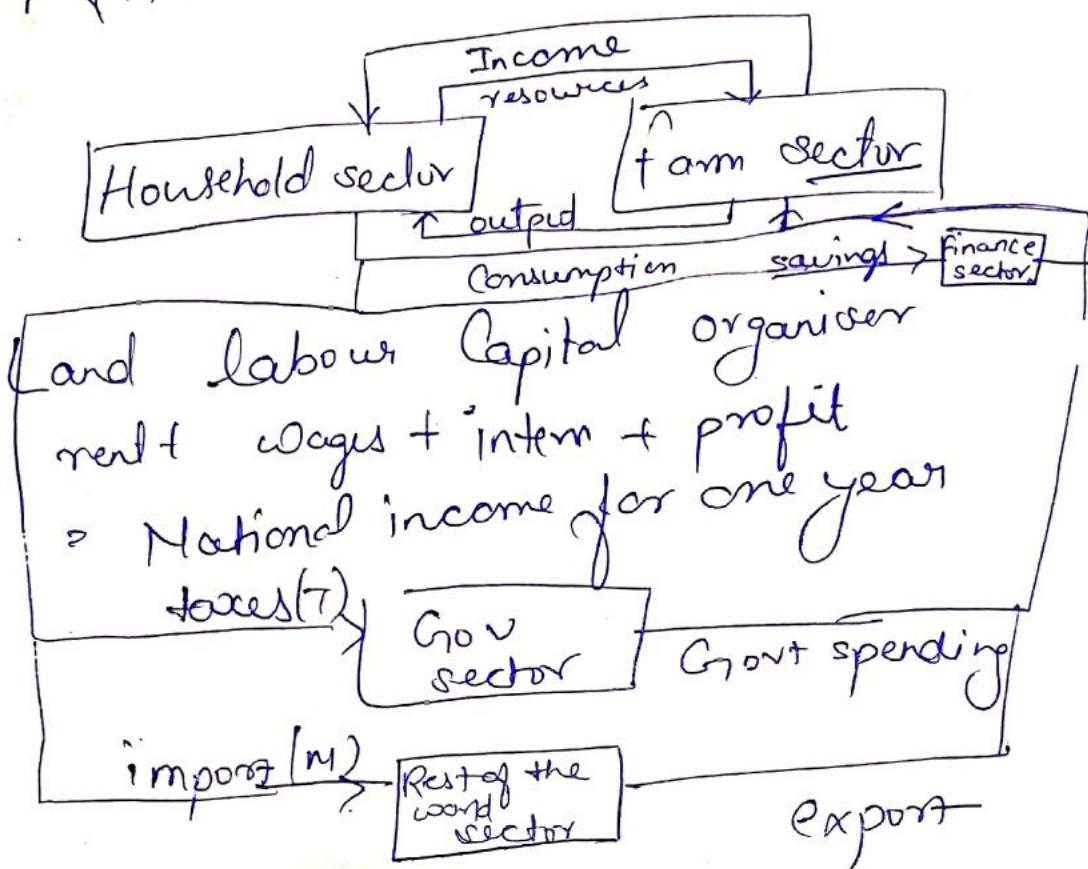


NATIONAL INCOME CONCEPTS :-



Gross Domestic Product

GDP at market price = Nominal GDP

If refers to the total market value of the final goods and services produced

in the country in one year calculated at market price.

$$GDP_{mp} = C + I + G + (X - M)$$

Gross National Product at market price

$$GNP = C + I + G + (X - M) + NFA$$

$$GNP = GDP + NFA \quad (\text{Net factor income from abroad})$$

It refers to the total market value of the final goods and services produced in the country in one year including the net factor income from abroad which refers to the net foreign income after deducting the foreign remittances living the country.

Net national product at market price

$$NNP = Depreciation$$

It refers to the total market value of the final goods & services produced in the country in one year including the net factor income from abroad after deducting the depreciation charges which the economy

has to spend on the maintenance of the produced
invested capitals asset.

NNP = Undiscounted + subsidies + taxes.

It refers to the final volume of the goods and services produced in a country in one year after including NNP and subsidies and discounts at

Demand Analysis

Demand in an economic sense refers to

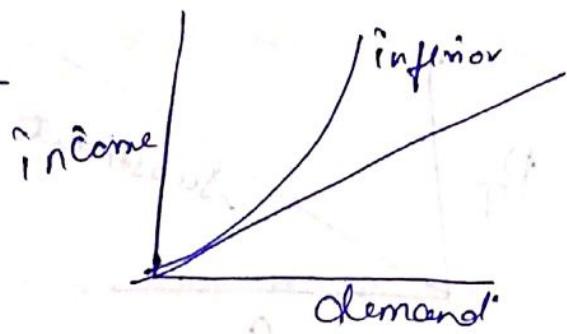
- i Desire for the commodity.
- ii Willingness to pay for the commodity.
- iii The ability to pay for the commodity.

Factors affecting demand

- i Price : Q_d = Quantity demanded varies inversely with the price; other factors remaining constant.

$$\frac{dQ_d}{dP_x} - \text{negative slope.}$$

② Income :-



If the quantity demanded of one commodity varies directly with the income of the consumer it is said to be a normal good while an negative relation with income shows that the product is inferior for the consumer.

③ Price of related commodities :-

Commodity : ~~both X & Y are~~

Price ratio : $P_x : P_y$ per unit

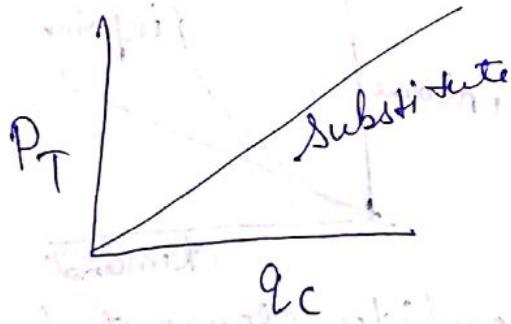
quantity consumed : Q_x, Q_y

Joint products/ Complementary goods.

Two commodity are said to be related if the quantity demanded of one product varies with the change in price of the other commodities.

$$\frac{\partial Q_x}{\partial P_y} > 0 \Rightarrow \text{Substitute}$$

$< 0 \Rightarrow \text{Joint}$



4. Taste and Preferences (Increase)

5. Advertisements (Ad) Increase

6. Future expectations of price and income (gold) (Bull & Bear)

Demand $f(P_x, P_y, Y, E_p, \dots)$

Law of Demand

It states that all other factors assumed constant, there will exist an inverse relationship between quantity and price.

Assumptions:-

- ① The consumer is assumed to be rational.
- ② There is no advertisement
- ③ There is no change in income and price of related commodities.

The commodity \times demand $\Rightarrow Q_m$

$\hat{e}^n D_{ij}(P_X)$

D_i = Demand of the i^{th} consumer ($i=1..n$)

Quantity demanded by consumer

Price	A	B	C	D	$\text{Cl} \times 0 \in B_i(P)$
10	1	0	3	0	4
9	3	1	6	4	14
8	7	9	9	7	95
7	11	4	12	10	37
6	13	6	14	12	45

Classification of goods

Nominal, inferior, Giffen

Price effect is + corr.

~~Income effect (SE)~~ Substitution effect (SE)

$$\frac{d\theta_\alpha}{dR_I} + \frac{d\theta_\alpha}{dP_\alpha} = PE$$

Price-effect: It refers to the overall change in quantity demanded of a product due to a change in price.

* The income effect refers to that part of the price effect which will measure the quantity variation in the product following the change in the real income or purchasing power of the consumer due to the change in price - $\frac{\partial Q_x}{\partial R_x}$

* Substitution effect : It measure that part of price effect which shows the quantity variation due to a change in the position of the commodity relative to other similar commodities following the price level.

Fall of price of commodity effect:

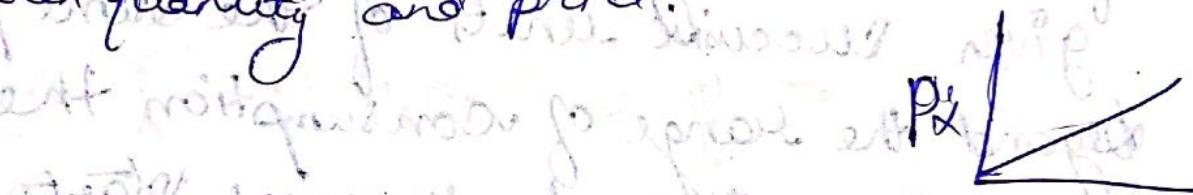
Normal : SE (negative) \uparrow = PET
 ——————
 IE (+ve) \uparrow

Inferior : SE ($-ve$) \uparrow \leftarrow = PET ($-SE > -IE$)
 cheap pos.
 IE ($-ve$) \downarrow

Giffen : SE ($-ve$) \uparrow + IE ($-ve$) \uparrow = PET
 ($-IE > -SE$)

Inferior: In this case the law of demand still operates because the negative substitution effect is stronger than the negative income effect.

Giffen: goods are those category of inferior group with the very strong (-ve) income effect which outways the negative substitution effect breaking down the inverse relationship between quantity and price.



Rise in price of comm X

Normal: SE (-ve) ↓ → PET
IE (+ve) ↓

Inferior: SE (-ve) ↓ → PET
IE (-ve) ↓ (-SE > -IE)

Giffen: SE (-ve) ↓ → PET
IE (+ve) ↑ (-IE > -SE)

Reasons for downward slope of demand curve:

1. Diminishing Marginal Utility

Change in utility (satisfaction how much)

$$MU = \underline{TU_n - TU_{n-1}}$$

Utility refers to the ~~want~~ satisfying power of a commodity. As a consumer is given successive units of the same product beyond the range of consumption the marginal utility he receives starts decreasing. At a higher level of consumption where the utility is low, only a lower price can induce the consumer to purchase more of the product and vice-versa.

Substitution effect : When the price of a commodity falls it becomes cheaper relative to other similar commodities and so more of it will be purchased and vice-versa.

Income effect : When the price of a commodity falls the real income of the consumer increases and so more of the normal commodities will be purchased and vice-versa.

New consumers:

Due to fall in price, others also get attracted.

Exceptions to the law of demand.

Giffen goods - they represent extremely inferior good with a very strong +ve income effect which outweighs the negative substitution effect breaking down the inverse relationship between quantity and price.

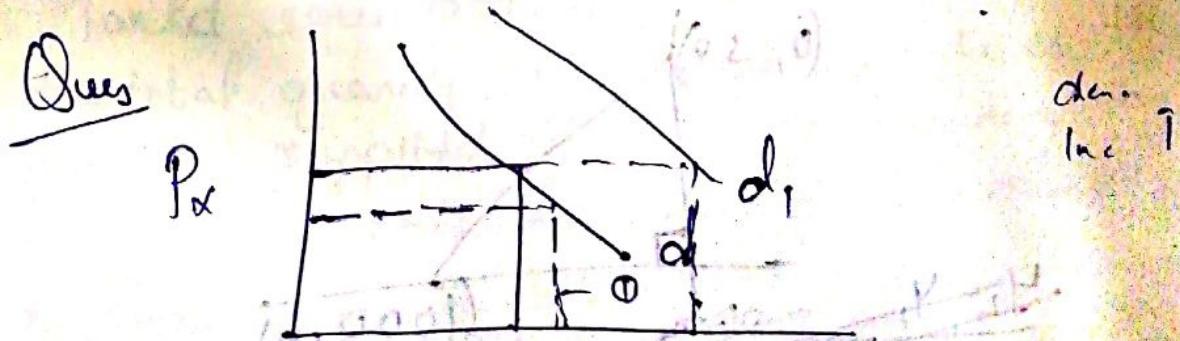
Cases of independence of demand:

- 1 Bandwagon effect
- 2 Snob effect (exclusive)
- 3 Veblen effect (status effect)

Future Expectations

Change in fashion

Ignorance



D-1

~~$X = gP_x - 0.2P_y$~~

Substi $\frac{\partial Q_x}{\partial P_y} > 0 \Rightarrow$ Sinks
 $\angle O \rightarrow$ Joint

$$X = 9P_x - 0.2P_y$$

$$\frac{\partial X}{\partial P_y} = g \frac{\partial R_x}{\partial P_y} - 0.2$$

$$\frac{\partial X}{\partial P_y} = 0.7 P_y^{-0.7} P_x^{-0.2} P_2^{-0.1} > 0$$

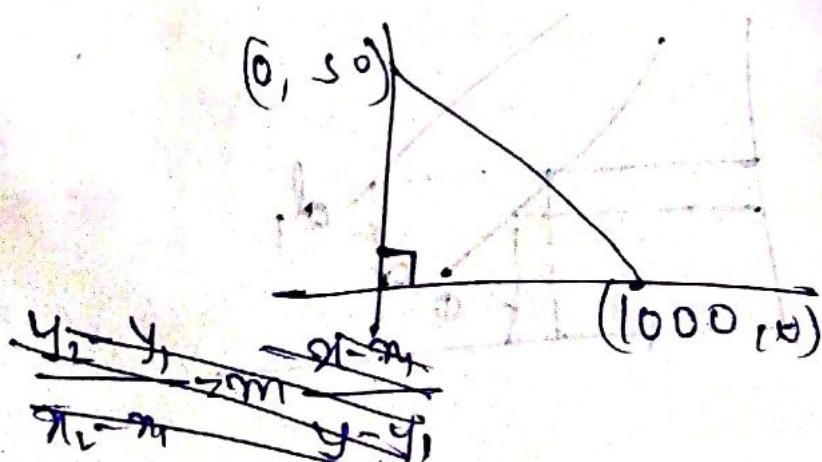
Compliment

$$X = 9P_x - 0.2P_y \cdot 0.3P_2^{-0.1}$$

$$\frac{\partial X}{\partial P_x} = -0.18 P_x^{-0.3} P_y^{-0.3} P_2^{-0.1} < 0$$

law of demand
 is satisfied

$\frac{\partial X}{\partial P_2} < 0$, compliment.

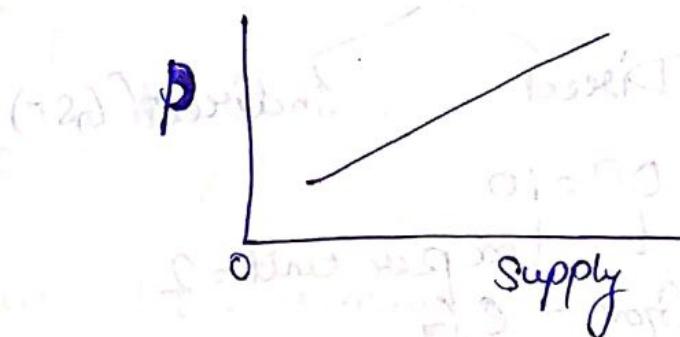


~~$y - y_1 = x(21 - 20)$~~

$$y - y_1 = x(21 - 20) \quad y = 50 - \frac{x}{20}$$

Supply analysis

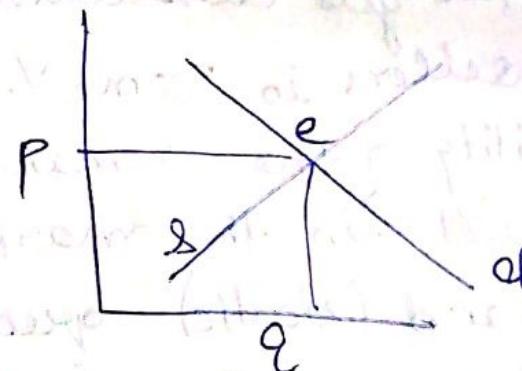
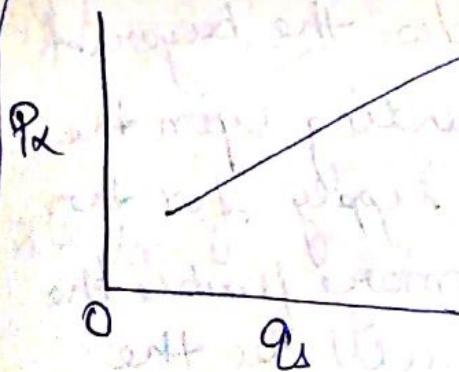
Supply is a function of price
 $S = f(\text{Price})$



Foreign Exchange Market Equilibrium

Supply analysis

Factors affecting Supply (Write short notes)



Market equilibrium refers to the point where the total quantity demanded equals the quantity supplied thereby determining the equilibrium price & quantity. Demand = Supply

→ 1. Price of commodity.

