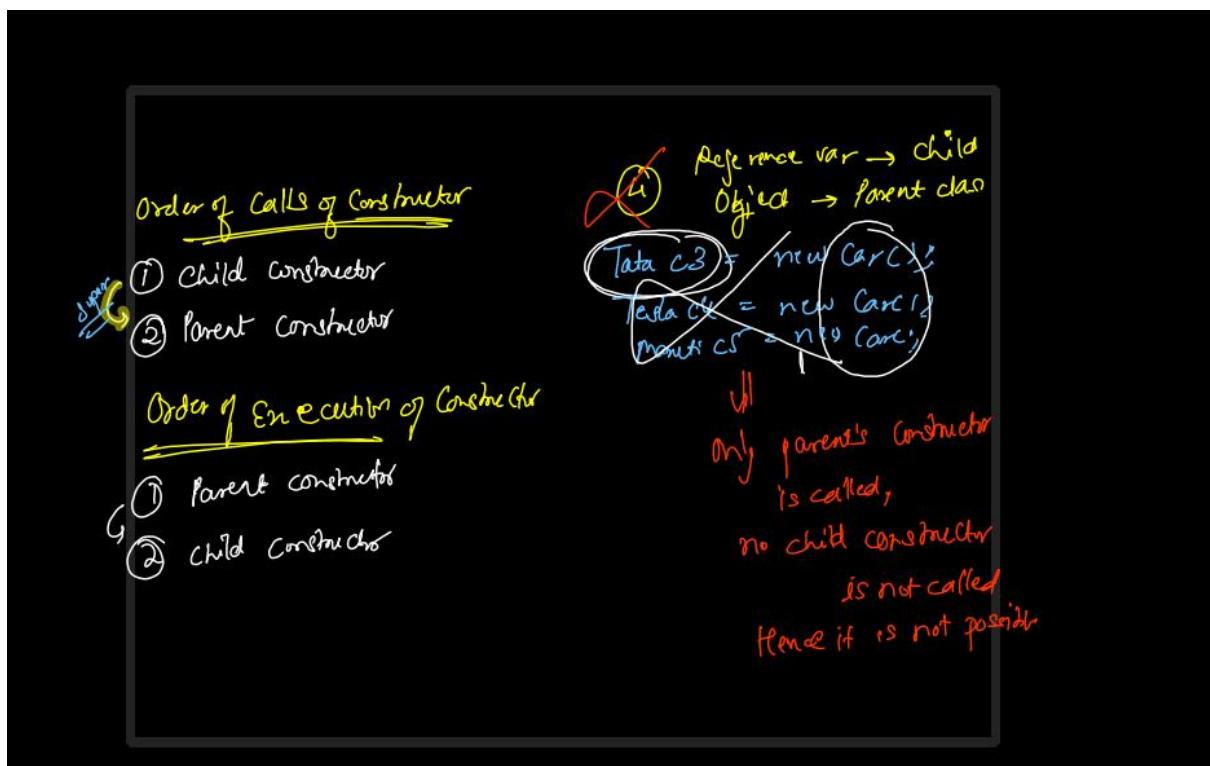
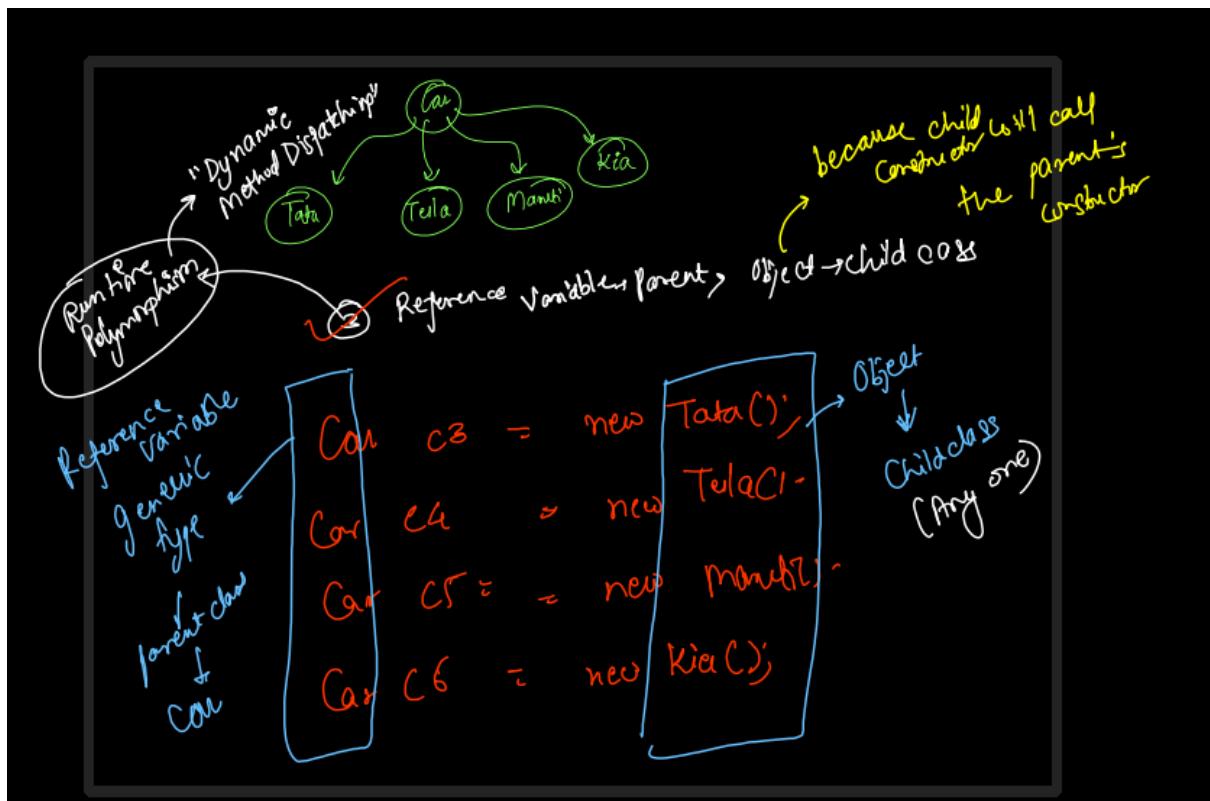
Runtime polymorphism  
or  
Dynamic polymorphism  
or  
Function overriding

