

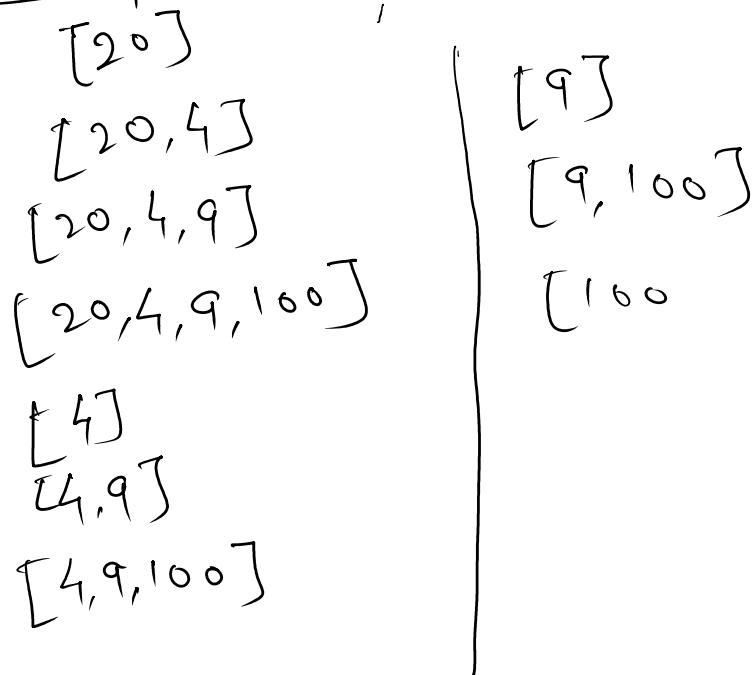
## Subarrays

- ↳ It is continuous part of an array
- ↳ It should be in forward direction

### Example

arr = [20, 4, 9, 100]

## Subarrays



Is it a subarray?

- (i.) [4, 100] → No
- (ii.) [20, 9, 100] → No
- (iii.) [20, 4, 9] → Yes

Q. Find all the possible subarrays in

.. .. .. .

V: Find all the possible subarrays in given array

↳ [40, 9, 6, 1, 0]

Algorithm :-

$\begin{array}{cccc} 0 & 1 & 2 & 3 \\ [2^0, 4, 9, 100] \end{array}$

20 (start=0, end=0)

20 4 (start=0, end=1)

20 4 9 (start=0, end=2)

20 4 9 100 (start=0, end=3)

4 (start=1, end=1)

4 9 (start=1, end=2)

4 9 100 (start=1, end=3)

9 100 (start=2, end=2)

9 100 (start=2, end=3)

100 (start=3, end=3)

start=0, end=0 to 3

start=1, end = 1 to 3

start=2, end = 2 to 3

start=3, end = 3 to 3.

```
for(int start=0; start<n; start++) {  
    for(int end=start; end<n; end++) {  
        /* start=0 | start=0 | start=0 | start=0 |  
         *          | start=1 |          | start=2 |          | start=3 |  
         *          |          | end=1 |          |          | end=3 |  
         *          |          | arr[0] arr[1] arr[2] arr[3] arr[4] */  
    }  
}
```

```

/*
    Start = 0 | >---->
    end = 0 | end = 1 . . .
    arr[0] . | arr[0] arr[1]
              | arr[1]
              | arr[2]
              | arr[2]
    printSubarray(start, end);
}

```

```

void printSubarray(int start, int end) {
    for (int i = start; i <= end; i++) {
        System.out.print(arr[i] + " ");
    }
    System.out.println();
}

```

---

```

1 import java.io.*;
2 import java.util.*;
3
4 public class Solution {
5
6     public static void main(String[] args) {
7         /* Enter your code here. Read input from STDIN. Print output to STDOUT. Your class sh
8         Scanner sc = new Scanner(System.in);
9         int n = sc.nextInt();
10        int arr[] = new int[n];
11        for (int i = 0; i < n; i++) {
12            arr[i] = sc.nextInt();
13        }
14
15        for (int start = 0; start < n; start++) {
16            for (int end = start; end < n; end++) {
17                printSubarray(arr, start, end);
18            }
19        }
20    }
21    static void printSubarray(int arr[], int start, int end) {
22        for (int i = start; i <= end; i++) {
23            System.out.print(arr[i] + " ");
24        }
25        System.out.println();
26    }
27 }