2. Price of related commodities

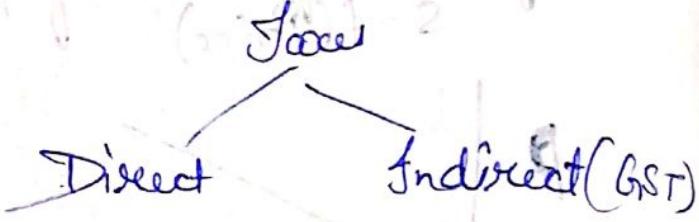
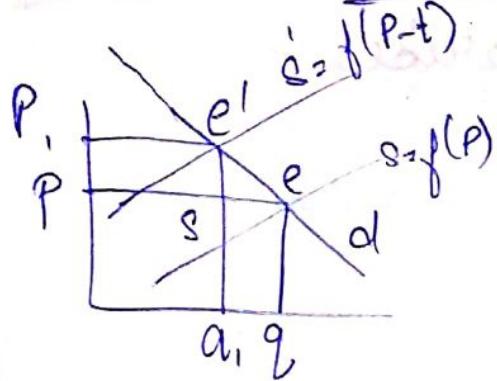
3. State of technology

4. Factor availability & their prices

5. Time

Before eq $S > D$
After eq $D > S$

Market eq with Tax & Subsidies



$$OP = 10$$

$$t = \text{tax per unit} = 2$$

$$G_{\text{GST}} = \text{e}, G_r$$

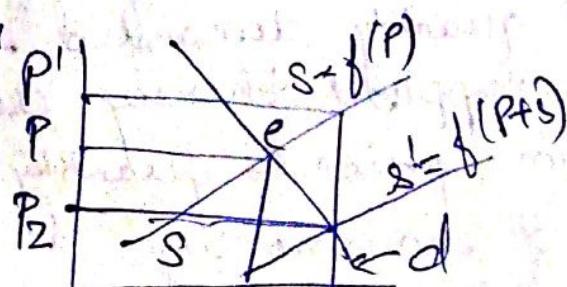
$$\text{Buyer} = \text{e}, H$$

$$\text{Seller} = H, G_r$$

Depends on if product is elastic/inelastic
 ↓
 TV petrol
 frige salt

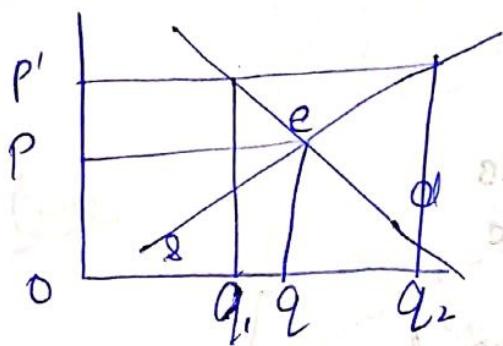
In case of indirect taxes the total burden of the tax gets distributed b/w the buyers & the sellers in some %. depending upon the flexibility of the demand & supply for the product. In the market more flexible the demand (elastic), greater will be the burden on seller & vice versa.

② Subsidies.



It refers to the difference from the market price which is paid by the govt ~~which~~ to encourage the production & consumption of the product in the market.

3. Maximum support price

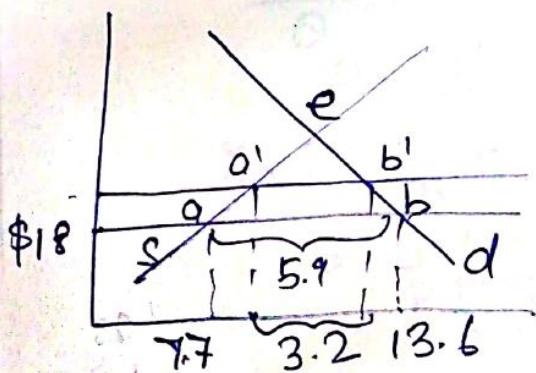


$$\begin{aligned} \text{Dem} &= DQ_1 \\ \text{Supply} &= SQ_2 \\ \text{Surplus} &= Q_2 - Q_1 \end{aligned}$$

Ques Total demand - 13.6 million barrels/day
7.7 M bpd - US produces

Rest imported

Avg price of oil = \$18 → below the eq price



$$\begin{aligned} \textcircled{1} \quad \text{T}_{\text{exc}} &= 33\frac{1}{3}\% \text{ on } \$18 \\ &\rightarrow \frac{100}{3 \times 100} \times 18 = \$6 \end{aligned}$$

\textcircled{2} \quad b' = 12.8 \text{ million}, Q' = 9.0 \text{ million}

$$\text{Revenue} = P \times Q = 3.0M \times 6 = 18.0M$$

- Tariff = tax on imported goods
- + Supply increased, import decreased.

Ques 4 Consumers

A B C

A: $P = 85 - 0.5 Q_A$

B: $P = 50 - 0.25 Q_B$

C: $P = 40 - 2.00 Q_C$

i) find the market demand function.

$$Q_d = Q_A + Q_B + Q_C$$

$$P = 85 - 0.5 Q_A$$

$$Q_A = \frac{P - 85}{0.5}$$

$$Q_B = \frac{P - 50}{0.25}$$

$$Q_C = \frac{P - 40}{2}$$

$$Q_A + Q_B + Q_C = \frac{P - 85}{0.5} + \frac{P - 50}{0.25} + \frac{P - 40}{2}$$

$$0.25$$

$$Q_d = 290 - 6.5P$$

$$Q_d = Q_s = 40 + 3.5P$$

$$290 - 6.5 = 40 + 3.5P$$

$$(P = 25)$$

ii)

$$Q_d = 290 - 6.s \quad (2s)$$

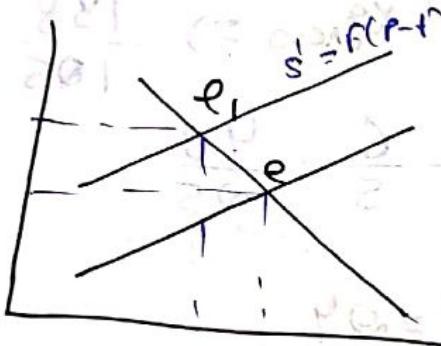
$$\therefore Q_d = 290 - 162.s$$

$$Q_d = 127.5$$

$$\begin{array}{r} 65 \\ \hline 25 \\ 25 \\ \hline 130 \\ \hline 162.5 \end{array}$$

$$\begin{array}{r} 90.0 \\ 162.5 \\ \hline 27.5 \end{array}$$

Ques



$$X_d = \frac{1}{2}(5-P)$$

$$X_s = 2P - 3$$

i)

$$X_d = X_s$$

$$\frac{5-P}{2} = 2P - 3$$

$$P = \frac{11}{5}$$

$$X_d = \frac{1}{2}\left(5 - \frac{11}{5}\right)$$

$$\Rightarrow \frac{1}{2}\left(\frac{14}{5}\right) = \frac{7}{5}$$

ii)

$$X_s = 2P - 3$$

$$X_s' = 2\left(P - \frac{6}{5}\right) - 3$$

$$\frac{5-P}{2} = 2P - \frac{19}{5} - 3$$

$$\frac{5}{2} - \frac{P}{2} = 2P - \frac{12}{5} - 3$$

$$\frac{5}{2} + \frac{12}{5} + 3 = \frac{P}{2} + 2P$$

$$\frac{25+24+30}{10} = \frac{P+4P}{2}$$

$$\frac{79}{10} = \frac{5P}{2}$$

$$\Rightarrow P' = \frac{79}{25}$$

$$\begin{array}{r} 25 \\ \hline 50 \\ 25 \\ \hline 25 \\ \hline 25 \end{array}$$

$$\begin{array}{r} 152 \\ \hline 30 \\ \hline 200 \end{array}$$

$$\begin{array}{r} 21 \\ \hline 27 \\ \hline 52 \end{array}$$

Consumer's Equilibrium

Consumer's Equilibrium refers to that point where the total utility of the consumer is maximized given his budget constraint.

Indifference Curve

An indifference curve of the consumer represents the different combinations of the commodities which will give the consumer the same level of satisfaction.

$$\text{utility} \rightarrow U = f(x, y)$$

$$\text{change: } \frac{\partial U}{\partial x} dx + \frac{\partial U}{\partial y} dy$$

$$\Rightarrow Muxdx + Muydy = 0$$

$$-\frac{dy}{dx} = \frac{Mux}{Muy} = \text{marginal rate of substitution.}$$

Marginal rate of substitution - MRS_{xy}

It refers to the rate at which the consumer is able to substitute one commodity with another without affecting his total utility level.

Table

Combination	Units of X	Units of Y	U ₁ U ₂	MRS
A	1	30	U ₁ U ₂	-
B	2	24	U ₁ U ₂	6:1
C	3	19	U ₁ U ₂	5:1
D	4	15	U ₁ U ₂	4:1

Budget Line \rightarrow $P_x Q_x + P_y Q_y = M$

- $M = P_x Q_x + P_y Q_y$ (say \$ 100)
- $M = \text{total budget}$
- $P_x = \text{price per unit of commodity } X$ (say ₹ 10)
- $P_y = \text{price per unit of commodity } Y$ (say ₹ 50)
- $Q_x, Q_y = \text{Quantity of commodity } X \& Y.$

2nd class in PDF: 39 no marks for 200

3rd class in PDF:

Diminishing marginal utility

Elasticity of Demand

Ed refers to the proportionate change in quantity demanded of a product due to a certain proportionate change in

- ① price
- ② income
- ③ Price of related commodity

3 types of Ed :

① Price elasticity of demand = $f(P_x, Y, \bar{P}_y)$ (e_p)

Income Ed shows as $f(Y, \bar{P}_x, \bar{P}_y)$

Cross Ed shown as $e_C \Rightarrow f(P_y, Y, \bar{P}_x)$

1. $e_p = \frac{\text{Proportionate change in quantity demanded}}{\text{Proportionate change in price}}$

$$= \frac{\Delta q/q}{\Delta p/p} = \frac{\Delta q}{\Delta p} \cdot \frac{p}{q}$$

(P & q) \rightarrow initial value

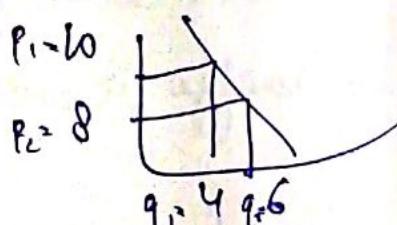
$$\Delta q = q_1 - q_2$$

$$\Delta p = p_1 - p_2$$

$$\Delta p = 2$$

$$\Delta q = -2$$

$$-1 \times \frac{10/5}{4/2} = \frac{-5}{2}$$



(inverse relation between price and demand)

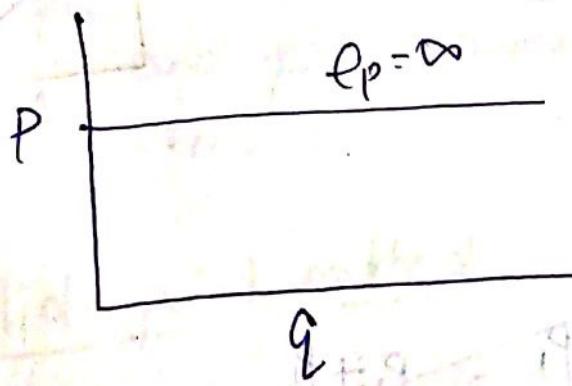
Price elasticity will always have a negative sign, because of the inverse relationship between quantity and price.

So for interpretation we take its absolute value.

for every 1% change in price, the quantity is responding by 0.5%.

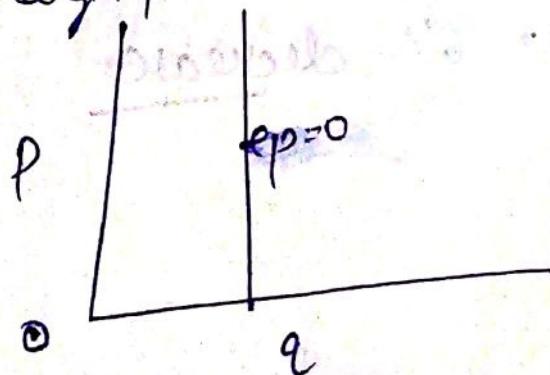
Degree of Price Ed :-

① Perfectly elastic demand! In this case without any change in price the quantity demanded responds infinitely.



② Perfectly inelastic demand!

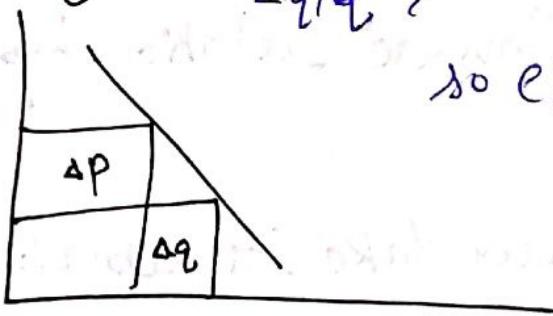
whatever demand does not change in price, no matter the change in price.



3. Relatively elastic demand

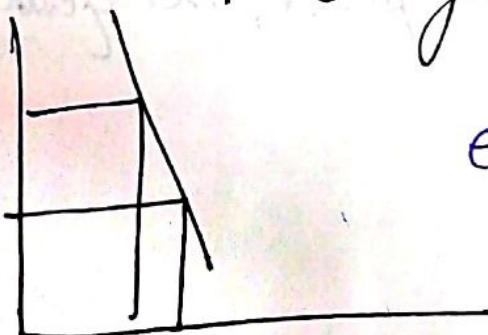
$$\frac{\Delta q/q}{\Delta p/p} > 1$$

$$\text{so } e > 1$$



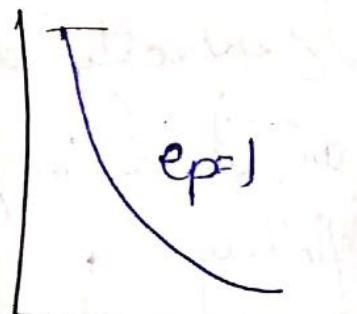
4.

Relatively inelastic demand



$$e < 1$$

5. Unitary elastic demand.



Ques $e = 1.2$

$$\frac{P_2 - P_1}{P_1} = \frac{Q_2 - Q_1}{Q_1}$$

~~100/20~~

$$1.2 = \frac{Q_2 - Q_1}{Q_1}$$

$\Delta Q/Q = 6\%$, decrease

Methods of Measuring Price Ed:

- (i) Point/percentage method
- (ii) Mid-point method
- (iii) Total revenue method
- (iv) Graphical method.

① Percentage method

$$\epsilon_p = \frac{\Delta q}{\Delta p} \frac{P}{q}$$

Bcz getting diff value.

The limitation of this method is that it gives different values of price elasticity even for the same absolute change in quantity and price depending on the initial value taken.

② Mid-point method

In this method, instead of taking the initial values we will take the average of the price and quantity variable.

$$(\frac{\Delta q}{\Delta p}) * \frac{P_1 + P_2}{Q_1 + Q_2}$$

Ques

$$q_1 = 80$$

$$p_1 = 1$$

$$q_2 = 48$$

$$p_2 = 2$$

Ques

$$\epsilon_d = -\frac{32}{1} \times \frac{3}{64 \times 2} = \frac{-3}{4} = -0.75$$

its < 1 , so relatively inelastic

(iii) Total revenue method:

$$\% \text{pt} \approx \frac{\Delta TR}{TR} = \frac{\Delta P \times Q + P \times \Delta Q}{P \times Q}$$

In this method we observe the total revenue of the producer before and after the price change to know about the elasticity of the product.

(ii)

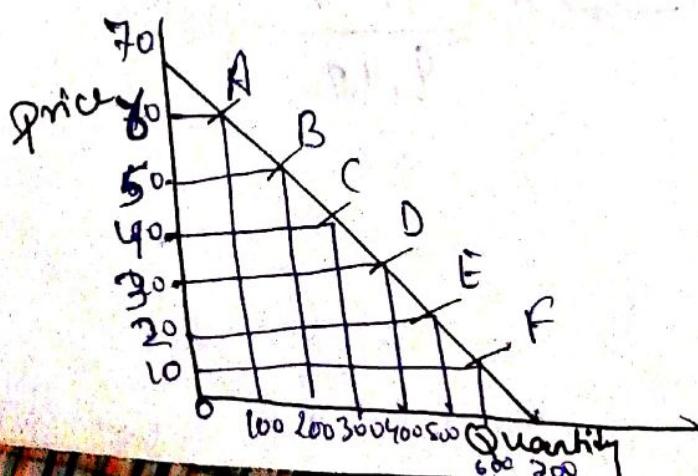
Reverse change of Q is less.

$$\begin{cases} P \uparrow \\ P \downarrow \end{cases} \times Q \Delta \uparrow \Rightarrow \begin{cases} TR \uparrow \\ TR \downarrow \end{cases} \Rightarrow \text{inelastic.}$$

$$\begin{cases} P \uparrow \\ P \downarrow \end{cases} \times Q \Delta \downarrow = \begin{cases} TR \downarrow \\ TR \uparrow \end{cases} \Rightarrow \text{elastic}$$

Same - Inelastic

The price very and



Ques

for A, B

$$\frac{\Delta Q}{\Delta P} \times \frac{P_{av}}{Q_{av}}$$

$$= \frac{-1/\phi}{1/\phi} \times \frac{u/\phi}{3/\phi} = \frac{11}{3}$$

$= 3.66 > 1$
Relatively elastic

for C, D,

$$\frac{1/\phi}{-1/\phi} \times \frac{9/\phi}{50^0} = 1$$

for E dF = 0.27

(i) B \leftarrow A
 $50 \rightarrow 60$

$$T_P = 50 \times 20^0$$

$$T_P = 6000$$

Revenue is falling
elastic product.

The producer should not go for the price increase because the product is very elastic in this price range, means $A \rightarrow B$ and so the revenue is falling.