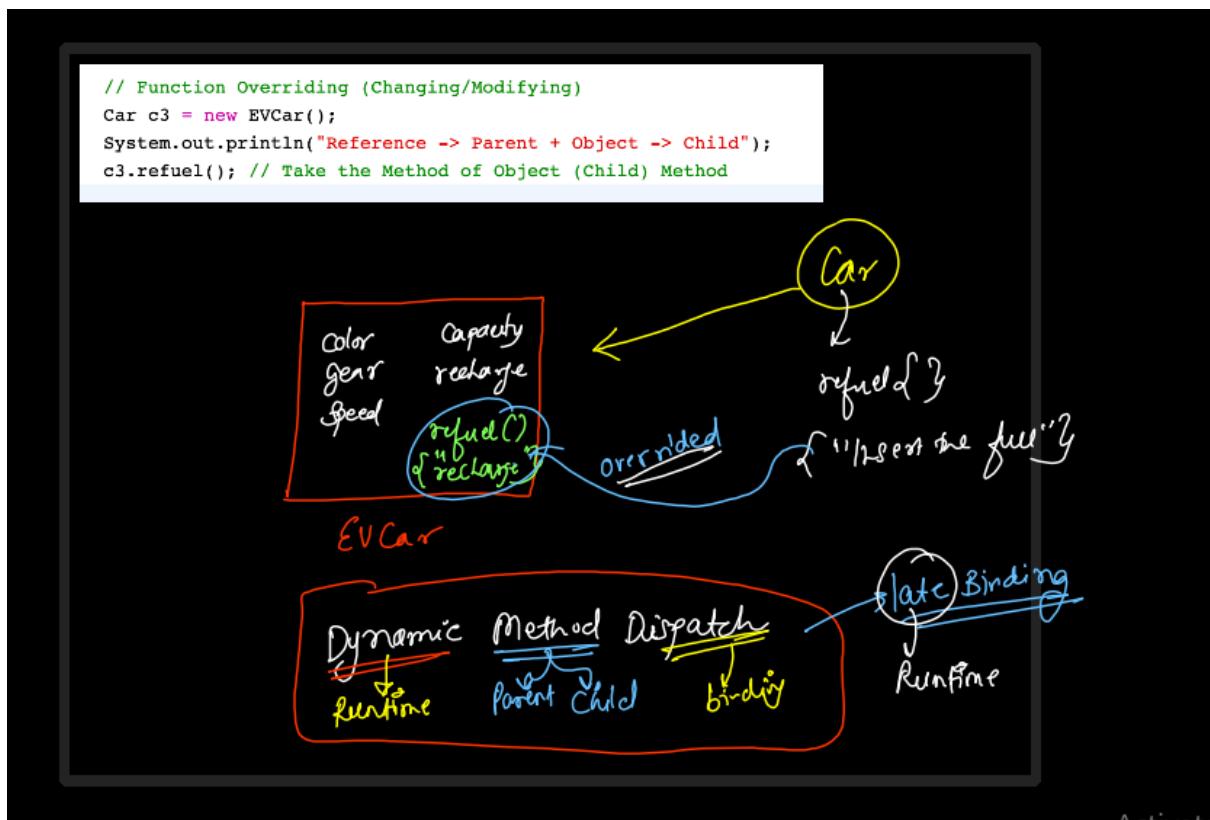
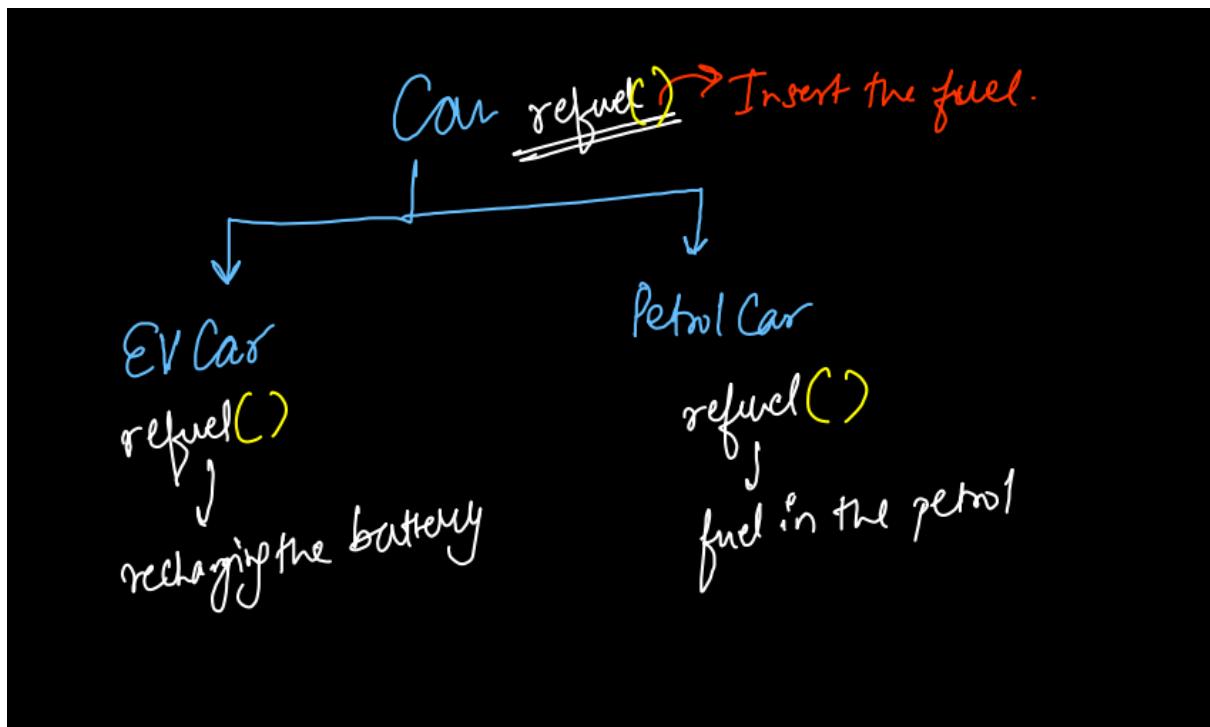