```

# Sum Equals zero

$4 \rightarrow n$

arr = [-1, 1, 2, 3]

Subarrays of given array

Sum

-1 ← -1

0 ← -1 1

2 ← -1 1 2

5 ← -1 1 2 3

1 ← 1

3 ← 1 2

6 ← 1 2 3

Sum

2 → 2

2 3 → 5

3 → 3

p.s.v.m (String[] args) {

for (int start=0; start < n; start++) {

    for (int end=start; end < n; end++) {

        sum = 0;

        0

```
function int sum=0;
for [int i:= start; i<=end; i++) {
    sum+=arr[i];
}
if (sum == 0) {
    s.o.println("true");
    return;
}
}
}
}
s.o.println("false");
}
}
```

## Max Subarray 2

$n \rightarrow 5$

$$\text{Q8x} = [-1, 2, 3, -2, 1]$$

### Subarrays

-1	2	3 -2
-1 2	2 3	3 -2 1
-1 2 3	2 3 -2	-2
-1 2 3 -2	2 3 -2 1	-2 1
-1 2 3 -2 1	3	1

Time Complexity by finding all subarrays  
then find maxsum

↳  $O(n^3)$  (Brute Force Approach)

## Kadane's Algorithm

↳  $O(n)$

It is used where we need to find maximum sum subarrays or maximum product subarrays

Example 1.

$$arr = [2, 4, 6, 1]$$

$$2, 4, 6 \rightarrow 12$$

$$[2, 4, 6, 1] \rightarrow 13$$

2

2 4

2 4 6

$$\checkmark 2 4 6 1$$

Example 2

$$arr = [10, 50, 2, 1]$$

$$[10, 50, 2, 1] \rightarrow 63$$

Example 3.

$$arr = [10, 50,$$

$$-2, 1]$$

max  $\rightarrow$  min. value

$$[10, 50] = 60 \checkmark$$

$$\text{sum} = 0$$

$$\text{sum} = 10 < \text{max} = 10$$

$$\text{sum} = 60 < \text{max} = 60$$

$$\text{sum} = 58 < \text{max} = 60$$

$$\text{sum} = 59 < \text{max} = 60$$

$$[10, 50, -2, 1] = 59$$

Example 4.

$$arr = [90, -20, 30, 80, 7]$$

$$[30, 80, 7] = 117$$

$$[90, -20, 30, 80, 7] = 187$$

$$\text{sum} = 0$$

$$\text{sum} = 90 + (-20)$$

$$= 70 + 30$$

$$= 100 + 80$$

$$= 180 + 7 = 187$$

Example 5

$$arr = [40, -60, 15, 10, 25]$$

$$[15, 10, 25] \rightarrow 50.$$

$$\text{sum} = 0$$

$$\text{sum} = 0 + 40 = 40 \leftarrow \text{max}$$

$$\text{sum} = 40 + (-60) = -20 . \text{max} = 40$$

$\left. \begin{array}{l} \text{Sum} = -20 + 15 = -5, \max = 40 \\ \text{Sum} = -5 + 10 = 5, \max = 40 \\ \text{Sum} = 5 + 25 = 30, \max = 40 \end{array} \right\}$   
 ↓  
 $\begin{array}{l} \text{sum} < 0 \\ \text{sum} = 0 \\ \text{Sum} = 0 + 15 = 15, \max = 40 \\ \text{Sum} = 15 + 10 = 25, \max = 40 \\ \text{Sum} = 25 + 25 = 50, \max = 50 \end{array} \checkmark$

Code:-

```

int sum=0; int maxSum=Integer.MIN_VALUE;
for(int i=0; i<n; i++) {
    sum+=arr[i];
    if(sum>maxSum) {
        maxSum=sum;
    }
    if(sum<0) {
        sum=0;
    }
}
    
```

Example:-    sum= 0  
 $\text{arr} = [10, -5, -15, 20, 30]$

$$\text{arr} = [10, -5, -15, 20, 50]$$

$$\text{sum} = 10, \text{max} = 10$$

$$\text{sum} = 10 + (-5) = 5, \text{max} = 10$$

$$\text{sum} = 5 - 15 = -10, \text{max} = 10$$

$$\text{sum} < 0, \text{sum} = 0$$

$$\text{sum} = 0 + 20 = 20, \text{max} = 20$$

$$\text{sum} = 20 + 30 = 50, \text{max} = 50$$