Q-2

$$P_1 = 150$$

$$P_2 = 142.5$$

$$q_1 = 2000$$

$$\epsilon_p = 0.7$$

$$TR_1 = 150 \times 2000$$

$$= 300000$$

$$\frac{150}{142.5} \times 271$$

~~Ques TR~~

$$\frac{150}{142.5} \times 292.5$$

$$0.7 = \frac{2000 - q_2}{150 - 142.5} \times \frac{180 + 142.5}{2000 + q_2}$$

$$0.7 = \frac{(2000 - q_2)(192.5)}{(7.5)(2000 + q_2)}$$

$$0.7 = \frac{\Delta q}{7.5} \times \frac{180}{200}$$

$$0.7 = \frac{\Delta q \times 8}{100}$$

$$70 = \frac{\Delta q}{200} \times 1930$$

$$TR \Rightarrow q_1 - q_2 = \Delta q$$

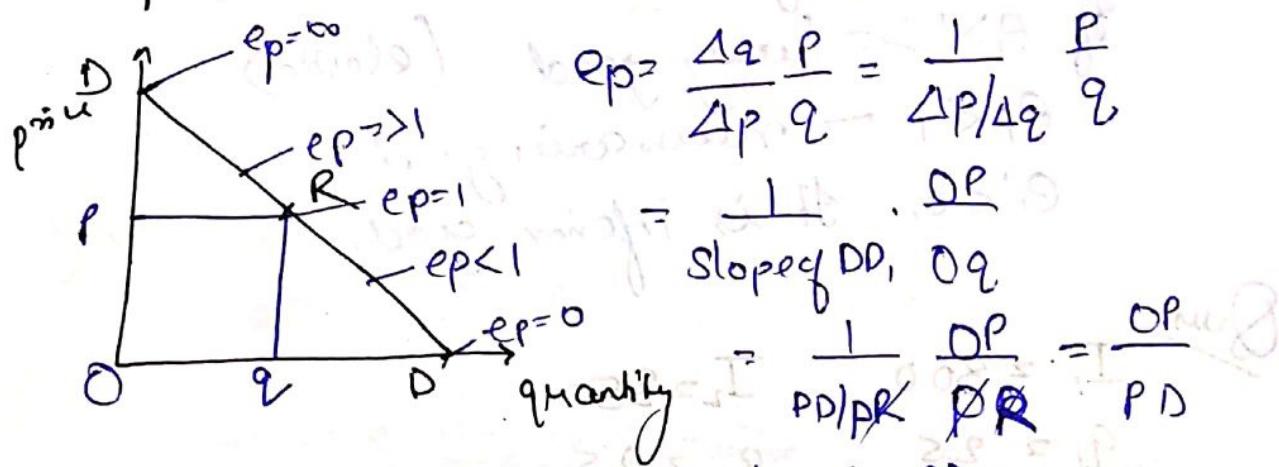
$$2000 - q_1 = 70$$

$$2000 + 70 = q_2$$

$$1930 = q_2$$

$$TR_2 = (1930)(142.5) = 275,025$$

Graphical method



Triangle PDR is similar to $\triangle qRD$, \rightarrow
so would have proportional sides.

$$e_p = \frac{OP}{PD} = \frac{QR}{PD} = \frac{RD'}{RD} = \frac{\text{lower segment of DD'}}{\text{upper segment of DD'}}$$

Income Elasticity of Demand (e_i)

It will measure the proportionate change in quantity demanded of the product due to a ~~fixed~~ proportionate change in income of the consumer.

$$\text{Percentage method} \Rightarrow e_i = \frac{\Delta q}{\Delta Y} \cdot \frac{Y}{q}$$

$$\text{ARC / mid point} \Rightarrow e_i = \frac{\Delta q}{\Delta Y} \cdot \frac{Y_1 + Y_2}{q_1 + q_2}$$

It will be true.

Values of e_i

- If $e_i > 1 \geq$ luxury good (elastic)
- $e_i < 1$ — necessary good
- $e_i < 0$, it is inferior good.

Ques

$$I_1 = 300 \quad I_2 = 350$$

$$q_1 = 25 \quad q_2 = 35$$

$$e_i = \frac{I_2 - I_1}{I_1} \times \frac{\frac{q_2 - q_1}{q_1}}{\frac{P_2 - P_1}{P_1}} = \frac{13}{25} \times \frac{13}{6} = \frac{169}{150}$$

Cross Elasticity of Demand

It will measure the proportional change in quantity demanded of a product due to a certain proportional change in the price of some other related commodities.

Percentage method -

$$e_c = \frac{\Delta q_x}{\Delta p_y} \cdot \frac{P_y}{q_x}$$

Mid point

$$e_c = \frac{\Delta q_x}{\Delta p_y} \cdot \frac{P_{y_1} + P_{y_2}}{q_{x_1} + q_{x_2}}$$

$e_c > 0 \Rightarrow$ Substitute
 $e_c < 0 \Rightarrow$ complement
 $e_c = 0 \Rightarrow$ unrelated

Ques

$$\frac{20}{\cancel{60}} \quad \frac{-8}{\cancel{30}} = 2$$

$$\Delta q = \frac{-10}{1} \times \frac{4}{50} = \frac{4}{5}$$

$$e_i \Rightarrow \frac{-10}{-1} \times \frac{4}{50} = \frac{4}{5} \text{ substitute}$$

$\Delta q \Rightarrow -10 \times \frac{4}{50} = \frac{4}{5}$ ~~Teal coffee~~ Butter

$$e_i \Rightarrow \frac{-10}{-1} \times \frac{7}{80} = -\frac{7}{8} \text{ complementary}$$

Ques

$$P_1 = 100$$

$$I_1 = 100$$

$$P_2 = 110$$

$$I_2 = 105$$

$$p_i = -1.4$$

$$I_i = 2.2$$

$$Q_1 = 50000$$

$$P_1 = 10000$$

$$Q_2 = 10000 \times \frac{10}{100} = 1000$$

$$(-1.4) = \frac{\Delta Q/2}{0.19} + 2.2 = \frac{\Delta Q/2}{0.05}$$

Net effect \rightarrow

$$-1.4 + 2.2 = -3\%$$

$$TR = 5 \times 10^8 = 5 \text{ crore}$$

$$TR_2 = (q - \Delta q)(P + \Delta P)$$

$$(48500)(11000) = 53.35 \text{ crore}$$

$$TR = P \times Q$$

$$\frac{dTR}{dQ} = P + Q \frac{dP}{dQ}$$

$$\Rightarrow P \left(1 + Q \frac{dP}{dQ} \right)$$

$$MR = AR \left(1 - \frac{1}{e_P} \right)$$

$$e_P^2 = \frac{AR}{AR - MR}$$

$$AR = P$$

$$e_P^2 = \frac{dQ}{dP} \cdot \frac{P}{Q}$$

Ques. 4 $P = 50 - 3x$

$$Sx > 4S$$

$$x > 1S$$

$$Sx > 4S$$

$$x > 1S$$

$$P = 50 - 3x$$

$$\frac{dx}{dP} \cdot \frac{P}{x} = e_P$$

$$P = 50 - 3x$$

$$\frac{dP}{dx} = -3$$

$$\frac{1}{-3} \times \frac{50}{15} = \frac{1}{9}$$

~~e_P~~ $\bullet MR = P = S$

$$MR = \frac{dTR}{dX} =$$

$$P = 50 - 3x$$

$$TR = 50x - 3x^2$$

$$\frac{dTR}{dX} = 50 - 6x$$

$$= 60 - 90$$

$$= \cancel{60} - 40$$

18
98

$$\epsilon P = \frac{5}{5-(-40)} = \frac{1}{9}$$

$$P = 400 - 2q - 3q^2$$

$$\frac{dP}{dq} = -2 - 6q \quad P = 400 - 20 - 300$$

$$\frac{dP}{dq} = -2 - 60 \quad P = 80$$

$$\chi = A - \frac{1}{62} \times \frac{80}{4} = \frac{4}{31}$$

$$MR = P = 80$$

$$TR = 400q - 2q^2 - 3q^3$$

$$\frac{dTR}{dx} = 400 - 4q - 9q^2$$

$$= 400 - 40 - 900$$

$$= -540$$

$$\frac{80}{80+540} = \frac{80}{620} = \frac{4}{31}$$

$$\text{translating to } \frac{80}{80+540} = \frac{80}{620} = \frac{4}{31}$$

Class in PDF

5. Equal Payment Present worth factor

$$P = A \left[\frac{(1+i)^n - 1}{i(1+i)^n} \right] \rightarrow n(P/A, i, n)$$

$$P = A \left[\frac{A}{(1+i)} + \frac{A}{(1+i)^2} + \dots + \frac{A}{(1+i)^n} \right]$$

Divide both sides with $(1+i)$

$$\frac{P}{(1+i)} = \frac{A}{(1+i)^2} + \frac{A}{(1+i)^3} + \dots + \frac{A}{(1+i)^{n+1}}$$

Subtract ⑪ from ⑩

$$P - \frac{P}{(1+i)} = \frac{A}{(1+i)} - \frac{A}{(1+i)^{n+1}} \quad \text{--- ⑪}$$

$$P(1+i) - P = A \left[1 - \frac{1}{(1+i)^n} \right] \quad \text{--- ⑩}$$

$$P = A \left[\frac{(1+i)^n - 1}{i(1+i)^n} \right]$$

The objective of this mode of investment is to find the present worth of a series of annuity investment made at the end of each interest period.

G Capital Recovery factor

$$A = P \left(\frac{i(1+i)^n}{(1+i)^n - 1} \right)$$

$$\Rightarrow P(A(P,i,n))$$

The objective of this mode of investment is to find the ~~total amount~~ ^{at the end of each period} of annuity investment made to recover the ~~capital~~ presently invested sum of the capital.

Interest Formula

- ① Single Payment Future Worth factor:

$$F = P(1+i)^n = P(F/P,i,n)$$

- ② Single Payment Discount Factor

$$P = F \left(\frac{1}{(1+i)^n} \right)$$

- ③ Equal Payment Future Worth Factor

$$F = A \left\{ [(1+i)^n - 1] / i \right\}$$

- ④ Equal Payment sinking fund factor:

$$A = F \left\{ i / [(1+i)^n - 1] \right\}$$

- ⑤ Equal Payment Present worth factor

$$P = A \left\{ [(1+i)^n - 1] / [i(1+i)^n] \right\}$$

- ⑥ Equal payment capital recovery factor.

$$A = P \left\{ i(1+i)^n \right\} / \left\{ [(1+i)^n - 1] \right\}$$

- ⑦ Uniform gradient series formula.

$$A = A' + G \left\{ \left[(1+i)^n - 1 \right] / [i(1+i)^n - i] \right\}$$

$P \rightarrow 0^m$
 $F = n^{th}$ - last
 $A \Rightarrow$ Yearly

① $F = 10 \text{ Lakh}$

$$P = F \left(\frac{1}{(1+i)^n} \right)$$

$$P = 1000000 \left(\frac{1}{(1+0.15)^{10}} \right)$$

$$= 1000000 \left(\frac{1}{(1.15)^{10}} \right)$$

$$= 1000000 \left(\frac{1}{4.04} \right)$$

$$= 24752.4$$

$$= 2.47 \text{ lakh}$$

Ans

~~$A = F \times i / [1 - (1+i)^{-n}]$~~

$$A = 10000$$

$$F = A \left\{ [1+i]^n - 1 \right\}^{-1}$$

$$n = 25$$

$$F = 10000 \cdot \frac{[(1+0.2)^{25} - 1]}{0.2}$$

$$F = 10000 \left[\frac{94.39}{0.2} \right]$$

$$F = 4769$$

Ques. 3

$$F = ?$$

$$P = 50000$$

$$F = 50000 (1 + 0.5)^{30}$$

$$\approx 50000 (4.32)$$

$$\approx 5.03 \text{ lakh}$$

Ques. 4

$$P = 2000 \text{ lakh}$$

$$A =$$

$$A = 2000000 \frac{[0.12(1.12)^{20}]}{[(1.12)^{20} - 1]}$$

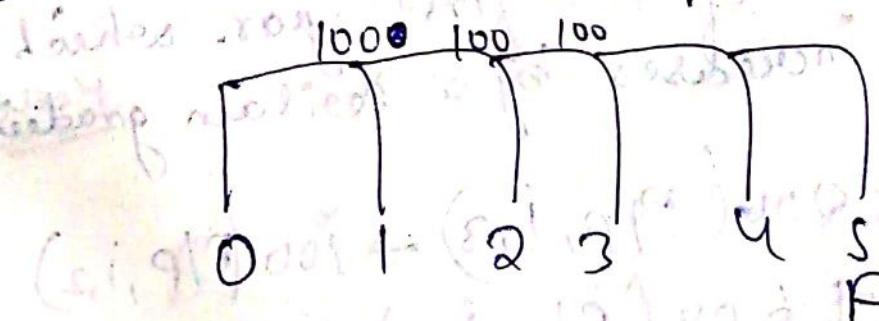
$$A = 2000000 \frac{[1.157]}{(8.646)}$$

$$A = 2000000$$

$$A = 2.67 \text{ lakh}$$

Ques. 1 $m = 5$

Cash flow diagram



$$\textcircled{10} P = A \left\{ \frac{[1+i]^n - 1}{i(1+i)^n} \right\}$$

$$\textcircled{11} P = 100 \left\{ \frac{1}{[1 + 0.05]^{35}} \right\}$$

7 Uniform Gradient Series formula!

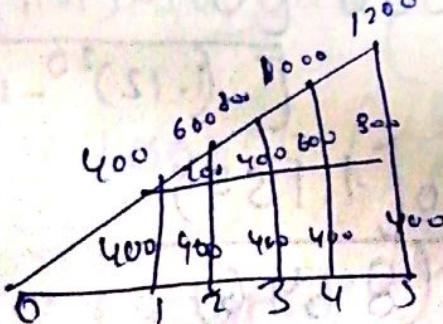
400 \rightarrow Base annuity - A
 800 \rightarrow Gradient - G

n = 5 years

400, 400+200, 400+400, 400+600,

400+800

A, A + 14G, A + 28G, A + 42G, A + 56G



The objective of this mode of investment is to find the annuity amount equivalent to a given series of investment with a base year amount at the end of the first year which thereafter increases by a certain gradient

$$F = 200(F/P, i, 3) + 400(F/P, i, 2)$$

$$+ 600(F/P, i, 1) + 800$$

$$= 14(1+i)^3 + 24(1+i)^2 + 34(1+i)$$

multiply $(1+i)$ both sides

$$F(1+i) = 16(1+i)^4 + 24(1+i)^3 + 36(1+i)^2 + 48(1+i) \quad \text{--- (1)}$$

Subtract (11) from (9)

$$F - F(1+i) = -16(1+i)^4 - 16(1+i)^3 \\ - 16(1+i)^2 - 16(1+i) + 4G$$

$$F_i = 16 \left[(1+i)^4 + (1+i)^3 + (1+i)^2 + (1+i) + i \right] - nG$$

$$F_i = 16(F/A, i, n)$$

To convert into annuity
mut $(A/F, i, n)$

$$A_i = 16 \left[1 - \frac{1}{(1+i)^n} \right]$$

$$A^* = 16 \left[\frac{(1+i)^n - 1 - i^n}{i((1+i)^n - 1)} \right]$$

$$A = A_i + A^*$$

Ques 4 $A_i = 400, A^* = 200, n = 5 \text{ yrs}, i = 10\%$

$$A = 200 \left(\frac{(1.10)^5 - 1 - (0.1)(5)}{(0.1)(1.1)^5 - 0.1} \right)$$

$$A^* = 200 \left(\frac{(1.61) - 1 - 0.5}{(0.1)(1.61) - 0.1} \right)$$

$$A^* = 200 \left(\frac{0.11051}{0.061} \right) = 362.32$$

$$A = 400 + 362.32$$

Ques $i = 15\%$

$$A_1 = 4000 \left[\frac{(1+0.15)^{10} - 1 - 0.15}{(0.15)(1.15)^{10} - 0.15} \right]$$

$$A_2 = 500 \left[\frac{4.04 - 1 - 0.15}{(0.15)(4.04) - 0.15} \right]$$

$$A_2 = 500 \left[\frac{2.89}{0.456} \right] = 8168.85$$

\Rightarrow ~~$A_1 + A_2$~~

$$A = A_1 + A_2 = 5691$$

$$F = 5691 \left[\frac{(1.15)^{10} - 1}{0.15} \right]$$

$$= 5691 \left[\frac{3.045}{0.15} \right]$$

$$= 115548$$

Ques

$$G = 500, A_1 = 8500$$

$$i = 15\%, n = 10$$

~~$A_2 = 500, A = 8500 = 1691.11$~~

~~$A = 102972 = 6808.9$~~

~~$F = 10191.11 F$~~

~~$F = 8060879.8 1.38 \text{ Lakh}$~~

Ques

$$G = 30, A = 120, i = 5\%.$$

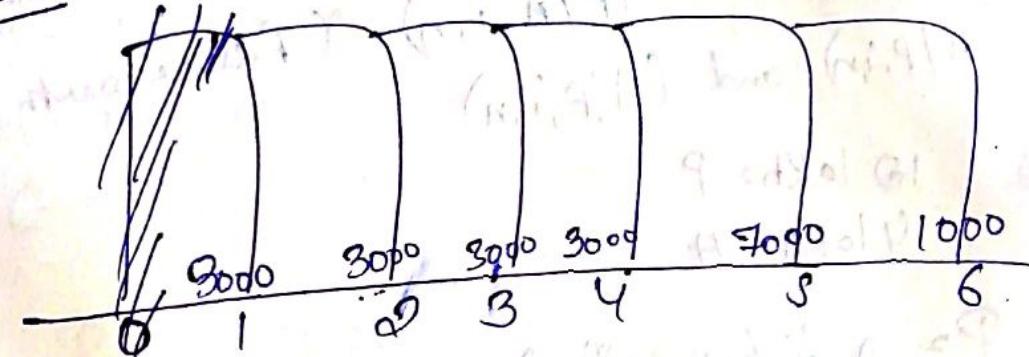
1.05

$$\textcircled{B} \quad A = [120 + 30 \left(\frac{(1+i)^n - 1 - in}{i(1+i)^n - i} \right)]$$

$$A = [120 + 30 \left(\frac{(1.05)^6 - 1 - 6in}{i(1.05)^6 - i} \right)]$$

$$\textcircled{B} \quad F = 762 - \approx$$

Q-3



$$P = ?$$

$$P = [3000 \left\{ \frac{(1+0.14)^4 - 1 - 4in}{(0.14)(1-0.14)^4} \right\}] \left(\frac{1000}{(1.14)^5} \right)$$

$$\textcircled{B} \quad P = \left[3000 \left\{ \frac{(1+0.14)^4 - 1 - 4in}{(0.14)(1-0.14)^4} \right\} + \frac{1000}{(1.14)^5} \right]$$

Bases of Comparisons of alternatives

Five bases for comparison.

