

Minimum Cost of ropes 3

$$\text{arr} = \begin{matrix} & 0 & 1 & 2 & 3 & 4 \\ \left[\begin{array}{ccccc} 2 & 3 & 5 & 4 & 2 \end{array} \right] \end{matrix}$$

PO
minHeap

2	4
3	7
5	9
4	16 ←
2	

$$\text{Rope1} = \cancel{2} \cancel{3} \cancel{4} 7$$

$$\text{Rope2} = \cancel{2} \cancel{4} \cancel{5} 9$$

$$\begin{aligned} \text{cost} &= 4 + 7 + 9 + 16 \\ &= 36 \end{aligned}$$

gmp

pseudo
code

- 1) create min heap
- 2) add all elements of arr in pq
- 3) loop until only 1 element left in PQ

3.1) get 2 smallest ropes from PQ

3.2) $ans += (num1 + num2)$

Imp \longrightarrow 3.3) add $(num1 + num2)$ in P

code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for ( int i = 0; i < n; i++ ) {
        arr[i] = scn.nextInt();
    }
    int ans = minCost(arr, n);
    System.out.println(ans);
}

public static int minCost(int[] arr, int n) {
    PriorityQueue<Integer> pq = new PriorityQueue<>();
    for (int i = 0; i < n; i++) {
        pq.add( arr[i] );
    }

    int cost = 0;
    while ( pq.size() > 1 ) {
        int num1 = pq.poll();
        int num2 = pq.poll();
        int rope = num1 + num2;

        cost = cost + rope;

        pq.add( rope );
    }
    return cost;
}
```

$T.C = O(n \log n)$

$S.C = O(n)$

subtract numbers 1

$$\text{arr} = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ [1, & 5, & 0, & 3, & 5, & 5, & 1, & 3, & 5] \end{matrix}$$

step 1:- choose a minimum no, which is non-zero (x)

step 2:- subtract x from every no. except zero

$$\boxed{\text{Ans} = 3}$$

process

$$x = 1, \text{ arr} = [0, 4, 0, 2, 4, 4, 0, 2, 4]$$

$$x = 2, \text{ arr} = [0, 2, 0, 0, 2, 2, 0, 0, 2]$$

$$x = 2, \text{ arr} = [0, 0, 0, 0, 0, 0, 0, 0, 0]$$

approach

arr = ^{0 1 2 3 4 5 6 7 8}
[1, 5, 0, 3, 5, 5, 1, 3, 5]

x, y, z ^{non-zero}
[x, z, 0, ~~y~~, z, z, x, ~~y~~, z]

~~a~~ ^{a, b}
[~~a~~, b, 0, 0, b, b, ~~a~~, 0, b]

0 [0, ~~a~~, 0, 0, ~~a~~, ~~a~~, 0, 0, ~~a~~]

set

1
5
3

Key observation :-

In 1 step, we are removing all
1 type of elements (non-zero)

Note:- our ans is no. of non-zero elements
(without duplicacy)

code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for (int i = 0; i < n; i++) {
        arr[i] = scn.nextInt();
    }
    int ans = subtractOne(arr, n);
    System.out.println(ans);
}

public static int subtractOne(int[] arr, int n) {
    HashSet<Integer> set = new HashSet<>();
    for (int i : arr) {
        if (i > 0) {
            set.add(i);
        }
    }
    return set.size();
}
```

$T.C = O(n)$

$S.C = O(n)$

→ duplication is removed

Reduce Array Size to the half

arr = [~~3~~, 2, ~~3~~, ~~3~~, 2, 1, 2, 1, 2, ~~3~~, ~~3~~]

task :- perform mini. steps

↳ in 1 step :- pick any no. and remove all the occ. of that no.

hash map

freq	
1	→ 2
2	→ 4
3	→ 5

PO (max heap)

4	2	5
freq		

pseudo
code

- 1) create hashmap
- 2) calculate freq
- 3) create max heap
- 4) store all the freq of map
- 5) loop until array size become half or less
 - 5.1) $size = size - pq.poll()$
count++
- 6) return count.

Code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for (int i = 0; i < n; i++) {
        arr[i] = scn.nextInt();
    }
    int ans = reduceSize(arr, n);
    System.out.println(ans);
}

public static int reduceSize(int[] arr, int n) {

    [ HashMap<Integer, Integer> map = new HashMap<>();
      for (int i = 0; i < n; i++)
        map.put( arr[i], map.getDefault( arr[i], 0 ) + 1 );

    [ PriorityQueue<Integer> pq = new PriorityQueue<>(Collections.reverseOrder());
      for (int val : map.values()) {
        pq.add( val );
      }

    int size = n;
    int count = 0;
    [ while ( size > n / 2 ) {
      size = size - pq.poll();
      count++;
    }
    return count;
}
```

$$\begin{aligned} T.C &= O(n + n \log(n) + n \log n) \\ &\approx O(n \log n) \\ S.C &= O(n + n) \\ &\approx O(n) \end{aligned}$$