① Reference Variable  $\rightarrow$  Parent class  
Object  $\rightarrow$  Parent class  
 $\text{Car } c1 = \text{new Car();}$   
 $\downarrow \text{speed, gear, color}$

② Reference Variable  $\rightarrow$  Child class  
Object  $\rightarrow$  Child class

$\text{EVCar } c2 = \text{new EVCar();}$   
 $\downarrow \text{speed, gear, color, capacity, recharge time}$





## Function overriding

Relat<sup>n</sup>

①st criteria →

1 is in the parent, other is in child class  
(Inherit the func) (Recharge the latter)

②nd criteria

Function name  
Parameters  
Return type

Some

Car() {  
    → void drive();  
    → void drive();  
}  
Overriding (✗)  
(Same class)

Overloaded (✗)  
(Same parameters)

Error

Car() {  
    → void drive();  
    → int drive();  
}  
Overloading  
(Same class)

Overloading  
(Only the return  
type is diff)

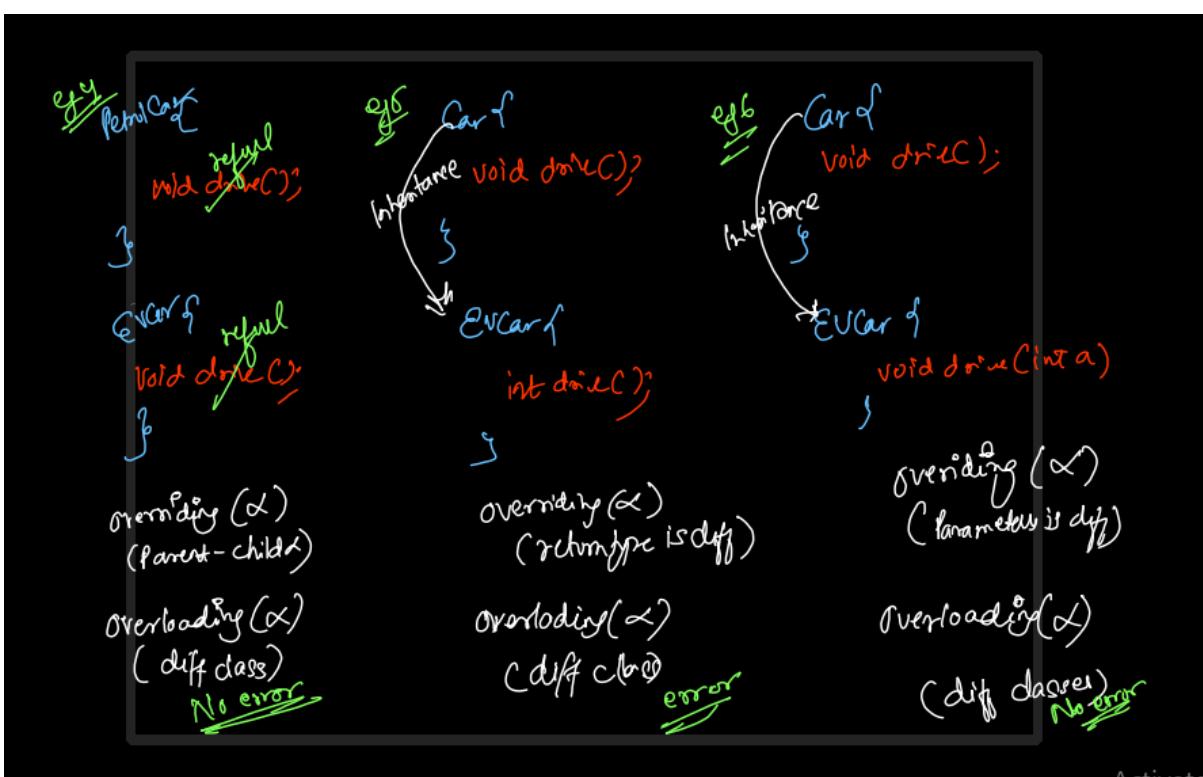
Error

Car() {  
    → void drive(int a);  
    → void drive(int a, int b);  
}  
Overriding (✗)  
same class

Overloading (✓)  
(parameters ✓)  
No error

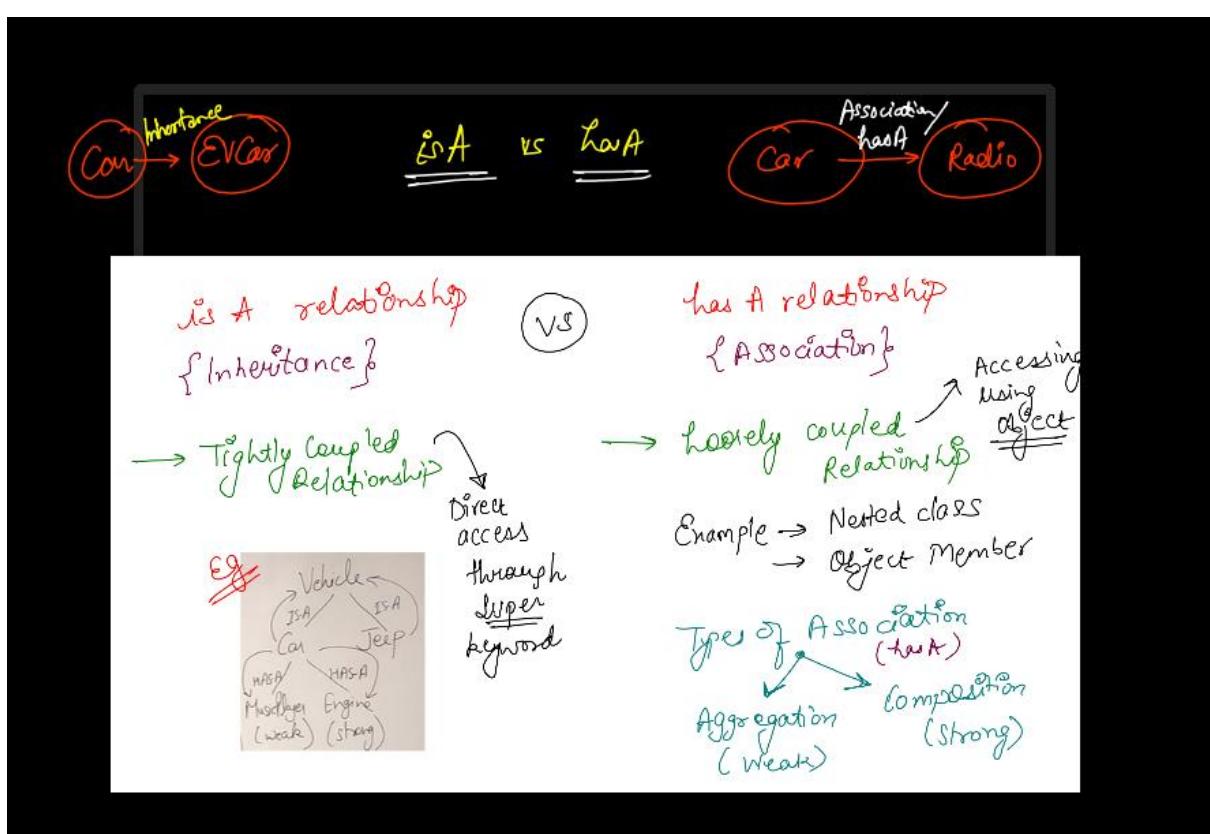
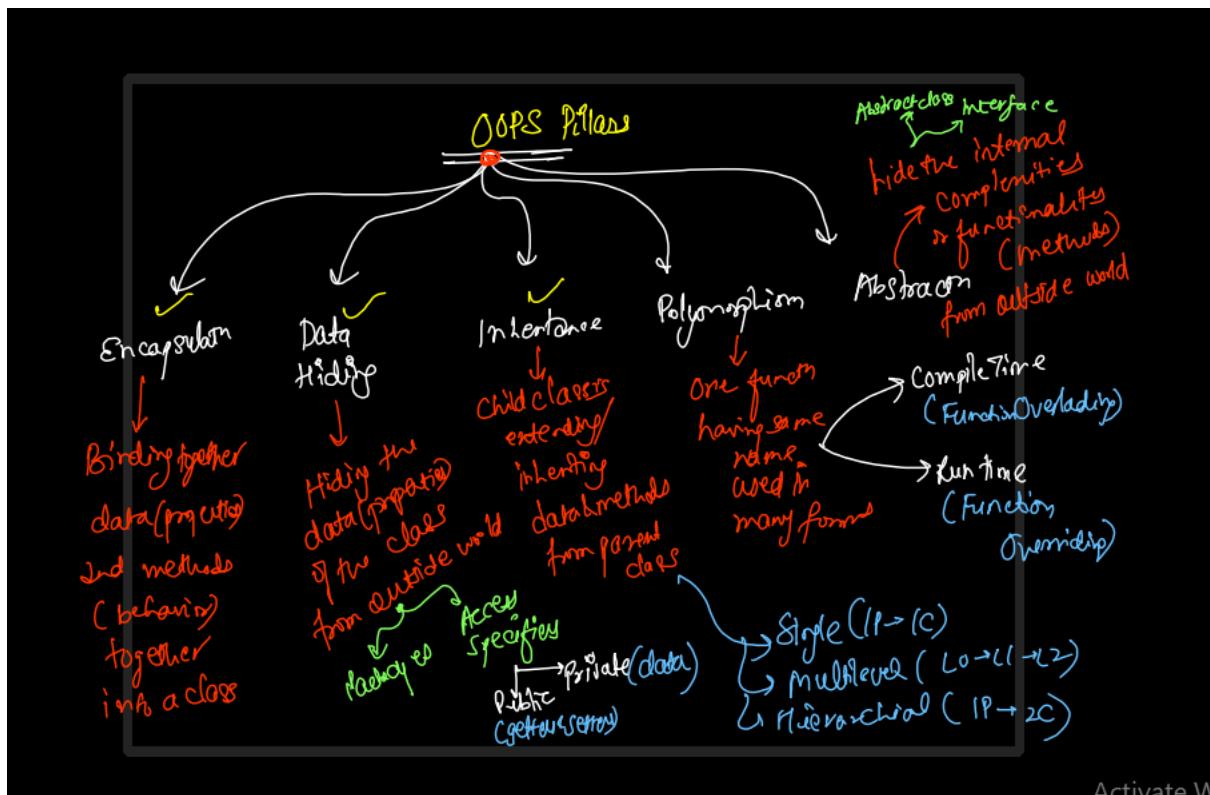
Active