① Present worth criteria

In this method of comparison, we convert all the cash flow details to the 0th year for evaluation.

② ~~P~~ $P/F, i, n$ and $(P/A, i, n)$ (Present worth criteria)

③ $(F/P, i, n)$ and $(F/A, i, n)$ (Future worth criteria)

④ $(A/P, i, n)$ and $(A/F, i, n)$

Ques $12 \text{ lakh} = P$
 $4 \text{ lakh} = A$

$$P = A \left\{ \frac{(1+i)^n - 1}{(1+i)^n} \right\}$$

$$P = 4 \left\{ \frac{(1.20)^{10} - 1}{(1.20)^{10}} \right\}$$

$$(0.20)(1.20)^{10}$$

$$P = 4 \left(\frac{5.19}{1.238} \right)$$

$$P = 16.76$$

$$\text{Profit} = 16.76 - 12 \text{ lakh} \\ \Rightarrow 4.76$$

$$P_{W_2} = \cancel{P = 6}$$

$$\textcircled{2} P_{\text{Profit}} = 5.15 L$$

~~$$\textcircled{2} \text{ Profit} = 2.90 L$$~~

future worth

$$fP_1 = -12L(F/P, i, 10) + 4L(F/A, i, 10)$$

~~\textcircled{2}~~ A will be return

Ques

$$P = 4,50000$$

$$n = 15$$

$$C = 30000$$

$$\textcircled{3} P_{W_1} = \frac{30000 \left((1.15)^{15} - 1 \right)}{(0.15)(1.15)^{15}}$$

$$P_2 = 30000 \times \frac{7.13}{(1.22)}$$

$$P_2 = 175327.86$$

Cost

~~$$P_{\text{Profit}} = 6.25 \text{ Lakh} \Rightarrow P_{W_1}$$~~

$$P_{\text{Profit}} = 1.8 \quad P_{W_2} = 6.36 \Rightarrow \text{Cost}$$

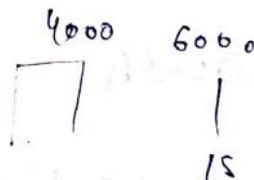
The first project is selected because its cost is less.

Q3 $P = 1000$ } Scheme I
 $n = 15$
 $F = 12000$

$$P = 1000$$

$$F = 4000$$

$$n = 10$$



$$P = 12000 \left\{ \frac{1}{(1+0.12)^{15}} \right\}$$

$$\text{Projt}^2 = 2.19 \text{ L}$$

$$P_{W_1} = -1000 + 2.19$$

$$\Rightarrow 1.19$$

~~$$P_{W_1} = -187.8$$~~

$$P_{W_2} = -1000 + \left[\frac{4000}{(1.12)^{10}} + \frac{6000}{(1.12)^{15}} \right] \\ \Rightarrow 1386$$

Ques 4

$$P = -100000 + \left[\frac{3000}{1.18} + \frac{3000}{(1.18)^2} \right. \\ \left. + \frac{7000}{(1.18)^3} + \frac{6000}{(1.18)^4} \right]$$

$$P = -100000 + 2542.3 + 905.6$$

$$4260.4 + 3094.7$$

~~$$P_{W_1} = 803.03$$~~

Nominal and effective rate of interest

In case of nominal rate, the compounding is done once in a year. In case of effective rate. The compounding is done more than once in a year.

$$r = \left(1 + \frac{i}{m}\right)^m - 1$$

m = the number of compounding done per year.

$$r = \left(1 + \frac{i}{m}\right)^m - 1$$

$$F = P \left(1 + \frac{i}{m}\right)^{mn}$$

Ques

$$r = \left(1 + \frac{0.13}{8}\right)^8 - 1$$

$$r = \left(1 + \frac{0.13}{8}\right)^2$$

$$r = 0.034$$

$$r = \left(1 + \frac{0.13}{8}\right)^4 - 1 = 13.64$$

$$r = \left(1 + \frac{0.13}{12}\right)^{12} - 1$$

$$r = \left(1 + \frac{0.13}{52}\right)^{52} - 1$$

$$1 \frac{1}{2} - \frac{3}{2}\%$$

~~$$i = 1.5\%$$~~

~~$$i = \left(1 + \frac{j}{m}\right)^m - 1$$~~

~~$$i = 1 + \underline{0.015}$$~~

$$\textcircled{1} \quad i = \frac{3}{4} \times 8 = 6\% \quad \text{nominal rate}$$

$$r = \left(1 + \frac{0.06}{4}\right)^4 - 1$$

$$r = 6.19 \quad (\text{Effective rate})$$

Ques

$$i = 15\%$$

$$m = 4$$

$$n = 3$$

$$F = 1000 \left(1 + \frac{0.15}{4}\right)^{12}$$

$$= 1000 \times 1.555$$

Q-3

$$P = ?$$

$$F = n^m$$

A - repeating every year

Each year A

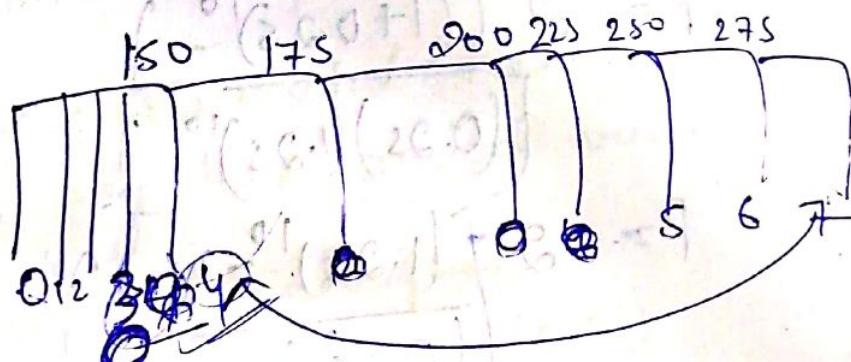
$$P = \frac{3000 \left(\frac{(1.14)^4 - 1}{(0.14)(1.14)^4}\right)}{1}$$

$$P_2 = 3000 \left(\frac{0.688}{0.236} \right)$$

$$\Rightarrow 87457.62$$

P_2

Ques



$P - 0^{\text{th}} \text{ year}$ gives A

$P = ?$

$$\begin{array}{c} 7 \\ 5 \\ 2 \end{array} \quad A = 150 \quad P = ? \quad G_1 = 25$$

$$P = [150 + 25]$$

5

$$P = 16 \text{ lakhs}$$

$$i = 25\%$$

$$A = 2 \text{ lac}$$

$$n = 10 \text{ years}$$

18c.

$$\begin{aligned} P &= 2 \left[\frac{\left(1 + 0.25\right)^{10} - 1}{0.25(1.25)^{10}} \right] \\ P_2 &= 2 \left[\frac{(1.25)^{10} - 1}{(0.25)(1.25)^{10}} \right] \\ &\approx \frac{(8.3)}{2.32} \\ &\approx 7.16 + 4L \\ &= 12.98 \end{aligned}$$

~~= 12.98~~ ~~2.9 + 2.9~~ ~~12.98~~

Scheme I - 16

Scheme II - 12.98 ✓

Capital Budgeting Techniques OR

Investment Criteria

They refer to the different criteria based on which we either accept or reject a given investment proposal.

① Non-discounted techniques:-

The pay-back period criteria.

② Discounted Techniques

i) Net present value (NPV)

ii) Internal rate of return criteria (IRR)
and

iii) Benefits - cost ratio criteria.

Pay back period criteria

It refers to the minimum no of years within which the initial cost of investment is recovered.

I. Pay back in case of annuity returns.

$$P_B = \frac{\text{Initial cost}}{\text{annuity returns}}$$

$$C_0 = 1 \text{ Lakh}$$

$$A = 12500$$

$$P_B = 8 \text{ years}$$

II P_B in case of non-constant returns.

Co = 20,000

Yr Returns of P_B

1 8000

2 7000

3 4000

4 2000

5 2000

6 4000

$$\frac{1000}{2000} \times 12 = 6 \text{ months}$$

By 6 months.

Though the method is simple and cost effective but the limitations are

- ① It gives no time preference.
- ② It ignores the returns after the pay back period.

Q-1 Project 1 - By 4 month

2 - By 10 month.

~~1000~~ x ~~1/4~~

~~800~~ x ~~1/4~~

~~200~~ x ~~1/4~~

Net present value criteria - P

Return - cost

In this method we discount the returns from the project over the years and compare it with its initial cost for evaluation.

$$NPV = \left[\frac{R_1}{(1+i)} + \frac{R_2}{(1+i)^2} + \dots + \frac{R_t}{(1+i)^t} \right] -$$

$$\left[C_0 - \frac{SV}{(1+i)^n} \right]$$

$$= \sum_{t=1}^n \frac{R_t}{(1+i)^t} - \left[C_0 - \frac{SV}{(1+i)^n} \right]$$

F = SV - Recall value

R_t = Return value

C₀ = Initial cost

SV = Salvage value

i = opportunity cost of investment

Decision Rule

If $NPV > 0 \rightarrow$ accept

If $NPV < 0 \rightarrow$ reject

If $NPV = 0 \rightarrow$ state of indifference.

* Salvage value refers to the scrap or end value of an asset when it is disposed off at the end of its productive lifetime.

i = market prevailing interest

①

$$n = 10$$

$$P = 40000 = C_0$$

$$SV = 10000$$

$$r = 10\%$$

$$\begin{aligned} NPV = & \left[\frac{7000}{(1.1)} + \frac{9800}{(1.1)^2} + \frac{10800}{(1.1)^3} + \frac{11100}{(1.1)^4} \right. \\ & + \frac{9400}{(1.1)^5} + \frac{7600}{(1.1)^6} + \frac{5700}{(1.1)^7} + \frac{4000}{(1.1)^8} \\ & \left. + \frac{2000}{(1.1)^9} + \frac{2000}{(1.1)^{10}} \right] - \left[40000 - \frac{10000}{(1.1)} \right] \end{aligned}$$

$$\begin{aligned} NPIV = & 6363.63 + 8099.17 + 8114.19 \\ & + 7581.44 + 5836.66 + 4290 \\ & + 3925. + 1866.02 + 848.19 \\ & + 771.08 - [36144.56] \\ = & 10550.82 \end{aligned}$$

Internal Rate of Return

$$\sum_{t=1}^n \frac{R_t}{(1+r)^t} = \left[C_0 - \frac{S_v}{(1+i)^n} \right]$$

r profitable

If IRR refers to that rate of discount which will make the present value of the returns equal to the initial cost of investment. Thus it is the rate of discount which will make the NPV of the project 0.

Decision rule

- If $r > i$ = accept
- $r < i$ = reject
- $r = i$ = state of indifference.

IRR in case of annuity returns:

$$P = 1 \left[\frac{(1+0.15)^{-1}}{(0.15)(1.15)^{10}} \right]$$

$$P = 1 \left[\frac{3.04}{0.606} \right] = 7.600$$

Steps

① Calculate the p ratio = $\frac{\text{Initial cost}}{\text{Annuity factor}}$ (Q. 22)

② find the range of IRR

③ The exact IRR = $\gamma = \frac{P - P_L}{P_n - P_L} (\gamma_n - \gamma_L)$

γ_n and γ_L are the upper value of rates in range.

P_n and P_L are p-ratios of γ_n and γ_L .

P = computed P-ratio.

Ques ① p ratio = $\frac{60000}{18000} = 3.33$

② Range

25% up 30% down

3.859 3.268

P_L P_u

$$\gamma = 0.03 - \frac{3.33 - 3.859}{3.859 - 3.268} (-0.05)$$

$$\gamma = 0.28 +$$

$$\gamma = 0.255 \text{ or } 25.5\%$$

(11)	$P_u = 5.86$	γ_u	88
	r_L	16 to 17	
	6.097	5.766	
	P_L	P_u	

$$\gamma = 0.17 - \left(\frac{5.86 - 6.097}{5.76 - 6.097} \right) \left(\frac{0.01}{0.006666666666666666} \right)$$

$$\gamma = 0.17 - \left(\frac{5.86 - 6.097}{5.76 - 6.097} \right) (0.01)$$

$$= 0.17 + \left(\frac{0.231}{0.331} \right) (0.01)$$

$$= 0.17$$

most profitable
(decreasing order)

= If opportunity cost is given select in order greater than γ .

In case of non uniform returns, the IRR is calculated by the trial and error method which utilizes the concept that, it is the rate of discount which makes the $NPV = 0$.

Steps

- ① Take any arbitrary rate of discount and find the NPV of the project
 If $NPV \rightarrow +ve \quad \gamma \uparrow$
 $NPV \rightarrow -ve \quad \gamma \downarrow$

If you get a negative NPV increase the
rate of discount and vice versa.

A negative and positive NPV gives us
range of IRR

② Within the range

$$IRR = r_L + \frac{d_L}{d_u} (r_u - r_L)$$

$$d_L = \text{NPV at } r_L - \text{NPV required}$$

$$d_u = \text{NPV at } r_u - \text{NPV at } r_L$$

Ques $r = 20\%$

$$\text{NPV}_L = \cancel{16000} \left(\frac{8000}{(0.2)^1} + \frac{7000}{(0.2)^2} + \frac{6000}{(0.2)^3} \right) - [16000]$$

$$\text{NPV} = 40000 + 175000 + 7500$$

$$- 1000$$

$$r = 16\%$$

$$\text{NPV} = -57$$

$$j = 15\%$$

$$\text{NPV} = \cancel{6956150} + 194$$

$$\begin{array}{r}
 \gamma_L \\
 15 \\
 194 \\
 d_L
 \end{array}
 \quad
 \begin{array}{r}
 \gamma_u \\
 -16 \\
 -57 \\
 d_u
 \end{array}$$

$$\gamma = 15 + \frac{194}{194 - (-57)} (16 - 15)$$

$$\Rightarrow \underline{15 + 3.4039} = 1$$

$$= 15 + \frac{194}{194 + 57}$$

$$\Rightarrow 15 + \frac{194}{251} = 15.77$$

Ques $\gamma = 15\%$

$$NPV = 30000 \left(\frac{(1.15)^5 - 1}{(1.15)^5 (0.15)} \right)$$

$$\Rightarrow 30000 \frac{(1.01)}{(0.301)}$$

$$\Rightarrow \underline{99.86 - 100764.11} \\ - 100000$$

$$\cancel{\gamma = 15\%} = 764.11$$

$\gamma = 9\%$

$$NPV = 30000 \left(\frac{(1.09)^5 - 1}{(0.09)(1.09)^5} \right)$$

$$30000$$

$$\gamma = \frac{19-1}{19}$$

$$NPV = 30000 \left(\frac{(1.19)^3 - 1}{(1.19)^3 (0.19)} \right)$$

$$30000 \frac{(1.38)}{(0.483)}$$

$$15 - 19 \\ 764.11 - \frac{8609.27}{21} = 8609.27$$

$$IRR = 15 + \frac{764.11}{(764.11 + 8609.27)} \{ 0.04 \}$$

$$= 15 + \left(\frac{764.11}{9373.38} \right) (4)$$

$$= 15.32$$

$$P_B = \frac{100000}{30000} = 3.33$$

(3)

$$C_0 = 1075$$

$$i = 15\%$$

$$P = F \left[\frac{1}{(1+i)^n} \right]$$

$$\begin{aligned} NPV &= \frac{150}{(1.15)^1} + \frac{300}{(1.15)^2} + \frac{450}{(1.15)^3} + \frac{600}{(1.15)^4} \\ &\quad + \frac{750}{(1.15)^5} - 1075 \end{aligned}$$

$$\begin{aligned} NPV &= 130.43 + 226.84 + 895.88 + 343.05 \\ &\quad + 872.88 \end{aligned}$$

$$NPV = 1369.08 - 1075$$

$$NPV = 94.08$$

$$i = 16\%$$

$$\begin{aligned} NPV &= 109.31 + 222.94 + 288.29 \\ &\quad + \cancel{860.12} 331.37 + 3575.07 \end{aligned}$$

Benefit - Cost ratio Criteria

In case of public alternatives like the provision of Health and educational facilities; infrastructure facilities etc. the concerned authority evaluates

$\frac{B}{C}$ ratio of the project which if at least ≥ 1 is accepted otherwise rejected

Ques

$$C_0 = 40 \text{ lakh} = P$$

$$n = 15$$

$$A = 1,50,000$$

$$\text{Fuel}_1 = 6 \text{ lakh}$$

$$\text{Fuel}_2 = 50,000$$

$$i = 12\%$$

$$A = \frac{6,00,000}{(1.12)^{15} - 1} + 50,000 \left[\frac{(1.12)^{15} - 1 - (0.12)(15)}{(0.12)(1.12)^{15} - (0.12)} \right]$$

$$A = 6,00,000 + 50,000 \left[\frac{4.47 - 1.8}{0.53} \right]$$

$$A = 8,51,886.79$$

$$A = \frac{4000000}{(1.12)^{15} - 1}$$

~~$$A = \frac{4000000}{(0.65)(4.47)}$$~~

$$F = \frac{851886.79}{(0.12)} (1 + 0.12)^{15} - 1$$

$$F = 31758096.45$$

$$F = 4000000 (1.12)^{15}$$

$$C \rightarrow F = 31894263.04$$

$$\frac{B}{C} = \frac{1.15}{1}$$

$$A = 31894263.04$$

Ques $P = 150000000$

A should be deducted from cost

$$A = 20 + 25 + 35 + 10$$

$$A = 90 \text{ lakh} \rightarrow B$$

$$P = 1500 \text{ lakh} - 1400 \text{ lakh}$$

$$A = 1500 \left(\frac{(0.09)(1.09)^{50}}{(1.09)^{50} - 1} \right)$$

$$= 1500 \left(\frac{0.09}{1.038} \right) = 40268836.80$$

Project A
 $\frac{B}{C} = \text{SCR } 1.23$

Project B - (ii)

A ~~scr~~ $A = 2S + 3S + 4S + 20$

$$A = 12S \text{ lakh}$$

$$A = 2800 \frac{(1.12)^{50}}{(1.12)^{50} - 1}$$

$$A = 2800 \frac{34.68}{288.002}$$

$$A = 301.03 = 0.415$$

Depreciation of an asset

Depreciation of an asset refers to the loss in productivity over its life which is interpreted in 3 sense.

