

3 Sum

$$\text{arr}[i] + \text{arr}[j] + \text{arr}[k] == 0$$

Gdea

$$\text{arr}[i] + \text{arr}[j] == -1 * \text{arr}[k]$$

↓
element1

↓
element2

↓
target

Note :- we are going to run the previous template of code, K no. of times

dry run

$n = 6$
 $arr = [-2, 0, 2, 4, -2, -8]$

sort the array

$arr = [-8, -2, -2, 0, 2, 4]$

Indices: 0 1 2 3 4 5
 ↑ ↑ ↑
 K i j

(duplication)

O/P

-2	4	-2
0	2	-2
0	2	-2

$i = k+1$
 $j = n-1$

$k=0$, target = 8, sum = ~~2~~ ~~2~~ ~~4~~ 6

$k=1$, target = 2, sum = ~~2~~

$k=2$, target = 2, sum = ~~2~~

$k=3$, target = 0, sum = 6

$k=4$, target = -2, sum =

$k=5$, target = -4, sum =

```
int i = 0;
int j = n - 1;
while ( i < j ) {
    int sum = arr[i] + arr[j];
    if ( sum == target ) {
        System.out.println(i + " " + j);
        i++;
        j--;
    } else if ( sum < target ) {
        i++;
    } else {
        j--;
    }
}
```

pseudo
code

1) Sort the array

2) traverse k pointer from 0 to n

2.1) declare $target = -1 * arr[k]$

2.2) declare $i = k+1, j = n-1;$

2.3) loop until $i < j$

2.3.1) find $sum = arr[i] + arr[j]$

2.3.2) check if $sum == target$
print triplet

$i++, j--;$

handle duplicacy for i & j

2.3.3) check if $sum < target$

$i++;$

2.3.4) check if $sum > target$

$j--;$

2.4) handle duplicacy for k pointer

Code

```
- public static void findTriplet(int[] arr, int n) {  
    → Arrays.sort(arr);  
    for (int k = 0; k < n; k++) {  
        int target = -1 * arr[k];  
        int i = k + 1;  
        int j = n - 1;  
        while ( i < j ) {  
            int sum = arr[i] + arr[j];  
            if ( sum == target ) {  
                System.out.println( arr[k] + " " + arr[i] + " " + arr[j]);  
                i++;  
                j--;  
                while ( i < j && arr[i] == arr[i - 1] ) {  
                    i++;  
                }  
                while ( i < j && arr[j] == arr[j + 1] ) {  
                    j--;  
                }  
            } else if ( sum < target ) {  
                i++;  
            } else {  
                j--;  
            }  
        }  
        while ( k + 1 < n && arr[k] == arr[k + 1] ) {  
            k++;  
        }  
    }  
}
```

T.C = $O(n^2 + n \log n)$

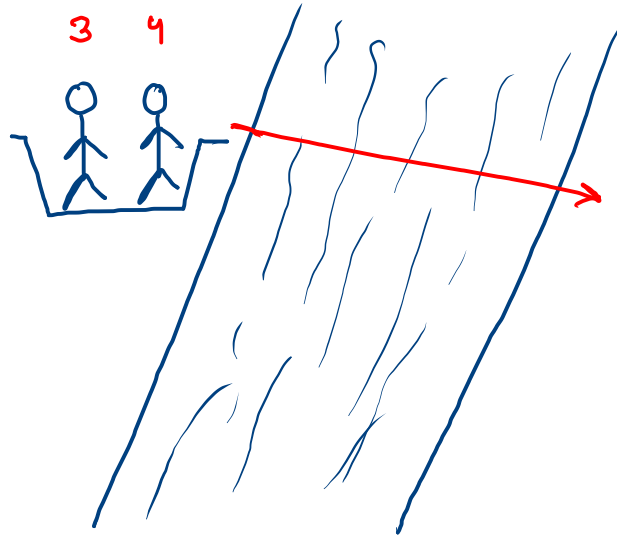
Count boat

- weight of people avail
- each boat can carry 'limit' weight
- each boat can carry atmost 2 people

t

∞ boats

limit = 6



ans = no. of boats

$$\text{arr}[i] + \text{arr}[j] \leq \text{limit}$$

target

$$\left. \begin{array}{l} \text{arr}[i] \leq \text{limit} \\ \text{arr}[j] \leq \text{limit} \end{array} \right\} \begin{array}{l} \text{always} \\ \text{true} \end{array}$$

Ex:- arr = [3 , 2 , 1 , 2]

Sorting arr = [1 , 2 , 2 , 3] , limit = 3

↑ ↑
j i

$$\underline{\underline{arr[i] + arr[j] \leq limit}}$$

sum = ~~4~~ ~~3~~ 4

boats = ~~0~~ ~~1~~ ~~2~~ 3

pseudo code

- 1) sort
- 2) $i = 0, j = n-1, boats = 0$
- 3) loop until $i \leq j$
 - 3.1) $sum = arr[i] + arr[j]$
 - 3.2) if $sum == target$
 $i++, j--, boats++;$
 - 3.3) if $sum > target$
 $j--, boats++;$
 - 3.4) if $sum < target$
 $i++, j--, boats++;$
- 4) return boats.

code

```
public static int countBoats(int[] arr, int n, int limit) {
```

```
    → Arrays.sort(arr);
```

```
    int i = 0;
```

```
    int j = n - 1;
```

```
    int boats = 0;
```

```
    while ( i <= j ) {
```

```
        int sum = arr[i] + arr[j];
```

```
        if ( sum <= limit ) {
```

```
            i++;
```

```
            j--;
```

```
        } else {
```

```
            j--;
```

```
        }
```

```
        boats++;
```

```
    }
```

```
    return boats;
```

```
}
```

$T.C = O(n + n \log n)$

arr = [1, 1, 3, 4, 4, 5, 6] limit = 6

\uparrow \uparrow
 j i

sum = ~~7~~ ~~6~~ ~~5~~ ~~7~~ 6

count = 5

✓ [6]

✓ [1 5]

✓ [1 4]

✓ [3 3]

✓ [4]