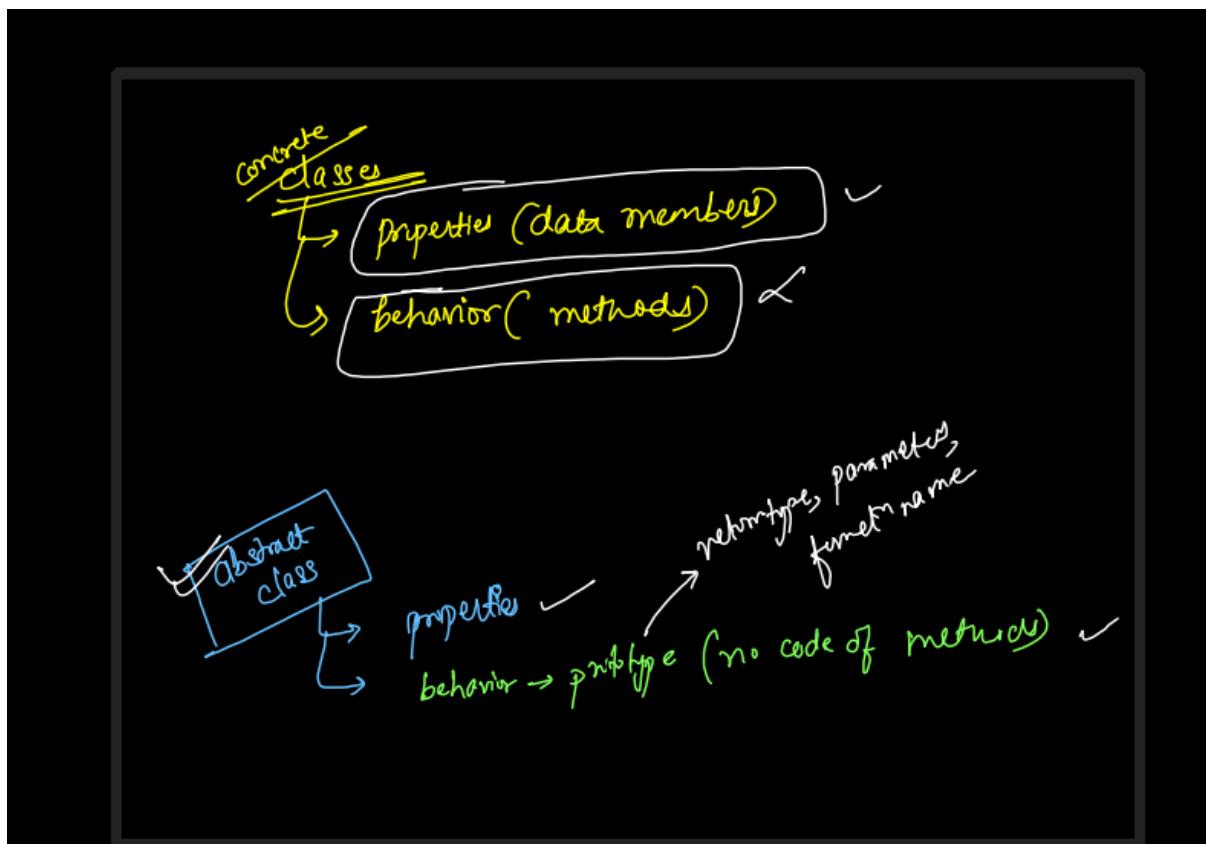
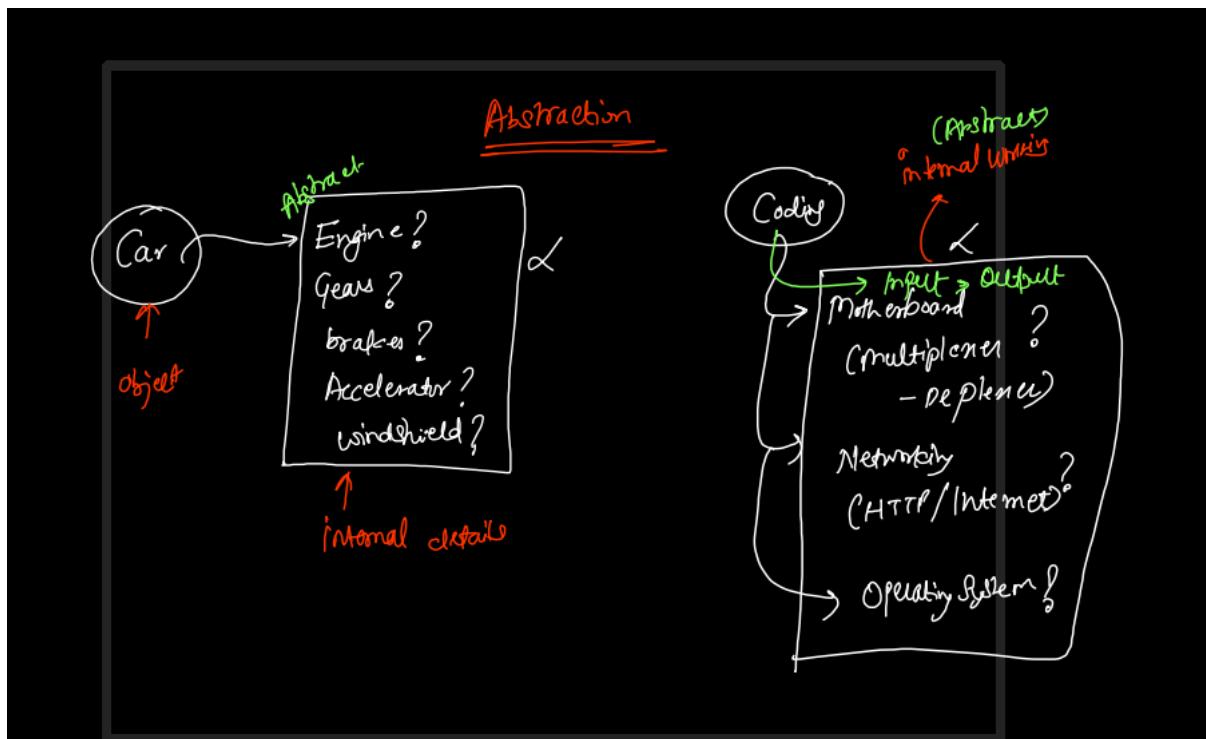
Function Overloading	Function overriding
→ Compiletime / static polymorphism	→ runtime / dynamic Polymorphism
→ same class (Inheritance is not required)	→ Different class → (Inheritance is required) ↳ Parent ← child reln
→ funtn name (same)	→ function-name (same)
→ Parameters (Diff) ↗ No Type Order	→ Parameters (same)
→ Return type does not matter	→ return type should be same as well