- (i) Physical depreciation which refers to the actual decline in product of an asset measured in terms of goods and services produced.

~~Ques~~

(ii) Economic depreciation

It refers to the loss in value due to factors other than physical depreciation like the obsolescence of technology, change in choice of consumer etc.

(iii) Accounting Depreciation.

It refers to the total loss in productivity of the asset both due to physical as well as economic depreciation.

Poly

Production Analysis

Consumption - Destruction of utility.

production - Creation

The concept of production not only refers to the physical transformation of input into output but also includes their storage, transport, exchange and distribution till they reach the final consumer.

Ques Production is defined as the creation of utility.

Concepts of Production

① Production Function

- Short Run Production
- Long " "

The production f" is defined as the technical relationship between the output and the different inputs of production.

$$Q = f \text{ (Land (N), Labour (L), Capital (K), Organisation (O), raw materials)}$$

① Short run production function :-

If the producer is able to vary the output only by changing the variable factors of production while he is constrained by certain fixed factors, the production function is said to be in the short run which is observed by the law of variable proportion.

② Long run production function :-

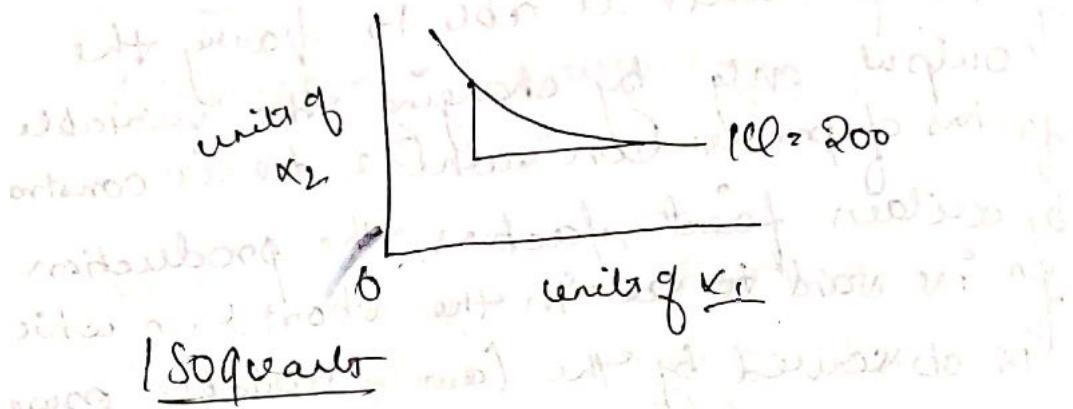
When the producer has no constraints of any fixed factor then the production process is said to have entered the long run which is observed under the law of return to scale.

The producer's equilibrium :- (PEC)

A producer is in equilibrium at the point where he maximises the production function given the cost constraint or minimises the cost given the output constraint.

$$P.F = q_0 = f(x_1, x_2)$$

Isoquant Curve



Production Schedule

Combination	X ₁	X ₂	Q const	MRTS _{X₁, X₂}
A	1	15	200	-
B	2	10	200	4:1
C	3	8	200	3:1
D	4	6	200	2:1
E	5	5	200	1:1

An isoquant curve of the producer represents the different combination of the inputs which will give the producer the same level of output.

$$\begin{aligned}
 \frac{dq_0}{dm_1} &= \frac{\partial q_0}{\partial m_1} dm_1 + \frac{\partial q_0}{\partial m_2} dm_2 \\
 &= f_1 dm_1 + f_2 dm_2 \\
 \frac{dm_1}{dx_1} &= \frac{f_1}{f_2} = \frac{\frac{dq_0}{dm_1}}{\frac{dq_0}{dm_2}}
 \end{aligned}$$

→ marginal production of x_1 ,
marg. production of x_2 = Marg. rate
 of Technical
 substitution.

$$MRTS_{x_1 x_2} = \frac{-d x_2}{d x_1} = \text{slope of isoquant}$$

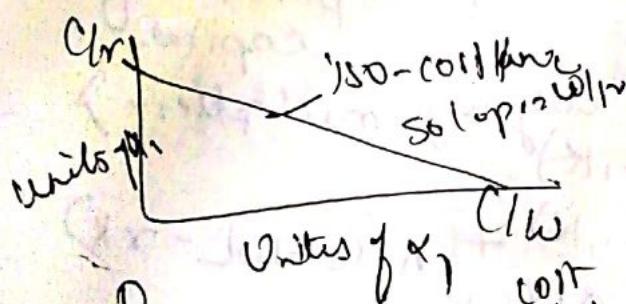
$$\Rightarrow \frac{MP_{x_1}}{MP_{x_2}}$$

The $MRTS_{x_1 x_2}$ refers to the rate at which the producer will be able to substitute one input with another without affecting the total output.

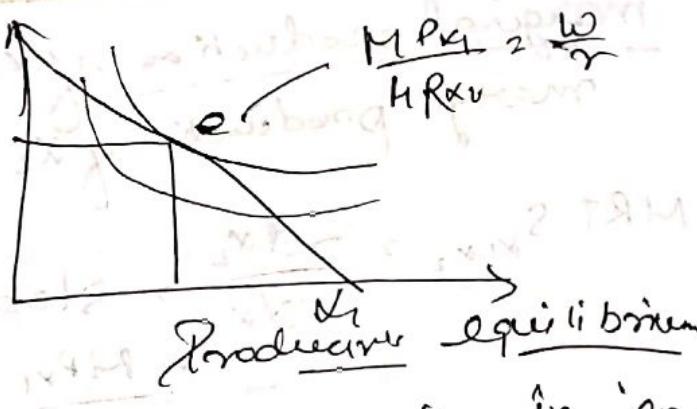
It is -ve implying that lesser and lesser quantity of 1 input can be given up to substitute some other factor under the technical assumption that no particular input can be a perfect substitute of some other factor thought the producer can only vary their combination.

$$\text{Iso Cost Line} \Rightarrow C = w_1 x_1 + r x_2$$

$C = \text{total cost of production}$
 $r = \text{--- of input } x_2$



The isoquant line of production graph shows the different combinations which the producer can afford with his total cost of production.



The producer will be in equilibrium at the point where the isocost line is tangent to the highest attainable isoquant curve ~~highest attainable~~ which satisfies the following condition.

$$\frac{MP_{X_1}}{MP_{X_2}} = \frac{w}{r}$$

Derivation of public equilibrium condition ①

Maximise $Q = P(L, K)$ subject to $wL + rK = C$

L = Labour units

K = Capital "

w = price per unit labour

r = price per unit of capital

Lagrange multiplier = λ

$$Z = P(L, K)$$

$$Z = P(L, K) + \lambda (C - wL - rK)$$

$$\frac{\partial Z}{\partial L} = 0 \Rightarrow \frac{\partial P(L, K)}{\partial L} - w\lambda = 0$$

$$\Rightarrow MP_L - w\lambda = 0 \quad ②$$

$$\frac{\partial Z}{\partial K} = 0 \Rightarrow \frac{\partial F(L, K)}{\partial K} - \gamma \lambda = 0$$

$$\Rightarrow MP_K - \gamma \lambda = 0 \quad (1)$$

$$\frac{\partial Z}{\partial \lambda} = 0 \Rightarrow C_0 - \omega L - \gamma K = 0 \quad (1)$$

$$MP_K - \gamma \lambda = MP_L - \omega \lambda$$

$$\cancel{M(P_K - P_L)} = \cancel{\lambda(\gamma - \omega)}$$

$$\cancel{\lambda} = \cancel{M(P_K - P_L)} \\ \cancel{\gamma - \omega}$$

$$\frac{MP_L}{MP_K} = \frac{\omega}{\gamma}$$

Write minimization condition.

minimize the cost constraints

$$\text{Minimize } C = \omega L + \gamma K \text{ sub to } Q_0 = f(L, K)$$

$$Z = \omega L + \gamma K + \alpha (Q_0 - f(L, K))$$

$$\frac{\partial Z}{\partial L} = 0 \Rightarrow \omega - \frac{\partial f(L, K)}{\partial L} = 0 \Rightarrow \omega - \gamma MP_L = 0 \quad (1)$$

$$\frac{\partial Z}{\partial K} = 0$$

$$\alpha - \gamma MP_K = 0 \quad (2)$$

$$\frac{\partial Z}{\partial \alpha} = Q_0 - f(L, K) = 0$$

$$\frac{MP_L}{MP_K} = \frac{\omega}{\gamma}$$

$$Q = \sqrt{LK}$$

$$K = 4$$

$$Z = \sqrt{LK} + n(80 - \sqrt{2L} - 4K)$$

$$C = 80$$

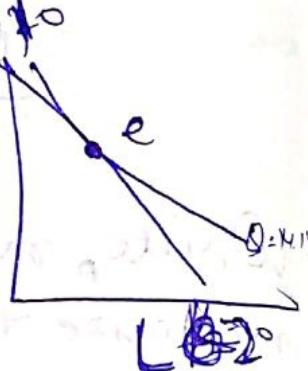
$$\frac{d^2}{dL^2} = \frac{\cancel{1}}{2\sqrt{L}} - 0$$

$$\frac{dZ}{dL} = 0 \rightarrow \textcircled{11}$$

$$\frac{dZ}{dK} = 0 \Rightarrow \frac{80 - \cancel{2L} - \cancel{4K}}{2\sqrt{L}} = 0 \rightarrow \textcircled{11}$$

$$L = 2K$$

$$K = 10$$



Ans.

$$80 - 2(2K) - 2L - 4K = 0$$

$$K = 10$$

$$L = 20$$

$$Q = \frac{1}{2}L^{1/2}K^{1/2}$$

$$= 14.14$$

$$\frac{MP_L}{MP_K} = \frac{\frac{\partial Q}{\partial L}}{\frac{\partial Q}{\partial K}} = \frac{K}{2L}$$

$$Q = \sqrt{LK}$$

$$\frac{\partial Q}{\partial L} = \frac{1}{2\sqrt{L}}K - 2n = 0$$

$$\frac{\partial Q}{\partial K} = \frac{1}{2\sqrt{K}}L - 2n = \frac{1}{2}L^{1/2}K^{-1/2}$$

$$\frac{MP_L}{MP_K} = \frac{L}{K} = \frac{1}{2}$$

$$L = 2K$$

α^2

$$80 - \alpha L - 4K = 0$$

$$80 - 2(2K) - 4K = 0$$

$$80 - 8K = 0$$

$$80 = 8K$$

$$80 = 8K$$

$$K = 10$$

$$\boxed{K = 10} \quad L = 20$$

Ans 2

Q & L & K

$$PF = Q^2 100L^0.5 K^0.5$$

$$W = 30, \gamma = 40$$

$$C = 120^\circ \quad K = \frac{3}{4} L$$

$$\frac{MPL}{MPK} = \frac{1}{2} L^{3/2} + \frac{1}{2} K^{3/2}$$

$$30L + 40K = 120^\circ$$

$$L = 20$$

$$K = 15$$

$$Q = 1732$$

Ans 4

$$PF = Q^2 100K^0.5 L^0.5$$

$$W = 50, \gamma = 40$$

$$100K^0.5 L^0.5 = 1118$$

$$50L + 40K = C$$

$$Z = 50L + 40K + n \underbrace{(1118 - 100K^0.5 L^0.5)}$$

$$\frac{4K = S}{L = 2S}$$

$$100 K^{0.5} L^{0.5} = 1118$$

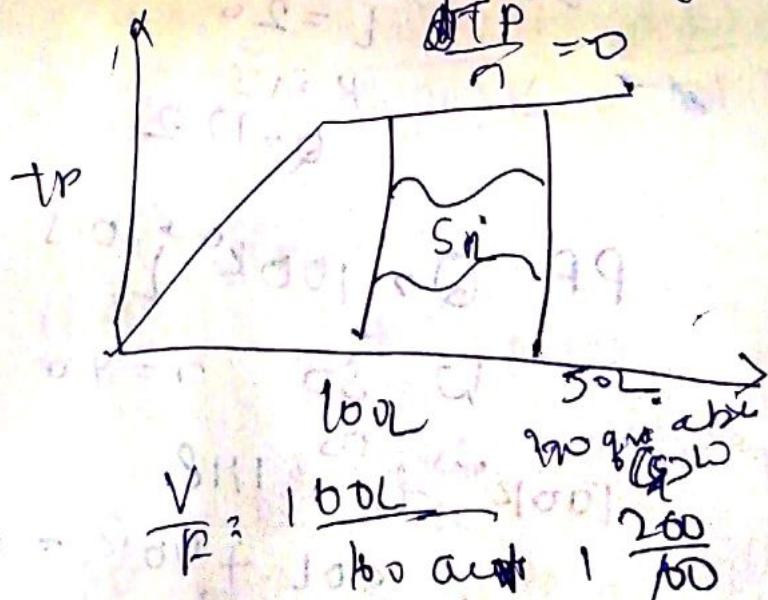
~~100 K^{0.5}~~ $L \leq 10$
 $K = 12.50$

$$C = 1000$$

LAWS OF VARIABLE PROPORTION

The short term production function
 Observes the productivity changes in the short run when the producer has some constraints of the fixed factors.

Different equipment \rightarrow Several



$$\frac{VTP}{TP} = \frac{1600}{1000} = 1.60$$

1600 units / 1000 units = 1.60

The case of variable proportion is the industrial proposal of the concept known as diseconomies of scale in the short run

there is a ~~fixed~~ for

two factors of production. It

beyond the range of production, wages ~~advertising costs~~ starts declining.

of the ~~factors~~

Q = $\bar{P} = (PA) \frac{L}{K}$ ~~variable costs~~

for fixed cost two factors of production
wages, advertising costs

(PA) ~~variable~~ ~~costs~~

Let us consider it at first with
given long-run cost of each factor
then revision of the initial
long-run cost of production
(costs)

Q = $\bar{P} = \frac{L}{K}$

and Q = $\bar{P} = \frac{L}{K}$

Productivity Concepts

- Total product (TP_L) = Q
- It will refers to the total output produced with different combination of the fixed and the variable factors.
- Average product (AP_L) = $\frac{TP}{\text{no. of variable unit}} \approx \frac{Q}{L}$
It refers to the output per unit of the variable factors.
- Marginal product (MP_L)
Which refers to the change in total product due to a marginal change in the no. of variable units.
$$= \frac{\text{Change in total product}}{\text{Change}}$$
$$MP \Rightarrow \frac{\Delta Q}{\Delta L}$$

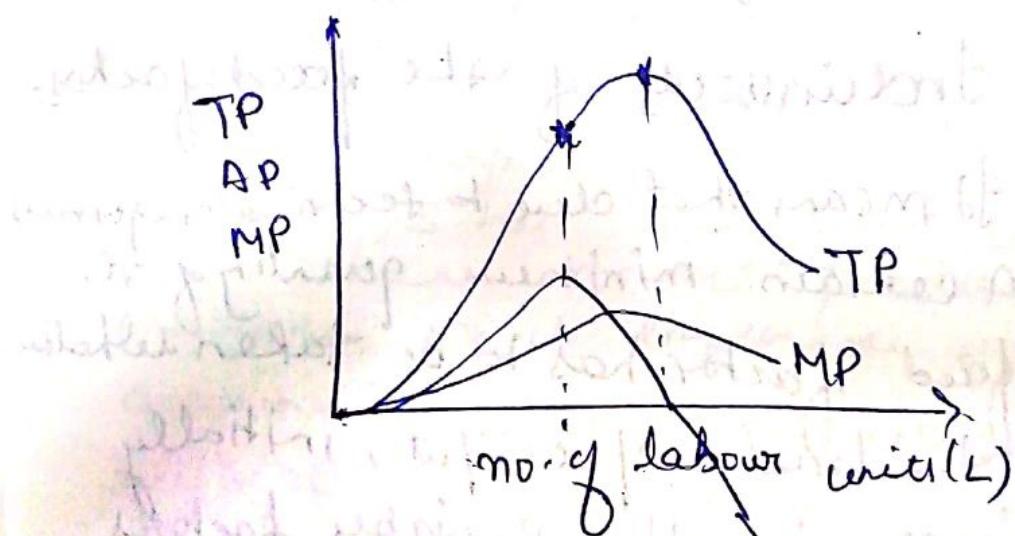
Assumptions of Law variable proportion

1. Constant state of technology
2. Short run phenomena
3. Possibility of variation in the proportion

of the fixed and the variable factor.

