

Time complexity 2

$n=4$
 $\text{for (int } i=0; i \leq n; i++) \{$
 $\quad \text{syso}(i); \checkmark O(1)$
 $\}$

$\underbrace{0(n+1)}_{O(n)}$
 $O(1) + O(1) + O(1) + \dots + n \text{ times } O(1) = n \cdot O(1) = O(n)$

$n=5$
 $\underbrace{n \rightarrow 0}_{n \rightarrow 0} \quad \underbrace{(n+1)}_n$

$\text{int count} = 0;$
 $\text{for (int } i=n; i \geq 0; i--) \{$
 $\quad \text{count}++; \rightarrow O(1)$
 $\}$
 $\text{syso(count); } \rightarrow O(1)$
 $\rightarrow O(n)$

$n \rightarrow 1 \rightarrow n$
 $n \rightarrow 0 \rightarrow (n+1)$

$5 \rightarrow 1$
 $4 \rightarrow 2$
 $3 \rightarrow 3$
 $2 \rightarrow 4$
 $1 \rightarrow 5$
 $0 \rightarrow 6$

$n=5$
 $\text{for (int } i=n; i \leq 0; i--) \{$
 $\quad \text{syso}(i);$
 $\}$

$\underbrace{5 \leq 0}_{\text{false}}$
 $O(1)$

$n=8$
 $\text{for (int } i=0; i < n; i+=2) \{$
 $\quad \text{syso}(i); \rightarrow O(1)$
 $\}$

$O(\frac{n}{2})$
 $\frac{1}{2} \cdot O(n) = O(n)$

$0 \quad 0$
 $2 \quad 2$
 $4 \quad 4$
 $6 \quad 6$
 8

⑤ for (int i=0; i<n; i++) {
 syso(i);
 }
 $\rightarrow \frac{n}{3}$
 $= O(n)$

⑥ for (int i=0; i<=n; i++) {
 for (int j=0; j<=n; j++) {
 syso(j);
 }
 }
 $n=4$

i=0 {0,1,2,3,4}
 i=1 {0,1,2,3,4}
 i=2 {0,1,2,3,4}
 i=3 {0,1,2,3,4}
 i=4 {0,1,2,3,4}

$n+n+n+n \dots n$ times.

$n(1+1+1+1 \dots n \text{ times});$

$n(1 \times n) = n^2$

⑦ for (int i=0; i<=n; i++) {
 for (int j=i; j<=n; j++) {
 syso(j);
 }
 }
 $n=4$

i
 0 {0,1,2,3,4} n
 1 {1,2,3,4} n-1
 2 {2,3,4} n-2
 3 {3,4} n-3
 4 {4} n-4
 1

$(n + n-1 + n-2 + n-3 \dots 1)$

$$\frac{n+(n+1)}{2} = \frac{1}{2} (n^2 + n) = \frac{n^2 + n}{2} = O(n^2)$$

⑧ for (int i=0; i<n; i++)
 for (int j=0; j<=i; j++)
 sys(j);

$O(n^2)$

4

4

0 1
 1 0, 1 2
 2 0, 1, 2 3
 3 0, 1, 2, 3 4

$$1+2+3+4+\dots+n$$

$$= \frac{n(n+1)}{2}$$

$$= O(n^2) \checkmark$$

⑨ for (int i=1; i<=n; i++)
 sys(j);

$\sqrt{2}=1$

$O(\sqrt{n})$

4

$$\sqrt{16} \rightarrow 4$$

$$\sqrt{25} \rightarrow 5$$

$$\sqrt{36} \rightarrow 6$$

n 0 1 - - - n

100
 $n=16$

5

5

1	1
2	2
3	3
4	4
5	5

int q = (int) Math.sqrt(n);

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for (int i = 1; i <= q; i++) {

$n = \sqrt{16} = 4$ ✓

sys(i)

\sqrt{n}

i
1
2
3
4

1
2
3
4

$O(n)$
 $O(n^2)$
 $O(\sqrt{n})$

$O(\sqrt{n})$

(int)

for (int i = 1; i <= Math.sqrt(n); i++) {
sys(i);