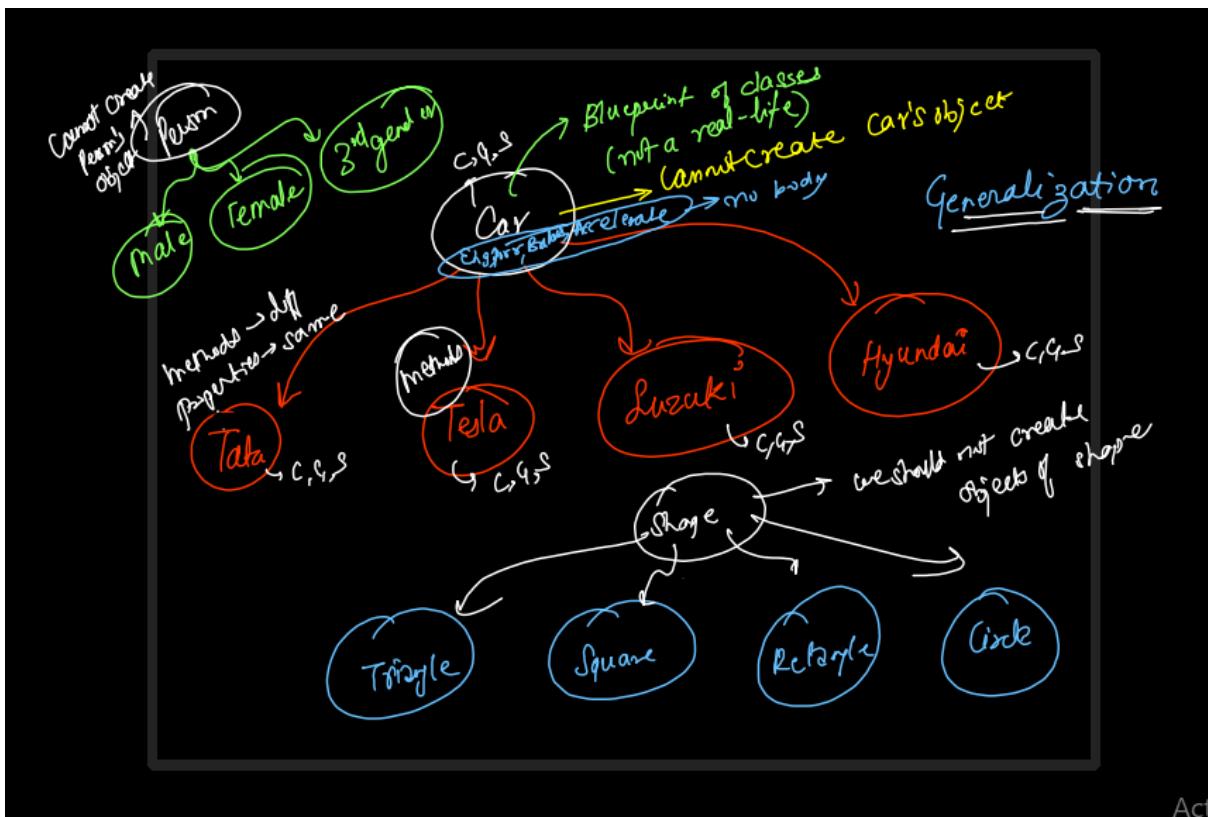


q7  
 Car() {  
 void drive();  
 }  
 EVCar {  
 void drive();  
 }  
 Overriding (✓)      ↗  
 ↗ Function name  
 ↗ Return type same  
 ↗ Parameters same  