Productivity Schedule

Q	L	TP_L	AP_L	MP_L	
10	0	-	-	-	$\frac{10}{10} = 1$
10	1	5	5	5	
10	2	15	7.5	10	
10	3	30	11.67	20	
10	4	45	11.25	10	
10	5	50	10	5	
10	6	50	1000	0	
10	7	45	8.33	5	



- ① Stage of Increasing returns From 0 level until somewhere the AP_L is max.
- ② Stage of Diminishing Returns
- ③ Stage of Decreasing Returns In This Stage the total product initially increases at an increasing rate and beyond a point of inflection. Starts increasing at the lowest rate, highest in the middle and lowest at the end.

short run production function the way product takes place ~~when~~ is known as the point of inflection which represents the maximization of the marginal product for that MP / MP contribution.

This stage ends where the average product is maximum, when it also coincides with the marginal product of the variable factor.

① Invariability of the fixed factors.

It means that due to technical requirement a certain minimum quantity of the fixed factor has to be taken determine the level of output, initially increasing the variable factors takes the production unit towards its optimum combination with the variable factors, thereby increasing the efficiency of both other factors.

② Division of Labour or Specialisation

With increasing variable factors the production process have specialization of the production

process. This refers to subdividing the task and assigning to each group a particular task. Doing the same work rapidly. Doing the same work rapidly increases this efficiency and also needs less wastage of resources.

Stage of Decreasing Returns.

1. Scarcity of the fixed factors.

In this stage the total product continues to increase at an decreasing rate.

In this stage both the avg product and the marginal product are declined but are still +ve. This stage ends where the total product is maximum, which employs the marginal product of the variable factor will be zero. To the production process.

② Factors are imperfect substitutes of each other.

With each increase in variable factors every additional unit will have lesser and lesser of the fixed factor to work with, thereby decreasing the efficiency of both the factors.

Factors are im
If some other factors could run
replaced ~~the~~ the slaves foodfat
and optimum ~~and~~ ~~points~~
could be maint.

but as the factors are interrelated
of each other ~~decreased~~
decreasing product is also.

State of Negative Returns

In this state the total products

Starts adding while means the

Marginal productivity.

are zero. $T(x) = \underline{x}$

This stage occurs when the

Variables-factors are increased
much beyond the capacity
of the fixed ~~costs~~
and that their over

utilization leads to the frequent breakdown affecting the productivity of the overall production.



and believed that the rational

Rational producer will always operate in the second stage of production where

every additional variable unit is still adding to the total

output ~~there~~ $q - p^t$

The producer will stop hiring any

more labour

after ~~satisfy~~ where the marginal product turns 0.

poly

Causes of Increasing Returns to Scale

31



The IRS occurs due to certain advantages of a large scale production units (LSU) which are known as

"Economies of scale divided into

- ① Internal
- ② External economies.

Internal economies of scale

① Technical economies

- a) with increased productivity of a large scale unit, the per-unit cost gets highly reduced

$$AC = \frac{TC}{Q} \text{ (Total cost)}$$

- b) there is better linking and coordination among the different sectors of a large scale unit.

③ Managerial economies

A large scale unit can afford to hire the services of experts to manage and coordinate its diff sectors.

3 Labour economies

a) With increasing variable factors, there occurs specialization in the production process, which increases their efficiency and also cuts to less wastage of resources.

4 Marketing economies

A large scale unit have better marketing facilities like storage, transport, advertisement, finance etc for wider publicity of its products.

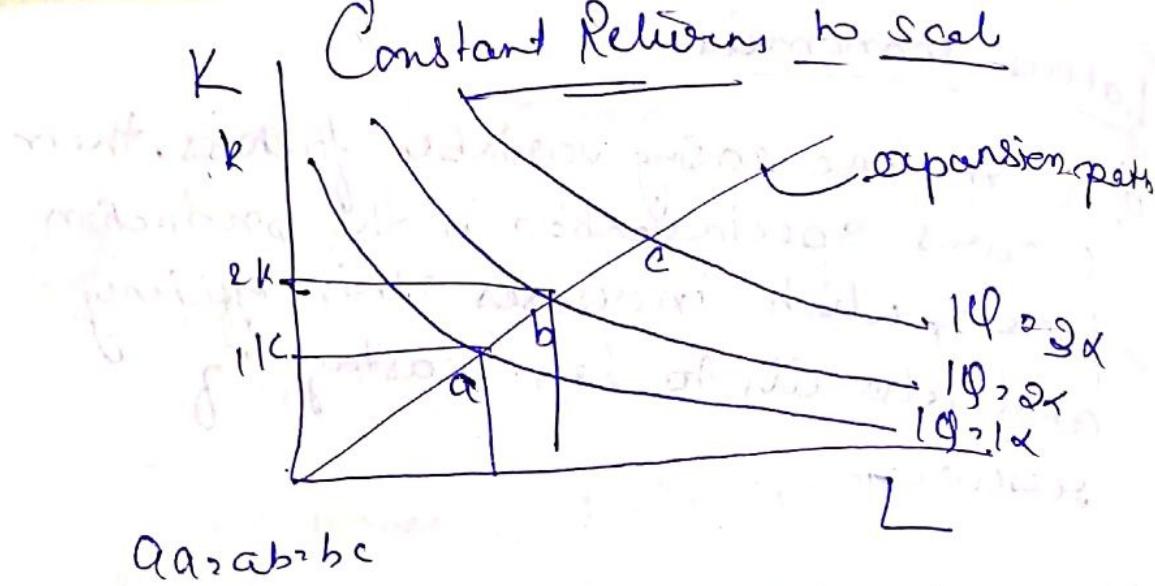
5 Financial economies

A large scale unit can raise huge capital from the market because of the superior goodwill it enjoys.

External economies

Some external advantages of a large scale units are:-

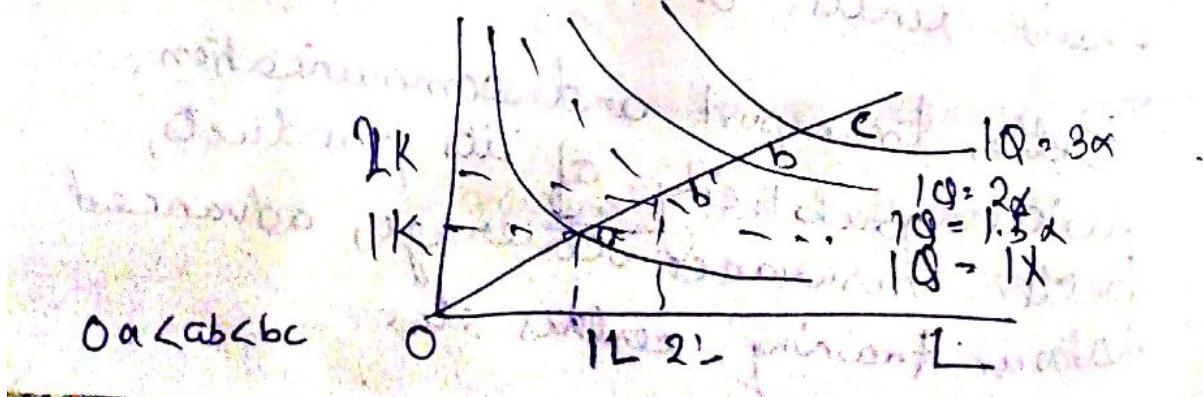
Better transport and communication, wider publicity of its products, better insurance coverage, advanced labour training centres etc.



In this stage, the proportional change in output is same as proportional change in input, which is implied by the equal distance between the successive isoquants.

This phase occurs where a firm has expanded beyond a certain optimum such that the economies of scale experienced by it in the initial phase gradually gets exhausted giving way to the diseconomies of large-scale production units.

1) Decreasing Returns to Scale



In this stage the proportional change in output is less than the proportional change given to all inputs which is implied by the increasing distance between the successive isoquants.

Causes of decreasing returns to scale

This arises due to certain diseconomies of a large scale units divided into the internal and external diseconomies.

① Internal diseconomies of scale

a) Indivisibility of the entrepreneur

Though all the factors can be expanded in the long run, but the entrepreneurs still remain an indivisible factor. Beyond the certain range of expansion, this may affect productivity if the other supervisors are not equally efficient.

b) Technical difficulties

Every factor has an optimum capacity to work as well as an optimum combination with the other inputs. If this proportion can get imbalance at any stage of production. Decreasing returns

may occur in the long run production fn.

External diseconomies

which are found to effect productivity in the long run.

- ① Scarcity of essential inputs
- ② Rise of cost of factors when many other industries also compete for the same in the long run.

Ques 1

①

①

A
g

C

C

C

P

②

g

th

③

④

⑤

⑥

⑦

⑧

⑨

⑩

⑪

Cost of Production

Types of cost

① Actual cost (Or outlay or accounting cost)

It refers to all the direct payments made by the producers to hire the different factors of production.

Examples are rent, wages, interest, profit etc.

② Sunk cost

It refers to that part of the total ^{actual} cost of the producer which is invested in lump sum and is gradually recovered in the production process.

Examples are:- fixed cost, depreciation charges etc.

③ Fixed cost and Variable cost

In this fixed cost refers to the cost of the fixed factors of production which remains independent of the level of output produced.

Ex - rent, interest, salary of permanent employees.

The variable cost refers to the cost of the variable factors of production which remains independent of the level of output produced. Ex - wages, profit.

4. Explicit and implicit cost

Explicit cost refers to the actual cost of the producer.

Implicit cost refers to the cost of all the factors which are own and invested by the producer in his own enterprise.

It is equivalent to the earning of the factors which is forgone by the producer.

(5)

Opportunity cost

It refers to the minimum amount which has to be paid to a factor to be able to higher and retain it in one's own enterprise.

(6)

Private cost and social cost

Private cost refers to the cost incurred by the producer in undertaking the production process. ex- wages, rent.

Social cost refers to all the indirect cost (+ve or -ve) of which the production process puts on the society for which the producer is not compensated or is not made liable to pay. ex- pollution (-ve)

Schools
Costs:

Cost function

of the producer

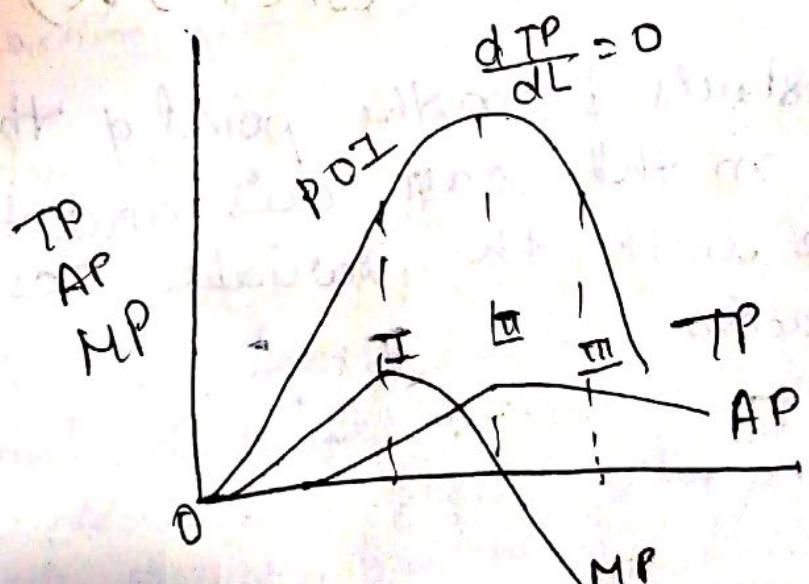
The cost function can be expressed as

$C = F(S, X, PF, T, \dots)$ where $S =$ size of the plant, $X =$ level of output, $T =$ Technology/Techiques of production. $PF =$ price of inputs.

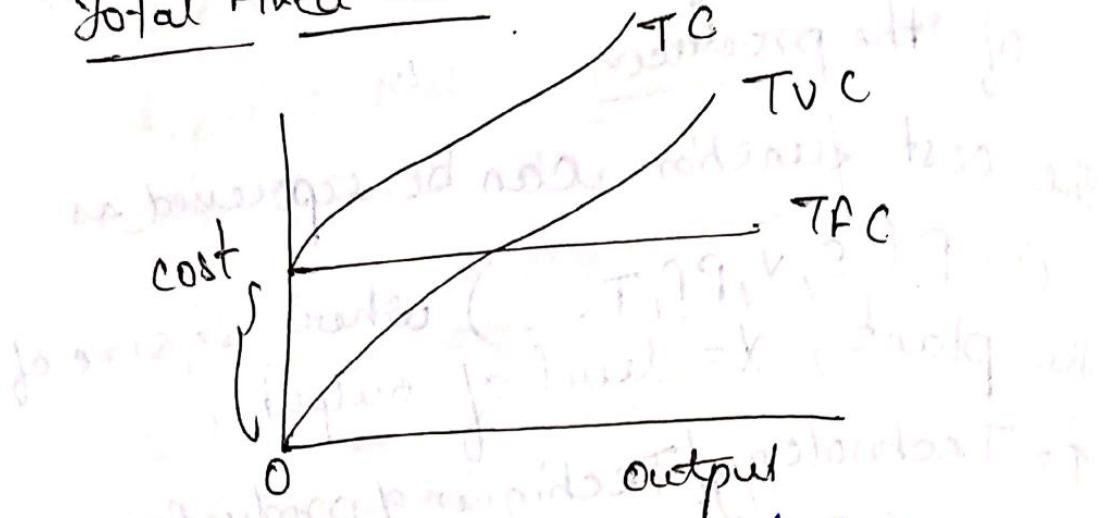
Concepts of Cost of a producer

Output	Total Fixed cost	Total Var. cost	Total cost	Avg Fixed cost	Avg Var. cost	Avg. Cost	Marginal cost
0	1000	0	1000	-	0	-	-
10	1000	400	1400	140	40	180	120
20	1000	700	1700	85	35	95.3	95.3
30	1000	930	1930	64.3	31	80	80
40	1000	1000	2100	52.5	27.5	76	76
50	1000	1400	2400	48	28	79.96	79.96
60	1000	1900	2900	48.3	31.66	85.71	85.71
70	1000	2500	3500	50	35.71	-	-

Cost Variation in the short run



Total Fixed cost



The total fixed cost will be a horizontal line to the output axis as it remains independent of the level of production.

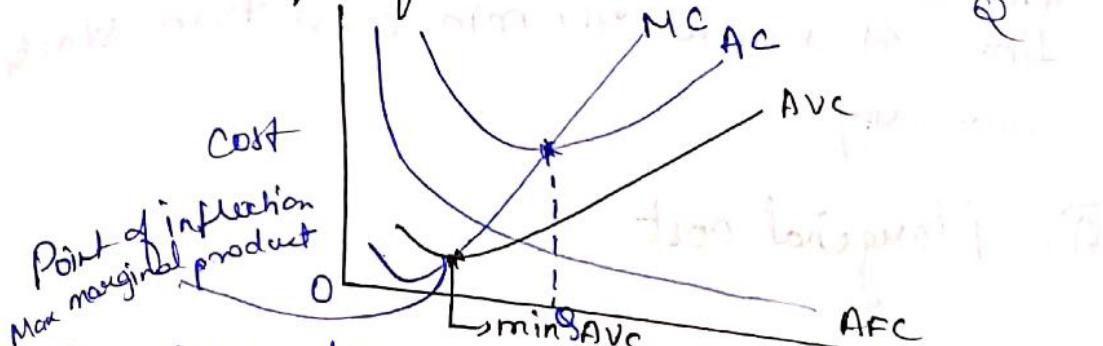
Total variable cost

The TVC varies inversely with the total product in the short run, if initially increases at a decreasing rate and beyond the point of inflection (POI) it starts increasing at an increasing rate.

The Total cost ($TFC + TVC$)

It starts from the point of the fixed cost on the cost axis and thereafter rise with the variable cost of production.

4. Average fixed cost (AFC) - $\frac{TFC}{Q}$



The AFC takes the shape of the ^{max AP = End of stage I} hyperbola as the constant of fixed cost gets distributed over larger and larger units of output.

5. Average variable cost

$$AVC = \frac{TVC}{Q} = \frac{WL}{Q} = \frac{wL}{QL} = \frac{w}{AP_L} = w\left(\frac{1}{AP_L}\right)$$

The AVC varies inversely with the avg product in the short run prod^n. It initially dec, reaches the min at the end of stage I in the short run production function.

$$6 \text{ Avg cost} = \frac{TC}{Q} = \frac{TFC + TVC}{Q}$$

$$AC = AFC + AVC$$

The avg cost takes a U shape. It initially decreases as both the AFC and AVC are declining. beyond stage I, the AVC starts increasing but the rapid decline in the AFC

makes the AC to decline for some time. It reaches the min and then starts increasing

④ Marginal cost

$$\begin{aligned} MC &= TC_n - TC_{n-1} \\ &= (TFC + TVC_n) - (TFC + TVC_{n-1}) \\ &= TVC_n - TVC_{n-1} \end{aligned}$$

$$MC = \frac{\Delta TVC}{\Delta Q}$$

$$= \frac{\omega \Delta L}{\Delta Q} = \frac{\omega}{Q/\Delta L}$$

The marginal cost varies inversely with the marginal product in the short run. It initially decreases, reaches the min at the point of inflection and thereafter starts increasing, passing through a min of both the AVC and AC.