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for (int i = 0; i <= n; i++) {
for (int j = 1; j <= \sqrt{n} ; j++) {
sys(i);
}

$O(n \times \sqrt{n})$

(12) $\text{for } i = 1; i \leq n$
 $\quad \text{syso}(i);$

$n = 32$

$i = 1$
 2
 4
 8
 16
 32

$\log_2 n = \log_2 32 = 5$
 $\log_2 2 = 1$
 $\log_2 4 = 2$
 $\log_2 8 = 3$
 $\log_2 16 = 4$
 $\log_2 32 = 5$

$T.C = O(\log^k n)$

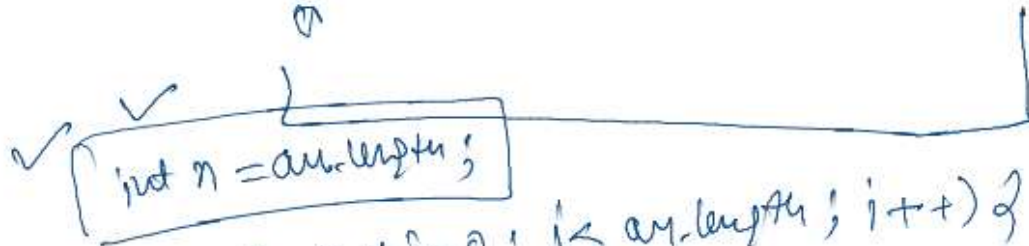
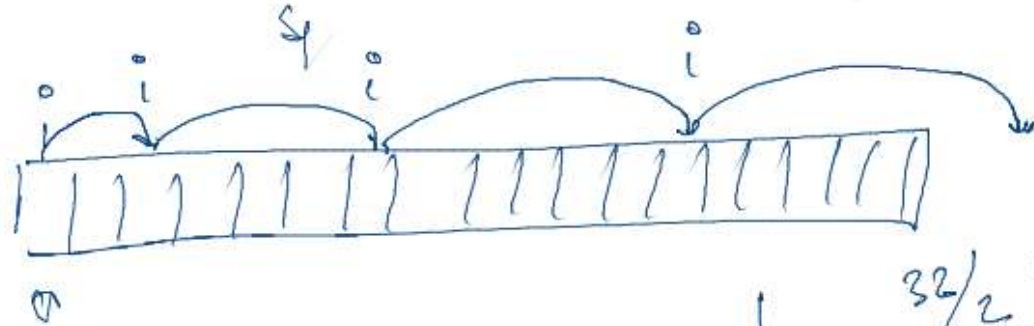
13) for (int i = n; i >= 1; i /= 2) {
 syso(i);
 }
 n = 2
 u = $O(\log n)$
 = $O(\log 2)$

n	u
32	5
16	4
8	3
4	2
2	1
1	0
0	0

14) for (int i=0; i<n; i++) { arr.length();
O(n) { for (int j=1; j<n; j*=2) { }
O(n log n)

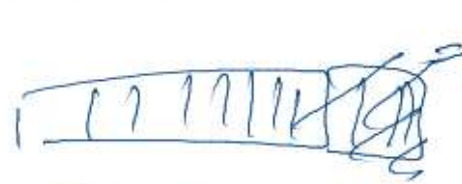
15

for (int i=0; i < arr.length; i+=2) {
 sys(arr[i]);
 }
 $\log(n)$



16

for (int i=0; i < arr.length; i++) {
 }
 $\log_2(n)$



$32/2 = \log_2$

$16/2$

$8/2$

$4/2$

$2/2$

1

n
 \downarrow
 $n/2$
 \downarrow
 $n/4$
 \downarrow
 $n/8$
 \downarrow
 $n/16 \dots$

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for (int i=0; i < str.length; i++) {
 sys(str.charAt(i));
 }
 $= O(n)$

$= O(n)$

$\log n$

education

0 1 2 3 4 5 6 7 8

0
2
4
6
8
10