 Overloading (✗) (diff class)

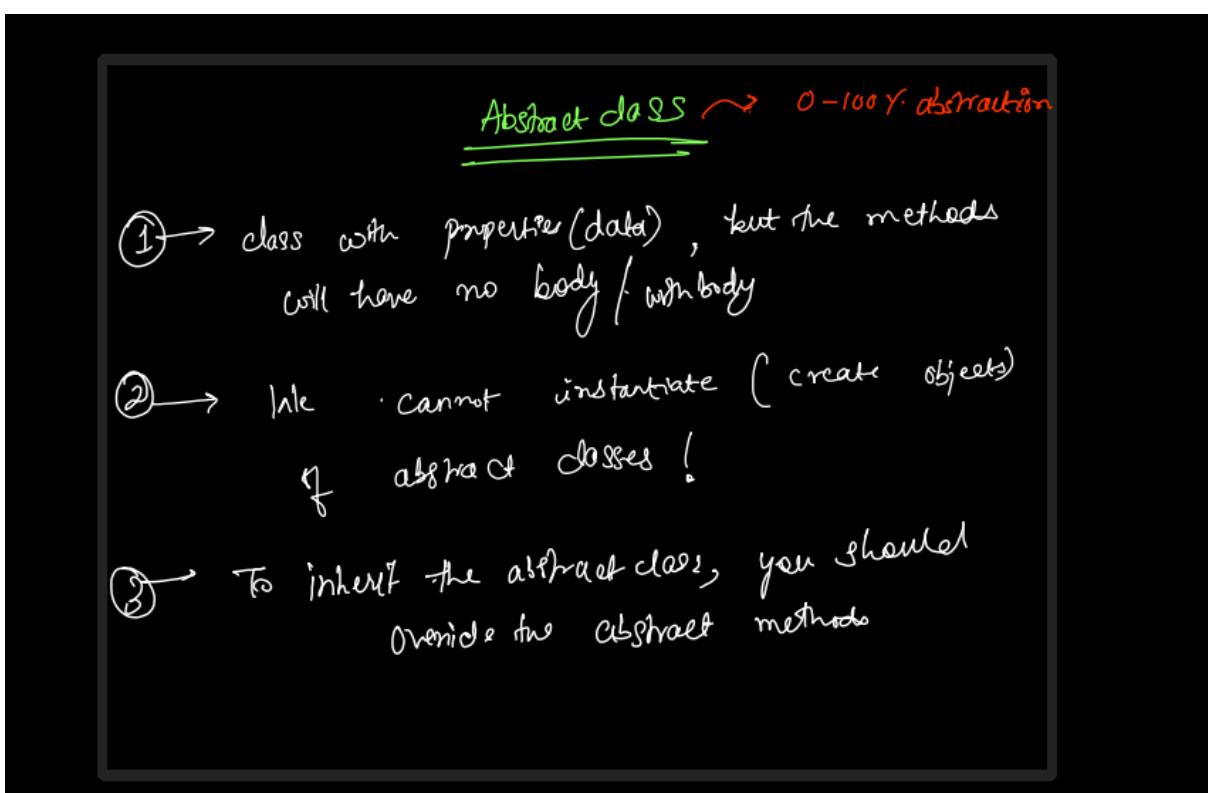
q8  
 Car() {  
 void drive();  
 }  
 EVCar {  
 void drive();  
 void drive(int a);  
 }  
 Overriding ✓  
 Overloading ✓