I $MC = \min AVC \Rightarrow$ Why?

\therefore It represents end of st-1 in SRPF
when $AP = MP$

$$\text{As } AVC = \frac{1}{AP} \text{ and } MC = \frac{1}{NP}$$

$$MC = \min AVC$$

$MC = \min AC \Rightarrow$ why

$$TC = C$$

$$AC = \frac{C}{Q}$$

$$\frac{dAC}{dQ} = \frac{Q \frac{dC}{dQ} - \frac{C}{Q^2}}{Q}$$

$$= \frac{1}{Q} \left(\frac{dC}{dQ} - \frac{C}{Q} \right)$$

$$= \frac{1}{Q} (MC - AC)$$

Now Assuming $Q > 0$

i) when $MC < AC$, $\frac{dAC}{dQ} < 0$ (declining)

ii) when $MC = AC$, $\frac{dAC}{dQ} = 0$ (Min)

iii) when $MC > AC$, $\frac{dAC}{dQ} > 0$ (rising)

Ques

$$TC = 100 + 50Q - 12Q^2 + Q^3$$

$$AC = \frac{TC}{Q}$$

$$AC = \frac{100}{Q} + 50 - 12Q + Q^2$$

$$AC = \cancel{100} + \cancel{50} - 12Q + 100$$

$$\Rightarrow 10 + 50 - 12Q + 100$$

$$AC = 160$$

$$AVC = \frac{TVC}{Q} = \frac{50 - 12Q + Q^2}{Q} = 50 - 12 + Q = 30$$

$$TVC = 50 - 12Q + Q^2$$

$$\frac{\partial TVC}{\partial Q} = 50 - 12 + 2Q$$

$$= 50 - 12 + 2Q$$

$$= 50 - 24 + 2Q$$

$$= 40 + 2Q$$

(ii)

$$AC = \frac{200}{Q} - 64 + 8Q^2$$

$$TC = 200 - 64Q + 8Q^3$$

$$(i) TFC = 200$$

$$(ii) AVC = -64 + 8Q^2$$

~~$$\frac{\partial AVC}{\partial Q} = -12 + 16Q$$~~

~~$$16Q - 12 = 0$$~~

~~$$Q(16Q - 12) = 0$$~~

~~$$16Q = 12$$~~

$$Q = \frac{12}{16} = \frac{3}{4}$$

(vii)

(vi)

$$-64 + 8y^2$$

70
58

$$-6 + 16y$$

$$\cancel{-6} + 16y = 6$$

$$\boxed{y^2 - \frac{3}{8}}$$

(viii)

$$TVC = -6y + 8y^2$$

$$= -6 + 8y$$

$$-6 + 32 = \cancel{336}$$

240
80
160

$$TVC = -6y^2 + 8y^3$$

$$\frac{\partial TVC}{\partial y} = -12y + 24y^2$$

$$= (-12)(4) + (24)(4)$$

$$= -48 + 96$$

$$= (-12)(4) + (24)(16)$$

$$= -48 + 384$$

$$= 336$$

294
144
144
336

$$\textcircled{3} \quad TC = 400 + 30x - 12x^2 + x^3 \quad \textcircled{4}$$

$$TVC = 30x - 12x^2 + x^3$$

$$AVC = \frac{30 - 12x + x^2}{30 - 12x + x^2}$$

$$\frac{\partial AVC}{\partial x} = 30 - 24 + 6x$$

$$x = -1$$

$$\min MC$$

$$MC = 30 - 24x + 3x^2$$

$$\frac{\Delta MC}{\Delta x} = 30 - 24 + 6x$$

$$6x = 24$$

$$\boxed{x = 4}$$

\textcircled{11}

End of stage I

$$\min AVC \text{ or } AVC = MC$$

$$AVC = 30 - 24x + 3x^2$$

$$\frac{\Delta AVC}{\Delta x} = -24 + 6x$$

$$AVC = 30 - 12x + x^2$$

$$\frac{\Delta AVC}{\Delta x} = -12 + 2x \quad \boxed{x > 6}$$

$$\textcircled{1} \quad TC = Q73\sqrt{x^2} \quad \frac{1-2}{3} = \frac{1}{3}$$

$$TVC = Q73\sqrt{x^2}$$

$$MC = \frac{\partial TC}{\partial x}$$

$$Q73x^{\frac{2}{3}}$$

$$Q73 \frac{2}{3}x^{-\frac{1}{3}}$$

$$MC = \frac{18}{3} = 6$$

$$\textcircled{2} \quad MC = 0.6x^2 - 2x + 5 \quad x = 10$$

$$TFC = 1000$$

$$TC = TVC + TFC$$

$$TVC = \int 0.6x^2 - 2x + 5$$

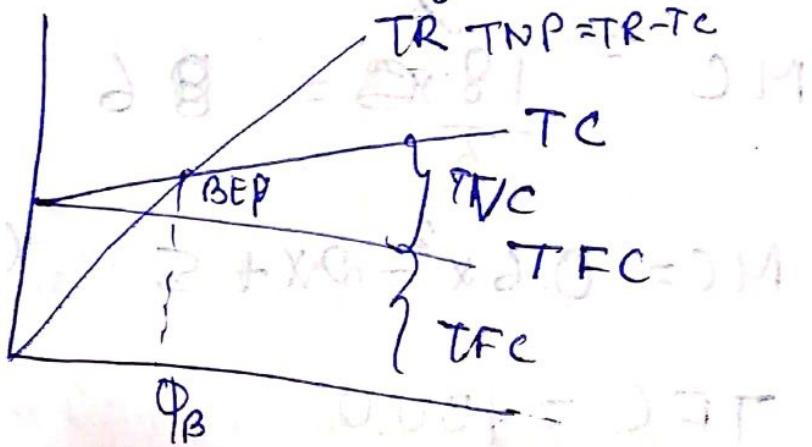
$$TVC = 0.6 \frac{x^3}{3} - \frac{2x^2}{2} + 5x + C$$

$$= 0.6 \frac{(10)^3}{3} - 2 \frac{(10)^2}{2} + 5(10) + 1000$$

$$= 2000$$

Break Even Analysis

The break even point of a producer represents the point where he equilises his total revenue with the total cost of investment. In other words it is the min level of output which has to produce by a producer to be able to sustain in the industry in the long run.



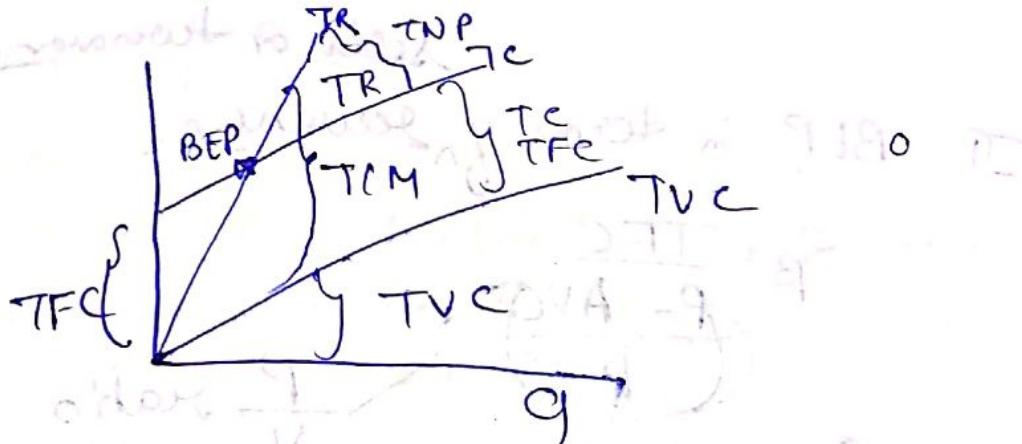
Total net profit = $TNP \Rightarrow \pi = TR - TC$

Total contribution Margin. (TCM)

In the short run where a major component of the producer's total

total cost is the form of sunk investment, it evaluates its profit

in the form of total contribution margin which refers to the revenue of the producer over the variable cost of production.



$$\begin{aligned}
 \text{TCM} &= \text{TR} - \text{TVC} \\
 &= \text{TR} - (\text{TC} - \text{TFC}) \\
 &\Rightarrow (\text{TR} - \text{TC}) + \text{TFC} \\
 &= \text{TNP} + \text{TFC}
 \end{aligned}$$

At BEP, $\text{TNP} = 0$

$$\text{TCM} = \text{TFC}$$

Derivation of Break even point

J. BEP in terms of output

$$\text{at BEP} \Rightarrow \text{TR} = \text{TC}$$

$$P \times Q_B = \text{TFC} + \text{TVC}$$

$$P Q_B = \text{TFC} + Q_B \cdot (\text{AVC})$$

$$Q_B = \frac{\text{TFC}}{P - \text{AVC}}$$

P price

$$\text{Note} - \text{TCM} = \frac{\text{TR} - \text{TVC}}{Q}$$

$$\text{ACM} = P - \text{AVC}$$

Avg contributory margin.

sells or turnover on

II BEP in terms of Revenue

$$S_p = \frac{TFC}{P - \frac{AVG}{V}}$$

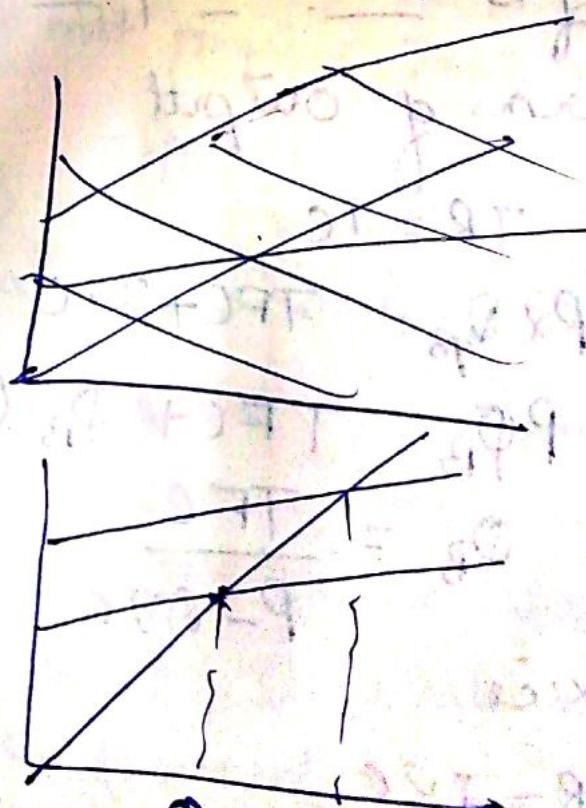
P ratio

$$S_p = \frac{TFC}{\frac{(TR - TVC)}{TR}}$$

$$S_p = \frac{TFC}{\text{TV ratio}}$$

BEP with target profit

π = target profit



Margin of Safety

The margin of safety of a producer measures the distance between the actual production and the break-even production of a producer.

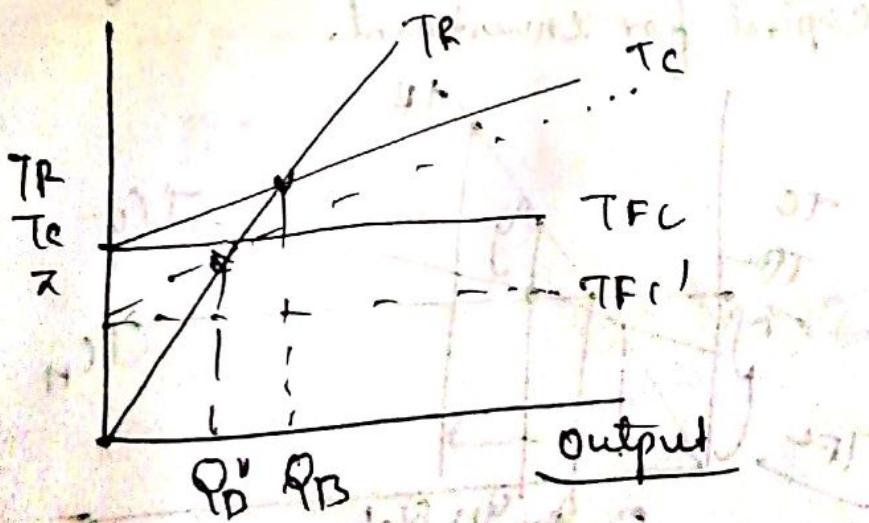
Higher the margin of safety more is the efficiency of the producer and vice versa.

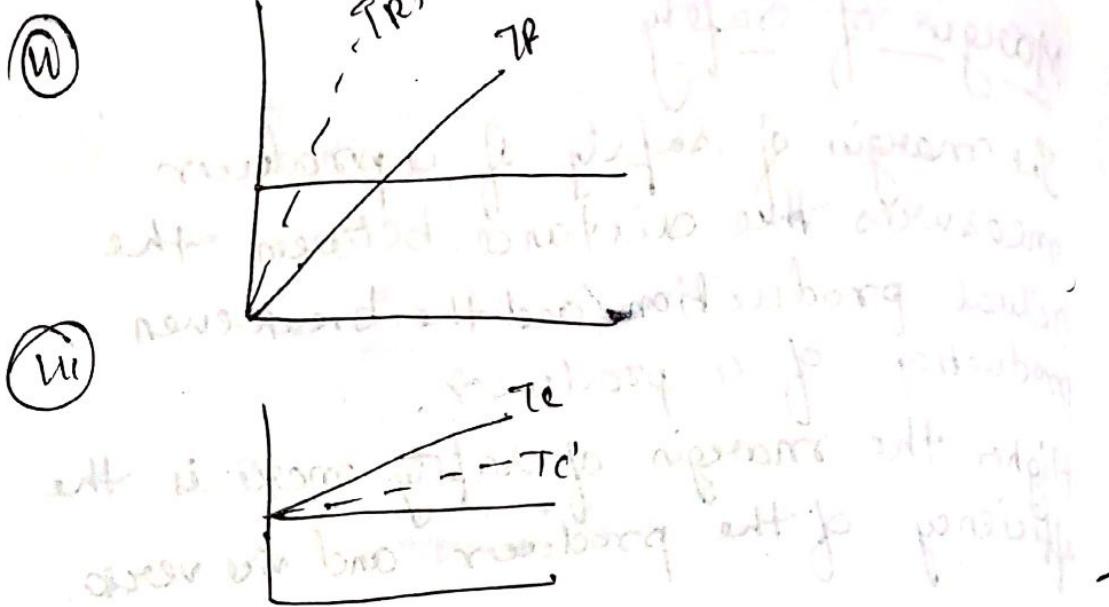
$$MOS \text{ (in output)} = \left[\frac{Q_s - Q_B}{Q_s} \right] * 100$$

$$MOS \text{ (in sales)} = \frac{\text{Total Sales} - \text{Break even sales } (s_B)}{\text{Total Sales}} * 100$$

Methods of reducing the break-even point

- ① A lower BEP is desirable because it signifies quicker recovery of the total cost of production.
- ② Reducing TFC
- ③ Increasing the price per unit
- ④ Reducing the AC.



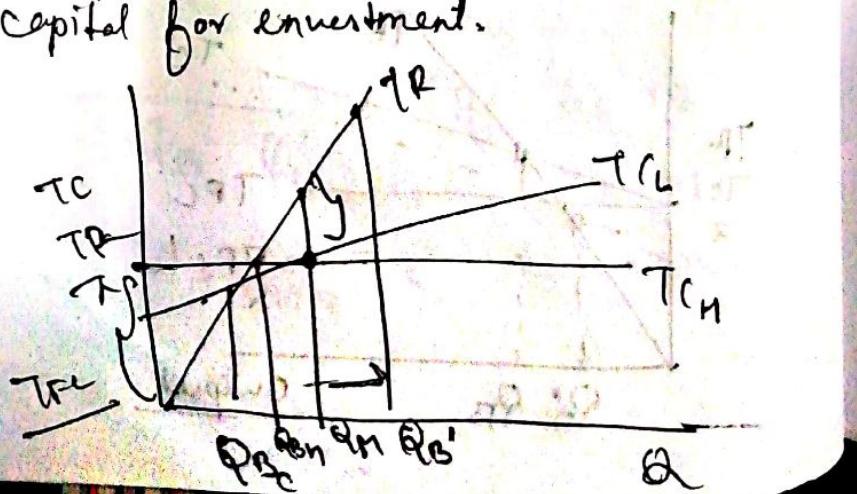


Operating Leverage

$$OL \Rightarrow \frac{TFC}{TVC}$$

(i) Operating leverage refers to the relation between the total fixed cost and the total variable cost of a production unit. Higher the ratio more highly leveraged a firm is and vice versa.

A firm can become a highly leveraged by increasing its fixed cost component through processes like automation of its production unit, borrowing the capital for investment.



A highly leveraged firm have more sensitivity of profit with any change in output than the long run because it experiences lower variation in their total cost of production relative to a low leverage producer.

Ques 2

$$\text{BEP} = \frac{\text{TFC}}{\text{P}-\text{AVC}} = \frac{5000}{25} = 200$$

$$\text{ATC} = 25 + \frac{\text{TFC}}{\text{Q}} = 25 + \frac{5000}{200} = 42.5$$

$$Q_B^B = \frac{\text{TFC} + \text{P}}{\text{P} - \text{AVC}} = \frac{5000 + 30}{30 - 25} = 100$$

Ques

$$Q_B = \frac{50000}{30 - 25} = 10000$$

$$50000 - \frac{250000}{30} = 50000$$

$$P = 35/-$$

$$Q_B^I = \frac{50000 + 25000}{35 - 25} = 7500$$

$$= 7500$$

Ques 2

$$TC = 3000 + 5x$$

$$TR = 30x$$

$$P = 30$$

$$TVC = 5x$$

$$AVC = \frac{TVC}{x}$$

i

$$Q_B = \frac{3000}{30 - 5} = \frac{3000}{25} = 12$$

$$\textcircled{1} \quad T_{CM} = TR - TC$$

$$TCM = TR - TVC$$

$$TCM = TNP + TFC \quad Q_B = 50$$

$$\cancel{TFC + TVC = TR}$$

$$\cancel{TFC} \quad 300 = TMP +$$

$$TR - TVC = \cancel{(TNP)} + TFC$$

$$30X - 5X = TMP + 300$$

$$TMP = 950$$

③

$$TFC = 4500$$

$$TVC = 7500$$

$$Q = 5000$$

$$S_B = 15000 = TR$$

①

$$TCM = TR - TVC$$

$$= 15000 - 7500$$

②

$$S_B = 4500$$

$$\cancel{7500}$$

$$\cancel{15000}$$

$$\cancel{4500}$$

$$\cancel{25}$$

$$\cancel{150}$$

$$\cancel{15000}$$

$$\cancel{4500 \times 150}$$

$$\cancel{75}$$

$$\cancel{4500 \times 150}$$

$$\cancel{75}$$

$$\textcircled{i} \quad R_B = \frac{\text{TFC}}{P - \text{AVC}}$$

$$= \frac{4500}{3 - 1.5} = 3000$$

$$\text{MOS} = \text{Total sale} - S_B$$

$$\text{in terms of sale} = 15000 - 9000$$

$$\text{of output} = 6000$$

~~Sal term~~ ~~MOS~~

$$\text{MOS} = \frac{Q_2 - Q_1}{Q_2} \times 100 = 40\%$$

~~in terms of sale~~

$$\text{of output} = \frac{Q_2 - Q_1}{Q_2} \times 5000$$

$$\textcircled{ii} \quad \text{Profit} = TR - TC$$

$$\textcircled{iv} \quad S_B' = \frac{\text{TFC} + \text{Profit}}{\frac{TR - TVC}{TR}}$$

$$S_B' = \frac{4500 + P}{\frac{10500}{0.5}} = 7800$$

$$S_B' = \frac{10500}{Q_2}$$

(4)

$$TFC = 60000$$

$$AVC = 10$$

$$P = 20$$

$$Q = 10000$$

$$MOS = \frac{Q_s - Q_D}{Q_s} \times 100$$

$$= \frac{10000 - 6000}{10000} \times 100 = 40\%$$

$$Q_D = \frac{TFC}{P - AVC}$$

$$= \frac{60000}{20 - 10} = 6000$$

$$MOS = \frac{4000}{6000} \times 100$$

$$= 66.67\%$$

$$MOS = Q_D \times P - Q_s \times P$$

$$\text{intervals} = 12000 - 60000$$

(5)

$$\frac{Q_s - Q_D}{Q_s} \times 100 = \frac{40000}{60000} \times 100 = 66.67\%$$

The second producer is more efficient because it has higher MOS.

Types of Market

And its equilibrium

A market is defined as any contact between the buyers and the sellers which facilitates the exchange of goods and services.

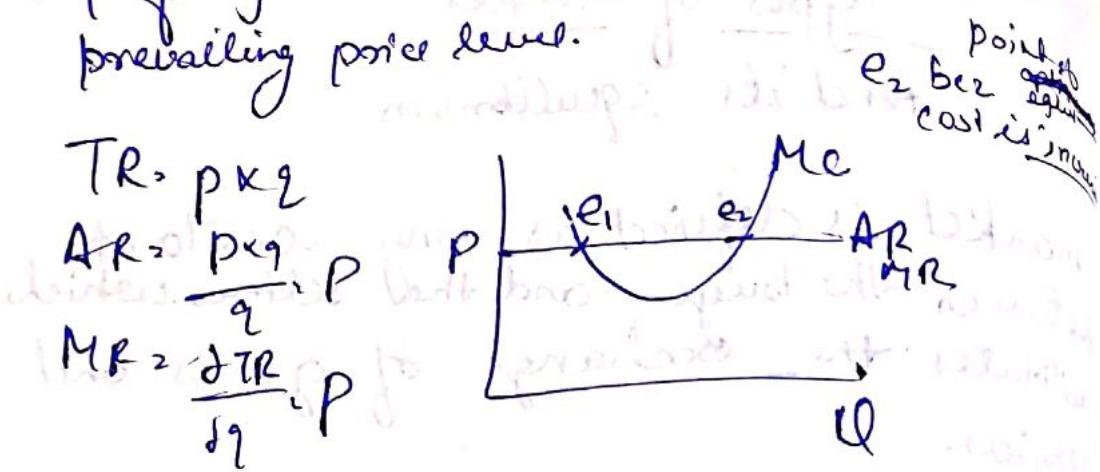
- ① No. of buyers & sellers
- ② Types of product sold

Perfect Competition

Features

- ① There are large no. of buyers and sellers in the market.
- ② All the products sold under PC are exactly identical or homogeneous in nature.
- ③ There is free entry and exit of firms in and out of industry.
- ④ There is no interdependence among the firms under perfect competition.
- ⑤ There is perfect knowledge among the buyers and sellers about the price condition prevailing the market.
- ⑥ In such type of market, one the price is determined by the equilibrium of the industries demand and supply, every producer working it will have to face a

perfectly elastic demand curve at the prevailing price level.



Equilibrium and profit maximizing condition:

$$(TNP) = \pi = TR - TC$$

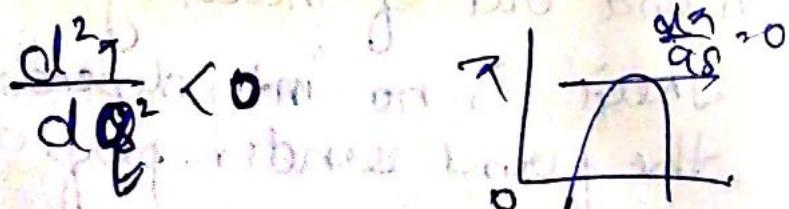
(profit)

$$\frac{d\pi}{dq} = 0$$

$$\frac{\partial TR}{\partial q} - \frac{\partial TC}{\partial q}$$

$MR - MC = 0$ Marginal cost

$$\underline{MR = MC}$$



A producer will maximize his profit at the point where

- ① He equalizes the marginal revenue with the marginal cost of production
- ② The marginal cost must be increasing

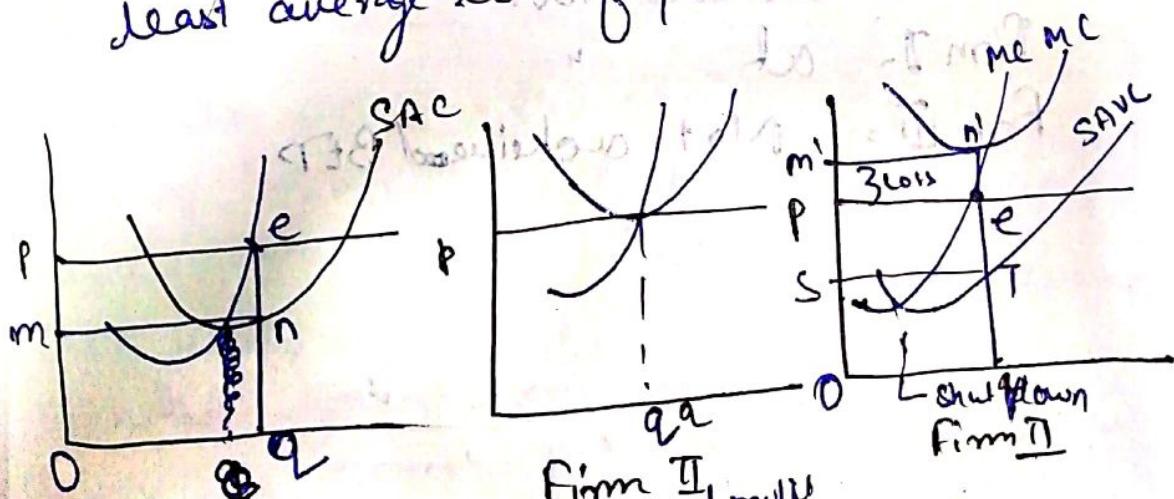
factor than the marginal revenue at the point of equilibrium.

Short Run Equilibrium Under Perfect Competition

As the same demand condition prevails for all the producers under perfect competition, it is their differential cost conditions which will determine their profit and losses.

The differential cost conditions may arise due to factors like the location of the production unit from the source of raw material and the market.

- ① The price at which they get their input, the efficiency of entrepreneur and other skilled factors etc. ~~AC should~~
- ② The most efficient firm will have the least average cost of production and vice versa.



$$\text{Firm I} \quad TR - TC = 0 \text{ p. eq.}$$

$$\therefore TR = TC$$

$$TC = OM \times OQ \\ = OM \cdot q$$

$$TR > TC$$

$$TR = OPeq \\ TC = OM' \cdot q$$

$$TC > TR \\ TFC + TVC > TR$$

$$\begin{aligned} &\rightarrow PM'ne \\ &TC = TFC + TVC \\ &= OM' \cdot q + OStG \end{aligned}$$

A loss making unit will remain in prod
so long as

$$\text{price} > \min \text{AVC}$$

by doing so it will cover its total
variable cost including a part of the
fixed cost of prodⁿ. The firm will
shut down and quit the industry at
the point where the price = min AVC.

By shutting down the variable cost will
be zero and losses will be only the fixed cost
of production.

$$P > \min \text{AVC}$$

or

$$\min \text{AVC}$$

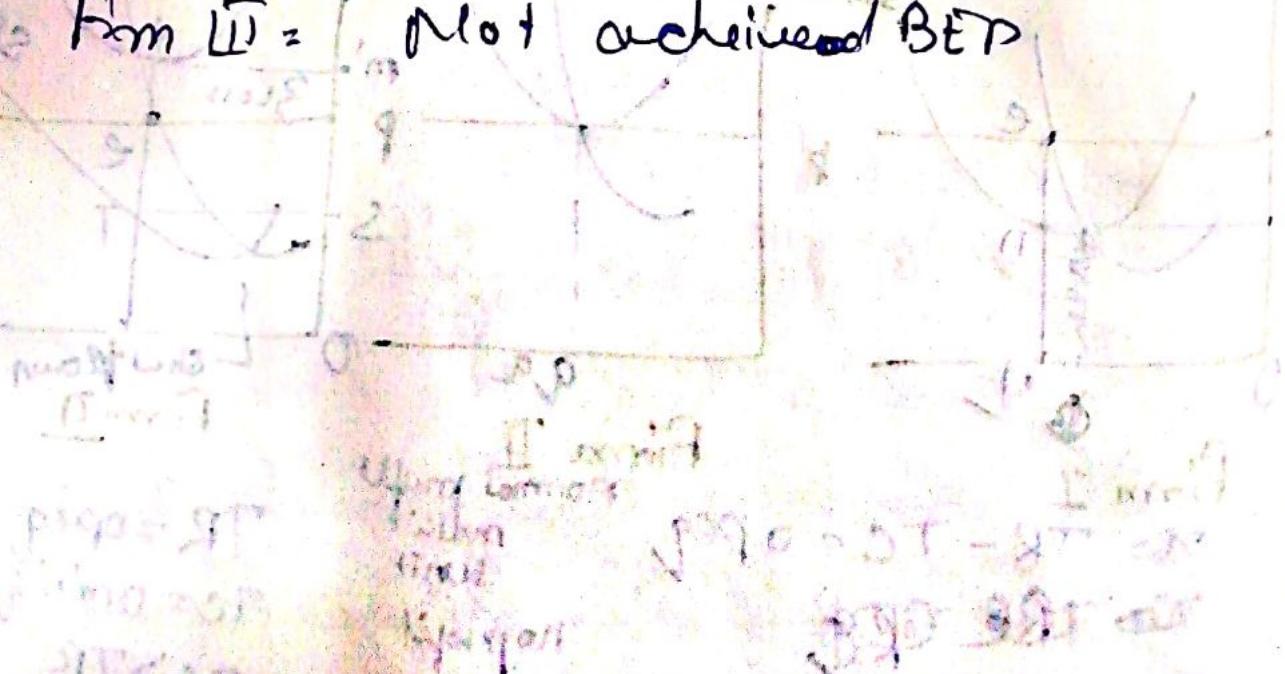
or

$$MC > \text{AVC}$$

Firm I - achieved BEP

Firm II - at "

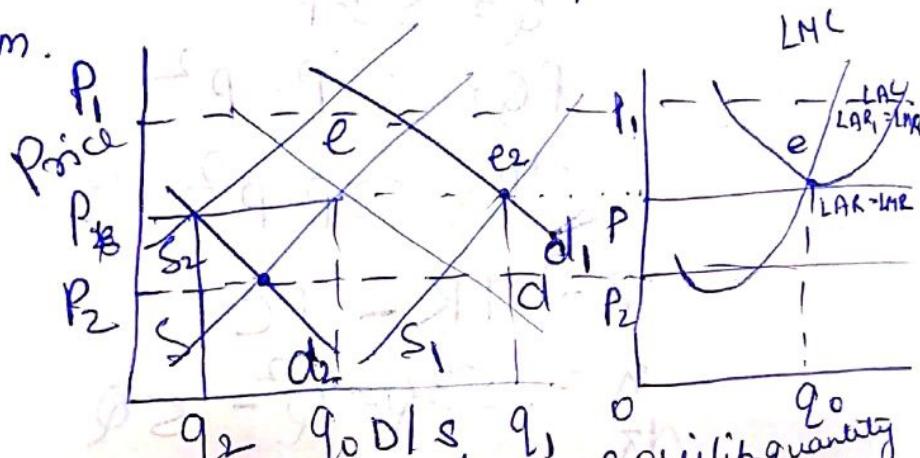
Firm III - Not achieved BEP



Long Run Equilibrium Under Perfect Comp

In the long run the industry will be in equilibrium where all the producers working under it just makes normal profit at the prevailing price level.

If there is any deviation from the equilibrium price, with free entry and exit, the market has the ability to generate forces which will reverse the price back to equilibrium.



If the price increases above equilibrium due to increase in demand, many producers will make more than normal profit. This will attract new producers into the market, which will increase the supply and reverse the price back to equilibrium.

$$D \uparrow \rightarrow P_1 \rightarrow \pi_1 \Rightarrow S_1 \uparrow = \downarrow P$$
$$D \downarrow \rightarrow P_2 \rightarrow \pi_2 \Rightarrow S_2 \uparrow = \downarrow P \text{ back to equil.}$$

and they leave the market

Ques $TC = 5Q$

$Q = 53 - P$

$\frac{d\pi}{dq}$

Find the output where maximum profit.

① $TFC = 5Q$

$\pi = TR - TC$

③

$Q = 53 - P$

$PQ = 53P - P^2$

$TR = 53P - P^2$

$\pi = TR - TC$

$\pi = 53Q - Q^2 - 5Q$

$\frac{d\pi}{dQ} = 53 - 2Q - 5$

~~$53 - 2Q - 5 = 0$~~

$Q = 24 \text{ units}$

④ approach $MC = MR$

④

Ques

$TR = 200q - 0.01q^2$

$\pi = 200q - 0.01q^2 - 50q - 20000$

$\pi = 150q - 0.01q^2 - 20000$

$$\frac{d\pi}{dq} = 150 - 0.02q$$

$$= 150 - (0.02)q = 0$$

$$0.02q = 150$$

$$2q = 15000$$

$$q = 7500$$

$$\pi = \$42500 \text{ (putting in } \pi \text{ fn)}$$

$$\textcircled{3} \quad C = \frac{1}{3}q^3 - 2.5q^2 + 6q$$

~~$$AVC = \frac{1}{3}q^2 - 2.5q + 6$$~~

~~$$\frac{dAVC}{dq} = \frac{2}{3}q - 2.5$$~~

$$\frac{2}{3}q = 2.5$$

$$q = \frac{2.5}{2} \times 3.75$$

~~$$AVC = \frac{1}{3}(3.75)^2 - 2.5(3.75) + 6$$~~

~~$$\min AVC = 1.3125$$~~

$$\textcircled{4} \quad TC = 6000 + 400Q - 20Q^2 + Q^3$$

$$TFC = 400Q - 20Q^2 + Q^3$$

$$AVC = 400 - 20Q + Q^2$$

$$= 400 - 200 + 100$$

$$\min AVC = \underline{\underline{300}} = P$$

(ii) $P > \min AVC$ so it can continue

Ques(5)

$$D: x = 200 - 10P$$

$$C = 10x + \frac{x^2}{25}$$

$$\frac{x^2}{25} - 10x$$

$$\frac{499}{25}$$

①

$$\text{Profit} \rightarrow TR - TC$$

$$= 200x - 10x^2 - 10x + \frac{x^2}{25}$$

$$= 190x - \frac{499}{25}x^2$$

$$\Rightarrow 190 - \frac{2(499)}{25}x$$

$$190 = \frac{2(499)}{25}x$$

$$\frac{190x^2}{499} = x$$

$$x = 0.76$$

$$\text{Profit} = (200)(0.76) - 10(0.76)^2 - \frac{10(0.76)}{25}$$

$$+ \frac{(0.76)^2}{25}$$

$$190(0.76) - \frac{499}{25}(0.76)^2$$

$$144.4 - 11.52$$

$$\Rightarrow 132.87$$

$$R = \frac{250}{F}$$