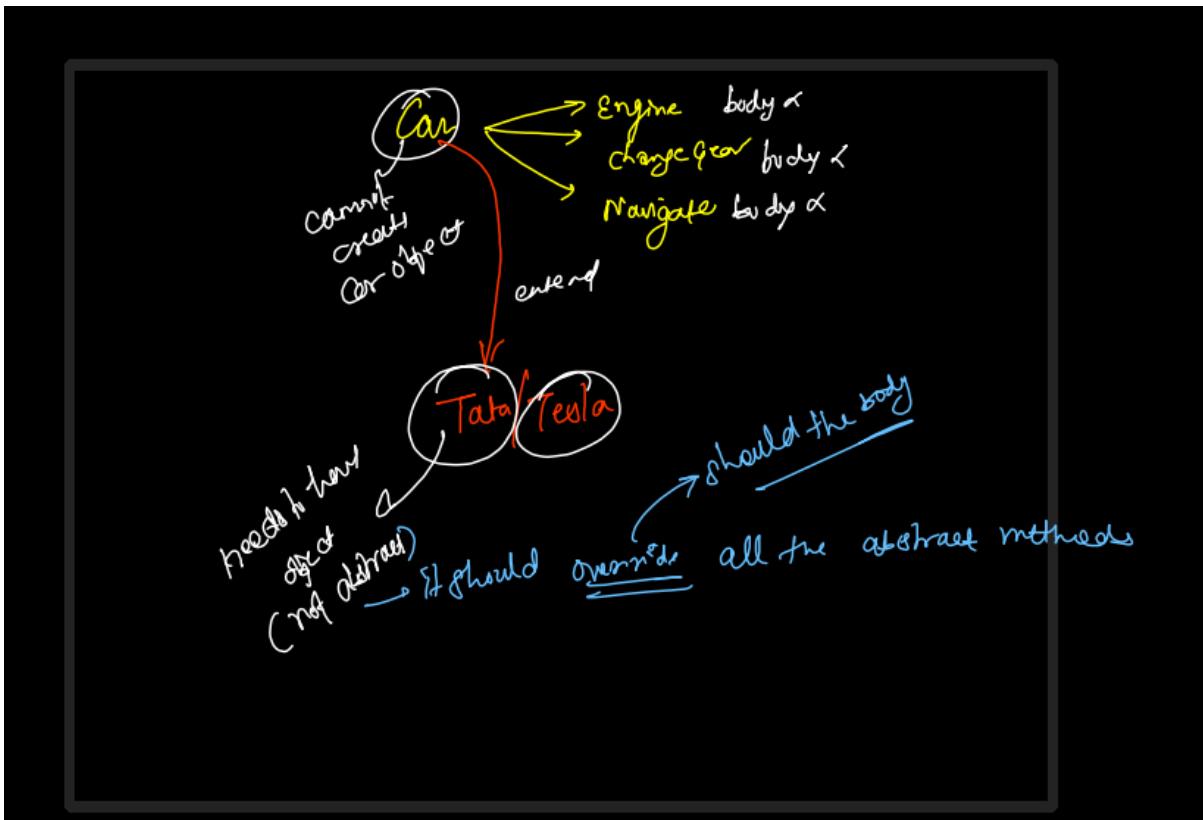






Act





- Interface → Pure form of abstraction
- ② → Data/Properties can be there (Static)
- ③ → All methods will be abstract (no body)
- ④ → Instantiation(object creation) of interfaces is not possible
- ⑤ → Instead of inheritance (extend), we will use  
(implement) keyword → class implementing  
interface will need  
to override all  
the functions.

*Car* → cannot have any function with body,  
⇒ it can become interface

by abstract

```
abstract class Car{
    int gears, speed;
    String color;

    public Car(){
        gears = 5;
        speed = 40;
        color = "White";
    }

    // Functions with No Body
    public abstract void engineStart();
    public abstract void changeGear();
    public abstract void navigate();

    // Functions with Body
    public void accelerate(){
        System.out.println("Please press accelerate pedal");
    }
    public void applyBrake(){
        System.out.println("Please press break pedal");
    }
}
```

by abstract

```
interface Car{
    static int gears = 5, speed = 40;
    static String color = "White";

    // Functions with No Body
    public abstract void engineStart();
    public abstract void changeGear();
    public abstract void navigate();
}
```